Grain Boundary Oxidation and Fatigue Crack Growth at Elevated Temperatures

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October 1986

Prepared for
Lewis Research Center
Under Grant NAG3-348
I. INTRODUCTION

Fatigue crack growth in the air at elevated temperatures is often faster than the rate at room temperature. The accelerated fatigue crack growth has been attributed to creep and/or oxidation [1,2,3]. Creep induces grain boundary void formation and grain boundary cavitation, and the formation and the growth of grain boundary voids and cavities will accelerate fatigue crack growth.

Hull and Rimmer [4] studied the growth of grain boundary voids under stress in polycrystal copper wire. The nucleation of creep cavities in a copper base alloy was observed by Fleck, Taplin, and Beevers [5]. The nucleation and growth of cavities in iron during creep deformation at elevated temperatures was studied by Cane and Greenwood [6]. Grain boundary cavity and void nucleations during creep under a sustained stress have been analyzed by a number of investigators [7 to 16].

The cavity growth rate is related to either grain boundary vacancy diffusion or surface diffusion. The cavity growth rate has the form of the Arrhenius relation. However, grain boundary cavity nucleation and growth under a cyclic load and the relation between the growth rates of grain boundary cavities and fatigue crack have yet to be studied.

Gibb's free energies of metal oxide formation are negative. When in direct contact with oxygen, metals oxidize easily, and the rate of oxidation depends on the rate of diffusion of oxygen or metal through the oxide layer. Grain boundary is a site of high energy and a path of rapid diffusion. Therefore, the oxidation
II. GRAIN BOUNDARY OXIDATION PENETRATION

Oshida and Liu [31] have studied grain boundary oxidation penetration in a nickel base superalloy, TAZ-8A, under a stress-free condition. Each disk coupon, 15 mm in diameter and 5 mm in thickness, was oxidized in air. The oxidation temperatures were 600, 800, and 1000°C, and the exposure times varied from 100 to 1000 hours. After oxidation, each coupon was sectioned, and the sectioned surface was examined under an optical microscope. Figure 1 shows the picture of a cross section of a test coupon. The grain boundary oxide penetrates deeper than the surface oxide.

On each sectioned surface, the grain boundary oxidation penetration varied widely from one grain boundary to another. The maximum grain boundary oxidation penetration depth, \( a_m \), of a sectioned surface was measured. After the measurement, a thin layer of the coupon, approximately 80 \( \mu \)m thick, was ground off, the new surface was polished, and another maximum grain boundary oxidation penetration depth was measured. This process was repeated twelve times for each test coupon. Altogether, 144 data points were collected at the three oxidation temperatures, \( T \), and at various exposure times, \( t \). The regression analysis of the data gives the following empirical relation.

\[
a_m = \alpha t^n \exp(-Q/RT)
\]  

where \( a_m \) is in cm; \( t \), in seconds; the activation energy, \( Q \) is 4.25 Kcal/mol; \( T \) in °K; and \( R = 1.987 \) cal/mol/°K. \( \alpha = 1.34 \times 10^{-3} \). \( n = 0.25 \). The coefficient of auto-correlation is 0.96.
Reuchet et al. [32,33] studied oxidized depth of MC carbides in a cobalt-base superalloy (Mar M509). They found a time exponent \( n = 0.25 \). Stott et al. [34,35] studied intergranular oxidation in Ni-Cr alloys, and they found \( n = 0.48 \) for 60Ni - 40Cr alloy, 0.51 for Ni - 15.1Cr - 1.1Al alloy, and 0.66 for Ni - 28.8Cr - 1.0Al alloy. They concluded that the intergranular oxide penetration depth in Ni-Cr alloys followed a parabolic rate relation.

Grain boundary oxide penetration is controlled by grain boundary diffusion of oxygen, and grain boundary diffusion is a function of the relative orientations of the two neighboring grains [36,37,38], as shown in Figure 2. The variation of grain boundary diffusion rate could be one of the causes for the statistical scatter of the measured oxide penetration depths.

