Performance Characteristics of a Combination Solar Photovoltaic Heat Engine Energy Converter

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Abstract
A combination solar photovoltaic heat engine energy converter is proposed. Such a system is suitable for either terrestrial or space power applications. The combination system has a higher efficiency than either the photovoltaic array or the heat engine alone can attain. Advantages in concentrator and radiator area and receiver mass of the photovoltaic heat engine system over a heat-engine-only system are estimated. A mass and area comparison between the proposed Space Station organic Rankine power system and a combination PV-heat engine system is made. The critical problem for the proposed converter is the necessity for high-temperature photovoltaic array operation. Estimates of the required photovoltaic temperature are presented.

Nomenclature
\begin{align*}
A_c & \text{ concentrator collection area, m}^2 \\
A_h & \text{ effective heat transfer area of PV array, m}^2 \\
A_{PV} & \text{ active photovoltaic area, m}^2 \\
A_{RAD} & \text{ radiator area, m}^2 \\
A_{REC} & \text{ aperture area of receiver, m}^2 \\
A_s & \text{ structural area in PV array, m}^2 \\
A_T & \text{ total area of PV array, } A_{PV} + A_s, m^2 \\
a & \text{ ratio of } A_h \text{ to } A_T \\
B & \text{ electrical storage specific mass, kg/kW} \\
C & \text{ concentrator specific area, m}^2/kW \\
C_P & \text{ specific heat of working fluid at PV array, J/kg K} \\
f_{PV} & \text{ fraction of active area in PV array, } A_{PV}/A_T \\
h & \text{ heat transfer coefficient between PV array and working fluid, W/m}^2K \\
K & \text{ heat transfer parameter for PV array (Eq. (20)), K} \\
M & \text{ mass, kg} \\
m & \text{ specific mass, kg/kW} \\
P & \text{ power, W} \\
P_{SUN} & \text{ solar flux (1.35 kW/m}^2 \text{ at earth orbit), kW/m}^2 \\
R & \text{ receiver specific mass, kg/kW} \\
r & \text{ radiator specific mass, kg/kW} \\
T & \text{ temperature, K} \\
\Delta T & \text{ temperature rise between working fluid and PV array, } T_{PV} - T_B \\
t_{SH} & \text{ time system is in shade} \\
t_{SUN} & \text{ time system is in sunlight} \\
u & \text{ heat transfer parameter for PV array (Eq. (C-7)), 1/K} \\
\alpha & \text{ absorptivity of PV array} \\
\gamma_{BAT} & \text{ specific energy density of electrical energy storage system, kWh/kg} \\
\beta_{REC} & \text{ specific mass of receiver, kg/kW} \\
\gamma_{BAT} & \text{ parameter that compares electrical energy storage efficiency to thermal energy storage efficiency (Eq. (5))} \\
\gamma_{BAT} & \text{ parameter that determines effectiveness of electrical energy storage (Eq. (15))} \\
c & \text{ emissivity} \\
\eta & \text{ efficiency} \\
\mu & \text{ time parameter (Eq. (6))} \\
\rho & \text{ reflectivity of PV array} \\
\sigma & \text{ Stefan-Boltzmann constant, 5.67x10}^{-8} \text{ W/m}^2\text{K}^4 \\
\tau & \text{ transmittance of PV array} \\
\nu & \text{ time parameter} \\
\gamma_{BAT} & \text{ electrical energy storage system} \\
\gamma_{BAT} & \text{ concentrator} \\
\gamma_{BAT} & \text{ electrical power output} \\
\gamma_{BAT} & \text{ heat engine} \\
\gamma_{BAT} & \text{ input power} \\
\gamma_{BAT} & \text{ PV array} \\
\gamma_{BAT} & \text{ receiver} \\
\gamma_{BAT} & \text{ heat leaving PV array to working fluid of system} \\
\gamma_{BAT} & \text{ stored energy or power} \\
\gamma_{BAT} & \text{ PVHE system} \\
\gamma_{BAT} & \text{ heat-engine-only system}
\end{align*}
The proposed energy converter combines a PV array and a heat engine to produce a higher combined power system efficiency than either a PV array or heat engine alone can attain. Improved efficiency is achieved by splitting the solar spectrum. Part is converted by the PV array and the remaining part converted to heat for use in a heat engine. Photocells consist systems that split the solar spectrum in order to obtain better performance have been considered.\(^1\)\(^2\)\(^3\)\(^4\) Multiple cells with different energy bandgaps are used in these systems. Each cell is designed to have maximum response to a different portion of the solar spectrum. Two approaches have been considered. The first approach attempts to construct a multiplet-bandgap cell as a single structure. The other approach uses separate PV cells and splits the solar spectrum with beam splitters,\(^2\) prisms,\(^3\)\(^4\) or diffraction gratings.\(^4\) Early studies\(^3\)\(^4\) using prisms or diffraction gratings showed no improvements in performance when all the optical losses were considered. However, a recent study using highly efficient beam splitters\(^2\) predicts an efficiency greater than 30 percent for a three cell system.

