HIGH ACCURACY FUEL FLOWMETER

PHASE II — FINAL REPORT

PREPARED FOR
NATIONAL AERONAUTICS & SPACE ADMINISTRATION
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FOREWORD

We wish to recognize the technical contributions made by Dr. James Whetstone of the National Bureau of Standards, in Gaithersburg, Maryland as well as Douglas B. Mann and Dr. James D. Siegwarth of the National Bureau of Standards in Boulder, Colorado.
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1.0 **SUMMARY**

This report concludes the Phase II effort of NASA contract NAS3-22139 to develop a high accuracy fuel flowmeter. The following tasks were completed:

- Comprehensive study on Test and Calibration System
- Experimental and analytical investigation on Vortex Flowmeter
- Prototype evaluation on Dual Turbine Flowmeter with Densi-viscometer
- Prototype evaluation on Angular Momentum Flowmeter

All three flowmeter concepts (vortex, dual turbine and angular momentum) were subjected to experimental and analytical investigation under Tasks 1 through 4 to determine the potential prototype performance. The three concepts were subjected to a comprehensive rating. Eight parameters of performance were evaluated on a zero-to-ten scale, weighted and summed. The relative ratings of the vortex, dual turbine and angular momentum flowmeters are 0.71, 1.00 and 0.95 respectively. At the conclusion of Task 4, the dual turbine flowmeter concept was selected as the primary candidate and the angular momentum flowmeter as the secondary candidate for prototype development and evaluation.

The detailed design and evaluation on the Test and Calibration System and the three flowmeter concepts and their potential in meeting overall NASA requirements are described in respective sections.

In summary, the existing COX weigh-time calibration stand will not be adequate for the intended accuracy requirement. The most accurate method of calibration investigated was through the use of a Flow-Thru Calibrator for volumetric measurement combined with a densitometer for density measurement. It is estimated that this combination would have an overall accuracy of within 0.13 percent throughout the required range of operating conditions.

The vortex flowmeter does not have the required dynamic range and it also exhibits high non-repeatability at all flow rates. It is not likely to achieve the required time response and the pressure drop across the flowmeter is too excessive.

Test results indicate that the dual turbine concept with an accurate densitometer offers the best opportunity to meet NASA requirements. The dual turbine portion of the flowmeter is accurate enough for its intended application while the densitometer will require further investigation to reduce the noise level under vibration and high viscosities.

The angular momentum flowmeter exhibits highly non-linear calibration characteristics at flow rates above 5450 kg/hr (12,000 lb/hr). It is unlikely that this concept will meet NASA requirements for the whole dynamic range. Potential application is to use the existing design for up to 5450 kg/hr (12,000 lb/hr).

Investigation of the problem areas in the dual turbine/densi-viscometer and angular momentum concepts is to be continued in Phase IIIC of the development contract.
2.0 INTRODUCTION

Precision flight-type fuel flowmeters are needed to make accurate measurements of engine fuel consumption under flight conditions. At the present time much effort is being focused on improving engine and airframe components which have a direct effect on fuel consumption. Component improvements that result in fuel consumption improvements of only a few tenths of a percent, although costly to implement, have been shown to produce significant net savings over engine and/or airframe life cycles. However, the ability to accurately measure such small changes in fuel consumption during short duration flight tests is presently beyond the state of the art.

Precision fuel flowmeters also have application in computerized systems for minimizing fuel consumption during a given flight mission. In addition, future engine control systems can potentially be improved by the direct and precise measurement of fuel mass flow rate.

To a lesser degree there is a need to improve the accuracy of determination of fuel mass remaining in order to reach a desired gross weight at a particular point in a flight mission. Totalizing is also required for center-of-gravity adjustments in flight. Near real-time data processing is a requirement for the last two applications.

Technology related to aircraft fuel mass flowmeters was comprehensively reviewed in Phase I of NASA contract NAS3-22139 to determine what flowmeter types could provide 0.25%-of-point accuracy over a 50 to 1 range in flow rates. Three types of flowmeters were identified, namely, the vortex precession flowmeter with densitometer, dual turbine flowmeter with densitometer, and angular momentum flowmeter. This report covers the development efforts in experimental and analytical analyses, prototype design, fabrication and evaluation associated with each flowmeter concept.

In conjunction with the prototype flowmeter development, a comprehensive study was also performed on existing calibration systems to review if they are accurate enough for the purpose of this project.

The work statement of Phase II of NASA contract NAS3-22139 consisted of nine separate tasks, providing a methodical and controlled approach to the development of a Test and Calibration System and a high accuracy flowmeter. In brief, the tasks were the following:

Task 1. Calibration Study - Conduct a study to determine the method of mass flow rate calibration suitable for use on the High Accuracy Fuel Flowmeter with potentials of meeting NASA requirements.

Task 2. Experimental and Analytical Investigation Plan Formulations - Formulate a plan for the comprehensive investigation of the problem areas associated with the three methods selected for further study in Task 4.

Task 3. Review - Conduct a review of the Task 2 test plan at Lewis Research Center.
Task 4. **Experimental and Analytical Investigation** - Execute the Experimental and Analytical Investigation Plan developed in Task 2 and approved in Task 3.

Task 5. **Prototype Design and Test Plan Formulations** - Using results of Task 4, two prototype flowmeters shall be designed based on the method selected and approved in Task 4. Plans for testing the prototype flowmeters shall also be formulated and presented to NASA for approval.

Task 6. **Fabrication and Tests** - Fabricate two prototype flowmeters and test apparatus based on the designs and test plans of Task 5. Analyze the results of all tests performed in this task to determine the extent to which each flowmeter meets the contract goals.

Task 7. **Further Analysis of Prototype Design** - Determine which prototype designs have the best potential of meeting contract goals based on the test results and analysis of Task 6.

Task 8. **Briefing** - Conduct a one day oral briefing at NASA facilities with detailed discussions of Task 1 and Task 7.

Task 9. **Reporting Requirements** - Technical, financial, and schedular reporting, including this report were required.

Task 1 for the Test and Calibration Study is covered in Section 3.0 of this report. The rest of the tasks are divided into each flowmeter prototypes and the densi-viscometer. Sections 4.0 through 7.0 cover the vortex flowmeter, dual turbine flowmeter, angular momentum flowmeter, and densi-viscometer respectively for Tasks 2 through 7.

Each of the three flowmeter concepts were evaluated in Tasks 2 through 4, resulting in selecting the dual turbine flowmeter as the primary concept and the angular momentum flowmeter as the secondary concept for prototype development in Tasks 6 and 7.
3.0 TEST AND CALIBRATION SYSTEM STUDY

This section describes the conclusions and recommendations resulting from a study performed by the General Electric Company, Aircraft Instruments Department (GE/AID), Wilmington, MA under Task 1 of Phase II of NASA Contract No. NAS 3-22139 to develop a high accuracy fuel flowmeter (HAF). The primary purpose of the study was to determine a suitable method of calibrating high accuracy fuel flowmeters. The primary goal of the HAF program is to develop a mass flowmeter having an absolute accuracy within 0.25 percent of reading. Since this accuracy requirement is approximately the best that many excellent testing laboratories are willing to certify for calibrations, it was necessary to search for a calibration method having an accuracy of within 0.10 to 0.15 percent.

The purpose of this study under Task 1 was to determine the best method of calibration of a mass flow rate meter for a maximum flow rate of 3.15 liters/sec (20,000 lb/hr) and a 50:1 operating flow range using various jet fuels over a temperature range of -55 to 130°C (-67 to 266°F).

A survey was made of the (1) patent literature, (2) fluid flow measurement literature, (3) manufacturers of flow calibration equipment and (4) various government flow calibration laboratories as a basis for this study. It was concluded that the most advanced and accurate method of fluid flow calibration available is by the use of a "Flow-Thru Calibrator" as a primary standard for calibration. The type of Flow-Thru Calibrator which was selected from this study is a rigid piston Flow-Thru Calibrator which displaces fluid as the piston moves through a precision bored cylindrical pipe section. Since the Flow-Thru Calibrator is a precise volumetric calibration device, it must be used in conjunction with a precision density measuring device to determine average mass flow rate over an interval of time. A suitable Flow-Thru Calibrator has a calibrated displacement volume of approximately 18.93 liters (5 gallons). The inside diameter of the cylinder is precision honed. A high accuracy densitometer will directly sample the calibration fluid during flowmeter testing with the Flow-Thru Calibrator.

Several government calibration laboratories in the United States, Canada and Europe have acquired, or are in the process of acquiring, a Flow-Thru Calibrator of one particular manufacturer due to the many features incorporated in the design. This Flow-Thru Calibrator is traceable to the National Bureau of Standards by a water draw test which is performed by the manufacturer. The relatively simple water draw test can also be performed by the user. The manufacturer certifies the volume displacement of the water draw test within 0.03 percent. The proposed flow calibration system will be capable of an absolute calibration accuracy of within 0.1 percent at room temperature and an accuracy of within 0.13 percent from -55 to 200°C (-67 to 392°F).
3.1 Introduction

The primary method of calibrating aircraft fuel flowmeters at GE/AID since 1969 has been the use of dynamic weigh stands. The operating instructions for one of these stands states that the time for two sequential runs should be within ± 0.2 percent. Such a repeatability was probably quite satisfactory to many users 13 years ago, since these flowmeters were never guaranteed to an accuracy greater than within ± 0.5 percent. The dynamic weigh stands are also relatively easy to operate and the average mass flow rate for a given run is calculated simply by dividing the mass of the accumulated calibration fluid by the run time.

Shafer and Ruegg [1] reviewed the various techniques for liquid flowmeter calibration in 1958. They gave a rather extensive discussion of one inherent error associated with the dynamic weigh stand. They elaborated on a timing or inertia error related to the movement of the balanced weigh beam. Although this is a bias error that can be predicted to a reasonable accuracy, the correction apparently has not been widely adopted as a means of increasing the absolute accuracy. The timing error increases with an increase in the calibration flow rate. The timing error can be approximately 0.1 percent at a flow rate of 9091 kg/hr (20,000 lb/hr) for one particular dynamic weigh stand.

There is also a significant correction related to the buoyancy effect of the air in precision weighing. Most precision mass balance systems use or are calibrated with brass weights which have a density of 8400 kg/m³. The buoyancy effect can be illustrated by the following examples:

(1) If a one kilogram mass of aluminum (2700 kg/m³) is placed on a precision balance, the apparent mass indicated by the balance will be 0.999698 kg. This discrepancy occurs because the larger volume of the aluminum mass experiences a greater buoyant force due to the density of the surrounding air than a one kilogram brass weight.

(2) If a one kilogram mass of jet fuel (770 kg/m³) is weighed, the apparent mass would be 0.9985826 kg or an error of 0.142 percent if the apparent mass is not corrected for the air buoyancy effect.

A precision gravimetric system obviously requires a correction for buoyancy. The equation for the buoyancy correction factor is somewhat different for a gravimetric calibration system than for the case of weighing a material other than brass on a precision balance. A derivation of the correction factor for a gravimetric calibration system is presented in Appendix A.

Ruegg and Shafer [2] also published a paper in 1972 where they discussed the capabilities of the National Bureau of Standards in Gaithersburg, MD [NBS(G)]. This paper also refers to the timing errors due to the change in inertia of the weigh system during a run. They do not discuss buoyancy corrections. NBS(G) claims a calibration capability within 0.1 percent using dynamic weigh stands and a flow calibration range of 0.03 to 2 liters/sec (0.5 to 30 gpm) with liquid hydrocarbons.
Olsen [3] published NBS TN-831 in 1974. This paper also surveyed various methods of liquid flow rate calibration. Olsen gives an equation for the buoyancy correction in gravimetric flow calibration systems which neglects the contribution of vapor density as shown in Appendix A.

Dean et al [4] and Mann [5] describe the cryogenic liquid flow metering facilities at the National Bureau of Standards Boulder, CO [NBS(B)] which use a dynamic gravimetric system. Dean and his coworkers [6] present an excellent accuracy statement in tabular form for the cryogenic flow calibration stand at NBS(B). They arrived at an overall accuracy of within 0.12 percent for mass flow measurement with liquid nitrogen. This accuracy statement was modified and used as a model for the accuracy statement in this report for the proposed flow rate calibration system using a Flow-Thru Calibrator.

Scott [7] conducted a survey of the capabilities of the world-wide flow calibration facilities. A letter was sent inviting various groups and countries to submit a description of their flow calibration facilities with about a 50 percent response. Apparently no specific information was requested in the letter such as details to support the accuracy claims. The results tabulated by Scott indicated that most respondents only described (1) the calibration method used, (2) types of calibration fluids used, (3) types of flowmeters that were calibrated and (4) the flow rate range. Scott did not summarize temperature range capabilities if such information was provided by the respondents. Only a few respondents mentioned traceability.

Relatively few respondents to Scott [7] mentioned the accuracy of their flow calibration facilities. NBS(G) stated an accuracy of within 0.13 percent with water in a static gravimetric system. NBS(G) apparently did not mention that they use dynamic flow calibration methods as a standard for calibration.

National Engineering Laboratory (NEL), Glasgow, Scotland, UK claimed an accuracy for pipe provers and a static gravimetric system with oils (1 to 800 centistoke viscosity) of within 0.1 percent.

The British Petroleum Co., Ltd, UK claimed and accuracy of within 0.055 percent with a "dynamic gravimetric" test facility using water, kerosene or oils up to 36 liter/sec.

In a comment on accuracy statements, Hayward [8] suggests that where a pessimist might arrive at an accuracy claim of within 0.2 percent for a given facility an optimist might claim an accuracy of within 0.05 percent for the same facility.

McIrvin et al [9] present an accuracy statement for a ballistic flow calibrator. This method of calibration is discussed further in Section 3.5.2. They estimated a calibration accuracy of within 0.05 percent using this calibration method with water at ambient conditions.
A "rule-of-thumb" in metrology is to use a calibration standard which is 10 times as accurate as the accuracy requirement for the device being calibrated. Those experienced in flow rate measurements seem to agree that such a rule is generally difficult to apply to liquid flow rate calibration if an accuracy of within 0.5 percent or less is sought for the instrument being calibrated.

It seems unfortunate that more attention has not been given to improving the repeatability and absolute accuracy of the dynamic flow calibration stands. This type of stand has several advantages and, in particular, the ability to directly calibrate a mass flow rate meter.

3.2 Survey of Calibration Laboratories

Several calibration laboratories were contacted regarding their flow calibration capabilities. The laboratories contacted are listed as follows:

(1) U. S. Department of Commerce  
National Bureau of Standards FM-105  
Volume, Density and Fluid Meters Group  
Gaithersburg, MD 20877

(2) U. S. Department of Commerce  
National Bureau of Standards  
Thermophysical Properties Division  
Boulder, CO 80303

(3) Alden Research Laboratories  
Worcester Polytechnic Institute  
Holden, MA 01520

(4) Bionetics Corp.  
Kennedy Space Center, FL 32899

3.2.1 National Bureau of Standards, Gaithersburg – NBS(G) – The National Bureau of Standards, NBS(G) in Gaithersburg, MD only performs flow calibrations at room temperature using water or calibration fluid (MIL-C-7024C, Type II Special Run Stoddard Solvent). Within the range of flow rates of interest to this program, they would use a COX 311 Flowmeter Calibrator. The COX 311 is a dynamic weigh stand which requires three principal corrections:

(1) Buoyancy correction which is a function of the density of the air–vapor mixture and the density of the fluid in the weigh tank.

(2) Correction for time measurement errors due to the dynamic response of the weighing mechanism.

(3) Correction for the volume of the calibration fluid collected in the weigh tank during a calibration run.
The above corrections are discussed in more detail in the description of the COX Flowmeter Calibrator. NBS(G) only makes a correction for buoyancy. The correction factor they use for buoyancy is based on the density of the air surrounding the weigh tank—it will be shown later that the correction should be based on the density of the air-vapor mixture which is displaced by the calibration fluid accumulated in the weigh tank.

NBS(G) does not make a correction for dynamic response even though Shafer and Ruegg [1] of NBS(G) appear to have been the first to discuss these errors. NBS(G) periodically checks the weigh beam for sensitivity and to insure the beam scale ratio of 50:1 is within 0.03 percent.

Shafer et al [1] also suggest that the third error above is canceled in the differential weighing process. The writer believes that impulse of the fluid jet spilling into the weigh tank is an important factor in the dynamics of the weighing system and may have to be treated independently depending on the weigh tank configuration. The relationship between the mass of a falling fluid jet and impulse forces is derived in Appendix B.

3.2.2 National Bureau of Standards, Cryogenics Division NBS(B) Boulder, CO

The National Bureau of Standards at Boulder, CO perform liquid flow rate calibrations from 1.3 to 13.2 liters/sec with either liquid nitrogen (72-90 K/–201 to –183°C) or liquid argon (85-100 K/–188 to –173°C). Although these temperatures are considerably below our range of interest, their attention to making a precise and careful assessment of the accuracy of their flow calibrations has been very instructive. They have also recently tested various turbine flowmeters and densitometers at low temperature. Since they have tested components at such temperature extremes, their results are rather conservative when applied at –55°C (–67°F).

Dean et al [4] and Mann [5] describe the cryogenic flow measurement facilities at NBS(B) and Dean et al [6] give a provisional statement of the accuracy of their measurements. A schematic diagram of the flow calibration facility at NBS(B) is also presented by Brennan et al [10].

They achieved an estimated accuracy of within 0.18 percent for mass flow rate measurements and an estimated accuracy of within 0.47 percent for volumetric flow measurements with liquid nitrogen. These error estimates include a value of 0.06 percent for random error. The inaccuracy of the mass flow rate measurement was 0.12 percent (excluding the random error). This was largely due to the uncertainty in the buoyancy correction related to predicting the density of helium–nitrogen vapor mixtures.

The error experienced in the volumetric flow measurement is largely due to uncertainty in the density of liquid nitrogen. The density is used to convert the mass flow rate measurement to a volumetric flow rate measurement. The use of a densitometer for in situ measurement of density will probably permit improvement in volumetric flow rate measurements in the future.

More details of this system are described in Section 3.6.3.
3.2.3 **Alden Research Laboratories, Holden, MA** - The Alden Research Laboratories (ARL) are an adjunct of the Worcester Polytechnic Institute. They calibrate flowmeters with water at ambient temperature conditions.

These facilities are primarily designed for high fluid flow rates. The smallest flow calibration facility uses a 4536 kg (10,000 lb) weigh tank with a diverter valve to rapidly divert the flow from a sump tank to the weigh tank and vice versa. Large head tanks are used to maintain steady flow during calibration. The source of water is from nearby ponds. ARL will certify a volumetric displacement or turbine type flowmeter to an accuracy of +0.25 percent - they certify a venturi type flowmeter to +0.5 percent.

3.2.4 **Bionetics Corp, Kennedy Space Center, FL** - This company has a metrology laboratory which is dedicated, at this time, to the calibration of turbine flowmeters for the Space Shuttle. They customarily calibrate flowmeters at ambient temperature using MIL-H-5606 hydraulic fluid and simulate the properties of hypergolic fuels with water-ethylene glycol mixtures and polymers. The room temperature calibrations are used to simulate the viscosity of fuels to -34°C (-30°F).

A Brooks dynamic weigh stand calibrator similar to the COX 311 stand is currently used at Bionetics for flow calibration. This unit was manufactured in Hatfield, PA and installed around 1968-69.

Bionetics is currently in the process of acquiring a 0.0568 m³ (15 gallon) Brooks flow prover permitting a flow calibration range of 1.1 to 110 liters/sec (1.75 to 1750 gpm). The flow prover will be of all stainless steel construction for use with water-ethylene glycol mixtures. The primary interest in the use of the Brooks flow prover at Bionetics is the ability to provide on site traceability to NBS. This is easily accomplished by a "water draw" test using calibrated Seraphin volumetric cans certified by NBS.

3.3 **Survey of Patent Literature on Liquid Flowmeter Calibration**

The search of the patent literature conducted by the Washington Patent Operation of the General Electric Co. resulted in a total of 80 patent descriptions. The search covered the period from 20 February 1962 through 12 May 1981.

Only 57 patents of the 81 reviewed were related to calibration of liquid flowmeters. The other 24 patents were related to gas flow calibration or used the key word "calibration" in the title or abstract. The word "calibration" was often used to connote a means of adjustment for a flowmeter.

A brief abstract of the 57 patents is given in Appendix C. The abstracts are in the words of the writer and not taken from the patent abstracts. Each patent was reviewed with enough depth to determine the essential embodiments of the patent.
The 57 patents which were related to fluid flow calibration were also classified. Table 3-1 gives the classification of the patents and the number of patents related to each classification.

The following two patents found in the search were the only patents considered pertinent to high accuracy flow calibration:

(A) FLOWMETER CALIBRATOR
3,034,331 15 May 1962
Inventor: A. W. Brueckner
Assignee: George L. Nankervis, Detroit, MI

(B) APPARATUS AND METHOD FOR DETERMINING THE CHARACTERISTIC OF A FLOWMETER
4,152,122 8 May 1979
Inventor: E. E. Francisco, Jr.
Assignee: Flow Technology Inc., Phoenix, AR

Item A above gives an elementary description of the COX Flow Calibrator (Weigh Stand). Item B above gives a rather complete description of the Flow-Thru Calibrator which was developed by Flow Technology.

3.4 Summary of the Various Methods of Liquid Flowmeter Calibration

A search of the technical literature was made to determine if any precision methods of calibration of liquid flowmeters had been recently described. The search was in the interest of discovering any new or novel methods which would lead to an improved and more precise flow calibration method than currently used.

The search revealed several publications which discuss the various methods of calibrating flowmeters with liquids. An excellent survey paper was written by Hayward [11] formerly of the National Engineering Laboratory (NEL), Glasgow, U.K. This was the only paper that referred to a more advanced method of calibrating liquid flowmeters than customarily described in earlier papers.

The literature search revealed no liquid flow calibrating devices which were as advanced as the Flow-Thru Calibrator invented by Francisco (Pat. 4,152,922 on 8 May 1979).

3.4.1 Comparison of Various Methods of Calibrating Liquid Flowmeters - There are two principal methods for precision calibration of liquid flowmeters. They are:

(1) Volumetric methods

(2) Gravimetric methods

Since we are primarily interested in measuring the absolute accuracy of a mass flowmeter, the volumetric method has the slight disadvantage that it must be used with a precision densitometer to determine true mass flow rate.
Two types of flowmeters which are volumetric devices were investigated at GE/AID under the HAFF program. It is expected that it will be possible to determine the mass flow rate with a volumetric type flowmeter by multiplying volumetric flow rate times density to achieve a high measurement accuracy over a range of flow rates, temperatures and pressure conditions. To achieve this goal, it is first necessary to develop a liquid flowmeter which determines volumetric flow rate to a high accuracy.

A method for precisely determining volumetric flow rate is thus essential during the early development of a basic flowmeter. A measurement of the fluid viscosity is also needed for the compensation of the volumetric flowmeters – this is particularly true at low flow rates and with high viscosity which occurs at low temperature. This logic leads to the conclusion that a precise method of volumetric flow rate calibration (coupled with in situ liquid viscosity and precision liquid density measurements) is the most advantageous approach to mass flow rate calibration.

Tables 3-2 and 3-3 present a condensed description of each calibration method. Table 3-2 gives a brief description of various methods of **volumetric flow rate calibration**. Table 3-3 gives a brief description of various methods for **gravimetric flow rate calibration**. Both Tables 3-2 and 3-3 list the advantages and disadvantages of each method. These tables are not intended to be a comprehensive summary of all existing methods. Many methods were eliminated from the summary due to low potential accuracy. A more complete description of each method is presented in Sections 3.5 and 3.6.

An "alpha numeric" code was used in Tables 3-2 and 3-3 to clarify the identity of the method in the tables and elsewhere in this report. A prefix "V" was used to classify the volumetric methods and a prefix "G" was used to identify the gravimetric methods. A "dash number" after the letter was used to identify each type in the "V" or "G" series.

### 3.5 Methods of Liquid Flowmeter Calibration Using Volumetric Standards

Table 3-2 gives a summary of the various methods of using volumetric standards for liquid flowmeter calibration. The following sections present a more detailed description of these methods.

#### 3.5.1 Flow-Thru Calibrator (Type V-1)

The Flow-Thru Calibrator is a relatively recent development in liquid flow rate calibration technology. It could be considered a refinement of the pipe prover (Type V-3). The pipe prover has been a highly successful liquid flow rate calibration device in the petroleum industry. The pipe prover has certain limitations which have been overcome with the Flow-Thru Calibrator.

The most advanced Flow-Thru Calibrator design found was one currently being manufactured by Flow Technology. The Flow-Thru Calibrator is referred to as a Flow Prover when used as transportable flow meter calibration device. A Flow Prover is often trucked to a remote site in an oil field for flow meter calibration.
The Flow-Thru Calibrator with a few minor modifications appears to meet all of our requirements for a highly accurate means of volumetric flow rate calibration.

The Flow-Thru Calibrator could be coupled to a COX weigh stand for a low cost installation. The COX weigh stand would then provide the functions of pumping, flow control, temperature control and filtration of the calibration fluid and the Flow-Thru Calibrator would determine the precise volume of fluid which has passed through the flow meter during a calibration run.

3.5.1.1 History of the Flow-Thru Calibrator - The Flow-Thru Calibrator was originally developed at Flow Technology, Inc., Phoenix, AZ. The essential features of the Flow-Thru Calibrator are described in US Patent 4,152,922 issued on 8 May 1979. Edward E. Francisco, Jr. is the inventor and also the founder of Flow Technology to which the patent is assigned.

Mr. Francisco has had two previous patents relating to piston type calibration devices. "Ballistic" flow calibrators (Type V-2) are also being marketed by Flow Technology. The ballistic flow calibration devices are similar to the Flow-Thru Calibrator device but only permit a transient precision volumetric flow calibration.

3.5.1.2 Operating Principles of the Flow-Thru Calibrator - The Flow-Thru Calibrator is a precision piston displacement device with a provision for establishing steady state flow and temperature conditions prior to precise displacement of a quantity of fluid by an essentially rigid "calibrator" piston.

The ability to establish steady state operating conditions is accomplished by an ingenious poppet valve which is built into the calibrator piston as shown in Figures 3-1 through 3-4. The poppet valve remains open until thermal and fluid flow equilibrium conditions are established. A pneumatic actuator piston initiates the calibration sequence by first closing the poppet valve. The poppet valve is sealed against a conical seat within the calibrator piston and the pneumatic actuator piston serves as a boost to minimize the differential pressure across the calibrator piston which has been measured as 0.25 to 0.75 kPa (1 to 3 in. water) differential.

Figures 3-2 through 3-4 show the operating sequence of the Flow-Thru Calibrator. Three position sensors control the precision volumetric measurement sequence. The function of these position sensors is described as follows:

(1) Standby Position: The actuator piston and the calibrator piston are returned to a start position by hydraulic fluid (MIL-H-5606) pumped against the actuator piston. The standby position sensor causes the hydraulic fluid to be diverted when the calibrator piston is returned to the starting position.

(2) Start Position: At the start of a run, a solenoid valve opens allowing dry nitrogen from a storage bottle (plenum) to pressurize the actuator piston. The actuator piston first drives the poppet
valve closed. As soon as the poppet valve closes, the calibrator piston starts to move. The calibrator piston is now displacing fluid at the calibrated flow rate. There may be a slight perturbation of the flow at the instant the poppet valve closes due to the inertia of the calibrator piston. The calibrator piston travels approximately 18 to 20 cm (7 to 8 in.) before the start position sensor is reached and the actual timed displacement begins. Only 2.5 to 5 cm (1 to 2 in.) of piston travel is actually required for the starting transient perturbation to die out.

(3) **End Position:** After the calibrator piston has traveled approximately 75 cm (29.5 in.) the end position sensor is actuated and the timed piston displacement ends. The actual distance traveled by the calibrator piston is not important. The volume displaced between the actuating positions of the start and end position sensors is precisely determined by a "water draw" test which is described in Para 3.5.1.4.

After the end position is passed, a solenoid valve is actuated to cause hydraulic fluid to be pumped against the hydraulic side of the actuator piston and thus return the calibrator to the start position. The hydraulic pump runs continuously. The return of the actuator piston first causes the poppet valve to open and then the travel of calibrator piston to cease since the controlled flow rate now passes through the calibrator piston. After the poppet valve is fully opened, the actuator piston then returns the calibrator piston to the starting position. The flow of hydraulic fluid to the actuator piston is stopped at the instant the calibrator piston returns to the start position.

A double seal with a weep hole between the two seals is used to seal the poppet valve actuator rod. This assures that neither hydraulic fluid nor calibrating fluid leaks through these essential seals. The two seals are cup seals which are made from graphite filled Teflon® and spring loaded radially outward with metal leaf springs.

As the hydraulic pressure drives the actuator piston back to the starting position, the dry nitrogen is compressed and returned to the nitrogen storage bottle (plenum). This arrangement conserves the use of nitrogen. As long as the operating pressure in the Flow-Thru Calibrator is essentially constant, the pressure in the nitrogen storage bottle (plenum) remains constant. The following formulas are typically used to determine the pressure to be stored in the plenum:

\[
P_N(k\text{Pa}) = 413.7 + \frac{P_c(k\text{Pa})}{4}
\]

or \[P_N(\text{psig}) = 60 + \frac{P_c(\text{psig})}{4}\]  \hspace{1cm} (3-1)

where \[P_N = \text{Nitrogen pressure in the actuator cylinder}\]

\[P_c = \text{Pressure in the Flow-Thru Calibrator cylinder}\]
The Flow-Thru Calibrator has a tube mounted on the outlet head and which is concentric with the outlet pipe. This tube acts as a "fail safe stop" as shown in Figure 3-1(b) and Figure 3-4 to drive the poppet valve in the calibrator piston open in the event that the control system does not cause the actuator piston to return to the start position. Should the poppet valve be mechanically driven open, the calibration fluid would continue to circulate through the system at the rate previously set.

Three separately mounted magnetic reed switches were originally used to detect the movement of a magnet attached to the pneumatic piston. The calibration sequence started at the position of the first reed switch and the other two reed switches actuated the timer at the start and end of the calibrated displacement interval. Since reed switch actuation was somewhat erratic, consistent volume displacement calibrations were difficult to achieve. Flow Technology has made the following improvements to the above displacement measuring method:

1. A separate rod was attached to the calibrator piston which extends to outside the cylinder through a seal gland. This is referred to in this report as the "extension rod."

2. A flag was attached to the extension rod which can actuate three electro-optical sensors for position sensing within ±0.008 mm (0.0003 in.)

3. An invar rod which is approximately 6.4 mm (0.25 in.) diameter is used to maintain the relative position of the two electro-optical sensors which determine the calibrated displacement.

The repeatability of the electro-optical sensors was established by testing an assembly on a milling machine which used a digital readout having a resolution of 0.0025 mm (0.0001 in.). This test arrangement permitted evaluating the sensors at slewing speeds approximating the maximum calibrator piston speed of 0.6 m/s (2.0 ft/s).

3.5.1.3 Advantages of the Flow-Thru Calibrator - The Flow-Thru Calibrator has the following advantages when compared to a dynamic (flow calibration) weigh stand:

1. The Flow-Thru Calibrator can be operated in a pressurized, closed system. This gives the hydrocarbon test fluid immunity from fluid contamination due to water condensation at low temperatures and boil-off of the lighter hydrocarbon fractions at high temperature. The use of a closed system also obviates the need to add an icing inhibitor to absorb condensed moisture and introduce changes in the fluid properties of the calibration fluid.
The Flow-Thru Calibrator is a precision volumetric displacement measuring device that is particularly suited to the calibration of flow meters which are primarily sensitive to volumetric flow rate such as turbine, vortex shedding or positive displacement flow meters. Some density correction is still required for precise volumetric flow rate calibration if the temperature at the instrument is significantly different from the temperature in the Flow-Thru Calibrator.

When the Flow-Thru Calibrator is used with a precision densitometer, it is possible to calibrate mass flow rate sensitive instruments to a greater accuracy than is achievable with a dynamic weigh stand. Using a conservative accuracy of within 0.05 percent for a densitometer and knowing the displaced volume of the Flow-Thru Calibrator within 0.04 percent, the accuracy of a mass flow rate determination would be within 0.13 percent over a wide temperature range. This estimate of accuracy is based on other known and estimated errors as described in Section 3.9.

The accuracy of the Flow-Thru Calibrator not only depends on the precision to which the metered volume is known, but also depends on having essentially zero leakage across the calibrator piston seals. Flow Technology has developed some unique procedures for verifying zero leakage. These procedures and an analysis of problems with leakage testing are discussed in Para. 3.5.1.5.

The control console for the Flow-Thru Calibrator can be set for repeated runs. A new run is started as soon as the calibrator piston is returned to the standby position. A thumbwheel switch on the control console allows dialing in as many repeated runs as desired by the operator.

3.5.1.4 Volumetric Displacement Calibration of a Flow-Thru Calibrator - The Flow-Thru Calibrator is primarily calibrated by a method referred to as a "water draw". A solenoid valve and several quick-operating hand valves are used to transfer fluid from the flow tube to a series of Seraphin® cans. The Seraphin cans are stainless steel cans with a graduated, narrow neck for precise volumetric calibration. The cans are certified by NBS to within ±0.03 percent.

Flow at the outlet of the Flow-Thru Calibrator is blanked off either by a blank-off plate or a double block and bleed valve. A solenoid valve and a hand valve are connected to the end of the calibrator cylinder to allow liquid to be bled from the cylinder to a 5 gallon Seraphin can. The Flow-Thru Calibrator is filled with fluid and trapped air is bled off through a port in the cylinder head. The actuator piston is pressurized with nitrogen to cause the poppet valve to close and fluid to be displaced by the calibrator piston. Fluid flows out of the open solenoid valve and is diverted away from the Seraphin can until the start position is reached. The solenoid valve is closed when the start position sensor is reached. The movement of the calibrator piston also stops at this time since the closed solenoid valve will not allow fluid to leave the flow tube. The Seraphin can is placed under the outlet of the solenoid valve and a manual override switch opens the solenoid...
valve to begin the sample collection. The manual override switch is actuated
until there is sufficient movement of the calibrator piston to allow the flag
on the optical shaft to clear the position sensor at the start position. The
solenoid valve will then remain open until the flag on the optical shaft
reaches the stop position. The time for the collection process is reduced by
opening the hand valve to increase the flow rate into the Seraphin can. The
hand valve is closed when the end position sensor is neared to allow the
solenoid valve to stop the sample collection process. The volume displaced by
the Flow-Thru Calibrator is matched closely enough to the volume of a Seraphin
can that the actual volume displaced can be accurately determined at the end
of the "water draw" test by reading a calibrated sight glass attached to the
neck of the can.

The total volume of fluid collected is recorded and the "water draw" is
repeated until there is a satisfactory agreement among several such tests.
Flow Technology normally conducts three to four "water draw" tests prior to
shipment. Flow Technology recommends that the user conducts on site at least
two "water draw" tests or until two successive tests agree within 0.02 percent
at the site of the installation.

Flow Technology uses tap water to conduct the "water draw" tests. The water
temperature must be carefully measured within the cylinder of the Flow-Thru
Calibrator as well as within Seraphin cans since an error of 0.5°C alone will
result in a 0.01 percent error in the volumetric determination. The density
of the tap water is determined by weighing a water sample in a narrow-neck,
certified flask.

If the "water draw" test were conducted with Stoddard solvent, an error of
0.5°C would produce 0.055 percent error because of the higher coefficient of
volumetric expansion. It will generally be more convenient to conduct the
"water draw" test on site using the test fluid currently in use rather than
risk contamination of the calibration fluid.

3.5.1.5 Calibrator Piston Seal Leakage - The accuracy of the Flow-Thru
Calibrator depends not only on the precision to which the metered volume of
liquid is known but also depends on there being zero leakage across the seals
of the calibrator piston.

The calibrator piston uses two (redundant) Teflon® (TFE) U-shaped seals with
an internal spring to cause the lip of the seal to maintain contact with the
cylindrical wall of the flow tube. If the flow tube is manufactured from
carbon steel, an electroless nickel finish is applied on the inside of the
flow tube. Chrome plating is used on the inside of a stainless steel flow
tube. Low friction and low wear is achieved with TFE rubbing over a 12 rms
finish. Two Rulon® (glass filled TFE) glide rings are used to keep the
calibrator piston centered and reduce the wear on the Omniseals®.
3.5.1.5.1 Testing for Calibrator Piston Seal Leakage - Flow Technology has developed a unique procedure to verify that essentially zero leakage exists across the calibrator piston. The procedure is as follows:

1. Any outlet piping is detached and a blind flange is sealed against the outlet flange of the Flow-Thru Calibrator.
2. The actuator piston is pressurized at 620 kPa (90 psig).
3. Fluid is bled off the top of the flow tube to exclude air.
4. Any movement of the calibrator piston is sensed by a dial indicator resting on the end of the extension rod used for detecting piston displacement.
5. Step (4) is repeated with an actuator cylinder pressure of 69 kPa (10 psig).

The Omniseals are self energizing (i.e. a differential pressure across the seal tends to increase the force of the lip against the cylindrical wall of the flow tube, thus improving the seal effectiveness). There is an area ratio of approximately 12.5:1 between the calibrator piston and actuator piston resulting in a simulated 5.5 kPa (0.8 psid) differential pressure across the calibrator piston with 69 kPa (10 psig) at the actuator piston. The simulated leakage pressure is low although the normal maximum differential pressure across the calibrator piston is 0.7 kPa (0.1 psid) during a calibration run.

A so-called double block and bleed valve is sometimes used at the outlet of the Flow-Thru Calibrator in lieu of a blind flange for sealing. The double block and bleed valve is a valve with two O-ring seals with a weep hole between the seals to insure that no leakage is occurring at either seal of the valve. The double block and bleed valve makes it unnecessary to disconnect the piping to run the leak test.

The inside diameter of the flow tube of the Flow-Thru Calibrator is checked for ovality and uniformity of the bore size every 15 cm (6 in.) along the length. The leakage test may be conducted at any position should leakage be suspected. The possibility of leakage at some intermediate position can be eliminated by comparing a 7.57 liter (2 gallon) run with a subsequent 11.36 liter (3 gallon) run at a low flow rate and while using a turbine flowmeter to indicate steady flow.

3.5.1.5.2 Thermal Effects During Calibrator Piston Leakage Testing - The thermal volumetric expansion coefficient for JP-4 and other jet fuels is approximately 0.001/°C (0.00055/° F). If the calibrator piston is located 10 in. from the outlet head of the flow tube, a 0.5°C temperature change will produce a 0.14 mm (0.0055 in.) movement of the calibrator piston. A good dial indicator, which is used to sense the movement at the end of the extension rod, has a resolution of 0.0025 mm (0.0001 in.). This amount of movement is equivalent to a 0.01°C (0.02°F) temperature change.
The above example illustrates the need for good temperature control and temperature measurement during a leak check. It will probably be necessary to correlate the temperature of the liquid in the Flow-Thru Calibrator with the movement of the calibrator piston versus time. The Flow-Thru Calibrator acts as a sensitive liquid bulb thermometer during the leak check.

Flow Technology normally conducts this test with tap water. Water has a thermal expansion coefficient which is 0.00022/°C (0.00013/°F) near room temperature, or about 25 percent of jet fuel. The temperature sensitivity during the leak check can be reduced by conducting the test with the calibrator piston close to the outlet head of the flow tube. If the calibrator piston is within 2.54 cm (1 in.) of the outlet head the temperature sensitivity with hydrocarbon fluids is reduced to 0.1°C/0.0025 mm (0.2°F/0.0001 in.) movement.

Brooks normally conducts the leakage test for 600 sec (10 min) with the calibrator piston located 5 to 7.5 cm (2 to 3 in.) from the standby position. This will produce a temperature sensitivity of 0.25 mm/°C (0.0055 in./°F) since there is approximately 28.3 liters (1.0 ft³) of water in the prover at such a position. If a calibrator piston movement of 0.038 mm (0.0015 in.) is observed in 600 sec (10 minutes) indicating leakage past the piston and the movement appears not to be due to temperature change, such a leakage amounts to only 0.01 per cent of the minimum flow rate 0.016 liter/sec (0.25 gpm) recommended for use with the 20.3 cm (8 in.) Flow-Thru Calibrator.

### 3.5.1.6 Theory of Double Chronometry

When a turbine flowmeter is calibrated using a Flow-Thru Calibrator, there is a discrete time when the proving run begins and a fraction of a second later the passing of a blade is detected by a proximity detector. It is impossible to make these two events simultaneous. The same situation occurs at the end of the run.

If the number of blades \( N_b \) are counted during a calibration run starting with the first blade detected after the start of the run and ending with the first blade detected after the end of the run the turbine flowmeter calibration constant \( K_M \) could be determined from the following equation:

\[
K_M = \frac{N_b - 1}{V_p} \tag{3-2}
\]

where \( K_M \) = Flowmeter constant, pulses/m³ (pulses/gal)

\( V_p \) = Certified Flow-Thru Calibrator volume, m³ (gallon)

\( N_b \) = No of blades counted during the calibration run

The maximum error introduced by Equation (3-2) can be estimated from the following equation:

\[
e_T(\text{percent}) = \frac{100}{N_b - 1} = \frac{100}{K_M V_p} \tag{3-3}
\]
The potential error introduced by using Equation (3-2) can be virtually eliminated by measuring the time interval $t_M$ for the passing of $N_b$ blades as well as the time interval $t_c$ for the displacement of the Flow-Thru Calibrator. The calibration correction procedure which uses two nearly simultaneous time interval measurements is referred to as double chronometry.

The two time measurements are illustrated graphically in Figure 3-5. The volume of liquid displaced by the Flow-Thru Calibrator is proportional to time. Equation (3-2) can then be rewritten to correct the certified displacement volume $V_C$ to correspond to the effective displaced volume which occurs during the time interval for $N_b$ blades to pass or

$$K_H = \left(\frac{t_p}{t_M}\right) \left(\frac{N_b - 1}{V_p}\right) \quad (3-4)$$

where

- $K_H = \text{Corrected flowmeter constant, pulses/unit volume}$
- $t_M = \text{Time to count } N_b \text{ blades, sec}$
- $t_p = \text{Time for certified displacement of Flow-Thru Calibrator, sec}$

3.5.1.7 Control Console for Flow-Thru Calibrator — A photograph of the control console for the Flow-Thru Calibrator is shown in Figure 3-6. The control console has the following features:

1. Precision internal 100 kHz clock which is accurate to $\pm 0.000010$ sec.
2. Provision for double chronometry.
3. A series of switches for setting a constant corresponding to the certified displacement volume are inside the console to prevent accidental change in setting.
4. Operator can set external thumbwheel switch for $N$ sequential runs. The console automatically returns the calibrator piston to standby position and stops after $N$ runs.
5. Built in frequency meter displays blade passing frequency for turbine, vortex shedding or other flowmeters having a discrete pulsed output.
6. Internal microprocessor calculates and displays results from each proving run including corrected flowmeter constant per Equation (3-4).
7. Microprocessor averages the results for $N$ runs.
8. IEEE-488 interface can transfer data to an external microprocessor.
3.5.1.8 Flow Rate Calibration System Using a Flow-Thru Calibrator - Figure 3-7 shows a schematic diagram of a liquid flow rate calibration system using a Flow-Thru Calibrator as the primary standard for the calibration of flowmeters.

Liquid is continuously circulated through the system by use of one of two centrifugal pumps. One pump is used for high flow rates and the other for low flow rates. A check valve at the outlet of each pump prevents recirculation of the liquid through the non-operating pump.

