USER'S MANUAL FOR THREE DIMENSIONAL BOUNDARY LAYER (BL3-D) CODE

by
O.L. Anderson
B. Caplin

Prepared for:
National Aeronautics and Space Administration
Lewis Research Center
**Abstract:**

An assessment has been made of the applicability of a three dimensional boundary layer analysis to the calculation of heat transfer, total pressure losses, and streamline flow patterns on the surfaces of both stationary and rotating turbine passages. In support of this effort, an analysis has been developed to calculate a general nonorthogonal surface coordinate system for arbitrary three dimensional surfaces and also to calculate the boundary layer edge conditions for compressible flow using the surface Euler equations and experimental data to calibrate the method. Calculations are presented for the pressure endwall, and suction surfaces of a stationary cascade and for the pressure surface of a rotating turbine blade. The results strongly indicate that the three dimensional boundary layer analysis can give good predictions of the flow field, loss, and heat transfer on the pressure, suction, and endwall surfaces of a gas turbine passage.

## TABLE OF CONTENTS

<table>
<thead>
<tr>
<th>Section</th>
<th>Description</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.0</td>
<td>SUMMARY</td>
<td>I-1</td>
</tr>
<tr>
<td>2.0</td>
<td>INTRODUCTION</td>
<td>II-1</td>
</tr>
<tr>
<td>3.0</td>
<td>GENERAL DESCRIPTION OF BL3D CODE</td>
<td>III-1</td>
</tr>
<tr>
<td></td>
<td>Geometry Analysis</td>
<td>III-2</td>
</tr>
<tr>
<td></td>
<td>Surface Euler Analysis</td>
<td>III-3</td>
</tr>
<tr>
<td></td>
<td>3-D Boundary Layer Analysis</td>
<td>III-4</td>
</tr>
<tr>
<td></td>
<td>Operation of Computer Codes</td>
<td>III-4</td>
</tr>
<tr>
<td>4.0</td>
<td>OPERATION OF SETUP CODE</td>
<td>IV-1</td>
</tr>
<tr>
<td>4.1</td>
<td>Input Format</td>
<td>IV-1</td>
</tr>
<tr>
<td>4.2</td>
<td>Output Format</td>
<td>IV-11</td>
</tr>
<tr>
<td>4.3</td>
<td>Output Data Files</td>
<td>IV-17</td>
</tr>
<tr>
<td>4.4</td>
<td>Diagnostics</td>
<td>IV-19</td>
</tr>
<tr>
<td>4.5</td>
<td>Sample Input</td>
<td>IV-21</td>
</tr>
<tr>
<td>5.0</td>
<td>OPERATION OF BL3D CODE</td>
<td>V-1</td>
</tr>
<tr>
<td>5.1</td>
<td>Input Format</td>
<td>V-1</td>
</tr>
<tr>
<td>5.2</td>
<td>Output Format</td>
<td>V-4</td>
</tr>
<tr>
<td>5.3</td>
<td>Input/Output Data Files</td>
<td>V-10</td>
</tr>
<tr>
<td>5.4</td>
<td>Diagnostics</td>
<td>V-15</td>
</tr>
<tr>
<td>5.5</td>
<td>Sample Input</td>
<td>V-15</td>
</tr>
<tr>
<td>6.0</td>
<td>DESCRIPTION OF SETUP CODE</td>
<td>VI-1</td>
</tr>
<tr>
<td>6.1</td>
<td>SETUP Main Program</td>
<td>VI-1</td>
</tr>
<tr>
<td>6.2</td>
<td>SETUP COMMON Block Variables</td>
<td>VI-3</td>
</tr>
<tr>
<td>6.3</td>
<td>Description of SETUP Subroutine</td>
<td>VI-13</td>
</tr>
<tr>
<td>7.0</td>
<td>DESCRIPTION OF BL3D CODE</td>
<td>VII-1</td>
</tr>
<tr>
<td>7.1</td>
<td>BL3D Main Program</td>
<td>VII-1</td>
</tr>
<tr>
<td>7.2</td>
<td>BL3D COMMON Block Variables</td>
<td>VII-4</td>
</tr>
<tr>
<td>7.3</td>
<td>Description of BL3D Subroutines</td>
<td>VII-13</td>
</tr>
<tr>
<td>Section</td>
<td>Title</td>
<td>Page</td>
</tr>
<tr>
<td>--------------</td>
<td>---------------</td>
<td>------</td>
</tr>
<tr>
<td>8.0</td>
<td>LIST OF SYMBOLS.</td>
<td>VIII-1</td>
</tr>
<tr>
<td>9.0</td>
<td>REFERENCES</td>
<td>IX-1</td>
</tr>
</tbody>
</table>
1.0 SUMMARY

This User's Manual contains a complete description of the computer codes developed and utilized under NASA contract NAS3-23716 "Assessment of a Three Dimensional Boundary Layer Code to Predict Heat Transfer and Flow Losses in a Turbine". The SETUP code calculates a general nonorthogonal surface coordinate system and the boundary layer edge conditions from a known static surface pressure distribution. The BL3D code utilizes this coordinate system and the edge conditions for the calculation of the three dimensional boundary layer on an arbitrary surface such as a turbine blade or end wall. A companion report to this User's Manual which is entitled "Assessment of a 3-D Boundary Layer Analysis to Predict Heat Transfer and Flow Field in a Turbine" documents the technical approach used in the SETUP and BL3D codes and presents results which have been obtained in the application of the three dimensional boundary layer theory to the flow in a turbine passage with blade rotation. Although the primary thrust of this work has been for gas turbine application, the compressible three dimensional boundary layer analysis is very general and can be used for a wide range of applications in internal and external aerodynamics.

The User's Manual is essentially divided into two parts. In the first part, Sections 3.0, 4.0, and 5.0, a description of the input, output, and general operation of both codes is presented. In the second part, Sections 6.0 and 7.0, a detailed description of the computer codes including a listing and description of all FORTRAN variables in COMMON blocks and a detailed description of the subroutines are given. These latter sections of the User's Manual are presented for the user who wishes to obtain a detailed understanding of the codes.
2.0 INTRODUCTION

This User's Manual describes the computer codes known collectively as the Three Dimensional Boundary Layer (BL3D) code which was developed under NASA Contract NAS3-23716. A description of the analysis used in the SETUP code is given by Anderson (Ref. 1). A comprehensive outline of the analysis used in the BL3D code is also given by Anderson (Ref. 1). The three dimensional boundary layer analysis used in the BL3D codes was developed by Vatsa (Refs. 2 and 3). Reference 3, in particular, describes in detail the solution algorithm including the finite difference equations and the matrix inversion method. Assessment of these codes for gas turbine applications is also given in Ref. 1 through 3. The SETUP code contains a prepackaged surface spline fitting routine developed by McCartin (Ref. 6) which is not described.