For the proposed PV-heat engine (PVHE) converter to be successful, the PV array must absorb photons in the energy range that can be efficiently converted to electrical energy. Photons outside this energy range must be either transmitted or reflected to a receiver which converts the photon energy to thermal energy. The thermal energy is then converted to electrical energy by a heat engine.

Improved efficiency means that a smaller, less massive energy converter can be constructed. As a result, the PVHE converter is applicable to both terrestrial and space applications. Besides the efficiency, size and mass improvements, the PVHE converter offers another important advantage. Since the PVHE converter consists of two independent energy converters there is system redundancy. Should one of these energy converters fail the other converter is available to produce a portion of the electrical power requirement. This system redundancy is inherent in the PVHE system.

### Description of Solar PV Heat Engine (PVHE) Systems

There are two possible configurations for the PVHE converter. Both of these configurations are shown in Fig. 1. In the transmitting system (Fig. 1(b)), the PV array absorbs the portion of the spectrum that can be efficiently converted to electrical energy, \(P_{\text{EL}}\), and transmits the remaining spectrum to the receiver. In the reflecting system (Fig. 1(a)) the PV array reflects the unused portion of the spectrum to the receiver. The photon flux incident on the receiver is converted to thermal energy. This energy together with the thermal waste energy of the PV array, \(P_{\text{W}}\), is then used by the heat engine to produce electrical energy, \(P_{\text{EL}}\). The waste heat, \(P_{\text{RAD}}\), must then be rejected. For a space system the waste heat must be rejected as thermal radiation.

For a space system in Earth orbit storage of energy is necessary during the portion of the orbit that is in sunlight. This energy is then used during the shade portion of the orbit. In Fig. 1 both electrical and thermal energy storage are indicated. For electrical energy storage a portion, \(P_{\text{EL}}/n_{\text{EL}}\), of the total PV array power output, \(P_{\text{EL}}\), is stored and the remaining portion, \(P_{\text{EL}}\), is supplied to the load. A portion, \(P_{\text{W}}/n_{\text{W}}\), of the thermal power output of the receiver during the sun portion of the orbit is stored for use by the heat engine during the shade portion of the orbit.

The efficiency relations for the two systems in Fig. 1 have similar forms. Therefore, efficiency, mass, and area improvements compared to a heat engine only converter will be similar for each system. Different design advantages and disadvantages exist between the systems, however. For the transmitting system there are no difficult optical design problems for the PV array. Whereas the reflecting system requires an accurate optical surface on the PV array in order to direct the input light flux to the receiver. It may also be possible to design the PV array in the transmitting system as a lens to focus the input light on the receiver aperture. Thus radiation emission losses of the receiver would be reduced.

The principal design difficulty for the PV array of the transmitting system is providing for the removal of the waste heat. If cooling coils are used within the array then the light intercepted by the coils cannot be utilized by the PV array. It would be desirable to locate the cooling coils on the outer edge of the PV array to eliminate the light blocks problem. The reflecting system does not have this problem. The backside of the PV array can be covered with cooling coils without causing any performance loss.

Since the reflecting system is a Cassegrainian design it has structural advantages over the transmitting system. With the concentrator and receiver located next to each other pointing of the system is simpler than for the transmitting system.

Although there are design advantages and disadvantages for both systems the major problem for either system is the necessity for the PV array to operate at high temperature. In order to make the PVHE concept feasible a high temperature PV cell must be developed. In a later section the temperature requirements for the PV array will be discussed.

Three different configurations of the PVHE converter are of interest. First of all, a system without energy storage, second a system with all thermal energy storage, and finally a system with both electrical and thermal energy storage. As shown in Ref. 5, the all thermal energy storage system has higher efficiency than the combination electrical and thermal energy storage system. However, it also requires that the heat engine operate at two power levels. It must produce electrical power, \(P_{\text{EL}}\), during sun time and electrical power, \(P_{\text{W}} + P_{\text{EL}}\), during shade time. This is an added complication that the system that uses both
electrical and thermal energy storage does not have. In that case the heat engine operates at the same power level, $P_{EL}$, all the time. In this study only the combination electrical and thermal energy storage PVHE system will be considered.

**Performance Analysis**

In order to determine the performance of the PVHE systems a model for the optical properties of the PV array is required. It is assumed that the PV array is made up of active PV cells separated by structural material. One of the purposes of the structural materials is to provide cooling of the PV cells. It is assumed that the PV cells and the structural material can be characterized by uniform total optical properties (transmittance, $T$, absorptivity, $\alpha$, and reflectivity, $\rho$). Then if the PV array is illuminated by a uniform flux, the optical properties of the array are just averages of the PV cell and structural material optical properties. Also, the electrical power output, $P_{EL}$, of the PV array is given in terms of the power from the concentrator reaching the PV array, $P_C$, the PV efficiency, $n_{PV}$, and the fraction of active PV area, $fp_A$.

$$P_{EL} = fp_A n_{PV} P_C$$  \hspace{1cm} (1)

Also, for conservation of energy, the following relation holds for the PV array.

$$\alpha + \rho + \tau + fp_A n_{PV} = 1$$  \hspace{1cm} (2)

Using the described optical properties and electrical efficiency the performance of the PV array can be calculated.