Three flow regulating valves are used in parallel to achieve a wide range of controlled flow rates. A typical flow regulating valve has a "turn down" ratio of 15 to 1. The regulating valve combination gives a controllable flow ratio of 500 to 1. Each regulating valve has a scale which is calibrated in volumetric flow rate. A single scale setting will maintain the flow rate within ± 1.5 percent of the set point with a variation in differential pressure across the valve of 69 to 1034 kPa (10 to 150 psid).

The densitometer and viscometer are located in the low flow rate line. This allows controlling the sample flow rate without a significant effect on the higher flow rates.

One heat exchanger is used for low temperature operation and electrical pipe heaters are used for high temperature operation. The circulating pumps tend to heat the circulating fluid. An additional heat exchanger, which uses water for cooling, is used to maintain operating temperature near ambient conditions. The liquid flows continuously through the check valve located in the piston of the Flow-Thru Calibrator. This allows flow rate, temperature and pressure to stabilize before the control system initiates a "calibration run".

A piston accumulator is used to control the pressure in the closed liquid system. The accumulator provides for thermal expansion of the liquid over the operating temperature range as well as damping out pressure pulsations produced by the pumps.

In addition to providing a flow calibration system having a high accuracy, the system shown in Figure 3-7 is completely immune to boiloff of the lighter fractions of hydrocarbons and to freezing.

3.5.1.9 Effect of Thermal Expansion on Design - The volume displaced by the Flow-Thru Calibrator will vary with operating temperature due to thermal expansion effects. The volume displaced is a product of the cross-sectional area of the flow tube and the actual calibrator piston travel between actuation points of the optical sensors. The seals on the calibrator piston can conform to slight differences in radial expansion between the calibrator piston and flow tube. The change in the effective area of the displacement is determined by the thermal expansion of the flow tube.

Figure 3-8 shows the thermal expansion characteristics of several materials. Considering the wide range of operating temperatures for the HAFF program, one manufacturer recommended that the calibrator piston be manufactured from 400 series stainless steel if the flow tube was made from 1020 carbon steel. These two materials have about the same thermal expansion characteristics as shown in Figure 3-8.
The calibrator piston is customarily made from 300 series stainless steel but few customers use the Flow-Thru Calibrator at extreme temperature conditions. It would be preferable to manufacture the cylinder and the calibrator piston from 300 series stainless steel and completely avoid the problem of differential thermal expansion as well as achieving excellent protection against corrosion.

The area correction factor versus temperature is shown in Figure 3-9 for various materials. Figure 3-10 shows curves for estimated errors in the area correction factors due to different values of uncertainty in the thermal expansion effects.

3.5.1.10 Transient Thermal Expansion of the Extension Rod (Stroke Measurement) — The correction for piston stroke due to thermal expansion effects is somewhat more difficult to estimate. The extension rod is near the ambient temperature prior to a calibration run. The extension rod directly contacts the calibration liquid at the operating temperature during the run. The extension rod thus may experience a transient change in temperature during an initial calibration run. The extension rod has more time to equilibrate to the temperature of the calibration liquid at low flow rates than at high flow rates.

The problem of estimating the effect of temperature change on the effective stroke is further complicated by the sequential calibration runs where the extension rod has already acquired the temperature of the working fluid, but is slow to equilibrate to the ambient temperature when the calibrator piston returns to the standby position. When the extension rod is external to the flow tube, the heat transfer mechanism between the extension rod and the ambient is by free convection in a gas. When the extension rod is inside the flow tube, the heat transfer mechanism is by forced convection in a liquid. The transient temperature is thus biased towards the temperature of the calibration liquid since the latter heat transfer mechanism is more effective. The effective stroke length, as determined by the temperature distribution in the extension rod, will finally reach an equilibrium length after one or more sequential calibration runs. When the Flow-Thru Calibrator is used at a temperature significantly different from ambient, the results from the first of several sequential calibration runs should be ignored until the results agree within an acceptable deviation. The effect of temperature on the length of the extension rod is a function of the time the rod is directly exposed to the liquid and the exposure time is dependent on the calibration flow rate. The thermal effects on extension rod length are thus dependent on both liquid flow rate and the calibration temperature.

The effect of temperature on the change in length of the extension rod constitutes a bias error. One way to reduce the effect of this error is to make the extension rod of a material with a low expansion coefficient such as Invar®. A conservative estimate of the error introduced by using an Invar extension rod is shown in Figure 3-10. It would be desirable to further reduce this error. Further analysis using transient heat transfer theory should make it possible to significantly reduce the error caused by this thermal effect.
3.5.1.11 Improvements in the Flow-Thru Calibrator - There are two options which are recommended, in addition to manufacturing the extension rod from Invar, to make the Flow-Thru Calibrator practical over a wide range of operating temperatures and flow rates. These options are described in the following paragraphs.

3.5.1.11.1 Sealed Cover for Displacement Sensing Mechanism - The present design of the Flow-Thru Calibrator provides a thin tubular cover about 12.7 cm (5 in.) in diameter and 122 cm (48 in.) long which protects the displacement measuring mechanism (extension rod, optical sensors, etc.) from accidental damage or stray light effects. Icing or condensation would probably affect this mechanism at low temperature. The mechanism could be adapted to lower temperature operation by the following modifications:

(1) Use an O-ring gasket seal where the protective tube fits over a cylindrical adapter at the surface of the inlet flange.

(2) Use an O-ring gasket seal where the protective tube fits over a tie rod at its end cap.

(3) Provide a hermetic electrical connector for penetration of the electrical leads for the optical sensors.

(4) Provide fittings for purging the interior of the protective tube with dry nitrogen.

3.5.1.11.2 Additional Optional Sensors - Table 3-5 shows the displacement measuring time for various flow rates with the 20.3 cm (8 in.) Flow-Thru Calibrator including the effect of adding two additional position sensors. The standard metered displacement-stroke is 75 cm (29.5 in.). The metering times become unreasonably long below 315 cm³/sec (5 gpm). Just one additional optical sensor positioned at 15 cm (5.9 in.) or 3.785 liters (1 gallon) displacement would greatly reduce the metering time at low flow rates without a significant compromise in accuracy.

A fourth optical sensor in an intermediate position at 30 cm (11.8 in.) or 7.57 liters (2.0 gallons) would further improve the calibration run times which could be selected with only a minor design change. This would result in a total of five (5) optical sensors, one (1) for the standby positioning of the calibrator piston and four (4) for displacement measurement.

3.5.2 Ballistic Flow Calibrator (Type V-2) - The ballistic flow calibrator is similar to the Flow-Thru Calibrator described earlier. A schematic diagram of the ballistic flow calibrator is shown in Figure 3-11. Both the ballistic flow calibrator and the Flow-Thru Calibrator use a rigid metal piston with dual glide rings and dual elastic seal rings on the piston. The piston is fitted inside a metal cylinder having a precision bore.

The piston in the ballistic Flow-Thru Calibrator does not have an internal poppet valve which allows flow to pass through the piston to establish steady state conditions prior to a run.
The ballistic flow calibrator is actuated by gas pressure acting on one side of the calibrator piston which forces the calibration fluid through the flowmeters and into a storage tank. This makes a simple calibration system since no pumps, valves or filters are required, but there is no provision for temperature calibration at other than room temperature. The ballistic flow calibrator and its associated equipment could be soaked in an environmental chamber to permit calibration over a wide temperature range.

The ballistic flow calibrator only provides a flow calibration under transient conditions. A commercial version is designed for calibrating turbine flowmeters which have a relatively high rate of response to change in flow rate. This ballistic flow calibrator is not suitable for calibrating a flowmeter having a significantly lower rate of response than a turbine flowmeter. McIrvin et al [9] discuss the use and accuracy of a commercial version of the ballistic flow calibrator.

An extension rod is attached to the piston of the ballistic flow calibrator. The rod extends through a seal on the inlet end of the flow tube to detect precise movement of the piston. An optical encoder is attached to the extension arm. The optical encoder provides a means of counting lines which are precisely photo-etched on a glass grid which is rigidly attached to the frame. Up to 20,000 lines per inch are etched on the grid providing a displacement resolution of 0.00127 mm (0.00005 in.). The volume displaced can be reduced to decrease the testing time for low flow rates by setting the counter to stop the test at a reduced stroke.

3.5.3 Pipe Prover (Type V-3) - The pipe prover is similar to the Flow-Thru Calibrator and ballistic flow calibrator. Figure 3-12 shows a pictorial view of a calibration system using a bidirectional pipe prover. The pipe prover literally uses a pipe for the cylindrical sections. The piston displacer is a sphere made from an elastomeric material. The pliable characteristic of the sphere makes it possible to maintain a "piston seal" as it moves through pipe sections having long radius bends. The sphere is propelled by the differential pressure created by the flow of liquid behind the sphere.

A typical pipe prover having a capacity similar to the 18.927 liter (5 gallon) Flow-Thru Calibrator is presented in Table 3-6. This pipe prover has a "proving" displacement of 227 liters (60 gallons). The run times would thus be 12 times as long as for a comparable Flow-Thru Calibrator. The large "proving volume" is necessary to reduce errors due to the inaccurate method of detecting the sphere at the start and stop of a run.

The inside of the elastomeric sphere is hollow and filled with an ethylene-glycol mixture to prevent freezing. The sphere is filled through a flush mounted valve similar to a football valve. The sphere is overinflated by two percent — that is, the sphere has a larger diameter than the pipe it transverses through. A 15.2 cm (6 in.) sphere has a diameter about 3 mm (0.12 in.) greater than the inside diameter of the pipe.
The sphere is typically "launched" at one end of a "U-shaped" pipe through a 25.4 cm (10 in.) section. After the sphere enters the 15.2 cm (6 in.) pipe section, it strikes a pin which actuates a microswitch to start a timer. The timer is stopped at a corresponding position at the other end of the pipe. The sphere comes to rest after it is captured in the 25.4 cm (10 in.) pipe section at the far end of the pipe.

The pipe prover shown in Figure 3-12 is a bidirectional pipe prover. A four-way valve arrangement reverses the flow through the prover for the next "proving" run. The patent review revealed 5 patents relating to bidirectional pipe provers and 21 relating to unidirectional pipe provers.

The sphere which acts as a piston seal is recirculated in a unidirectional pipe prover. The spheres are transferred from the outlet to the inlet through an interchange passage. Some patents describe the use of multiple spheres in the interchange passage – two or more spheres in the interchange passage act as seals to prevent leakage from the inlet to the outlet of the pipe prover.

The pipe prover is in very common usage in the petro-chemical industry and is often referred to as a "custody transfer" standard. The volume of a pipe prover is traceable to NBS(G) by a "water draw" test. No weld joints are used in a pipe prover unless they are near a flange where the inside diameter can be ground smooth. The inside of the pipe typically has an epoxy coating for a smooth surface and to prevent pipe corrosion as a consequence of "water draw" testing.

Figure 3-13 shows a rigid piston design for use in a pipe prover which is described briefly by Hayward [11]. This piston device apparently is used as an improvement over the use of an elastomeric sphere in a pipe prover. It has been used at the Central Measurement Laboratory in Budapest, Hungary and NEL, UK. The piston device has a provision for capturing any leakage past the redundant seals. NEL claims the ability to detect discrete positions of the piston within ± 0.02 mm (0.0008 in.). This is not as accurate as the position-accuracy claimed for the Flow-Thru Calibrator manufactured by Flow Technology. This accuracy is, however, an improvement over that obtained by using a pin – actuated microswitch when struck by a elastomeric, spherical prover piston.

The pipe prover is limited to an operating temperature range of -18 to +82°C (0 to 180°F). One manufacturer of pipe provers also manufactures custom designed Flow-Thru Calibrators (similar to Type V-1) for liquid propane applications where fluid temperatures are near -42°C (-44°F).

The pipe prover can demonstrate a typical repeatability of a run to 0.01 percent. The pipe prover is also recognized by an international standard – American Petroleum Institute Standard API-2531.
3.5.4  **Volumetric Tank Calibration Methods** — Various calibration methods using calibrated volumetric tanks have been used. Hayward [11] discusses a method which has been used at the National Engineering Laboratory (NEL), Glasgow, Scotland. A schematic diagram of the method is shown in Figure 3-14. Detail of the tank design is shown in Figure 3-15. The calibrated volumetric tank has a narrow tubular entrance and a narrow tubular neck at the top of the tank. The volume of the tank is precisely determined between a reference level on the entrance tube and a reference level on the neck of the tank.

The volumetric calibration method shown in Figures 3-14 and 3-15 utilizes a standing start and finish. There is substantial error produced by transient flow conditions as the stop valve opens and closes.

A similar volumetric calibration method has been tried at NEL using a flying start and finish, but accuracy achieved was insufficient to justify continued use.

3.6  **Methods of Liquid Flowmeter Calibration Using Gravimetric Standards**

Table 3-3 gives a summary of four (4) methods of using gravimetric standards for liquid flowmeter calibrations. The following paragraphs present a more detailed description of these methods.

3.6.1  **Dynamic Weight Stand Using a Weigh Beam (Type G-1)** — The method of calibrating mass flowmeters at GE/AID has been to use a dynamic flowmeter calibration stand. Since the principal product to be calibrated has been true mass rate flowmeters, the dynamic weigh stand has represented a direct and accurate method of calibrating flowmeters. The weigh stand in current use is not considered to have sufficient accuracy for the high accuracy fuel flow meter (HAFF) development program. A study of this flow calibration equipment was undertaken to determine if the equipment could be used as an interim flow calibration facility for the HAFF program. The dynamic weigh stand which is used as the primary calibration equipment for quality assurance was manufactured by the COX Instrument Division of AMETEC (formerly of the Lynch Corp).

3.6.1.1  **COX Flowmeter Calibrators** — Figure 3-16 shows a schematic diagram of the COX Flowmeter Calibrator system. Figure 3-17 shows a pictorial view of the fluid flow components and the flow calibrator. The principal assembly, which affects the accuracy of the system, consists of a weigh tank suspended on a precision weigh beam mechanism. The weigh tank is suspended on the mechanism using knife-edge pivots made from hardened tool steel. All pivots in the weighing mechanism are high quality knife-edge pivots.

Figure 3-18 shows a pictorial drawing of the weigh tank and weigh beam mechanism for the COX 311H Flowmeter Calibrator. The weigh beam has a lever arm ratio of approximately 4 to 1 and the tare beam has a lever arm ratio of approximately 12.5 to 1. The knife-edge pivot which supports the weight pan is adjustable such that the overall lever arm system can be adjusted to a ratio of 50 to 1 within 0.03 percent. There is a proximity switch located at the end of
the "tare" beam. The proximity switch senses the position of an aluminum "button" 19 mm diameter x 12.6 mm thick mounted on the top and at the end of the tare beam. There are two stops to limit the travel of the tare beam. These stops are located between the weigh pan and the proximity switch. The stops limit the travel of the tare beam to ± 0.76 mm (0.03 in.) from the horizontal position. The tare beam never strikes the end of the proximity switch. The proximity switch is actuated when the end of the tare beam rises approximately 0.26 mm (0.010 in.) above the horizontal position of the tare beam. After the tare beam rises off the lower stop it thus travels approximately 1.0 mm (0.04 in.) before actuating the proximity switch.

The sensitivity of the balanced system is such that a single 400 mg weight when added to the weigh tank will cause the beam to "trip" and start the timing mechanism with 189.6 kg mass on the weigh tank pivots including the mass of the weigh tank. This is equivalent to a sensitivity of 0.0002 percent.

Table 3-7A gives the design and accuracy characteristics of the COX 311H Flowmeter Calibrator. Table 3-7B gives the same information for the COX 305T Flowmeter Calibrator.

Figure 3-18 shows a sliding weight on the tare beam. There are actually two sliding (tare) weights. One sliding weight 1.0 kg (2.2 lb) is permanently attached to the tare beam and an additional 1.0 kg (2.2 lb) weight can be stacked on the permanent weight. These tare weights are used to vary the tare time. A linear scale 40.6 cm (16 in.) long is attached to the tare beam as a guide to positioning the tare weight (or weights) prior to a run.

The sequence of events during a run on the COX 311H calibration stand is as follows:

1. The sliding tare weight or weights are set to achieve the minimum "tare time" recommended by COX as follows:

<table>
<thead>
<tr>
<th>kg/sec</th>
<th>lb/hr</th>
<th>Tare Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.063-0.126</td>
<td>500-1,000</td>
<td>15 sec</td>
</tr>
<tr>
<td>0.126-18.9</td>
<td>1,000-150,000</td>
<td>5 sec</td>
</tr>
</tbody>
</table>

2. The dump value at the bottom of the weigh tank is closed and fluid starts accumulating in the weigh tank. The tare beam is "down" due to the force of gravity of the sliding tare weights and the weight of the scale beam mechanism.

3. As soon as sufficient fluid accumulates in the weigh tank - the tare beam rises and causes the proximity switch to start the 1000 Hz clock.

4. A weight or combination of precision brass weights are now placed on the weigh pan forcing the tare beam "down". The total weight placed on the pan is equal to 1/50th of the total weight of fuel to be accumulated in the weigh tank.
(5) When the total accumulated fuel in the weigh tank is in balance with the counterweights and scale beam mechanism, (a) the tare beam again rises, (b) the proximity switch at the end of the tare beam is actuated and (c) the 1000 Hz clock is stopped.

(6) The fluid in the weigh tank is dumped into the storage tank in preparation for the next calibration run.

The flow rate of the calibration fluid from the above sequence of events is calculated from the following equation:

\[ W_s = \frac{M_bR_0}{t_A} \]  \hspace{1cm} (3-5)

where 
- \( W_s \) = Mass rate of fluid flow based on static balance (kg/sec)
- \( R_0 \) = Scale beam ratio (i.e. 50)
- \( M_b \) = Mass of brass weights placed on the scale pan (kg)
- \( t_A \) = Actual clock time between proximity switch actuation at start and end of run

Equation (3-5) is generally the only equation used to determine mass rate of flow during a calibration run. There are three correction factors that should be applied to the value given by Equation (3-5), they are as follows:

(1) Buoyancy correction factor (see Appendix A)

(2) Timing errors caused by the momentum forces resulting from the fluid spilling into the weigh tank and the inertia of the weighing mechanism

(3) Mass of fluid jet which is captured by the rising fluid level in the weigh tank but is not counterbalanced by the force of the reference mass.

The buoyancy correction factor is derived in Appendix A. A mass balance is generally calibrated with precision brass weights for which a true mass is known. If the mass balance is used to determine the mass of a material which has a density significantly different than brass, a correction factor must be applied which is caused by a difference in the buoyancy forces of the air surrounding the two masses being weighed. The buoyancy forces on the mass being weighed are equal to the volume of the mass times the density of the surrounding air according to Archimedes principle. If the density of a given material being weighed has half the density of brass, the buoyancy forces on the material would be twice as great as that for brass – depending on the desired accuracy, this difference could be significant.
NBS(G) routinely corrects the mass flow rate given by Equation (A-6) in Appendix A with a factor of approximately 1.00142 or a 0.142 percent correction. This factor may vary slightly with change in density of the calibration fluid. A derivation for the buoyancy correction factor as it applies to the COX 311H flow calibration stand is presented in Appendix A as Equation (A-5).

Figure 3-19 presents the estimated variation of the buoyancy correction factor $K_B$ for jet fuels as a function of temperature and the molecular weight of the fuel vapor. Data for the molecular weight of the fuel vapor is difficult to obtain. A more precise method of determining the buoyancy factor would be to measure the density of the air vapor mixture in weigh tank with a densitometer in situ. The buoyancy correction factor could then be easily determined from Equation (A-5) of Appendix A.

Figure 3-20 illustrates the deviations from the ideal time interval measurement for a run. These deviations result from change in the dynamic forces and system inertia during a run. Figure 3-20 also illustrates how the actual time interval measurement can be corrected to the ideal time interval which is equivalent to balancing the weigh tank under static conditions.

The fluid falls the greatest distance from the spreader cone at the start of a run. The fluid accelerates as it falls and imparts an impulse to the weigh tank and fluid contents which causes the tare arm to start lifting earlier than if they were in static balance at the time the proximity switch is actuated. The tare beam starts rising $t_s$ seconds prior to the ideal start time when the system would be in static balance. The inertia of the system is low at the start. The inertia of the system is greater at the end than at the start due to fluid accumulating in the weigh tank and the calibration weight which is added to the weigh pan. The time to move the tare beam from its lower stop to the point where the proximity switch is actuated is less at the start than at the end when the inertia of the weighing system has increased. Figure 3-20 shows graphically that:

\[ t_{T2} > t_{T1} \]

where $t_{T1} =$ Time required for tare beam to lift off lower stop and actuate proximity switch at start of run

$t_{T2} =$ Time required for same tare beam movement at end of run
The fluid does not fall as far before impacting on the surface of the fluid or tank bottom at the end of a run as it does at the start of a run. The impulse from the velocity of the falling fluid is thus smaller at the end of a run and the tare beam does not start to rise as early, or as shown in Figure 3-20:

\[ t_{s1} > t_{s2} \]

where

- \( t_{s1} = \) Time of start of tare beam movement in advance of ideal (static balance) trip time at start of run
- \( t_{s2} = \) Time of start of tare beam movement in advance of ideal (static balance) trip time at end of run

Equation (3-5) assumes that a static balance exists in the dynamic flow calibration system. The actual clock time \( t_A \) between proximity switch actuation time should be replaced in Equation (3-5) with the corrected time \( t_c \). The corrected time \( t_c \) is from the start to the end of the run if no fluid momentum or inertia effects existed. An examination of Figure 3-20 shows that the corrected time can be calculated from the following equation:

\[
t_c = t_A + \left[ t_{T1} - t_{S1} \right] - \left[ t_{T2} - t_{S2} \right]
\]

or

\[
t_c = t_A - \left[ t_{T2} - t_{T1} \right] - \left[ t_{S1} - t_{S2} \right]
\]

and a timing correction factor \( K_T \) can be used to correct the flow rate from Equation (3-6) for timing errors where

\[
K_T = \frac{t_A}{t_c} = 1 + \left( \frac{t_{T2} - t_{T1}}{t_c} \right) + \left( \frac{t_{S1} - t_{S2}}{t_c} \right)
\]

Equation (3-7) can be rewritten as the following approximation with negligible error:

\[
K_T \approx \left[ 1 + \left( \frac{t_{T2} - t_{T1}}{t_c} \right) \right] \cdot \left[ 1 + \left( \frac{t_{S1} - t_{S2}}{t_c} \right) \right]
\]

The timing correction factor will always be greater than unity or \( K_T > 1.0 \). The timing error is a function of mass flow rate—the greater the flow rate, the greater the timing error \( K_T \).
Figure 3-21 illustrates the approximate geometry of the liquid as it spills from the spreader cone of the weigh tank in the COX 311H calibration stand. The spreader cone has an angle of approximately 30° with the horizontal direction – the initial vertical velocity component $u_v$ is therefore 0.5 times the absolute velocity $w_o$ leaving the spreader cone. As the liquid falls, the vertical velocity component increases due to the acceleration of gravity.

The approximate mass flow rate from Equation (3-5) can be corrected to improve the estimate of the mass flow rate by the following equation:

$$W_A = K_B(K_TK_J)K_EW_s$$  \hspace{1cm} (3-9)

where

$W_A$ = Actual mass flow rate (kg/s)

$K_B$ = Buoyancy correction factor, Equation (A-5) or Figure 3-19

$K_T$ = Timing correction factor

$K_J$ = Liquid jet mass correction factor, Equation (B-7)

$(K_TK_J)$ = Combined flow rate correction factor, Appendix D or Figure 3-23

$K_E$ = Correction factor for differential thermal expansion of the weigh beam due to temperature gradients

$W_s$ = Mass flow rate based on static balance, Equation (3-5)

The volume of the liquid jet $V_L$ between the liquid levels at the start and end of the run contains a mass of fluid that has already entered the "control volume" $V_0$ as shown in Figure 3-21. The mass of the liquid jet $M_L$ will be weighed as a portion of the mass of the liquid at the end of the run but this mass was virtually already in the weigh tank at the start of the run. A correction factor $K_J$ for this error is derived in Appendix B.

The determination of the correction factor used in Equation (3-9) can be simplified by multiplying Equation (3-8) by Equation (B-15) with the following result:

$$(K_TK_J) \approx \left[ 1 + \left( \frac{t_{T2} - t_{T1}}{t_c} \right) \right]$$ \hspace{1cm} (3-10)
The derivation given in Appendix B as well as Equation (3-10) assumes that the falling fluid jet impinges on the liquid surface in the weigh tank at the start as well as at the end of a flow calibration run. Equation (3-10) greatly simplifies the correction calculations. The time required for the weigh beam to rise at the start and end of a calibration run [(tT1 and tT2)] can be determined from the analysis given in Appendix D.

Figure 3-22 is a schematic diagram of the weighing system for the COX 311H Flowmeter Calibrator. Figure 3-22 is used to relate the various dimensional characteristics of the COX 311H Flowmeter Calibrator for static and dynamic analysis. An example of the method for calculating the combined flow rate correction factors (KTKP) is given in Appendix D. These equations are generalized for the compound lever arm system of the COX 311H Flowmeter Calibrator but these equations can be simplified to apply to the COX 305T Flowmeter Calibrator which uses a single weigh beam.

Figure 3-23 shows the combined flow rate correction factor (KTKP) as a function of the flow rate for the COX 305T Flowmeter Calibrator. Figure 3-23 also shows the effects of varying the tare and run time on the combined flow rate correction factors (KTKP). The rise of the tare beam above the lower stop and prior to actuation of the proximity sensor is adjustable. COX recommends that the rise be set at approximately y0 = 2.54 mm (0.1 in.). Figure 3-23 shows that if the rise y0 is reduced below the value recommended by COX, the percent correction decreases in magnitude. If the deflection is reduced ten fold from y0 = 2.54 mm to 0.254 mm (0.010 in.) the percent correction is reduced approximately 50 percent. If the deflection is reduced to y0 = 0.0254 mm (0.001 in.), the correction is reduced to approximately 25 percent of the correction required for the deflection recommended by COX of y0 = 2.54 mm. A deflection as small as 0.0254 mm, however, may be impractical unless a device such as a load cell could detect a small change in the unbalanced forces without being damaged by over-range forces.

The lever arm ratio of a given weigh beam will not be affected if the temperature of the beam is significantly different from room temperature as long as there are essentially no temperature gradients along the length of the beam. The weigh beam which supports the weight tank would tend to be the most affected by temperature gradients since the length L1 is directly above the weigh tank and length L2 is more exposed to the ambient temperature as shown in Figure 3-22. If the temperature of the weigh tank and contents were greater than the ambient temperature, the length L1 would tend to increase more than L2 and Ke = 1.0. No attempt was made to estimate of value of Ke for various operating conditions since the temperature gradients in a beam should be determined experimentally.

The weigh beams in the COX Flowmeter Calibrators are manufactured from aluminum which should minimize the effect of thermal expansion on the lever arm ratio. Although aluminum has a thermal expansion coefficient which is about 45 percent greater than stainless steel, the thermal conductivity of aluminum is about twelve (12) times that of austenitic stainless steel. Only a few thermocouples should be necessary to determine the temperature distribution of a given weigh beam which is exposed to extreme temperatures. The correction factor Ke should be evaluated during operation since the temperature gradient of a beam cannot be accurately predicted from the temperature of the calibration liquid.
3.6.1.2 Improved Calibration Accuracy Using the COX Flowmeter Calibrators

Since several correction factors are needed to properly correct the apparent mass flow rate \( W_m \) based on a static balance to the actual mass flow rate as given by Equation (3-9), it is difficult to achieve an accuracy greater than 0.25 percent using the COX flowmeter calibrators. There are several things that can be done, however, to improve the accuracy of the COX flowmeter calibrators as interim calibration facilities.

During the calibration of true mass rate flowmeters, there are possibly two types of readouts: (1) continuous and (2) sequential. The continuous readout devices should be averaged over the same interval of time as for the flow calibration run on the COX Flowmeter Calibrator. Some mass flow rate meters require a finite amount of time for each read out. This type of flow rate meter should be read out sequentially at equal time intervals from the start to the end of a calibration run. The average indicated flow rate during the run can then be found by dividing the sum of the sequential readings by the number of readings during a run.

During the calibration of volumetric type flowmeters (i.e. turbine flowmeters), the following improvements should be made:

1. The number of pulses from the output of the turbine flowmeter should be counted for the time interval between the start and end of a run for a COX Flowmeter Calibrator in the determination of the flowmeter calibration constant, \( K_m \).

2. Use a precision densitometer in situ for converting mass flow rate from Equation (3-9) to volumetric flow rate corresponding to the proportional output of the turbine flowmeter.

3. Use a viscometer in situ for establishing the correlation between the calibration constant \( K_m \) and the parameter equal to output frequency divided by kinematic viscosity, \( f/\nu \) for a turbine flowmeter.

One possible source of error and a cause of lack of repeatability during the calibration of turbine flowmeters is the flow of entrained gas through the flowmeter. Hayward [11] describes two precautions used at NEL, Glasgow, UK to prevent air entrainment from causing calibration errors. NEL uses 60 mesh wire screen in the sumps at the pump suction inlets to prevent bubbles from entering the suction lines. NEL also uses a transparent plastic section in the calibration line to visually determine if gas bubbles are approaching a flowmeter being calibrated.

There is some indication that the COX Flowmeter Calibrators are designed such that a pocket of air or fuel vapor can develop in the standpipe at the entrance to the weigh tank. This pocket of gas would tend to occur in the piping after the back pressure control valve and above the spreader cone (see Figures 3-16 and 3-17). The volume of this gas pocket could vary due to changes in flow rate during a calibration run. The repeatability of the COX flowmeter calibrators would thus be affected due to a change in the mass of fluid retained in the standpipe.
COX states a repeatability of 0.1 percent for successive runs in their sales brochure for the COX Flowmeter Calibrators. Tests on the COX 305T Flowmeter Calibrator indicate a standard deviation for the repeatability of the calibration constant of a turbine flowmeter of approximately 0.05 percent at 1.5 kg/s (11,900 lb/hr). From the standpoint of absolute accuracy, the standard deviation for repeatability should be multiplied by two since it is a random error or $2\sigma = 0.10$ percent. This random error must be added to the estimated systematic errors to determine the uncertainty in the accuracy of a calibration.

No attempt was made to make an accuracy statement for the COX Flowmeter Calibrators since additional improvements and testing are needed to approach the accuracy requirements for calibration in the HAFF program.

3.6.2 Dynamic Weigh Stand Using a Weight Substitution Method (Type G-2) - Figure 3-24 shows a simplified method of dynamic weighing by placing a reference weight on the platform with the weigh tank at the start of the test. The weight is precisely equal to the mass of calibration liquid to be accumulated during a timing run. This is a flying start and finish method. As soon as enough liquid accumulates in the weigh tank to cause the scale beam to rise and start the timer, the reference weight is removed from the scale platform. The counterweight on the scale beam is not changed during a run since the counterweight is in equilibrium with the platform weight at the start and end of the run. When sufficient liquid enters the weigh tank to again lift the scale beam, the timer is stopped. Since the counterweight is not changed during the test and the inertial mass is almost the same at the end as at the start, the time response of the scale beam is virtually the same at the start as at the end of the run.

The calculated flow rate must be corrected using the correction factor for buoyancy error $K_b$ from Equation (A-5). The mass of liquid captured by the rising fluid can be assumed to be canceled by the change in impulse of the falling liquid jet by virtue of Equation (B-6).

Although this method eliminates the timing errors characteristic of Type G-1 calibrators (shown graphically in Figure 3-20) the handling of large weights is not practical for a weigh stand capable of calibrating flowmeters having flow rates up to 18.9 kg/s (150,000 lb/hr).

3.6.3 Dynamic Weigh Stand Using a Precision Load Cell (Type G-3) - Another method of eliminating the timing error characteristic of the dynamic weigh stand is to suspend the weigh tank on a precision load cell. This method has been used effectively at the National Bureau of Standards, Boulder, CO, NBS(B) cryogenic flow calibration facilities. Figure 3-25 shows a simplified drawing of how the weigh tank is suspended on the load cell at NBS(B). Since the load cell acts as a spring, the weigh tank and load cell act as a stiff spring-mass system. The weigh tank has a mass of about 70 kg dry and 454 kg filled. The natural frequency of the spring mass system during a run will be about 40 Hz indicating that the load cell will have a satisfactory rate of dynamic response to load changes.
Figure 3-26 shows a schematic diagram of the complete NBS(B) Cryogenic Flow Research Facility. A centrifugal pump driven by a variable speed motor is used to control the flow rate through the flowmeter under test. Helium is used to pressurize the cryogenic liquids allowing operation from 0.22 to 0.77 MPa (32 to 112 psia). During a calibration run, the dump valve on the weigh tank is closed and the change in mass of fluid accumulated in the weigh tank is determined from a calibrated load cell having a maximum range of 4450 N (1000 lb). The load cell is maintained near room temperature to avoid the need for temperature corrections. Four 113 kg (250 lb) brass weights were used to check the load cell calibration in situ. More complete descriptions of the NBS(B) facilities are given by Dean, Brennan and Mann [4] and Mann [5].

Table 3-8 presents an accuracy statement revised from a table presented by Dean et al [6]. The estimated error for mass flow rate measurements is estimated to be 0.18 percent with 0.12 percent from systematic errors and 0.06 percent from random errors. The random error is based on a statistical variation in the standard deviation of $\sigma = 0.02$ percent observed during repeated runs. The random error was taken as three times the standard deviation or $3\sigma = 0.06$. This accuracy was partially achieved by ability to calibrate the load cell in situ. The load cell accuracy is based on a percentage of full scale readout. One disadvantage to using load cells is that long calibration run times are necessary to achieve a high weighing accuracy at low flow rates.

3.6.4 Static Weigh Stand Using a Diverter Valve (Type G-4) - One method of eliminating the dynamic problems associated with the dynamic weigh stands has been to determine the mass of the weigh tank before and after a run under static conditions. This is accomplished by using a diverter valve such as shown in Figure 3-27. A flying start and finish is achieved by designing the diverter valve to switch the flow from the sump tank to the weigh tank in a fraction of a second.

This method has two bias errors:

1. A buoyancy error which can be corrected by an estimate using Equation (A-5)

2. A differential timing error associated with the increase and decay of the flow rate into the weigh tank at the start and end of a run. This error is minimized by adjusting the proximity switch on the diverter valve.

Since it takes a finite time for the actuation of the diverter valve, Hayward [11] shows in Figure 3-28 that there is an increase in the flow rate at the beginning and a decay at the end of a calibration run. Ideally it would be desirable if the diverter valve could be actuated in an infinitesimal time at the start and the end of a run. The flow variation with time would then follow the dotted line EFGH. The actual variation in flow rate with time is the curve ABCD. If the following relationship exists (see Figure 3-28):
where \( W_s = \text{steady state flow rate} \)
then the integrated deviations in flow rate at the start will be exactly compensated by the deviations at the end of the run.

Assuming the flow rate curve in Figure 3-28 is symmetrical, the clock is stopped slightly late. The net result of this timing error will be that the calculated flow rate will be somewhat less than the true flow rate. A means is generally provided for adjusting the "trip time" of the proximity switch on the diverter valve.

The longer the time from E to H in Figure 3-28, the less the influence of the timing errors on the accuracy. The proper setting of the timing switch is accomplished by performing several calibrations at identical flow rates and various run times as indicated by a precise and reliable flowmeter. If the flow rates vary with run time, the timing switch on the diverter valve is incorrectly set. The timing switch is then adjusted until the flow rates tabulated from a series of calibration runs are essentially independent of run time.

Hayward [11] estimates that the accuracy of a typical diverter system including systematic and random errors is within \( \pm 0.1 \) percent.

3.7 Fluid Density Measurement

Several commercial density meters were evaluated for use in the conversion of volumetric flow rate measurements to gravimetric flow rate equivalents and vice versa. One commercial density meter had an accuracy of about 0.01 percent from -30 to +200°C (-22 to 392°F). A density meter designed for low temperature operation and manufactured by the same company only had an accuracy of 0.1 percent in the range of -270 to +75°C (-454 to +167°F).

Extensive research has been conducted by NBS(B) on density meters suitable for density measurement of liquified natural gas (LNG). A Portable Reference Densimeter (PRD) and Density Reference System (DRS) have been developed at NBS(B) by Siegwarth and LaBrecque [12, 13, 14]. These low temperature density reference systems use Archimedes principle. The plummet is made from a pure silicon crystal having a density of 2.32900 \( \pm 0.00002 \) gm/cm\(^3\) at 25°C.

A cross-section of the PRD is shown in Figure 3-29. The density of pure methane was measured by Siegwarth et al [13] to be 422.63 kg/m\(^3\) within \( \pm 0.14 \) kg/m\(^3\) or \( \pm 0.033 \) percent at the normal boiling point of -161.52°C (-258.74°F). This high accuracy at low temperature primarily resulted from the reproducibility of the thermal expansion characteristics as well as the precise measurement of the expansion coefficient for a pure silicon crystal.

Several commercial density meters have been compared with the density measuring standards which were developed at NBS(B). This work was done by Siegwarth et al [15, 16]. An accuracy at the normal boiling point of methane was found to be \( \pm 0.1 \) percent for a typical commercial density meter.
3.7.1 Paar Density Meter - The density meter which appeared to have the highest potential accuracy was the Paar Density Meter manufactured by Anton Paar, Graz, Austria and distributed in the United States by the Mettler Instrument Co, Hightstown, NJ.

Figure 3-30 shows a cross-sectional view of the Paar Density Meter Model 602HT. The magnetic vane attached to the end of the U-tube is pulsed by an excitation coil and vane oscillation is sensed by a pickup coil. A phase-locked loop oscillator assures that the U-tube oscillates at its natural frequency. The glass U-tube is enclosed in two glass envelopes. The inner envelope is hermetically sealed and contains hydrogen at a pressure of approximately 50 kPa (0.5 bar or 7.25 psia). The outer glass jacket has ports which permit circulation of a liquid for stabilizing the temperature of the liquid contained in the U-tube. The hermetically sealed jacket around the U-tube gives complete assurance that condensation on the exterior of the tube will not affect the accuracy. The hydrogen within the jacket provides a high thermal conductivity medium for equilibrating the temperatures between the fluid sample and the fluid circulating through the outer jacket.

The period of oscillation of the U-tube can be determined from the following fundamental equation from vibration theory:

\[ t = 2\pi \sqrt{\frac{M_o + Vd}{C}} \]  
(3-12)

where \( t \) = Period of oscillation, sec

\( M_o \) = Equivalent mass of glass tube and magnetic vane, gm

\( d \) = Density of fluid in tube, gm/cm\(^3\)

\( V \) = Volume of capillary, cm\(^3\)

\( C \) = Constant

Solving Equation (3-12) for density and combining the constants gives the following equation:

\[ d = C_1(t^2 - C_2) \]  
(3-13)

where \( C_1 \) and \( C_2 \) are constants which are determined from calibration.

Table 3-10 lists various fluids which can be used to calibrate a density meter. The Paar density meter is normally calibrated with water and air at room temperature. Table 3-10 also lists several hydrocarbon fluids which may be used over a wide temperature range but the density of these hydrocarbon fluids is only known to \( \pm 1.0 \) kg/m\(^3\). This is equivalent to an accuracy of 0.13 percent. Higher accuracy could be attained by having the density cell and meter calibrated with the Portable Reference Densimeter (PRD) at NBS(B).
The calibration and accuracy of the density meter measurements is highly dependent on precise temperature measurements. The well for the temperature probe in the Paar Density Meter only permits entry of a sensor with a diameter of approximately 2 mm. This could limit the temperature measurement to use of a precision thermistor rather than a four terminal platinum resistance thermometer (i.e. 100 ohm RTD). A thin film platinum RTD which is small enough for insertion into a 2 mm diameter hole is currently available and may be suitable for this application.

The thermistor has the disadvantage that several must be used over a wide temperature range to achieve good resolution. This requires insertion of several thermistors when operating over a range of temperatures.

The constants $C_1$ and $C_2$ in Equation (3-13) must be determined for each temperature. Personal communication with the Mettler Instrument Co. indicates that these constants are reasonably linear with temperature.

The Paar density cell has a high inherent accuracy. If the full accuracy potential could be realized when using this density meter in situ during flow calibration testing, conversion between volumetric and gravimetric units could be accomplished with a relatively negligible effect on flow rate measurement accuracy.

The Paar density meter has the following advantages and disadvantages:

**Advantages:**

1. Highest resolution and potential accuracy of any densitometer investigated.

**Disadvantages:**

1. The small size of the temperature sensor "well" could require interchanging thermistors for precision temperature measurement for a wide range of temperature.

2. Operation over a wide temperature range requires calibration with a precision density meter such as the PRD at NBS(B) to achieve maximum accuracy potential.

3. The results of the testing would have to be post processed from the outputs of the Paar oscillator/timer and the temperature measurement. On site interpretation of the results could also be obtained by use of a dedicated microprocessor.

4. Glass cell may require careful handling.
3.7.2 Agar Density Meters - The Agar density meters were primarily developed for use in the petrochemical industry. These density meters are manufactured by Redland Automation Ltd, Kings Worthy, Hampshire, UK. The Agar Division maintains sales, calibration and service facilities in Houston, TX.

Figure 3-31 shows a pictorial view of the Agar Density Meter, Model FD820 and Table 3-11 gives a summary of the characteristics of this density meter. The Model FD820 is accurate to ± 0.1 kg/m³ or ± 0.016 percent of the upper limit of density range from -30 to +200°C (-22 to +392°F). The liquid sample flows through three parallel stainless steel tubes. The center tube vibrates as a beam with both ends fixed. Excitation and pickup coils are attached at the center of the two outer tubes.

The entire tube assembly is sealed with a cylindrical cover between the inlet and outlet flanges. Elastomeric O-ring seals are used to seal the cover. The enclosure is purged with dry nitrogen to insure that condensation will not cause erroneous readings at low temperature. A desiccant with a blue indicator can be viewed through a transparent port. If the seal has been disturbed and leakage occurs, the indicator turns pink indicating that the interior humidity is too high.

An Agar Model HC900 Density Converter is necessary to drive the density meter and interpret the output. The HC900 is actually a microprocessor with the ability to directly display density and compensate for temperature and pressure. The HC900 also has the ability to store a matrix of correction values when required. The HC900 also has an RS232 serial interface as well as alarm features.

Figure 3-32(a) shows a cross-sectional view of the Agar Model FD781B density cell and Table 3-12 gives a summary of the characteristics of this liquid density meter. The Model FD781B is not as accurate as the Model FD820 and has an entirely different mode of vibration. For a temperature range of -55 to 75°C, a span of 200 kg/m³ appears to be adequate for jet fuels. This would result in an accuracy of ± 0.7 kg/m³ or approximately ± 0.1 percent of the upper limit of the density range.

Figure 3-32(b) shows the approximate radial circumferential mode shape of the vibration of the thin walled center section of the spool. The spool is made from Ni-Span C for low temperature operation and cannot be used above +75°C. The center of the spool is directly excited by an excitation coil, and Ni-Span C becomes non-magnetic at the Curie temperature of +171°C (+340°F) in the annealed condition and +193°C (380°F) in the age-hardened condition.
Both the Model FD520 and the Model FD781B use the following equation for density:

\[ d = 2d_0 \left( \frac{t - t_o}{t_o} \right) \left[ 1 + \frac{K}{2} \frac{t - t_o}{t_o} \right] \]  

(3-14)

where 

- \( d_0 \) = Density at the calibration temperature, g/cm\(^3\)
- \( K \) = Nondimensional calibration constant
- \( t \) = Period of oscillation, \( \mu s \)
- \( t_o \) = Reference period of oscillation, \( \mu s \)
- \( t'_o = t_o + \alpha(T - T_{cal}) + \beta(P - P_{cal}) \)
- \( \alpha \) = Temperature coefficient, \( \mu s/°C \)
- \( \beta \) = Pressure coefficient, \( \mu s/kPa \)
- \( T \) = Temperature, °C
- \( P \) = Pressure, kPa

Subscripts:

- \( cal \) = Reference temperature and pressure during calibration

The low temp Agar Density Meter Model FD781B is not as accurate as the Model FD820 but both are durable instruments and both can use a common HC900 Density Converter for data readout or as a microprocessor interface.

