Agreement Between Experimental and Theoretical Effects of Nitrogen Gas Flowrate on Liquid Jet Atomization

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AGREEMENT BETWEEN EXPERIMENTAL AND THEORETICAL EFFECTS OF NITROGEN GAS FLOW RATE ON LIQUID JET ATOMIZATION

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Abstract

Two-phase flows were investigated by using high velocity nitrogen gas streams to atomize small-diameter liquid jets. Tests were conducted primarily in the acceleration-wave regime for liquid jet atomization, where it was found that the loss of droplets due to vaporization had a marked effect on drop size measurements. In addition, four identically designed two-fluid atomizers were fabricated and tested for similarity of spray profiles. A scattered-light scanner, developed at NASA Lewis Research Center, was used to measure a characteristic drop diameter, \( D_c \), which was correlated with nitrogen gas flow rate, \( W_n \), in the expression

\[ D_c = k W_n^z \]

where \( D_c \) and \( W_n \) are given in centimeters and grams per second, respectively. The exponent of 3.15 for \( W_n \) may be expressed as volume median, Sauter mean, or volume-linear mean, \( D_{31} \), drop diameter. At a distance of 2.2 cm downstream from the atomizer and a water flow rate of 3.15 g/sec, the following expressions were obtained:

\[ D_{5} = 240 W_n^{1.33} \]

\[ D_{31} = 320 W_n^{1.33} \]

\[ D_{32} = 400 W_n^{1.33} \]

where \( D_c \) and \( W_n \) are given in centimeters and grams per second, respectively. The exponent of 1.33 for nitrogen gas flow rate is identical to that predicted by atomization theory for liquid jet breakup in the acceleration-wave regime. This is higher than the value of 1.2 which was previously obtained at a sampling distance of 4.4 cm downstream of the atomizer. The difference is attributed to the fact that drop-size measurements obtained at a 2.2 cm sampling distance are less affected by vaporization and dispersion of small droplets and therefore should give better agreement with atomization theory.

Profiles of characteristic drop diameters were also obtained by making at least five line-of-sight measurements across the spray at several horizontal positions above and below the center line of the spray. Comparisons of spray symmetry of \( D_{5} \) profiles were made for the four identical atomizers and values of \( D_{5} \) obtained near the spray center line were found to be considerably higher than the overall values of \( D_{5} \) obtained for the entire spray.

Introduction

In an experimental investigation of two-phase interacting-flows, characteristic drop diameters and spray profile data were obtained for small liquid jets atomized with high velocity nitrogen gas streams. A recently improved scattered-light scanner, developed at the NASA Lewis Research Center, was used to obtain the drop size data. The instrument was primarily designed to study small-droplet sprays with Sauter mean diameters in the order of 10 \( \mu \)m. Such sprays are useful in simulating clouds for icing research and combustion studies of rapidly vaporizing fuel sprays. At present, very little data are available on small-droplet sprays due to difficulties involved in producing and measuring characteristic drop sizes in the order of 10 \( \mu \)m.

When a liquid jet is injected into an airstream, both atomization and vaporization can occur simultaneously. In order to determine the initial drop size of a spray from data obtained downstream of an atomizer, the effect of vaporization on the drop size must be known. In Ref. 1, the effect of mass velocity of the nitrogen gas flow, \( \rho_n W_n \), on the volume median drop diameter, \( D_{5} \), was determined and it was found that \( D_{5} = (\rho_n W_n)^{-0.8} \) at a sampling distance of 25 cm downstream of the atomizer. In a later study, values of \( D_{5} \) were determined at 4.4 cm downstream of the atomizer and it was found that \( D_{5} = (\rho_n W_n)^{-1.2} \). The decreases in the exponent from -1.2 to -0.8, when sampling distance is increased from 4.4 to 25 cm, was attributed to the effect of vaporization on the drop size measurements.

From the study reported in Ref. 2, it was found that drop size data should be taken as close to the atomizer as possible in order to minimize vaporization effects. As a result, the present study was undertaken primarily to obtain drop size data even closer to the atomizer orifice. The exponent for \( \rho_n W_n \) would continue to increase as axial sampling distance decreased. If a sample were taken too close to the atomizer, however, the exponent for \( \rho_n W_n \) could also decrease due to incomplete formation of the liquid into droplets.

