Comparison of the Bidirectional Reflectance Distribution Function of Various Surfaces

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Comparison of the Bidirectional Reflectance Distribution Function of Various Surfaces

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SUMMARY

This paper describes the development and use of a system to measure the Bidirectional Reflectance Distribution Function (BRDF) of various surfaces. The BRDF measurements will be used in the analysis and design of optical measurement systems, such as laser anemometers. An argon ion laser (514 nm) was the light source. Preliminary results are presented for eight samples: two glossy black paints, two flat black paints, black glass, sand blasted aluminum, unworked aluminum, and a white paint. A BaSO₄ white reflectance standard was used as the reference sample throughout the tests. The reflectance characteristics of these surfaces are compared in this paper.

1. INTRODUCTION

The geometrical reflectance properties of a surface is of importance in many fields and has a broad range of applications. Some examples are: minimizing stray light reflections for Space Telescopes, modeling the performance of solar energy collectors, and knowing how surface reflections affect the signal-to-noise (SNR) ratio in laser anemometry (LA) measurements. The latter application is of relevance in this paper. The reflectance characteristics of surfaces are expressed in terms of the Bidirectional Reflectance Distribution Function (BRDF).

The results from this study can be used to define the surface model used in a computer simulation of an LA system used near a wall. Preliminary results are presented for eight samples: two glossy black paints, two flat black paints, black glass, sand blasted aluminum, unworked aluminum, and a white paint. With an accurate surface model, the optical system can be optimized. Later LA experiments would be required to verify the performance predictions of the computer model.

Aluminum was used as the base material for all the paints because it is a commonly used structural material for fluid flow test facilities and models. Black Schott NG-1 neutral density filter glass was tested because it is frequently used in the construction of optical systems, such as light traps.
Therefore the objective of this study was to measure the BRDF of various surfaces and to compare the results in order to pick candidates for the surface models.

2. APPARATUS & TEST METHODS

The BRDF is a function that specifies and describes the geometrical reflectance properties of a surface. The BRDF is a function of four angles (two angles for the incident radiation and two angles for the reflected radiation), and the surface's reflecting properties:

\[
\text{BRDF}(\Theta_i, \phi_i ; \Theta_r, \phi_r) = \frac{dL_r(\Theta_i, \phi_i ; \Theta_r, \phi_r ; E_i)}{dE_i(\Theta_i, \phi_i)}
\]

where:
- \(\Theta\) = polar angle
- \(\phi\) = azimuthal angle
- \(i\) = incident
- \(r\) = reflected
- \(L\) = reflected radiance
- \(E\) = incident irradiance

The angles are illustrated in figure 1. The surface's reflecting properties manifest themselves in the reflected radiance of the incident irradiance.

Figure 2 shows a schematic representation of the optical configuration. The reason for the circuitous beam path is that the same laser is used for two experiments, this BRDF study and LA studies. When the removable mirror is in place (as in figure 2), it intercepts the laser beam and reflects it back to the sample holder used in this study. Lenses L1 and L2 are used to focus the laser beam on the sample surface. The laser beam was linearly polarized in the upward direction. Therefore, the incident beam on the sample surface was polarized perpendicularly to the measurement plane, i.e. it had "S" polarization.

The sample was mounted on a two-axis goniometer and the photodetector was mounted on an arm (Stage A) that could be rotated \(\pm 45^\circ\) as shown in figure 2. The goniometer could only rotate the sample holder about two orthogonal axes; Stage B rotated the sample holder in the horizontal plane and Stage C rotated it in the vertical plane. Because clockwise rotations, i.e. rotations about the normal to the sample surface, were not possible, \(\phi_i\) and \(\phi_r\) were combined into one difference angle, \(\delta\phi\). Where \(\delta\phi\) is the difference between the incident azimuthal angle, \(\phi_i\), and the exitent azimuthal angle, \(\phi_r\). Conversion equations were developed that related this angle as well as the polar angles, \(\Theta_i\) and \(\Theta_r\), to the actual experimental configuration angles, i.e. the goniometer angles and the rotational positioner angle. Because these equations were highly non-linear, a computer routine based on the Newton Raphson technique was used.