**Efficiency.** Of primary importance for an energy converter is the overall efficiency, $n_T$. This efficiency is defined as follows.

$$n_T = \frac{(t_{SH} + t_{SUN})(P_{EL} + P_C)}{t_{SUN} P_C}$$  \hspace{1cm} (3)

The numerator of Eq. (3) is the total electrical energy produced and the denominator is the total input energy. Where $t_{SUN}$ is the time the system is in the sun and $t_{SH}$ is the time the system is in the shade. For a system in earth orbit, $t_{SH} + t_{SUN}$ is the orbit period. In Ref. 5 the derivation of $n_T$ for the various PVHE systems is presented. The form of the expression for $n_T$ is the same for both the transmitting and reflecting systems. For a transmitting system that uses both electrical and thermal energy storage the overall efficiency is the following

$$n_T = n_{REC} \left[ fp_A n_{PV} \left( n_{BAT} - n_{HE} \right) + n_{HE} \left( 1 - (1 - n_{REC}) - \rho \right) \right]$$  \hspace{1cm} (4)

$$t_{SUN} n_{REC}$$

Appearing in the expression are the concentrator efficiency, $n_{REC}$, the PV efficiency, $n_{PV}$, the heat engine efficiency, $n_{HE}$, the receiver efficiency, $n_{REC}$, the fraction of active PV area, $fp_A$, the PV array transmittance, $\tau$, and reflectivity, $\rho$, and the parameters, $Q_{BAT}$ and $\mu$.

$$f_{BAT} = \frac{1}{1 + \frac{t_{SH}}{t_{SUN} n_{BAT}^{n_{BAT}}}}$$  \hspace{1cm} (5)

$$Q_{BAT} = \frac{t_{SUN} t_{SH}}{t_{SUN} + n_{BAT}^{n_{BAT}}}$$  \hspace{1cm} (6)

The important approximations made in obtaining $n_T$ are the following.

1. Radiation loss from PV array negligible compared to radiation loss from receiver.
2. Radiation from receiver impinging on PV array is neglected.

Equation (4) is for a transmitting system. By interchanging $\tau$ and $\rho$ the results for a reflecting system are obtained. The parameter, $Q_{BAT}$, compares the electrical storage efficiency to thermal storage efficiency. If electrical energy storage efficiency ($n_{BAT}^{n_{BAT}}$ where $n_{BAT}$ is the efficiency the stored energy is delivered to the load and $n_{BAT}^{n_{BAT}}$ is the efficiency the energy from the PV array is stored) is greater than the thermal energy storage efficiency, $n_{HE}$, then $Q_{BAT} > 1$. The more likely situation is that $Q_{BAT} < 1$. As a result $f_{BAT} < 1$.

Now consider a comparison between the PVHE system and a heat engine only system. To obtain the efficiency, $n_{HE}$, of the heat engine only system let $fp_A n_{PV} = 0$, $\tau = 1$ and $\rho = 0$ in Eq. (4).

$$n_{HE} = n_{REC} \frac{Q_{BAT}}{Q_{HE}}$$  \hspace{1cm} (7)

Therefore, from Eqs. (4) and (7) for the case where $f_{BAT}$, $n_{REC}$ and $n_{HE}$ are the same for both the PVHE and heat engine only systems the following is obtained.

$$n_T = n_{PV} n_{PV} \left[ f_{BAT} - 1 \right] + \frac{1}{n_{HE}} \left[ 1 - (1 - Q_{HE}) + (1 - \rho) + \rho \right]$$  \hspace{1cm} (8)

This result applies for a transmitting system, but by interchanging $\tau$ and $\rho$ results for a reflecting system are obtained.

For an efficient reflecting system it is required that $\tau > 0$. whereas for an efficient transmitting system $\rho > 0$ is desired. For these conditions since $0 < \rho < 1$ and $0 < \tau < 1$ the terms $1/n_{REC} \left( 1 - \tau - \rho \right) + \rho$ for a reflecting system and $1/n_{REC} \left( 1 - \tau - \rho \right) + \tau$ for a transmitting system will always be greater than 1. Also, if $f_{BAT} > 1$, then as Eq. (8) shows, $n_T/n_{HE} > 1$.

In Fig. 2, $n_T/n_{HE}$ is plotted as a function of $Q_{BAT}$. For the case $Q_{BAT} = 1$. This result applies to both the transmitting and reflecting systems for $1/n_{REC} \left( 1 - \tau - \rho \right) + \tau = 1$ in the transmitting case and $1/n_{REC} \left( 1 - \tau - \rho \right) + \rho = 1$ in the reflecting case. Since these terms are greater than 1, as discussed above, and for most cases $f_{BAT} > 0.9$ the results in Fig. 2 should be representative of
PVHE systems. It is expected that $0.1 \leq f_{PVNPV/REC} \leq 0.25$. As a result $n_{HE} / n_{REC}$ is plotted as a function of $n_{HE}$ for $f_{PVNPV/REC} = 0.1, 0.15, 0.2$, and 0.25.