To investigate the effect of aerodynamic forces on characteristic drop sizes of atomized liquid jets, the scattered-light scanner originally described\(^\text{a}\) was modified for use in the present study. It was modified not only to measure the overall drop size characteristics of the spray but also to obtain several line-of-sight drop size profiles at various sampling locations downstream of the atomizer. For this measurement, the laser beam size was decreased and by adjusting the atomizer up and down from the center line, at least five line-of-sight measurements were obtained across the spray cross section. The instrument was also used to obtain exponents for the Rosin-Rammler and Nukiyama-Tanasawa drop size distribution expressions.

In the present study, values of the volume-linear mean drop diameter, \( D_{31} \), were measured with the scattered-light scanner as well as exponents for the two drop size distribution expressions mentioned above. All of the sprays were formed in a low velocity, 5 m/sec, airflow to aid in transporting small drops through the laser beam. Liquid and gas pressures for the atomizers were varied over a range of 0.2 to 1.0 MPA and the resulting sprays were sampled at distances of 2.2, 4.4, and 6.7 cm downstream of the atomizer orifice.

Nomenclature

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td>( D_{5} )</td>
<td>Drop size parameter in Nukiyama-Tanasawa expression, cm</td>
</tr>
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</table>

\(^a\) originally described
With a control valve, an airstream velocity of 0.24 m inside diameter test section which auxiliary equipment are shown in Fig. 1. Fluid atomizer with assist nitrogen gas flow was applied at ambient temperature, 293 K, measured with a 0.51 cm diameter sharp edge orifice. After air, nitrogen, and water flowrates were set, volume median and other characteristic drop diameters and exponents for drop size distribution expressions were determined using the scattered-light scanner. The optical system is shown in Fig. 2. It consisted of a 1-mW helium-neon laser, a 0.003-cm-diameter aperture, a 7.5-cm-diameter collimating lens, a 10-cm-diameter converging lens, a 5-cm-diameter collecting lens, a scanning disk with a 0.05-cm slit, a timing light, and a photomultiplier detector.

The spatial resolution of the scattered-light scanner is 2.86 cm and corresponds to the laser beam diameter. A sufficient volume of each spray was sampled to minimize spray pattern effects when measuring mean drop diameters for the entire spray. Effects of the drop size distribution function on scattered-light scanner measurements is discussed in detail. It was found that the irradiance distribution is only weakly related to the particle diameter distribution function, and therefore, irradiance distribution was used to determine characteristic drop diameters and changes in the drop size distribution function were assumed to have a negligible effect on drop size measurements. Reproducibility tests gave experimental measurements of drop size that agreed within ±5 percent. Five sets of monosized polystyrene spheres having diameters of 8, 12, 25, 50, and 100 μm, were used to calibrate the scattered-light scanner. A more complete description of the scattered-light scanner, the mean drop diameter range, and the method of determining mean or median particle diameter can be found in Refs. 3 and 4.

Tests were made with four pneumatic two-fluid atomizers fabricated from the same design and the volume median, Dv,5, the Sauter mean, D32, and the volume-linear mean, D31 drop diameters were measured with the scattered-light scanner. The entire cloud of droplets was sampled at three axial locations downstream of the atomizers. Also, line-of-sight profiles of characteristic drop diameters were obtained to determine the spatial dispersion of the spray as a function of the nitrogen gas flowrate, water flowrate, and the spray sampling distance downstream of the atomizer. Drop-size distribution exponents for both the Rosin-Rammler and the Nukiyama-Tanasawa expressions were also determined with the scattered-light scanner.

Experimental Results

The four atomizers were initially tested at an axial downstream distance of 4.4 cm. The effect of axial sampling distance on characteristic drop size was then investigated and a comparison was made of three characteristic drop size expressions. Finally, line-of-sight profiles of the characteristic drop diameter, Dv,5, were obtained for each of the four atomizers. Characteristic exponents

\[
D_{v,5} \text{ volume median drop diameter, cm}
\]

\[
D_{32} \text{ Sauter mean drop diameter, } \left( \sum_i nD_i^2 / \sum_i nD_i \right)^{0.5} \text{ cm}
\]

\[
D_{31} \text{ volume-linear mean drop diameter, } \left( \sum_i nD_i / \sum_i nD_i^3 \right)^{0.5} \text{ cm}
\]

\[
k \text{ correlation coefficient, sec/g-cm}
\]

\[
N_n \text{ exponent for Nukiyama-Tanasawa drop size distribution expression}
\]

\[
N_v \text{ exponent for Rosin-Rammler drop size distribution expression}
\]

\[
n \text{ number of droplets}
\]

\[
v \text{ volume fraction of droplets having diameter x cm}
\]

\[
w \text{ weight flow of fluid, lb/sec or g/sec}
\]

\[
x \text{ droplet diameter in drop size distribution expressions, cm}
\]

\[
\bar{x} \text{ axial downstream spray sampling distance, cm}
\]