This report is divided into sections for the convenience of the user. Section 3.0 contains an overall description of the computer codes describing how they are linked together functionally and through data files. Sections 4.0 and 5.0 contain a description of the input and output files so that the user can run the codes and interpret the printed output. These sections also contain a sample input data file to assist the user in setting up new cases. Although these codes are very robust, they sometimes fail. If the cause of the failure is known, a DIAGNOSTIC is printed and the calculation is terminated. A description of these failures and DIAGNOSTICS is also given. Sections 3.0 through 5.0 contain all the information required by the user who wishes to run these codes but does not require a detailed understanding of the codes.
Sections 6.0 and 7.0 contain a more detailed description of these computer codes for the user who wishes to modify these codes. These sections are divided into three subsections. The first subsection describes the MAIN program including a global tree structure chart which provides the user with an overview of the code. This section includes all calling and called subroutines. The second subsection contains a list of all FORTRAN symbols which are contained in COMMON blocks. These FORTRAN symbols may be identified with the corresponding algebraic symbols which are the same as those used in Ref. 1. The third subsection contains a detailed description of each subroutine. These subroutine descriptions are arranged according to the same format. First, the object of the subroutine is described. Second, any input options used in the subroutine are described so that the user can understand any branching that takes place. Third, a list of local FORTRAN symbols is given. Finally a description of the analysis used in the subroutine is given. If the analysis is described in Ref. 1, it is referenced by subsection. If the analysis is not described in Ref. 1, it is described in these subroutine descriptions. In cases where well known analyses, such as interpolation formulas, are used the source reference is given.
3.0 GENERAL DESCRIPTION OF BL3D CODE

The Three dimensional boundary layer (BL3D) code requires three separate analyses: 1) an analysis to construct a general nonorthogonal coordinate system for a twisted turbine blade, 2) an analysis referred to as a surface Euler analysis to calculate the boundary layer edge conditions from a known wall static pressure distribution, and 3) an analysis to calculate the three dimensional boundary layer growth on the turbine blade surface. These analyses are contained in two separate computer codes. The SETUP code contains the coordinate analysis and the boundary layer code analysis. The BL3D code contains the boundary layer analysis. A detailed description of the coordinate analysis and boundary layer edge analysis contained in the SETUP code is given by Anderson (Ref. 1). A general outline of the boundary layer analysis contained in the BL3D code is given by Anderson (Ref. 1). A detailed description of the boundary layer analysis including the finite difference equations and the matrix inversion analysis is given by Vatsa (Refs. 2 and 3).

A flow chart describing the operation of these computer codes is shown on Fig. 1. The geometry analysis calculates a surface coordinate system which is required by both the surface Euler analysis and the three dimensional boundary layer analysis. The surface Euler analysis calculates the boundary layer edge conditions. This data is then input into the 3D boundary layer analysis. A brief description of these codes is given below.
Geometry Analysis

Since the boundary layers lie on the blade surface, a convenient coordinate system is a surface coordinate system \((X_1,X_2,X_3)\) which has the properties that two coordinates \((X_1,X_2)\) lie on the blade surface and the third coordinate \((X_3)\) is normal to the blade surface. \(X_1\) is generally taken to be in the streamwise direction and \(X_2\) is generally in the crossflow direction. This coordinate system, in general, must be a non-orthogonal coordinate system, therefore \(X_1\) is not necessarily orthogonal to \(X_2\). Furthermore we note that a given twisted turbine blade is not a developable surface (i.e., it can not be flattened to a plane surface without distortion). Thus if we describe the turbine blade in Cartesian coordinates \((Y_1,Y_2,Y_3)\), where \(Y_1\) is generally in the streamwise direction, \(Y_2\) in the crossflow direction, and \(Y_3\) orthogonal to \((Y_1,Y_3)\), then a mathematical transformation must be found for the relation between the computational coordinates \((X_1,X_2,X_3)\) and the physical coordinates \((Y_1,Y_2,Y_3)\). In general, the equation of the physical surface can be expressed as \(Y_3 = Y_3(Y_1,Y_2)\). Thus if a unique relation can be found \(Y_1 = Y_1(X_1,X_2)\) and \(Y_2 = Y_2(X_1,X_2)\), then the third coordinate is known \(Y_3 = Y_3(X_1,X_2)\). This unique relation is provided by the transfinite mapping of Gordon and Thiel (Ref. 4). Once the transformation from the computational coordinates \((X_1,X_2,X_3)\) to the physical (Cartesian) coordinates is known, the covariant matrix tensor, metric scale coefficients, and the direction cosines from the computational coordinates to the Cartesian coordinates can be determined using the relations given in Ref. 5. In addition it is noted that since the turbine blade surface is only known as numerical data, the surface spline analysis of McCartin (Ref. 6) and Spath (Ref. 7) is used to
interpolate points on the surface and calculate first and second derivatives of the surface. Details of this geometric analysis are given by Anderson (Ref. 1).

Surface Euler Analysis

The three dimensional boundary layer equations require the boundary layer edge conditions, which include the two free stream velocity components, their derivatives, and the free stream temperature, as boundary conditions over the whole computational domain. These may be obtained directly from experimental data, however, in practice it is very expensive to survey an entire three dimensional flow field. These conditions may also be obtained from a solution of the Euler equations. However, since the generation of the passage vortex is viscous in nature, the Euler solutions may not provide good edge conditions for the crossflow without special treatment. A third method is to obtain the edge conditions from the experimental pressure distribution by integrating the surface Euler equations. These surface Euler equations are obtained from the boundary layer equations in the limit as the normal coordinate approaches the edge of the boundary layer so that normal derivatives of all variables go to zero. Since the pressure distribution is known, only two momentum equations and an energy equation are required for a complete solution of all the dependent variables. These surface Euler equations are hyperbolic in character and may be solved using the same computational (X1,X2) grid, finite difference module, and inflow edge conditions as the three-dimensional boundary layer analysis. A detailed presentation of this analysis are given by Anderson (Ref. 1).
3-D Boundary Layer Analysis

The three dimensional boundary layer analysis used in this computer code is that developed by Vatsa (Refs. 2 and 3). This analysis solves the finite difference form of the compressible three-dimensional boundary layer equations (including the energy equation) in a non-orthogonal surface coordinate system which includes Coriolis forces produced by coordinate rotation. These equations are solved in Levy-Lees variables using an efficient, implicit, fully coupled finite difference procedure. These boundary layer equations are hyperbolic in character and require, besides the edge boundary conditions, the inflow conditions along the computational boundaries where flow enters the domain. These inflow conditions are estimated by solving the 3-DBL equations along the inflow boundary using an assumption of either local similarity or plane of symmetry which reduces the equations to two dimensional differential equations with edge conditions provided by the boundary layer edge analysis.

Operation of Computer Codes

The description of the input and output of the SETUP code is given in Section 4.0 and a description of the input and output for the BL3D code is given in Section 5.0. Sample inputs for both codes are given in the respective sections. Since the BL3D code requires the surface coordinate data and the boundary layer edge conditions, the SETUP code must be run first. The linking of these two codes through data files is shown in Fig. 2. Note on Fig. 2 that output Units 8, 9, and 10 for the SETUP code correspond to the input Units 10, 11, and 12 respectively for the BL3D code. Output Units 13, 15, and 16 are
special output files for CALCOMP or TEKTRONIX plot packages. Since plotting
codes are machine dependent, they are not available on the NASA Lewis version of
these codes. Unit 20 for the BL3D code serves as both an input and output file.
BLADE DESCRIPTION KNOWN 
Y₁, Y₂, Y₃ CARTESIAN COORDINATES

FLOW CONDITIONS KNOWN 
WALL PRESSURE Cᵢ (Y₁, Y₂, Y₃)

GEOMETRY ANALYSIS

SURFACE EULER ANALYSIS

Y₁, Y₂, Y₃ CARTESIAN COORDINATES 
g₁, h, METRIC DATA 
KNOWN AS A FUNCTION OF 
X₁, X₂, X₃ SURFACE COORDINATES

EDGE VELOCITIES 
U₁, U₂ KNOWN AS A FUNCTION OF 
X₁, X₂, X₃ SURFACE COORDINATES

3-D BOUNDARY LAYER ANALYSIS

BOUNDARY LAYER PARAMETERS 
δ*, φ, C₁, S₁ KNOWN 
AS A FUNCTION OF 
Y₁, Y₂, Y₃ CARTESIAN COORDINATES

Fig. 1 Flow Chart of Geometry, Surface Euler and 3-D Boundary Layer Analysis
Fig. 2 Data File Links Between Setup and BL3 D Codes
4.0 OPERATION OF SETUP CODE