A Computer Numerical Control (CNC) positioning controller received these transformed angles from a PDP-11/44 computer and placed the rotational positioner stage (A stage) and goniometers (B and C stages)
at the correct angles. The photodetector was attached to stage A, 41.45 ± 0.05 cm from the sample. The data recording was automated; the A stage would sweep in an arc on command from the computer. When the A stage would stop after each angle increment, the light intensity striking the photodetector would be recorded on disk. The increment angle between data points was 2° for all the data shown in this paper.

Table 1 lists the relevant features of the various components in the test apparatus, and Table 2 lists the samples tested. As shown in Table 1, the Argon ion laser (514.5 nm) was operated at output powers relevant to LA, approximately 1 watt. There were two exceptions to this power level. When the Chemglaze Z302 sample was tested, scorching would occur for long exposures to any power level above 0.35 watts. Therefore, the Chemglaze was tested at a power level of 0.3 watts. Scorching would occur at 0.6 watts for the Sikkons 443-3-17 sample. Therefore, that sample was tested at a level of 0.51 watts. Drift in beam power was minimized in two ways. First, the laser was run in light control mode which uses a feedback circuit to maintain constant power output. Second, the data collection program constantly monitored the laser power. If the power varied by more than ± 2% an error message was issued.

Stray radiation was minimized by enclosing the test table in black velvet. A small hole was left for the incoming laser light. Background radiation runs were made with no samples and the laser set at various output power levels. For these, the laser beam did not strike the sample holder, but exited into the room through another small hole. These background light intensities were subtracted from the test sample light intensities for the corresponding laser power levels.

Table 2 lists the eight samples that were tested. The stock aluminum was tested at two different striation orientations. It was oriented with the striations horizontally and then it was tested again with the striations angled at 60° from horizontal. The black glass sample was tested on two bases, a black glossy base and a white lambertian base. All the painted samples were prepared by depositing a layer of paint, from an airbrush, on the surface of a smooth aluminum base and setting aside to cure as per the manufacturers instructions.

The Schott NG-1 black glass was tested on two different bases, the glossy black Chemglaze Z302 and the white BaSO₄ reference, in order to compare the subsurface scatter effects. Figure 3 illustrates the reflections from the upper and lower surfaces of a glass sample.

The reference sample method of computing BRDFs was used. The reference sample was a BaSO₄ packed powder which was nearly an ideal white Lambertian reflector. The BRDF of a Lambertian surface is defined to be:

\[
\text{BRDF} = \frac{\rho}{\pi}
\]

where: \(\rho\) = the absolute reflectance of the surface
The reflectance of the test sample, \( \rho = 0.991 \pm 0.005 \) at 500 nm, was taken from the manufacturer's specification sheet for our particular lot number.

Once the BRDF of a reference surface is known, the BRDF of a test sample can be found by:

\[
\text{BRDF}_s = \text{BRDF}_{\text{ref}} \left( \frac{V_s}{V_{\text{ref}}} \right)
\]

where: \( V_{\text{ref}} \) = the reference sample's photodetector voltage
\( V_s \) = the test sample's photodetector voltage

After the data recording was completed, another computer program would take the light intensites that were recorded on the computer disk and plot the BRDF profiles. It computed the BRDF by using the system parameters, i.e. laser power, gain settings, and angular positions, that were stored on disk at the start of each test run.

3. DISCUSSION OF RESULTS

Plots which show the BRDF for the test samples are presented in figures 4 to 9. The BRDF is presented in the figures by a polar plot. The radial scale shows the BRDF level while the circumferential scale shows the angular position of the photodetector (figure 2). Data were recorded for a photodetector angle sweep from \(+45^\circ\) to \(-45^\circ\). Some of the plots show an angle less than \(45^\circ\) on one side of the normal to the surface and an angle greater than \(45^\circ\) on the other side. This was due to stage B rotating the sample to achieve the desired beam incidence angle. The angle of incidence is indicated in the figure by the arrow labeled I. Because the scale was automatically selected by the computer plotting package, scale changes must be considered when comparing one figure to another.