3.8 Properties of Jet Fuels

This section was included in this report since some of the data in the literature describing the properties of jet fuels appear to be in error. Most of the data presented in Figures 3-33 through 3-39 is from NACA TN3276 by Barnett and Hibbard [17]. Although this report was published in 1956, it was the primary source for information published on jet fuels in the Data Book For Designers [18] by the EXXON Corporation in 1973.

Figures 3-33 through 3-35 present the variation of density versus temperature for jet fuels.

The data for the average kinematic viscosity of jet fuels were replotted in Figure 3-36 from Barnett and Hibbard [17] using coordinates developed by W. A. Wright [19]. These coordinates provide a "straightline" variation of kinematic viscosity versus temperature for jet fuels over a wide temperature range.
The distillation characteristic curves presented in Figures 3-37(a) through 3-37(b) give some insight as to the amount of fuel that will be vaporized at one atmosphere of pressure [101.3 kPa (14.696 psia)] and elevated temperatures during calibration. Figure 3-38 shows the variation of true vapor pressure versus temperature for various jet fuels. This data emphasizes the need to pressurize the fuel during flowmeter calibration at elevated temperature. At 130°C (266°F), JP-4 has a vapor pressure of approximately 213 kPa (31 psia) as shown in Figure 3-38. The other jet fuels have a lower vapor pressure but the flowmeter calibrations with all jet fuels should be conducted under pressurized conditions to avoid evaporation errors at elevated temperatures and particularly at temperatures of 130°C and above.

Figure 3-39 shows the variation of the molecular weight of jet fuel vapor versus the 10 percent-distillation temperature. This data is useful for estimating the buoyancy correction factor, $K_b$, for gravimetric systems using enclosed weigh tanks as shown in Figure 3-19. It appears difficult to estimate the density of air and jet fuel mixtures from data available in the literature. It is probably desirable to directly measure the density of the air-vapor mixture in the weigh tank to avoid uncertainties in estimating the density of the mixture when calculating the buoyancy correction factor from Equation (A-5) in Appendix A.

3.9 Accuracy Statement for a Calibration System Using the Flow-Thru Calibrator

Table 3-13 presents a summary of the estimated errors for a flowmeter calibration system using a Flow-Thru Calibrator. Table 3-13 covers a temperature range of -55 to 200°C (-67 to 392°F).

Table 3-13 assumes a 300 series stainless steel cylinder and Flow-Thru Calibrator piston assembly with an Invar extension rod. An all Invar assembly could virtually eliminate errors due to thermal expansion but the manufacturing costs for such an assembly may be excessive.

The only precision density meter that can cover the operating range is the Paar Density Meter Model 602HT. This density meter can be calibrated to a high accuracy with water at room temperature but will require calibration against a precision density meter such as the NBS(B), Portable Reference Densimeter at the temperature extremes.

Table 3-13 shows estimated absolute error in the mass flow rate calibration to be better than 0.1 percent at room temperature and better than 0.13 percent at extreme operating temperatures when using the Flow-Thru Calibrator in the flowmeter calibration system shown in Figure 3-7. It is possible that actual experience will produce a repeatability of 0.01 percent thus giving an absolute accuracy ranging from 0.05 to 0.1 percent.
Conclusions and Recommendations

The following conclusions resulted from a study of possible methods of verifying the absolute accuracy of mass flow rate meters being developed under the NASA HAFF program:

(1) There are no flow rate calibration facilities known at present that meet the calibration requirements of the NASA HAFF program. The only known planned facility that would have the potential accuracy is dedicated to the NASA Space Shuttle program. Any testing at this facility will use the Flow-Thru Calibrator as a volumetric standard but tests will only be conducted with referee water solutions at ambient temperatures.

(2) The best flow rate calibration facility at GE/AID (the COX 311H Flowmeter Calibrator) is inadequate to meet the ultimate calibration accuracy requirements for the flowmeters being developed under the NASA-HAFF development program. This facility could be improved, however, on a short term basis until a more precise facility is available. Some necessary improvements are possible without the luxury of coupling the COX 311H to a Flow-Thru Calibrator. Reproducibility of results is more important than absolute accuracy at the present stage of the development program.

(3) The dynamic weigh stands, which are used in flow rate calibration facilities at GE/AID, are inadequate to meet the accuracy requirements for the NASA-HAFF program for the following reasons: (a) calibration fluid properties may change significantly during a runs at high temperature, (b) the published repeatability of 0.1 percent is normally considered the random error to which other systematic errors must be added to obtain absolute accuracy, (c) it is necessary to estimate and apply several correction factors, which are not customarily used, to improve the absolute accuracy and (d) it is not presently possible to compare the accuracy of dynamic weigh stands to a standard which has a higher accuracy than the dynamic weigh stands at GE/AID.

(4) The best approach to acquiring a high accuracy flow rate calibration facility in the least time would be to purchase a Flow-Thru Calibrator and connect the Flow-Thru Calibrator in series with flowmeters under calibration on the COX 311H Flowmeter Calibrator at the Wilmington, MA facility of GE/AID. This arrangement would also require the use of a precision density meter, and viscometer as well as precision temperature measurements for adequate data correction and correlation. This approach would achieve two important results (a) provide an interim calibration facility and (b) ultimately expand the flow rate calibration facilities by determining the true accuracy capability of the COX 311H Flow Calibrator.
(5) The ultimate flow calibration facility, within the current state of the art, is to use a Flow-Thru Calibrator in a closed system similar to the system shown in Figure 3-7. This would be used with a Paar Density Meter, calibrated against a NBS(B) PRD, for determination of true mass flow rate.

The following recommendations are listed in the approximate order in which they can be accomplished:

(1) Incorporate corrections for buoyancy and timing errors into the procedures for interpretation of the data resulting from COX 311H flow calibration testing.

(2) Conduct an experimental investigation to determine why the COX 311H Flow Calibrator is apparently lacking in reproducibility under certain operating conditions.

(3) Make changes in the COX 311H flow calibration facility as required to improve the repeatability and use for Phase II testing.

(4) Plan a flow calibration facility using the Flow-Thru Calibrator in a closed calibration system similar to that shown in Figure 3-7.

(5) Procure a Flow-Thru Calibrator.

(6) Procure precision equipment for in situ density measurement.

(7) Procure an instrument of adequate accuracy for in situ viscosity measurement.

(8) Conduct final calibration tests using the Flow-Thru Calibrator in a closed-loop calibration facility.
### Nomenclature

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>Cross-sectional area, cm²</td>
</tr>
<tr>
<td>C</td>
<td>Constant</td>
</tr>
<tr>
<td>d</td>
<td>Density, gm/cm³</td>
</tr>
<tr>
<td>dₐ</td>
<td>Density of air</td>
</tr>
<tr>
<td>dₐₜ</td>
<td>Density of air surrounding brass weights</td>
</tr>
<tr>
<td>dₐₜ</td>
<td>Density of air surrounding weigh tank</td>
</tr>
<tr>
<td>eₜ</td>
<td>Relative timing error</td>
</tr>
<tr>
<td>f</td>
<td>Output frequency, Hz</td>
</tr>
<tr>
<td>h</td>
<td>Vertical height or head, cm</td>
</tr>
<tr>
<td>g</td>
<td>Local acceleration of gravity, cm/sec²</td>
</tr>
<tr>
<td>g₀</td>
<td>Standard acceleration of gravity = 980.665 cm/sec²</td>
</tr>
<tr>
<td>K</td>
<td>Calibration constant</td>
</tr>
<tr>
<td>Kₘ</td>
<td>Buoyancy correction factor</td>
</tr>
<tr>
<td>Kₑ</td>
<td>Correction factor for thermal expansion</td>
</tr>
<tr>
<td>Kₖ</td>
<td>Liquid jet mass correction factor</td>
</tr>
<tr>
<td>Kₗ</td>
<td>Flowmeter constant, (volume/pulse)</td>
</tr>
<tr>
<td>Kₜ</td>
<td>Timing correction factor</td>
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<tr>
<td>L</td>
<td>Length, cm</td>
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<tr>
<td>M</td>
<td>Mass, kg</td>
</tr>
<tr>
<td>m</td>
<td>Molecular Weight</td>
</tr>
<tr>
<td>Nₜ</td>
<td>Number of passing blades (flow meter pulses)</td>
</tr>
<tr>
<td>P</td>
<td>Pressure, kPa</td>
</tr>
<tr>
<td>Q</td>
<td>Volume, cm³</td>
</tr>
<tr>
<td>Rₒ</td>
<td>Lever arm ratio (overall)</td>
</tr>
</tbody>
</table>
Temperature, °C
Time, s
Corrected time, s
Start time (weigh beam), s
Tare time (weigh beam), s
Vertical fluid velocity component, cm/s
Vertical velocity of tare beam, cm/s
Mass rate of flow, kg/s
Mass rate of flow (actual)
Mass rate of flow (static balance)
Mean fluid velocity
Distance of tare weight from center of rotation
Vertical displacement of tare beam at weigh pan pivot
Temperature coefficient or coefficient of expansion
Pressure coefficient
Angle
Standard deviation
Kinematic viscosity, mm²/s (centistokes)
Subscripts:

A  Air
B  Brass
C  Calibrator
E  Equivalent
F  Fuel
L  Liquid
LK Linkage
M  Flowmeter
P  Flow prover or weigh pan
T  Weigh tank or tare weight
TB  Tare beam
V  Vapor or air-vapor mixture
W  Weigh tank
WB  Weigh beam
O  Initial or reference conditions
1  Start
2  Finish or end
3.12 References


18. Annon: Data Book for Designers, EXXON Corp, Marketing Tech Services, Houston, TX (1973)

### TABLE 3-1

CLASSIFICATION OF PATENTS RELATED TO FLUID FLOW CALIBRATION FROM 20 FEBRUARY 1962 THROUGH 12 MAY 1981

<table>
<thead>
<tr>
<th>Classification</th>
<th>Patents</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Ball Prover Technology</td>
<td></td>
</tr>
<tr>
<td>1.1 Unidirectional Ball Prover</td>
<td>21</td>
</tr>
<tr>
<td>1.2 Bidirectional Ball Prover</td>
<td>5</td>
</tr>
<tr>
<td>1.3 Method of Detecting Passage of a Ball in a Ball Prover</td>
<td>1</td>
</tr>
<tr>
<td>2. Double Chronometry Method for Comparing a Turbine Flowmeter with a Flow Prover or a Calibrated Standpipe</td>
<td>3</td>
</tr>
<tr>
<td>3. Calibration by Weighing Fluid Collected in a Tank</td>
<td>2</td>
</tr>
<tr>
<td>4. Flow-Thru Calibrator Using a Rigid Piston in a Straight Cylinder and Elastomeric Seals on Ends of Piston</td>
<td>7</td>
</tr>
<tr>
<td>5. Comparison of a Flowmeter with a Master Flowmeter</td>
<td>3</td>
</tr>
<tr>
<td>6. Transient Response Calibration of a Flowmeter</td>
<td>1</td>
</tr>
<tr>
<td>7. Flow Calibration Using a Calibrated Standpipe on a Tank of Known Volume Level Sensing of Varying Precision</td>
<td>8</td>
</tr>
<tr>
<td>8. Timing of a Fluid Wave Front Using Various Substances Injected into a Flow Stream and Detected Downstream</td>
<td>2</td>
</tr>
<tr>
<td>9. Fluid is Driven out of a Cylinder of Known Cross-sectional Area by Means of a Lead Screw which is driven by a Variable Speed Motor.</td>
<td>2</td>
</tr>
<tr>
<td>10. Diaphragm is used to Seal Corrosive Fluid from a Calibration Fluid During Calibration of Flowmeter Through which Corrosive Fluid is Flowing</td>
<td>1</td>
</tr>
<tr>
<td>11. Method of Checking the Electromagnetic Circuitry of a Turbine Flowmeter without Disconnecting or Removing the Blade Position Sensor.</td>
<td>1</td>
</tr>
</tbody>
</table>
TABLE 3-2
PRINCIPAL VOLUMETRIC METHODS
OF CALIBRATING LIQUID FLOWMETERS -
SUMMARY OF ADVANTAGES AND DISADVANTAGES

Type V-1: FLOW-THRU CALIBRATOR

Displacement of fluid with a rigid piston in a honed cylinder with flying start and finish (a separate pump is required to produce flow fluid through a Flow-Thru Calibrator).

Advantages:

(1) A direct and convenient method of calibrating volumetric flowmeters.

(2) Can be used to directly calibrate a mass flowmeter when used in conjunction with a precision densitometer.

(3) One or more fixed displacement volumes resulting from precise movements of the calibrator piston can be traced to NBS by the "water draw" method of collecting displaced water in vessel having a certified volume.

(4) Highest potential accuracy of any flow calibration system at the present time.

(5) Can be coupled to a dynamic weigh stand (see Type G-1 Table 3-2) for calibration and verification of dynamic timing errors when used with a precision densitometer.

(6) Can be used in a system which is totally sealed to prevent condensed water vapor causing contamination of the calibration fluid at low temperature and to prevent change in composition of a hydrocarbon fluid at high temperature due to boiloff of light ends.

(7) The only calibration system which has the capability of operating from -55 to 200°C with virtually no compromise.

(8) High operating pressures are possible. Total system can be pressurized at a pressure greater than the vapor pressure of the calibration fluid.

(9) A valve incorporated in the prover calibrator allows flowrate, temperature and pressure conditions can be stabilized to steady state prior to a calibration run.

(10) Can be portable if stationary ancillary equipment such as fluid storage, pump valves and filters are available for completing a flow system.

(11) Can be coupled into a fluid system containing an active flowmeter.
TABLE 3-2 (Continued)

Type V-1: FLOW-THRU CALIBRATOR (Continued)

(12) Since a proving run lasts only a few seconds at high flowrates there is little time for the steady state conditions to fluctuate and several prover runs can automatically be repeated within 30 to 60 seconds.

(13) Low fire hazard when used in a totally enclosed system.

Disadvantages:

(1) Internal area of cylinder (flow tube) of Flow-Thru Calibrator must be corrected for a difference in temperature between the operating temperature and the temperature at the time of a water draw test. (This is a simple correction).

(2) Stroke of calibrator may have to be corrected for change in temperature as the extension rod which attaches to the calibrator piston comes in contact with fluid in the cylinder. The extension rod experiences a transient change in temperature but the error is significantly minimized by making the extension rod of INVAR.

Type V-2: BALLISTIC FLOW CALIBRATOR

Fluid is displaced with a rigid piston in a honed cylinder - transient start and finish.

Advantages:

(1) Simple system for calibrating flowmeters with same accuracy potential as the Flow-Thru Calibrator (Type V-1) described above.

(2) No auxiliary pumps or valves are required since Calibrator piston is propelled by an attached air actuated piston.

(3) Potentially lower cost installation than the Flow-Thru Calibrator (Type V-1).

Disadvantages:

(1) Not very suitable for wide temperature range operation since entire system including the flowmeters and piping would have to be stabilized in a temperature controlled chamber prior to a proving run.

(2) Transient startup time would not allow sufficient time for certain types of flowmeters to reach steady state output prior to the proving run under high flowrate operating conditions. Generally used to calibrate turbine type flowmeters.
### Type V-3: PIPE PROVER

Fluid flow propels an elasomeric spheroid through a relatively long section of pipe—flying start and finish. Commonly uses two plunger operated microswitches actuated by the passing of a spherical displacer.

**Advantages:**

1. Can be coupled to a piping system having an active flowmeter to be calibrated.
2. Volumetric calibration traceable to NBS by a "water draw" calibration.
3. Flowrate, temperature and pressure conditions can be stabilized to steady state conditions prior to proving run.
4. Can be sealed for high temperature operating conditions and thus presents a low fire hazard and immunity from boil-off of volatile fractions.
5. Typical repeatability of 0.01 percent
6. An internationally recognized standard per API 2531 (American Petroleum Institute)

**Disadvantages**

1. Requires large amount of space. A typical 17.665 liter/sec (280 gpm) pipe flow prover is 12.2 m long x 0.91 m wide x 1.83 m high (40 ft x 3 ft x 6 ft) and weighs 1724 kg (3800 lb) filled with water.
2. Operating temperature range is limited to -18 to 82°C (0 to 180°F).
3. Long calibration run time. Run time is approximately 12 times as long as the Type V-1 flow prover. Since a long pipe length is required to achieve high volumetric accuracy.
TABLE 3-3
GRAVIMETRIC
PRINCIPAL METHODS OF
CALIBRATING LIQUID FLOWMETERS —
SUMMARY OF ADVANTAGES AND DISADVANTAGES

Type G-1: DYNAMIC WEIGH STAND (WEIGH BEAM BALANCE)

Dynamic weighing using weigh beam for balancing weigh tank with flying start and finish. Small weights can be used to determine change in mass of fluid in weigh tank.

Advantages:

(1) A direct and convenient method of calibrating mass flowmeters.

(2) Reasonable degree of sealing of hydrocarbon fluids against contamination from water condensation at low temperature and boiloff at high temperature.

(3) Vapor in weigh tank is transferred to sump tank during a run. Density of air-hydrocarbon vapor can thus be more accurately determined for buoyancy corrections.

(4) Flowrate, temperature and pressure conditions can reach steady state prior to a calibration run.

Disadvantages:

(1) Timing errors become significant at moderate and high flowrates since mass of weighing system changes during run. Data can be corrected for this error but is not usually done due to complexity of error determination.

(2) Sealing is not perfect — methanol must be added to hydrocarbon at very low temp and fluid density will change at high temperature due to boiloff of light fractions.

(3) Correction for density required if a volumetric flowmeter (i.e. turbine flowmeter) is being calibrated.

(4) Methanol must be added to hydrocarbon fuels for operation from 0 to -55°C to prevent icing of piping from condensed water vapor.
TABLE 3-3 (Continued)

Type G-2: DYNAMIC WEIGH STAND (WEIGHT SUBSTITUTION)

Dynamic weighing by direct weight substitution on weigh stand and with flying start and finish.

Advantages:
(1) No timing errors due to change since mass of weigh tank and contents are same at start and finish.

Disadvantages:
(1) Only suitable for small flowrates since weight removed from tank platform must equal weight of fluid accumulated.

Type G-3: DYNAMIC WEIGHING STAND (PRECISION LOAD CELL)

Dynamic weighing using load cell to determine changes in weight of weigh stand and with flying start and finish.

Advantages:
(1) Tightly sealed system can be used (method has been used for cryogenic flow calibration at very low temperatures).
(2) Dynamic errors are not reduced compared with Type G-1 since suspension of tank on a load cell produces a stiff spring-mass system, thus reducing total deflection during a run.

Disadvantages:
(1) Inert gas such as helium used to pressurize vapor spaces to control system pressure results in some inaccuracy in estimating density of helium-vapor mixture for buoyancy correction.
(2) Low weighing accuracy compared with beam balance method (typical accuracy is 0.1 percent of rated output) and accuracy is also reduced if nearly full range of load cell is not utilized.
(3) Flexible piping or bellows connections needed for complete sealing—such piping may produce weighing errors when pressurized.
(4) Weights for calibration must be sealed within enclosure and suspended during a run for maximum calibration accuracy.
TABLE 3-3 (Continued)

Type G-4: STATIC WEIGH STAND (DIVERTER VALVE)

Static weighing with flying start and finish. Diverter valve is used to divert flow between weigh tank and the sump tank at start and finish.

Advantages

(1) Static weighing eliminates dynamic timing errors associated with Type G1.

(2) Can be used at very high flowrates.

Disadvantages

(1) A difficult system to seal without interfering with the weighing mechanism. Hydrocarbon fuels are subject to change in composition properties and during extremely low and high temperature operation.

(2) Although weighing system is precise, errors occur due to flow diversion.
<table>
<thead>
<tr>
<th>Characteristic</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cylinder (Flow Tube) Length (Approx)</td>
<td>1.22 m (48 in.)</td>
</tr>
<tr>
<td>Metered displacement length</td>
<td>74.9 cm (29.5 in.)</td>
</tr>
<tr>
<td>Inside diameter (Nom)</td>
<td>17.9 m (7.060 in.)</td>
</tr>
<tr>
<td>Pneumatic/Hydraulic Actuator Piston</td>
<td>5.08 cm (2.00 in diam)</td>
</tr>
<tr>
<td>Actuator Rod Diameter</td>
<td>2.54 cm (1.00 in.)</td>
</tr>
<tr>
<td>Extension Rod Diameter</td>
<td>1.27 cm (0.50 in.)</td>
</tr>
<tr>
<td>Calibrator Displacement</td>
<td>18,927 cm³ (5.00 gal)</td>
</tr>
<tr>
<td>Minimum flow rate</td>
<td>15.77 cm³/s (.25 gpm)</td>
</tr>
<tr>
<td></td>
<td>0.0121 kg/s (96 lbm/hr)*</td>
</tr>
<tr>
<td>Maximum flow rate</td>
<td>15,770 cm³/s (250 gpm)</td>
</tr>
<tr>
<td></td>
<td>12.13 kg/s (96,250 lbm/hr)*</td>
</tr>
<tr>
<td>Standard flow tube (cylinder)</td>
<td>Carbon steel with electroless nickel plating</td>
</tr>
<tr>
<td>Optional flow tube</td>
<td>304 stainless steel with chrome plating</td>
</tr>
<tr>
<td>Pressure drop (Piston only)</td>
<td>0.25 to .75 kPa (0.036 to 0.108 psid) diff</td>
</tr>
<tr>
<td>Pressure Drop (Between inlet and outlet flanges at max. flow)</td>
<td>69 kPa (10 psid)</td>
</tr>
<tr>
<td>Calibrator Piston Seals</td>
<td>Spring loaded TFE U-cup (OMNI-SEAL®)</td>
</tr>
<tr>
<td>Calibrator Piston (Riders) or Glide Rings bearing</td>
<td>RULON® (glass filled) (TFE)</td>
</tr>
<tr>
<td>Operating Pressures (Maximum)</td>
<td>9.9 MPa (1440 psig)</td>
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<tr>
<td>Operating Temperatures</td>
<td>-29 to 93°C (-20 to +200°F)</td>
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<tr>
<td>Standard</td>
<td>-129 to 204°C (-200 to +400°F)</td>
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<tr>
<td>Optional</td>
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<tr>
<td>Repeatability</td>
<td>0.02 percent</td>
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</tbody>
</table>

*Based on fluid density = 0.77 gm/cm³
<table>
<thead>
<tr>
<th>VOLUMETRIC FLOW RATE cm$^3$/s (gpm)</th>
<th>MASS FLOWRATE kg/s (lbm/hr)</th>
<th>3788 cm$^3$ (1 gal)</th>
<th>7571 cm$^3$ (2 gal)</th>
<th>18,927 cm$^3$ (5 gal)</th>
</tr>
</thead>
<tbody>
<tr>
<td>15.8 (0.25)</td>
<td>0.012 (96)</td>
<td>(4 min)</td>
<td>(8 min)</td>
<td>(20.0 min)</td>
</tr>
<tr>
<td>63.1 (1.00)</td>
<td>0.048 (385)</td>
<td>60 sec</td>
<td>(2 min)</td>
<td>(5.0 min)</td>
</tr>
<tr>
<td>126.2 (2)</td>
<td>0.097 (770)</td>
<td>30</td>
<td>160 sec.</td>
<td>(2.5 min)</td>
</tr>
<tr>
<td>315.5 (5)</td>
<td>0.243 (1925)</td>
<td>12</td>
<td>24</td>
<td>60 sec</td>
</tr>
<tr>
<td>631 (10)</td>
<td>0.485 (3850)</td>
<td>6</td>
<td>12</td>
<td>30</td>
</tr>
<tr>
<td>1,262 (20)</td>
<td>0.97 (7700)</td>
<td>3</td>
<td>6</td>
<td>15</td>
</tr>
<tr>
<td>3,155 (50)</td>
<td>2.245 (19250)</td>
<td>1.2</td>
<td>2.4</td>
<td>6</td>
</tr>
<tr>
<td>6,309 (100)</td>
<td>4.85 (38500)</td>
<td>1.2</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>12,618 (200)</td>
<td>9.70 (77000)</td>
<td></td>
<td></td>
<td>1.5</td>
</tr>
<tr>
<td>15,772 (250)</td>
<td>12.13 (96250)</td>
<td></td>
<td></td>
<td>1.2</td>
</tr>
</tbody>
</table>

*Based on a fluid density = 0.77 gm/cm$^3$
<table>
<thead>
<tr>
<th>Characteristic</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Overall Dimensions</td>
<td>1.83 x 0.91 x 12 m (H x W x L) (6 x 3 x 40 ft)</td>
</tr>
<tr>
<td>Volumetric Flowrate (Max)</td>
<td>18 x 10^{-3} m³/s (280 gpm)</td>
</tr>
<tr>
<td>Operating Temperature Range</td>
<td>-18 to +82°C (0 to +180°F)</td>
</tr>
<tr>
<td>Pipe Size (6 in. Sch 40)</td>
<td>16.83 x 15.40 cm (6.625 x 6.065 in.)</td>
</tr>
<tr>
<td>Pipe Displacement Length</td>
<td>18.3 m (60 ft)</td>
</tr>
<tr>
<td>Volumetric Displacement</td>
<td>0.341 m³ (90 gal)</td>
</tr>
<tr>
<td>Run Time for a Flowrate of 63 x 10^{-6} m³/s</td>
<td>5400 (90 min)</td>
</tr>
<tr>
<td>Elastomeric sphere material</td>
<td>Buna-N (Nitrile) or Polyurethane Rubber</td>
</tr>
<tr>
<td>Dimensions of Spherical Piston</td>
<td>15.2 cm OD x 5.1 cm wall (6.0 in. OD x 2 in. wall)</td>
</tr>
</tbody>
</table>
### TABLE 3-7A

**COX 311H FLOWMETER CALIBRATOR**

**DESIGN AND ACCURACY CHARACTERISTICS**

<table>
<thead>
<tr>
<th>CAPACITY AND RANGES</th>
</tr>
</thead>
</table>
| **Flow Range**       | 0.063 to 18.9 kg/s  
                       | (500 to 150,000 lb/hr) |
| **Temperature Range** | -53.9 to 176.7°C  
                        | (-65 to +350°F) |
| **Back Pressure Range** | 101 to 515 kPa  
                          | (14.7 to 74.7 psia) |
| **Weigh Tank Capacity** | 0.946 m³ (250 gal) |
| **Weigh Tank Capacity (Overflow)** | 0.798 m³ (211 gal) |
| **Supply Tank Capacity** | 1.5142 m³ (400 gal) |
| **Filtration**       | 25 micron |
| **Low Flow Pump**    | 1.89 x 10⁻³ m³/s at 43 m |
|                      | (30 gpm at 140 ft) |
| **High Flow Pump**   | 18.9 x 10⁻³ m³/s at 55 m |
|                      | (300 gpm at 180 ft) |
| **Flow Calibration Line** | 4.0 in. Pipe |
| **Accuracy**         | ± 0.2 percent |
| **Repeatability**    | ± 0.01 percent |
| **Test Weights**     | ± 0.03 percent |
| **Scale Beam Ratio**  | ± 0.0002 percent |
| **Scale Beam Sensitivity (Est)** | ± 0.001 sec |
| **Timer**            | ± 0.6°C (± 1.0°F) |
| **Temperature Control** | 4:1 (approx) |
| **Weigh Beam Ratio**  | 12.5:1 (approx) |
| **Scale Beam Ratio**  | 50:1 ± 0.03 percent |
| **Weigh Tank Weight (Est)** | 166.9 kg (368 lb) |

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### TABLE 3-7B

**COX 305T FLOWMETER CALIBRATOR**

**DESIGN AND ACCURACY CHARACTERISTICS**

#### CAPACITY AND OPERATING RANGES

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Specification</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Flow Range</strong></td>
<td>0.189 to 113 kg/s (25 to 15,000 lb/hr)</td>
</tr>
<tr>
<td><strong>Temperature Range</strong></td>
<td>-53.9 to 176.7°C (-65 to +350°F)</td>
</tr>
<tr>
<td><strong>Back Pressure Range</strong></td>
<td>101 to 515 kPa (14.7 to 74.7 psia)</td>
</tr>
<tr>
<td><strong>Weigh Tank Capacity (Usable)</strong></td>
<td>0.114 m³ (30 gal)</td>
</tr>
<tr>
<td><strong>Supply Tank Capacity</strong></td>
<td>0.170 m³ (45 gal)</td>
</tr>
<tr>
<td><strong>Filtration</strong></td>
<td>10 microns</td>
</tr>
<tr>
<td><strong>Circulating Pump</strong></td>
<td>3.785 x 10⁻³ m³/s at 49 m (60 gpm at 160 ft)</td>
</tr>
</tbody>
</table>

#### Accuracy

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Specification</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Repeatability</strong></td>
<td>± 0.2 percent</td>
</tr>
<tr>
<td><strong>Test Weights</strong></td>
<td>± 0.01 percent</td>
</tr>
<tr>
<td><strong>Scale Beam Ratio</strong></td>
<td>± 0.03 percent</td>
</tr>
<tr>
<td><strong>Scale Beam Sensitivity (Est)</strong></td>
<td>± 0.0002 percent</td>
</tr>
<tr>
<td><strong>Timer</strong></td>
<td>± 0.001 sec</td>
</tr>
<tr>
<td><strong>Temperature Control</strong></td>
<td>± 0.6°C (+ 1.0°F)</td>
</tr>
</tbody>
</table>

#### Weighing Mechanism

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Specification</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Weigh Beam Ratio</strong></td>
<td>5:1 ± 0.03 percent</td>
</tr>
</tbody>
</table>
### A. MASS FLOWRATE MEASUREMENTS

<table>
<thead>
<tr>
<th>Source of Error</th>
<th>Estimated From</th>
<th>Relative Error (Percent)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.0 Calibration weights</td>
<td>Calibration</td>
<td>0.01</td>
</tr>
<tr>
<td>2.0 Load Cell</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2.1 Non-linearity</td>
<td>Manufacturer &amp; Measurement</td>
<td>0.05</td>
</tr>
<tr>
<td>2.2 Calibration</td>
<td>Measurement</td>
<td>0.02</td>
</tr>
<tr>
<td>2.3 Temperature</td>
<td>(Operates at design temp.)</td>
<td>0.00</td>
</tr>
<tr>
<td>3.0 Buoyancy</td>
<td>Labeled</td>
<td></td>
</tr>
<tr>
<td>3.1 Helium-Nitrogen Vapor Density</td>
<td>Est (Density error)</td>
<td>0.10</td>
</tr>
<tr>
<td>3.2 Diffuser suspended in liquid</td>
<td>Est (Density error)</td>
<td>0.03</td>
</tr>
<tr>
<td>4.0 Reaction Forces</td>
<td>Est from dynamics</td>
<td>0.01</td>
</tr>
<tr>
<td>5.0 Impact Forces</td>
<td>Designed to be zero</td>
<td>0.00</td>
</tr>
<tr>
<td>6.0 Systematic Error</td>
<td>Quadrature*</td>
<td>0.12</td>
</tr>
<tr>
<td>7.0 Random Error (3σ)</td>
<td>Estimated</td>
<td>0.06</td>
</tr>
<tr>
<td>8.0 Estimated Error of Mass Flowrate</td>
<td>Sum of Estimates</td>
<td>0.18</td>
</tr>
</tbody>
</table>

### B. ESTIMATES OF DENSITY

<table>
<thead>
<tr>
<th>Source of Error</th>
<th>Estimated From</th>
<th>Relative Error (Percent)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.0 Equation of State for Liquid Nitrogen</td>
<td>Strobridge (1962)</td>
<td>0.39</td>
</tr>
<tr>
<td>2.0 Temperature Measurement</td>
<td>Calibration to ± 0.05°K</td>
<td>0.03</td>
</tr>
<tr>
<td>3.0 Thermometry Circuit</td>
<td>Calibration</td>
<td>0.01</td>
</tr>
<tr>
<td>4.0 Pressure Effects</td>
<td>Calibration</td>
<td>0.00</td>
</tr>
<tr>
<td>5.0 Systematic Error</td>
<td>Quadrature*</td>
<td>0.39</td>
</tr>
<tr>
<td>6.0 Summation with Item A.6.0</td>
<td>Quadrature*</td>
<td>0.41</td>
</tr>
<tr>
<td>7.0 Random Error (3σ)</td>
<td>Estimated</td>
<td>0.06</td>
</tr>
<tr>
<td>8.0 Estimated Error of Volumetric Flow</td>
<td>Sum of Estimates</td>
<td>0.47</td>
</tr>
</tbody>
</table>

* Square root of sum of the squares of systematic errors.
### TABLE 3-9

**CHARACTERISTICS OF THE PAAR DENSITY METER**

| Manufacturer: | Anton Paar K.G.          |
|               | Graz, Austria            |
| US Distributor: | Mettler Instrument Co.   |
|               | Hightstown, NJ           |

**Type:** Vibrating Glass U-Tube

| Glass U-Tube: | Duran (Borosilicate) Glass |
|              | 20 mm OD x 2 mm ID       |
| Tube Size    | 7.4 cm                   |
| Internal Volume | 0.7 cm³                  |
| Tube Length  | 22 cm                    |

| Glass Thermistor Well: | 2.3 mm ID x 100 mm long |
| Thermistor Size (max) | 2 mm diameter           |
| Density Cell Model    | DMA602HT                 |

- **Temperature Range:** -160 to +150°C (-256 to 302°F)
- **Pressure Range:** 0 to 100 kPa (0 to 145 psia)
- **Range:** ±0.5 gm/cm³ (0 to 145 psia)
- **Accuracy (Note A):** ±0.0001 gm/cm³
- **Resolution:** ±0.000001 gm/cm³

**Physical Properties of Duran Glass:**

- **Density:** 2.23 gm/cm³
- **Modulus of Elasticity:** 67.8 GPa (9.8 × 10⁶ psia)
- **Poisson's Ratio at 20°C:** 0.22

- **Tensile Strength (Safety Factor = 5):**
  - Fire-bright Surface: 7.8 MPa (11,400 psia)
  - Cut Surface: 3.9 MPa (5,700 psia)
- **Coefficient of Expansion (20°C to 300°C):** 3.2 × 10⁻⁶/°C
- **Resistance to sudden change in temperature (DIN 52325):** 250°C (482°F)
- **Thermal Conductivity:** 1.168 W/m-°K
- **Specific Heat at 20°C:** 0.18 cal/gm°K
- **Glass Transition Temp:** 530°C (986°F)

**NOTES:**
A. Higher accuracies obtainable depending on range and environmental conditions.
### TABLE 3-10

**SUMMARY OF FLUIDS SUITABLE FOR DENSITY METER CALIBRATION [A]**

<table>
<thead>
<tr>
<th>Fluid</th>
<th>Temp. Range</th>
<th>Resolution gm/cm³</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water</td>
<td>0 to 40°C (32 to 104°F)</td>
<td>1 x 10⁻⁷ [B]</td>
</tr>
<tr>
<td>Hexane, C₆H₁₄</td>
<td>-100 to +60°C (-148 to 140°F)</td>
<td>1 x 10⁻³ [C]</td>
</tr>
<tr>
<td>Heptane, C₇H₁₆</td>
<td>-90 to +70°C (-130 to 158°F)</td>
<td>1 x 10⁻³ [C]</td>
</tr>
<tr>
<td>Toluene, C₇H₈</td>
<td>+14 to +110°C (57 to 230°F)</td>
<td>1 x 10⁻³ [C]</td>
</tr>
<tr>
<td>Chlorobenzene C₆H₅Cl</td>
<td>+13 to +132°C (55 to 270°F)</td>
<td>1 x 10⁻³ [C]</td>
</tr>
<tr>
<td>Chinoline, C₅H₇N</td>
<td>0 to +150°C (32 to 302°F)</td>
<td>1 x 10⁻³ [C]</td>
</tr>
<tr>
<td>Aniline, C₆H₇</td>
<td>+20 to +150°C (68 to 302°F)</td>
<td>1 x 10⁻³ [C]</td>
</tr>
<tr>
<td>Nonane, C₉H₂₀</td>
<td>Proposed low temperature calibrated fluid</td>
<td></td>
</tr>
<tr>
<td>Air, N₂, He, Ne, Ar</td>
<td>-100 to +150°C (-148 to 302°F)</td>
<td>1 x 10⁻⁷ [D]</td>
</tr>
</tbody>
</table>

**NOTES:**

[A] Data from Density Seminar, Dr. H. Heimel, Institute for Measuring Technique, Research Center, Graz, Austria (Sept. 1981)

[B] Water is the only officially authorized substance for calibration of the Paar density meter.