At any given combination of temperature, \( T \), and exposure time, \( t \), the value of \( a \) can be calculated from the measured \( a_m \) value by using Equation (1). The variation of the calculated \( \alpha \)-values reflects the statistical scatter of the measured \( a_m \)-values. The Weibull plot of all of the 144 values of \( a \) is shown in Figure 3. The Weibull distribution function is

\[
[1 - P(a)] = \exp[- \frac{(a - a_u)}{a_o}] = \exp[- \frac{(a - a_u)}{\eta_a}]
\]

where \( P(a) \) is the probability of finding an \( a \)-value less than \( a \) on a sectioned surface. \( a_u \) is the location parameter. It is the horizontal shift for each of the data points so that all of the points will be on a straight line in the plot. \( b \) is the slope of the line, and it is called shape parameter or Weibull modulus. \( a_o \) and \( \eta_o = a_o^b \) set the scale for the Weibull distribution. \( a_o \) is the value of \( (a - a_u) \) at \( \ln \ln(1/[1 - P(a)] \} = 0 \). For the data in Figure 3, \( a_u = 0.53 \times 10^{-3} \), \( b = 1.85 \), and \( a_o = 0.51 \times 10^{-3} \). The experimental details and a more
detailed discussion on the oxide formation and the statistical scatter are given in Reference [31].

If the grain boundary oxidation penetration rate is controlled by the grain boundary diffusion rate, and if grain boundary diffusion can be considered as a one-dimensional flow, the oxidation penetration depth can be written as

\[ a_m = at^{0.5} \exp \left(-\frac{Q_{gb}}{2RT}\right) \]

(3)

\( Q_{gb} \) is the activation energy of grain boundary diffusion. This result is certainly different from the empirical relation, Equation (1).

The coefficient of grain boundary diffusion is several orders of magnitude higher than that of lattice diffusion. Nevertheless, the grain boundary diffusion kinetics are affected by lattice diffusion. Whipple [39] has analyzed the effects of lattice diffusion on grain boundary diffusion. These effects for TAZ-8A have yet to be assessed quantitatively.

The kinetics of grain boundary oxide penetration will certainly be related to the morphology of the oxide. Grain boundary oxides have two different shapes: pancake type and cone type. Furthermore, the detailed chemical processes of oxidation have also to be taken into consideration in a theoretical analysis. Grain boundary oxide penetration is further complicated by the internal stresses caused by the oxide formation.

For the moment, Equation (1) can be treated as an empirical relation. Perhaps, the oxide penetration depth at a crack tip can be written in the form

\[ \frac{a_m}{C} = F \left( \frac{D}{C} \right) \]

(4)
where $D$ is diffusion coefficient, and $C$ is the magnitude of the diffusion jumping vector or interatomic spacing. The details of the function, $F$, are unknown. Assuming a simple power relation, we have

$$a_m = \beta C(D_0 t/C)^n \exp(-n\Delta H/RT) = \alpha t^n \exp(-Q/RT)$$

(D_0)$ is the diffusion coefficient at $T = 0$. $\alpha$, $\beta$, and $n$ are constants. The apparent activation energy, $Q$, for grain boundary oxide penetration is not necessarily equal to the activation energy of diffusion, $\Delta H$. If the penetration depth is dependent on both grain boundary and bulk diffusions, $a_m$ is related to both $(D_{gb} t/C)$ and $(D_b t/C)$. $D_{gb}$ and $D_b$ are grain boundary and bulk diffusion coefficients.
III. THE INTERMITTENT MICRO-RUPTURE MODEL FOR HIGH TEMPERATURE FATIGUE CRACK GROWTH

Fatigue crack growth at elevated temperatures is sensitive to both frequency and temperature. Figures 4a \([40, 41]\) and 4b \([42]\) show the frequency and temperature effects on the fatigue crack growth in IN-100. The data merge onto two limiting lines, one on the right and one on the left of the data band. Along these two limiting lines, the fatigue crack growth rate is independent of frequency and temperature. The right hand side limiting line is for high frequency and low temperature. The left hand side limiting line is for high temperature and low frequency. However, it is not certain that the left limiting line always exits. Between these two limiting lines, \(\frac{da}{dN}\) is sensitive to both frequency and temperature. "\(\frac{da}{dN}\)" increases with temperature and decreases with an increase in frequency.