From Fig. 2 it can be seen that for a heat engine with $n_{HE} = 0.2$ the PVHE system shows an improvement in efficiency $1.4 \leq n_{HE} / n_{REC} \leq 2$ over the heat engine only system. For $n_{HE} = 0.3, 1.2 \leq n_{HE} / n_{REC} \leq 1.6$ and for $n_{HE} = 0.4, 1.1 \leq n_{HE} / n_{REC} \leq 1.4$. Therefore, the PVHE system offers significant improvement in efficiency over a heat engine only system. In the next section an estimate of area and mass savings for the PVHE system will be made.

Concentrator area savings. The concentrator area savings for the PVHE system compared to a heat engine only system are given by the following result:

$$C_T = \frac{n_0}{n_T}$$

Where $C_T = A_{C/}(P_{EL} + P_{EL})$ is the concentrator specific area in the PVHE system and $C_0$ is concentrator specific area in the heat engine only system. Thus the reduction in concentrator specific area is inversely proportional to the efficiency improvement. Figure 3 shows $C_T/C_0$ as a function of the heat engine efficiency, $n_{HE}$, for the same conditions as Fig. 2. As can be seen significant reductions in concentrator specific area are possible with the PVHE system.

Heat engine radiator area savings. In Ref. 5 the following expression for the ratio of the radiator specific area, $y = \frac{A_{RAD}/(P_{EL} + P_{EL})}$, for the PVHE system to radiator specific area $y_0$, for the heat engine only system is developed.

$$y_T = \frac{n_0}{n_T} \left( \frac{a}{a - \tau} \right)$$

This result is for a transmitting system; replace $\tau$ by $\rho$ to obtain the result for a reflecting system. In obtaining Eq. (10) it is assumed that both systems operate with the same radiator temperature, emissivity and heat engine efficiency. As will be discussed later, in order to have $T_{PV}$ (PV array temperature) as low as possible the absorptivity, $a$, must be small. Therefore, the term in brackets in Eq. (10) will be less than one. In that case the reduction in $y_T/y_0$ will be greater then the concentrator area reduction $C_T/C_0$.

Only the heat engine radiator area has been considered above. If the electrical energy storage efficiencies ($n_{ST}$ and $n_{BAT}$) are not large then the radiator area necessary to reject the waste heat from the electrical energy storage system may be significant.

Receiver mass savings. The receiver (including thermal storage material) is one of the most mass components in a heat engine system. To estimate the receiver mass assume the mass, $M_{REC}$, is proportional to the input power.

$$M_{REC} = \frac{\pi}{4} D_{REC}^2$$

where $D_{REC}$ (kg/kW) is a constant and $P_{REC}$ is the total receiver power input. Using results from Ref. 5, the following is obtained for the ratio of PVHE receiver specific mass, $(R_T = M_{REC}/(P_{EL} + P_{EL}))$, to heat engine only specific mass, $R_0$.

$$\frac{R_T}{R_0} = \frac{1 - f_{PVNPV}}{R_T} \frac{n_0}{n_T}$$

Equation (12) applies for a transmitting PVHE system; replace $\rho$ by $\tau$ to obtain the result for a reflecting system. In obtaining Eq. (12) it was assumed that both systems have the same $n_{HE}$, $T_{SUN}$, $T_{SH}$ and $D_{REC}$.

In the PVHE system part of the energy storage is done electrically. Therefore, to make a valid comparison of receiver mass savings between the PVHE and heat engine only systems the electrical energy storage mass must be included. Assume the electrical energy storage system mass, $M_{BAT}$, is proportional to the amount of stored energy, $E_{ST}$.

$$\frac{E_{ST}}{E_{ST}} = \frac{t_{SUN} + t_{SH}}{t_{SUN} + t_{SH}}$$

where $\alpha_{BAT}$ (kW/kg) is the specific energy density of the electrical energy storage system.

Based on the results of Ref. 5, the following is obtained.

$$B_T = \frac{\alpha_{BAT} / \alpha_{BAT}}{t_{SUN} + t_{SH} + t_{SH}} \frac{n_0}{n_T}$$

Where $\alpha_{BAT}$ is the electrical storage specific mass, $(\alpha_{BAT}/(P_{EL} + P_{EL}))$, and the parameter, $\gamma_{BAT}$, is a measure of electrical energy storage effectiveness. The smaller $\gamma_{BAT}$ is, the more effective electrical energy storage will be.

In deriving Eq. (14) it was assumed that $n_{HE}$, $T_{SUN}$, and $T_{SH}$ are the same for both the PVHE and heat engine only system.