TABLE 3-11
CHARACTERISTICS OF THE
MODEL FD820
AGAR DENSITY METER (HIGH TEMP)

**Operating Characteristics**

<table>
<thead>
<tr>
<th>Characteristic</th>
<th>Specification</th>
</tr>
</thead>
<tbody>
<tr>
<td>Temperature Range</td>
<td>-30 to +200°C (-22 to +392°F)</td>
</tr>
<tr>
<td>Pressure (Max):</td>
<td>7 MPa (1000 psi)</td>
</tr>
<tr>
<td>Pressure Loss:</td>
<td>Equivalent to 1.4 m (4.5 ft) of 19 mm (0.75 in.) smooth bore pipe with two 180° bends</td>
</tr>
<tr>
<td>Temperature Sensor</td>
<td></td>
</tr>
<tr>
<td>Type: Platinum Resistance thermometer</td>
<td></td>
</tr>
<tr>
<td>Resistance:</td>
<td>100 ohm at 0°C</td>
</tr>
<tr>
<td>Temperature Range:</td>
<td>-30 to +550°C (-22 to 1022°F)</td>
</tr>
</tbody>
</table>

**Construction Materials**

<table>
<thead>
<tr>
<th>Component</th>
<th>Material</th>
</tr>
</thead>
<tbody>
<tr>
<td>Body and Flanges</td>
<td>AISI 321</td>
</tr>
<tr>
<td>Bellows</td>
<td>AISI 316</td>
</tr>
<tr>
<td>Castings</td>
<td>ANC 3B Stn Stl</td>
</tr>
<tr>
<td>Seals</td>
<td>Viton(Std) or Kalrez(Special)</td>
</tr>
</tbody>
</table>

**Performance**

<table>
<thead>
<tr>
<th>Characteristic</th>
<th>Specification</th>
</tr>
</thead>
<tbody>
<tr>
<td>Operating Span (min):</td>
<td>0.02 gm/cm² (1.3 lb/ft³)</td>
</tr>
<tr>
<td>Accuracy (within):</td>
<td>± 0.0001 gm/cm² (0.006 lb/ft³)</td>
</tr>
<tr>
<td>Repeatability (within):</td>
<td>± 0.00003 gm/cm² (0.002 lb/ft³)</td>
</tr>
<tr>
<td>Hysteresis (within):</td>
<td>± 0.00003 gm/cm² (0.002 lb/ft³)</td>
</tr>
<tr>
<td>Drift (less than):</td>
<td>0.12 percent/year</td>
</tr>
<tr>
<td>Time constant:</td>
<td>Milliseconds</td>
</tr>
<tr>
<td>Temp Coeff:</td>
<td>( \leq 0.0005 ) (1 + d/1000) gm/cm²/°C where d = density, gm/cm²</td>
</tr>
<tr>
<td>Press Coeff (Typ)</td>
<td>0.004 gm/cm²/MPa (0.0018 lb/ft³/psi)</td>
</tr>
<tr>
<td>Viscosity Effect:</td>
<td>(&lt; 0.001) gm/cm³ error at 15 Pa-s with zero flow</td>
</tr>
</tbody>
</table>
TABLE 3-12
CHARACTERISTICS OF THE
MODEL FD781B
AGAR DENSITY METER (LOW TEMP)

Operating Characteristics

Temperature Range: \(-270 \text{ to } +75^°C \text{ (-454 to } +167^°F)\)
Press (Max): \(70 \text{ MPa (10,000 psi)}\)
Press Loss: Equivalent to 25 cm (10 in.) length of 19 mm (0.75 in.) smooth bore pipe

Temperature Sensor

Type: Platinum Resistance Thermometer
Resistance: 100 ohm at 0°C (Special four term)
Temp Range: \(-200 \text{ to } +75^°C \text{ (-330 to } +167^°F)\)

Construction Materials

Body: AISI 316
Spool: Ni-Span C

Performance

Operating Span (max): \(2.0 \text{ gm/cm}^3 \text{ (125 lb/ft}^3)\)
Minimum Span: \(0.01 \text{ gm/cm}^3 \text{ (0.6 lb/ft}^3)\)
Accuracy (within): \(\pm (0.001 \times \text{Range } + 0.0005) \text{ gm/cm}^3\)
Repeatability (within): \(\pm 0.01 \text{ percent of range}\)
Hysteresis (within): \(\pm 0.01 \text{ percent of range}\)
Drift (less than): 0.12 percent /year
Time Constant: Milliseconds

Temperature Coeff: \(\leq (7 \times 10^{-6} + 4 \times 10^{-8}d) \text{ gm/cm}^3/°C\)
where \(d = \text{density, gm/cm}^3\)

or \(0.0002 (1 + d/10) \text{ lb/ft}^3/°F\)
where \(d = \text{density, lb/ft}^3\)

Pressure Coeff: Not detectable to 70 MPa

Viscosity: Compensated to 0.02 Pa-s
<table>
<thead>
<tr>
<th>SYSTEMATIC ERRORS</th>
<th>TEMPERATURE, °C (°F)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>-55 (-67) 20 (68) 130 (266) 200 (392)</td>
</tr>
<tr>
<td>Flow Prover Volume</td>
<td>0.03 0.03 0.03 0.03</td>
</tr>
<tr>
<td>NBS Volumetric Certification</td>
<td>0.01 0.01 0.01 0.01</td>
</tr>
<tr>
<td>Displacement</td>
<td></td>
</tr>
<tr>
<td>Volume Corr [a]</td>
<td>0.0155 0 0.025 0.042</td>
</tr>
<tr>
<td>Temperature [b]</td>
<td>0.007 0.007 0.007 0.007</td>
</tr>
<tr>
<td>Density</td>
<td>0.05[c] 0.0015[d] 0.05[c] 0.05[c]</td>
</tr>
<tr>
<td>Systematic Errors [e]</td>
<td>0.062 0.032 0.065 0.073</td>
</tr>
<tr>
<td>RANDOM ERRORS</td>
<td></td>
</tr>
<tr>
<td>Position Sensor Error [f]</td>
<td>0.002 0.002 0.002 0.002</td>
</tr>
<tr>
<td>Timing Error [g]</td>
<td>0.0003 0.0003 0.0003 0.0003</td>
</tr>
<tr>
<td>Run Reproducibility (2σ)[h]</td>
<td>0.06 0.06 0.06 0.06</td>
</tr>
<tr>
<td>Random Errors [e]</td>
<td>0.06 0.06 0.06 0.06</td>
</tr>
</tbody>
</table>

Uncertainty of Flowrate Calibration [i] | 0.122 0.092 0.125 0.133 |

NOTES:

[a] 300 series Stn Stl Cylinder with Invar Ext Rod [Figure 3- 10]
[b] ± 0.05°C Uncertainty in Temperature (Flow Prover to Flowmeter and Densitometer to Flowmeter)
[c] Paar Densimeter calibrated with PRD, NBS(B)
[d] Paar Densimeter calibrated with Distilled Water
[e] Quadrature Summation [Square Root of Sum of Squares]
[f] ± 0.0076 mm (± 0.0003 in.) per Position Sensor in 75 cm (29.5 in.)
[g] ± 0.00001 sec per Position Sensor in 6 sec at 146 kg/s (19250 lb/hr)
[h] Estimated
[i] Algebraic sum of Systematic and Random Errors
Section 3.14

FIGURES
FIGURE 3-2 FLOW-THRU CALIBRATOR - STANDBY MODE

FIGURE 3-3 FLOW-THRU CALIBRATOR - START OF RUN

FIGURE 3-4 FLOW-THRU CALIBRATOR - END OF RUN
\[ V_p = \text{Calibrated volume of the prover flow tube between detectors} \]
\[ t_p = \text{Time required to displace volume } V_p \]
\[ N_b = \text{Whole flowmeter pulses counted during Time } t_M \]
\[ t_M = \text{Time required to accumulate whole flowmeter pulses } N_b \]

**Figure 3-5** Schematic Diagram Illustrating Double Chronometry
FIGURE 3-7  SCHEMATIC DIAGRAM OF FLOW CALIBRATION SYSTEM USING A FLOW-THRU CALIBRATOR AND FLOW REGULATING VALVES
FIGURE 3-8  THERMAL EXPANSION COEFFICIENTS FOR VARIOUS METALS
FIGURE 3-9 DISPLACEMENT VOLUME CORRECTION FOR A FLOW-THRU CALIBRATOR
**Figure 3-10** Estimated error in displacement volume correction for a flow-thru calibrator.
FIGURE 3-12 BIDIRECTIONAL PIPE PROVER

(Reproduced from Hayward [11] by permission from Measurement and Control)
FIGURE 3-13 RIGID PISTON DESIGN FOR A PIPE PROVER

(Reproduced from Hayward [11] by permission from Measurement and Control)
FIGURE 3-14  PRINCIPLE OF CALIBRATION OF A FLOWMETER USING A VOLUMETRIC TANK STANDARD IN THE STANDING-START-AND-FINISH MODE

FIGURE 3-15  DESIGN OF VOLUMETRIC TANK STANDARD USED AT NEL GLASGOW, SCOTLAND, UK

(The above illustrations were reproduced from Hayward [11] by permission from Measurement and Control)
FIGURE 3-17 PICTORIAL VIEW OF COX311H FLOW CALIBRATOR SHOWING FLUID FLOW COMPONENTS
**Figure 3-19**: Estimated Buoyancy Correction Factors for Jet Fuels in a Weigh Tank Calibration System

- $m =$ MOLECULAR WEIGHT OF FUEL VAPOR
- $P_A =$ 101.32 kPa (14.696 psid)

Temperature, °F

-80  0  100  200  300  400

Buoyancy Correction Factor, KB

-50  0  50  100  150  200

Temperature, °C

-50  0  50  100  150  200

*(Image of graph showing estimated buoyancy correction factors for jet fuels across different temperatures and molecular weights.)*

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\[ t_C \text{ (corrected)} = t_A \text{ (actual)} + (tT_1 - tS_1) - (tT_2 - tS_2) \]

Values Shown are Typical for a COX 311H Calibration
[Run at 2.52 kg/s \( (20,000 \text{ lb/hr}) \)]

**FIGURE 3-20** DIAGRAM ILLUSTRATING TIMING DEVIATIONS WHICH OCCUR IN A DYNAMIC WEIGH STAND (TYPE G-1)
FIGURE 3-21 : DIAGRAM OF FLUID JET ENTERING WEIGH TANK
FIGURE 3-23  ESTIMATED TIMING CORRECTIONS FOR COX 305T FLOWMETER CALIBRATOR
FIGURE 3-24 DYNAMIC WEIGH STAND USING WEIGHT SUBSTITUTION (TYPE G-2)

FIGURE 3-25 DYNAMIC WEIGH STAND USING A PRECISION LOAD CELL (TYPE G-3)
FIGURE 3-26 SCHEMATIC DIAGRAM OF CRYOGENIC FLOW RESEARCH FACILITY AT NBS(B), BOULDER, COLORADO

(From Brennan et al [10] )
FIGURE 3-27 GRAVIMETRIC FLOWMETER CALIBRATION SYSTEM USING A WEIGH TANK AND FLOW DIVERTER - NEL 50 TONNE SYSTEM (TYPE G-4)

FIGURE 3-28 VARIATION OF FLOW RATE ENTERING A WEIGH TANK WITH A FLYING START AND FINISH DIVERTER SYSTEM (TYPE G-4)

(The above illustrations were reproduced from Hayward [1] by permission from Measurement and Control)
PORTABLE REFERENCE DENSIMETER

Figure 3-29
*NOTE: Center Tube Vibrates as a Beam in the Horizontal Plane

FIGURE 3-31 PICTORIAL VIEW OF AGAR MODEL FD820 DENSITY CELL (HIGH TEMPERATURE) WITH OUTER SEAL COVER REMOVED

Temperature Range: -30 to +200°C (-22 to +392°F)
Figure 3-32 Agar Model 781-B Density Cell

(LOW TEMPERATURE)
Temperature Range: -270 to +75°C (-454 to +167°F)
FIGURE 3-33 DENSITY OF JP-4 FUEL
FIGURE 3-34: DENSITY OF JET A, A-1 FUEL
FIGURE 3-35: DENSITY OF JP-5 FUEL
FIGURE 3-36  AVERAGE KINEMATIC VISCOSITY VERSUS TEMPERATURE FOR JET FUELS
FIGURE 3-37(a) DISTILLATION CHARACTERISTICS PER ASTM D-86 FOR JP-4, JET B FUEL

(DATA FROM NACA TN3276 [17])
FIGURE 3-37(b)  DISTILLATION CHARACTERISTICS PER ASTM D-86 FOR JET A, A-1 FUEL
(DATA FROM NACA TN3276 [17])
FIGURE 3-37(c) DISTILLATION CHARACTERISTICS PER ASTM D-86 FOR JP-5 FUEL.
(DATA FROM NACA TN 3276 [17])
FIGURE 3-38 TRUE VAPOR PRESSURE FOR JET FUELS
(RANGE OF 10% DISTILLATION TEMPERATURE SHOWN FOR EACH FUEL TYPE)

TEMPERATURE, °F

MOLECULAR WEIGHT OF FUEL VAPORS, m

TEMPERATURE, °C

FIGURE 3-39  MOLECULAR WEIGHT OF FUEL VAPOR FROM SLIGHTLY VAPORIZED FUEL VS. 10% DISTILLATION TEMPERATURE
4.0 VORTEX FLOWMETER

This section describes the experimental and analytical investigation performed on the vortex flowmeter concept under Tasks 2 and 4 of Phase II of NASA contract No. NAS3-22139 to develop a High Accuracy Fuel Flowmeter (HAFF).

4.1 Introduction

The best approach to gain a better understanding of the capabilities and limitations of this technology is to pursue vigorous testing of various models. Comprehensive analysis of the fluid dynamics of precessing vortices will have to wait for the development of three-dimensional, non-axisymmetric time-marching computer techniques for geometries having no core, which is beyond the scope for this program with respect to time and content. Accordingly, a test approach described in section 4.2 has been designed with the intent of learning the most about vortex generation and sensing by building and testing several models, and then evaluating overall performance, especially repeatability of the best candidate model.

The first task in testing is to determine the contour of the flow passage and the geometry of the swirl generator which together produce strong and regular vortex precession over a 65:1 volumetric flow range. Several concepts are presented in the literature and patents that were reviewed in Phase I and serve as a starting point for design of the models. Each model, made of clear Plexiglass (acrylic), will provide visual evidence of the vortex which can be "stopped" by synchronized strobe flash and enhanced with injections of dyed fuel or air bubbles in the central core. Dynamic pressure sensors are to be placed at the inside diameter at various axial and radial positions to help determine vortex physics and evaluate model performance.

After testing several models, a "best" candidate is to be selected for comprehensive evaluation of the fluid dynamics of the vortex. Complete charting of fluid velocity profiles over selected radial and axial positions is to be performed using hot film or hot wire anemometer probes and using high speed movies of fuel with aluminum particles in suspension. The evaluations are to be made at several flow ranges including the minimum and maximum. Anemometer readings will provide data on flow speed and oscillation frequency and strength but will not provide data on flow direction. Only high speed movies can provide indication of flow direction in such a complex flow pattern. This information will then be analyzed with two objectives in mind: (1) description of the fluid dynamics in quantitative terms and (2) design of an optimum vortex sensor.

The next step will be to build and test several sensor designs with information from the preceding work. The sensor that generates the best signal over the flow range, as judged by signal-to-noise ratio and regularity of sensed vortex frequency, will then be subjected to a series of tests that are intended to provide data on linearity, repeatability and stability.
4.2 Experimental and Analytical Investigation Plan Formulations

To evaluate the design concept of the vortex flowmeter and its potential in meeting NASA HAFF requirements, five major test groups were planned to be conducted in Task IV. They are:

(1) Vortex Generator Study
(2) Fluid Dynamics Study
(3) Sensor Evaluation
(4) Linearity and Repeatability Measurement
(5) Time Response Evaluation

4.2.1 Vortex Generation

Problem - Most of the vortex precession flowmeters described in the literature performed over a 20:1 range of Reynolds number with water, which falls short of the required 1300:1 range (65:1 volumetric times 20:1 viscosity). The minimum Reynolds number for vortex precession to occur was found to be 250 for one device while the maximum Reynolds number was as high as 230,000 for another device (920:1 ratio), yet no one device spanned the whole range. The objectives of this test group are to: (1) determine the extent of Reynolds number range for a single device, (2) find out what phenomenon limits the range (cavitation?) and (3) ascertain what aspects of swirler design and what contours of the flow passage extend the dynamic range.

Solution Approach - Several clear plastic models will be made with various inlet area ratios, expansion ratios, tapers and curves, and several swirler concepts will be made. Combinations of these swirlers and flow passage contours will be tested on a flow stand and evaluated for dynamic range. The test approach will be one of flexibility so that configurations which show promise can be studied in more detail while those showing little promise may be dispensed with quickly. In this regard, this plan is strictly tentative and most likely will change as work progresses and new ideas and understanding of operation evolve.

The flow passages are designed with multiple "O" ring sealed sections that are quickly interchanged so as to permit testing of a large number of combinations. Each venturi or central section of the vortex generator will have two diametrically opposed pressure sensors to provide a vortex signal output that will serve as one measure of performance.

The following swirler types are to be built and tested:

a) Multiple Flat Blade Assembly Figure 4-1
b) Machined Passages Figure 4-2
c) Tangential Inlet Figure 4-3
d) Delta Wing Figure 4-4
Each swirler will be mounted in a section of clear plastic tube that snaps into place upstream of each vortex section. Upstream of the swirler there may be a constant diameter section and flow straightener section, to eliminate incoming swirl.

Each vortex section will actually consist of three parts: (1) tapered inlet (2) constant diameter and (3) expansion outlet. The parameters of the vortex sections and different vortex precession models to be investigated are listed in Table 4-1 and Table 4-2 respectively.

Placement of a central core obstruction downstream of the expansion section may adversely affect the central flow reversal that is so critical to vortex precession. Its effect will be tested by placing a model densitometer section of various sizes at various distances downstream as shown in Figure 4-5. This information is vital to future design of the densitometer housing.

All of these sections - straightener, swirler, vortex generator and densitometer - will be placed in a 45.7 cm (18 in.) section of a 3.81 cm (1.5 in.) diameter pipe flow stand, as shown in Figure 4-6. With this set-up, the entire section under test may be removed, reconfigured and replaced in a matter of minutes. The two pressure sensor signals will be monitored on an oscilloscope and a frequency spectrum analyzer. The sum of the two output voltages will indicate common mode noise while the difference will represent the vortex frequency: the ratio of difference to sum will therefore provide an approximation of signal to noise ratio. The frequency analyzer will indicate the fundamental frequency, bandwidth and harmonic content of the pressure signals. Visual observations aided with a stroboscope flash unit will be made for indications of cavitation and vortex behavior.

4.2.2  Fluid Dynamics -

Problem - There is very little information currently available on the velocity distribution, strength of velocity changes in the precessing vortex and basic frequency of precession. Without this type of information the design of suitable sensors cannot proceed with any degree of confidence, and formulation of theories of operation have no valid basis.

Solution Approach - Several of the better performing configurations, as judged by lack of cavitation and flow separation, by regularity of vortex precession and by dynamic range, will have the flow velocities and directions mapped from the swirler to the de-swirl vanes. The following techniques will be employed to quantify flow characteristics:

1)  Anemometers -
   - Hot film type - Wedge side flow
     - Wedge end flow
     - Cylindrical

2)  High Speed Movies - Flow enhancement with injected aluminum particles and dye.

3)  Pressure Sensors - Various sensitivities and types
     - Quartz, strain gage.
ANEMOMETERS - Maximum flow velocity, through a vortex section, with a swirl ratio of 5 and a 2.69 cm (1.06 in.) diameter throat is 28.7 m/sec (94 ft/sec) which precludes the use of thin wire probe elements, which are reliable at flow rates below 2.13 m/sec (7 ft/sec) Wedge-end-flow hot-film sensors have been used to evaluate vortex flow but lack the directional sensitivity of the thin wire types. Other styles which are listed above are subject to cavitation and may also disturb the vortex itself. Despite these limitations, a series of tests will be conducted using thin film type sensors at flow rates below 636 kg/hr (1400 lb/hr) and wedge-end type sensors at higher flow rates. Flow velocity mapping will be done with apparatus shown in Figure 4-7 over flow ranges from the minimum for vortex precession to the maximum prior to cavitation, and for viscosities of one centistoke and ten centistokes (Tellus Oil).

A miniature drag force anemometer of the style developed by Krause and Fralick at LeRC can provide data on both velocity head and flow angle and will be useful in this investigation. Frequency response of the cantilever beams far exceeds the maximum expected vortex frequency (500 Hz) so the frequency compensation network can be replaced with a simple low-pass filter (at 2,000 Hz). Resizing the beam to handle the forces in liquid may be required. We will consult with LeRC on the design and availability of a unit for use in this test sequence.

HIGH SPEED MOVIES - Tracing individual particle paths and velocities will provide the best visual and quantitative evidence of vortex behavior. A frame rate of 7000 per second (which is typically attainable) will provide adequate frame to frame resolution of 4.3 mm (1.7 in.) for a particle moving 305 m/sec (100 ft/sec) which is the estimated maximum velocity. Enhancement of the vortex can be achieved by injecting aluminum particles and/or dye in various locations, as shown in Figure 4-8.

PRESSURE SENSORS - Spatial and temporal variations in total pressure through the region of vortex generation and dispersion can be measured by placing miniature pressure transducers directly in the flow stream or by inserting a small tube through the meter wall, as shown in Figure 4-9. Data from pressure distributions, in conjunction with velocity information, will provide excellent evidence from which theories of vortex precession can be based and from which sensors may be designed. Two types of pressure sensors will be tried: quartz and semiconductor strain gage. Both types have small sensitive areas 64 mm (0.25 in.) diameter or less and adequate sensitivity in 690 kPa (100 psig) range devices (4 volts output at 690 kPa). Differential pressure between two points will be evaluated by placing matched sensors at the desired points and electronically differencing, rather than by purchasing integral differential units, to provide flexibility and lower costs.
4.2.3 Sensor Evaluation

Problems - The vortex sensor must provide a signal sufficiently free from noise at all flows and environmental conditions (including vibration, pressure pulsations and turbulence) such that essentially no false triggers or lapses in triggering occur. The output device must be of sufficiently low impedance (50 ohms preferred, less than 1,000 ohms acceptable) such that signal transmission over lengthy cables is unaffected by conducted and radiated noise. The unique advantage of this sensor is that it must be sensitive to cyclic pressure or velocity variations (since volumetric flow rate is proportional to frequency of precession) but need not provide accurate data on absolute velocity or pressure.

Solution Approach - Velocity and pressure data from the previous test will be analyzed and several candidate sensors will be designed, built and tested. Each sensor candidate will be tested in the vortex generator combinations which were previously selected for the fluid dynamics studies. The tests will determine the maximum flow range where reliable signals can be obtained with Stoddard solvent (1 cs) and Tellus oil (10 cs). Output parameters such as peak-to-peak voltage, signal-to-noise ratio, frequency jitter of the fundamental vortex signal and noise spectrum will also be evaluated for each candidate sensor. One from each of the following "families" will be evaluated, provided that previous tests and experience deem it reasonable:

- Heat transfer
- Pressure
- Flow direction

4.2.4 Linearity and Repeatability Measurements

Problems - Vortex precession data for gas flow measurement show ± 0.15% repeatability and ± 2.25% linearity over a 35:1 flow range. Data in the literature indicates linearity of ± 12% over a range of 333:1, but provides no indication of repeatability over the expanded range. Furthermore, there is no indication of repeatability with water or jet fuel. In this program, non-linearities that are a function of Reynolds number are compensated for via a microcomputer and repeatability is most important. Reynolds number dependence cannot be too great, otherwise precise measurement of viscosity would be required for accurate compensation of the non-linearities.

Solution Approach - The efforts in the preceding test groups will produce several configurations suitable for evaluation of repeatability and linearity. The tests will be conducted on the flow stand with two calibrated turbine meters in parallel, and one selected according to the flow range that is applicable (see Turbine section). Three viscosities of liquid will be run over the available flow range to ascertain the degree of Reynolds number dependence and nonlinearity.
4.2.5 Time Response

Problem - Present estimates indicate a 0.032 sec response time at maximum flow rate and 1.6 sec at minimum flow rate, which exceeds the design requirement of 0.025 sec. Transport lag, measurement period and filter time were estimated but vortex re-establishment time remains an unknown.

Solution Approach - The vortex meter configuration selected for linearity and repeatability tests will be placed in a test rig designed to produce rapid reductions in flow rate. A turbine flowmeter will be placed upstream to provide an indication of actual flow change as shown in Figure 4-10. Since the vortex meter response is expected to be slow, the turbine meter and test rig do not have to produce step flow changes faster than 0.050 sec at mid-range flows, which is easily achievable. A hot film probe will also be installed as a velocity change monitor.

4.3 Experimental and Analytical Investigations

Data relating to the vortex precession flowmeter is included in the accompanying report supplement No. 1 dated December 15, 1984 as protectable data in accordance with contract NAS3-22139x, Item 8C.

4.4 Conclusions and Recommendations

The vortex precession concept exhibits greater non-repeatability at all flow rates and is not likely to achieve the required time response. Improvements in swirler and de-swirler designs may lower the now excessive pressure drop, but any gains here are likely to be lost when overall diameter is reduced to speed up time response, increase signal amplitude and improve linearity. Furthermore, the risks of cavitation of the central core and entrapment of any air in the fuel line make the concept less attractive.
Tables and Figures

Tables and figures for this Section 4 relating to the vortex precession flowmeter are included in a separate report supplement, as protectable data in accordance with contract NAS3-22139, Item 8C.
Table 4-1
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Table 4-2
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Figures
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Figure 4-4
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Figure 4-5
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Figure 4-9
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5.0 DUAL TURBINE FLOWMETER

This section describes the experimental and analytical investigation, the prototype construction and evaluation performed on the dual turbine flowmeter concept under Tasks 2 through 7 of Phase II of NASA contract No. NAS3-22139 to develop a High Accuracy Fuel Flowmeter.

5.1 Introduction

The turbine flowmeter is a widely accepted flowmeter with proven precision and accuracy. It was therefore considered an excellent potential candidate for a high accuracy mass flowmeter. The major drawback with the turbine type flowmeter is that it is only a volumetric device, and it needs a density measurement to yield mass flow rate. Also, it requires a viscosity measurement in order to cover the full flow range with reasonable accuracy.

The dual turbine flowmeter concept identified in Phase I offers a design that will enhance current turbine meter technology. The problems associated with standard turbine meters of sensitivity to upstream swirl, bearing friction/wear, limited range, and viscosity sensitivity are mitigated by the addition of a second free counter-rotating turbine element immediately downstream of the first element. The second turbine has only a fraction, say 20%, of the main turbine pitch (and, therefore, free rotational speed). The speed of each is measured and the sum of the speeds is used as the volumetric flow signal. An analysis of the flow vectors entering and leaving each turbine shows that this sum of speeds (as measured by blade passing frequency) is nearly independent of upstream swirl content and of bearing or viscosity induced drag on the main (high speed) turbine. Furthermore, by measuring the ratio of the two speeds the health of the flowmeter bearings can be monitored.

The mass flow rate can then be achieved by combining the outputs of the two turbines plus the precision density measurement from the densitometer.

5.2 Experimental and Analytical Investigation Plan Formulations

To evaluate the design concept of the dual turbine flowmeter and its potential in meeting NASA HAFF requirements, the following tests were planned to be conducted in Task 4:

(1) Turbine Start-up
(2) Turbine Blade Geometry
(3) Optimum Rotor Design
(4) Verify Dual Turbine Theory
(5) Repeatability in Critical Zone and Low Reynolds Number
(6) Viscosity Accuracy
(7) Signal Interaction
5.2.1 Turbine Start-up

**Problem** – The General Electric concept for 65:1 volumetric flow range capability from a turbine meter depends on low-end repeatability at 0.050 kg/s (400 lb/hr) and worst case (low temperature) start-up at about 0.025 kg/s (200 lb/hr) flow. Prediction of start-up flow depends on bearing friction (which can and will be measured) and on torque versus flow over a stalled blade, which is not addressed with sufficient detail in the literature. The difference between start-up flow and minimum flow where adequate repeatability exists is unknown.

**Solution Approach** – Measure the "start rotating" and "stop rotating" flows for two turbine flowmeters in fluids with 1 and 20 centistokes viscosity. The flowmeters will be the following:

<table>
<thead>
<tr>
<th>Size</th>
<th>Flow Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 1.27 cm (0.50 in.)</td>
<td>0.02 to 0.38 liter/sec (0.3 to 6 gpm)</td>
</tr>
<tr>
<td>0 2.54 cm (1.00 in.)</td>
<td>0.1 to 4.1 liters/sec (1.6 to 65 gpm)</td>
</tr>
</tbody>
</table>

Also, the smaller meter will be used to accurately determine the repeatability of the larger one in its low flow range (start-up critical). The results will be used to determine the flow range between "start-up" and "minimum adequate repeatability".

5.2.2 Turbine Blade Geometry

**Problem** – The optimal design of turbine blades depends on better understanding of the following effects:

- **Surface Roughness** – Its effects on boundary layer thickness and drag coefficient versus surface conditions and imperfections, unknown.

- **Trailing & Leading Edge Sharpness** – Critical to low drag coefficient in turbine blades.

- **Solidity Ratio** – Is solidity ratio of unity required and how sensitive is momentum exchange to this ratio? What is torque versus Re before startup for various ratios?
Solution Approach - A large scale clear plastic model (Figure 5-1) will be built. The rig consists of a variable speed motor driven upstream swirler section and a downstream section where the stationary test item is observed and where measurements in flow are to be made. The following measurements will be made with this apparatus:

1) Axial and tangential velocities via hot film anemometers.
2) Blade/vane pressure distribution via multiple ports and high accuracy pressure sensor.
3) Flow patterns with dye injection and high speed movies.

The following tests will be conducted:

Surface Roughness: - ground and polished
- sand (various grits)
- using one vane
- measure boundary layer versus Re

Trailing & Leading Edge Effects:
- 10° end
- 30° end
- 0° end
- 12° taper
- measure tangential flow downstream of vane.
- photograph wake with dye injection.
- determine effect of boundary layer.

Solidity Ratio: - construct turbine rotors with ratios of 0.5, 0.75, 1.0, and 1.3 and evaluate stalled flow patterns versus Re.

5.2.3 Optimum Rotor Design

Problem - Results of the preceding tests must be incorporated into the analytical model and from this model the optimum turbine rotor design must be extracted.

Solution Approach - The measured and calculated data from the above tests will be compared to actual calibration curves and the theoretical model will be validated and updated. Bearing friction and torque versus flow for a stalled rotor will predict start-up flow for the low speed sensor turbine. Leading and trailing edge test results, along with surface finish test results, will guide the design of turbine blades. Results of solidity ratio tests will also be taken into account in the updated model. The conceptual design from Phase I will then be optimized by taking into account all these factors.
5.2.4 Verify Dual Turbine Theory

Problem - Determine the relationship between the calculated calibration expression for a two rotor flowmeter and the actual curve. Determine if swirl effects have been negated and if other flow phenomenon affecting calibration are present.

Solution Approach - Test optimized turbine and sensor rotors; both separately and combined. Investigate any significant deviations from the predicted calibration expression for each rotor and then for the two rotor design. Mount a pre-swirler upstream of the flowmeter to ascertain that swirl has been negated or reduced to an acceptable level. A circulating flow stand will be used, which for flow measurement utilizes two precalibrated turbine flowmeters (see Figure 5-2). A smaller flowmeter has 0.02% repeatability capability over its linear (+5%) range of 0.02 to 0.38 liter/sec (0.3 to 6.0 gpm) when used with calibrating fluid of 1 cs. A larger unit with the same order of repeatability will cover the flow range of 0.1 to 4.1 liters/sec (1.6 to 65 gpm). A working model (Figure 5-3) will be fabricated which will be capable of accepting either turbine or sensor rotor in either upstream or downstream position or tested with both rotors. The modulated RF pickoff and signal conditioners will be purchased. The following order of testing, analysis and calculation will be undertaken.

1. Determine start-up flow and actual calibration curve for each rotor.
2. Analyze data to determine retarding torques and other variations from theoretical flow conditions.
3. Derive a calibration expression for the two rotor flowmeter.
4. Test and measure actual calibration.
5. Further investigate by test and analysis significant variations from the predicted curve.
6. Test, with known pre-swirlers, the effect of swirl and determine the level to which it has been eliminated or minimized.

5.2.5 Repeatability in Critical Zone and Low Reynolds Number

Problem - Repeatability, especially at "start-up/high viscosity" and in the "critical flow zone" must be evaluated so that overall system accuracy can be estimated.

Solution Approach - Measure repeatability of test model under worst case flow conditions by comparing with 0.02% known repeatability turbine flowmeters. Testing of low flow conditions will be conducted in the circulating stand with 20 cs fluid and measured with the smaller, 0.02 to 0.32 liter/sec (0.3 to 6.0 gpm) calibrated turbine flowmeter and also on a small COX weight stand with the temperature reduced to -55°C. Testing for repeatability in the critical zone will be similar, except the 0.1 to 4.1 liters/sec (1.6 to 65 gpm) flowmeter, in the circulating stand and the larger COX weight stand will be used.
5.2.6 **Viscosity Accuracy**

**Problem** - Determine the accuracy required of viscosity measurement for less than 0.05% contribution to overall system error.

**Solution Approach** - Measure change in calibration to the test model when tested with a 1 cs and a 20 cs viscosity fluid. A circulating stand with two turbine flowmeters will be used to measure flow rate as previously described. These flowmeters will have been previously calibrated at the two test viscosities.

5.2.7 **Signal Interaction**

**Problem** - Two RF amplitude modulated signals need to be conducted over long, adjacent leads and must not interact.

**Solution** - Twenty foot cables of the following conductor styles will be evaluated for signal interaction on the dual turbine model:

1. Untwisted Pair
2. Twisted Pair (independent grounds)
3. Twisted Shielded (mutual grounds)
4. Coaxial

5.3 **Experimental and Analytical Investigation**

Responding to a NASA requirement for a highly accurate mass flowmeter operating over a 65:1 volumetric flow range and a 30:1 viscosity range, General Electric proposed a dual turbine flowmeter with a densitometer. The significance of the dual turbine is its ability to detect and compensate for fluid swirl along with variations in retarding torque or turbine slip that are due to viscosity and mechanical changes, thereby reducing the effect on the flowmeter turbine speed versus volumetric flow relationship.

Along with a need to prove out the concept, problem areas were anticipated and the approaches to address these problems were outlined in Section 5.2.

To answer these questions, an engineering model was built and tested. This section contains a description of these tests, the test results and their meaning, and a discussion on recommended additional actions emanating from the test results.

5.3.1 **Engineering Model** - The model used for engineering evaluation consisted of a clear acrylic housing in which the main and sensor turbines rotated. A single miniature ball bearing containing a machined "self lubricating" duroid retainer was used for each turbine. See Figure 5-4.

The central shaft was designed to be either rotated by the dither mechanism or locked to prevent rotation. The turbines were spaced apart by a separator which was planned to be modified into a dither mass.
As constructed, the turbines could be individually tested or combined as a dual unit. The main turbine had 8 blades with a helical angle of approximately 52 degrees. Two sensing rotors were fabricated. Initially both had 8 blades; one with a 15° helical angle and the other with 22°. Later four blades were removed from the 22° rotor.

A flow straightener from a COX flowmeter was modified to provide the front support for the central shaft. The rear support was centrally positioned by three vanes. The modulated RF pickoffs were purchased from COX along with their driving electronic modules.

5.3.2 Test Results

5.3.2.1 Bearing Friction - A major factor that affected the flowmeter design, mainly because of the lower operating speed of the sensor turbine and the large dynamic operating range of the turbines, was the retarding torque value at low flow/high viscosity conditions; principally bearing friction.

In the proposed concept, slip calculations used a static bearing friction of 14.7 x 10^-6 N·m and a design of two bearings per turbine. With a dither mechanism it was planned to reduce this value by a factor of two. To develop adequate starting torque to overcome bearing friction, a larger diameter, narrow annulus, restricted flow passage was proposed. While this design generated larger torques at lower operational speeds, it did have the disadvantages of a higher pressure drop and an increased response time.

Tests on the main and sensing turbines revealed that for this application and with the type bearing chosen, friction is significantly lower than assumed. The main turbine readily rotated at a flow rate below 0.013 kg/s (100 lb/hr) in fluid with a viscosity of 12 cs. The 22° helical angle sensor turbine started coincidently with the main turbine.

As expected, the 15° sensor slightly lagged the main turbine in starting, and rotation beginning at a flow rate of 0.013 kg/s (100 lb/hr). It was smoothly rotating and fully operational at a flow rate of about 0.025 kg/s (200 lb/hr). From the results of rotational speed and flow values, bearing friction was ascertained to be approximately 0.98 x 10^-6 N·m.

These test results are highly significant. They show that a "dither mechanism" is not needed; nor is the narrow annulus. A more standard configuration can be used. Response time and pressure drop will therefore be typical of that for a 2.54 cm (1 in.) tube size turbine flowmeter.

5.3.2.2 Swirl Effect Test - A flow swirler consisting of a cluster of canted, small diameter, tubes was introduced upstream of the engineering model. It had been hoped to introduce up to 5% calibration change due to swirl. However, the flow straighteners in the model limited the swirl effect on the main turbine to about a 0.5% change. Attempts to introduce greater swirl through the use of a rotating impeller in a modified flowmeter mounted upstream of the model also proved to be ineffective. Of great importance, however, was the fact that the introduction of this swirl which normally would have caused an error in the flowmeter reading, was sensed by the sensor turbine and the combined readings of the sensor and main turbines remained unchanged.
The graphic results of the Swirl Test are shown in Figure 5-5. The bottom series of points are a calibration plot of the main turbine speed versus flow rate. They show an increase in the "K" factor with the introduction of swirl. The top series of points are a plot of the combined turbine and sensor speeds showing that the calibration, is the same with and without swirl.

It should be noted that because of functional difficulties, a spectrum analyzer with 0.5% frequency resolution was used to measure sensor turbine speed, and a frequency counter was used for the main turbine. This was equivalent to about 0.1% on the combined speed so that measurement resolution was no greater than the flowmeter repeatability it was hoped to prove. Essentially, the spread shown for the combined readings is equivalent to the resolution of the measuring equipment.

5.3.2.3 Turbine Repeatability - Several room temperature tests were conducted on both the COX AN-16 flowmeter supplied by NASA and an 8 blade rotor used as the main turbine in the engineering model. These tests were conducted over the specified operating range to check repeatability throughout and if it degraded, in the critical transitional flow range and at low starting flow rates.

It was found that repeatability in these ranges was no different from that in the more linear turbulent range. Figure 5-6 is a calibration plot of the AN-16 flowmeter. Points shown are from NASA supplied data and tests conducted by General Electric. At typical room temperature viscosity and density, the lower 0.050 kg/s (400 lb/hr) flow condition is equivalent to a chordal Reynolds number (Re) of 2000. It can be seen that the calibration shows no inflection at the critical Reynolds number of 5000. Also the scatter of data points is no greater for Re = 2000 than at higher Reynolds numbers.

The plot of data indicates a spread of about ± 0.4%, raising the question as to whether or not the COX weigh stands used were a source of error. Two separate tests on a newly operational flow stand that uses turbine meter masters at General Electric, indicated an extremely linear calibration, all data points falling within 0.1% linearity from 0.63 to 5.04 kg/s (5000 to 40,000 lb/hr); pointing to the COX weigh stands as the probable cause of the data spread. To more fully prove that the turbine flowmeter repeatability is within 0.1% would require better flow measuring approaches than those presently available.

5.3.2.4 Viscosity Effects Test - Tests were conducted at cold temperature in calibration fluid (5 cs viscosity) and at room temperature in Tellus #10 (12 cs viscosity). The results of these tests for the AN-16 are shown in Figure 5-6.

When plotted against Reynolds number, good agreement was achieved for the cold and Tellus runs. Data were taken at a lower output frequency equivalent to 0.03 liter/sec (0.5 gpm), below which the output became unreliable. Because of this problem at low frequencies it was difficult to determine whether the calibration between room temperature and cold was predictable solely by Reynolds number. At room temperature and at Re of 1500, the output of the AN-16 was approximately 20 Hz. Below this value, the signal rapidly attenuated, mixed with side frequencies and caused count inaccuracy. The two
test points shown at Re of 1000 could therefore be in error. However, while it is likely that some error exists, sufficient experimentation was done in this flow range to indicate a high probability that the room temperature calibration drops off faster than the cold temperature calibration.

Further testing is required before this phenomenon can be definitely established. If confirmed, this apparently small shift, (on the order of 2%) can readily be corrected using viscosity and temperature measurements. This shift can be minimized by changes in the turbine rotor design (see Section 5.4).

No valid viscosity information could be derived for the engineering model. Though still rotating, no signals could be read from the sensor turbine at the lower flow rate. The lowest room temperature Reynolds number attained was 3700, and the minimum for cold was 500. Therefore, between 3700 and 500, the area of possible calibration shift, no data are available.

5.3.2.5 Calibration Predictability Tests – Four turbines were tested to determine if their actual calibration corresponded to the calibration which was predicted using calculations based on drag torque and momentum theory.

Testing of both a six blade, 45° helical turbine and an eight blade, 52° helical turbine (used in the engineering model) revealed that the cusp in the calibration curve occurred well below the predicted chordal Reynolds number (Re) of 5000 and that the degree of "speed-up" or nonlinearity at the cusp was two to four times greater than predicted, as shown in Figure 5-7. Also, the slope of the actual calibration curves for both turbines was two to four times greater than the predicted curve in the laminar flow range where Re is less than 1000. Furthermore, the six blade turbine had excellent linearity at flow rates above 2.52 kg/s (20,000 lb/hr) while the eight blade turbine cavitated at flow rates above 1.89 kg/s (15,000 lb/hr) – an effect that is not predicted by momentum theory.

Calibration curves of the low speed sensor turbine proved equally unpredictable, as shown in Figure 5-8. Here the performance of an eight blade, 22° and a four blade, 22° turbine are compared. Of significance here is evidence that the airfoil theory for isolated blades, modified to account for blade interference, is more representative of actual performance than momentum theory. The figure shows that the 22° rotor actually speeded up when four of the eight original blades were removed; and that the relatively steep curve of the eight blade rotor was reduced by going to four blades. Blade interference and the space/chord ratio were reduced by reducing the number of blades, but rotor speed increased. Momentum theory predicts lower speed with fewer blades due to reduced guidance of the flow.

The top curve of Figure 5-8 shows how the sensor turbine was speeded up by the rotation imparted to the liquid by the upstream main turbine.

The design of a high accuracy turbine flowmeter in conjunction with a microprocessor dictates different design objectives than those used for normal turbines. Usually the turbine is designed for the best linearity over a 10:1 range above the critical Re so that sensitivity to viscosity is kept to a
minimum and calibration is via a single constant. Performance below
transition may be disregarded, and the calibration curve usually falls off
steeply as the flow goes into the laminar regime. However, with a
microprocessor that memorizes the calibration curve and computes Re with
viscosity information, the dynamic range can be extended far below the normal
range. But to do this, the linearity below transition must be improved with
some allowable sacrifice of high-end linearity. The factors in turbine design
that can produce this new characteristic performance must be evaluated further
and better understood.

5.3.4 Discussion and Conclusions - While the testing of the engineering
model proved the feasibility of the dual turbine concept and settled the
critical question of the sensor's ability to operate at low flow, it did
reveal some problems which have an impact on the turbine design.

While the actual turbine calibration was not as expected, this does not
necessarily present a problem but, if anything, points to a change in rotor
design philosophy which, in the end, means an improvement in overall
performance.

As mentioned previously in this report, linearity over a typical turbine range
of 10:1 is not a design objective. The calibration curves on Figure 5-6 show
little difference for Reynolds numbers above 10,000. The major changes are at
lower Reynolds numbers and it is important to minimize these variations and to
have a repeatable calibration for changes in temperature, density and
viscosity.

Different turbine geometry is also suggested. For example, a viscosity
change, with its effect on boundary layer thickness and therefore the average
velocity at the rotor blades, could possibly have its effect reduced by a
larger blade tip clearance. Alternately, since tests show that drag forces
are not adversely slowing down the turbine speed, the introduction of
additional drag could possibly flatten out the overall calibration.

While reducing the number of sensor blades proved beneficial, this only
amplified the problem of the already too low sensor output frequency. The
attenuation of the output at low frequencies by the electronics should be
correctable. However, the delay in generating updated information is more
serious.

At 0.050 kg/s (400 lb/hr) flow rate, the six blade main turbine would rotate
at approximately 3 Hz, an output frequency of 18 Hz. A four blade sensor,
even speeded up to run at 1/3 the main turbine speed or 1 Hz, would have an
output of 4 Hz or a signal update rate of 250 ms, which is not adequate to
meet the time response requirement. There are a number of ways to reduce this
time. Several pickoffs per turbine or a multi-core pickoff could generate a
greater number of pulses. More attractive from cost and simplicity would be
the use of a slotted rim over the rotor blades. This type of device could
serve a dual function: generating a greater number of pulses while reducing
the change in calibration at lower Reynolds numbers.
While the sensor signal update rate is probably the most significant shortcoming of the dual turbine approach, the many alternate solutions to this problem could undoubtedly reduce the delay time by an order of magnitude.

Test results were generally very favorable although one unanticipated problem, the inability to measure low rotational speeds limited testing at low flow rates. A brief summary of the significant results are listed below.

1. The sensor turbines accurately described and compensated for swirl introduced into the flow stream.

2. Bearing friction proved significantly lower than the values used for the proposal conceptual design.

3. The dither mechanism is not required.

4. Repeatability measurements of the dual turbine meter over the full flow range were within that of the measuring equipment.

5. The calibration curves of the main and sensor turbines were not predictable from drag force calculations alone.

6. At Reynolds numbers below 1000, the relationship between flow rate and Reynolds number apparently cannot be represented by a single calibration curve.

7. At frequencies below 20 Hz the pickoff output was attenuated by filters in the drive electronics making it impossible to measure low rotational speeds.

5.3.5 Recommendations - The swirl effects and bearing friction tests have demonstrated the feasibility of the dual turbine concept and the practicality of a lower operating speed sensor. The dual turbine flowmeter is still, therefore, a viable candidate for the high accuracy flowmeter. However, further investigation and testing are required and the following recommendations are made:

1. Based on the results of the friction tests, the restricted area, narrow annulus concept originally proposed is no longer a necessity. Future designs should utilize more typical turbine flowmeter sizing. Pressure drop and response time will be more to specification and in keeping with a 2.54 cm (1 in.) tube size turbine flowmeter.

2. Signal update rate must be improved. Several alternate approaches are suggested. These are:
   a. More than one pickoff per turbine.
   b. A single, multi-core, pickoff
   c. A multi-slotted rim over the turbine blades.
   d. Slots in the rotor blade tip.

3. The electronics must be corrected to eliminate the attenuation problem at low frequencies.
4. Flow factors affecting calibration must be better understood and rotor geometry optimized to reduce changes in calibration and minimize viscosity effects. Areas requiring further investigation are:

a. Blade number/width relationship
b. Optimum space/chord
c. Main turbine and sensor turbine axial spacing relationship
d. Blade tip clearance effects
e. Added drag coupling effects

In summary, the inherent repeatability, dynamic range and fast-time response of the dual turbine concept make it the best candidate for the NASA high accuracy fuel flowmeter. Additions of a microprocessor and density and viscosity measurements extend the usable range of the turbine meter below the flow rates where transition and laminar flow normally introduce unacceptable non-linearity and viscosity dependence. Although the effects of blade tip clearance, solidity ratio and blade edge shape are not yet fully understood, the combined effects of these parameters on repeatability and non-linearity are so slight that they are not of great concern. Further investigation in these areas will provide the answers necessary to more carefully design the next prototype.

5.4 Prototype Design and Test Plan Formulations

A prototype high accuracy fuel flowmeter has been designed based on the Dual-turbine Densi-viscometer concept that was selected by General Electric and NASA as the best of three alternatives at the conclusion of Phase II, Task 4. The turbine design is based on currently available 2.54 cm (1.0 in.) size units, but makes use of a second low speed turbine to compensate for swirl of incoming flow and to increase linearity of the characteristic calibration curve at low Reynolds numbers. The Densi-viscometer sensor is mounted directly in the flow stream and when driven by the closed loop electronics oscillates torsionally at a frequency that depends on fuel density. The electronics also modulates the frequency of oscillation so that fuel viscosity can be derived. The circuit does this with precision phase shifting. A platinum resistance temperature device compensates for temperature sensitivity of the Densi-viscometer. Calibration constants and computation algorithms that lead to mass flow rate will be programmed into the data acquisition and processing system, not considered as part of the flowmeter at this stage of development.

A two phase test plan has been formulated to allow calibration of the Dual-turbine half and the Densi-viscometer half of the flowmeter independently of each other. Following calibration the two halves will be joined and subjected to the following performance evaluations: repeatability, accuracy over the temperature range, vibration, inlet swirl, pressure drop, attitude, time response, and alternate fuels.
5.4.1 Prototype Flowmeter Design - The prototype flowmeter measures volumetric flow rate and fuel density, viscosity and temperature via four separate sensor elements. It provides frequency based signals for all but temperature, which is inferred from the resistance of a platinum RTD, and densitometer frequency modulation, which is a two wire logical output. Figure 5-9 shows these prototype functional elements divided into a flowmeter section and an electronics section. The flowmeter and electronics have been designed so that the Dual-turbine and the Densi-viscometer halves of the flowmeter can be easily separated for independent operational checks and calibration, and then mated for evaluation of the complete flowmeter. The electronics do not contain power supplies which must be provided with the proper voltages and current levels from laboratory power supplies.