4.1 Input Format

The input format is described on the pages which follow. The type and amount of data read by the code is controlled by the input options IOPT1 through IOPT12 and the user should be very careful to be sure that the input data agrees with the input options. In general the input cards are loaded as follows:

Card(s) 0 Title Card
Card(s) 1 Computational Grid Data
Card(s) 2 Computational Boundary Data
Card(s) 3 Coordinate Surface Data
Card(s) 4 Pressure Distribution Data
Card(s) 5 Inflow Conditions Data
Card   6 Print Options
Card(s) 7 Reference Flow Variables
Card(s) 8 Rotor Parameters (load only if IOPT8 = 1)
Card(s) 9 Upstream Flow Conditions (load only if IOPT11 = 1)

In the loading of the input cards, the variable name, column numbers, and description are given. Integer numbers are right adjusted and real numbers may have any number of significant digits.
Card(s) 0 Title Card (load 72 alphanumeric characters)

Card(s) 1 Computational Grid Data

Card   _  la Options (8I10) __________________________________________

IOPT4  1-10  Mesh distribution option
       IOPT4 = 0 Calc. uniform grid
       1 Calc. stretched grid
       2 Read grid points

LPLAST 11-20  No. X1 grid points
KPLAST 21-30  No. X2 grid points

Card   _  lb Stretcing Parameter (F10.0) ___ If IOPT4 = 1 _____________

A  1-10  Stretching parameter

Card(s) 1b Input grid Points __ (8F10.0) __ If IOPT4 = 2 _____________

(X1(LP),LP=1,LPLAST)  X1 grid points
Load LPLAST numbers (8 numbers/card)

(X2(KP),KP=1,KPLAST)  X2 grid points
Load KPLAST numbers (8 numbers/card)

Card(s) 2 Computational Boundary Data

Card   _  2a Options _______ (8I10) ________________________________

IOPT2  1-10  Grid boundary option
       IOPT2 = 0 Cartesian Grid on a plane
       = 1 Skewed grid on a plane
       = 2 1D mapping  Y2=Y2(X1,X2)
       = 3 1D mapping  Y1=Y1(X1,X2)
       = 4 2D mapping

LPLAST 11-20  No. X1 input boundary points
KPLAST 21-30  No. X2 input boundary points
If \( \text{IOPT2} = 0 \):

<table>
<thead>
<tr>
<th>Card</th>
<th>2b Boundary Corners</th>
<th>((5F10.0))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Y1L</td>
<td>1-10</td>
<td>Lower Y1 boundary</td>
</tr>
<tr>
<td>Y1U</td>
<td>11-20</td>
<td>Upper Y1 boundary</td>
</tr>
<tr>
<td>Y2L</td>
<td>21-30</td>
<td>Lower Y2 boundary</td>
</tr>
<tr>
<td>Y2U</td>
<td>31-40</td>
<td>Upper Y2 boundary</td>
</tr>
<tr>
<td>SS10</td>
<td>41-50</td>
<td>Initial arc length on X1</td>
</tr>
</tbody>
</table>

If \( \text{IOPT2} = 1 \):

<table>
<thead>
<tr>
<th>Card</th>
<th>2b Boundary Corners</th>
<th>((4F10.0))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Y100</td>
<td>1-10</td>
<td>Y1(0,0)</td>
</tr>
<tr>
<td>Y101</td>
<td>11-20</td>
<td>Y1(0,1)</td>
</tr>
<tr>
<td>Y111</td>
<td>21-30</td>
<td>Y1(1,1)</td>
</tr>
<tr>
<td>Y110</td>
<td>31-40</td>
<td>Y1(1,0)</td>
</tr>
</tbody>
</table>

If \( \text{IOPT2} = 1 \):

<table>
<thead>
<tr>
<th>Card</th>
<th>2c Boundary Corners</th>
<th>((4F10.0))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Y200</td>
<td>1-10</td>
<td>Y2(0,0)</td>
</tr>
<tr>
<td>Y201</td>
<td>11-20</td>
<td>Y2(0,1)</td>
</tr>
<tr>
<td>Y211</td>
<td>21-30</td>
<td>Y2(1,1)</td>
</tr>
<tr>
<td>Y210</td>
<td>31-40</td>
<td>Y2(1,0)</td>
</tr>
</tbody>
</table>

If \( \text{IOPT2} = 2 \):

<table>
<thead>
<tr>
<th>Card</th>
<th>2b Y1 Boundary Points</th>
<th>((2F10.0))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Y1L</td>
<td>1-10</td>
<td>Lower Y1 boundary</td>
</tr>
<tr>
<td>Y1U</td>
<td>11-20</td>
<td>Upper Y1 boundary</td>
</tr>
</tbody>
</table>
Card(s) 2c  Side 2 and Side 4  (8F10.0)  If(IOPT2 = 2)
(Y1X11(LB),LB=1,LBLAST)  Y1 boundary points side 2 (X2 = 1)
(Y2X11(LB),LB=1,LBLAST)  Y2 boundary points side 2 (X2 = 1)
(Y1X10(LB),LB=1,LBLAST)  Y1 boundary points side 4 (X2 = 0)
(Y2X10(LB),LB=1,LBLAST)  Y2 boundary points side 4 (X2 = 0)

Load 4*LBLAST numbers (8 numbers/card)

Card 2b  Y2 Boundary Points  (2F10.0)  If (IOPT2 = 3)
Y1L  1-10  Lower Y1 boundary
Y1U  11-20  Upper Y1 boundary

Card(s) 2c  Side 1 and Side 3  (8F10.0)  If(IOPT2 = 3)
(Y10X2(KB),KB=1,KBLAST)  Y1 boundary points side 1 (X1 = 0)
(Y20X2(KB),KB=1,KBLAST)  Y2 boundary points side 1 (X1 = 0)
(Y11X2(KB),KB=1,KBLAST)  Y1 boundary points side 3 (X1 = 1)
(Y21X2(KB),KB=1,KBLAST)  Y2 boundary points side 3 (X1 = 1)

Load 4*KBLAST numbers (8 numbers/card)

Card(s) 2b Four Sides  (8F10.0)  If IOPT2 = 4
(Y10X2(KB),KB=1,KBLAST)  Y1 boundary points side 1 (X1 = 0)
(Y20X2(KB),KB=1,KBLAST)  Y2 boundary points side 1 (X1 = 0)
(Y1X11(LB),LB=1,LBLAST)  Y1 boundary points side 2 (X2 = 1)
(Y2X11(LB),LB=1,LBLAST)  Y2 boundary points side 2 (X2 = 1)
(Y11X2(KB),KB=1,KBLAST)  Y1 boundary points side 3 (X1 = 1)
(Y21X2(KB),KB=1,KBLAST)  Y2 boundary points side 3 (X1 = 1)
(Y1X1φ(LB),LB=1,LBLAST)  Y1 boundary points side 4 (X2 = 0)
(Y2X1φ(LB),LB=1,LBLAST)  Y2 boundary points side 4 (X2 = 0)

Load 4*(LBLAST + KPLAST) numbers (8 numbers/card)
Card(s) 3 Coordinate Surface Data

Card_ _ 3a_Options_ _ _ _ _ _ _ _ (3I10)

