Dynamic Gas Temperature Measurement System
Denny L. Elmore, Woodrow W. Robinson and William B. Watkins
Pratt and Whitney Aircraft Engineering Division

SUMMARY

The objective of this effort was to develop a gas temperature measurement system with compensated frequency response of 1 KHz and capability to operate in the exhaust of a gas turbine combustor (Figure 1). Results of the initial portions of this effort were reported in the first Hot Section Technology Conference (Reference 1). Further progress in this development effort is summarized in this presentation. Environmental guidelines for this measurement are presented, followed by a preliminary design of the selected measurement method. Transient thermal conduction effects were identified as important; a preliminary finite-element conduction model quantified the errors expected by neglecting conduction. A compensation method was developed to account for effects of conduction and convection. This method was verified in analog electrical simulations, and used to compensate dynamic temperature data from a laboratory combustor and a gas turbine engine. Detailed data compensations are presented. Analysis of error sources in the method were done to derive confidence levels for the compensated data.

Environmental Guidelines and Sensor Selection

The sensor design and environmental guidelines for this effort are listed in Figure 2. Environmental parameters are representative of a modern gas turbine engine combustor exhaust, and sensor life, accuracy, spatial resolution and vibration capability are nominal goals for experimentation.

The sensor approach chosen for development is shown in Figure 3. The thermocouple employs two wires of different sizes to obtain data necessary for evaluation of the time constant for each wire. If two thermocouples are positioned in close proximity such that both are exposed to the same instantaneous temperature and velocity, the difference in their thermal responses will be governed by their relative diameters. These responses can then be used to obtain time constants for compensating the thermocouples. The unique feature of these wire thermocouples is a beadless laser butt-welded element, which allows the geometry to be modelled as a cylinder in crossflow.

A detailed review of the platinum/rhodium alloys tensile strengths, melting temperatures, emf outputs, thermal conductivities, stresses to rupture, and specific heats was made. Tensile and stress-rupture values are higher for increasing rhodium content, indicating the best thermocouple should have a high rhodium content. The Type B (platinum - 6% rhodium/platinum - 30% rhodium) was selected over the other commercially available thermocouple materials based on its higher emf output, availability, and known fabrication characteristics. Detailed structural analysis revealed that allowable yield stresses contrained design length-to-diameter ratios to less than 6.5 for the support wires and less than 15.5 for the thermocouple elements.

* Work performed under contract NAS3-23154
Probe Thermal Analysis and Compensation Method

A preliminary thermal model of the thermocouple probe wires was generated to evaluate the effects of radiation losses and end conduction losses. Governing equations and the model nodal breakup are shown in Figures 4 and 5 respectively. The physical thermocouple junction, the small wire, and the larger support wires were simulated by a finite difference model. The gas temperatures were assumed to be periodic fluctuations. The worst case gas temperature was assumed to be a mean gas temperature of 1400K (2520°R) with fluctuations of ±500K (±900°R). The more realistic case defined in the data acquisition analysis, ±65K (±117°R) was also evaluated. These cases were evaluated at frequencies of 20, 100, and 1000 Hz.

Results of the transient simulations (shown in Figure 6) indicate that radiation heat losses are not significant (less than 10K), but the conduction losses are too large (maximum of 67K) to be ignored and because of structural requirements previously discussed, cannot be reduced by making the wires longer. This discovery required that analysis of the measured temperature data be performed with a second order equation containing both conduction and convection terms, rather than the simplified first order equation containing only convection terms. The second order energy equation is a linear equation in time and space, whereas the first order equation is only time dependent.

A compensation method which accounts for both conduction and convection effects was developed. A second finite difference model using nine nodes (Figure 10) was used for the remainder of the calculations in this effort. The method is outlined in Figure 7 and explained below.