To obtain mass flow rate the frequency, temperature and logical output signals must first be converted to accurate volumetric flow rate and density representations through known calibration constants and then multiplied. A digital microcomputer will perform these tasks in the production flowmeter system, but for the prototype evaluation, these computations will be performed by the Data Acquisition and Processing System described in Section 5.4.4. The constants and algorithms will be developed in the prototype testing phase. They will become valuable "paper parts" of the flowmeter, and will be fully documented.

An outline drawing of the flowmeter is shown in Figure 5-10.

All the detailed sketches of piece parts and subassemblies are shown in Appendix E.

5.4.1.1 Dual Turbine Design - Volumetric flow rate is equal to a constant times the sum of the main and sensor turbine pickoff frequencies as detailed in Section 5.0 of the Phase I Final Report. The sensor turbine has been added to provide accurate compensation for swirl which may be in the incoming flow stream. The sensor turbine rotates in the direction opposite to that of the main turbine so that swirl will speed up one and slow down the other; then the frequency sum undergoes no change with swirl. Both turbines have six blades, but the sensor blade angle is less than the angle in the main turbine in order to increase overall linearity with laminar flow, as discussed in the Phase I Final Report. Furthermore, the dual turbine design permits a continuous self-check of bearing health.

The dual turbine assembly, shown in Figure 5-11, consists of two major subassemblies: the turbine and shaft assembly which includes the inlet straightening vane and the nose cone that diverts flow around the Densi-viscometer sensor (not shown); and the housing that contains the turbine speed pickoff. The turbine and shaft assembly is secured inside the housing with a retaining ring. The flow straightener at the inlet removes most of the swirl from the incoming flow and also supports the upstream end of an integral shaft. The main turbine follows downstream of the straightening vanes and is made of magnetic stainless steel. The frequency is measured by a variable reluctance pickoff which senses the change in magnetic reluctance induced by passing turbine blades. This turbine is a proven design that is typical of commercially available turbine flowmeters and it is supported by a single high quality ball bearing. The sensor turbine is similar to the main turbine with the exceptions that its blade angle is a 23.5° helix and it has a left-handed sense. The downstream end of the shaft is located by the nose cone and is secured by a lock nut.
The outer housing is made of 304 stainless steel in order to provide a suitably strong structure which is nonmagnetic and of low conductivity so as not to interfere with the pickoff performance.

Two pickoffs are made by winding wire around the central pole of a magnetic core. When a magnetic turbine blade is aligned with the pickoff its inductance increases and this change is sensed by the signal conditioning circuitry. The signal conditioning circuitry is typical of current technology and is a RF modulated carrier type. This design exerts no torque on the turbine blades which helps to maximize the range of flow measurement.

The electrical receptacle is fastened to the housing and provides a suitable environment for the pickoff coils and wiring.

5.4.1.2 Densi-viscometer Design - Data relating to the densi-viscometer design are included in Section 7.4.1.1 of the accompanying report supplement No. 1 dated December 15, 1984 as protectable data in accordance with contract NAS3-221391, Item 8C.

5.4.1.3 Densi-viscometer Electronics - Data relating to the densi-viscometer electronics design are included in Section 7.4.1.2 of the accompanying report supplement No. 1 dated December 15, 1984 as protectable data in accordance with contract NAS3-221391, Item 8C.

5.4.2 Test Plan - The prototype will be initially assembled and made operational in two parts: the Dual-turbine half and the Densi-viscometer half. This will include careful calibration of each half since they have distinctly different functions. The calibration characteristics of the dual turbine, the temperature sensor and the Densi-viscometer will then be programmed into the Data Acquisition and Processing System (DAP system) being developed expressly for Prototype evaluation, and described in Section 5.4.4. The completely calibrated prototype will then be connected to the DAP system, inserted in the flow line and subjected to a battery of tests designed to establish how well the flowmeter meets the design specifications and guidelines.

5.4.2.1 Dual Turbine System Calibration - Prior to calibration, two tests will be conducted to verify suitability of the turbine design and construction. First, the effects of inlet swirl on the angular velocity of both turbines and on the summed frequency signals will be determined and the effectiveness of the inlet flow straighteners will also be determined by placing a swirl generator consisting of two 90°-out-of-plane bends upstream of the turbines. Turbine frequencies will be measured for four cases: with and without the straightening vanes, with and without swirl. Comparison of turbine constants will indicate effectiveness of the dual turbine compensation technique, and will provide a measure of actual inlet swirl rate.

Second, to determine suitable sample times for measuring stable turbine frequencies and to initially evaluate repeatability of the turbines, the dual turbine half will be tested over the flow range at room temperature. A flow calibrator, such as a COX 311H (weigh-time) or COX 620
(volumetric-density), and a monitor turbine will provide stable references against which the dual turbine will be compared. Measurement times from 1/5 to 60 seconds (minimum 10 sec with flow calibrators, less with monitor turbine) and flow rates from 0.050 kg/s (400 lb/hr) to 2.52 kg/s (20,000 lb/hr) will be evaluated with multiple readings at each of several points.

After these initial checks indicate satisfactory performance, the calibration factor K vs Reynolds number characteristics will be measured and programmed into the DAP system. This calibration will be done at room temperature with three different fluids having viscosities of approximately 1.3, 5.0 and 15 centistokes. MIL-C-7024A, Type II calibration fluid will be used for the 1.3 cs viscosity, and mixtures of Almag and Tellus #10 oils will be used for higher viscosities. Further, several runs will be made with calibration fluid near the temperature extremes (-55 and +100°C) to verify the predicted effects that material expansion and contraction have on the turbine constants.

For purposes of these calibrations and subsequent prototype evaluations it is necessary to establish "in house" standards of mass flow rate, volumetric flow rate, density and viscosity. For the above turbine calibrations, the two volumetric flow rate standards will be 2.54 cm (1.0 in) and 1.27 cm (0.5 in) size turbines. These monitor turbines will be calibrated using COX 305 and 311H weigh-time stands (mass flow rate) combined with in-line density measurements using a Mettler-Paar DMA 60 and DMA 620HT high accuracy digital density meter.

During calibration of the monitor turbines, the number of flow measurements that are taken at each flow rate will be determined by statistical analysis. Typically, enough measurements will be taken at a particular flow rate to ensure that the mean of the COX flow stand outputs is known within + 0.05% at a 95% confidence level using the Students'-t statistic. Average mass flow rate divided by density will then be the reference volumetric flow rate that determines the turbine K factors. During subsequent prototype evaluations (described in the following section) the same weigh-time stand outputs and the prototype output will be in terms of mass flow rate and may be compared directly, without the conversion to volumetric flow rate. However, tests may show that the outputs of the monitor turbines and the densitometer standard can be combined to provide a more repeatable indication of mass flow rate than the COX stands, in which case, the monitor turbines will serve as the standards against which prototype accuracy is determined.

If the COX stands prove to be adequate for use as a standard in the evaluation phase, then the tare and sample weights used during evaluation for each range of flow measurement will be used again in the calibration phase. Since the systematic errors of the COX flow stand (as reported in the Section 3.0 Calibration Study) depend heavily on the selection of tare and sample times (and weight) this technique will effectively eliminate any variations in the systematic errors caused by buoyancy effects and timing errors resulting from changes in fluid forces, holding tank inertia and
Sample control volume. This technique also permits direct readout of COX flow rate without compensation for the systematic errors and greatly simplifies the task.

While these techniques will not provide evaluation of absolute accuracy (i.e., the known systematic errors of the COX flow stands are not corrected) they will provide an excellent measure of prototype repeatability. In the future, when a more accurate flow standard is available, the biases introduced with the COX flow stands can be easily compensated out by introducing new calibration constants in the software.

Viscosity of the calibration fluid will be calculated from an accurate temperature measurement at the flowmeter and from a viscosity versus temperature curve which is evaluated just prior to the test. The temperature sensor will be an RTD and the viscosity measurements will be made with a suspended capillary type viscometer. See Table 5-1 for a listing of these measurement standards.

For purposes of this prototype evaluation, it is also necessary to establish standards for time, temperature, density and viscosity that are accurate, stable and readily available. Table 5-1 describes these standards.

5.4.2.2 Densi-Viscometer Calibration - Density and viscosity ranges for JET-A, Jet A-1, JP-3, JP-4, and JP-5 fuels taken from the Test and Calibration System Study (Section 3.0 of this report), are summarized in Table 5-2. These fuel characteristics will be simulated at room temperature by mixing various liquids also listed in the table. With these mixtures held at fixed temperature, in the apparatus shown in Figure 5-12, the frequency characteristic of the Densi-viscometer to both density and viscosity will be evaluated. This will expedite adjustment of the electronics and calibration of the sensor because shifts caused by temperature changes will be minimized.

After initial calibration over the density and viscosity ranges, the Densi-viscometer will be calibrated over the temperature range, (-55°C to +100°C with the electronics at room temperature) in air and in calibration fluid. The test apparatus shown in Figure 5-12 will circulate heat transfer fluid in a loop that includes a temperature controller, the fully assembled Densi-viscometer with RTD, the density standard and the viscosity standard. Insulating the loop will assure temperature stability. The calibration fluid samples will be closed and pressurized so that atmospheric water vapor will not condense into and contaminate them at low temperatures, and so that light distillates will not vaporize at high temperatures and thereby prevent gradual increase in density with time. Concurrent with density calibration, the temperature-viscosity characteristics of the test fluid will be derived from a kinematic viscometer standard immersed in the heat transfer medium. The results of the calibration will be correlated by a least squares polynomial that will be programmed into the DAP system for subsequent evaluation of the prototype.

A third test will be conducted to assure insensitivity of the sensor to fluid flow. The Densi-viscometer half will be placed in a flow stand with
the nose cone and aft deflector in place. Flow rate will be varied from zero to 2.52 kg/s (20,000 lb/hr) while sensor frequency is monitored for change. Improvements in flow diversion will be made at this time, if required.

5.4.3 Prototype Evaluation - The following tests will be made on the complete flowmeter:

- Repeatability
- Accuracy
- Vibration Sensitivity
- Attitude Sensitivity
- Pressure Drop
- Response Time
- Alternate Fuel

For all tests except response time and pressure drop the prototype outputs will be connected to the DAP system. The above tests are briefly described in what follows.

5.4.3.1 Repeatability

**Objective** - To determine the constancy of measurement of mass flow rate.

**Method** - Pass a flow rate, which is known approximately, through the flow sensor. Measure the flow with at least two other flow sensors to establish a reference for repeatability. Measure and record the output frequency of the two turbines and densitometer of the flowmeter under test. Use the time interval determined by the repeatability tests made previously on the Dual-turbine sensor alone.

**Apparatus** - Flow calibration stand with flow measuring sensors, turbine meter for a monitor and the DAP system.
5.4.3.2 **Accuracy**

**Objective** - To determine any biases, calibration shifts or inaccuracies of the prototype over the ranges of flow rate, temperature, density and viscosity.

**Method** - Measure and compare the mass flow rates from the COX 305 or 311H flow calibrator and the prototype with calibration fluid. Also measure volumetric flow rate with the monitor turbines and fluid density with the density standards to provide an alternate means of establishing mass flow rate. The flow calibrators and prototype will be connected to the DAP system for this evaluation. In this set-up, the measurement time interval of the weigh-time stand will gate the measurement intervals of the signals listed in Table 5-3. This ensures that fluctuations of actual flow rate do not cause measurement errors between the various inputs. These input frequencies and the temperature will be averaged over the 30 to 60 second measurement interval prior to calculation of mass flow rate.

Multiple readings will be taken at each of ten flow rates over the 50 to 1 flow range (next higher flow about 50% greater than the present), both upscale and downscale. The same points (flow rates within ±10%) will be run at -55°C, -35°C and +100°C. Percent-of-point error will be calculated at each reading as:

\[
\% \text{ ERROR} = \frac{m_{\text{Prototype}} - m_{\text{Standard}}}{m_{\text{Standard}}} \times 100
\]

The errors will be plotted versus flow rate for each of the three runs (R.T, Hot, Cold).

**Apparatus** - COX 305 and 311 weigh-time flow calibrators, monitor turbines and the DAP system.
5.4.3.3 Vibration Sensitivity

**Objective** - To determine the sensitivity of flow rate performance to vibration inputs.

**Methods** - Mount the flowmeter on a vibration machine by means of a suitable fixture. Pass a constant fuel flow rate of about 25 percent of full scale through the flowmeter. Vary the vibration input over the range specified in the design guidelines and monitor the indicated flow rate from the flowmeter during vibration. Repeat the procedure with vibration inputs along each of three orthogonal axes. During each vibration scan, particular attention will be paid to mechanical resonances and variations of indicated flow.

**Apparatus** - Servo type sinusoidal vibration machine, flow stand, flow sensor to monitor flow input to flowmeter being tested, and DAP system.

5.4.3.4 Attitude Sensitivity

**Objective** - To determine if accuracy is adversely affected by the orientation of the flowmeter.

**Method** - Mount the flowmeter in a selected orientation. Pass a constant fuel flow rate of about 25 percent of full scale through the flowmeter using a standard turbine to monitor flow. Change the orientation of the flowmeter under test and record any changes in mass flow rate output. Repeat the procedure for each orientation desired. The positions to be tested are with axis of flow vertical and with the axis of flow horizontal and the flowmeter rotated 90° between successive orientations.

**Apparatus** - Flow stand, turbine meter to monitor flow, means to hold the flowmeter under test in the desired orientation, and the DAP system.

5.4.3.5 Pressure Drop

**Objective** - To determine the pressure drop across the flowmeter for a range of flow rates up to full scale.

**Method** - Mount the flowmeter with the axis of flow horizontal. Connect a differential pressure meter across the flowmeter. Pass fuel flow through the flowmeter and measure flow rate and differential pressure for each point from low flow to full scale.

**Apparatus** - Flow stand, differential pressure meter, inlet and outlet pipes with pressure taps.
5.4.3.6 **Time Response**

**Objective** - To measure the time constant of the turbine speeds when subjected to step changes in flow rates.

**Method** - The square wave output from both signal conditioners of the main and sensor turbines and the output from a hot film anemometer placed in the flow stream just ahead of the prototype will be recorded on magnetic tape. An inlet pipe fixture with two parallel pipes, each pipe having a throttle valve and one having a snap action valve, will be used both to create a fast step change in flow rate and to control the initial and final flow rates. The recorded tape will be played back at reduced speeds while the outputs are recorded on strip chart paper for detailed analyses.

**Apparatus** - Parallel pipe manifold with valves, tape recorder, strip chart recorder, hot film anemometer system.

5.4.3.7 **Alternate Fuel**

Repeat Accuracy test (5.4.3.2) at room, hot, and cold temperatures with JP-8.

5.4.4 **Data Acquisition and Processing System (DAP)** - The prototype flowmeter has a total of five electrical signal outputs with the ranges and characteristics listed in Table 5-3. Synchronization of the measurement interval for these signals with flow calibrator and monitor turbine signals is essential to obtaining reliable measurements of prototype repeatability and accuracy. Furthermore, the conversion of the signals to mass flow rate through the various calibration functions requires a dedicated computer to obtain meaningful results in a timely fashion (i.e., real time). These requirements were recognized early in the test plan formulation and led to the design of a Data Acquisition and Processing System, herein referred to as the DAP system. Figure 5-13 is a functional block diagram showing the key elements of the system.

Frequency signals are routed to digital counters that output to a digital bus (IEEE 488 compatible, HPIB) and are controlled (synchronized) by the bus. This includes the prototype frequency signals and the monitor turbine frequency signal. The weigh-time interval of the COX 311H flow calibrator and the modulation output of the Densi-viscometer electronics are converted to digital signals through a General Purpose Input/Output Port (GPIO). The RTD resistance is output to the digital bus via a digital multimeter. An HP86A computer controls the data flow and is programmed in BASIC to compute mass flow rates for both the flow calibrator and the prototype. A monitor, disk storage and printer/plotter make the DAP system a complete and versatile tool necessary for the successful development of the high accuracy fuel flowmeter for NASA.
5.5 Fabrication, Tests, and Analyses of Prototype Design

The design and test plan described in Section 5.4 were carried out by fabrication of the prototype design outlined in Appendix E. As expected, several minor design changes were made and test plan was slightly altered. Adjustments to calibration equipment and techniques were also deemed necessary. These changes together with the actual test data and analyses are covered in this section.

5.5.1 Introduction - This portion of the report covers Task 6 and Task 7 of the dual turbine/densi-viscometer concept. The design combines a high accuracy turbine meter with a high accuracy densi-viscometer. The turbine meter provides a precise measurement of volumetric flow rate when the meter is corrected for viscosity effects. The densitometer portion of the densi-viscometer measures fluid density which is used to convert volumetric flow rate to mass flow rate, and the viscometer provides the viscosity information that is needed for the turbine meter viscosity corrections.

The dual turbine/densi-viscometer should satisfy the following specification requirements:

<table>
<thead>
<tr>
<th>Specification</th>
<th>Requirement</th>
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</thead>
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<tr>
<td>Flow Range</td>
<td>0.050 to 2.52 kg/s</td>
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<tr>
<td></td>
<td>(400 to 20,000 lb/hr)</td>
</tr>
<tr>
<td>Accuracy Requirement</td>
<td>± 0.25% of reading</td>
</tr>
<tr>
<td>Accuracy Goal</td>
<td>± 0.10% of reading</td>
</tr>
<tr>
<td>Response-Time Constant</td>
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</tr>
<tr>
<td>Below 10% of Full Scale</td>
<td>100 ms</td>
</tr>
<tr>
<td>Above 10% of Full Scale</td>
<td>25 ms</td>
</tr>
<tr>
<td>Ambient Temperature</td>
<td>-55°C to 130°C</td>
</tr>
<tr>
<td>Fuel Temperature</td>
<td>-55°C to 130°C</td>
</tr>
<tr>
<td>Maximum Fuel Pressure</td>
<td>7000 kPa</td>
</tr>
<tr>
<td></td>
<td>(1000 psi)</td>
</tr>
<tr>
<td>Maximum Pressure Drop</td>
<td>69 kPa</td>
</tr>
<tr>
<td></td>
<td>(10 psi)</td>
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<td>Vibration</td>
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<td>5 to 40 Hz</td>
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<td>14 to 23 Hz</td>
<td>± 1 g</td>
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<td>23 to 90 Hz</td>
<td>± 0.45 mm</td>
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<td>90 to 2000 Hz</td>
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<td></td>
<td>Operating Attitude</td>
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</table>

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5.5.2 Background - A turbine meter is an established method of measuring volumetric flow rate simply, reliably, and repeatably, but it has some limitations. Maximum flow for a given size is limited by maximum allowable bearing speed of about 250 rps. Turbine meters typically have a calibration constant that is linear down to about one-tenth of maximum flow rating, so the specified 50:1 range of mass flow rate (65:1 volumetric flow rate) requires special consideration.

Earlier sections of this report theorized that the calibration curve of a turbine meter could be made more nearly linear for a wider range by including a counter rotating turbine in the flowmeter design. Moreover, the calibration curve would be a single valued function of output frequency divided by kinematic viscosity, so the volumetric flow rate could be determined by measuring turbine frequency and fuel viscosity. By adding a densitometer, mass flow rate could be derived. The densitometer portion of this report presents an approach to derive both density and viscosity information from a proven densitometer design.

The primary goal of Phase II, Task 6 is to determine the validity of the theory of Phase II, Task 1. To do this, a dual turbine flowmeter was designed and built. The turbine meter was calibrated over a range of viscosities and flow rates, and the calibration information was stored in the program of a data acquisition and processing system. The densi-viscometer was calibrated by using fluids of known density and viscosity as references and adjusting the electronic drive and control circuits to give the required outputs.

After each portion had been calibrated separately, the dual turbine and the densi-viscometer were mated into one assembly for testing as a complete flowmeter. The product design and the test program were presented and discussed in the Phase II, Task 5 report detailing the prototype design and test plan. The following sections of this present report on Phase II, Task 6 cover calibration and testing of each of the two portions and of the entire flowmeter.

5.5.3 Dual Turbine Portion - Figure 5-11 shows the dual turbine design. Fuel flowing from left to right first passes through the main turbine (6 blades of 45° helix angle) and then the sensor turbine (6 blades at 23.5° left hand helix). The blades of both turbines are magnetic, so, as each blade passes the pickoff coil, the 45 kHz excitation current is modified. The change in current is detected by the signal conditioning electronics which output one pulse for each blade passing.

One important reason for having the sensor turbine as part of the design is to provide compensation for any swirl that might be in the in-flowing fuel stream. Depending on the direction of rotation of the swirl, it could either increase or decrease the speed of the main turbine. There will be an equal but opposite effect on the counter-rotating sensor turbine, so the effects of swirl should be cancelled when the frequencies of the two are summed.

5.5.3.1 Effects of Swirl - Several tests were made on the dual turbine to determine the effectiveness of the swirl compensation. First the turbine meter was temporarily modified by removing the flow straightener from the inlet end
so that any swirl in the incoming flow stream would affect the operation of the main turbine directly. Then the transmitter was tested to measure the effects of the swirl.

Swirl was generated by a double elbow configuration at the inlet of the dual turbine meter as shown in Figure 5-14. The amount of swirl that was added to the incoming flow by the double elbow arrangement was determined by measuring the "K" factor of the main turbine first with the swirl generator and then with a straight inlet pipe that would have no swirl. The two "K" factors are plotted in Figure 5-15 and show that the swirl affected the main turbine by about 10%. This is enough swirl to give a good indication of the degree of compensation provided by the sensor turbine. Figure 5-16 shows that the sum of the frequencies of the main and sensor turbines, which is the output from the dual turbine, is affected by 2.5 parts in 550, or 0.45%, when 10% swirl is introduced. The swirl compensation thus seems to be effective.

The flow straightener was put back into the inlet of the turbine and the turbine meter was retested to determine if the flow straightener would also remove swirl. The "K" factor of the main turbine was measured with and without the swirl generator at the inlet. Figure 5-17 demonstrates that the flow straightener is very effective in removing swirl because the two curves for tests with swirl and without swirl are indistinguishable from each other.

5.5.3.2 Characterization - After the swirl sensitivity tests had been completed, the dual turbine characterization was started. The purpose was to measure the "K" factor of the dual turbine over the specified mass flow rate range for the specified fuel temperatures and viscosities. The test data are stored in the memory of the Data Acquisition and Processing System. In service, fuel temperature and viscosity are measured by the densi-viscometer so the "K" factor of the dual turbine can be determined from the stored information. Being able to determine the "K" factor means that the turbine meter need not have a precisely linear calibration in order to be used over a wide range of flow rates and still yield accurate results. The turbine meter need only be repeatable, which is an inherent characteristic of turbine meters in general, and have a calibration curve that is single valued and does not show rapid changes over the operating flow range.

The characterization of the dual turbine meter was determined by using a weigh-time stand to measure mass flow rate of calibration fluid for which density and viscosity had been determined over the specified fuel temperature range. The temperature of the calibration fluid was measured at the outlet of the turbine meter so the density and viscosity of the fuel which the turbine meter had measured were known. Volumetric flow rate was calculated by dividing the measured mass flow rate by the density of the fuel. The "K" factor, which is expressed in terms of pulses per cubic meter (or turbine frequency divided by cubic meters per second), was calculated from measured turbine frequency and volumetric flow rate.

A conventional turbine meter was included in the flow loop to act as a monitor in case some anomaly should appear. A schematic representation of the flow loop is shown in Figure 5-18. The flow comes in from the weigh-time flow stand and normally passes first through the dual turbine and then the monitor.
turbine. There is a length of straight pipe, about 40 diameters long, in front of each turbine meter to minimize swirl in the incoming fuel. Valves in the main loop and in a by-pass give flexible control of both steady state and transient flows. There is a calibrated resistance temperature detector (RTD) measuring probe at the outlet of each turbine meter. The frequency outputs from the turbine meters, the resistance measurements of the temperature probes, together with the weight and time from the flow stand are all fed into the Data Acquisition and Processing System where the desired parameters are calculated and printed out.

The turbine meter characteristics were measured for following conditions:

a - Calibration fluid, room temperature
b - Calibration fluid, 100°C
c - Calibration fluid, -35°C (viscosity = 3.5 cs)
d - Calibration fluid, -55°C (viscosity = 8.5 cs)
e - Vacmul oil, room temperature (viscosity = 11 cs)
f - Tellus oil, room temperature (viscosity = 7.3 cs)

The test results for these characterization runs are plotted on several curves:

- Dual Turbine - Figure 5-19
- Main Turbine - Figure 5-20
- Sensor Turbine - Figure 5-21
- Monitor Turbine - Figure 5-22

All of these curves show separations that seem to be viscosity dependent - separations which could introduce serious errors in volumetric and mass flow calculations. In order to identify the cause of these separations, the monitor turbine was sent to an outside facility that regularly calibrates turbine meters. This outside facility could not readily test with hot and cold fuel, but could use fuels that covered a range of viscosity of Figures 5-19 through 5-22.

The results of tests (Figure 5-23) of the monitor turbine at the outside facility are different from those shown in Figure 5-22 for the same turbine meter, and the difference is ascribed to the mass flow measurement equipment. Phase III of the High Accuracy Fuel Flowmeter program addresses the need for the Test and Calibration System (TACS) which has much better flow measurement capability. The TACS as described in Section 3.0 will be available in the fourth quarter of 1984 which is too late for testing the dual turbine/densi-viscometer prototype.

The monitor turbine appeared to be the best means of measuring mass flow rate if accurate density and viscosity were available. Density and viscosity could be obtained by measuring the temperature of pre-characterized fuel. The characterization of the monitor turbine, as determined by measurements at the outside facility, was converted to an eleventh order equation and stored in the data processing system. The characteristic curve that is calculated from this equation is shown in Figure 5-24. The measured points are also plotted in Figure 5-24 to indicate the correlation between the measured points and the calculated curve.
The next step was to re-calculate all the previously measured values of the dual turbine (shown in Figure 5-19) using the monitor turbine curve of Figure 5-24 as the flow standard. Fuel density and viscosity had been determined before the tests of Figure 5-19 through 5-22 were made, and temperature was measured at each flow point, so the fuel characteristics were known for each test point. The re-calculated points for the dual turbine, together with the calculated curve to fit the points, are plotted in Figure 5-25. If the data for -55°C calibration fluid is omitted, the re-calculated points and curve are as in Figure 5-26, and there is much less scatter than in Figure 5-25. The extra scatter of Figure 5-25 is probably associated with temperature errors in the mass flow measurement equipment which is used to obtain the data. The curve of Figure 5-26 was used as the dual turbine characterization curve for the prototype test program that follows.

5.5.4 Mass Flowmeter Tests - After the dual turbine meter and the densi-viscometer had each been calibrated as separate units, the two portions were mated to form a complete flowmeter. The prototype flowmeter was then evaluated by performing the tests that are listed in Section 5.4.3. Test results are presented in the same order in which the tests were made.

5.5.4.1 Pressure Drop - Pressure drop across the flowmeter was measured for several flow rates from 0.25 kg/s (2000 lb/hr) to 2.77 kg/s (22,000 lb/hr). The data were plotted on a log-log scale in Figure 5-27, and the points form a straight line. The pressure drop at 2.52 kg/s (20,000 lb/hr) is 110 kPa (16 psi) as determined graphically from Figure 5-28. That value is about 60% greater than the specified pressure drop of 69 kPa (10 psi) at 2.52 kg/s (20,000 lb/hr). Quoted pressure drop for a turbine meter of the size used and allowing for the second turbine is about 50 kPa (7.3 psi), so a large portion of the pressure drop is across the densitometer portion of the assembly. If the pressure drop is critical and must be brought down to 69 kPa (10 psi), it should be possible to redesign the densitometer housing to give a lower pressure drop.

5.5.4.2 Repeatability - The purpose of the repeatability tests was to find out how many times the flow rate at any calibration point has to be measured in order to be sure, at the 95% confidence level as determined from the student "t" test, that the measured values were correct. Another purpose of repeatability testing was to provide some insight into the quality of the dual turbine sensor by seeing how closely the flow measurements were clustered.

The monitor turbine, the dual turbine, and a weigh-time calibrator were set up to have the same mass flow rate pass through all three units. The flow rate as measured by each unit was recorded 20 times in succession at nominal flow rates of 0.063 (500), 0.63 (5000), 1.26 (10,000), and 2.52 kg/s (20,000 lb/hr) which covers the full rated flow range. These measurements were analyzed statistically, based on the assumption that the actual flow rate was constant, and a summary of these calculations is given in Table 5-4.

The repeatability of the dual turbine as related to the monitor turbine (last column in Table 5-4) is better than for the monitor turbine alone which indicates that the flow rate did not actually remain constant at each flow.
point. The repeatability of the weigh-time calibrator is much poorer than that of the Monitor Turbine which reinforced the decision to use the Monitor Turbine output as the time measure of flow rate.

The last column of Table 5-4 shows that ten readings are enough to provide repeatability of better than 0.05% at any flow rate. Ten or more readings at each flow rate were taken for all later tests that required an accurate flow measurement.

5.5.4.3 Attitude - Flow rate was measured 20 times with approximately 0.63 kg/s (5,000 lb/hr) flow rate through the dual turbine with the flow axis vertical and with the flow axis horizontal and the electrical receptacle positioned at 12, 3, 6, and 9 o'clock. The results are summarized in Table 5-5. The percent errors for the five different orientations are all nearly alike which shows that the flowmeter accuracy is not affected by mounting position. All the errors were positive which were probably caused by a shift in the densi-viscometer calibration.

5.5.4.4 Accuracy - Accuracy was measured by comparing the mass flow rate output of the dual turbine/densi-viscometer to the output of the monitor turbine. The volumetric flow rate of the dual turbine was obtained from the characterization equation that is plotted in Figure 5-26 by using the sum of the main and sensor turbine frequencies divided by the kinematic viscosity, as measured by the viscometer, to determine the turbine "K" factor which in turn gave the volumetric flow rate. The density of the fluid was measured directly by the densitometer and the product of volumetric flow rate times density yielded the mass flow rate as measured by the product under test.

The actual mass flow rate was measured by means of the monitor turbine together with fluid density and viscosity characteristics that had been pre-determined as a function of temperature. Volumetric flow rate came from the curve of Figure 5-24 by using the measured frequency from the Monitor Turbine and kinematic viscosity derived from a temperature measurement of the pre-calibrated fuel in the flowmeter. The fuel density was also obtained from the same temperature measurement of pre-calibrated fuel, and the product provided mass flow rate.

All of the calculations mentioned above were performed by the Data Acquisition and Processing System which also calculated percentage errors for mass flow rate, density, and viscosity. Ten flow rate measurements, each about 11 seconds long, were made at each test flow point and the averages were calculated and printed out by the computer. A typical printout for one test point is shown in Figure 5-28.

The accuracy of the dual turbine/densi-viscometer was measured both upscale and downscale at 25°C, 100°C, -35°C and -55°C using MIL-C-7024A, Type II calibration fluid for flow rates from 0.050 kg/s (400 lb/hr) to 2.52 kg/s (20,000 lb/hr). At high flow rates, fluid flow forces affected the operation of the densi-viscometer giving invalid outputs of density and viscosity. Figure 5-29 is a plot of the transmitter error at room temperature from 0.050 kg/s (400 lb/hr) to 1.76 kg/s (14,000 lb/hr). Above that flow rate, the densi-viscometer output was unreliable so the 2.52 kg/s (20,000 lb/hr) point
was not plotted. Although the flowmeter error does not remain within ±0.25 percent specification limit for the entire flow range, the error is within limits for most of the flow range and is only slightly out at the lowest and highest portions. The mass flow rate error curve is divided into measured density and calculated volumetric flow rate error curves in order to understand the source of errors. Figure 5-29 shows that there is virtually no error in the densitometer measurement and that most of the flow rate error is due to the measurement of volumetric flow rate. It is expected that the volumetric flow rate measurements from both the monitor turbine and the Dual Turbine, will be much improved when TACS is available so that the mass flow rate measurement from the Dual Turbine/Densi-viscometer will be within ±0.25%.

Accuracy at 100°C is shown in Figure 5-30, again for the flow range of 0.050 kg/s (400 lb/hr) to 1.76 kg/s (14,000 lb/hr). Again the mass flow rate is not far above the ±0.25% specification limit and should improve when the new calibrator is available. The density measurement error also increases and is an important reason that the mass flow rate is 0.3 to 0.4% above 0.25%g/s (2000 lb/hr).

Figure 5-31 for -35°C fuel and Figure 5-32 for -55°C fuel show a similar density measurement error which is about 1% too high over the full flow range. For both -35°C and -55°C, the volumetric flow rate is also out of limits for portions of the flow range and contributes to the mass flow error. Much of the error in volumetric flow results from the errors in viscosity measurement which are shown in Figure 5-33. An error in viscosity means that the wrong value of the Hz/cs will be used when determining the "K" factor from Figure 5-26. This effect is particularly noticeable for the -35°C tests, Figure 5-31.

Volumetric flow rate equals the sum of the turbine frequencies divided by the "K" factor, so if the calculated "K" factor is too small, the volumetric and mass flow rates will be too large. The measured sum of the frequencies from the Dual Turbine at 0.25 kg/s (2000 lb/hr) mass flow rate at -35°C was 174 Hz and the measured kinematic viscosity was 5.6 centistokes which gives a value of Hz/cs equal to 31. This is just at the maximum "K" factor point of Figure 5-26. Since the viscosity measured by the Densi-viscometer is too high, and because the "K" factor curve of Figure 5-26 falls off sharply below the maximum point, the calculated value of the Hz/cs will be too low, the derived "K" factor will also be too low and the flow rate will be too high. The steep increase in flow rate error in Figure 5-31 below 0.25 kg/s (2000 lb/hr) reflects this effect.

The error at -55°C, Figure 5-32 also shows the effects of viscosity error. The peak "K" factor again comes at 0.25 kg/s (2000 lb/hr) where the sum of turbine frequencies equals 175 Hz, the measured viscosity equals 6.0 cs, and Hz/cs equals 29. For smaller flow rates, measured viscosity remains too large which gives a "K" factor that is too low and leads to an increasingly positive flow rate error with decreasing flow rate.

The analysis of anticipated dual turbine performance that was presented in the Phase I report indicated that the "K" factor curve for the dual turbine would be flatter than test data have shown it to be, meaning that an accurate
measurement of viscosity would not be needed. The results shown in Figure 5-31 and 5-32 indicate that the "K" factor curve (Figure 5-26) must be made flatter, or viscosity must be measured more accurately, or both must be done. The repeat tests to be made when the new flow calibration system is available will help to determine how accurate the viscosity measurement must be.

Figures 5-31 and 5-32 also show that the densitometer has a large error at cold temperatures, and that the temperature error contributes greatly to the mass flow rate error. The subject of the densi-viscometer errors is treated in Section 7.0 of this report.

5.5.4.5 Vibration Sensitivity - This test was to see if the performance of the dual turbine/densi-viscometer changed when it was subjected to sinusoidal vibration inputs along any of the three main axes. The vibration inputs were:

- 5-14 Hz
- 14-23 Hz
- 23-90 Hz
- 90-2000 Hz

A constant flow rate of approximately 25% of full scale was maintained through the flowmeter while the vibration frequency was changed up to 2000 Hz and back down to 5 Hz. The main turbine and the sensor turbine output frequencies and the densitometer output as well as the flow rate output, were monitored throughout the vibration scans in order to determine how vibration would affect the operation of the flowmeter. In addition, an output accelerometer was fastened to the flowmeter so that mechanical resonances could be measured. The three directions of vibration input and the mechanical resonance test results are shown in Figure 5-34. All resonances occur at relatively high frequencies and the amplifications are low so there should not be vibration induced structural fatigue problems.

The operational flow data showed that the main and sensor turbine frequencies were unaffected by vibration but the densitometer had a large vibration induced error for vibration frequencies greater than about 45 Hz. This is discussed in greater detail in the densi-viscometer portion of this report.

Flowmeter accuracy was measured after all vibration tests were completed and is plotted in Figure 5-35. A comparison of Figure 5-35 to the room temperature test before vibration, Figure 5-29, shows that the densitometer output has increased by about 0.25% but that volumetric flow rate curves are very similar which indicates that the dual turbine meter calibration was not permanently affected by temperature and vibration stresses.

5.5.4.6 Alternate Fuel - The MIL-C-7024A Type II calibration fluid was removed from the flow stand and refilled with JP-5 fuel to see if the Dual Turbine/Densi-viscometer flowmeter was capable of measuring the rate of flow of fuel having different density and viscosity characteristics.
Figure 5-36 shows the accuracy at room temperature with JP-5 and should be compared to Figure 5-35 which was the preceding room temperature curve with calibration fluid. All three curves - mass flow, volumetric flow, and density - of Figures 5-35 and 5-36 look similar to each other showing that there is little error with an alternate fuel. Comparing Figure 5-37 which is the JP-5 curve at 100°C with Figure 5-30 shows some discrepancies, but if the permanent changes in the densi-viscometer caused by temperature and vibration are considered, the discrepancies in the flowmeter are greatly reduced.

Near the start of tests at -55°C with JP-5, the flow stand suffered serious damage and the testing program had to be halted before measurements could be made with JP-5 at -55°C and -35°C.

5.5.4.7 Time Response - Response time of an instrument can be measured by putting a step input in and measuring the output versus time. It is difficult to produce an abrupt change in flow rate to simulate the step input. If it is possible to measure actual flow by using some sort of fast responding auxiliary equipment, then the time response of the flowmeter under test can be determined by comparing flowmeter output to the fast response measurement.

It was planned to measure the time response of the dual turbine/densi-viscometer prototype by using a hot wire anemometer probe to monitor actual flow rate. A great deal of time and effort was spent trying to obtain usable signals from the hot wire anemometer, but the output was always too noisy to be useful, and the anemometer approach was abandoned.

A more successful approach to measuring response time was made by opening a quick-opening valve upstream from the flowmeter and recording the output from the Main Turbine signal conditioning electronics. A typical frequency trace is shown in Figure 5-38. The time constant of the response curve from the trace (Figure 5-39) is approximately 25 ms, but the change in flow rate was probably far from being instantaneous.

Other considerations indicate that the response of a turbine meter is much faster than 25 ms. An article by M.R. Shafer entitled "Performance Characteristics of Turbine Meters" and published in the ASME Journal of Basic Engineering shows several time response curves which were plotted from experimental data. These curves are reproduced in Figure 5-40 and show a time constant of about 5 ms. This is probably typical for small turbine meters.

The data for the curve of Figure 5-40 was obtained by recording and plotting the peak voltage of each output pulse of an induced voltage type pickoff. It had previously been determined that the voltage level was directly proportional to speed, so the peak value was a measure of instantaneous turbine speed. The data for Figure 5-39 was derived from frequency recordings and each point contains one half of the time for the turbine to turn from one blade to the next. In practice, the response time would contain the full time for the turbine to turn through the angle between two adjacent blades, and at slow turbine speeds this would be the most important element in the response time. For example, at 0.071 kg/s (560 lb/hr), the
main turbine output frequency measured about 40 Hz which is a time interval of 25 ms between successive blade passings. It appears, then, that even if the turbine responds in 5 ms or so, the time to obtain that information may be much greater and may be the limiting factor.

5.6 Conclusions and Recommendations

5.6.1 Conclusions — Test results indicate that the dual turbine concept does not offer an advantage over a conventional flow straightener for eliminating the effects of swirl in the incoming flow stream.

The "K" factor of both the monitor turbine and the dual turbine is a single valued function of turbine frequency divided by kinematic viscosity for room temperature fuel.

Since the dual turbine/densi-viscometer concept requires that each turbine meter be accurately mathematically modeled based on test data, a very accurate flow test facility is essential to characterize the turbine and to test the complete flowmeter.

Fuel viscosity must be accurately measured if errors at low flow and high viscosity must be kept small.

Although the dual turbine/densi-viscometer flowmeter had errors greater than 0.25% for a number of test conditions, tests with room temperature and 100°C fuel were very encouraging.