IOPT1 1-10 Surface geometry option
IOPT1 = 0 plain surface
= 1 Y3 = Y3(Y1)
= 2 Y3 = Y3(Y2)
= 3 Y3 = Y3(Y1,Y2)

LSLAST 11-20 No. input Y1 points

KSLAST 21-30 No. input Y2 points

Card(s) 3b_Surface_Coordinates_ _ (8F10.0)_ _ If IOPT1 = 1
(Y1(LS),LS=1,LSLAST) Y1 coordinate
(Y3(LS),LS=1,LSLAST) Y3 coordinate

Load 2*LSLAST numbers (8 numbers/card)

Card(s) 3b_Surface_Coordinates_ _ (8F10.0)_ _ If IOPT1 = 2
(Y2(KS),KS=1,KSLAST) Y2 coordinate
(Y3(KS),KS=1,KSLAST) Y3 coordinate

Load 2*KSLAST numbers (8 numbers/card)

Card(s) 3b_Surface_Coordinates_ _ (8F10.0)_ _ If IOPT1 = 3
(Y1(LS),LS=1,LSLAST) Y1 coordinate

Load LSLAST numbers (8 numbers/card)

(Y2(KS),KS=1,KSLAST) Y2 coordinate

Load KSLAST numbers (8 numbers/card)

((Y3(LS,KS),LS=1,LSLAST),KS=1,KSLAST) Y3 coordinate

Load LSLAST*KSLAST numbers (8 numbers/card)
CARD(S) 4 Pressure Distribution Data

Card  4a Options  _______ (5I10)

IOPT3  1-10 Pressure data option
       IOPT3 = 0 No pressure data
       = 1 CP=CP(X1,X2)
       = 2 CP=CP(Y1,Y2)
       = 3 CP=CP(Y1,X2)
       = 4 CP=CP(X1,Y2)

LILAST  11-20 No. X1 or Y1 input points

KILAST  21-30 No. X2 or Y2 input points

IOPT7  31-40 SMOOTH CP DATA IOPT7 times

IOPT8  41-50 Rotor/Stator option
       IOPT8 = 0 Stator
       = 1 Rotor load data hub to tip
       =-1 Rotor load data tip to hub

Card(s) 4b Coordinate Data  ______ (8F10.0)

(Y1I(LD),LD=1,LILAST) Y1 Coordinate

Load LILAST numbers (8 numbers/card)

(Y2I(KD),KD=1,KILAST) Y2 Coordinate

Load KILAST numbers (8 numbers/card)

((Y3I(LD,KD),LD=1,LILAST),KD=1,KDLAST) CP (Y1,Y2)

Load LILAST*KILAST numbers (8 numbers/card)
### Card(s) 5 Inflow Conditions Data

<table>
<thead>
<tr>
<th>Card</th>
<th>Options (3I10)</th>
<th>Inflow option</th>
</tr>
</thead>
</table>
| IOPT5 | 1-10 | IOPT5 = 0 U1E = SQRT(1-CP) : U2E = 0.0  
|       |     | IOPT5 > 0 integrate bl edge equations  
|       |     | = 1 U2(0,X2) = 0.0 : U2(X1,0) = 0.0  
|       |     | = 2 U2(0,X2) = 0.0 : U2(X1,0) Input  
|       |     | = 3 U2(0,X2) Input : U2(X1,0) = 0.0  
|       |     | = 4 U2(0,X2) Input : U2(X1,0) Input |

<table>
<thead>
<tr>
<th>LULAST</th>
<th>11-20</th>
<th>No. X1 input points</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th>KULAST</th>
<th>21-30</th>
<th>No. X2 input points</th>
</tr>
</thead>
</table>

**Card(s) 5b X2=0 inflow boundary (8F10.0)**  
*If IOPT5 = 2*

(Y1IU(LP),LP=1,LULAST)  
Y1 coordinate  
Load LULAST numbers (8 numbers/card)

(U2X1(LP),LP=1,LULAST)  
U2(Y1)  
Load LULAST numbers (8 numbers/card)

**Card(s) 5b X1=0 inflow boundary (8F10.0)**  
*If IOPT5 = 3*

(Y12U(KP),KP=1,KULAST)  
Y2 coordinate  
Load KULAST numbers (8 numbers/card)

(U2X2(KP),KP=1,KULAST)  
U2(Y2)  
Load KULAST numbers (8 numbers/card)
Card(s) 5b X2=0 inflow boundary (8F10.0) If IOPT5 = 4
(YIU(LP),LP=1,LULAST) Y1 coordinate

Load LULAST numbers (8 numbers/card)

(U2X1(LP),LP=1,LULAST) U2(Y1)

Load LULAST numbers (8 numbers/card)

(Y1U(KP),KP=1,KULAST) Y2 coordinate

Load KULAST numbers (8 numbers/card)

(U2X2(KP),KP=1,KULAST) U2(Y2) 8 numbers/card)

Load KULAST numbers (8 numbers/card)

<table>
<thead>
<tr>
<th>Card 6 Print Options</th>
<th>(5110)</th>
</tr>
</thead>
<tbody>
<tr>
<td>IOPT6</td>
<td>1-10</td>
</tr>
<tr>
<td>IOPT9</td>
<td>11-20</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>IOPT10</td>
<td>21-30</td>
</tr>
<tr>
<td>IOPT11</td>
<td>31-40</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>IOPT12</td>
<td>41-50</td>
</tr>
</tbody>
</table>
### Card(s) 7  Reference Flow Variables  (6F10.0)

<table>
<thead>
<tr>
<th>Card</th>
<th>Reference Flow Variables</th>
</tr>
</thead>
<tbody>
<tr>
<td>PINFI</td>
<td>1-10 Static pressure (psf)</td>
</tr>
<tr>
<td>TINFI</td>
<td>11-20 Static temperature (deg. R.)</td>
</tr>
<tr>
<td>UINFI</td>
<td>21-30 Velocity (ft/sec)</td>
</tr>
<tr>
<td>BET11</td>
<td>31-40 Not used</td>
</tr>
<tr>
<td>XLREF</td>
<td>41-50 Length (ft)</td>
</tr>
<tr>
<td>DHINF</td>
<td>51-60 Not used</td>
</tr>
</tbody>
</table>

### Card(s) 8  Rotor Parameters  (Load only if IOPT8 = 1)

#### Card 8a  Rotation Vector  (4F10.0)

<table>
<thead>
<tr>
<th>Card</th>
<th>Rotation Vector</th>
</tr>
</thead>
<tbody>
<tr>
<td>VBTI</td>
<td>1-10 Rotor tip speed (ft/sec)</td>
</tr>
<tr>
<td>GO1</td>
<td>11-20 Components of omega</td>
</tr>
<tr>
<td>GO2</td>
<td>21-30 in the Y1, Y2, Y3</td>
</tr>
<tr>
<td>GO3</td>
<td>31-40 directions</td>
</tr>
</tbody>
</table>

#### Card 8b  Rotor Parameters  (6F10.0)

<table>
<thead>
<tr>
<th>Card</th>
<th>Rotor Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>RADHI</td>
<td>1-10 Hub radius</td>
</tr>
<tr>
<td>RADTI</td>
<td>11-20 Tip radius</td>
</tr>
<tr>
<td>YRADHI</td>
<td>21-30 Hub Y2 coordinate</td>
</tr>
<tr>
<td>YRADTI</td>
<td>31-40 Tip Y2 coordinate</td>
</tr>
<tr>
<td>GAPI</td>
<td>41-50 Mid span gap</td>
</tr>
<tr>
<td>DELCP</td>
<td>51-60 Not used</td>
</tr>
</tbody>
</table>
Card(s) 9  Upstream Flow Conditions (load only if IOPT11 = 1)

<table>
<thead>
<tr>
<th>Y2RI(K) 1-10</th>
<th>Spanwise coordinate (Y2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PTAI(K) 11-20</td>
<td>Inlet absolute total pressure (psf)</td>
</tr>
<tr>
<td>TTAI(K) 21-30</td>
<td>Inlet absolute total temperature (deg. R.)</td>
</tr>
<tr>
<td>UZAI(K) 31-40</td>
<td>Inlet axial velocity (ft/sec)</td>
</tr>
<tr>
<td>BTRI(K) 41-50</td>
<td>Inlet flow angle (deg.)</td>
</tr>
</tbody>
</table>

Load KILAST cards
4.2 Output Format

The output for the SETUP code echoes the input data and also lists certain additional calculated data which can be used for input to the BL3D code. The output description is given by headings on the following pages.

