A New Model for Broadband Waveguide to Microstrip Transition Design

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SUMMARY

A new model is presented which permits the prediction of the resonant frequencies created by antipodal finline waveguide to microstrip transitions. The transition is modeled as a tapered transmission line in series with an infinite set of coupled resonant circuits. The resonant circuits are modeled as simple microwave resonant cavities of which the resonant frequencies are easily determined. The model is developed and the resonant frequencies determined for several different transitions. Experimental results are given to confirm the models.

INTRODUCTION

The use of frequencies above 18 GHz for government and commercial communications applications is expected to increase rapidly in the next few years. Low cost systems in this frequency range will utilize solid state devices in the form of monolithic microwave integrated circuits (MMIC's). The current trend in solid state microwave integrated circuits is to use microstrip transmission lines for device interconnections. However, all test equipment in the millimeter wave frequency range utilizes rectangular waveguide. In addition, rectangular waveguide will be used in phased array antennas and other systems in which the signal must travel an appreciable distance in a medium other than free space. Therefore, a low cost, easily fabricated waveguide to microstrip transition which has low loss and broad bandwidth will be essential in the test and implementation of any system utilizing MMIC's.

The antipodal finline waveguide to microstrip transition was first demonstrated by J.H.C. van Heuven (ref. 1). This and the many derivations of it seen in the literature (refs. 2 to 4) (fig. 1) are attractive from the system integration point of view since they are in line with the waveguide and can be easily manufactured on inexpensive, soft substrates using standard printed circuit board techniques. The problem with using the antipodal finline transition has been obtaining broadband response from a simple set of design rules. The design is complicated since the transition creates a set of resonant modes which limit the useful bandwidth of the transition. A typical S21 measurement of a transition demonstrating this phenomenon is shown in figure 2.

The resonances are a major problem in transition design and may even exclude this type of transition from being used under certain circumstances. In a standard configuration, the component under test is inserted between two transitions with a short section of microstrip separating the device from the transition to minimize loss. The resonances of the transition may therefore couple to the device under test if the bandwidth of the device overlaps the
resonant frequencies. This may be observed by placing two different trans-

sitions back to back and measuring the resonance. It will be seen that the 

resonant frequency is between the resonant frequencies of each individual tran-

sition. Therefore, the use of antipodal finline transitions of the type shown 

in figure 1 may be limited for such standard applications as microstrip trans-

mission line resonator studies and filters where the inserted device has a 

resonance of its own. Applying transitions in phased array antenna systems may 

be limited by the associated phase shift at each resonance. In the passband 

portion of the transition, the phase shift is linear, but near a resonance a 

rapid phase shift occurs which is difficult to predict.

Existing design rules (ref. 5) do not address the problem of placement of 

the resonant frequencies. Therefore, trial and error design is still used. 

this paper presents a new model for predicting the resonances which permits 

placement of the resonant frequencies outside the desired band during the 

design process. This will eliminate the need for much of the iterative design 

process and therefore reduce the time and cost involved in implementing wave-

guide to microstrip transitions.

PHYSICAL DESCRIPTION OF THE RESONANCE

The transition shown in figure 1(b) is the easiest to describe and will 

therefore be used to develop a physical description of the resonances. The 

transition has been separated into two regions in order to describe how the 

transition works. Region I is a tapered antipodal finline which concentrates 

and rotates the electric fields of the incident TE_10 waveguide mode 90° 

into the quasi-microstrip mode which propagates in antipodal finlines with 

overlapping fins (fig. 3 sections AA-DD). In addition, region I transforms 

the high impedance of the TE_10 waveguide mode to a lower impedance close 

to the 50 \Omega impedance usually used for microstrip transmission lines. 

Region II makes the transition from antipodal finline to microstrip (fig. 3 

sections EE-HH). The resonances are created in region II as will be shown.