1. The theoretical transfer functions between the 76μm (3 mil) t/c signal \( \theta_1 \) and the gas stream signal \( a_g \) and the 254μm (10 mil) t/c signal \( \theta_2 \) and the gas stream are computed from the finite difference solution of the differential equations for various values of an aerodynamic parameter \( \Gamma \), at a number of discrete frequencies falling between the corner frequencies of the two t/c's. These data are then used to compute the theoretical transfer function \( H_\theta(f) \) between the 254μm (10 mil) t/c and the 76μm (3 mil) t/c \( (\theta_2/\theta_1) \) for the corresponding values of \( \Gamma \) and frequency. These curves \((\theta_2/\theta_1)\) will be used to determine the in situ value of \( \Gamma \) from the measured transfer function of \( \theta_2/\theta_1 \). The process is as follows:

   a. The following parameters are input or already stored in the computer. For the thermocouple wire - L, l, D, d, \( \rho_w \), \( Kw \), \( Cp_w \), and \( \alpha_w \). For the gas stream - \( \rho_g \), \( Kg \), \( Cp_g \), \( \gamma_g \), \( \mu_g \) and \( Pr_g \).

   b. The average or mean conditions for the test data for the following variables are entered into the computer:

      - \( T \) = mean gas temperature
      - \( P \) = mean gas pressure
      - \( F/A \) = fuel air ratio
      - \( f_1-f_\text{x} \) = frequencies of \( f_n \) at which transfer functions will be evaluated
      - \( Mn \) = Mach No.

   c. The program computes an estimated value of \( \Gamma \) based on the test conditions.
d. The program then computes $\xi_0$, the transfer function between the wire thermocouples and the gas stream, for the 76$\mu$m (0.003 in.) and the 254$\mu$m (0.010 in.) thermocouple from 0.5$\Gamma$ to 1.5$\Gamma$ in steps of 0.1$\Gamma$ at frequencies $f_1, \ldots, f_x$ which are user selected to fall in between estimated values of the crossover frequencies of the two t/c's. The equations are evaluated until steady state conditions are reached. The computer code determines the sampling interval for each frequency evaluated to ensure mathematical stability of the finite element model and minimize computation time. The normalized ratio of the magnitude of the temperature fluctuation in the wire to the temperature fluctuation of the gas stream ($\xi_0 = \theta_/a_\Gamma$) at frequency $f_i$ is determined by locating the maximum peak amplitude after the model has iterated to steady-state conditions. The phase shift ($\eta_\Gamma$) of the temperature fluctuation in the wire is determined by locating the time at which the $\xi_0$ crossed zero going positive at the beginning of the period in which the model reached steady-state conditions.

e. The data from (d) are then used to compute the theoretical transfer function $\theta_{2n}/\theta_{1n}$ from 0.5$\Gamma$ to 1.5$\Gamma$ at frequencies of $f_1$ through $f_x$.

2. Thermocouple test data are digitized into the Fourier system computer, typically 32 to 120 records each of the 76$\mu$m t/c dynamic signal and the 254$\mu$m t/c dynamic and dc signals. Each record contains 2048 samples of data. These data are then converted from millivolts to temperature utilizing NBS calibration curve coefficients for type B thermocouples. The 254$\mu$m dc channel is utilized as the mean for both dynamic data channels in converting the nonlinear t/c mv sigals to linearized temperature. These data records are then saved for recall for additional processing or plotting.

3. An ensemble averaged FFT (Fast Fourier Transform) transfer function analysis is then performed on $x$ number of records of the dynamic records to yield the measured value of $\theta_{2n}/\theta_{1n}$ as a function of frequency. The transfer function is computed as the FFT crosspower divided by the FFT autopower of the 76$\mu$m signal:

$$H_e(f) = \frac{\theta_{1n} \theta_{2n}^*}{\theta_{1n} \theta_{1n}^*} \Rightarrow \frac{\theta_{2n}}{\theta_{1n}}$$

where $^*$ = complex conjugate multiplication.

In conjunction with the computation of the measured transfer function, the coherence function is computed and utilized to assess the quality of the measurement. For the 2048 time sample data record lengths utilized 1024 line FFT's are produced. For the typical sampling rate of 4096 Hz, the FFT analyses yield spectral information dc to 2048 Hz in 2 Hz intervals. A standard Hewlett Packard windowing function (P301) is utilized prior to computation of the FFT's. This window is characterized by excellent spectral amplitude accuracy (+ 0.1%). Side lobe suppression is > - 70 db at + spectral lines and the effective noise bandwidth is 3.4 spectral lines.

4. Each measured value of $\theta_{2n}/\theta_{1n}$ at frequencies $f_n = f_1 - f_x$ are used in
conjunction with the theoretical curves of $\theta_{2\text{B}} / \theta_{1\text{B}}$ vs $I$ to determine a measured value of $I$ (the program interpolates between the 0.1 $I$ increments computed in (1) above). The arithmetic average obtained for each frequency is taken as the insitu measured value.