Unit 12 Output (file name OUTPUT.DAT)

Title Card

72 alphanumeric characters

Input Options

All input options are listed in order with its value and meaning beside it.

Independent Variables

The input calculation grid points X1(L) and X2(K) are listed as input. If IOPT4 = 0 or 1, the calculated grid points are listed.

Computational Boundaries

The input computational boundaries are listed by sides where:

- Side 1  Y1(0.0,X2) , Y2(0.0,X2)
- Side 2  Y1(X1,1.0) , Y2(X1,1.0)
- Side 3  Y1(1.0,X2) , Y2(1.0,X2)
- Side 4  Y1(X1,0.0) , Y2(X1,0.0)

are parametric pairs of points describing the boundaries. If IOPT2 < 4, the boundaries are calculated and then listed.
Coordinate Surface Data

The Cartesian coordinates of the computational surface are listed next. It is assumed that the independent variable Y1 is only a function of L and the independent variable Y2 is only a function of K. These arrays are listed first. Next Y3(Y1,Y2) is listed. For IOPT1 = 0, the computational surface is a plane surface and Y3 is not listed. For IOPT1 = 1 or 2, the surface is a two dimensional (developable) surface Y3=Y3(Y1) or Y3=Y3(Y2). With these options only Y1 and Y3 are listed or Y2 and Y3.

Pressure Distribution Data

The independent variables are listed first. Again it is assumed that Y1 or X1 is only a function of L and Y2 or X2 is only a function of K depending upon the input option IOPT3. The pressure coefficient data is listed next.

Inflow Conditions (If IOPT5 > 1)

The independent variables Y1 or X1 are listed first and followed by the inflow velocities U2(Y1) or U2(X1). Then the independent variable Y2 or X2 is listed followed by U2(Y2) or U2(X2).

Flow Parameters

The following input parameters are listed:

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Description</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>PINFI</td>
<td>$p_\infty$</td>
<td>Reference static pressure</td>
<td>(psf)</td>
</tr>
<tr>
<td>TINFI</td>
<td>$t_\infty$</td>
<td>Reference static temperature</td>
<td>(deg. R.)</td>
</tr>
<tr>
<td>UINFI</td>
<td>$u_\infty$</td>
<td>Reference velocity</td>
<td>(ft/sec)</td>
</tr>
<tr>
<td>BETI1</td>
<td>$\beta_{100}$</td>
<td>Reference inlet flow angle</td>
<td>atan(UZA/UPR) (deg.)</td>
</tr>
</tbody>
</table>
Reference length \((\text{ft})\)

Not used

Rotor tip speed \((\text{ft/sec})\)

Direction cosines of rotation vector with respect to the Cartesian coordinates

Hub Radius

Tip Radius

Hub Y2 coordinate

Tip Y2 coordinate

Reference gap

Not used

The following calculated parameters are listed next. These quantities are nondimensionalized in the same manner as the input to the BL3D code and may be used as input to the BL3D code. Note that rotor parameters are only listed if \(\text{IOPT8} > 0\).

Reference freestream static pressure

Reference static temperature

Reference freestream static temperature

Reference freestream static enthalpy

Not used

Reference freestream Mach number

Magnitude of rotation vector
OMEGA1
OMEGA2
OMEGA3

VBINF \( V_{B\infty} \) Reference rotor speed
UPINF \( U_{\phi\infty} \) Reference inlet tangential velocity
ALP11 \( a_{100} \) 90. - BET11
HTABSF \( a_{T\infty} \) Reference absolute total enthalpy
PTABSF \( \bar{a}_{T\infty} \) Reference absolute total pressure

Nonuniform Inflow Conditions (If IOPT8 = 1)

The following inflow conditions are input and listed.

Y2RI(K) \( Y_2 \) Y2 coordinate
PTAI(K) \( \bar{p}_T \) Inlet absolute total pressure \((\text{psf})\)
TTAI(K) \( \bar{T}_T \) Inlet absolute total temperature \((\text{deg. R})\)
UZAI(K) \( U_Z \) Inlet absolute axial velocity \((\text{ft/sec})\)
BTRI(K) \( \beta_1 \) Inlet relative flow angle \(\text{atan}(UZA/UPR)\) \((\text{deg.})\)

Rotor Inlet Conditions (if IOPT8 = 1)

The following variables are calculated and listed.

Y2RI(K) \( Y_2 \) Y2 coordinate
PT/PINF \( P_T/P_{T\infty} \) Absolute total pressure ratio
TT/TINF \( T_T/T_{T\infty} \) Absolute total temperature ratio
P/PINF \( P/P_{\infty} \) Static pressure ratio
T/TINF \( T/T_{\infty} \) Static temperature ratio
Boundary Layer Edge Conditions

The boundary layer coordinates and edge conditions are calculated on a LPLAST*KPLAST grid. Depending on the input option IOPT6, the following quantities are listed at grid points which are multiples of IOPT6.

\[ L, K \]
\[ X_1P, X_2P \]
\[ Y_1P, Y_2P \]
\[ CP \]
\[ U_1E, U_2E \]
\[ DU1EDX1 \]
\[ DU1EDX2 \]
\[ DU2EDX1 \]
\[ DU2EDX2 \]
The output on unit 11 provides a detailed short listing of all L stations for a given K = KPT station. This output is very useful for aligning a computational coordinate with the corresponding Cartesian coordinate and the arc length along the coordinate surface. It also lists the coordinates of a calculated streamline starting at the point (L = 1, K = KPT). The pair of points (SlP, SLS) form a parametric curve of the streamline on the surface starting at the point (L = 1, K = KPT). The following variables are currently listed on the file.

- **L**: Coordinate point
- **X1P**: Computational coordinate
- **Y1P**: Cartesian coordinate
- **S1P**: Arc length along X1 coordinate
- **Y3P**: Cartesian coordinate of surface
- **CP**: Static pressure coefficient
- **U1E**: Edge velocity components
- **U2E**: Edge velocity components
- **OMEGA3**: Vorticity component normal to surface
- **SLS**: Spanwise arc length of streamline
- **ALPE**: Flow angle at streamline

Unit 11 Output (file name CORSCL.DAT)
4.3 Output Data Files

The output data files are written on units 8, 9, and 10. These data files contain some of the data which is required as input by the BL3D code. A detailed listing of the files are given below.