5.6.2 Recommendations — The dual turbine seems to offer no advantage in accuracy or swirl compensation and has a slower response time. Consider using only the main turbine to measure flow rate but retain the sensor turbine to provide an auxiliary output to measure bearing degradation. When the new high accuracy test and calibration system is operational, use it to characterize the dual turbine and to evaluate the complete flowmeter.
<table>
<thead>
<tr>
<th>TABLE 5-1</th>
<th>STANDARDS FOR PROTOTYPE EVALUATION</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>MASS FLOW RATE</strong></td>
<td>Weigh-Time Flow Calibrators</td>
</tr>
<tr>
<td>CoK 311H</td>
<td>CoK 305.</td>
</tr>
<tr>
<td><strong>VOLUMETRIC FLOW RATE</strong></td>
<td>Turbine flowmeters</td>
</tr>
<tr>
<td>0.64 liter/sec (10 gpm) maximum flow</td>
<td>Nominal 1.3 cm (0.5 in.) size</td>
</tr>
<tr>
<td>3.8 liters/sec (60 gpm) maximum flow</td>
<td>Nominal 2.5 cm (1.0 in.) size</td>
</tr>
<tr>
<td><strong>DENSITY</strong></td>
<td>Mettler-PAAR Densitometer</td>
</tr>
<tr>
<td>DMA 60 Processing Unit</td>
<td>DMA 602HT Density Measuring Cell</td>
</tr>
<tr>
<td><strong>TEMPERATURE</strong></td>
<td>Platinum RTD Sensor</td>
</tr>
<tr>
<td><strong>VISCOSITY</strong></td>
<td>Cannon-Ubbelohde Kinematic Viscometers</td>
</tr>
<tr>
<td>Suspended Level Type</td>
<td>Certificate of Calibration from Mfg.</td>
</tr>
<tr>
<td>Four Ranges, 0.5 to 30 cs.</td>
<td></td>
</tr>
</tbody>
</table>
### TABLE 5-2  DENSITY AND VISCOSITY RANGES

Ranges for JP-5, JP-4

JET-A, Jet A-1; JP-8

Simulated at 25°C with Fluid Mixture

<table>
<thead>
<tr>
<th>Temp (°C)</th>
<th>Viscosity (cS)</th>
<th>Density (gm/cm³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>-55</td>
<td>Min. 7.0</td>
<td>Min. 0.80</td>
</tr>
</tbody>
</table>
|           | Max. 18.0      | Max. 0.90        | Tellus #10 + Freon TMC
|           |                |                  | Tellus #10
| 20°       | Min. 1.1       | Min. 0.74        | Cal. Fluid + Heptane
|           | Max. 2.2       | Max. 0.85        | Tellus #10 + Heptane
| +130      | Min. 0.38      | Min. 0.65        | Cal. Fluid + Heptane
|           | Max. 0.64      | Max. 0.77        | Pentane

### TABLE 5-3  PROTOTYPE OUTPUT SIGNAL CHARACTERISTICS

<table>
<thead>
<tr>
<th>Signal</th>
<th>Range</th>
<th>Amplitude</th>
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</thead>
<tbody>
<tr>
<td>Main Turbine Frequency</td>
<td>24 to 1600 Hz</td>
<td>0 to 5V Square Wave</td>
</tr>
<tr>
<td>Sensor Turbine Frequency</td>
<td>12 to 800 Hz</td>
<td>0 to 5V Square Wave</td>
</tr>
<tr>
<td>Densi-viscometer Frequency</td>
<td>4500 to 6000 Hz</td>
<td>0 to 5V Square Wave</td>
</tr>
<tr>
<td>Resistance (Temperature)</td>
<td>76 to 150 Ohms</td>
<td>0.385 Ω/°C</td>
</tr>
<tr>
<td>Densi-viscometer Frequency</td>
<td>Two wire logical</td>
<td>0 to 5 V Output</td>
</tr>
</tbody>
</table>
### Table 5-4  Repeatability

**Percent Deviation from Mean - 95% Confidence Level**

<table>
<thead>
<tr>
<th>Number of Tests</th>
<th>Weigh-Time Calib (Mass Flow Rate) + %</th>
<th>Monitor Turbine (Mass Flow Rate) + %</th>
<th>Dual Turbine Freq Monitor Turbine Freq + %</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.063 kg/s (500 lb/hr)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>0.93</td>
<td>0.15</td>
<td>0.088</td>
</tr>
<tr>
<td>10</td>
<td>0.75</td>
<td>0.083</td>
<td>0.046</td>
</tr>
<tr>
<td>20</td>
<td>0.55</td>
<td>0.057</td>
<td>Not calculated</td>
</tr>
<tr>
<td>0.63 kg/s (5000 lb/hr)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>0.41</td>
<td>0.084</td>
<td>0.093</td>
</tr>
<tr>
<td>10</td>
<td>0.26</td>
<td>0.038</td>
<td>0.038</td>
</tr>
<tr>
<td>20</td>
<td>0.15</td>
<td>0.022</td>
<td>Not calculated</td>
</tr>
<tr>
<td>1.26 kg/s (10,000 lb/hr)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>0.20</td>
<td>0.094</td>
<td>0.022</td>
</tr>
<tr>
<td>10</td>
<td>0.13</td>
<td>0.046</td>
<td>0.018</td>
</tr>
<tr>
<td>20</td>
<td>0.092</td>
<td>0.031</td>
<td>Not calculated</td>
</tr>
<tr>
<td>2.52 kg/s (20,000 lb/hr)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>0.15</td>
<td>0.038</td>
<td>0.023</td>
</tr>
<tr>
<td>10</td>
<td>0.087</td>
<td>0.029</td>
<td>0.011</td>
</tr>
<tr>
<td>20</td>
<td>0.059</td>
<td>0.019</td>
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### TABLE 5-5 ATTITUDE SENSITIVITY

<table>
<thead>
<tr>
<th>Installed Position</th>
<th>Indicated Mean Flow Rate</th>
<th>Error</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Monitor Turbine kg/s</td>
<td>Dual Turbine kg/s</td>
</tr>
<tr>
<td>Horizontal - 12 o'clock</td>
<td>0.6374</td>
<td>0.6385</td>
</tr>
<tr>
<td>Horizontal - 3 o'clock</td>
<td>0.6342</td>
<td>0.6357</td>
</tr>
<tr>
<td>Horizontal - 6 o'clock</td>
<td>0.6324</td>
<td>0.6335</td>
</tr>
<tr>
<td>Horizontal - 9 o'clock</td>
<td>0.6306</td>
<td>0.6316</td>
</tr>
<tr>
<td>Vertical</td>
<td>0.6373</td>
<td>0.6386</td>
</tr>
</tbody>
</table>

(Average of 80 measurements)

Note: Twenty (20) measurements were made in each of four (4) positions with flow axis vertical.
Section 5-8

FIGURES
FIGURE 5-1 SWIRL APPARATUS FOR TURBINE BLADE AND ANGULAR MOMENTUM ROTOR
Figure 5-9 Model of Turbine Flowmeter

- Rear Bearing Support
- Shaft Lock
- Pickoff Fittings
- Separator
- Turbine Rotor
- Inlet Body
- Outlet Body
- Sensor Turbine
FIGURE 5-5 K VS FLOWRATE FOR THE ENGINEERING MODEL SHOWING THE EFFECTS OF SWIRL ON K.
FIGURE 5-9  DUAL-TURBINE DENSI-VISCOMETER
PROTOTYPE FLOWMETER

FLOWMETER

FLOW

ELECTRONICS

DUAL-TURBINE HALF

DENSI-VISCOMETER HALF

TURBINE SIG. COND.

TURBINE SIG. COND.

Densi-Viscometer Electronics

20' Cables w/Connectors (2)

+28VDC Power

Outputs

FREQ.

FREQ.

Resistance (Temp.)

FREQ

Modulation

±15VDC Power
FIGURE 5-12 TEST APPARATUS FOR CALIBRATING THE DENSI-VISCOMETER OVER THE TEMPERATURE RANGE
Figure 5-13 Data Acquisition and Processing System (DAP System)
FLOW LOOP SCHEMATIC

FIGURE 5-18  FLOW LOOP SCHEMATIC
FIGURE 5-19  CHARACTERIZATION OF DUAL TURBINE WITH DIFFERENT FLUID AT VARIOUS TEMPERATURES
FIGURE 5-21  CHARACTERIZATION OF SENSOR TURBINE WITH DIFFERENT FLUID AT VARIOUS TEMPERATURES
FIGURE 5-23  CHARACTERIZATION OF MONITOR TURBINE WITH DIFFERENT FLUID AT ROOM TEMPERATURE.
MONITOR TURBINE

Calculated curve to fit test data from tests at outside facility

FIGURE 5-24 CHARACTERIZATION OF MONITOR TURBINE PERFORMED AT OUTSIDE FACILITY
FIGURE 5-25 CHARACTERIZATION OF DUAL TURBINE AT VARIOUS TEMPERATURES
TEMPDENSREF = 0
DENSIREF = 780.5368
DENSALPHA = .773772

YOUR PROGRAM IS FINALDVT1

THE NAME OF YOUR FILE IS FINRT11/14

YOUR FLOWSTAND S/N IS 100251

THIS FLOWMETER IS DUAL TURB ROOM TEMP FINAL TEST

THE OPERATOR IS MR. LINGEL

THIS TEST IS RUN ON NOVEMBER 14, 1983

***************************************************************

YOUR TEST POINT IS APPROXIMATELY 400 PPH

THE WEIGHT IS 1.5 LB

THE TARE IS 3 INCHES

-----------------------------------------------------------------

<table>
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<tr>
<th>DVFPSS</th>
<th>DVFNNEG</th>
<th>MONITOR</th>
<th>MAIN</th>
<th>SENSOR</th>
<th>SUMTURB</th>
<th>DVTTEMP</th>
<th>MONITOR TEMP</th>
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<tr>
<td>5108.12</td>
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<td>27.937</td>
<td>28.438</td>
<td>10.333</td>
<td>38.771</td>
<td>20.94</td>
<td>21.54</td>
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</tbody>
</table>

YOU HAVE MADE 10 RUNS AT THIS TEST POINT

THE FOLLOWING ARE YOUR TOTAL OUTPUTS

<table>
<thead>
<tr>
<th>COX-PH</th>
<th>MON-PH</th>
<th>DVT-PH</th>
<th>PPH-PER</th>
<th>IL-DEN</th>
<th>DV-DEN</th>
<th>DEN-%</th>
<th>IL-VIS</th>
<th>DV-VIS</th>
<th>VIS-%</th>
</tr>
</thead>
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<tr>
<td>413.5</td>
<td>413.1</td>
<td>410.9</td>
<td>-.53</td>
<td>764.01</td>
<td>764.26</td>
<td>.03</td>
<td>1.2720</td>
<td>1.3112</td>
<td>3.08</td>
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<td>412.1</td>
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<td>1.2714</td>
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<td>1.2705</td>
<td>1.3104</td>
<td>3.14</td>
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<tr>
<td>411.4</td>
<td>413.4</td>
<td>444.0</td>
<td>7.39</td>
<td>763.92</td>
<td>764.14</td>
<td>.03</td>
<td>1.2700</td>
<td>1.3089</td>
<td>3.06</td>
</tr>
<tr>
<td>415.7</td>
<td>418.9</td>
<td>417.8</td>
<td>-.26</td>
<td>763.91</td>
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<td>.03</td>
<td>1.2697</td>
<td>1.3083</td>
<td>3.05</td>
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<tr>
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<td>-.32</td>
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<td>.03</td>
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<td>1.3076</td>
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<tr>
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<td>-.14</td>
<td>763.88</td>
<td>764.10</td>
<td>.03</td>
<td>1.2690</td>
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<td>-.14</td>
<td>763.87</td>
<td>764.09</td>
<td>.03</td>
<td>1.2688</td>
<td>1.3078</td>
<td>3.07</td>
</tr>
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</table>

<table>
<thead>
<tr>
<th>FIGURE 5-28 TYPICAL COMPUTER OUTPUT OF ACCURACY ANALYSIS</th>
</tr>
</thead>
<tbody>
<tr>
<td>187</td>
</tr>
</tbody>
</table>
ACCURACY

Temperature: 25°C

- Mass Flow Rate
- Volumetric Flow Rate
- Density

FIGURE 5-29  TRANSMITTER ACCURACY AT ROOM TEMPERATURE
FIGURE 5-32  TRANSMITTER ACCURACY AT -55°C
FIGURE 5-33 VISCOSITY ERROR AT VARIOUS TEMPERATURES
**Figure 5-34** Input and Output Data of Vibration Test

**Transverse Vibration**

- **Mechanical Resonances:**
  - Hz: 757
  - Input: 15 g's
  - Output: 23 g's
  - Hz: 1818
  - Input: 15 g's
  - Output: 47 g's

**Longitudinal Vibration**

- **Mechanical Resonances:**
  - Hz: 826
  - Input: 15 g's
  - Output: 28 g's
  - Hz: 1446
  - Input: 15 g's
  - Output: 26 g's

**Vertical Vibration**

- **Mechanical Resonances:**
  - Hz: 1844
  - Input: 15 g's
  - Output: 52 g's
FIGURE 5-36 TRANSMITTER ACCURACY WITH JP5 FUEL
MAIN TURBINE
39.5 Hz (MIN FLOW)
344.2 Hz (MAX FLOW)
40 in./sec
.01 sec/div
1/25/84

TRANSIENT RESPONSE
TRACE OF PICKOFF OUTPUT

FIGURE 5-38 TRANSIENT RESPONSE OF MAIN TURBINE
FIGURE 5-39  RESPONSE OF MAIN TURBINE TO RAPID CHANGE IN FLOW RATE
FIGURE 5-40  RESPONSE OF A TYPICAL 1/2 INCH SIZE TURBINEMETER TO THREE DIFFERENT STEP FUNCTIONS
6.0 **ANGULAR MOMENTUM FLOWMETER**

This section describes the experimental and analytical investigations, the prototype construction, and evaluation performed on the angular momentum flowmeter concept under Tasks 2 through 7 of Phase II of NASA contract No. NAS3-22139 to develop a High Accuracy Fuel Flowmeter.

6.1 **Introduction**

The flowmeter as shown in Figure 6-1 is essentially a single element angular momentum flowmeter. Straightened flow enters the long straight passages of a motor driven rotor where the entire flow achieves the same rotational speed. The torque required to accelerate the flow to this rotational speed is proportional to the product of the mass rate of flow and the rotor speed. This torque turns the rotor relative to its drive shaft until balanced by the torque of the rotor spring. This angle, which is proportional to the product of mass flow rate and rotor speed, is measured by the time difference between the passage of a reference point on the drive shaft and a similar point on the rotor. The two reference points are aligned at zero flow rate. Since the time required for the rotor to traverse the deflection angle is proportional to that angle divided by the rotor speed, the speed term cancels from the equation, and the time difference is directly proportional to mass flow. A viscosity shroud rotating with the rotor prevents viscous drag from introducing an error into the time delay. By driving the viscosity shroud through a precision spring similar to that driving the rotor, and measuring its deflection relative to the same reference on the drive shaft, viscosity can be measured. Viscous drag between the outer diameter of the shroud and the housing deflects the shroud spring resulting in a time based signal analogous to that for mass flow. A Reynolds number correction can also be performed by the microcomputer, further improving the accuracy of the measurement.

Since the response time of the spring-mass system described is high (approximately 1 second), a free spinning turbine element is added upstream of the flowmeter. The fast response rate of the turbine is combined with the overall accuracy of the mass flowmeter to meet the requirements of the specification.

6.2 **Experimental and Analytical Investigation Plan Formulations**

To evaluate the design concept of the angular momentum flowmeter and its potential in meeting NASA requirements, the following areas for investigation were identified in Phase I, to be conducted in Task 4:

1. Spring Characteristics
2. Rotor Blade Geometry
3. Inlet Geometry and Flow Profiles Versus Reynolds Number
6.2.1 Spring Characteristics

Problem - The following effects directly influence the accuracy of an angular momentum flowmeter:

- Thermo-elastic coefficient (T.E.C.)
- Hysteresis
- Mounting

The most important is T.E.C. which is a combination of modulus and expansion effects with temperature and which can produce significant temperature dependences if not properly controlled. Stability of T.E.C. over long periods of time (months) is also of interest here.

Solution Approach - A spring test fixture (Figure 6-2) will be built. This fixture provides an overall indication of spring performance in an actual flowmeter installation by using a production shaft, spring and rotor. The spring material will be NI-SPAN-C alloy 902. Spring thickness and heat treat temperature will be varied over the following ranges to determine where improvements can be made:

Thickness: 0.25 to 0.51 mm (0.01 to 0.04 in.), four thicknesses
Heat Treat Temperatures: 649°C (1200°F) to 871°C (1600°F)

6.2.2 Rotor Vane Geometry

Problem - The optimal design of rotor vanes depends on better understanding of the following effects:

Surface Roughness - The effects on boundary layer thickness and drag coefficient versus surface condition and imperfections.

Trailing & Leading Edge Sharpness - Critical to rotor vanes in angular momentum type flowmeters; proven to have large effect on skew stability versus Reynolds number (based on fluid passage hydraulic diameter) but not well understood.

Passage Length - What length and aspect ratio are needed to assure repeatable momentum capture over range of Reynolds number (based on fluid passage hydraulic diameter)? In angular momentum flowmeters at low flows, flow deflection angle is large (70°) and requires long passages to settle out eddys. Is minimum Reynolds number design the best? (see Figure 6-3).
Secondary Rotational Flow – Between the vanes of the angular momentum rotor there exists momentum exchange due to rotational flow. (see Figure 6-3). Means to reduce this flow must be evaluated.

Solution Approach – A large scale clear plastic model (Figure 5-1) will be built. The rig consists of a variable speed, motor driven, upstream swirler section and a downstream section where the stationary test item is observed and where measurements are to be made. The following measurements will be made with this apparatus:

1) Axial and tangential velocity via hot film anemometers.
2) Blade/vane pressure distribution via multiple ports and high accuracy pressure sensor.
3) Flow patterns with dye injection and high speed movies.

The following tests will be conducted:

Surface Roughness: Using one vane, measure boundary layer versus Re for
- ground and polished
- sand (various grits)

Trailing & Leading Edge Effects:
- measure tangential flow downstream of vane.
- photograph wake with dye injection.
- determine effect of boundary layer.
- 10° end
- 30° end
- 0° end
- 12° taper

Passage Length:
- Measure pressure profile along vane centerline, inside and outside diameters, for the following Reynolds numbers and swirl ratios. (see Figure 6-4)

<table>
<thead>
<tr>
<th>Re</th>
<th>Swirl Ratio (V_r/V_a)</th>
</tr>
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<tbody>
<tr>
<td>4,000</td>
<td>0.1 to 3.0 in 4 steps</td>
</tr>
<tr>
<td>8,000</td>
<td>0.1 to 3.0 in 4 steps</td>
</tr>
<tr>
<td>16,000</td>
<td>0.1 to 3.0 in 4 steps</td>
</tr>
<tr>
<td>32,000</td>
<td>0.1 to 3.0 in 4 steps</td>
</tr>
<tr>
<td>64,000</td>
<td>0.1 to 3.0 in 4 steps</td>
</tr>
</tbody>
</table>
Secondary Rotational Flow: — Observe flow with dye injection techniques for the following vane geometries in aspect ratio (ratio of passage height to mean passage width):

<table>
<thead>
<tr>
<th>Aspect Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>4</td>
</tr>
<tr>
<td>2</td>
</tr>
<tr>
<td>1</td>
</tr>
<tr>
<td>0.5</td>
</tr>
</tbody>
</table>

6.2.3 **Inlet Geometry and Flow Profiles Versus Reynolds number**

Problem — Inlet design has a large effect on the profile of flow entering the rotor. Unpredictable changes in profile with Re change the radius of gyration and thus meter accuracy.

Solution Approach — A large scale model of the present inlet design (see Phase I Report) will be constructed with clear plastic (see Figure 6-5). Flow profiles will be plotted versus Re, and analyzed for change in radius of gyration.

6.3 **Experimental and Analytical Investigations**

There are three major areas of investigation for the angular momentum flowmeter, namely, the spring characteristics, the rotor geometry, and the inlet geometry. The test equipment, models and set-ups for each of these areas of investigation are described in detail. Test results are also presented and discussed in subsequent sections to address all the significant findings and merits of the design.

6.3.1 **Equipment Set-up and Test Procedures**

6.3.1.1 **Spring** — The spring characteristics study involved heat treating nine springs of 0.46 mm (0.018 in.) thick at temperatures of 500°C, 666°C and 732°C (932°F, 1230°F and 1350°F). This spring thickness was chosen to best simulate the operating range of the prototype flowmeter. The medium temperature 666°C (1230°F) is the optimal temperature for minimum TEC recommended by the manufacturer. Tests were performed using existing high performance spring calibration equipment and each spring was tested upscale and downscale three times with a maximum wind-up angle of 180 degrees.

6.3.1.2 **Rotor-Vane Geometry** — A large scale rotating model (Figure 6-6) was constructed for the rotor-vane geometry study. This rig consisted of a variable speed, motor driven, upstream swirler section and a downstream section where the stationary test item could be observed and flow measurements made. The following measurements were performed using this apparatus:
a) Pressure profile along an adjacent pair of vanes via multiple ports and high accuracy pressure sensor for different flow parameters. See Figure 6-7.

b) Velocity profiles across two adjacent vanes via hot film anemometer for different parameters.

c) Velocity profiles across two adjacent vanes having their trailing edges tapered.

d) Velocity profiles across two adjacent vanes having different degree of surface roughness.

The different flow parameters under consideration were Reynolds number, angle of attack, and aspect ratio (or solidity ratio).

6.3.1.3 **Inlet Geometry Study** - The inlet geometry study utilized a two dimensional scale model (Figure 6-8) for velocity profile assessments. The model is made of plexiglass and velocity profiles were measured using a hot film anemometer.

6.3.2 **Test Results and Discussion**

6.3.2.1 **Springs** - Each of the nine springs was tested (and two were found defective) by measuring the torque versus angle of deflection at every ten degrees up to 180 degrees. Each test was repeated upscale and downscale three times and linear regression analysis was performed. The deviation of upscale and downscale data points from their corresponding torque values were normalized as percentage of point error and plotted versus angle of deflection. Tests were performed on springs heat treated at temperatures of 500°C (932°F), 666°C (1230°F) and 732°C (1350°F), and results are as shown in Figures 6-9 through 6-15. The solid line shows the upscale nonlinearity while the dotted line shows that of the downscale. The difference between these two lines is the hysteresis of the spring and spring tester.

The average hysteresis at the mid-point and the nonlinearity of the seven springs are tabulated in Table 6-1 and the averages for each heat treating temperature are tabulated in Table 6-2. The average mechanical hysteresis is much lower at low heat treating temperatures than at high heat treating temperatures. This agrees very closely with the manufacturer's data for this kind of spring material (NI-SPAN-C alloy 902). The average nonlinearity, however, does not exhibit a clear trend of its dependance on heat treating temperature. But on the average, a nonlinearity of about 0.2% of point value can be expected for this spring material. This nonlinearity is an inherent source of error in flowmeter performance. But it can be easily compensated for in the proposed angular momentum flowmeter by microprocessor technology. The calibration curve of the flowmeter which includes the effect of the spiral spring can be stored in memory and retrieved during the operation of the flowmeter, thus eliminating any system calibration error caused by this nonlinearity. However, the mechanical hysteresis can be minimized but cannot be eliminated as error source.
6.3.2.2 Rotor-Vane Geometry

6.3.2.2.1 Pressure Distribution - The pressure distributions along two adjacent vanes (see Figure 6-7) were measured under different conditions, namely, aspect ratio ($A_R$), Reynolds number ($Re$) and angle of attack ($\alpha$). The static pressure ($P_{tap}$) along the passage referenced to system inlet static pressure was normalized by the inlet dynamic pressure ($pV^2/2$). This pressure coefficient ($P_{tap} - P_s)/(pV^2/2$) was plotted versus the nondimensionalized passage length ($X/L$) as shown typically in Figure 6-16. The solid line represents the pressure distribution of the leading surface of the incoming flow while the dotted line represents that of the trailing surface.

As fluid enters the channel, it becomes separated at the trailing surface of the leading edge and, depending on the flow conditions, this separation will propagate downstream or re-attach to the surface after a certain entrance distance. When the flow passage has a very large aspect ratio ($A_R = 3.7$) as shown in Figures 6-16, 6-17 and 6-18, fluid always gets re-attached to the surface after about 20% of the passage length. This distance decreases with decreasing flow angle. The pressure coefficient, on the average, is about 2% higher on the trailing surface than the leading surface at the end of the passage. This agrees with the fact that fluid on the leading surface has a high velocity due to the incoming flow angle, and the channel is not long enough to allow the flow to become fully developed. Again, this difference in pressure coefficient decreases with decreasing flow angle.

When the aspect ratio is decreased to 1.5 (Figures 6-19, 6-20, 6-21), the separation distance increases to about 30%. The difference in pressure coefficient at the channel exit ranges from 12% at $\alpha = 13.1^\circ$ (Figure 6-19) to 17% at $\alpha = 27.6^\circ$ (Figure 6-20) at the same Reynolds number. This pressure coefficient increases to about 25% when the Reynolds number is reduced while the angle of attack remains about the same (Figure 6-20 and 6-21).

When the aspect ratio is further reduced to 0.69, fluid tends to remain separated throughout the whole length of the passage under all flow conditions.

An interesting phenomenon about the pressure coefficient is that it remains negative throughout the passage at $A_R = 3.7$ (Figure 6-16) and yet it is positive at $A_R = 1.6$ (Figure 6-19) or 0.69 (Figure 6-22) except at the very short separation region at the inlet. Theoretically, the pressure coefficient should be zero at the inlet for non-rotating flow, if the system static pressure is used as a reference. Furthermore this pressure coefficient should decrease along the flow passage as surface roughness induces head loss. The pressure coefficients for $A_R = 1.5$ and 0.6 are higher because the incoming rotating fluid has converted the swirl component of velocity head into static pressure resulting in higher pressure coefficients. When the aspect ratio is increased to 3.7, however, the blockage effect of the vane thickness becomes more prominent resulting in a head loss at the channel entrance. This head loss is larger than the gain from the swirl component and the net result is a lower than zero pressure coefficient.
It was pointed out earlier that there is always a separation zone at the channel entrance caused by the swirl component of incoming fluid. One possible solution to reduce this separation length is to apply boundary layer suction techniques, which can be accomplished by cutting slots on the rotor vane at some distance from the entrance during rotor fabrication. The pressure difference across the vane can be greatly reduced and this will enhance the symmetry of the pressure distribution across the channel. This technique could reduce the large \( \frac{L}{D_h} \) requirement and the pressure drop could also be decreased.

6.3.2.2.2 Velocity Profiles — The axial velocity profiles at the trailing edge of two adjacent vanes were measured using a hot-film anemometer for two different aspect ratios, three different Reynolds numbers and three different angles of attack (defined as \( \tan^{-1}\frac{V_T}{V_a} \) in Figure 6-4). The measured velocities \( u \) were normalized to the maximum channel velocity \( U \) and plotted against the nondimensionalized channel width \( \frac{y}{W} \) where \( y \) is the linear dimension from the center of the channel and \( W \) is the half width of the channel. A typical velocity profile is as shown in Figure 6-25 of which the zero ordinate indicates the center of the channel, and 1 and \(-1\) indicate the leading and trailing edges of the channel respectively (see Figure 6-7). Data beyond the 1 and \(-1\) values indicate the wakes on the vanes and are insignificant for data presentation.

The results for \( AR = 3.7 \) are shown in Figures 6-25 through 6-29. All of the curves exhibit unsymmetric velocity profiles skewed toward the leading surface of the channel. These agree very closely with the pressure distribution measurements in section 6.3.2.2.1. When the aspect ratio and angle of attack are kept constant (Figures 6-25, 6-26, and 6-27), Reynolds number plays an important role in the shape of the velocity profile. High Reynolds numbers tend to distort the profile more severely than low Reynolds numbers. When the aspect ratio and Reynolds number are kept constant (Figures 6-27, 6-28, and 6-29), the velocity profiles seem to be relatively insensitive to the angle of attack and show little or no distortion.

However, when the aspect ratio is reduced to 1.5 and the angle of attack is kept constant (Figures 6-30, 6-31 and 6-32), distorted velocity profiles exist throughout a large range of Reynolds numbers. If the Reynolds number is kept constant (Figures 6-32, 6-33, and 6-34), the velocity profiles remain distorted and also shift at different angles of attack. It is evident that the aspect ratio and the hydraulic diameter of the passage play a very important role in the performance of fuel flow transmitters. It would be ideal to have moderate aspect ratio and yet small hydraulic diameter so that a large length to hydraulic diameter ratio can be realized. This will allow viscous dissipation of any upstream disturbances and separation, resulting in a more evenly distributed velocity profile. A distorted velocity profile, however, does not adversely affect the performance of the flowmeter if it remains a constant shape over a wide range of Reynolds numbers.

In the proposed angular momentum flowmeter, viscosity will be measured directly and this can be easily transformed into Reynolds number, thus allowing compensation for Reynolds number effects which will reduce the overall system error.
6.3.2.2.3 Tapered-Vane Effect - The condition of trailing edges plays a very important part in the performance of angular momentum flowmeters. General Electric's experience has been that chamfered edges will produce unfavorable skew effects, especially when there are changes in viscosities or Reynolds numbers.

The effect of the trailing edge condition of two adjacent vanes was studied using a hot film anemometer. The trailing and leading surfaces of the two adjacent vanes at the channel exit were ground to a 15° taper. The velocity profiles at the trailing edge were measured across the channel with and without the 15° taper for two different aspect ratios. Results are as shown in Figures 6-35 and 6-36 for $A_r = 3.7$ and 1.5 respectively. The solid line is for square edges while the dotted line is that of the tapered edges. In both cases, the tapered edge improves the original unevenly distributed velocity profile. And the effect for small aspect ratio is more pronounced than large aspect ratio.

These results seem to be contradictory to what is generally believed. The true effect of trailing edge condition is still not known, and further experimental work is necessary to cover a wider range of Reynolds numbers.

6.3.2.2.4 Surface Roughness - Another item of interest for the satisfactory performance of angular momentum type flowmeters is the surface roughness of the channel. Roughness of the surface has little effect in laminar flow but profoundly influences turbulent flow. This is because the inner or viscous dominated region in laminar flow is very wide but in turbulent flow it is very thin. Therefore, small roughness elements at the surface will break up the viscous layer and cause strong changes in the velocity profile.

A piece of medium grade sandpaper (Grit Number 50) was glued on the trailing surface of the passage to simulate the rough surface finish. Velocity profile measurements were taken for two different aspect ratios at the trailing edges of the vanes and compared with those without the sandpaper (the smooth channel condition). It was hoped that the surface roughness would break up the viscous layer at the trailing surface and produce a more evenly distributed profile. But Figure 6-37 shows that, for an aspect ratio of 3.7, the velocity profile of rough surface is almost the same as that of smooth surface (Figure 6-25) and no major improvement was achieved. Likewise, the same situation exists for a smaller aspect ratio (Figure 6-38 vs Figure 6-30). This suggests that the velocity profile is relatively insensitive to the surface roughness for Reynolds number up to 3100 which covers about 60% of the range of the proposed angular momentum flowmeter ($34 \leq Re \leq 55000$).

6.3.2.3 Inlet Geometry Study - The amount of angular momentum generated by the rotating annular turbine is proportional to the square of the radius of gyration. Slight changes in the radial velocity profile of axial flow at the inlet to the turbine typically occur during transition to laminar flow and can significantly affect the radius of gyration, causing Reynolds number
dependencies in the non-linearities of the flowmeter calibration. Careful
design of the inlet, primarily length to hydraulic diameter ratio \(L/D_h\) can reduce these velocity profile changes and thereby minimize the resultant non-linearity. The inlet of the preliminary design angular momentum flowmeter was designed with this in mind \((L/D_h = 30)\), and a scale model of the inlet was constructed and tested to evaluate its performance. Figure 6-8 shows this model with the hot film anemometer fixture with traversing micrometer.

The radial velocity profile for axial flow was evaluated at two Reynolds numbers using Stoddard solvent for high Re and Almag oil (viscosity = 5 centistokes) for low Re conditions. Figures 6-39 and 6-40 show hot film anemometer voltage output across the 1.59 cm (0.625 in.) wide channel. The slight dip in Figure 6-40 near the center of the channel is thought to be caused by an uncontrolled shift in liquid temperature, and not to be representative of the flow profile. Of significance here is that over a 200:1 range in Reynolds number, no appreciable shift in the radius of gyration occurred, thus indicating adequate \(L/D_h\) ratio.

6.3.3 Discussion and Conclusions

6.3.3.1 Spring - The performance of the seven remaining springs at three different heat treating temperatures is quite satisfactory. The average mechanical hysteresis suggests that a lower heat treating temperature is desirable because it reduces the hysteresis of the spring. The inherent nonlinearity of the springs, on the average, is about 0.2% of point. However, this can be easily compensated for by the microprocessor.

6.3.3.2 Rotor Geometry - The pressure distribution experiment shows that there is a difference in velocity between the leading and trailing surfaces of the passage, and that is further confirmed by the velocity profile experiment. These differences are larger at a small aspect ratio (radial height to mean width of fluid passage) as the length to hydraulic diameter ratio is not large enough to allow adequate viscous dissipation for fully developed profiles. Also, the angle of attack plays an important role in determining the location of fluid reattachment as the incoming fluid is highly vertical and severe separation takes place in the first few hydraulic diameters. These results suggest strongly that an adequate length to hydraulic diameter ratio \((L/D_h = 20)\) and also a very moderate aspect ratio \((A_R)\) on the order of one are necessary to avoid these problems.

The velocity profile experiment suggests that there is profile shifting when Reynolds number changes and also confirms the importance of large \(L/D_h\) ratio. The shift in velocity profile does not present great deficiencies in terms of flowmeter performance. The proposed angular momentum type flowmeter will measure the kinematic viscosity which, when combined with mass flow rate by the microprocessor, will compensate for the changes in velocity profile.
It was widely believed that a sharp trailing edge condition would be highly desirable for evenly distributed velocity profiles, but the tapered vane experiment suggested otherwise. More experiments are required to gain full understanding of this phenomenon.

The surface roughness of passages has little effect in laminar flow but could greatly influence turbulent flow. It was found, however, that surface roughness had little or no effect in the proposed angular momentum transmitter.

6.3.3.3 Inlet Geometry - Another aspect that could effect flowmeter performance is shifting of radius of gyration in the inlet due to viscosity change. The inlet geometry study has covered a Reynolds number range of about 200 to 1 and no significant shift in the radius of gyration was observed. This indicates that the inlet geometry has sufficient L/Dh to allow the flow profile to become fully developed at the exit.

6.3.4 Recommendations - The basic hydraulic design of the angular momentum flowmeter requires sufficient length to hydraulic diameter ratio (L/Dh) for all channels and passages to obtain fully developed flow. This can only be done insofar as the flowmeter geometry will allow without any sacrifice to pressure drop. The proposed design will satisfy both hydraulic requirements.

One of the key requirements of the angular momentum flowmeter is the overall response time. As was pointed out in the Phase I Final Report, the main sensing element (rotor) has a response time of about 4 seconds which can be combined electronically with the fast spinning turbine to meet the 25 ms response requirement. This concept seems to be feasible, but a more in depth look and prototype testing are necessary to determine the actual algorithm.

The temperature performance of the spring requires further investigation, especially the thermo-elastic coefficient (TEC). Low TEC only can be achieved at the expense of mechanical hysteresis since these properties have opposite behavior with heat treat temperature. These two spring parameters have to be optimized for the optimal performance of the angular momentum flowmeter.

While the angular momentum concept can provide repeatability as good as the turbine meter at flow rates above 1818 kg/hr (4000 lb/hr), at lower flow rates bearing friction adds some non-repeatability. Even though the concept includes a turbine for transient response, there is some risk that the combined response of the turbine and angular momentum signals may not provide the desired quickness and accuracy. There is some attitude sensitivity inherent in the angular momentum concept, although it is minimized with precision balancing and 180° pickoffs, while the turbine concept has virtually no attitude sensitivity. Another slight detraction of the angular momentum concept is the oversize side protrusion beyond the specified envelope where the four pickoffs are located. All these are of concern for the high accuracy concept and make the angular momentum flowmeter less likely to meet NASA requirements as compared with the dual turbine flowmeter. However, further investigation into these areas will provide more clues about the viability of this concept.
6.4 Prototype Design and Test Plan Formulation

This section describes the flowmeter prototype design and test plan formulation relating to the secondary candidate, and completes in part Phase II Task 5 of NASA Contract NAS3-22139, Mod 03.

The prototype angular momentum flowmeter as shown in Figure 6-41 measures the true mass flow rate based on the angular momentum principle and does not require any density measurement or compensation. As fluid enters the flowmeter, it passes through the transient turbine which provides the necessary fast response signal. Steady angular speed of the rotor is generated by the motor and gearhead assembly via the magnetic couplers. The angular momentum, or the fluid torque generated, is proportional to the mass flow rate, and causes an angular displacement of the spring restrained rotor. This spring deflection will result in a proportional time interval between the start and stop pulses generated by magnets rotating past fixed pickoff coils on the flowmeter housing. The viscosity shroud between the rotor outer surface and housing inner surface is similar to the rotor construction. It eliminates the viscous drag on the rotor outer surface and also provides a measurement of fluid viscosity which is used to improve the overall flowmeter accuracy. The two stop signals from rotor and viscosity shroud, the reference start signal and the transient turbine signal will interface with the Data Acquisition and Processing (DAP) System. The DAP system has been pre-programmed and contains various calibration constants, and computational algorithms to provide an accurate mass flow rate output.

A test plan for the calibration of the prototype and subsequent evaluation of system performance regarding repeatability, accuracy over the temperature range, vibration effects, attitude sensitivity, pressure drop, time response and operation with alternate fuels, has also been formulated.

6.4.1 Prototype Component Description - The transient turbine, which measures the volumetric flow rate, is a COX ANC-20 turbine meter. Its primary function is to provide a fast dynamic response in order to enhance the slow responding but highly accurate mass flow rate output from the rotor. The transient turbine sensor is a modulated carrier pickoff, utilizing a 45 kHz carrier frequency which is amplitude modulated by the passage of the transient turbine rotor blades.

The fluid angular momentum is supplied by a 400 Hz, 26 volt synchronous motor coupled with a high density gearhead via magnetic couplers. This drive mechanism provides a constant angular speed for the rotor assembly, shroud assembly and reference wheel.
The rotor assembly, which is spring restrained, has 28 vanes in its fluid passage and is designed with the maximum length to hydraulic diameter ratio \( \frac{L}{D_h} = 11 \) possible given the size constraint of the flowmeter and other hydraulic parameters such as vane aspect ratio, pressure drop, etc. As fluid enters the rotor, the rotational fluid torque is balanced by the spring torque resulting in an angular displacement of the spring from its null position. This angular displacement is converted to a time-based signal via the magnets on the rotor and the induction pickoff coil on the housing. This signal, in conjunction with the reference signal, yields a time difference measurement (see Figure 6-42) which is directly proportional to the mass flow rate. The rotor spring has a maximum wind-up angle of less than 180° and the dual magnet arrangement at the rotor assembly eliminates any error caused by the imbalance effect of the rotor assembly.

The viscosity shroud assembly is similar in construction to the rotor assembly. It is also spring restrained and has a long thin shell section between the housing internal diameter and the rotor outside diameter. The primary function of the viscosity shroud is to eliminate the viscous drag on the rotor outer surface. The shroud also measures the fluid viscous drag, thus providing viscosity information for Reynolds number compensation. In order to minimize skew effects and the addition of angular momentum fluid torque, the shroud has only five, short vanes in its annulus.

The reference wheel which was listed as "fluid assist" in earlier sections, has only three very short support struts. It provides a start or reference signal for both the rotor and shroud assemblies through the same magnet and pickoff arrangement. The fluid assist is not required because the motor gearhead provides adequate torque at all flow rates.

Figure 6-43 shows the prototype functional elements divided into a flowmeter section and an electronics section. The mass flow rate will be calculated from the three signal pulses using known calibration constants and a viscosity compensation algorithm. This slow responding but accurate mass flow rate reading will be combined with the fast responding frequency output of the turbine meter to give the necessary fast responding and accurate mass flow rate. A digital microcomputer will perform these tasks in the production flowmeter system, but for prototype evaluation, these computations will be performed by the Data Acquisition and Processing (DAP) System described later in Section 6.4.4.

All the detailed sketches of piece parts, and subassemblies are shown in Appendix F.

6.4.2 Test Plan - The prototype flowmeter will be calibrated initially without the DAP system. The calibration characteristics of the transient turbine portion and the angular momentum portion of the flowmeter will then be programmed into the DAP system being developed for prototype evaluation. The completely calibrated prototype will then be connected to the DAP system and system performance tests will be run according to the design specifications and guidelines.
Flowmeter Calibration

There are two major components - the rotor and viscosity shroud which need to be calibrated as a complete unit. The output characteristic of the rotor in terms of time period (ms) versus mass flow rate (lb/hr) will be determined. The viscosity shroud output characteristic in terms of time period (ms) versus absolute viscosity will also be measured.

All of the initial calibration will be done at room temperature with three different fluids having viscosities of approximately 1.3, 5.0 and 15 centistokes. The MIL-C-7024A, Type II calibration fluid will be used for the 1.3 cs viscosity and mixtures of Almag and Tellus #10 oils will be used for higher viscosities. A flow calibrator, such as the COX 311H with a monitor turbine meter and temperature sensor, will be used for these calibration measurements. The respective output signals of the three components will be measured at flow rates ranging from 182 kg/hr (400 lb/hr) to 9090 kg/hr (20000 lb/hr) with multiple upscale anddownscale readings at each of ten flow points. The sensitivity of these output signals to changes in viscosity and flow rate can be inferred. The algorithm for viscosity compensation can then be determined.

Furthermore, tests will be conducted at -55°C and 100°C to determine if there is any temperature effect on the output characteristics of the flowmeter.

In order to achieve the high accuracy and fast responding output from the flowmeter, the transient turbine and rotor signals will pass through high-pass and low-pass filters respectively having the same time constant, and these filtered outputs will be summed to create the fast responding and accurate output signal.

For purposes of these calibrations and subsequent prototype evaluations it is necessary to establish "in house" standards of mass flow rate, volumetric flow rate, density and viscosity. For the above prototype calibrations, the two volumetric flow rate standards will be 2.54 cm (1 in.) and 1.27 cm (0.5 in.) size turbines. These monitor turbines will be calibrated using COX 305 and 311H weigh-time stands (mass flow rate) combined with in-line density measurements using a Mettler-Paar DMA 60 and DMA 620HT high accuracy digital density meter.

During calibration of the monitor turbines, the number of flow measurements that are taken at each flow rate will be determined by statistical analysis. Typically, enough measurements will be taken at a particular flow rate to ensure that the mean of the COX flow stand outputs is known within \( \pm 0.05\% \) at a 95% confidence level using the Students'-'t statistic. During subsequent prototype evaluations (described in the following section) the prototype output will be in terms of mass flow rate and may be compared directly to the weigh-time stand outputs. However, tests may show that the outputs of the monitor turbines and the densitometer standard can be combined to provide a more repeatable indication of mass flow rate than the COX stands, in which case, the monitor turbines will serve as the standards against which prototype accuracy is determined.
If the COX flow stands prove to be adequate for use as a standard in the evaluation phase, then the tare and sample weights used during evaluation for each range of flow measurement will be used again in the flowmeter calibration. Since the systematic errors of the COX flow stand (as reported in the Section 3.0 Calibration Study) depend heavily on the selection of tare and sample times (and weight), this technique will effectively eliminate any variations in the systematic errors caused by buoyancy effects and timing errors resulting from changes in fluid forces, holding tank inertia and sample control volume. This technique also permits direct readout of COX flow rate without compensation for the systematic errors and greatly simplifies the task.

While these techniques will not allow evaluation of absolute accuracy (i.e., the known systematic errors of the COX flow stands are not corrected) they will provide an excellent measure of prototype repeatability. In the future, when a more accurate flow standard is available, the biases introduced with the COX flow stands can be easily compensated out by introducing new calibration constants in the software.

Viscosity of the calibration fluid will be calculated from an accurate temperature measurement at the flowmeter and from a viscosity versus temperature curve which is evaluated just prior to the test. The temperature sensor will be an RTD and the viscosity measurements will be made with a suspended capillary type viscometer.

6.4.3 Prototype Evaluation – The following tests will be made on the prototype flowmeter:

- Repeatability
- Accuracy
- Vibration Sensitivity
- Attitude Sensitivity
- Pressure Drop
- Response Time
- Alternate Fuel

For all tests except response time and pressure drop the prototype outputs will be connected to the DAP system. All tests, unless otherwise specified, will be run at room temperature using MIL-C-7024A, Type II calibration fluid. The above tests are briefly described in what follows.
6.4.3.1 Repeatability

Objective - To determine the repeatability of the measurement of mass flow rate.

Method - Pass a flow rate, which is known approximately, through the flow sensor. Measure the flow with two other flow sensors to establish a reference for repeatability. Measure and record the output of the prototype flowmeter under test. Measurements will be made upscale and downscale at five different flow points and the test procedures will be repeated once after three days.

Apparatus - Flow calibration stand with flow measuring sensors, monitor turbine meter and the DAP system.

6.4.3.2 Accuracy

Objective - To measure any calibration shifts of the prototype over the ranges of flow rate, temperature, density and viscosity.

Method - Measure and compare the mass flow rates from the COX 305 or 311H flow calibrator and the prototype with calibration fluid. Also measure volumetric flow rate with the monitor turbines and fluid density with the density standards to provide an alternate means of establishing mass flow rate. The flow calibrators and prototype will be connected to the DAP system for this evaluation. In this set-up, the measurement time interval of the weigh-time stand will gate the measurement intervals of the signals. This ensures that fluctuations of actual flow rate do not cause measurement errors between the various inputs. The inputs will be averaged over the 30 to 60 second measurement interval prior to calculation of mass flow rate.

Multiple readings will be taken at each of ten flow rates over the 50 to 1 flow range (next higher flow about 50% greater than the present), both upscale and downscale. The same points (flow rates within ±10%) will be run at -55°C, -35°C, 25°C and +100°C. Percent-of-point error will be calculated at each reading as:

\[
\% \text{ ERROR} = \frac{m_{\text{Prototype}} - m_{\text{Standard}}}{m_{\text{Standard}}}
\]
The errors will be plotted versus flow rate for each of the four runs.

**Apparatus**

COX 305 and 311 weigh-time flow calibrators, monitor turbines and the DAP system.

### 6.4.3.3 Vibration Sensitivity

**Objective**

To determine the effect of vibration on flowmeter performance.

**Methods**

Mount the flowmeter on a vibration machine by means of a suitable fixture. Pass a constant fuel flow rate of about 25 percent of full scale through the flowmeter. Vary the vibration input over the range specified in the design guidelines and monitor the indicated flow rate from the flowmeter during vibration. Repeat the procedure with vibration inputs along each of three orthogonal axes. During each vibration scan, particular attention will be paid to mechanical resonances and variations of indicated flow. Endurance test will not be performed.