At a constant \(\Delta K\) level and at a given test temperature, the more detailed frequency effects on the fatigue crack growth rate are shown in Figure 5 \([41, 43-48]\). The cyclic crack growth rates, \(\frac{da}{dN}\), of a number of materials in the low frequency region are inversely proportional to cyclic frequency, \(v\), and are linearly proportional to the length of the time period per cycle. The time rate of the fatigue crack growth, \(\frac{da}{dt} = (\frac{da}{dN})(1/v)\), is constant. In this region, the fatigue crack growth is intergranular.

The fatigue crack growth rate decreases as cyclic frequency increases. At a very high frequency, the fatigue crack growth rate is independent of frequency and temperature. It corresponds to the right
hand side limiting line. At such a high frequency, the fatigue crack growth is **transgranular**, and the observed fatigue striations on a crack surface indicate that fatigue crack growth is caused primarily by crack tip cyclic plastic deformation.

In the **intermediate frequency** region, a fatigue crack grows in a **mixed mode** both intergranularly and transgranularly, and the growth rate is sensitive to both frequency and temperature.

For constant-K tests at elevated temperatures, two crack growth features are common: (i) the time rate of crack growth is constant, (i.e. $da/dt = \text{constant}$) and (ii) crack growth is intergranular. Crack growth at constant-K is often referred to as creep crack growth.

In the low frequency region, $da/dN$ is inversely proportional to frequency, $v$, and frequency is the inverse of the time period per cycle. Therefore, in the low frequency region, the time rate of fatigue crack growth is also constant as the creep crack growth rate. Furthermore, fatigue crack growth in this region is also intergranular. Therefore, fatigue crack growth in the low frequency region, where the intergranular crack growth rate $da/dN$ is inversely proportional to $v$, is often referred to as creep crack growth.

However, a few questions remain unclear. Does creep crack growth imply that the fatigue accelerated crack growth is caused by grain boundary void nucleation and growth and/or by crack tip creep deformation? Does the inverse relation between $da/dN$ and $v$ preclude the possibilty that grain boundary oxidation is the under-lyng cause for the accelerated fatigue crack growth at elevated temperatures? In this section, oxidation will be analyzed as a possible cause of the accelerated fatigue crack growth at elevated temperatures.
In the low frequency region of Figure 5, the fatigue crack growth rates of Inconel 718, Inconel X-750, Astroloy at 700\(^\circ\)C and 760\(^\circ\)C, and Cr-Mo steels, are inversely proportional to frequency. The cyclic loading patterns are also shown in the figure. For Inconel 718 and Astroloy, a hold time, \(\Delta t_H\) at \(K_{\text{max}}\) was applied. For Inconel X-750, Cr-Mo steels, and Astroloy at 700\(^\circ\)C, a triangular loading pattern was used.

Antolovich et al. [49] found that oxide in a smooth specimen ruptured when the applied stress reached a critical value. The applied stress at rupture is inversely related to the oxide size. The critical crack tip oxide size at rupture must be related to the stress intensity factor, \(K\). The oxygen arriving at a crack tip will have to diffuse along the grain boundary into the region ahead of the crack tip forming oxide. When the crack tip grain boundary oxide reaches the critical size, \(\delta a\), the oxide will rupture and the crack will grow by the amount of \(\delta a\). Once the crack tip advances to its new position, this process of grain boundary diffusion, grain boundary oxidation, rupturing of the grain boundary oxide, and crack advancing will be repeated again. This process of micro-ruptures of crack tip grain boundary oxides can reoccur intermittently many times during a fatigue cycle. Coffin (1) has suggested this process as a mechanism of the accelerated fatigue crack growth at elevated temperatures. In this paper, a quantitative model of intermittent micro-ruptures of grain boundary oxide will be constructed and it will be shown that the intermittent micro-ruptures of grain boundary oxide can lead to a fatigue crack growth rate inversely proportional to \(V\).