To develop the physical picture of the electromagnetic fields associated 

with the resonances which will be used to derive the model, consider the tran-

sition to look like an \( \mathbf{E} \) plane filter to a propagating TE_10 mode signal 

in rectangular waveguide. If a solid metal sheet is inserted into a waveguide 

in the center of the \( \mathbf{H} \) plane and parallel to the \( \mathbf{E} \) plane of the waveguide, 

the TE_10 waveguide mode is cutoff and evanescent modes are created. Figures 

4(a) and 4(b) show the two lowest-order evanescent modes in the bisected wave-

guide region, labeled the TE_{10}^{e} and TE_{20}^{e} modes (ref. 6). Inductive energy 

is stored in the evanescent modes. If a slot is placed in the bisecting metal 

sheet, electric fields will be created in the slot parallel to the \( \mathbf{E} \) plane 

of the waveguide. When the capacitive energy created by the slot equals the 

inductive energy stored in the evanescent modes, a resonance will occur. 

Figure 4(c) shows the electric and magnetic fields which are created when a 

slot is added to the bisecting metal sheet. The waveguide to finline inter-

face and the finline discontinuities create a similar set of evanescent modes. 

The inductive energy stored in the evanescent modes is one component of the 

loss in propagating power associated with the transitions. Region II appears 

to the evanescent modes as a slot in a bisecting metal sheet and a source of
capacitive energy. Therefore, region II is the source of the resonances which plaque the transition.

MODEL DEVELOPMENT

Analytical methods to obtain the resonant frequencies using the above description would be difficult to implement for a complicated structure such as the transition. Therefore, a model based on the electromagnetic field diagrams derived in figure 4 and experimentally derived parameters is developed. In the tapered antipodal finline region, a quasi TE_{10} mode propagates. In region II and the microstrip, a quasi TEM mode propagates. The evanescent modes decay rapidly and therefore do not propagate. Therefore, the quasi TEM and the TE_{10} modes must propagate independently of the evanescent modes for all frequencies except those near the resonant frequency, \( f_r \), of region II. Near \( f_r \), the propagating wave couples energy to the resonator in the same manner as any transmission line would couple energy to a reactive resonant cavity placed within the electromagnetic fields of the propagating wave. Therefore, if the resonant frequency could be modeled by a cavity resonator of a form related to the shape of region II, an equivalent circuit model could be used such as in figure 5. Each RLC circuit represents a mode of an equivalent resonant cavity. Assuming the Q of each resonator is large and the resonant modes are not close together, then each resonant mode can be considered to be decoupled and placement of the resonant frequencies may be made by a simple alteration to region II.

The choice of the resonant cavity to model region II must be dependant on the electric and magnetic fields of region II. The primary mode in region II is a LSE mode. The electric fields are concentrated in the slot, or region II, in the E plane of the waveguide. Outside of the center of the H plane, the electric fields decay to zero at the waveguide walls, \( X = \pm b/2 \) of figure 4(d). The magnetic field lines must encircle the electric field lines and are constrained by the waveguide walls and the metal sheet which forms region II.

The shape of region II and the LSE mode fields in the region suggest a cylindrical waveguide cavity with a bisecting metal sheet in the E plane. Resonant modes of the form TE_{n11}, \( n \geq 1 \), have fields which are similar to those of region II. In addition, unlike an elliptical waveguide resonant cavity which would more closely describe region II, the resonant frequencies of cylindrical cavities are easily obtained. Therefore, a cylindrical cavity filled with a material of some \( \varepsilon_{\text{eff}} \) having a radius of \( \chi/2 \) and a length \( b \) is proposed to model region II (see fig. 6(a)).