**Unit 8 Metric Data (7E14.7)**

<table>
<thead>
<tr>
<th>HH1</th>
<th>H1</th>
<th>Metric scale coefficient for X1</th>
</tr>
</thead>
<tbody>
<tr>
<td>HH2</td>
<td>H2</td>
<td>Metric scale coefficient for X2</td>
</tr>
<tr>
<td>DH11</td>
<td>( \partial H_1 / \partial X_1 )</td>
<td>( D(HH1)/DX1 )</td>
</tr>
<tr>
<td>DH12</td>
<td>( \partial H_1 / \partial X_2 )</td>
<td>( D(HH1)/DX2 )</td>
</tr>
<tr>
<td>DH21</td>
<td>( \partial H_2 / \partial X_1 )</td>
<td>( D(HH2)/DX1 )</td>
</tr>
<tr>
<td>DH22</td>
<td>( \partial H_2 / \partial X_2 )</td>
<td>( D(HH2)/DX2 )</td>
</tr>
<tr>
<td>GL12</td>
<td>G12</td>
<td>Covariant metric tensor component</td>
</tr>
<tr>
<td>DG</td>
<td>(</td>
<td>G</td>
</tr>
<tr>
<td>DG121</td>
<td>( \partial G_{12} / \partial X_1 )</td>
<td>( D(GL12)/DX1 )</td>
</tr>
<tr>
<td>DG122</td>
<td>( \partial G_{12} / \partial X_2 )</td>
<td>( D(GL12)/DX2 )</td>
</tr>
<tr>
<td>RAD</td>
<td>R</td>
<td>Radius</td>
</tr>
<tr>
<td>DRAD1</td>
<td>( \partial R / \partial X_1 )</td>
<td>( D(R)/DX1 )</td>
</tr>
<tr>
<td>OMEGA3</td>
<td>( \partial \Omega / \partial X_2 )</td>
<td>( D(R)/DX2 )</td>
</tr>
</tbody>
</table>

**Unit 9 Boundary Layer Edge Conditions (714.7)**

<table>
<thead>
<tr>
<th>U1E</th>
<th>U(_1)e</th>
<th>X1 edge velocity</th>
</tr>
</thead>
<tbody>
<tr>
<td>U2E</td>
<td>U(_2)e</td>
<td>X2 edge velocity</td>
</tr>
<tr>
<td>PP</td>
<td>P</td>
<td>Static pressure</td>
</tr>
<tr>
<td>DU1DX2</td>
<td>( \partial U_1 / \partial X_2 )</td>
<td>( D(U1E)/DX2 )</td>
</tr>
</tbody>
</table>
DU2DX2 \( \frac{\partial U_2}{\partial x_2} \) \( \frac{D(U_2E)}{DX_2} \)
DU1DX1 \( \frac{\partial U_1}{\partial x_1} \) \( \frac{D(U_1E)}{DX_1} \)
DU2DX1 \( \frac{\partial U_2}{\partial x_1} \) \( \frac{D(U_2E)}{DX_1} \)
HR 1 Rothalpy

Unit 10 Transformation Variables (7E14.7)

Y1 or S1  X1 coordinate or X1 arc length
Y2 or S2  X2 coordinate or X2 arc length

\(((\Gamma(I,J), J=1,3), I=1,3)\) Direction cosines

Note: If IOPT9 = 0 Y1 and Y2 are written
If IOPT9 = 1 S1 and S2 are written
4.4 Diagnostics

A number of checks are made during the course of the calculation. If a minor error occurs, a DIAGNOSTIC message is printed and the calculation is continued. If a serious error occurs, a DIAGNOSTIC message is printed and the calculation stops. A description of the DIAGNOSTIC message is given below. These messages are always of the form

** DIAGNOSTIC NO. XX **

where the number XX refers to one of the errors listed below.

1) **ERROR** X PT DOES NOT CORRESPOND TO GRID LINE or **ERROR** Y PT DOES NOT CORRESPOND TO GRID LINE

This error is detected in Subroutine INTR1D and occurs whenever the computational boundary lies outside the boundaries of the input surface coordinates or outside the boundaries of the input pressure distribution. This is not a fatal error and the calculation continues by extrapolation of the data. However, the input data should be examined to be certain it is correct and the computational boundaries should be inside the input data boundaries.

2) **ERROR** 1-D INTERPOLATION ROUTINE CALLED HOWEVER NEITHER X NOR Y LIE ON A GRIDLINE

This error ordinarily should not occur, however, due to round off error, an IF test may fail and the error message occurs. This is not a fatal error and the calculation continues.
3) CONVERGENCE DID NOT OCCUR

This error is detected in subroutine UITER and occurs whenever convergence of the successive substitution iteration did not occur or if only imaginary solutions exist. This is a fatal error and the calculation stops. Check to see if the input pressure distribution is correct and that the input inflow conditions are correct. One may also smooth the input data using the IOPT7 option.
4.5 Sample Input

A sample input to the SETUP code is given below card by card as described in Section 4.1. To assist the user in setting up a new case comments are inserted between blocks of data in lower case letters. These comments of course should not be on the input cards.

<table>
<thead>
<tr>
<th>Card(s) 0 Title Card</th>
</tr>
</thead>
<tbody>
<tr>
<td>LSR76 PRESSURE SURFACE ROTATING RIG (LEADING EDGE START)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Card(s) 1 Computational Grid Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 40 40 .48</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Card(s) 2 Computational Boundary Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 21 21 .01601 0.94699 0.01893 0.92729</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Card(s) 3 Coordinate Surface Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 50 7</td>
</tr>
<tr>
<td>0.01000 0.02000 0.03000 0.04000 0.05000 0.06000 0.07000 0.08000</td>
</tr>
<tr>
<td>0.09000 0.10000 0.12500 0.15000 0.17500 0.20000 0.22500 0.25000</td>
</tr>
<tr>
<td>0.27500 0.30000 0.32500 0.35000 0.37500 0.40000 0.42500 0.45000</td>
</tr>
<tr>
<td>0.47500 0.50000 0.52500 0.55000 0.57500 0.60000 0.62500 0.65000</td>
</tr>
<tr>
<td>0.67500 0.70000 0.72500 0.75000 0.77500 0.80000 0.82500 0.85000</td>
</tr>
<tr>
<td>0.87500 0.90000 0.91000 0.92000 0.93000 0.94000 0.95000 0.96000</td>
</tr>
<tr>
<td>0.97000 0.98000</td>
</tr>
<tr>
<td>0.01892 0.11828 0.23656 0.47311 0.70967 0.82795 0.92730</td>
</tr>
<tr>
<td>-.42037 -.40957 -.40300 -.39908 -.39723 -.39723 -.39909 -.40302</td>
</tr>
<tr>
<td>-.40933 -.41594 -.43076 -.44336 -.45392 -.46258 -.46945 -.47461</td>
</tr>
<tr>
<td>-.47813 -.48006 -.48045 -.47932 -.47670 -.47261 -.46705 -.46003</td>
</tr>
<tr>
<td>-.45157 -.44165 -.43026 -.41739 -.40301 -.38708 -.36958 -.35047</td>
</tr>
<tr>
<td>-.32973 -.30730 -.28313 -.25717 -.22931 -.19947 -.16755 -.13341</td>
</tr>
<tr>
<td>-.09689 -.05780 -.04139 -.02451 -.00716 .01069 .02542 .03137</td>
</tr>
<tr>
<td>.03310 .03140</td>
</tr>
<tr>
<td>-.43945 -.42865 -.42209 -.41817 -.41632 -.41633 -.41820 -.42213</td>
</tr>
<tr>
<td>-.42841 -.43489 -.44939 -.46164 -.47185 -.48015 -.48667 -.49147</td>
</tr>
<tr>
<td>-.49463 -.49620 -.49620 -.49465 -.49158 -.48697 -.48083 -.47315</td>
</tr>
<tr>
<td>-.46393 -.45318 -.44085 -.42688 -.41118 -.39373 -.37451 -.35352</td>
</tr>
<tr>
<td>-.33075 -.30621 -.27988 -.25175 -.22177 -.18991 -.15611 -.12028</td>
</tr>
<tr>
<td>-.08234 -.04217 -.02543 -.00831 .00920 .02713 .04187 .04782</td>
</tr>
<tr>
<td>.04955 .04785</td>
</tr>
<tr>
<td>-.46218 -.45138 -.44483 -.44091 -.43906 -.43907 -.44094 -.44487</td>
</tr>
<tr>
<td>Card(s) 3</td>
</tr>
<tr>
<td>----------</td>
</tr>
<tr>
<td></td>
</tr>
<tr>
<td>-0.5108</td>
</tr>
<tr>
<td>-0.5138</td>
</tr>
<tr>
<td>-0.47754</td>
</tr>
<tr>
<td>-0.32990</td>
</tr>
<tr>
<td>-0.06470</td>
</tr>
<tr>
<td>-0.50768</td>
</tr>
<tr>
<td>-0.49628</td>
</tr>
<tr>
<td>-0.55078</td>
</tr>
<tr>
<td>-0.50108</td>
</tr>
<tr>
<td>-0.32148</td>
</tr>
<tr>
<td>-0.02840</td>
</tr>
<tr>
<td>0.10830</td>
</tr>
<tr>
<td>-0.55319</td>
</tr>
<tr>
<td>-0.54132</td>
</tr>
<tr>
<td>-0.58597</td>
</tr>
<tr>
<td>-0.52026</td>
</tr>
<tr>
<td>-0.30503</td>
</tr>
<tr>
<td>0.00913</td>
</tr>
<tr>
<td>0.14746</td>
</tr>
<tr>
<td>-0.57592</td>
</tr>
<tr>
<td>-0.56381</td>
</tr>
<tr>
<td>-0.60322</td>
</tr>
<tr>
<td>-0.52898</td>
</tr>
<tr>
<td>-0.29522</td>
</tr>
<tr>
<td>0.02813</td>
</tr>
<tr>
<td>0.16705</td>
</tr>
<tr>
<td>-0.59501</td>
</tr>
<tr>
<td>-0.58270</td>
</tr>
<tr>
<td>-0.61768</td>
</tr>
<tr>
<td>-0.53625</td>
</tr>
<tr>
<td>-0.28685</td>
</tr>
<tr>
<td>0.04412</td>
</tr>
<tr>
<td>0.18350</td>
</tr>
</tbody>
</table>
Card(s) 4 Pressure Distribution Data