5. Using the measured insitu average value of $I$ obtained in (4), $\xi_9$, the normalized transfer function (gain $\theta_{1\text{B}} / a_n$, and phase $\eta_1$) of the 76 $\mu$m thermocouple with respect to the gas stream temperature is then computed at all frequencies from the 1st spectral line of the FFT spectrum to the Nyquist frequency of the FFT for each discrete frequency contained in the FFT. This is typically from 2 Hz to 2048 Hz in 2 Hz increments. This spectrum is then used to compensate the 76 $\mu$m t/c data as follows.

6. To compute the compensated ensemble averaged power spectral density function, the ensemble averaged auto power spectrum of the 76 $\mu$m (3 mil) t/c obtained in (3) above is divided by the auto power of its compensation spectrum:

$$\frac{\theta_{1\text{B}} \theta_{1\text{B}}^*}{\left[ \frac{\theta_{1\text{B}}}{a_n} \right] \left[ \frac{\theta_{1\text{B}}}{a_n}^* \right]} \rightarrow a_n^{2}$$

where $^* =$ complex conjugate multiplication.

Scaling factors for effective noise bandwidth and FFT Fourier symmetry are applied.

7. To compute the compensated instantaneous time waveform, an FFT spectrum is made on a specific data record. This spectrum is then divided by the compensation spectrum. The compensated spectrum is then inverse Fourier transformed to yield the compensated instantaneous time waveform. The software contains information on specific techniques employed to prevent time waveform distortions associated with the inverse Fourier transform. A threshold, in relative db, is applied to the frequency spectrum of the data signal prior to division by the compensation spectrum to prevent errors where the signal to noise ratio is too low.

$$\frac{\theta_{1\text{B}} m_{1\text{B}} + \phi_n}{\left( \frac{\theta_{1\text{B}}}{a_n} \right) m_{1\text{B}}} \rightarrow a_n \phi_n$$

Sensor Test Program

The test program summarized in the following section was based on three test series consisting of (1) System Shakedown and Compensation Verification Lab Tests, (2) Laboratory Burner Tests, and (3) Full Scale F100 Engine Tests (Figure 8). These tests allowed for a step by step checkout and optimization of the various components of the system while allowing for the experimental evaluation and substantiation of sensor guidelines and development effort goals.
Equations were derived for the electrical analog equivalent, passive RC network of the nine node finite difference thermocouple model for use in lab evaluations of the dual t/c approach. Two breadboard nine node RC element network models, one for the 76\(\mu\)m (3 mil) and one for the 254\(\mu\)m (10 mil) thermocouple were fabricated. The circuits were modeled for the F100 probe geometry operating at the following conditions:

\[T_T = 1200^\circ K \ (1700^\circ F)\]
\[P_T = 19.7 \text{ atm} \ (290 \text{ psia})\]
\[M_n = 0.233\]
\[F/A = 0.02.\]

Design values of resistance and capacitance for these simulators are shown in Figure 11. Potentiometers were used for the resistive components and values were set by measurement with a digital ohmmeter (+ 1%). Values of capacitive components were combinations of standard value capacitors (+ 10%) and were not measured. Schedule constraints precluded obtaining more precise capacitance values.

The purpose of this test was to determine the compensation spectrum (gain and phase as a function of frequency) of the 76\(\mu\)m (3 mil) analog circuit (and the 254\(\mu\)m analog circuit) from the measured transfer function taken between the outputs of the analog circuits of the 76\(\mu\)m (3 mil) t/c and the 254\(\mu\)m (10 mil) circuit (Figure 9) utilizing the HOST software and compare it with the known frequency response spectrum (measured single input - single output using conventional FFT techniques). Wideband (1250 Hz BW) random noise was input in these measurements. Because of the lack of precision in the analog circuit components, thermocouple length and diameter values input to the HOST program compensation software were varied until best agreement between the HOST program results and the known compensation spectra were obtained. The conventionally measured spectra were generated by measuring the transfer function between the input and output of the analog circuit using the 256 ensemble averaged FFT transfer function:

\[H(f) = \text{Gain} \angle \text{phase} (f) = \frac{G_{in}(f)G^*(f)}{G_{in}(f)G_{in}(f)}\]

where \(* = \text{complex conjugate multiplication}\)

The best match for the 76\(\mu\)m (3 mil) t/c was obtained when it was modeled with an element diameter of 74.9\(\mu\)m (2.95 mils) and an element length of 711.2\(\mu\)m (28.00 mils). The analog circuits were designed to model the t/c as 76.2\(\mu\)m (3.00 mils) diameter with a length of 609.6\(\mu\)m (24.00 mils). Gain match was within \(\pm 15\%\) and phase match within \(\pm 4.2\) to \(- 0.8\) deg. over the frequency range of 4Hz to 1000Hz.