The resonant frequencies are dependent on the available cavity volume so an effective permittivity is introduced to make the resonant frequency of the cylindrical cavity coincide with the experimental values. The proposed model is simple and its usefulness is dependant on whether or not a single value of \( \varepsilon_{\text{eff}} \) can be found such that various resonant frequencies can be accurately predicted. It will be shown that this is the case for many transitions that have been studied experimentally. It was found that \( \varepsilon_{\text{eff}} \) is dependant on the length parameter \( \chi \) but was essentially independent of frequency. Thus, for a given transition, the various resonant frequencies can be predicted accurately from the model.
The resonant frequencies are derived by setting the propagation constant for cylindrical waveguide equal to \( \pi/b \) where \( b \) is the length of the waveguide cavity. The resulting equation for the resonant frequencies is:

\[
f_{nll} = \frac{C}{2\pi \sqrt{\varepsilon_{\text{eff}}}} \left[ \left( \frac{p_{nll}}{x/2} \right)^2 + \left( \frac{\pi}{b} \right)^2 \right]^{1/2}
\]

where

\( x/2 \) is the radius of the cylinder

\( p_{nll} \) are roots of the equation \( \frac{dJ_{n}(kr)}{dr} = 0 \),

\( r = x/2 \), and \( Kc \) = cut off wave number of the waveguide

\( \varepsilon_{\text{eff}} \) is some frequency dependant effective dielectric constant (ref. 7). The solution for \( \varepsilon_{\text{eff}} \) would permit the determination of the resonant frequency. Unfortunately, a theoretical determination of \( \varepsilon_{\text{eff}} \) is difficult. Therefore, an experimentally derived \( \varepsilon_{\text{eff}} \) will be found.

**EXPERIMENTAL RESULTS**

Transitions were fabricated for various lengths of region II, \( x \). In general, the total length of the transition, \( L = \) length of region I plus \( x \), was kept constant. The transition length, \( L \), was equal to \( \lambda g \) (\( f = 32 \) GHz) of the TE_{10} rectangular waveguide mode for Ka band transitions. The transitions were fabricated on 10 mil, \( \varepsilon_{f} = 2.22 \) Duroid and 10 mil, \( \varepsilon_{f} = 2.17 \) Cu Clad substrates. All testing was done for two back-to-back transitions interconnected by 3.80 cm of 50 \( \Omega \) microstrip. The transitions were mounted for testing in a test fixture shown in figure 7 which when clamped together supplied sufficient contact between the metal finlines and the waveguide walls. Measurements were taken on a modified Hewlett Packard 8409 automatic network analyzer.

The measured resonant frequencies, \( f_r \), are plotted versus \( x \) for two different shaped region II in figure 8. In addition, transitions were made with straight finline tapers and/or triangular shaped region II. It was found that the finline taper made only small differences in the resonant frequency. Also, as can be seen in figure 8, the exact curvature of region II did not significantly alter the resonant frequency. The dominating determination of \( f_r \) is the length \( x \). This permits the developed curves to be used for a broad range of antipodal finlines without an exact knowledge of the curvature of region II. Using equation (1) and the results from figure 8 values of \( \varepsilon_{\text{eff}} \) as a function of \( x \) and frequency were obtained and are plotted in figure 9.

**MODEL DERIVATION FOR OTHER TRANSITIONS**

The curves drawn in figure 8 may be obtained using only a few well placed data points. This allows a quick determination of the resonant frequency for a region II of any length, \( x \). This approach was followed for a determination of the resonant frequency for K band transitions (fig. 10). All dimensions were directly scaled from Ka band transitions.
The van Heuven transition may be described by the equivalent circuit model in figure 5. A major complication though is that the RLC circuits must describe two resonant cavities and all of their resonant modes. In addition, the resonant modes of the two cavities are now closely coupled. Therefore the positioning of the resonant frequencies by an independent change of either $x_1$, or $x_2$ becomes impossible without an accurate model of the coupling coefficients. Empirically derived curves such as those in figures 8 and 10 may be developed. When this was done, it was noticed that the bandwidth of the transition was less than that for the transition in figures 1(b) and (c).