If Eqs. (12) and (14) are added the following results:

$$\frac{R_T + \gamma_{BAT} B_T}{R_0} = \frac{1 - f_{PVNPV}}{R_T} \frac{n_0}{n_T}$$

This result applies to a transmitting PVHE system. If $\rho$ is replaced by $\tau$ then results for a reflecting PVHE system are obtained. As Eq. (16) shows, the receiver mass savings for the PVHE system are sensitive to the parameters $\gamma_{BAT}$ and $B_T$ (determines $n_0/n_T$, Eq. (8)). Evaluating $\gamma_{BAT}$ and $B_T$ requires choosing a specific electrical energy storage system. Consider three battery storage systems as being representative of the state of development of electrical storage systems. First, assume for the the presently available nickel-cadmium battery a specific energy density of $0.004$ kWh/kg, $a_{BAT} = 0.8$, $n_{BAT} = 0.9$. Second, assume for the soon to be available nickel-hydrogen battery a specific energy density of $0.0139$ kWh/kg, $n_{BAT} = 0.8$, $n_{BAT} = 0.9$. Finally, for a future system consider
the sodium-sulfur battery with \( \eta_{BAT} = 0.77\) kWh/kg, \( \eta_{THERM} = 0.8\), \( \eta_{BAT} = 1\). For the receiver assume \( \eta_{REC} = 6.4\) kg/kW and \( \eta_{THERM} = 0.9\), which is representative of the receiver being considered for the Space Station Rankine cycle power system. Therefore, for a system in low earth orbit with \( t_{SUN} = 1\) hr, \( t_{SH} = 38\) min, Eqs. (5) and (15) yield the following results. For Ni-Cd; \( \eta_{BAT} = 0.91\), \( \eta_{THERM} = 14.6\), for Ni-H; \( \eta_{BAT} = 0.91\), \( \eta_{THERM} = 4.2\), and finally for Na-S; \( \eta_{BAT} = 0.95\), \( \eta_{THERM} = 0.72\). Since \( \eta_{BAT} > 0.9\) for all three systems, the efficiency \( \eta_{BAT} = 0.8\). For the receiver assume \( \eta_{BAT} \) to be sodium-sulfur battery with \( \eta_{BAT} \). For the transmitting PVHE system \( \eta_{BAT} \) and finally for Na-S; \( \eta_{BAT} \). Since \( \eta_{BAT} > 0.9\) for all three systems, the efficiency ratio, \( \eta_{BAT} / \eta_{THERM} \), will be nearly the same for each system. However, the wide variation in \( \eta_{BAT} \) means there will also be a wide variation in \( (R_T + B_T)/R_T \). In Fig. 4 \( (R_T + B_T)/R_T \) is shown as a function of heat engine efficiency for the same conditions as Fig. 2 with \( fp_{PV}/\eta_{REC} = 0.15 \) and for three values of the quantity \( 1 + fp_{PV}(\eta_{BAT} - 1) - \rho \) for the transmitting PVHE system or \( 1 + fp_{PV} (\eta_{BAT} - 1) - \tau \) for the reflecting PVHE system. A value of 3 is representative of Ni-Cd, a value of 1.5 is representative of Ni-H\(_2\) and a value of 1.0 is representative of Na-S. As Fig. 4 indicates no receiver mass savings will occur if Ni-Cd batteries are used. In the case of Ni-H\(_2\) batteries savings will occur for \( \eta_{HE} < 0.25 \) and for Na-S batteries savings occur for all \( \eta_{HE} \). A large mass addition will result if a PVHE system must use Ni-Cd batteries. This large mass penalty makes a PVHE system using Ni-Cd batteries unattractive for a low earth orbit power system.

### Photovoltaic Array Temperature Requirements

As already mentioned, the major problem for the PVHE system is temperature operation of the PV array. The PV array temperature, \( T_{PV} \), must be greater than the bottom temperature of the heat engine radiator, \( T_B \), in order for the PV array to reject its waste heat \( \text{(w)P}<P_{INW} \) to the heat engine working fluid.

To estimate \( T_{PV} \), a simple heat transfer analysis presented in Ref. 5 was carried out. The assumptions made in that analysis are the following.

1. **PV array temperature, \( T_{PV} \), is constant**
2. **heat transfer coefficient, \( h \), is constant**
3. **specific heat, \( c_T \), of working fluid flowing over PV array is constant**
4. **radiation from PV array neglected**

Using these assumptions the following result was obtained for \( K_u \gg 1 \).

\[
\alpha T = T_{PV} - T_B = \alpha K
\]

(17)

Therefore, in order to minimize \( \alpha T \) the absorptivity must be low.

The parameter, \( K \), is determined by the PV array optical properties the ratio of shade time to sun time, \( t_{SH}/t_{SUN} \), and a characteristic temperature for the heat engine. This characteristic temperature is \( \Delta H/c_T \), where \( \Delta H \) is the enthalpy change of the working fluid across the receiver in a heat engine only system and \( c_T \) is the specific heat of the working fluid and the PV array. The parameter, \( u \), is determined by the ratio of total PV array area to concentrator area, \( A_T/A_C \), and the heat transfer coefficient \( \alpha \).