The tests with hold time will be analyzed first. During the
hold time, \( \Delta t_H \) at \( K_{\text{max}} \), a number of intermittent micro-ruptures will take place. Assume that every micro-rupture will advance the crack to the "tip" of the oxide. Therefore, the time increment, \( \delta t \), necessary for the oxide starting from the crack tip, to reach the critical rupture size, \( \delta a \), is given by Equations (4) and (5). For a simple power relation, we have

\[
\delta t = \left( \frac{C}{D_{\text{gb}}} \right) \left( \frac{\delta a}{\beta C} \right)^{1/n}
\]

(6)

The number of micro-ruptures during \( \Delta t_H \) is

\[
m = \frac{\Delta t_H}{\delta t} = \left( \frac{\Delta t_H}{D_{\text{gb}}} \right) \left( \frac{\beta C}{\delta a} \right)^{1/n}
\]

(7)

"m" is proportional to \( \Delta t_H \). Both \( m \) and \( \Delta t_H \) are inversely proportional to frequency, \( \nu \).

Fatigue crack growth per cycle is the sum of the rapid and intermittent micro-ruptures per cycle.

\[
\frac{da}{dN} = m \delta a
\]

(8)

Substituting Equation (7) into Equation (8), we have

\[
\frac{da}{dN} = \beta' \Delta t_H \frac{D_{\text{gb}} (C/\delta a)^{(1-n)/n}}{\nu (C/\delta a)^{(1-n)/n}} = \beta' \frac{D_{\text{gb}}}{\nu} (C/\delta a)^{(1-n)/n}
\]

(9)

da/dN are inversely proportional to \( \nu \).
For \( n = 0.25 \), \( \frac{da}{dN} \) is inversely proportional to \( \delta a^3 \). Fatigue crack growth rate increases rapidly as \( \delta a \) becomes small. \( \delta a \) is smaller if the oxide is more brittle.

For a given material, \( \delta a \) and \( m \) are functions of \( K_{\text{max}} \) during the hold time. Therefore, we have

\[
\frac{da}{dN} = \frac{1}{\nu} f(K_{\text{max}}, T).
\] (10)

as shown by the data in the low frequency region in Figure 5.

For the triangular loading pattern, let us assume that the critical crack tip oxide size, \( \delta a \), at rupture is a function of the crack tip field, the crack tip field can be characterized by the stress intensity factor, \( K \), and the crack tip field is independent of the cyclic frequency, \( \nu \).

Figure 6 shows the triangular loading at two different frequencies. (We use the triangular loading as an illustration, but the following analysis is applicable to any other wave shape). If the crack tip fields at \( K_i \) are the same at both of these two frequencies, the critical oxide penetration depths, \( \delta a_i \) at rupture must be the same. During the time interval \( \Delta t_i \) at \( K_i \), a number of intermittent micro-ruptures will take place. At the same \( K_i \) level, the time increment, \( \delta t_i \), necessary for the oxide to reach the critical size, is directly related to \( \delta a_i \), Equation (6). The number of micro-ruptures, \( m_i \), during the time interval, \( \Delta t_i \) at \( K_i \) is simply \( \Delta t_i / \delta t_i \). "\( m \)" is proportional to \( \Delta t \) and inversely proportional to frequency, \( \nu \). This inverse relation between \( m_i, \Delta t_i \), and \( \nu \) is true at any \( K_i \)-level.

The fatigue crack growth rate is the sum of the rapid and intermittent micro-ruptures at all the \( K_i \)-levels during one cycle.
"m" is inversely proportional to \( v \) at any \( K \)-level. Therefore, \( \frac{da}{dN} \) is inversely proportional to \( v \).