**Apparatus**

Servo type sinusoidal vibration machine, flow stand, flow sensor to monitor flow input to flowmeter being tested, and DAP system.

### 6.4.3.4 Attitude Sensitivity

**Objective**

To determine the effect of the orientation of the flowmeter on accuracy.

**Method**

Mount the flowmeter in a selected orientation. Pass a constant fuel flow rate of about 25 percent of full scale through the flowmeter using a standard turbine to monitor flow. Change the orientation of the flowmeter under test and record any changes in mass flow rate output. Repeat the procedure for each orientation desired. The positions to be tested are with axis of flow vertical and with the axis of flow horizontal and the flowmeter rotated 90° between successive orientations.

**Apparatus**

Flow stand, monitor turbine meter, fixture to hold the flowmeter under test in the desired orientation, and the DAP system.
6.4.3.5 Pressure Drop

Objective - To determine the pressure drop across the flowmeter for a range of flow rates up to full scale.

Method - Mount the flowmeter with the axis of flow horizontal. Connect a differential pressure meter across the flowmeter. Pass fuel flow through the flowmeter and measure flow rate and differential pressure for each point from low flow to full scale. In addition to room temperature testing, this test will be repeated at -55°C.

Apparatus - Flow stand, differential pressure meter, inlet and outlet pipes with pressure taps.

6.4.3.6 Response Time

Objective - To measure the time constant of the flowmeter when subjected to step changes in flow rate.

Method - The outputs from the transient turbine and rotor and the output from a hot film anemometer placed in the flowstream just ahead of the prototype will be recorded on magnetic tape. An inlet pipe fixture with two parallel pipes, each pipe having a throttle valve and one having a snap action valve, will be used both to create a fast step change in flow rate and to control the initial and final flow rates. The recorded tape will be played back at reduced speeds while the outputs are recorded on strip chart paper for detailed analysis. The two output signals will also be passed through their respective filters and the combined signal will be tested for the time response requirement.

Apparatus - Parallel pipe manifold with valves, tape recorder, strip chart recorder, hot film anemometer system.

6.4.3.7 Alternate Fuel

Repeat Accuracy (6.4.3.2) testing with JP-8.
6.4.4 Data Acquisition and Processing System (DAP) - The prototype flowmeter has a total of four electrical signal outputs with the ranges and characteristics listed in Table 6-3. Synchronization of the measurement interval for these signals with the flow calibrator and monitor turbine signals is essential to obtaining reliable measurements of prototype repeatability and accuracy. Furthermore, the conversion of the signals to mass flow rate through the various calibration functions requires a dedicated computer to obtain meaningful results in a timely fashion (i.e., real time). These requirements were recognized early in the test plan formulation and led to the design of a Data Acquisition and Processing System, herein referred to as the DAP system. Figure 6-44 is a functional block diagram showing the key elements of the system.

Frequency signals are routed to digital counters which send the measurements to a digital bus (IEEE 488 compatible, HPIB) and are controlled (synchronized) by the bus. These include the prototype flowmeter signals (transient turbine frequency, mass flow rate stop pulse, viscosity stop pulse and common reference pulse) and the monitor turbine frequency signal. The weigh-time interval of the COX 311H flow calibrator and the modulation output of the counter are converted to digital signals through a General Purpose Input/Output Port (GPIO) or through the HPIB. The temperature information as measured by the Resistance Temperature Detector (RTD) will be another input to the digital bus via a digital multimeter. An HP86A computer controls the data flow and is programmed in BASIC to compute mass flow rates for both the flow calibrator and the prototype from the calibration data taken earlier. A monitor, disk storage and printer/plotter make the DAP system a complete and versatile tool necessary for the successful development of the high accuracy fuel flowmeter for NASA.

6.5 Fabrication, Tests and Analyses of Prototype Design

This section of the report covers Tasks 6 and 7 of the angular momentum concept. It includes the fabrication of the prototype design described in the Section 6.4.1 and the component drawings in Appendix F. As expected, some minor design changes were made and the test plan was slightly altered. Tests and analyses were performed on the prototype using the DAP system and the results of which are covered in this section.

6.5.1 Prototype Description - The angular momentum prototype flowmeter comprises of 24 major components (Figure 6-41). The flowmeter body consist of the forward and aft housings which are assembled at about the mid-point using O-ring for fluid sealing. This type of arrangement is necessary for ease of assembly and disassembly of all the internal components.

A transient turbine which provides the fast response of the angular momentum flowmeter is mounted at the housing core. The transient turbine pickoff is a modulated carrier pickoff, utilizing a 45 kHz carrier frequency which is amplitude modulated by the passage of the turbine rotor blades.

The housing core which is located inside the forward housing serves two purposes. It has long annulus vane passages on its outside diameter to provide the necessary deswirling action for the incoming flow after the transient turbine. The inside of the core houses the power train of the miniature motor and reduction gearhead.
The torque transmission from the motor to the mechanism assembly is accomplished by the two magnetic couplers which are of similar construction and each has six pole magnets. The two couplers are separated by the motor cover which prevents fluid leakage into the housing core.

The rotor assembly contains 28 axial flow channels and is mounted on bearings to the shaft. A spiral restraining spring is also attached to the rotor assembly at one end and to the rotating shaft at the other end. The restraining spring controls the angle of deflection of the rotor and its wind-up is a measure of fluid torque which is directly proportional to mass flow rate of fuel.

The viscosity shroud assembly has similar construction as the rotor assembly and the wind-up angle of the shroud spring is directly proportional to the absolute viscosity of the fluid under test.

The reference wheel is mounted rigidly to the rotating shaft and provides a reference point for the signal generation of both mass flow rate and viscosity.

The signal generation is accomplished by the magnets mounted on the rotor assembly, the viscosity shroud assembly and reference wheel together with their respective pickoff coils on the housing. The signals are generated by passing a magnet by the pole piece of the pickoff coil and the changing flux level in the core generates a signal pulse.

6.5.2 Prototype Evaluation – It was planned that the prototype flowmeter would be subjected to a series of tests as identified in Section 6.4.3. However, due to difficulties encountered during the first phase of prototype evaluation which impeded other tests, only a portion of the original test plan was accomplished. The followings are detailed descriptions of the actual tests performed, problems encountered, corrective actions taken and results of the angular momentum prototype flowmeter.

6.5.2.1 Calibration – The prototype flowmeter was assembled and calibration tests were performed using the COX weigh-time flow stand. The purpose of the calibration tests was to adjust and minimize the error of the prototype flowmeter at room temperature over the flow range, and also to evaluate its relative performance at both high and low temperature conditions.

6.5.2.1.1 Negative Peaked Error – In the initial calibration, the prototype flowmeter showed a large negative error at a flow rate of about 5450 kg/hr (12,000 lb/hr) at all temperatures. It was determined that this type of error might be caused by the non-linearity of the rotor spring at that specific flow rate. Another probable cause was due to magnetic interference imposed on the rotor spring by the magnetic coupler. To investigate these effects, a new rotor spring (with smaller spring constant) was constructed to provide better resolution in flow rate measurements. In addition, the field of the magnetic coupling to the drive motor was made weaker to reduce magnetic attraction torque on the rotor spring. When the prototype flowmeter was tested with these modifications, the calibration curve was smooth and the large negative error at flow rate of 5450 kg/hr (12,000 lb/hr) was eliminated.
6.5.2.1.2 Motor Slippage - In the process of eliminating the negative peak error at 5450 kg/hr (12,000 lb/hr), the magnetic coupler flux linkage was altered. This effect reduced the magnetic torque exerted on the driven coupler by the motor. And when flow rate was increased to about 5910 kg/hr (13,000 lb/hr), the fluid torque caused the motor to slip and made it impossible to conduct measurements at high flow rates. The magnetic coupler was later rebuilt to allow better flux linkage. A relatively smooth calibration curve was achieved at flow rates up to 5910 kg/hr (13,000 lb/hr), but erratic measurements persisted at flow rates between 5910 kg/hr (13,000 lb/hr) and 9090 kg/hr (20,000 lb/hr).

6.5.2.1.3 Zero Shifting - Calibration runs were made at high and low temperature after modifications were made to the magnetic coupler. The calibration curves at various temperatures showed a zero offset of up to 91 kg/hr (200 lb/hr) from that of the room temperature. It was determined by analysis that this zero shifting was caused by the viscous drag (a phenomenon known as Couette Flow between concentric rotating cylinders) of the fluid exerted on a small area of the rotating rotor by the housing of the flowmeter. This small area, due to the magnetic pickoff arrangement, was not separated from the housing by the viscosity shroud. The amount of zero offset was also confirmed by the analysis based on the geometry of the hardware. Modification was made to the housing as shown in Figure 6-45, which increased the radial gap between the rotor and housing. Calibration runs were then performed on the flowmeter at different temperatures, (Figure 6-46) which showed that the calibration error tracked very well at low rates up to about 5910 kg/hr (13,000 lb/hr). The small difference of about 23 kg/hr (50 lb/hr) between the room and cold temperatures was predictable and was due to viscosity changes. This error can be eliminated by using a compensation scheme based on the viscosity information obtained from the viscosity shroud.

6.5.2.1.4 Erratic Calibration Curve - Various attempts had been made to correct the erratic calibration characteristics of the prototype flowmeter at flow rates above 5910 kg/hr (13,000 lb/hr). The annulus at the rotor inlet was increased by shortening the length of the vanes to allow better turbulent mixing and dissipation of incoming fluid. This modification showed very little effect on the calibration curve. The prototype flowmeter was further examined to determine if any mechanical interference existed. The four bearings in the mechanism assembly were found badly contaminated during flow testings. They were subsequently replaced and calibration curves at all temperature were improved, but the erratic behavior at higher flow rates persisted.

The large calibration error at flow rate above 5910 kg/hr (13,000 lb/hr) at high and low temperatures was probably due to the "skew" effect on the rotor exit after repetitive skewing and de-skewing during initial calibration. The "skew" effect is a second order adjustment that can be made to the flowmeter to correct for any unparallelism of the flow passages relative to the main axis of the flow stream, and is particularly profound at high flow rates and temperature extremes. In an attempt to reduce this effect, the rotor was modified by machining 0.5 mm (0.02 inch) from the end of the vanes at the exit of the rotor. Testings showed no significant improvement in the calibration curve (Figure 6-47) at flow rates above 5910 kg/hr (13,000 lb/hr).
Further modification was performed on the straightening section of the forward housing by squaring its exit edges. The cold temperature calibration was satisfactory; however, the room temperature calibration did not match the cold data. A more detailed calibration at 186 kg/hr (300 lb/hr) intervals was performed and the data (Figure 6-48) indicate that there might be fluid coupling between the rotor and the viscosity shroud vanes, causing the highly erratic and non-repeatable behavior in the calibration curve.

In order to identify the source of the locking effect, the viscosity shroud was removed from the mechanism assembly and calibration runs were performed. The room temperature calibration as shown in Figure 6-49 was still very non-linear and was quite different from the cold temperature calibration. The modification to the straightening section of the forward housing (squaring its exit edges) seemed to have caused this calibration problem. The fluid locking effect was further investigated by modifying the viscosity shroud. The long vaned support struts of the shroud were replaced by very short rounded pins, thus eliminating any possible fluid coupling effect. The subsequent calibration curves as shown in Figure 6-50 are still erratic.

It is apparent that in trying to correct the erratic calibration characteristics at flow rates above 5910 kg/hr (13,000 lb/hr), flow interaction between the rotor and viscosity shroud was discovered. After reviewing all the data, it is doubtful that the current configuration will meet the specification requirements at flow rates above 5910 kg/hr (13,000 lb/hr). However, the prototype will be investigated for potential applications for lower flow rates.

6.5.2.2 Repeatability - The prototype flowmeter was evaluated for its repeatability performance at specific flow rates at different temperatures. Figure 6-51 shows the standard deviation of multiple readings at different flow rates at both room and cold temperatures. The data indicate that the prototype flowmeter is capable of meeting the 0.25% of point requirement.

6.5.2.3 Viscosity Calibration - In order to verify the design feasibility of the viscosity shroud, calibration of the prototype was performed at both room and cold temperatures. Figure 6-52 shows the actual outputs from the shroud versus the temperature inferred viscosity data of the calibration fluid at two different temperatures. There is good correlation between the two methods which indicate that the viscosity shroud is a viable method to measure fluid viscosity. The small differences between the two methods suggest that there were errors in the calibration constants which could easily be corrected.

6.6 Conclusions and Recommendations

6.6.1 Conclusions - The angular momentum flowmeter has a very low probability of meeting NASA overall requirements. It has highly non-linear point-to-point calibration at high flow rates, and the flowmeter errors cannot be predicted using a single high order correlation calibration curve. The calibration curve also shifts with temperature due to fluid
leakage at the radial clearances between the housing and mechanism assembly. There is also a considerable amount of hysteresis in the flowmeter affecting repeatability between upscale and downscale readings. Although the viscosity measurement from the viscosity shroud shows good correlation, it is questionable whether the compensation algorithm will compensate the viscosity related flow calibration problem at cold temperature.

6.6.2 Recommendations — The current flowmeter configuration, however, has a few positive features to be considered. It has very good repeatability at fixed flow points. The standard deviation of repeatability is well within the 0.25% requirement, which indicates that a look-up table for calibration is possible. The viscosity measurement is excellent over the active flow range. The prototype flowmeter also shows that calibration within 0.25% can be achieved at flow rates below 5450 kg/hr (12,000 lb/hr), which suggests that the current design could be upsized to achieve better high flow rate performance.
### TABLE 6-1 SUMMARY OF INDIVIDUAL SPRING PERFORMANCE

<table>
<thead>
<tr>
<th>Spring No.</th>
<th>Heat Treating Temp. (°C)</th>
<th>Ave. Hysteresis (%) of Point</th>
<th>Ave. Nonlinearity(%) of Point</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>500</td>
<td>0.020</td>
<td>0.286</td>
</tr>
<tr>
<td>2</td>
<td>500</td>
<td>0.009</td>
<td>0.153</td>
</tr>
<tr>
<td>3</td>
<td>500</td>
<td>0.037</td>
<td>0.086</td>
</tr>
<tr>
<td>4</td>
<td>666</td>
<td>0.088</td>
<td>0.169</td>
</tr>
<tr>
<td>5*</td>
<td>666</td>
<td>Not Available</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>666</td>
<td>0.017</td>
<td>0.298</td>
</tr>
<tr>
<td>7*</td>
<td>732</td>
<td>Not Available</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>732</td>
<td>0.079</td>
<td>0.093</td>
</tr>
<tr>
<td>9</td>
<td>732</td>
<td>0.134</td>
<td>0.352</td>
</tr>
</tbody>
</table>

* Defective

### TABLE 6-2 SUMMARY OF HEAT TREATMENT TEMPERATURE EFFECTS ON HYSTERESIS AND NON-LINEARITY

<table>
<thead>
<tr>
<th>Heat Treating Temperature (°C)</th>
<th>Average Hysteresis (%) of Point</th>
<th>Average Nonlinearity (%) of Point</th>
</tr>
</thead>
<tbody>
<tr>
<td>500</td>
<td>0.022</td>
<td>0.175</td>
</tr>
<tr>
<td>666</td>
<td>0.053</td>
<td>0.234</td>
</tr>
<tr>
<td>732</td>
<td>0.107</td>
<td>0.223</td>
</tr>
</tbody>
</table>

223
<table>
<thead>
<tr>
<th>Signal</th>
<th>Range</th>
<th>Amplitude</th>
</tr>
</thead>
<tbody>
<tr>
<td>Turbine</td>
<td>24 to 1600 Hz</td>
<td>0 to 5V Square Wave</td>
</tr>
<tr>
<td>Rotor</td>
<td>6 Hz</td>
<td>150 mV Zero to Peak</td>
</tr>
<tr>
<td></td>
<td></td>
<td>50 mV Zero to Trough</td>
</tr>
<tr>
<td></td>
<td></td>
<td>10 ms Pulse Width</td>
</tr>
<tr>
<td></td>
<td></td>
<td>36 mV/ms Zero</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Crossing Slope</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(See Figure 6-42)</td>
</tr>
<tr>
<td>Shroud</td>
<td>6 Hz</td>
<td>Same as rotor</td>
</tr>
<tr>
<td>Reference Wheel</td>
<td>6 Hz</td>
<td>Same as rotor</td>
</tr>
</tbody>
</table>
Section 6.8

FIGURES
FIGURE 6-1  PICTORIAL PRESENTATION OF OPERATION OF ANGULAR MOMENTUM FLOWMETER
FIGURE 6-3 ROTOR VANE GEOMETRY STUDIES

PASSENGE LENGTH STUDY

76° MAX AT MIN FLOW
3° MIN AT MAX FLOW

VELOCITY PROFILES
PRESSURE PROFILES

ASPECT RATIO
MINIMUM RE
SECONDARY FLOW

\[
dI = \text{dm} r^2 + \frac{\text{dm}}{2} \frac{1}{r^2}
\]

\[
\frac{1}{2} (\frac{0.07}{0.80})^2 = 0.38\%
\]

THE DIFFERENCE IN INERTIA IS
\[ \alpha = \tan^{-1} \left( \frac{V_p}{V_a} \right) \]
FIGURE 6–7 PRESSURE PORT ARRANGEMENT ON TWO ADJACENT VANES
FIGURE 6-8 THE 4" INLET TEST SECTION FOR EVALUATING INLET FLOW PROFILE. FLOW IS FROM LEFT TO RIGHT, WITH THE CENTER LINE SHOWN.
Figure 6.10  Percentage Error of Point Versus Angle of Deflection
FIGURE 6-12 PERCENTAGE ERROR OF POINT VERSUS ANGLE OF DEFLECTION
FIGURE 6-13 PERCENTAGE ERROR OF POINT VERSUS ANGLE OF DEFLECTION
Figure 6-15 Percentage Error of Point Versus Angle of Deflection

SPRING NO. 9 732°C

07/28/82 Angle of Deflection (Deg)
AR = 3.7; Re = 20400; α = 13.1°

07/26/82  PASSAGE LENGTH (X/L)

FIGURE 6-16 PRESSURE COEFFICIENT VERSUS PASSAGE LENGTH
AR = 3.7; Re = 11700; $\alpha = 42.4^\circ$

**Figure 6-18** Pressure Coefficient Versus Passage Length

- Leading Surface
- Trailing Surface

07/26/82 Passage Length (X/L)
AR=1.5; Re =31100; $\alpha=13^\circ$

**FIGURE 6-19 PRESSURE COEFFICIENT VERSUS PASSAGE LENGTH**
Figure 6-21: Pressure Coefficient Versus Passage Length

AR = 1.5, Re = 17800, α = 22.1°
$AR=0.69; \quad Re=42200; \quad \alpha=13.1^\circ$

![Graph showing pressure coefficient versus passage length](image)

**Figure 6-22** PRESSURE COEFFICIENT VERSUS PASSAGE LENGTH
AR=0.69; Re=42200; $\alpha=27.6^\circ$

**Figure 6-23** Pressure Coefficient Versus Passage Length
AR=3.7, Re=20400, $\alpha=27.6^\circ$
Figure 6-26  Velocity Profile Across Flow Channel

AR=3.7, Re=13400, $\alpha=27.6^\circ$
AR=3.7, Re=9000, $\alpha=27.8^\circ$
AR=1.5; Re=31100; \alpha=27.6°
FIGURE 6-34 VELOCITY PROFILE ACROSS FLOW CHANNEL
AR = 3.7; Re = 20400, $\alpha =$ 27.6°

FIGURE 6-35 VELOCITY PROFILE OF EDGE SHARPNESS EFFECT
FIGURE 6-36 VELOCITY PROFILE OF EDGE SHARPNESS EFFECT

AR=1.5; Re=31100; α=27.6°

Channel Width

07/29/82 CHANNEL WIDTH (y/W)
AR=3.7; Re=20400; α=27.5°; Grit Number=50

08/02/82 CHANNEL WIDTH (y/W)

FIGURE 6-37 VELOCITY PROFILE OF SURFACE ROUGHNESS EFFECT
AR=1.5; Re=31100; \alpha=27.6^\circ; Grit Number=50

FIGURE 6-38 VELOCITY PROFILE OF SURFACE ROUGHNESS EFFECT
FIGURE 6-41  ANGULAR MOMENTUM FLOWMETER ASSEMBLY

Note: Dotted lines represent purchased parts
(Dimensions are not finalized)
FIGURE 6-43  PROTOTYPE FUNCTIONAL ELEMENTS OF ANGULAR MOMENTUM FLOWMETER
**Figure 6-44** DATA ACQUISITION AND PROCESSING SYSTEM #2
FIGURE 6-46  CALIBRATION ERROR VS FLOW RATE AFTER LABYRINTH AND BEARING CHANGE
FIGURE 6-52  COMPARISON OF VISCOSITY MEASUREMENTS vs FLOW AT DIFFERENT TEMPERATURES

-60°F  Room Temp.
7.0 Densi-Viscometer

This section describes the experimental and analytical investigation, the prototype construction and evaluation performed on the densi-viscometer.

7.1 Introduction

The vortex precession and dual turbine flowmeters (Sections 4.0 and 5.0 respectively) are basically volumetric devices and require precise density and approximate viscosity measurements to perform as mass flowmeters. The conceptual design of the densi-viscometer can be found in the Phase I Final Report. It is based on a currently produced General Electric densitometer that oscillates at a frequency determined by fluid density, and from which viscosity data can also be derived.

7.2 Experimental and Analytical Investigation Plan Formulations

There are several characteristics of the densitometer/viscometer concept which require additional experimental investigation. The following areas for investigation were planned to be conducted in Task 4:

1. Damping coefficient (Q) versus viscosity
2. Damping coefficient and natural frequency (f_n) versus flow-through velocity
3. Stability over expanded temperature range
4. Methods of reducing temperature sensitivity

7.2.1 Damping Coefficient Versus Viscosity

Problem - As viscosity increases, the shear forces and boundary layer on the oscillating surfaces of the fluid couplers increase, thereby increasing the damping coefficient or lowering the Q of the spring mass system, as well as lowering the natural frequency, f_n. When the gain and phase of the loop-closing circuitry are properly set, the compound effects of lower Q and lower f_n are nullified and the closed loop frequency, f_d, is made constant so as to provide an accurate measure of density. Furthermore, by modulating the gain and phase of the circuitry, a small change in f_d can be generated whose magnitude indicates Q of the damped spring-mass system, from which viscosity is obtained. In order to design the circuitry, the frequency response (gain and phase vs. frequency) vs. density and viscosity must be known precisely. In addition, the coupling coefficient for couplers with different numbers of vanes must be ascertained.
Solution Approach - Frequency response of several densitometers will be measured in room temperature liquids having viscosities and specific gravities that cover the maximum ranges over which jet fuels vary (from temperature extremes and JP-4 to JP-8 characteristics). The units will have the following couplers:

- 16 vanes - 1.9 cm (0.75 in.) diameter
- 8 vanes - 1.9 cm (0.75 in.) diameter
- 4 vanes - 1.9 cm (0.75 in.) diameter

The reason for testing these types of couplers is that it will provide data which indicates how surface area and basic coupler shape affect the Q vs. viscosity function. The production model has a large circumferential area while the vaned types have minimal area; this difference may produce vastly different response to changing viscosity. Furthermore, the vaned units will have lower coupler inertia which results in improved sensitivity. Vaned couplers would also cost much less to produce than the present multi-hole coupler. This is a tradeoff since as the number of vanes is reduced, coupling efficiency is also reduced. See Figure 7-1.

Open loop frequency response will be measured and plotted for each unit in the following liquids.

<table>
<thead>
<tr>
<th>Liquid</th>
<th>Approximate Specific Gravity</th>
<th>Approximate Kinematic Viscosity Centistokes</th>
<th>Simulation of fuel at:</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tellus Oil #10</td>
<td>0.90</td>
<td>20</td>
<td>-55 Maximum</td>
</tr>
<tr>
<td>Silicone Oil</td>
<td>0.90</td>
<td>5</td>
<td>-55 Minimum</td>
</tr>
<tr>
<td>Stoddard Solv. &amp; Tellus Oil</td>
<td>0.77</td>
<td>5</td>
<td>20 Maximum</td>
</tr>
<tr>
<td>Stoddard Solv. &amp; Heptane</td>
<td>0.77</td>
<td>1</td>
<td>20 Minimum</td>
</tr>
<tr>
<td>Stoddard Solv. &amp; Heptane</td>
<td>0.65</td>
<td>0.8</td>
<td>130 Maximum</td>
</tr>
<tr>
<td>Pentane</td>
<td>0.65</td>
<td>0.25</td>
<td>130 Minimum</td>
</tr>
</tbody>
</table>

All tests will be run at 25°C to minimize frequency variations due to temperature sensitivity. The driving voltage will be varied to maintain a constant output voltage at resonance, and thereby more closely simulate actual closed loop operation. The engineering laboratory at General Electric is equipped with temperature control baths, drive and output circuits, and gain and phase measuring instruments.

7.2.2 Damping Coefficient (Q) and Natural Frequency (f_n) versus Flow-Through Velocity

Problem - As flow velocity through the densitometer increases, the energy conducted away by the exiting flow, through the motion of the coupler, increases. This, in turn, lowers both Q and f_n. In the turbine and vortex precession flowmeters, at least 1% flow diversion is needed through the
densitometer housing to ensure complete turnover of fuel in less than one minute at the minimum flow of 182 kg/hr (400 lb/hr). At the maximum rated flow of 9090 kg/hr (20,000 lb/hr), flow velocity through the vanes or holes is approximately 15 cm/sec (6 in./sec), which is of the same order of magnitude as vane tip or outside diameter velocity (5 cm/sec). The magnitude of the resultant Q and \( f_n \) changes must be known for future design of the densitometer housing, and for estimation of densitometer/viscometer accuracy.

**Solution Approach** – Fuel will be forced through a densitometer placed in a pipe as shown in Figure 7-2. Open loop Q and \( f_n \) will be measured at 25°C on the above mentioned densitometer. Should the sensitivity be minimal, a unit will be tested in a 3.8 cm (1.5 in.) diameter pipe over the 182 to 9090 kg/hr (400 to 20,000 lb/hr) flow range to see if the housing is, in fact, unnecessary.

Should flow velocity have adverse effects on Q and \( f_n \), attention will be focused on approaches to control the velocity to the maximum allowed over the wide range of viscosity and mass flow rate. The following techniques will be investigated analytically:

- Boundary layer scoops
- Variable orifice control
- Port location

**7.2.3 Stability Over Expanded Temperature Range**

**Problem** – Temperature sensitivity of closed loop frequency need not be perfectly linear since compensation for these effects is made in the computer algorithms. However, this approach is practical only if the frequency vs. temperature function is highly repeatable and stable for long periods of time (months). Our experience with the current production models shows that some "aging" occurs when the units are initially cycled over temperature extremes (-55 to +70°C) and that they settle out after two cycles and are repeatable within \( \pm 0.12\% \). This is adequate for current applications but must be reduced to less than 0.1% over a wider temperature range (-55 to +130°C) for the NASA application.

**7.2.4 Methods of Reducing Temperature Sensitivity**

**Problem** – If temperature sensitivity is reduced, the temperature sensor may be eliminated, thus lowering the cost and complexity of the flowmeter system. This problem is closely related to the stability problem so the solution approaches are discussed together.

**Solution Approach** – Several densitometers will be subjected to temperature cycling in air over a -55°C to +130°C range for the three month duration of Task IV. Frequency will be recorded automatically every hour and chamber temperature programmed to cycle hot and cold once daily. At the start, mid-point and finish of the test, three point density calibrations will be made to corroborate the air frequency data. The data will be analyzed at
mid-point to determine if any significant trends exist, and, if any changes in test approach are warranted. The unit will be operated closed-loop with the electronics at ambient room temperature (20°C) except that open loop gain and phase vs. frequency will be plotted at the start, mid-point and end of the test.

The following units will be built for this evaluation:

a) Production Unit
b) Minimum Solder Bond Thickness
c) Shot Peened Spring

7.3 **Experimental and Analytical Investigations**

Data relating to the densi-viscometer are included in the accompanying report supplement No. 1 dated December 15, 1984 as protectable data in accordance with contract NAS3-221394, Item 8C.
8.0 CONCLUSIONS AND RECOMMENDATIONS

After considering all the test results in Task 4 for all three different types of flowmeters, a rating scheme was established to evaluate the overall merit of all three flowmeter design. A rating chart (Table 8-1) summarizes the probability of meeting the listed requirements for each concept in its conceived final system configuration. The relative ratings of the vortex, dual turbine and angular momentum flowmeters are 0.71, 1.00 and 0.95 respectively.

The dual turbine flowmeter and angular momentum flowmeter were chosen for prototype development and evaluation in Tasks 5 through 7.

The following conclusions and recommendations are made for each of the sub-systems for the NASA HAFF program:

Test and Calibration System

Conclusions: 1) There are no flow rate calibration facilities known at present that meet the calibration requirements of NASA HAFF program.

2) The best flow rate calibration facility at GE/AID is inadequate to meet the ultimate calibration accuracy requirements of the flowmeters being developed under NASA HAFF program.

Recommendations: 1) Plan a flow calibration facility using a Flow-Thru Calibrator in a closed calibration system.

2) Procure precision density measuring equipment to combine volumetric flow rate with density to get mass flow rate.

Vortex Flowmeter

Conclusions: 1) The calibration constant becomes excessively non-linear at low Reynolds numbers.

2) The repeatability is only about 0.5% and it has limited dynamic range.

3) Cavitation causes inaccuracy at high flow rates and also the pressure drop is excessive.

4) Existing vortex sensing technique will not meet the time response requirement.
Recommendations: 1) Alternate vortex sensing technique should be evaluated.

2) The relationship between pressure drop and dynamic range should be investigated and optimized.

Dual Turbine Flowmeter

Conclusions: 1) Dual turbine concept does not offer an advantage over conventional flow straightener for eliminating the effects of swirl in the incoming flow stream.

2) The "K" factor is a non-linear but single value function and will require a very accurate flow test facility to characterize the turbine.

3) Fuel viscosity must be accurately measured to reduce errors at high and low temperatures.

4) Tests with room and high temperature fuels show that 0.25% accuracy can be achieved.

Recommendations: 1) The main turbine, with or without the input from sensor turbine, is adequate to measure volumetric flow rate. The sensor turbine should be used to measure bearing degradation.

2) The dual turbine should be re-evaluated using the Test and Calibration System for accuracy.

Angular Momentum Flowmeter

Conclusions: 1) The angular momentum flowmeter has low probability of meeting 0.25% point accuracy at flow rates above 5450 kg/hr (12,000 lb/hr).

2) The viscosity shroud provides good measurement of fluid viscosity.

3) The spring of the rotor has considerable amount of hysteresis, thus affecting flowmeter repeatability between upscale and downscale calibration.

Recommendations: 1) The existing prototype design should be considered for application at flow rate below 5450 kg/hr (12,000 lb/hr).

2) Alternatively, the existing design may be upsized to achieve better high flow rate performance.
Conclusions:

1) Significant improvements in the circuits response to noise are required, and are feasible with phase locked-loop designs. Synchronous detection of narrow band signals in noise of equivalent power is routinely achievable with such techniques.

2) The pickoff crystal of the densitometer is sensitive to bulk acoustic waves induced by vibration and sound transmission through the fluid.

3) Increased accuracy of fluid properties is required of calibration fluids used for simultaneous calibration of viscosity and density.

Recommendations:

1) Design, build, test and evaluate a noise-immune pickoff concept.

2) Design, build, test and evaluate a circuit based on the phase-locked loop principle.

3) Develop fluids having stable density and viscosity over a wide temperature range. An accuracy of 0.02% in density and 0.5% in viscosity are desirable of over -50°C to +120 °C temperatures.
### Table 8-1 CONCEPT RATING CHART

<table>
<thead>
<tr>
<th>Performance</th>
<th>Weighting</th>
<th>Turbine</th>
<th>Angular Momentum</th>
<th>Vortex Precession</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Factor</td>
<td>Rating</td>
<td>Points</td>
<td>Rating</td>
</tr>
<tr>
<td>Accuracy</td>
<td>9</td>
<td>6</td>
<td>24</td>
<td>4</td>
</tr>
<tr>
<td>- 400-4,000 lb/hr</td>
<td>4</td>
<td>10</td>
<td>50</td>
<td>9</td>
</tr>
<tr>
<td>- 4,000 - 20,000 lb/hr</td>
<td>5</td>
<td>9</td>
<td>63</td>
<td>10</td>
</tr>
<tr>
<td>Dynamic Range</td>
<td>7</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Response Time</td>
<td>7</td>
<td>4</td>
<td>9</td>
<td>7.5</td>
</tr>
<tr>
<td>- Above 2,000 lb/hr</td>
<td>4</td>
<td>5</td>
<td>15</td>
<td>5</td>
</tr>
<tr>
<td>- Below 2,000 lb/hr</td>
<td>3</td>
<td>8</td>
<td>40</td>
<td>10</td>
</tr>
<tr>
<td>Pressure Drop</td>
<td>5</td>
<td>10</td>
<td>50</td>
<td>10</td>
</tr>
<tr>
<td>Vibration Sensitivity</td>
<td>5</td>
<td>10</td>
<td>50</td>
<td>9</td>
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<tr>
<td>Attitude Sensitivity</td>
<td>5</td>
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<td>70</td>
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<tr>
<td>Flowmeter Size</td>
<td>7</td>
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<td>85.5</td>
<td>9</td>
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<tr>
<td>Probability of Success</td>
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<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td>483.5</td>
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<td>458</td>
</tr>
<tr>
<td>Relative Merit</td>
<td></td>
<td>1.00</td>
<td></td>
<td>0.95</td>
</tr>
</tbody>
</table>
APPENDIX A

DERIVATION OF THE EQUATION FOR A BUOYANCY CORRECTION FACTOR APPLICABLE TO WEIGH (FLOW CALIBRATION) STANDS
Figure 3-22 shows a schematic diagram of a weigh tank, equivalent lever arm and brass weight counterpoise system for determining the change in mass of liquid contained in the weigh tank during a calibration run.

The following notation is used for the derivation:

- \( d_L \) = Density of the liquid being measured, \( \text{gm/cm}^3 \)
- \( d_A \) = Density of air
- \( d_B \) = Density of the brass weights
- \( d_{AB} \) = Density of the air surrounding the brass weights
- \( d_{AT} \) = Density of the air surrounding the weigh tank
- \( d_V \) = Density of the air-vapor mixture in the void space within the weigh tank
- \( M_{L1} \) = Mass of liquid in the weigh tank at the start of the run
- \( M_{L2} \) = Mass of liquid in the weigh tank at the end of the run
- \( M_{B1} \) = Mass of brass weights in equilibrium with the weigh tank and contents at the start of the run
- \( M_{B2} \) = Mass of brass weights at the end of the run
- \( V_T \) = Internal volume of the weigh tank
- \( R_0 = L_2/L_1 \) = Equivalent lever arm ratio (also applicable to a compound lever arm system as used in the COX 311H stand)
- \( M_T \) = Mass of the weigh tank excluding all contents
At the start of the run, the moment on the right side is in equilibrium with the moment on the left side as shown in Figure 3-16. The air temperature surrounding the brass weights and the weigh tank may be significantly different when the test temperature of the fluid temperature differs from the ambient temperature. Equating the moments on the right side of the balance with moment on the left side and accounting for the air buoyancy forces gives the following relationship:

\[(\text{Volume of brass weights}) \times (d_B - d_{AB}) \times L_2 = L_1 \times (\text{Tank Weight} + \text{total mass of liquid in tank} + \text{total mass of air and vapor mixture in tank}) - L_1 \times (\text{Total volume of weigh tank}) \times d_{AT}\]

The above statement reduces to the following equation for the conditions at the start of a calibration run:

\[R_0 \left[ \frac{M_B}{d_B} \right] (d_B - d_{AB}) = M_T + M_{L1} + \left[ V_T - \frac{M_{L1}}{d_L} \right] dV - V_T d_{AT} \quad (A-1)\]

A similar equation can be written for the static balance of the lever system at the end of the run or

\[R_0 \left[ \frac{M_B}{d_B} \right] (d_B - d_{AB}) = M_T + M_{L2} + \left[ V_T - \frac{M_{L2}}{d_L} \right] dV - V_T d_{AT} \quad (A-2)\]

We can obtain an equation for the difference in the true liquid mass by subtracting Equation (A-1) from Equation (A-2) or

\[R_0 \left( \frac{M_{B2} - M_{B1}}{d_B} \right) \left[ 1 - \frac{d_{AB}}{d_B} \right] = \left( M_{L2} - M_{L1} \right) \left[ 1 - \frac{dV}{d_L} \right] \quad (A-3)\]

and rearranging Equation (A-3)

\[\left( M_{L2} - M_{L1} \right) = R_0 \left( \frac{d_{AB}}{d_B} \right) \left[ 1 - \frac{dV}{d_L} \right] \quad (A-4)\]
The last ratio of terms in Equation (A-4) corrects for the buoyancy forces based on (1) the density of the air surrounding the brass weights, (2) the density of the brass weights, (3) the density of the air-vapor mixture and (4) the liquid density within the weigh tank. It is fortuitous that the density of the air surrounding the weigh tank does not enter into the correction term inasmuch as it would be difficult to characterize the temperature gradients surrounding the tank. If we assume that the free convection forces on the tank are the same at the beginning as at the end of the run, we can also deduce that these forces would cancel since buoyancy terms \( V_T d_{AT} \) would be the same at the start and end.

The last ratio of terms in Equation (A-4) becomes the buoyancy correction factor \( K_{B1} \).

\[
K_{B1} = \frac{1 - \frac{d_{AB}}{d_B}}{1 - \frac{d_Y}{d_L}}
\]

(A-5)

The true change in fluid mass in the weigh tank is equal to the product of (1) the buoyancy correction factor, \( K_{B1} \), (2) the scale beam ratio, \( R_0 \), and (3) the change in mass of the brass weights on the scale pan.

Olsen [3] gives the following correction factor for buoyancy to determine true mass:

\[
K_{B2} = \frac{1 - \frac{d_A}{d_B}}{1 - \frac{d_A}{d_L}}
\]

(A-6)

Olsen's equation does not designate where the density of the air \( d_A \) in Equation (A-6) is determined. Equations (A-5) and (A-6) basically only differ by a single quantity \( d_Y \) versus \( d_A \). This infers that the buoyancy correction is primarily a function of the density of the air-vapor displaced by the liquid entering the weigh tank rather than a function of the density of the air surrounding the weigh tank.

At a temperature of 21°C (70°F), standard pressure, a density for the brass weights of 8.4 gm/cm³, a fluid density of 0.77 gm/cm³ and an air density of 1.2014 kg/m³, Equation (A-6) gives a buoyancy correction factor of \( K_{B2} = 1.00142 \).
At 21°C (70°F), the true vapor pressure of JP-4 is 10.7 kPa (1.55 psia) and using an estimated molecular weight of \(M_v = 126\ \text{gm/mole}\) for the hydrocarbon vapor, the density of the air/hydrocarbon vapor mixture above the liquid is \(d_y = 1.624\ \text{kg/m}^3\ (0.1014\ \text{lbm/ft}^3)\) and the buoyancy correction factor from Equation (A-5) is \(K_B^1 = 1.001972\) which is greater than the previous correction factor by 0.055 percent.

The difference between the two buoyancy correction factors is even greater at a temperature of 95°C (203°F). Using a true vapor pressure of JP4 is 90 kPa (13 psia) and a liquid density of 0.714 gm/cm\(^3\) results in a buoyancy correction factor from Equation (A-5) of \(K_B^1 = 1.005234\). This value may be compared with \(K_B^2 = 1.00121\) from Equation (A-6) or a difference of 0.402 percent. The only uncertainty in the data used in evaluation of Equation (A-5) is the value of the equivalent molecular weight of the hydrocarbon vapor.

It was previously assumed that the air vapor mixture is in equilibrium at the temperature of the hydrocarbon liquid. This assumption appears valid for the COX 311H calibration stand since the air-vapor mixture is repeatedly transferred between the weigh tank and the liquid reservoir below the weigh tank through the overflow tube.

A further improvement in the accuracy of the determination of the density of the air-vapor mixture would be to directly flow a sample of the mixture through a density meter suited for gas density measurements.

It should be emphasized that the value of the buoyancy correction factor \(K_B^1\) given by Equation (A-5) is independent of the tare weights or the density of the materials comprising the tare weights. The buoyancy correction factor is also independent of the density of the air surrounding the weigh tank or any thermal or forced convection currents acting on the weigh tank as long as the conditions surrounding the tank can be assumed identical at the start and finish of a calibration run. The buoyancy correction factor is only dependent on (a) the density of the air surrounding the brass weights, (b) the density of the brass weights, (c) the density of the air-vapor mixture displaced by the fluid entering the weigh tank and (d) the density of the calibration fluid.

Figure 3-19 gives estimated values of the buoyancy correction factor as a function of temperature and molecular weight of the fuel vapor for two jet fuels.
APPENDIX B

RELATIONSHIP BETWEEN CHANGE IN MOMENTUM OF A FALLING LIQUID TO VOLUME OF THE COLUMN OF LIQUID
APPENDIX B

RELATIONSHIP OF CHANGE
IN MOMENTUM OF A FALLING FLUID TO
THE VOLUME OF THE FLUID

Figure 3-21 shows the approximate geometry of a liquid as it spills into the weigh tank of a dynamic flowmeter calibrator. The liquid has a mean velocity of \( w_0 \) as it leaves the edge of the spreader cone as shown in Figure 3-21. The velocity \( w_0 \) is a function of the area of (1) the inlet nozzle opening, \( A_0 \) (2) the angle of the spreader cone, \( \Theta \) (3) the height between the center of the flow nozzle and the edge of the spreader cone, \( h_0 \) (4) and the volumetric flowrate, \( Q = \frac{W_L}{d_L} \). The vertical velocity component at the edge of the spreader cone is \( u_0 = w_0 \sin \Theta \). The vertical velocity at any height below the edge of the spreader cone can be calculated from the following equation:

\[
 u = \sqrt{2gh + u_0^2} \tag{B-1}
\]

where

- \( g = \) Local acceleration of gravity, cm/sec\(^2\)
- \( h = \) Distance below the edge of the spreader cone, cm
- \( u_0 = \) Initial vertical velocity component, cm/sec

The cross-sectional area \( A \) of the liquid jet at any height can be calculated from the continuity equation as follows:

\[
 A = \frac{W_L}{d_Lu} \tag{B-2}
\]

where

- \( A = \) Cross-sectional area of the liquid jet in the horizontal plane, cm\(^2\)
- \( W_L = \) Mass rate of liquid flow, kg/sec
- \( d_L = \) Density of the liquid, kg/cm\(^3\)
- \( u = \) Vertical velocity component of liquid jet, cm/sec

The volume of the liquid jet between the liquid levels at start and end can be calculated from the following equation:
where \( V_L = \) Volume of the liquid between the liquid levels at start and end of the run

and after integrating:

\[
V_L = \frac{W_L}{\gamma dL} \left[ \sqrt{2gh_1 + u_o^2} - \sqrt{2gh_2 + u_o^2} \right] \quad (B-4)
\]

from Equation (B-1)

\[
V_L = \frac{W_L}{\gamma dL} (u_1 - u_2) \quad (B-5)
\]

The mass of the liquid jet between the two reference levels is the product of the volume and the density of the fluid or

\[
M_L = V_L dL = \frac{W_L}{\gamma} (u_1 - u_2) \quad (B-6)
\]

At the start of the run, it is seen from Equation (B-6) that the mass of liquid between the two reference liquid levels is equal to the change in momentum of the liquid as it falls from the final level to the starting level. Since the change in impulse forces on the weighing mechanism are equal to the change in momentum, Shafer and Ruegg [2] assumed that this effect automatically compensated for the additional mass of the falling jet. This is a valid assumption if the fluid impinges on a fluid surface at the start and end of the run. The two effects should be treated separately, however, if the fluid impinges on the bottom of the tank at the start of a run or on the side of the tank at the start or end of the run.