Similarly, for the 254\(\mu\)m (0.010 in.) thermocouple case, the following parameters produced the best match of compensation spectra: the diameter was 260.4\(\mu\)m (10.25 mils) and the length was 1587.5\(\mu\)m (62.5 mils) as opposed to design values of diameter equal to 254\(\mu\)m (10 mils) and length equal to 1587.5\(\mu\)m (62.5 mils). Gain disagreement for this case was less than \(\pm 5\%\) out to 100Hz. The compensation program developed under this contract uses the 254\(\mu\)m (10 mil) data only out to about 40Hz. The agreement between the two methods is satisfactory despite lack of precision in the capacitance values in the analog model. Experiments performed
with the analog circuits verified that the finite difference models of the thermocouples work as required. Minor discrepancies, due to lack of precision in electrical component values, could easily be corrected, given adequate time and resources.

Subscale combustor probes were fabricated based on the detailed designs shown in Figure 14, which also shows the completed probe. The subscale combustor probe element junctions were inspected to determine the junction's actual dimensions and weld uniformity. Each thermocouple junction was inspected under a Nikon Metaphot microscope at 100X or 200X magnification, Figure 15. Photomicrographs of each junction and a graduated scale were made to measure the junction diameter and uniformity of the wire cross section. Two angular orientations of each wire were photographed 90 degrees apart. A number of different readings of each photograph were obtained to define the mean value and precision of each sample. Measurement uncertainty of the technique is $\pm 2 \mu m$ (9x10^{-5} in.) for the 76$\mu m$ elements and 9$\mu m$ (4x10^{-4}) for the 254$\mu m$ elements. Effects of these uncertainties on temperature uncertainty were later determined in sensitivity analyses using the completed data reduction method.

The probe was installed and tested in the subscale combustor rig (Figure 16). The probe and a platinum tube used for measuring gas stream total pressure were mounted downstream of the combustor exit plane. The mounting system was retractable so the probe was not in the gas stream except when data were recorded.

Dynamic temperature data and ambient temperature data were recorded on FM tape. The output of each Preston amplifier was double recorded on the FM tape recorder (0.5V rms and 1.0V rms full-scale record level channels). The signal levels were monitored on an oscilloscope and the fixed gain setting(s) of the Preston amplifier(s) were set as necessary to maintain optimum signal levels on the 0.5V rms record channel. Gain settings were correlated with test points to maintain calibration. Data were recorded at ten steady-state combustor test conditions ranging from the minimum conditions obtainable with the combustor facility. Average gas temperatures varied from 1048K (1887°R) to 1797K (3235°R). The gas stream Mach number and total pressure was relatively constant at 0.23 and 1.0 atm's, respectively.

Figure 17 are uncompensated and compensated dynamic temperature waveforms for the 3 mil thermocouple and test point 10. The uncompensated waveform has maximum fluctuations of approximately 400°F peak to peak with an rms value of 64°F. The compensated waveform has peak to peak fluctuations of approximately 1200°F and an rms value of 281°F. Figure 18 are uncompensated and compensated power spectral density plots for 120 record averages. Signal to noise ratios for compensated signal to compensated ambient noise are >18db up to 500Hz, >13db up to 1000Hz and >10db out to 2000Hz. A noticeable break in the compensated PSD can be seen at 1200Hz; this results from use of an anti-aliasing low-pass filter, and for this reason, signal to noise ratio from 1200 to 2000Hz is actually greater than 10db. Note that a combustor resonance is indicated by the peak at 145Hz.

The full scale test were conducted as planned in an F100 jet engine which was undergoing testing at P&W's Government Products Division (GPD) test facility. Test conditions for the data which follows were: $P = 158$ psia, $T = 1790°F$, $M = 0.355$. Figure 19 shows the uncompensated and compensated dynamic temperature waveforms. The uncompensated waveform has peak to peak characteristics of about 400°F and rms value of 73°F. The compensated waveform has peak to peak charac-
teristics of greater than 2000°F, and rms value of 393°F. Figure 20 are power
spectral density plots of compensated and uncompensated 120 record average data.
Signal to noise ratio is >26db to 500Hz, >20db to 1000Hz and >14db to 2000Hz. The
signal is basically wide band random, with no evidence of resonance.