Thus \( u \) can be varied by changing the location of the PV array with respect to the concentrator (varying \( A_T/A_C \)).

The ratio of PV array area, \( A_T \), to the heat transfer area, \( A_B \), is given by the parameter, \( u \).

Since, the heat transfer area will be equal on less than total array area, \( u \leq 1 \). The expression for \( K \) given by Eq. (20) is for a transmitting PVHE system. For a reflecting system merely replace \( \tau \) by \( \rho \) in Eq. (20).

Consider values for \( K \) that are representative of heat engines being studied for the Space Station. Two of these are the toluene Rankine heat engine \( (\Delta H/c_T = 280 K) \) and the He-Xe Brayton heat engine \( (\Delta H/c_T = 180 K) \). Also, assume a low earth orbit \( (t_{SH}/t_{SUN} = 2/3) \) and a value of 0.7 for the receiver temperature. Then, according to Eq. (17), the temperature rise, \( \Delta T < 200 \) K, should be attainable. For \( \alpha = 0.3 \), however, temperature rises greater than 200 K will result. In this case the temperature of the PV array, \( T_{PV} \), may be too high for PV conversion. For the toluene Rankine heat engine the bottom temperature of the cycle is \( T_B = 340 K \). The He-Xe Brayton heat engine has a bottom temperature \( 290 K \). However, the working fluid enters the compressor rather than the heat source at this temperature. Therefore, heat addition occurs after the compressor. At this point the temperature is \( T_B = 380 K \). Therefore, for \( \Delta T = 200 K \) the PV array temperature would be \( T_{PV} = 540 \) to 580 K. Operation of gallium arsenide (GaAs) PV cells at temperatures \( >600 \) K are discussed in Ref. 1. The efficiency \( \eta_{PV} \) decreases with increasing temperature. However, the decrease is partially balanced by operating at high intensity, as in the proposed PVHE systems. Efficiency increases with intensity \( \eta_{PV} \) up to about 1000 PSUN. Two possible candidates for a high temperature, high intensity PV cell are the vertical multijunction (VJM) cell10,12 and the interdigitated back contact PV cell13,14 considered for thermophotovoltaic conversion.

Besides low absorptivity, a reduced value of the parameter, \( K \), will also result in lower array temperature, \( T_{PV} \). A possible method for reducing \( K \) is to reduce \( \Delta H \). This can be done by increasing the mass flow rate in the heat engine cycle. However, such a change will also alter the heat engine.
cycle performance. In the design of a PVHE system it will be necessary to vary the heat engine operating conditions in order to find the optimum.

COMPARISON OF SPACE STATION ORGANIC RANKINE CYCLE AND PVHE

Earlier it was shown how the PVHE system can result in significant reductions in mass and area compared to a heat engine only system. Now consider a mass and area comparison between the tol- 

eu Rankine cycle (ORC) being considered for the Space Station® and a PVHE system that uses the same Rankine cycle. The Space Station system consists of two modules that each produce 25 kWe.

Table I lists the ORC performance parameters for a 25 kWe module taken from Ref. 8, as well as, the assumed values used for the PVHE system. The assumed PVHE system is either reflecting (ρ = 0.5, 

τ = 0.05, α = 0.3) or transmitting (ρ = 0.05, 

τ = 0.05, α = 0.3). Using Eq. (8) and the parameters in Table I, the efficiency ratio is the following.

\[ \eta_T = 1.39 \]

The overall efficiency of the ORC system is 0.17, which includes the power conditioning efficiency and the electrical power for the concentrator controls. Assuming these losses are the same for the PVHE system then the efficiency of the PVHE system is the following.

\[ \eta_T = 0.17(1.39) = 0.23 \]

Table II presents the results of the mass and area comparison. The concentrator and radiator areas for the PVHE system were calculated using Eqs. (9) and (10). The PVHE concentrator and radi- 

ator masses were obtained by assuming they are proportional to their respective areas. Receiver and battery mass for the PVHE system were cal-

culated using Eqs. (12) and (14). Two battery masses are shown in Table II: one based on bipolar nickel-hydrogen batteries (\( \alpha_{BAt} = 0.139 \) kWh/kg) and the other on sodium sulfur batteries (\( \alpha_{SBat} = 0.077 \) kWh/kg). The mass of the Rankine power conversion unit for the PVHE system was obtained by assuming the mass is a linear function of power output. Interface structure mass (including the gimbal joint for the concentrator,) for the PVHE system was obtained using the same fraction of the total mass as for the Rankine only system (structure mass/total mass = 0.15). Mass of the PV array in the PVHE system was calculated assuming the same specific mass as that of the concentrator (6.6 kg/m²) and a concentrator to PV array area ratio of 60. If it is necessary to reject the waste heat of the electri- 

cal storage system. An estimate of the mass and area of this radiator was obtained by assuming the waste heat was rejected at a temperature of 30 °C and emissivity of 0.9 with the same mass/area as the heat engine radiator. Not included in Table II is the mass of the power conditioning equipment.