The crack growth rate at a frequency \( v \) can also be written as

\[
\frac{da}{dN} = \frac{v_0}{v} \frac{da}{dN} \left( \frac{v_0}{v} \right) = \frac{v_0}{v} f(K_{\text{max}}, \Delta K, T)
\]  

(12)

\( \frac{da}{dN} v_0 \) is the crack growth rate at a reference frequency, \( v_0 \). Equations (11) and (12) for arbitrary wave shapes are derived with the assumption that \( K \) is capable of characterizing the crack tip field and the crack tip field is not affected by cyclic frequency. However, the creep stress relaxation at a crack tip and the internal stress caused by oxidation have not been taken into account. They could be the reasons why some of the data in the low frequency region in Figure 5 do not obey the inverse relation. No such assumption is necessary for the derivation of Equation (8) for the crack growth rate with a holdtime at \( K_{\text{max}} \).

In the low frequency region, when there is enough time for repeated grain boundary oxidation penetrations and repeated micro-ruptures of the oxides to take place, the fatigue crack growth rate along an embrittled grain boundary is inversely proportional to the frequency, and crack growth is intergranular. Therefore, these two crack growth features of inverse relation of \( da/dN \) with frequency and intergranular crack growth can be caused by grain boundary oxidation, and they cannot be attributed to creep cracking without
additional substantive experimental evidence. Such inverse relationship in the low frequency region is shown in Figure 5 for Inconel 718, Inconel X-750, Astroloy, and Cr-Mo steels.

In order to accelerate fatigue crack growth, the oxygen atoms must reach the crack tip during the process of crack growth rather than after. Therefore, the accelerated fatigue crack growth is closely related to the rate of the transport of oxygen.

For a given material at a given applied $K$ level, there exists an intrinsic crack growth rate, $(da/dN)_f$, which is caused by the fatigue process of cyclic crack tip plastic deformation alone, without the effect of oxidation. At a very high frequency, the diffusing species does not have enough time to travel in order to follow the crack tip. Therefore, oxidation does not have much effect on the fatigue crack growth. The fatigue crack growth is caused by cyclic plastic deformation, and the growth is transgranular. The $da/dN$ is not limited by the transport process, and it is independent of frequency and temperature, so that the crack growth rate data in Figures 4a and 4b will merge to the right hand side limiting line of high frequency and low temperature and the data in Figure 5 will level off in the high frequency region. If the cyclic plastic deformation is dependent on frequency and temperature, $da/dN$ will be weakly dependent on frequency and temperature.

In Figure 5, between the low-frequency faster intergranular fatigue crack growth caused by the intermittent micro-ruptures, and the high-frequency slower transgranular intrinsic fatigue crack growth due to cyclic plastic deformation, there exists a region of mixed mode of both intergranular and transgranular crack growth, as observed by Pelloux and Huang [46].
IV. DISCUSSIONS

The accelerated fatigue crack growth at elevated temperatures has been attributed to either oxidation or creep damage. Both oxidation and creep have been shown as possible mechanisms for the high temperature fatigue damage. Grain boundary void formation and cavitation are the result of surface diffusion and/or grain boundary vacancy diffusion, while grain boundary oxidation is primarily caused by the diffusion of oxygen. The kinetics of the diffusions of vacancies and oxygen atoms is shown schematically in Figure (7). The figure indicates that one mechanism dominates in the high temperature region and the other dominates in the low temperature region. Therefore, the question is not which one of these two mechanisms causes high temperature fatigue damage. The problem is to define the different regions dominated by these two different mechanisms.

The quantitative relations between the diffusion rates and the rate of oxide rupture and the rate of nucleation and growth of voids and cavities, and their relations with fatigue crack growth have not yet been established. It is obvious that fatigue crack growth rate is not necessarily linearly proportional to the diffusion rates, therefore, the activation energy for diffusion may not be equal to the "activation energy" for fatigue crack growth. The functional relationships between \( \frac{da}{dN} \) and the diffusion rates of vacancies and oxygen atoms depend on the detailed physical processes of fatigue crack growth. If a simple power relationship exists between \( \frac{da}{dN} \) and diffusion rate, then the rate, \( R \) (in Figure 7) can also be interpreted as the crack growth rate caused by the diffusion process.
Without a clear understanding of the underlying reasons for the observed fatigue crack growth behaviors, it is difficult and unsafe to extrapolate a limited amount of experimental data to make fatigue life predictions. For example, to extrapolate the crack growth data in Figure 5, from the low frequency region into the high frequency region or vice versa will underestimate the crack growth rate. Therefore it is unsafe.