Measurement Uncertainty

The overall compensation uncertainty was obtained by room-sum-squaring errors
associated with finite-windowing effects in the Fast Fourier Transform, thermo-
couple element diameter measurement, temperature waveform ratios, and data acquisi-
tion/reproduce noise. These errors are shown in Figure 21 for two input waveforms.
The 27°F peak to peak/√Hz wideband random waveform and corresponding errors are
representative of the signals observed experimentally.

LIST OF SYMBOLS

\[ \alpha = \frac{K_w}{\rho_w C_{pw}} = \text{thermal diffusivity of the wire} \]

- \( L \) = length of thermocouple support wire
- \( l \) = one half of length of smaller thermocouple wire
- \( D \) = diameter of thermocouple support wire
- \( d \) = diameter of smaller thermocouple wire
- \( \rho_w \) = density of thermocouple wire
- \( K_w \) = thermal conductivity of thermocouple wire
- \( C_{pw} \) = specific heat of ther thermocouple wire
- \( \rho_g \) = density of the gas stream
- \( C_{pg} \) = specific heat of the gas stream
- \( P_{rg} \) = Prandtl number of gas stream
- \( U_g \) = velocity of the gas stream
- \( \mu_g \) = viscosity of the gas stream
- \( \gamma_g \) = ratio of specific heats of gas stream
- \( \theta_{1n} \) = amplitude of the 75 \( \mu \)m (0.003 in.) thermocouple at frequency \( f_n \)
- \( \theta_{2n} \) = amplitude of the 254 \( \mu \)m (0.010 in.) thermocouple at frequency \( f_n \)
- \( a_n \) = amplitude of the gas temperature at frequency \( f_n \)
- \( \phi_n \) = phase shift of the gas temperature with respect to arbitrary time \( t_0 \)
at frequency \( f_n \)
\[ \eta_{1n} = \text{phase shift of 76 \mu m (0.003 in.) thermocouple with respect to gas temperature at frequency } f_n \]
\[ \eta_{2n} = \text{phase shift of 254 \mu m (0.010 in.) thermocouple with respect to gas temperature at frequency } f_n \]
\[ \lambda_{1n} = \text{phase shift of 76 \mu m (0.003 in.) thermocouple at frequency } f_n \text{ with respect to arbitrary time } t_0 \]
\[ \lambda_{2n} = \text{phase shift of 254 \mu m (0.010 in.) thermocouple at frequency } f_n \text{ with respect to arbitrary time } t_0 \]
\[ \Gamma = \frac{0.48k_p \sqrt{\rho g }}{\sqrt{\mu g \rho g}} = \text{Aerodynamic parameter} \]
\[ \xi = \text{Theoretical transfer function (gain and phase) of the wire thermocouple } x \text{ with respect to the gas temperature at frequency } f_n \]
\[ H_f(f) = \text{Theoretical transfer function between large and small thermocouples} \]
\[ H_e(f) = \text{Experimental transfer function between large and small thermocouple signals} \]
\[ K_g = \text{thermal conductivity of the gas stream} \]

REFERENCES

DYNAMIC GAS TEMPERATURE MEASUREMENT SYSTEM

Objective - Develop a temperature measurement system with:

- Compensated frequency response of 1 KHz
- Operation at jet engine combustor exit

Talk Outline -
- Environmental guidelines and sensor selection
  - Transient conduction effects and compensation method
  - Test program
    - Compensation checkout
    - Lab burner
    - Engine
  - Error analysis
- Summary

SENSOR DESIGN AND ENVIRONMENT GUIDELINES

Geometry: Annular combustor, 2 cm < H < 8 cm

Temperature: T ~ 1400°K (2060°F); T' ~ 500°K (900°F)

Frequency response: 1 kHz

Pressure: 10 < P < 20 ATM

Flow: v ~ 150 m/s; V' ~ 50 m/s

Gas composition: Fuel (nominal jet A) and air

Sensor life: 5 hr minimum

Accuracy: Temperature uncertainty ≤ 5% for f ≤ 200 Hz

Temperature uncertainty 10% for 200 Hz < f < 1 kHz

Spatial resolution: D ≤ 0.5 cm

Vibration: 10g
PRELIMINARY DESIGN CONCEPT: DUAL PASSIVE THERMOCOUPLE

- Ratio of T/C responses determines \( h_g \)

0.003 in. Type B
0.050 in.
0.010 in. Type B
0.040 in.
0.015 in.