<table>
<thead>
<tr>
<th></th>
<th>2</th>
<th>10</th>
<th>7</th>
<th>4</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0.01600</td>
<td>0.05600</td>
<td>0.09100</td>
<td>0.23800</td>
<td>0.39300</td>
</tr>
<tr>
<td></td>
<td>0.86200</td>
<td>0.94700</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>0.01892</td>
<td>0.11828</td>
<td>0.23656</td>
<td>0.47311</td>
<td>0.70967</td>
</tr>
<tr>
<td></td>
<td>0.34170</td>
<td>0.30740</td>
<td>0.25390</td>
<td>0.08700</td>
<td>0.18180</td>
</tr>
<tr>
<td></td>
<td>0.10400</td>
<td>0.15350</td>
<td>0.33820</td>
<td>0.48250</td>
<td>0.57320</td>
</tr>
<tr>
<td></td>
<td>0.10250</td>
<td>0.12500</td>
<td>0.11780</td>
<td>0.34470</td>
<td>0.46380</td>
</tr>
<tr>
<td></td>
<td>0.14290</td>
<td>0.22310</td>
<td>0.03990</td>
<td>0.44920</td>
<td>0.55130</td>
</tr>
<tr>
<td></td>
<td>0.15000</td>
<td>0.22800</td>
<td>0.31720</td>
<td>0.45170</td>
<td>0.54970</td>
</tr>
<tr>
<td></td>
<td>-0.12850</td>
<td>-0.11320</td>
<td>-0.11840</td>
<td>0.03430</td>
<td>0.10320</td>
</tr>
<tr>
<td></td>
<td>-0.56290</td>
<td>-0.53210</td>
<td>-0.47050</td>
<td>-0.43250</td>
<td>-0.39840</td>
</tr>
<tr>
<td></td>
<td>-1.17390</td>
<td>-1.16500</td>
<td>-1.13420</td>
<td>-1.10830</td>
<td>-1.10750</td>
</tr>
</tbody>
</table>

Card(s) 5 Inflow Conditions Data

<table>
<thead>
<tr>
<th></th>
<th>4</th>
<th>6</th>
<th>7</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0.0000</td>
<td>0.2819</td>
<td>0.4950</td>
</tr>
<tr>
<td></td>
<td>0.1000</td>
<td>0.1000</td>
<td>0.1000</td>
</tr>
<tr>
<td></td>
<td>0.0200</td>
<td>0.1182</td>
<td>0.2366</td>
</tr>
<tr>
<td></td>
<td>0.1000</td>
<td>0.3500</td>
<td>0.4500</td>
</tr>
</tbody>
</table>

Card 6 Print Options

Card(s) 7 Reference Flow Variables

<table>
<thead>
<tr>
<th></th>
<th>4</th>
<th>0</th>
<th>1</th>
<th>1</th>
<th>31</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>2074.976</td>
<td>516.035</td>
<td>107.314</td>
<td>44.600</td>
<td>0.52840</td>
</tr>
</tbody>
</table>

Card(s) 8 Rotor Parameters (load only if IOPT8 = 1)

<table>
<thead>
<tr>
<th></th>
<th>107.338</th>
<th>-1.00000</th>
<th>0.00000</th>
<th>0.00000</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>3.8039</td>
<td>4.7158</td>
<td>0.01829</td>
<td>0.92733</td>
</tr>
</tbody>
</table>

Card(s) 9 Upstream Flow Conditions (load only if IOPT11 = 1)

<table>
<thead>
<tr>
<th></th>
<th>0.0200</th>
<th>2117.000</th>
<th>519.000</th>
<th>75.351</th>
<th>40.000</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>0.1182</td>
<td>2117.000</td>
<td>519.000</td>
<td>75.351</td>
<td>40.000</td>
</tr>
<tr>
<td></td>
<td>0.2366</td>
<td>2117.000</td>
<td>519.000</td>
<td>75.351</td>
<td>39.000</td>
</tr>
<tr>
<td></td>
<td>0.4731</td>
<td>2117.000</td>
<td>519.000</td>
<td>75.351</td>
<td>44.600</td>
</tr>
<tr>
<td></td>
<td>0.7097</td>
<td>2117.000</td>
<td>519.000</td>
<td>75.351</td>
<td>42.000</td>
</tr>
<tr>
<td></td>
<td>0.8280</td>
<td>2117.000</td>
<td>519.000</td>
<td>75.351</td>
<td>47.000</td>
</tr>
<tr>
<td></td>
<td>0.9273</td>
<td>2117.000</td>
<td>519.000</td>
<td>75.351</td>
<td>50.000</td>
</tr>
</tbody>
</table>
5.0 OPERATION OF BL3D CODE

5.1 Input Format

The card input format is described on the pages which follow. In addition to the card input, the code also reads input data files contained on units 10, 11,12 which may be set up by the user or may be set up by the SETUP preprocessor code. In the loading of the cards the variable name, column numbers, and description are given. Integer variables are all right adjusted and real variables may have any number of significant figures.