Subscripts

\[
n \text{ nitrogen gas}
\]

\[
w \text{ water}
\]
Volume median drop diameters produced by the four atomizers S-4, S-14, S-53, and S-94 were measured with the scattered-light scanner. All four atomizers were constructed from the design shown in Fig. 3. In Fig. 4(a) to (d), the reciprocal of the volume median drop diameter $D_{v,5}$ is plotted versus nitrogen gas flowrate. Water flowrate was varied from 3.15 to 9.46 g/sec and the drop size data were obtained at a distance of 4.4 cm downstream of the atomizer. From these plots, the following general expression was derived for the four atomizers: $D_{v,5}^{-1} \propto W_n^{-1.2}$. In order to compare their atomizing performance, the following expressions were derived for atomizers S-4, S-14, S-53, and S-94, respectively: $D_{v,5}^{-1} = 310 W_n^{-1.2}$, $D_{v,5}^{-1} = 293 W_n^{-1.2}$, $D_{v,5}^{-1} = 277 W_n^{-1.2}$, and $D_{v,5}^{-1} = 300 W_n^{-1.2}$.

Where the correlation coefficient, $k$, was evaluated at a constant water flowrate of 3.15 g/sec, and $D_{c}^{-1}$ is given in cm$^{-1}$. The highest and lowest values of $k$ differ by approximately 10 percent. This variation between atomizers is somewhat greater than desired in the design of an array of atomizers for application in a combustor or an icing wind tunnel and was attributed to variations in physical dimensions of the atomizers such as tubing size and the 0.32 cm diameter orifice.

**Effect of Axial Sampling Distance on Characteristic Drop Size**

The entire spray was sampled at axial distances of $x = 2.2, 4.4,$ and 6.7 cm where $X$ is the distance from the atomizer orifice to the center line of the laser beam as measured along the spray center line. Water flowrate was held approximately constant at 3.15 g/sec and characteristic drop diameters, $D_v$ and $D_{32}$, were measured and plotted against nitrogen gas flowrate, $W_n$, as shown in Figs. 6(a) and (b). All of the atomizers were used for this series of tests, and the data plotted in Fig. 6(a) show that:

$D_{v}^{-1} = 240 W_n^{-1.33}$

$D_{32}^{-1} = 320 W_n^{-1.33}$

$D_{31}^{-1} = 400 W_n^{-1.33}$

The correlation coefficient, $k$, and nitrogen gas flowrate exponent, $a$, are given in Table 2 for comparison. It is interesting to note that at any of the three sampling distances, the value of $k$ varied by only about 6 percent whereas the exponent $a$ changed from 1.33 to 1.0 when $X$ was increased from 2.2 to 6.7 cm. These results indicate that vaporization and dispersion of the small drops had only a minor effect on the correlation coefficient $k$ but a major effect on the exponent $a$.

**Profiles of Characteristic Drop Diameter, $D_v$**

The beam height of the scattered-light scanner was reduced from 4.4 to 0.64 cm and line-of-sight measurements of the characteristic drop diameter were obtained at several horizontal locations in each spray. Measurements were obtained for the four atomizers S-4, S-14, S-53, and S-94 and values of $D_v$ are plotted against horizontal location as shown in Fig. 7. The spray profile data were obtained for the four atomizers at constant water and nitrogen gas flowrates and an axial downstream sampling distance of $X = 4.4$ cm.