Several interesting results are pointed out by Table II. First of all the total PVHE system mass for \( \alpha_{BAt} = 0.0139 \) kWh/kg is nearly 25 percent less than the ORC system. The PVHE concentrator area is 30 percent less than the ORC system concentration area. Also, the PVHE radiator area is 40 percent less than the ORC system radiator area. The major mass and area savings for the PVHE system occur for the radiator. Finally, since batteries are not a major portion of the total mass, using the optimistic sodium-sulfur batteries rather than nickel-hydrogen batteries does not result in a major reduction in the total mass of a PVHE system. For an all PV array power system the batteries are the major mass component. Therefore, in that case a large energy density electrical storage component is critical for obtaining a low mass system. Whereas, the PVHE system mass is much less sensitive to the electrical storage mass.

The large radiator mass and area savings of the PVHE system result because the waste heat of the PV array (Fig. 1) is used by the heat engine rather than rejected to space. Only by operating the PV array at high temperature is it possible to utilize the PV array waste heat in the heat engine cycle. If the PV array can not operate at high temperature then PREJ would have to be rejected to space. This lower temperature heat rejection would require a large radiator area.

Consider an estimate of the PV array temperature, \( T_{PV} \), required in the above example. Assuming \( K >> 1 \), then Eq. (17) can be used to estimate \( T_{PV} \). From the data in Table I, \( K = 646 \) K. Therefore, using Eq. (17) and a bottom temperature \( T_B = 60 \) °C, the following temperature \( T_{PV} = 527 \) K. Reaching PV array temperatures this high is the critical issue for the space PVHE system. Without high temperature PV array operation the large area and mass savings are not possible.

Conclusion

Both transmitting and reflecting PVHE systems result in significant efficiency improvements, over a heat engine only system (\( 1.1 \leq \eta_T / \eta_0 \leq 2 \)). Choosing between the reflecting and transmitting systems depends on several things. One important consideration is the PV array absorptivity, \( \alpha \). In order to maintain the PV array temperature, \( T_{PV} \), as low as possible \( \alpha \) must be small (\( \alpha < 0.3 \)). Also, for the transmitting system the reflectivity, \( \rho \), must be small. Whereas for the reflecting system the transmittance, \( \tau \), must be small.

Research on reflecting and transmitting PV arrays is necessary to determine which can best meet these requirements. However, the critical issue for both PV array types is the high temperature (\( T_{PV} = 600 \) K) is required. A suitable cell structure that will meet the high temperature requirements is the essential ingredient for a successful PVHE system.

As a result of improved efficiency over a heat engine (\( \eta_T / \eta_0 > 1 \)) the PVHE systems will have corresponding savings in concentrator area (\( C / C_0 = n_0 / n_T \)). Also, the PVHE system will result in heat engine radiator savings greater than concentrator area savings. Receiver and energy storage mass savings will occur for the PVHE system if high energy density electrical storage (\( \alpha_{BAt} < 1 \)) is available. A mass penalty will occur if low energy density electrical storage, such as nickel-cadmium batteries are used.

A mass and area comparison was made between the Space Station organic Rankine cycle power system and a hypothetical PVHE system using the same Rankine system. Nearly a 25 percent reduction in
overall mass was calculated, as well as a concentrator area reduction of 30 percent and a radiator area savings of 40 percent for the PVHE system.

Besides efficiency, area and mass savings the PVHE systems have a degree of inherent system redundancy. If the PV array should fail without blocking the input solar flux the heat engine part of the system would still be able to provide part of the electrical load. Similarly, if the heat engine should fail without interrupting the flow of the system fluid the PV array would be able to produce part of the electrical load.

References


### Table I. - Performance Parameters of Space Station
25 kWe Organic (Toluene) Rankine Cycle (ORC)
Power System and Hypothetical PVHE System
Using the Same ORC

<table>
<thead>
<tr>
<th>Parameter</th>
<th>ORC</th>
<th>PVHE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Concentrator efficiency, $n_C$</td>
<td>0.90</td>
<td>0.90</td>
</tr>
<tr>
<td>Receiver efficiency efficiency, $n_{Rec}$</td>
<td>.90</td>
<td>.90</td>
</tr>
<tr>
<td>Storage Efficiency $n_{st} =$</td>
<td>.91</td>
<td>.80</td>
</tr>
<tr>
<td>Heat engine Efficiency $n_{HE}$</td>
<td>.27</td>
<td>.27</td>
</tr>
<tr>
<td>PV array efficiency, $f_{pymax}$</td>
<td>.15</td>
<td></td>
</tr>
<tr>
<td>SUN time $\tau_{SUN}$, min</td>
<td>54.7</td>
<td>54.7</td>
</tr>
<tr>
<td>Shade time, $\tau_{SH}$, min</td>
<td>36.3</td>
<td>36.3</td>
</tr>
<tr>
<td>Receiver specific mass, $P_{REC}$, kg/kW</td>
<td>6.35</td>
<td>6.35</td>
</tr>
<tr>
<td>PV array absorptivity, $\alpha$</td>
<td>.30</td>
<td></td>
</tr>
<tr>
<td>PV array reflectivity, $\rho$</td>
<td>0.50 reflection system</td>
<td>.05 transmitting system</td>
</tr>
<tr>
<td>PV array transmittance, $\tau$</td>
<td>0.50 reflection system</td>
<td>.05 transmitting system</td>
</tr>
</tbody>
</table>
TABLE II. - COMPARISON OF SPACE STATION ORC POWER SYSTEM AND HYPOTHETICAL PVHE SYSTEM USING THE SAME ORC