Equation (B-6) provides an easy method of calculating the added mass of the liquid jet. If the flowrate varies during the test, the value of the flowrate \( W_L \) is used in Equation (B-3) through (B-6) should be the flowrate at the start of a run. The impulse effects on the weigh beam motion should be evaluated for the flowrate both at the start and the end of a run.

The void volume between the liquid level at the start of a run and the liquid level which will occur at the end of the run will be referred to as the control volume \( V_o \). The mass of liquid, \( M_L \), determined from Equation (B-6) has already entered the control volume at the start of the run and becomes a portion of the mass of the fluid within the weigh tank at the end of the run. The mass of fluid given by Equation (B-6) should therefore be subtracted from
the change in mass of liquid which accumulated in the weigh tank as determined as the product of the scale beam ratio \( R_0 \) and the brass weight added to the weight pan. The correction factor for the mass of the fluid jet would then be

\[
K_J = \frac{R_0 M_B - M_L}{R_0 M_B}
\]

or

\[
K_J = 1 - \frac{M_L}{R_0 M_B} = 1 - \frac{W_L (u_1 - u_2)}{g R_0 M_B}
\]  

(B-7)

where \( K_J \) = Correction factor for jet liquid volume

A typical value for this factor during the operation of the COX 311H Flowmeter Calibrator is \( K_J = 0.99925 \) or a 0.075 percent correction for a 35 sec run at 2.52 kg/s (20,000 lbm/hr).

The correction factor for the mass of the liquid jet can also be expressed by the following equation:

\[
K_J = \frac{W_{LT_C} - M_L}{W_{LT_C}} = 1 - \frac{M_L}{W_{LT_C}}
\]  

(B-8)

where \( W_{LT_C} = R_0 M_B \) = Mass of fluid which accumulates in the weigh tank during time \( t_C \)

\( t_C \) = Corrected run time based on static balance at the start and end of the run.

The downward force \( F_1 \) imparted to the weigh tank by the fluid jet at the start of a run is given as follows:

\[
F_1 = W_L u_1
\]  

(B-9)

The impulse force given by Equation (B-9) causes the weigh beam to start rising \( t_{S1} \) seconds earlier than due to true static balance. The time \( t_{S1} \) can be determined by calculating an equivalent weight of fluid which accumulates during this time period or

\[
F_1 = W_{LT S_1} g
\]  

(B-10)
The time $t_{S1}$ can then be determined by equating Equation (B-9) and (B-10) or:

$$t_{S1} = \frac{u_1}{g} \quad \text{(B-11)}$$

The impulse force of the falling jet causes the weigh beam to start rising $t_{S2}$ seconds earlier than due to a true static balance. The time $t_{S2}$ can be related to the vertical velocity component of the falling jet as follows:

$$t_{S2} = \frac{u_2}{g} \quad \text{(B-12)}$$

Subtracting Equation (B-12) from (B-11) gives

$$t_{S1} - t_{S2} = \frac{u_1 - u_2}{g} \quad \text{(B-13)}$$

and using Equation (B-6)

$$t_{S1} - t_{S2} = \frac{M_l}{W_L} \quad \text{(B-14)}$$

The substitution of the equivalence given by Equation (B-14) into Equation (B-8) results in the following equation:

$$K_J = 1 - \left[ \frac{t_{S1} - t_{S2}}{t_C} \right] \quad \text{(B-15)}$$

Equation (B-15) is useful to simplify the determination of the correction factor timing $K_T$ as shown in Section 3.6.1.1.
APPENDIX C

SUMMARY OF PATENTS RELATED TO LIQUID FLOW RATE CALIBRATION
APPENDIX C

SUMMARY OF PATENTS RELATED TO LIQUID FLOW RATE CALIBRATION

1. Proving Meters 3,021,703 20 Feb 1962
   Inventor: R. H. Pfrehm
   Assignee: ESSO Research and Engr., Elizabeth, NJ
   Abstract: Reciprocating piston in a straight pipe. Molded elastomeric seals fastened to a rigid cylindrical piston.

   Inventors: Marshall U. Bagwell and Donald H. Bond
   Assignee: Texas Pipe Line Co., Houston, TX
   Abstract: Miscible fluid injected in pipe line. Arrival of fluid wave front detected by change in dielectric constant of fluid. (Fluid velocity profile will greatly effect accuracy).

3. Flowmeter Calibrator 3,034,331 15 May 1962
   Inventor: A. W. Brueckner
   Assignee: George L. Nankervis, Detroit, Michigan
   Abstract: Essential elements of COX flow calibration (weigh) stand.

4. Apparatus for Proving Meters and the Like 3,040,558 26 June 1962
   Inventor: F. C. Whiteside
   Assignee: Hudson By Oil & Gas LTD, Calgary, Alberta, CANADA
   Abstract: Seraphin type tank with sight glass on upper and lower neck. Calibrated volume tank of ellipsoidal shape and means for cleaning interior to reduce effect of buildup of crude oil deposits.

5. Flow Meter Circuit Checker 3,073,417 15 Jan 1963
   Inventor: V. R. Bauman
   Assignee: North American Aviation, Canoga Park, CA
   Abstract: Oscillator drives an excitation coil which is positioned near a turbine flowmeter such that pickup coil and associated electronic circuitry can be checked without removing turbine meter from installation or disconnecting circuitry.

6. Meter Calibration 3,092,991 11 June 1963
   Inventor: W. C. Crawford, Jr.
   Assignee: Plantation Pipe Line, Decatur, GA
   Abstract: Describes double chronometry method of correcting flow prover volume for a fixed time interval to overlapping time interval for passing of N blades of turbine flowmeter.
7. Fluid Meter Calibration
   Inventor: R. E. Boyle
   Assignee: Service Pipe Line Co., Tulsa, OK
   Abstract: Rigid piston in straight pipe. Piston has molded elastomeric seals and uses electromagnetic proximity sensor for detecting discrete positions of prover piston.

8. System for Calibrating Pipe Line Flowmeters
   Inventor: R. G. Smith
   Assignee: Socony Mobil Oil Co., New York, NY
   Abstract: Method of comparing a volumetric flowmeter to be calibrated with a distant master flowmeter located on the same pipeline. Telephone circuit used to coordinate simultaneous measurement by two flowmeters.

9. Dynamic Error Calibrator
   Inventor: J. J. Lindquist
   Assignee: North American Aviation, Canoga Park, CA
   Abstract: Dynamic response of flowmeters - step changes in flowrates through flowmeter are induced by means of solenoid valves.

10. Volumetric Flowmeter Calibrator
    Inventor: J. J. Lindquist
    Assignee: North American Aviation, Canoga Park, CA
    Abstract: Liquid flowmeter calibration using a vertical standpipe with necked down areas for precise volume determination and special means of necking down to prevent sloshing.

11. Automatic Meter Prover
    Inventor: R. W. Hill
    Assignee: National Tank Co., Tulsa, OK
    Abstract: Method of comparing production flowmeter against a master flowmeter.

12. Calibration Device
    Inventor: J. S. Lomay
    Assignee: United Aircraft Corp., East Hartford, CT
    Abstract: Insulated tank suspended on loads cells and using flexible hose to minimize reaction forces of fluid entering and leaving tank. Level sensors in tank are used for volume determination. Integral weights used for weigh system calibration. Particularly suitable for cryogenic flowmeter calibration.

13. Proving Flowmeters
    Inventor: M L. Barrett, Jr.
    Assignee: Shell Oil Co., New York, NY
    Abstract: Two methods of recycling a neoprene ball in a pipeline prover.
Inventors: D. B. Fournier and U. A. Strang
Assignee: Jered Industries, Birmingham, MI
Abstract: Method of comparing an orifice with an orifice having a known flowrate characteristic with a liquid head tank system.

Inventor: R. W. Howe
Assignee: Halmor Industries, Tulsa, OK
Abstract: Rigid piston flow prover with four-way valve to reverse direction of piston motion and microswitches actuated by prover piston striking ball bearing.

Inventor: J. C. Halpine and B. M. Moroney
Assignee: Halmor Industries, Tulsa, OK
Abstract: Ball prover using four-way valve for reversing flow direction of neoprene ball in a U-shaped pipeline. Four-way valve has double seal and means for detecting leakage through either seal.

17. Method and Apparatus for Calibrating Flowmeters 3,324,707 13 June 1967
Inventor: R. Charbonnier
Assignee: Societe Rochar Electronique Montrouge, Seine, France
Abstract: Describes a method of double chronometry for calibrating a turbine flowmeter with a Seraphin type head tank.

18. Fluid Level Gauge 3,316,763 2 May 1969
Inventor: C. A. DeGiers
Assignee: Liquidometer Corp, Long Island City, NY
Abstract: Several methods of using magnetic forces to detect movement of a float in a standpipe.

19. Flowmeter Proving Apparatus 3,387,483 11 June 1968
Inventor: L. R. Van Arsdale
Assignee: M & J Valve Co., Houston, TX
Abstract: Two gate valves and access port between the two valves allows removal and insertion of the ball in a unidirectional ball prover.

Inventor: R. H. Pfrehm
Assignee: ESSO Research and Engineering Co., Houston, TX
Abstract: Turnstile actuator moves several balls through the sealing zone between the inlet and outlet of a ball prover. This arrangement permits recycling the balls in an oval shaped pipe prover.
Inventor: E. E. Francisco, Jr.
Assignee: Flow Technology, Inc., Tempe, AZ
Abstract: Describes method of double chronometry now used in the Brooks flow prover control. Also describes use of prover, magnetic means of sensing discrete positions of the free pistons and the use of annular valves for bypassing the flow around the prover piston/cylinder section.

Inventors: W. K. Luse and G. E. Smith
Assignee: Esso Research and Engr, Houston, TX
Abstract: Liquid flow prover using a straight cylindrical pipe and a rigid prover piston which moves bidirectional through the pipe. Uses the equivalent of a four-way valve to provide bidirectional movement of the prover piston. Piston uses two molded elastomeric scales on each end for sealing.

Inventors: M. H. Grove and L. R. Van Arsdale
Assignee: M & J Valve Co., Houston, TX
Abstract: A bidirectional flow prover using an elastomeric spherical plug. Proved pipe section is a U-shaped pipe layout. Means are provided for connecting any one of several flowmeters for calibration with one set up. Valves are double block and bleed configuration to insure no leakage through a closed valve will cause the calibration to be in error.

24. Meter Calibration 3,446,055 27 May 1969
Inventors: L. Tuck and B. E. Ewers
Assignee: Phillips Petroleum Co., Delaware
Abstract: Fluid flow prover using an elastomeric sphere as a free piston in a U-shaped piping arrangement. Primary claim is to use heating up to 200°F to expel hydrocarbon calibration fluid and thus prevent contamination with air when draining and refilling with another fluid.

Inventor: F. F. Shamp
Assignee: Callbration and Proving of Meters
Abstract: Fluorescent material is injected in a pipeline of known volume between the injection point and a downstream detection point (Would not be very accurate unless pipe is quite long. Accuracy would be affected by change in the wavefront of the fluorescent material).
26. Meter Proving 3,457,768 29 July 1969
Inventor: A. W. Jasek
Assignee: Esso Research and Engineering, Houston, TX
Abstract: Bidirectional flow prover using a straight pipe and rigid prover piston for calibrating orifices in a gas pipe line.

Assignee: Flow Technology Inc., Tempe, AR
Abstract: Flow prover using a rigid piston with a built in poppet valve. A cable wrapped on a threaded drum is described for piston displacement measurement.

Inventor: M. Layhe
Assignee: General Descaling Co. LTD, Worksop, England
Abstract: Two poppet valves allow the capture and recycle transfer of an elastomeric sphere in a ball prover. Prover pipe layout is U-shaped. Spherical piston drops through the poppet valves by gravity from the outlet capture point to the inlet starting location.

Inventor: F. M. Lathrop II
Assignee: M & J Valve Co, Houston, TX
Abstract: Elastomeric spherical piston is propelled by fluid flow in a pipeline flow prover. Means for detection of leakage between double block valves assures leakage does no affect calibration.

30. Calibrating Barrel 3,541,837 24 Nov. 1970
Inventors: B. E. Davis and P. V. Gillian
Assignee: Signet Controls Inc., Tulsa, OK
Abstract: A method of gravity return of a elastomeric spherical ball in a ball prover.

31. Meter Prover 3,580,045 25 May 1971
Inventor: R. H. Pfrehm
Assignee: Esso Research and Engr, Houston, TX
Abstract: Liquid flow prover using a rigid piston with two spring loaded, lip seals. Prover piston moves bidirectionally in a straight pipe section. Spool type four-way valve reverses flow through prover. Magnetic ring on prover piston is used for position sensing.

Inventor: W. B. Basler
Assignee: Firma Rheometron GmbH, Basel, Switzerland
Abstract: Calibration of a fluid meter using gravity feed of fluid from a head tank and level sensing means in the tank to determine fixed volume during calibration.

301
Inventors: E. C. Smith and C. P. Kimball
Abstract: A piston is driven by a variable speed motor through a ball lead screw for calibration of water meters.

34. Meter-Proving Method and Apparatus 3,638,475 1 Feb. 1972
Inventors: M. H. Grove and L. R. VanArsdale
Assignee: M & J Valve Co., Houston, TX
Abstract: Spool valve arrangement for recycle of an elastomeric spherical piston in a ball flow prover.

Inventors: B. E. Davis and P. V. Gillian
Assignee: Signet Controls, Tulsa, OK
Abstract: Method of recycling elastomeric spherical balls in a ball prover by gravity.

Inventor: R. A. Brown
Assignee: Eastman Kodak Co., Rochester, NY
Abstract: An annular, elastomeric diaphragm is used to separate a corrosive fluid being metered from a displaced, non-volatile fluid which is driven into a standpipe having a narrow entrance and exit for accurate detection of a fixed volume displacement.

37. Meter Proving Method and Apparatus 3,668,923 13 June 1972
Inventors: M. H. Grove and L. R. VanArsdale
Abstract: A bidirectional ball prover using a gate valve constructed as a four-way valve to reverse the flow. Valve has double seal and means of leak detection to assure leakage is not causing an error during a prover run.

38. Meter Proving System 3,673,851 4 July 1972
Inventors: E. L. Wright and E. Meseck
Assignee: Customline Control Products Inc., Linden, NJ
Abstract: Bidirectional piston type prover which may be used to check an active flowmeter.

Inventor: M. L. Barrett, Jr.
Abstract: Several elastomeric spherical balls are recycled in a unidirectional ball prover having a U-shaped piping layout. Various devices are described for capturing the balls in the interchange between the outlet and inlet. Auxiliary pumps are used to transfer the balls through the interchange as well as launch one ball into the inlet during a proving run.
<table>
<thead>
<tr>
<th>No.</th>
<th>Title</th>
<th>Patent No.</th>
<th>Date</th>
</tr>
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<tbody>
<tr>
<td>40.</td>
<td>Double Ball Meter Prover</td>
<td>3,720,089</td>
<td>13 May 1973</td>
</tr>
<tr>
<td></td>
<td>Inventors: B. E. Davis and R. G. Dunegan</td>
<td></td>
<td></td>
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<tr>
<td></td>
<td>Assignee: Signet Controls Inc., Tulsa, OK</td>
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<tr>
<td></td>
<td>Abstract: A unidirectional ball prover uses multiple balls in the U-shaped piping system. The interchange piping between the inlet and outlet has a diameter which is slightly smaller than the proving piping. A hydraulic or pneumatic actuator piston forces an elastomeric, spherical ball into the inlet for a proving run. The remaining balls in the interchange passage form multiple seals against leakage from the inlet to outlet.</td>
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<tr>
<td>41.</td>
<td>Valveless Prover</td>
<td>3,738,153</td>
<td>12 June 1973</td>
</tr>
<tr>
<td></td>
<td>Inventor: C. R. Simmons</td>
<td></td>
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<td></td>
<td>Assignee: Helmerick and Payne Inc., Houston, TX</td>
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<tr>
<td></td>
<td>Abstract: Operation is similar to Item 28 (3,504,523)</td>
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<tr>
<td>42.</td>
<td>Meter Prover Apparatus and Method</td>
<td>3,777,545</td>
<td>11 Dec. 1973</td>
</tr>
<tr>
<td></td>
<td>Inventors: M. H. Grove and T. K. Griffen</td>
<td></td>
<td></td>
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<tr>
<td></td>
<td>Assignee: M &amp; J Valve Co., Houston, TX</td>
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</tr>
<tr>
<td></td>
<td>Abstract: A unidirectional ball prover which uses a shuttle valve device for transferring an elastomeric, spherical ball through a sealed interchange from the outlet to the inlet of the prover.</td>
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<tr>
<td>43.</td>
<td>Meter Prover Apparatus</td>
<td>3,798,957</td>
<td>26 Mar 1973</td>
</tr>
<tr>
<td></td>
<td>Inventors: C. G. Shannon, B. M. Moroney and J. R. Neal</td>
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<td></td>
<td>Assignee: Metric Inc., Tulsa, OK</td>
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<tr>
<td></td>
<td>Abstract: Elastomeric, spherical balls are used for sealing in a four-way valve arrangement in conjunction with a bidirectional ball prover.</td>
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<tr>
<td>44.</td>
<td>Three-Sphere Prover Interchange</td>
<td>3,800,587</td>
<td>2 Apr 1974</td>
</tr>
<tr>
<td></td>
<td>Inventor: W. D. Clinton</td>
<td></td>
<td></td>
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<tr>
<td></td>
<td>Assignee: Signet Controls Inc., Tulsa, OK</td>
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<tr>
<td></td>
<td>Abstract: Operation is similar to Item 42 (3,777,545)</td>
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<td>45.</td>
<td>Meter Proving Apparatus</td>
<td>3,830,092</td>
<td>20 Aug 1974</td>
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<tr>
<td></td>
<td>Inventors: M. H. Grove and R. G. Dunegan</td>
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<tr>
<td></td>
<td>Assignee: M &amp; J Valve Co., Houston, TX</td>
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<tr>
<td></td>
<td>Abstract: Operation is similar to Item 42 (3,777,545)</td>
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<td></td>
<td>Inventor: ITT Corp, New York, NY</td>
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<tr>
<td></td>
<td>Abstract: Devices for detection of passage of ball in a ball prover to prevent contact bounce of a microswitch from affecting the timing accuracy.</td>
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<td>47.</td>
<td>Meter Proving Apparatus and Method</td>
<td>3,835,695</td>
<td>17 Sept. 1974</td>
</tr>
<tr>
<td></td>
<td>Inventor: M. H. Grove</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Assignee: M &amp; J Valve Co., Houston, TX</td>
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<tr>
<td></td>
<td>Abstract: Improvement of Item 42 (3,777,545)</td>
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</tbody>
</table>
48. Double Block and Bleed Gate Valve to Control Unidirectional Meter Prover Sphere 3,848,621 19 Nov. 1974
Inventor: H. G. Dickenson
Assignee: Valve Specialty Supply Inc., Tulsa, OK
Abstract: A valve for use in a unidirectional ball prover which uses a mechanical shuttle valve to transfer the ball from the outlet to the inlet.

49. Low Flow Gas or Liquid Calibrator 3,877,287 15 Apr. 1975
Inventor: J. L. Duntz, Jr.
Assignee: USA (Secretary of the Navy)
Abstract: Piston is driven by a variable speed motor through a lead screw. The rate of fluid displaced by the piston is determined from a precise measurement of the motor speed.

Inventors: B. Last, E. M. Weinberger, J. R. Gray, G. W. Clements and Ralph E. Deffenbaugh
Assignee: Rockwell International Corp., Pittsburgh, PA
Abstract: An automated flow calibration system is described which uses a calibrated volumetric tank and integral standpipe for volume measurement. Tank uses tapered probes to determine liquid level at discrete elevations – fluid must be conductive for level sensors to function.

Inventors: D. A. Misch and O. A. Huiber
Assignee: Edge Saw Mfg. Co., Grand Rapids, MI
Abstract: A system of clear plastic cylinders and pistons with O-ring seals are used to transfer calibrating fluids through a flowmeter. Scales on the side of the clear plastic cylinders are used to determine amount of liquid transferred.

52. System for Testing Flowmeters 3,940,971 2 Mar 1976
Inventors: M. W. Krause, D. H. Strobel and E. A. Seruga
Assignee: Badger Meter Inc., Milwaukee, MI
Abstract: Elaborate, automated system for calibrating banks of water meters by using multiple standpipes with ultrasonic level sensors for detecting discrete levels within the standpipes.

Inventor: B. J. Berrettini
Assignee: Air Products and Chemicals Inc., Allentown, PA
Abstract: A vortex shedding flowmeter is used as a master flowmeter for calibration of cryogenic flowmeters.
54. **Semi-Automatic Valve Control for a Prover Loop**
   3,958,444 25 May 1976
   Inventor: E. A. Baker
   Assignee: Sun Pipe Line Co., Tulsa, OK
   Abstract: Motorized device for automatic transfer of balls through the interchange piping in a ball prover.

55. **Liquid Meter Prover Apparatus**
   3,998,089 21 Dec. 1976
   Inventors: M. H. Grove and R. G. Dunegan
   Assignee: M & J Valve Co., Houston, TX
   Abstract: A unidirectional ball prover which uses a shuttle valve device for transferring an elastomeric, spherical ball through a sealed interchange from the outlet to the inlet of the prover.

56. **Apparatus and Method for Determining the Characteristic of a Flowmeter**
   4,152,922 8 May 1979
   Inventor: E. E. Francisco, Jr.
   Assignee: Flow Technology Inc., Phoenix, AR
   Abstract: Embodiment of the flow prover now marketed by Brooks Instrument Division, Emerson Electric Co., Statesboro, GA.

57. **Meter Provers**
   4,175,421 27 Nov. 1979
   Inventors: K. J. Elderfield and C. Griffiths
   Abstract: A bidirectional ball prover using a four-way valve and special device for launching an elastomeric, spherical ball at the start of a proving run. The device includes a means of capturing the ball at the end of a run.
APPENDIX D

DYNAMIC EQUATIONS FOR THE MOTION OF THE TARE BEAM IN A DYNAMIC WEIGHT STAND (TYPE G-1)
APPENDIX D

DYNAMIC EQUATIONS FOR THE MOTION OF THE TARE BEAM IN A DYNAMIC WEIGH STAND

Figure 3-22 shows the geometry of the weighing system as used in the COX 311H Flow Calibrator. There is normally no weight on the weigh pan at the start of a run. The sliding tare weights are adjusted to delay the start of a run for 5 to 15 sec after the dump valve is closed.

The weighing system used in COX 305T Flow Calibrator uses a single weigh beam and any tare weight is added directly to weight pan (see Figure 3-16).

The following notation is used for deriving the equations of motion:

- \( d_L \) = Density of the liquid kg/cm\(^3\)
- \( F \) = Force, N
- \( g \) = Local acceleration of gravity, cm/s\(^2\)
- \( J_{WB} \) = Moment of inertia of weigh beam, kg-cm\(^2\)
- \( J_{TB} \) = Moment of inertia of tare beam, kg-cm\(^2\)
- \( L \) = Beam lengths [see Figure 3-22], cm
- \( M_B \) = Mass of reference (brass) weights on weigh pan, kg
- \( M_E \) = Equivalent dynamic mass of weighing system concentrated at the weigh pan pivot including weigh tank, kg
- \( M_E' \) = Effective dynamic mass of weighing system concentrated at the weigh pan pivot including mass of brass weights and mass of fuel in weigh tank, kg
- \( M_F \) = Mass of fuel in the tank, kg
- \( M_{LK} \) = Mass of linkage between weigh beam and tare beam, kg
- \( M_T \) = Mass of tare weight or weights, kg
- \( M_{TB} \) = Mass of tare beam, kg
- \( M_p \) = Mass of weight pan, kg
- \( M_p' \) = Effective static mass of weigh pan, beams and linkage concentrated at the weigh pan pivot but excluding weigh tank, kg.

[See Equation D-1]
\[ M_W = \text{Mass of weigh tank (dry), kg} \]

\[ M_{WB} = \text{Mass of weigh beam, kg} \]

\[ R_o = \text{Lever arm ratio } = \left( \frac{L_2}{L_1} \right) \left( \frac{L_4}{L_3} \right) \]

\[ W_A = \text{Actual mass rate of liquid flow kg/S} \]

\[ t = \text{Actual time from start of run, s} \]

\[ t' = \text{Theoretical time from start of run, s} \]

\[ t_T = \text{Tare beam rise time, s} \]

\[ v = \text{Vertical velocity of tare beam at weigh pan pivot cm/s} \]

\[ X = \text{Distance of tare weight from center of rotation, cm} \]

\[ y = \text{Vertical displacement of tare beam at pan pivot, cm} \]

\[ \theta = \text{Angular displacement, radians} \]

Subscripts:

\[ \text{LK} = \text{Linkage} \]

\[ \text{T} = \text{Weigh tank} \]

\[ \text{TB} = \text{Tare beam} \]

\[ \text{WB} = \text{Weigh beam} \]
D.1 DERIVATION OF THE DYNAMIC EQUATIONS
FOR THE MOTION OF THE TARE BEAM

A static balance between the compound weigh beam system and the weigh tank and its contents as illustrated by Figure 3-22 is given by the following equation:

\[
R_0(M_p + M_B) + \left( \frac{X}{L_3} \right) \left( \frac{L_2}{L_1} \right) M_T g = (M_w + M_f) g \tag{D-1}
\]

where \( M_p \) = Effective static mass of the weighing system when concentrated at the weigh pan pivot but excluding the mass of the weigh tank and the tare weights.

The effective static mass of the weigh pan can be calculated by equating the moments produced by the various components of the weighing system from Figure 22 as follows:

\[
M_p + M_{WB} \left( \frac{L_5}{L_2} \right) \left( \frac{L_3}{L_4} \right) + M_{LK} \left( \frac{L_3}{L_4} \right) + M_{TB} \left( \frac{L_6}{L_4} \right) g = [M_p] g \tag{D-2}
\]

The effective force \( F \) tending to lift the tare beam at the pivot of the weigh pan is given by the following equation:

\[
F_y = \left[ \left( \frac{M_w + M_f}{R_0} \right) - (M_p + M_B) - M_T \left( \frac{X}{L_4} \right) \right] g \tag{D-3}
\]

It is assumed that there is no liquid in the weigh tank at the instant the dump valve is closed. The calibration run starts when the liquid starts accumulating in the weigh tank. The tare weight is positioned and/or selected to keep the tare beam resting against the lower stop for 5 to 15 seconds before the timer is started. Static balance is achieved the instant the tare beam starts to lift at the time \( t_1 \) when the right side of Equation (D-3) is equal to zero. The accumulation of the fuel at time \( t_1 \) is given by the following equation:

\[
M_{f1} = W_A t_1 \tag{D-4}
\]

where \( W_A \) = actual mass rate of liquid flow, kg/s.
At the start of a run, there are normally no reference weights on the weigh pan thus \( M_B = 0 \). The tare beam starts to lift at \( t_1 \) seconds after the dump valve closes. The position of the tare weight or weights can be calculated by equating the right side of Equation (D-3) to zero and solving for \( X \), or

\[
X = \left( \frac{L_4}{M_T} \right) \left[ \frac{M_W + W_A t_1}{R_O} - M_P \right]
\]  

(D-5)

where \( M_T = 1.0 \) or \( 2.0 \) kg for the COX 311H Flowmeter Calibrator.

For the case of the COX 305T Flowmeter Calibrator, \( X = L_4 \) since the tare weights are added at the weigh pan. The tare weight \( M_T \) to be added to the COX 305T weigh pan can be calculated from Equation (D-5) as

\[
M_T = \frac{M_W + W_A t_1}{R_O} - M_P
\]

(D-6)

A weight or weights having a mass \( M_B \) is then placed on the weigh pan after the tare beam rises sufficiently to actuate the proximity switch and start the timer.

The total mass of fuel which has accumulated in the weigh tank at the end of a run is given by the following equation:

\[
M_{F_2} = W_A t_2
\]

(D-7)

and the change in mass of fuel in the weigh tank can be found by subtracting Equation (D-4) from Equation (D-7) or

\[
(M_{F_2} - M_{F_1}) = W_A (t_2 - t_1)
\]

(D-8)

The change in mass of fuel in the weigh tank is equal to the product of the mass of the weights added to the weigh pan \( M_B \) after the run starts and the compound lever arm ratio \( R_O \), or from Equation (D-8)

\[
M_B = \frac{(M_{F_2} - M_{F_1})}{R_O} = \frac{W_A}{R_O} (t_2 - t_1)
\]

(D-9)

where \( (t_2 - t_1) \) = Run time between the events when the tare beam starts to lift at the start and end of a run.
It is assumed that the liquid flow rate \( W_A \) is constant throughout the calibration run. Additional timing errors can result if the liquid flow rate deviates from the average flow rate at the start and end of a calibration run. This type of error has not been investigated in this study.

Since a finite time is required for the tare beam to rise due to the inertia of the weighing system, additional liquid accumulates in the weigh tank before the actual start and stop times \( t_1 \) and \( t_2 \) occur when the proximity sensor is actuated by the rising tare beam. The liquid that accumulates in the weigh tank after the static balance point provides the unbalanced force that lifts the tare beam or

\[
F_1 = \frac{W_A}{R_0} (t_1 - t_1') g \quad \text{(D-10)}
\]

and

\[
F_2 = \frac{W_A}{R_0} (t_2 - t_2') g \quad \text{(D-11)}
\]

where the forces \( F_1 \) and \( F_2 \) are a function of time \( t \).

The total kinetic energy of the system in motion is given by the following equation:

\[
\text{K.E.} = \frac{1}{2} \left[ (M_B + M_p)L_4^2 + J_{TB} + M_T X^2 + M_{LK} L_3^2 \right] \left( \frac{d\theta}{dt} \right)^2_{TB}
\]

\[
+ \frac{1}{2} \left[ J_{WB} + (M_W + M_F) L_1^2 \right] \left( \frac{d\theta}{dt} \right)^2_{WB} \quad \text{(D-12)}
\]

The angular movement of the weigh beam can be related to the angular movement of the tare beam by the following equation:

\[
\theta_{WB} = \left( \frac{L_3}{L_2} \right) \theta_{TB} \quad \text{(D-13)}
\]

and differentiating Equation (D-13) gives

\[
\left( \frac{d\theta}{dt} \right)_{WB} = \frac{L_3}{L_2} \left( \frac{d\theta}{dt} \right)_{TB} \quad \text{(D-14)}
\]
The vertical movement $y$ of the tare beam at the location of the pivot for the weigh pan can be found from the following equation for small angular movement

$$y = L_4 \Theta_{TB}$$  \hspace{1cm} (D-15)

and the vertical velocity $v$ is found by differentiating Equation (D-15) or

$$v = \frac{dy}{dt} = L_4 \left(\frac{d\Theta}{dt}\right)_{TB}$$  \hspace{1cm} (D-16)

A mass which is equivalent to the total dynamic mass of the system but concentrated at the suspension pivot for the weigh pan can be calculated from Equation (D-12) by using Equation (D-16) or

$$M'_{E} = M_B + M_p + \frac{J_{TB}}{L_4^2} + M_T \left(\frac{X}{L_4}\right)^2 + M_{LK} \left(\frac{L_3}{L_4}\right)^2 \hspace{1cm} (D-17)$$

but since

$$R_o = \left(\frac{L_2}{L_1}\right) \left(\frac{L_4}{L_3}\right)$$

Equation (D-17) becomes

$$M'_{E} = M_B + M_p + \frac{J_{TB}}{L_4^2} + M_T \left(\frac{X}{L_4}\right)^2 + M_{LK} \left(\frac{L_3}{L_4}\right)^2 \hspace{1cm} (D-18)$$

letting

$$M'_E = M_E + M_B + \frac{M_F}{R_o^2}$$  \hspace{1cm} (D-19)
and using Equation (D-8) and (D-9), Equation (D-17) becomes

\[ M_E = M_p + \frac{J_{TB}}{L_4^2} + M_T \cdot \frac{X}{L_4}^2 + M_{LK} \cdot \frac{L_3}{L_4}^2 + \frac{J_{WB}}{L_4^2 R_0} + \frac{M_W}{R_0^2} \]  

(D-20)

The following assumptions are made relative to the dynamic motion of the weighing motion of the weighing mechanism:

1. The system is undamped

2. The motion of the tare beam at the centerline of the weigh pan is large relative to the deflection of the beams, linkages and knife edges.

The dynamic equation of motion using the equivalent dynamic mass of the system concentrated at the pivot is simply the product of the equivalent mass times the acceleration \( a = \frac{d^2y}{dt^2} \) equals the equivalent force \( F \) acting at the weigh pan and from Equation (D-19):

\[
\left[ M_E + M_B + \frac{M_F}{R_0^2} \right] \frac{d^2y}{dt^2} = F 
\]

where \( y \) = vertical motion of the tare beam at the centerline of pivot supporting the weigh pan.

The effective unbalanced force \( F \) which is tending to lift the tare beam is a force which is entirely produced by the accumulation of fuel in the weight tank. It is convenient to let the rise time of the tare beam from \( t_1 \) or \( t_2 \) be time \( t_T \). The unbalanced force \( F \) in Equation (D-21) is then given as follows:

\[
F = \frac{W_A g}{R_0} t_T 
\]

(D-22)

where \( (t - t') = \) time for tare beam to rise after static balance combining Equations (D-21) and (D-22) gives

\[
\left[ M_E + M_B + \frac{M_F}{R_0^2} \right] \frac{d^2y}{dt^2} = \frac{W_A g}{R_0} t_T 
\]

(D-23)

Assuming that the mass of the fuel in the weigh tank is constant during the time the tare beam is lifting, Equation (D-23) may be integrated to give the following equation:

\[
\left[ M_E + M_B + \frac{M_F}{R_0^2} \right] \frac{dy}{dt} = C_2 + \frac{W_A g}{2R_0} t_T^2 
\]

(D-24)
but since the tare beam velocity is zero \((dy/dt = 0)\) at time \(t_T = 0\), \(C_2 = 0\). Equation (D-24) can then be integrated to give:

\[
\left[ M_E + M_B + \frac{M_F}{R_0^2} \right] y = C_1 + \frac{W_A g}{6R_0} t_T^3 \tag{D-25}
\]

Since the lift of the tare beam is referenced from movement from the lower stop, \(y = 0\) at \(t_T = 0\). The constant in Equation (D-25) is thus \(C_1 = 0\), yielding:

\[
\left[ M_E + M_B + \frac{M_F}{R_0^2} \right] y = \frac{W_A g}{6R_0} t_T^3 \tag{D-26}
\]

The assumption that the mass of fuel in the weigh tank is constant is quite precise if the average mass of fuel \(M_F\) in Equation (D-21) is calculated from the average actuation time or

\[
M_{F1} = W_A \left[ t_1 + \frac{t_{T1}}{2} \right] \tag{D-27}
\]
at the start of the run and

\[
M_{F2} = W_A \left[ t_2 + \frac{t_{T2}}{2} \right] \tag{D-28}
\]
at the end of the run.

Equation (D-26) can be solved for the time function \(t_T^3\) for a more convenient form of the equation, or

\[
t_T^3 = \frac{6R_0}{W_A g} \left[ M_E + M_B + \frac{M_F}{R_0^2} \right] y \tag{D-29}
\]
D.2  **CALCULATION OF THE TIMING ERROR CORRECTION FACTOR**

The numerical example given below is based on actual weight and dimensional measurements on a COX 305T Flowmeter Calibrator.

**Example:**

\[ y = \text{(beam deflection)} = 0.254 \text{ cm (0.1 in.)} \]

\[ W_A = 1.89 \text{ kg/s (15,000 lbm/hr)} \]

\[ t_1^t \text{ (tare time)} = 10 \text{ seconds} \]

\[ (t_2^t - t_1^t) \text{ (run time)} = 30 \text{ seconds} \]

\[ t_2^t = 40 \text{ seconds} \]

\[ M_p = 4.121 \text{ kg (9.085 lbm)} \]

\[ J_{WB} = 375.75 \text{ kg \cdot cm}^2 \text{ (128.4 lbm \cdot in.}^2) \]

\[ M_{WB} = 1.173 \text{ kg (2.586 lbm)} \]

\[ M_W = 22.53 \text{ kg (49.68 lbm)} \]

\[ L_1 = 7.239 \text{ cm (2.85 in.)} \]

\[ L_2 = 36.20 \text{ cm (14.25 in.)} \]

\[ L_5 = 17.91 \text{ cm (7.05 in.)} \]

\[ R_o = \frac{L_2}{L_1} = 4.988 \]

\[ g = 980.42 \text{ cm/s}^2 \]

The effective **static** mass of the weigh pan can be determined from Equation (D-2) or

\[ M_p^t = M_p + M_{WB} \left( \frac{L_5}{L_2} \right) \]

(D-29)

since the last two terms are zero and \( L_3 = L_4 \) due to the absence of a tare beam. Substituting values from the above tabulation into Equation (D-29) gives

\[ M_p^t = 4.701 \text{ kg} \]
The tare weight \( M_T \) required for \( t_1^i = 10 \) second tare time can be found from Equation (D-6) as

\[
M_T = \frac{22.53 + 1.89(10)}{4.988} - 4.701 = 3.605 \text{ kg}
\]

The reference weight \( M_B \) required for a \( t_2^i - t_1^i = 30 \) second run time can be found from Equation (D-9) as

\[
M_B = \frac{1.89(30)}{4.988} = 11.367 \text{ kg}
\]

Nominal weights are normally used for testing. For the purpose of this example, the exact calculated tare weight and reference weights are used.

The equivalent mass of the system can be determined from Equation (D-20) for the COX 30ST Flowmeter Calibrator where (1) the weigh beam replaces the tare beam, \( J_{TB} = 0 \), (2) there is no linkage, \( M_{KX} = 0 \) and (3) the tare weights are added to the weigh pan, \( X = L_4 \). Equation (D-20) then becomes

\[
M_E = 4.121 + \frac{375.75}{(7.239×4.988)^2} + 3.605 + \frac{22.53}{(4.988)^2}
\]

\[
M_E = 8.920 \text{ kg}
\]

The mass of fuel in the weigh tank at time \( t_1^i = 10 \) seconds is 18.9 kg and substituting into Equation (D-28) gives

\[
t_{T_1}^3 = \frac{6(4.988)(8.920 + 18.9/(4.988)^2)(0.254)}{1.89(980.24)}
\]

\[
t_{T_1}^3 = 0.03971 \quad \text{and} \quad t_{T_1} = 0.34117 \text{ second}
\]
The mass of fuel in the weigh tank at $t_2' = 40$ seconds is 75.6 kg and substituting into Equation (D-28) gives

$$t_{T2}^3 = \frac{6(4.988)(8.920 + 11.367 + 75.6/(4.988)^2)(0.254)}{1.89(980.42)}$$

$t_{T2}^3 = 0.096591$ and $t_{T2} = 0.45739$ second

The combined flowrate correction factor can be found from Equation (3-10) where:

$$t_C = t_2' - t_1'$$

$$(K_T^a) = 1 + \frac{t_{T2} - t_{T1}}{t_2 - t_1} = 1 + \frac{0.45739 - 0.34117}{30}$$

$$(K_T^a) = 1.00387$$

This value is comparable to the value given in Figure 3-23 for a deflection of $y_0 = 2.54$ mm and the curve marked "10 + 30". An iterative calculation using the average values of the fuel weights given by Equations (D-26) and (D-27) does not substantially change the above value for $(K_T^a)$. 

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APPENDIX E

DETAILED SKETCHES OF PIECE PARTS, AND SUBASSEMBLIES
FOR DUAL TURBINE FLOWMETER
ORIGINAL PAGE IS OF POOR QUALITY

**STRUT**

**Material:** 304 ST ST  
**Finish:** PASSIVATE

**Material:** 6061 ALUM  
**Finish:** ANODIZE
BLANK, SENSOR TURBINE

MAT: 416 ST ST.

SENSOR TURBINE, MACHINED

BLADE INFO:
1) 6 BLADES EQUALLY SPACED
2) LEAD: 6 IN/REV, LEFT HAND (23.5° HELIX X .832 DIA)
Mat: Al-16 Strn
Slat: Non-Magnetic SS, Stc.

Mat: 304 SS, Sil
Fin: Passivate
Pickoff Assy

Core

Material: Permalloy
APPENDIX F

DETAILED SKETCHES OF PIECE PARTS, AND SUBASSEMBLIES
FOR PROTOTYPE ANGULAR MOMENTUM FLOWMETER
FORWARD HOUSING

6061-T6 Aluminum

Note: Dimensions not shown will depend on size of other purchased parts.
Note: Dimensions not shown will depend on size of other purchased parts.
MAGNETIC COUPLER
(DRY SIDE)

Carbon Steel

6 HOLES: 1.882 +0.005
-0.000

EQUALLY SPACED

A

A

1.000 ± 0.001

0.750 ± 0.002

DIA

0.100 ± 0.002

0.467 ± 0.001

0.480 ± 0.003

0.878 ± 0.005

+0.0005

DRILL AND TAP FOR #4-40

SECTION A-A

SCALE = 2:1

327
5 MAGNETIC COUPLER  Carbon Steel
(WET SIDE)

SECTION A-A

SCALE = 2:1
ROTOR ASSY.

SEE PART (3) FOR DETAIL

2.070 ± 0.001

1.731 ± 0.001

2.230 ± 0.001
8  ROTOR SHELL  6061-T6 Aluminum

SECTION A-A
SHROUD HUB
6061-T6 Aluminum

12 VANES .050 ±.005 THICK
EQUALLY SPACED

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<tr>
<td>A</td>
<td>1.902 ± .005</td>
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<tr>
<td>B</td>
<td>1.500 ± .001</td>
<td></td>
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<td>C</td>
<td>1.340 ± .005</td>
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<tr>
<td>D</td>
<td>.5003 ± .005</td>
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<td>E</td>
<td>1.210 ± .003</td>
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REFERENCE

6061-T6 Aluminum

3 WEBS .200 ±.020 WIDE
120° APART

SECTION A-A
OUTLET STRUT

6061-T6 Aluminum

3 WEBS .20 ± .01 THICK
EQUALLY SPACED

SECTION A-A

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<td>B</td>
<td>.500 ± .005</td>
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<td>C</td>
<td>.542 ± .002</td>
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<tr>
<td>D</td>
<td>.512 ± .003</td>
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COVER 6061-T6 Aluminum

3 PLACES

pickoff cavity (3)

.750 DIA.

.812 TIP.

.393

.150 TIP. DRILL AND TAP (8 HOLES)

.150 TIP. FOR #4-40 HELICOIL

.450 MAX. DEPTH

SECTION A-A
Each addressee will receive one copy unless indicated otherwise.

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<thead>
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<td>David Davidson</td>
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<td>C. B. Stegner</td>
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<tr>
<td>Arnold Engineering Development Center</td>
<td>Arnold Air Force Station, TN</td>
<td>Marshall Kingery</td>
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</tr>
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</table>
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Attn: Steve Wnuk

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Aircraft Engine Group
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