Note that the sharp drop off, in the direction of the incident beam, observed in some of the graphs, is because the photodetector was behind mirror M2 (figure 2). When the photodetector is behind this mirror, it is in a 3" eclipse region. All data shown are for "in-plane" measurements; the surface normal, the incident beam, and the scattered beam lie in a common plane. Three laser beam incident angles, 1°, 10°, and 20°, are presented in the figures.

Interesting observations were made. Figure 4 shows results for the two flat black paints, Sheffield Pot-belly black and 3M ECP-2200 on the same graph for easy comparison. For all the incident angles, the pot belly black had a higher BRDF than the 3M ECP-2200, although both were flat blacks. Since both the paints were deposited on the same type of substrate, the differences can be attributed to the paints' properties.

Similarly, the two glossy blacks (figures 5 and 6) differed in their BRDF functions; the Sikkons 443-3-17 sample had a consistently larger maximum BRDF, i.e. the specular scatter, than the Chemglaze Z302 sample. The diffuse scatter portion of the distributions, however, had the opposite relationship. The Chemglaze Z302 had a higher BRDF than the Sikkons 443-3-17 sample. For these figures, only
the diffuse scatter portion of the BRDF is shown. The dashed lines indicate that the large BRDF values corresponding to the specular reflections are off scale. The spread out shape of the distribution indicates that cratering or surface damage of the Chemglaze Z302 had occurred. Upon visual inspection of the surface, small indentations were observed. Although scorching did not occur, a laser power level of 0.3 watts is still too high to avoid surface damage.

The aluminum samples demonstrated the affect of various surface finishes on the same type of material. As shown in figure 7 the sand blasted sample had a much smoother, diffuse, reflectance function, while the unworked samples exhibited specular behavior. Rotating the unworked sample by 60 ° drastically cut down the BRDF values and made the reflection less specular.

The white Nextel sample was close to the lambertian reference, as figure 8 illustrates. For higher incidence angles (figure 8c), however, the the lambertian behavior breaks down and the sample reflects light back towards the incident beam path more than it reflects the light in the specular direction. The Nextel surface would be desirable for LA applications where a uniform BRDF is desirable.

Figure 9 shows the behavior of the Schott NG-1 black glass sample. As with the figures for the glossy black paints, the larger BRDF values corresponding to specular scatter are off scale. The diffuse scattering from the black glass was significantly less than the diffuse scattering from the black paints. This surface had the lowest diffuse scatter characteristics of all the samples tested.

The data for the black glass with the two different base surfaces, the Chemglaze Z302 and the white BaSO₄ reference, showed that the BRDF values were similar for both bases. This indicates that not much light was getting through the black glass and onto the base surface. Therefore subsurface scatter effects were not very significant.

Data for out-of-plane reflectance properties were obtained during the research effort. Although these data are not presented in this paper, the results were predictable. The diffuse scattering samples, Nextel 101-A10, Sheffield Pot Belly Black, and 3M ECP-2200, had distributed BRDF profiles. The more specular scattering samples had peaked BRDF profiles. Furthermore, the test apparatus is being used to evaluate the reflectance properties of new samples.

4. SUMMARY OF RESULTS

Of the samples evaluated, the Schott NG-1 black glass sample had the best overall characteristics: high specular scatter for the one reflection angle, low diffuse scatter for other angles, and not sensitive to high incident power levels. Although the Chemglaze Z302 and the Sikkons 443-3-17 satisfied the first two requirements they are both sensitive to incident light levels.

The Nextel 101-A10 would be the desirable sample for applications that require a predictable and uniform BRDF profile. An example of this is are LA studies were the photodiode may be aimed along the
specular reflection angle and there is a chance that it may be overwhelmed by reflections from a bright surface. A lambertian surface would minimize this possibility.

Using this highly automated BRDF measurement system a database of candidate surfaces for LA measurements near a wall has been established. Furthermore, there is little data in the literature on BRDF measurements made with the high incident light levels that were used in this study. We have shown that although a material may have good reflectance properties, an important consideration is the incident light intensity. Too high an intensity may damage the material. This set of data should be useful for researchers needing reflectance data for laser based optical measurement systems.