Laser butt weld (no bead)

(150 in.)

(110 in.)

View C

Alumina probe body

0.047 in.
0.095 in.

0.0875 in.
0.175 in.

FIGURE 3

FIRST-ORDER AND SECOND-ORDER MODELS COMPARED

First-order model

Rate of energy change = \( Q_{\text{convection}} + Q_{\text{radiation}} \)

\[
\frac{dT}{dt} = \frac{4h}{\rho w c_{pw} D} (T_g - T) + \frac{4\sigma \epsilon}{\rho w c_{pw} D} (T_e^4 - T^4)
\]

Second-order model

Rate of energy = \( Q_{\text{convection}} + Q_{\text{conduction}} + Q_{\text{radiation}} \)

\[
\frac{dT}{dt} = -\frac{4h}{\rho w c_{pw} D} (T_g - T) + \alpha \frac{\delta^2 T}{\delta x^2} + \frac{4\sigma \epsilon}{\rho w c_{pw} D} (T_e^4 - T^4)
\]

FIGURE 4
PHYSICAL MODEL REPRESENTED BY FINITE DIFFERENCE ANALYTICAL MODEL

FIGURE 5

MAXIMUM DEVIATION IN PREDICTED JUNCTION TEMPERATURE FROM A 1ST ORDER SYSTEM

Conduction effects must be included to meet accuracy goals

FIGURE 6
COMPENSATION METHOD

- Compute theoretical response (76μm and 254μm T/C's) vs heat transfer coefficient (finite element conduction effects included) over frequency range
- Measure (data) response of 76μm and 254μm T/C's over frequency range (using FFT techniques)
- Determine actual heat transfer coefficient from computed and measured response
- Generate theoretical response of 76μm T/C for actual heat transfer coefficient for frequency range
- Compensate 76μm T/C data in frequency domain
- Inverse Fourier transform to time domain

FIGURE 7

DYNAMIC GAS TEMPERATURE MEASUREMENT SYSTEM

Test program

- Compensation method checkout
- Lab burner
- Engine

FIGURE 8
SIMULATION OF DUAL WIRE T/C'S

Random Noise Generator

Anti-aliasing Filter - 1250 Hz

9 node RC Model - 76 \( \mu \text{m} \) (3 mil) T/C

9 Node RC Model - 254 \( \mu \text{m} \) (10 mil) T/C

Fourier analyzer

- RC networks modeled as F100 probe
  - 1200°K (1700°F)
  - 19.7 ATMS (290 psia)
  - \( \text{Mn} = 0.2231 \)
  - \( \text{F/A} = 0.02 \)

FIGURE 9

FINITE DIFFERENCE THERMAL MODEL

Used in computer compensation program

FIGURE 10
RC ANALOG NETWORK SIMULATION

Full scale test conditions

![Network Diagram]

Thermocouple element diameter
Where: 76μm 254μm

Where:

R₀  7592 Ω  46.2 KΩ  Note: Values listed
R₁  1739 Ω  11.8 KΩ  correspond to F100
R₂  217.4 Ω  5.66 KΩ  probe operating at:
R₃  3796 Ω  23.11 KΩ  Tₚ = 1200°K (1700°F)
R₄  1049 Ω  12.447 KΩ  Pₚ = 19.7 atm (290 psia)
R₅  543.5 Ω  8.515 KΩ  Mₑ = 0.2331
R₆  1087 Ω  17.031 KΩ  F/A = 0.02
C₀  0.5 μfd  0.5 μfd
C₁  1.0 μfd  1.0 μfd
C₂  2.45 μfd  4.34 μfd
C₃  78 μfd  7.67 μfd

Note:

R₃  3796 Ω  23.11 KΩ  PT = 19.7 atm (290 psia)
R₄  1049 Ω  12.447 KΩ  Mₑ = 0.2331
R₅  543.5 Ω  8.515 KΩ  F/A = 0.02

FIGURE 11

SIMULATION OF DUAL WIRE TC'S

76 μm (3 mil) compensation spectrum - measured single input/single output

![Gain vs Frequency Graph]

Gain (db)

256 avg's

Gain

Phase

φ (deg)

γ²

-90°

Frequency (hz)

FIGURE 12
SIMULATION OF DUAL WIRE TC’S

76 μm (3 mil) compensation spectrum - measured dual wire

![Graph showing gain and phase as a function of frequency with 64 avg's.]