Transitions with a semicircular metal fin added to region II on the microstrip side of the transition (fig. 1(c)) may be modeled as a slot line resonator. The electric and magnetic fields are shown in figure 6(b). An advantage of this type of transition is the accuracy to which the resonant frequencies may be predicted. The guide wavelength of a straight slot line may be accurately determined by such methods as the spectral domain method (ref. 8) and Cohn's method (ref. 9). It has been shown by Kawano (ref. 10) that the curvature of a slot line does not alter the resonant frequencies of a slot line resonator. Simons (ref. 11) has shown that the placement of a slot line in rectangular waveguide has negligible effect on $\lambda g/\lambda_0$. Therefore, the resonant frequencies may be modeled by a straight slot line resonator of length and width equal to those of the slot in region II located in the center of a rectangular waveguide. The guide wavelength of slots fabricated on $\epsilon_r = 2.22$, 10 mil substrates has been determined by Simons (ref. 11) using Cohn's technique for various slot widths and frequencies in Ka band $TE_{10}$ mode rectangular waveguide. This data was used to determine the resonant frequencies (slot length $L = n\lambda g/2$). The resonant frequencies are plotted in figure 11. Transitions were made with slot widths of 0.0254 cm and tested. There was good agreement to the predicted values. Kawano (ref. 10) has shown that the resonant frequency increases as the slot width increases. Therefore, there are two parameters which may be varied to change $f_r$.

CONCLUSIONS

A physical description of the resonant frequency modes of antipodal fin-line waveguide to microstrip transitions has been presented. A new model has been developed which permits the prediction of the resonant frequencies. Measurements have been performed to verify the models. The models are scalable to other frequency bands. The model for the transition shown in figure 1(c) is especially attractive since theoretical values for all the necessary parameters are available in the literature. The use of these models should reduce the time and cost involved in designing waveguide to microstrip transitions of a desired characteristic.

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REFERENCES


Figure 1. Types of antipodal finline waveguide to microstrip transitions.
Figure 2: $S_{21}$ measurements of antipodal finline waveguide to microstrip transition.
FIGURE 3.- ELECTRIC FIELDS AT VARIOUS CROSS SECTIONS ALONG THE TRANSITION FROM CONVENTIONAL RECTANGULAR WAVEGUIDE TO A 50 Ω MICROSTRIP AS SHOWN IN FIGURE 1B.
Figure 4. - $E$ and $H$ fields of region II. (Ref 6).
Figure 4. Concluded.

Figure 5. An equivalent lumped element model for a waveguide to microstrip transition.
(A) $\text{TE}_{111}$ mode of an equivalent cylindrical waveguide cavity, homogeneously filled with some material of $\varepsilon_{\text{eff}}$.

(B) First order, resonant mode of an equivalent slot resonator.

Figure 6. Equivalent resonant cavities for transitions shown in Figures 1B and 1C.
Fig. 7. - 26.5 - 40 GHz waveguide to microstrip transition in test fixture.

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FIGURE 8.- RESONANT FREQUENCY AS A FUNCTION OF $x$ FOR KA BAND TRANSITIONS.
**Figure 9.** $\varepsilon_{\text{eff}}$ versus $X$ for Ka band transitions.

**Figure 10.** Resonant frequency versus $X$ for K band transitions.
Figure 11. - Resonant frequency versus slot length $L$. 

Legend:
- $a = 0.3556$ cm
- $b = 0.7112$ cm
- $f = 2.22$
- $d = 0.0254$ cm
- $w = 0.0754$ cm

Graph shows resonant frequency in GHz versus length of slot $L$ in cm with marked points at $\frac{\lambda}{2}$, $\lambda$, and $\frac{3\lambda}{2}$.
A new model is presented which permits the prediction of the resonant frequencies created by antipodal finline waveguide to microstrip transitions. The transition is modeled as a tapered transmission line in series with an infinite set of coupled resonant circuits. The resonant circuits are modeled as simple microwave resonant cavities of which the resonant frequencies are easily determined. The model is developed and the resonant frequencies determined for several different transitions. Experimental results are given to confirm the models.