[Electrical Power Output = 25 kWe]

<table>
<thead>
<tr>
<th>Component</th>
<th>Mass for ORC, kg</th>
<th>Mass for PVHE, kg</th>
<th>Area for ORC, m²</th>
<th>Area for PVHE, m²</th>
</tr>
</thead>
<tbody>
<tr>
<td>Concentrator</td>
<td>1414</td>
<td>1018</td>
<td>213</td>
<td>153</td>
</tr>
<tr>
<td>Receiver and thermal storage</td>
<td>1426</td>
<td>821</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Electrical storage</td>
<td></td>
<td>610(αBAT = 0.0139 kWh/kg)</td>
<td>110(αBAT = 0.077 kWh/kg)</td>
<td></td>
</tr>
<tr>
<td>Heat engine</td>
<td>567</td>
<td>340</td>
<td></td>
<td></td>
</tr>
<tr>
<td>PV array</td>
<td></td>
<td>20</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Heat engine radiator</td>
<td>2182</td>
<td>1309</td>
<td>160</td>
<td>96</td>
</tr>
<tr>
<td>Electrical storage radiator</td>
<td></td>
<td>199</td>
<td></td>
<td>15</td>
</tr>
<tr>
<td>Interface structure and Beta Gimbel joint</td>
<td>982</td>
<td>756(αBAT = 0.0139 kWh/kg)</td>
<td>668(αBAT = 0.077 kWh/kg)</td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>6571</td>
<td>5073(αBAT = 0.0139 kWh/kg)</td>
<td>4485(αBAT = 0.077 kWh/kg)</td>
<td>373</td>
</tr>
</tbody>
</table>

ORC efficiency, $\eta_O = 0.17$

PVHE efficiency, $\eta_T = 0.23$

ORC specific mass = 263 kg/kWe

PVHE specific mass = 203 kg/kWe (αBAT = 0.0139 kWh/kg)

PVHE specific mass = 179 kg/kWe (αBAT = 0.077 kWh/kg)

Power ratio for PVHE system = $\frac{\text{Power output of ORC}}{\text{Power output of PV array}} = \frac{P_{EL}}{P_{EL}} = 0.78$
FIGURE 1. - SCHEMATIC DIAGRAMS OF PHOTOVOLTAIC HEAT ENGINE (PVHE) SYSTEMS.
FIGURE 2. - EFFICIENCY IMPROVEMENT FOR PVHE SYSTEM OVER HEAT ENGINE WITH BOTH SYSTEMS OPERATING WITH SAME CONCENTRATOR EFFICIENCY $\eta_C$ AND RECEIVER EFFICIENCY $\eta_{REC}$. ALSO, FOR REFLECTING PVHE SYSTEM $1/\eta_{REC} (1-T-p) + p = 1$, AND FOR TRANSMITTING PVHE SYSTEM, $1/\eta_{REC} (1-T-p) + \tau = 1$. FOR COMBINATION ELECTRICAL AND THERMAL ENERGY STORAGE $\Gamma_{BAT} = 1$. 

RATIO OF PVHE SYSTEM TO HEAT-ENGINE-ONLY SYSTEM EFFICIENCY, $\eta^*/\eta_0$
Figure 3. - Concentrator area savings for PVHE system over heat engine with same conditions as Fig. 2.
REFLECTING SYSTEM \[ 1 + f_{PV} \gamma_{PV} y_{BAT^{-1}} - \tau = \]

TRANSMITTING SYSTEM \[ 1 + f_{PV} \gamma_{PV} y_{BAT^{-1}} - \rho = \]

FIGURE 4. - RECEIVER MASS SAVINGS FOR PVHE SYSTEM OVER HEAT ENGINE ONLY SYSTEM WITH SAME CONDITIONS AS FIG. 2. IN ADDITION, \( f_{PV} \gamma_{PV} \eta_{REC} = .15 \).
Performance Characteristics of a Combination Solar Photovoltaic Heat Engine Energy Converter

A combination solar photovoltaic heat engine energy converter is proposed. Such a system is suitable for either terrestrial or space power applications. The combination system has a higher efficiency than either the photovoltaic array or the heat engine alone can attain. Advantages in concentrator and radiator area and receiver mass of the photovoltaic heat engine system over a heat-engine-only system are estimated. A mass and area comparison between the proposed Space Station organic Rankine power system and a combination PV-heat engine system is made. The critical problem for the proposed converter is the necessity for high-temperature photovoltaic array operation. Estimates of the required photovoltaic temperature are presented.