5. ACKNOWLEDGMENTS

We thank Mr. Gordon Driver for his quick repair of any electrical problems encountered and Mr. Jerry Nelson for his help with mechanical problems.

6. REFERENCES

Table 1. BRDF System Component Summary

<table>
<thead>
<tr>
<th>Component</th>
<th>Details</th>
</tr>
</thead>
<tbody>
<tr>
<td>Laser</td>
<td>5 watt Argon ion (514.5 nm) model, light control operation, linearly polarized</td>
</tr>
<tr>
<td>Sample spot size</td>
<td>2.5 mm (0.0984 in) diameter</td>
</tr>
<tr>
<td>Collecting Area</td>
<td>0.1781 cm$^2$ (0.0276 in$^2$)</td>
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<td>Solid angle</td>
<td>$1.037 \times 10^{-4}$ steradians</td>
</tr>
<tr>
<td>Light power meter</td>
<td>P.I.N. Si Photodiode, ± 5 % accuracy analog output</td>
</tr>
<tr>
<td>Signal amplifier</td>
<td>Variable gain amplifier, 10Hz bandwidth</td>
</tr>
<tr>
<td>A stage</td>
<td>Arm mounted on a rotational positioner, ± 45°</td>
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<tr>
<td>B &amp; C stages</td>
<td>Goniometers, ± 45°</td>
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Table 2. Test Samples

<table>
<thead>
<tr>
<th>Sample</th>
<th>Fabrication</th>
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</thead>
<tbody>
<tr>
<td>Aluminum, sand blasted</td>
<td>Stock aluminum, was sand blasted</td>
</tr>
<tr>
<td>Aluminum, stock</td>
<td>Stock aluminum with striations</td>
</tr>
<tr>
<td>Black glass (Schott NG-1)</td>
<td>1 mm thick, glossy black glass</td>
</tr>
<tr>
<td>Chemglaze Z302</td>
<td>Black paint sprayed on aluminum</td>
</tr>
<tr>
<td>Nextel 101-A10</td>
<td>White paint sprayed on aluminum</td>
</tr>
<tr>
<td>Sheffield Pot-belly black</td>
<td>Flat black sprayed on aluminum</td>
</tr>
<tr>
<td>Sikkons 443-3-17</td>
<td>Black paint sprayed on aluminum</td>
</tr>
<tr>
<td>3M ECP-2200</td>
<td>Flat black sprayed on aluminum</td>
</tr>
</tbody>
</table>

![FIGURE 1. - ANGLES FOR THE INCIDENT AND REFLECTED BEAMS.](image)
FIGURE 2. - THE OPTICAL CONFIGURATION.

FIGURE 3. - SUBSURFACE SCATTER EFFECT.
FIGURE 4. - POLAR PLOT OF BRDF FOR 3M ECP-2200 VERSUS SHEFFIELD POT BELLY BLACK.

(a) 0° INCIDENT ANGLE. MAXIMUM BRDF OF 5.79 AT 0° IS OFF SCALE.

(b) 10° INCIDENT ANGLE. MAXIMUM BRDF OF 7.18 AT -10° IS OFF SCALE.

(c) 20° INCIDENT ANGLE. MAXIMUM BRDF OF 10.38 AT -20° IS OFF SCALE.

FIGURE 5. - POLAR PLOT OF BRDF FOR CHEMLAZE Z302 CHEMLAZE Z302 (SURFACE DAMAGED).
Figure 6. - Polar plot of BRDF for Sikkens 443-3-17.

Figure 7. - Polar plot of BRDF for the aluminum samples.
Figure 8. Polar plot of BRDF for Nexel 101-A10 versus BaSO₄.

Figure 9. Polar plot of BRDF for black glass.

(a) 1° incident angle. The maximum BRDF of 427 at 0° is off scale.

(b) 10° incident angle. The maximum BRDF of 1.15 at -10° is off scale.

(c) 20° incident angle. The maximum BRDF of 14.79 at -20° is off scale.
**Title and Subtitle**
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