Peak values of $D_v$ at the liquid jet center line were reduced nearly 50 percent, from approximately 60 to 30 $\mu$m, when the nitrogen gas flowrate was increased from 1.59 to 2.59 g/sec. A similar reduction in $D_v$ occurred near the upper and lower fringes of the sprays. The asymmetry of the spray profiles was attributed to the effect of gravity on the drops and also to slight misalignments of the center tubes of the various atomizers. Values of $D_v$ show relatively good uniformity of drop size for the four atomizers. Differences in values of $D_v$ for the four atomizers were in the order of 10 to 20 percent.
Characteristic Exponents for Drop-Size Distribution Expressions

The scattered-light scanner gave data for the exponent $N_r$, which appears in the Rosin-Rammler expression as follows:

$$\frac{dv}{dx} = \frac{N_r}{N_r} \frac{N_r - 1}{c} e^{-(x/c)^{N_r}}$$

Data were also obtained for the exponent $N_n$, which appears in the Nukiyama-Tanasawa expression as follows:

$$\frac{dv}{dx} = \frac{6/N_n}{(6/N_n)} x^5 e^{-bx^n}$$

From a plot of the data obtained with the four atomizers, as shown in Fig. 8 the following relation was determined:

$$N_r = 2.8N_n^{0.45}$$

which is the same as that derived in Ref. 1. Thus it was found that although the downstream distance, $x$, varied from 2.2 to 6.7 cm, the relation between the exponents was not appreciably affected by vaporization and dispersion of the small droplets.

Concluding Remarks

When characteristic drop diameters of water sprays were measured with the scattered-light scanner at a distance of 2.2 cm downstream of the orifice of a pneumatic two-fluid atomizer, values of $D_{v, 5}^{-1}$, $D_{32}^{-1}$, and $D_{31}^{-1}$ were obtained that could be correlated with nitrogen gas flowrate raised to the 1.33 power. This exponent of 1.33 is the same as that derived theoretically in Ref. 5 for liquid jet atomization in the acceleration-wave breakup regime. The fact that experimental results agreed with atomization theory was attributed to a negligible loss of small droplets due to vaporization and dispersion. These effects were not negligible at a distance of 6.7 cm downstream of the atomizer orifice, where the exponent decreased to a value of 1.0. When the laser beam was positioned at a distance of less than 2.2 cm from the atomizer characteristic drop diameters increased markedly due to incomplete breakup of the liquid jet. With atomizer S-94, at a water flowrate of 3.15 g/sec and a sampling distance of 2.2 cm, the following expressions for characteristic drop diameter of the initial spray were obtained:

$$D_{v, 5}^{-1} = 240 W_n^{1.33}$$

$$D_{32}^{-1} = 320 W_n^{1.33}$$

$$D_{31}^{-1} = 400 W_n^{1.33}$$

which agree well with atomization theory.

Profiles of characteristic drop diameters were also determined from line-of-sight measurements made with the scattered-light scanner. Such data are useful in comparing the performance of similar atomizers by providing information concerning the spatial distribution of drop size characteristics within the spray cross section. Reproducibility of the spray data were within ±5 percent. Also, it was found that experimental values of the exponents $N_n$ and $N_r$, for the drop-size distribution expressions, were not appreciably affected when the sampling distance, $x$, was varied from 2.2 to 6.7 cm downstream of the atomizer orifice.

References

FIGURE 1. - APPARATUS AND AUXILIARY EQUIPMENT.

FIGURE 2. - ATMOSPHERIC PRESSURE TEST SECTION AND OPTICAL PATH OF SCATTERED-LIGHT SCANNER.
FIGURE 3. - DIAGRAM OF PNEUMATIC TWO-FLUID ATOMIZER.

FIGURE 4. - CORRELATION OF VOLUME MEDIAN DIAMETER $D_{v,5}$ WITH NITROGEN GAS FLOWRATE, $W_{N}$, AT $x = 4.4$ CM.
Figure 5. - Effect of spray sampling distance $x$ on characteristic drop diameters $D_{v,5}$ and $D_{32}$ with $W_W = 3.15$ g/sec.

(a) Variation of volume median, $D_{v,5}$ with $W_n$, atmizer S-53.

(b) Variation of sauter mean diameter, $D_{32}$ with $W_n$, atmizer S-94.

Figure 6. - Comparison of characteristic drop diameters with atmizer S-94 and water flowrate of 3.15 g/sec.

(a) At sampling distances, $x$, of 2.2 cm.

(b) At sampling distance, $x$, of 4.4 cm.

(c) At sampling distance, $x$, of 6.7 cm.
FIGURE 7. - SPRAY-PROFILE ENVELOPES FOR ATOMIZERS AT $W_0 = 6.36$ g/sec AND $X = 4.4$ cm.

FIGURE 8. - CORRELATION OF ROSIN-RAMMLER AND NUKIYAMA-TANASAWA EXPONENTS $N_r$ AND $N_{\theta}$, RESPECTIVELY.
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