Gain (db) vs Frequency (Hz)

-80 to 0 dB
-20 to 0 dB
-40 to 0 dB
-60 to 0 dB
-80 to 0 dB
0 to 90°

Φ (deg)

FIGURE 13

SENSOR GEOMETRY

![Diagram showing sensor geometry with dimensions labeled.]

- 0.003 in. dia Type B wire
- 0.020 in. dia Type B wire
- 0.010 in. dia Type B wire
- 0.048 in.
- 0.015 in. dia Type B wire
- 0.075 in.
- 0.100 in.
- 0.125 in.
- 0.0188 in. dia ceramic stick with four 0.031 in. holes

AV260430

FIGURE 14
MICROSCOPIC INSPECTION OF JUNCTIONS

Photomicrograph of 0.003 in. element (200×)
Measured diameter = 0.0029

Photomicrograph of 0.010 in. element (100×)
Measured diameter = 0.0099

FIGURE 15

SUBSCALE COMBUSTOR RIG TEST DATA

- Test pt. No. 10

  Press = 1.04 atms (15.215 psia)
  Probe $M_n = 0.227$
  Mean temp = 1837°K (2775°F)
  F/A = 0.025 (est’d)

- Ambient - probe retracted/rig running

FIGURE 16
SUBSCALE COMBUSTOR RIG TEST DATA

76μm (3 mil) T/C Output

Compensated 76 μm (3 mil) T/C output

FIGURE 17

SUBSCALE COMBUSTOR RIG TEST DATA

76μm (3 mil) T/C output

Compensated 76μm (3 mil) T/C output

FIGURE 18
F100 TEST DATA

FIGURE 19

F100 TEST DATA

FIGURE 20
DYNAMIC GAS TEMPERATURE MEASUREMENT SYSTEM

Overall accuracy - instantaneous time waveform

<table>
<thead>
<tr>
<th>Error due to data system SNR</th>
<th>Compensation technique Error</th>
<th>Error (dia's)</th>
<th>Error ($\sigma_{y}/\sigma_{x}$)</th>
<th>Total error (RSS)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1000°K (1800°F) p-p at 200 Hz</td>
<td>&lt;0.1%</td>
<td>1.8%</td>
<td>4.9</td>
<td>3.3</td>
</tr>
<tr>
<td>1000°K (1800°F) p-p at 1000 Hz</td>
<td>&lt;0.1%</td>
<td>2.5%</td>
<td>5.2%</td>
<td>3.5%</td>
</tr>
<tr>
<td>$\geq 15°K (27°F) p-p/\sqrt{Hz}$ 4 Hz-200 Hz</td>
<td>0.7%</td>
<td>4.4%</td>
<td>4.9</td>
<td>3.3</td>
</tr>
<tr>
<td>$\geq 15°K (27°F) p-p/\sqrt{Hz}$ 200 Hz-1000 Hz</td>
<td>3.8%</td>
<td>10.6%</td>
<td>5.2</td>
<td>3.5</td>
</tr>
</tbody>
</table>

Overall accuracy - averaged frequency spectrum

<table>
<thead>
<tr>
<th>Error due to data system SNR</th>
<th>Compensation technique Error</th>
<th>Error (dia's)</th>
<th>Error ($\sigma_{y}/\sigma_{x}$)</th>
<th>Total error (RSS)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1000°K (1800°F) p-p at 200 Hz</td>
<td>&lt;0.1%</td>
<td>1.1%</td>
<td>4.9</td>
<td>3.3</td>
</tr>
<tr>
<td>1000°K (1800°F) p-p at 1000 Hz</td>
<td>&lt;0.1%</td>
<td>2.0%</td>
<td>5.2</td>
<td>3.5</td>
</tr>
<tr>
<td>$\geq 15°K (27°F) p-p/\sqrt{Hz}$ 4 Hz-200 Hz</td>
<td>0.7%</td>
<td>1.2%</td>
<td>4.9</td>
<td>3.3</td>
</tr>
<tr>
<td>$\geq 15°K (27°F) p-p/\sqrt{Hz}$ 200 Hz-1000 Hz</td>
<td>3.8%</td>
<td>1.9%</td>
<td>5.2</td>
<td>3.5</td>
</tr>
</tbody>
</table>

FIGURE 21