If creep is the damage mechanisms for high temperature fatigue, and if grain boundary creep cavitation is induced by a tensile stress together with vacancy diffusion, the tensile stress in a redundant structure will decrease by creep stress relaxation, and the decreased tensile stress will reduce the rate of cavitation. Thermal stress is a transient stress. Thermal stress will be relaxed as creep deformation takes place. In a sense, it is "redundant". Therefore, creep damage may not be as important in thermal fatigue or thermal-mechanical fatigue in structural components, where creep relaxation takes place.

Multidisciplinary studies based on empirically observed physical processes are needed to develop mechanistic and quantitative models for oxidation damage and creep damage in high temperature fatigue. The first step in the development of such models for oxidation damage is a quantitative analysis of grain boundary oxidation.

The high temperature fatigue crack growth model of intermittent micro-ruptures of grain boundary oxides gives an inverse relationship between fatigue crack growth rate, \( \frac{da}{dN} \) and the cyclic frequency, \( \nu \). This inverse relation is observed for a number of high temperature alloys.
in the low frequency region. Grain boundary oxidation is certainly a possible mechanism for the accelerated fatigue crack growth at elevated temperatures.

Grain boundary oxidation was studied for samples free of stress. The effects of an applied stress and an imposed cyclic strain on the diffusion of oxygen and oxidation still need to be addressed.

Equation (1) is for grain boundary bulk oxide penetration. It is conceivable that even a monolayer of oxide will reduce the grain boundary cohesive strength and will accelerate fatigue crack growth. As indicated by the above discussion on the needs for additional knowledge, the work on the effects of oxidation on high temperature fatigue life is far from completed. This study is only one of the initial steps to construct a mechanistic and quantitative model based on the empirical data of grain boundary oxide penetration.
V. SUMMARY AND CONCLUSIONS

Grain boundary oxidation may accelerate fatigue crack growth at elevated temperatures. The grain boundary oxidation kinetics was studied. Grain boundary oxide penetration depth varies widely from one grain boundary to another. The measured grain boundary oxide penetration data agree well with the Weibull distribution. A model of intermittent micro-ruptures of the grain boundary oxide is constructed for the accelerated fatigue crack growth at elevated temperatures. The derived fatigue crack growth rate based on the model agrees well with the observed inverse relation between da/dN for a number of high temperature alloys.
References


Figure 1 Cross-section of oxidized coupon of TAX-8A at 1000°C for 500 hours
Figure 2  Grain boundary angle effect on the penetration of radioactive nickel along nickel bicrystals grain boundaries at 1050°C (37)
Figure 3 Weibull plot of $a_1$ in Equation 2
Figure 4  Frequency effect (a) and temperature effect (b) on fatigue crack growth in IN-100 (R = 0.1) (40,41,42)
Figure 5 Frequency effects on fatigue crack growth rate.
Figure 6  Cyclic loading at two different frequencies
Figure 7 The schematic plot of two rate processes
### Abstract

Fatigue crack growth rate at elevated temperatures can be accelerated by grain boundary oxidation. Grain boundary oxidation kinetics and the statistical distribution of grain boundary oxide penetration depth were studied. At a constant $\Delta K$-level and at a constant test temperature, fatigue crack growth rate, $da/dN$, is a function of cyclic frequency, $v$. A fatigue crack growth model of intermittent micro-ruptures of grain boundary oxide is constructed. The model is consistent with the experimental observations that, in the low frequency region, $da/dN$ is inversely proportional to $v$, and fatigue crack growth is intergranular.