Card 1 Title card (load 72 alphanumeric characters)

Card 2 Option Card (6I2,8X,3F10.0)

IGBAR 1-2 Levy-Lees option (recommended 0)
IGBAR = 0 Laminar Levy-Lees variables
= 1 Turbulent Levy-Lees variables

ITURB 3-4 Turbulence option
ITURB = 0 Laminar flow
= 1 Turbulent/transitional flow

IENRGY 5-6 Wall heat transfer option
IENRGY = 0 Specify wall temperature
= 1 Specify wall heat flux

LINIT 7-8 X1 = 0 inflow boundary
LINIT = 0 Local similarity start
= 1 Incompressible flat plate start
= 2 Incompressible stagnation start
= 3 Input profiles (not Programmed)

KINIT 9-10 X2 = 0 inflow boundary
KINIT = 0 Local similarity start
= 1 Plain of symmetry start
= 2 Input profiles (not programmed)

NITVC 11-12 Max. no. iterations (recommended 20)
R85-956834-1

CONV 21-30 Convergence tolerance (recommended .0001)
AK 31-40 Ratio of adjacent step size (recommended 1.05)
DNI 41-50 Step size at wall (recommended 0.1)

Card 3 Gas Properties (5F10.0)

R 1-10 Gas constant (air 1716.0)
G 11-20 Ratio specific heats (air 1.4)
PR 21-30 Prandtl number (air .72)
PRT 31-40 Turbulent Prandtl number (air .92)
CSTAR 41-50 Sutherland's constant (air 198.6)

Card 4 Flow Conditions (4F10.0)

XMA 1-10 Reference Mach number
TFS 11-20 Reference static temperature (deg. R.)
PFS 21-30 Reference static pressure (psf)
XLREF 31-40 Reference length (ft)

Card 5 Virtual origin/heat flux conditions (4F10.0)

XO 1-10 X1 virtual origin (recommended > .0001)
WO 11-20 X2 virtual origin (recommended .0000)
RHWIN 21-30 Wall temperature ratio (Tw/Tref)
QWSIN 31-40 Wall heat flux (ftlb/ft**2/sec)

Card 6 Transition points (3F10.0)

XT1 1-10 Beginning of transition
XT2 11-20 End of transition
CISO 21-30 Cross flow eddy viscosity parameter
     CISO = 1.0 isotropic turbulence
           = 0.4 nonisotropic turbulence
Card(s) 7  Print output station numbers (1615)

LPRO(L)  Load up to 16 numbers
KPRO(K)  Load up to 16 numbers
KPT  Unit 16 print parameter 1<KPT<1WEND
5.2 Output Format

The output for the BL3D code echoes the input data, lists the computational coordinates, prints certain calculated terms, and prints the calculated solution at selected output (L,K) points. The output description is given on the following pages.

Unit 7 Output (file name OUTPUT)

**Title Card**

72 alphanumeric characters

**Echo Input Data**

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>IE</td>
<td>Maximum number of points in boundary layer normal direction (in X3)</td>
</tr>
<tr>
<td>IWEND</td>
<td>Maximum number of points in spanwise direction (in X2)</td>
</tr>
<tr>
<td>IXEND</td>
<td>Maximum number of points in streamwise direction (in X1)</td>
</tr>
<tr>
<td>KSTOP</td>
<td>Maximum number of spanwise points at which boundary layer calculation is performed</td>
</tr>
<tr>
<td>LSTOP</td>
<td>Maximum number of streamwise points at which boundary layer calculation is performed</td>
</tr>
<tr>
<td>IGBAR = 0</td>
<td>Turbulent Levy-Lees variables are used</td>
</tr>
<tr>
<td>= 1</td>
<td>Laminar Levy-Lees variables are used</td>
</tr>
<tr>
<td>ITURB = 0</td>
<td>Turbulent flow (transitional)</td>
</tr>
<tr>
<td>= 1</td>
<td>Laminar flow</td>
</tr>
<tr>
<td>IENRGY = 0</td>
<td>Heat flux specified at the wall</td>
</tr>
<tr>
<td>= 1</td>
<td>Temperature specified at the wall</td>
</tr>
<tr>
<td>NITCV</td>
<td>Maximum number of iterations permitted at each station</td>
</tr>
</tbody>
</table>
Maximum error permitted in F2N at the wall

Freestream Mach number

Freestream static temperature (degrees Rankine)

Freestream static pressure (psf)

Gas constant (ft**2/sec**2-degree Rankine)

Ratio of specific heats

Prandtl number

Turbulent Prandtl number

Constant in Sutherland's viscosity law (degree Rankine)

Ratio of adjacent step sizes in boundary layer direction

Step size at the wall in boundary layer

Reference length in feet

Beginning of transition in X1 direction

End of transition in X1 direction

Constant used for scaling eddy viscosity in cross flow momentum equation for nonisotropic turbulent flows

Step size array in streamwise direction

Step size array in spanwise direction

X1 location at first streamwise location

X2 location at first spanwise location

Enthalpy ratio at the wall

Heat flux at the wall

Controls print in the streamwise direction
Controls print in the spanwise direction

Initial conditions; option at \( L = 1 \)
- \( \text{LINIT} = 0 \) Local similarity
- \( \text{LINIT} = 1 \) Incompressible flat plate
- \( \text{LINIT} = 2 \) Incompressible stagnation line
- \( \text{LINIT} = 3 \) Input profiles

Initial conditions option at \( K = 1 \)
- \( \text{KINIT} = 0 \) Local similarity
- \( \text{KINIT} = 1 \) Plane of symmetry
- \( \text{KINIT} = 2 \) Input profiles

### Calculated Reference Parameters

- **UFS** \( U_\infty \) Reference freestream velocity (ft/sec)
- **ROFS** \( \rho_\infty \) Reference freestream density (slug/ft**3**)
- **AMUFS** \( \mu_\infty \) Reference freestream viscosity (slug/ft/sec)
- **REFS** \( R_e \infty \) Reference freestream Reynolds number
- **TREF** \( t_{ref} \) Reference temperature (deg. Rankine)
- **AMURF** \( \mu_{ref} \) Reference viscosity (slug/ft/sec)
- **RE** \( R_e \) Reference Reynolds number
- **CPRIME** \( C' \) Normalized Sutherland's constant

### Calculated Local Parameters at point \((L,K)\)

These parameters are referenced to an intrinsic coordinate system composed of the boundary layer edge freestream direction and the cross flow (perpendicular) direction. In addition, certain parameters are referenced to their projections onto the \( Y_3 = 0 \) plane. Parameters in the intrinsic coordinate system are labeled (intr.). Parameters in the Cartesian coordinate system are labeled
(Cart.). Length scales are normalized with respect to the reference length $XLREF$ and velocities are normalized with respect to the reference freestream velocity $UFS$.

$X1/L \quad X1 \quad X1$ coordinate

$X2/L \quad X2 \quad X2$ coordinate

$Y1/L \quad Y1 \quad Y1$ Cartesian coordinate or

$S1/L \quad S1 \quad S1$ arc length distance

$Y2/L \quad Y2 \quad Y2$ Cartesian coordinate or

$S2/L \quad S2 \quad S2$ arc length distance

$Y3/L \quad Y3 \quad Y3$ Cartesian coordinate

$CFS \quad C_{fs} \quad$ Streamwise wall friction coefficient (intr.) $2\tau_s/\left(\rho e U_e^2\right)$

$CFC \quad C_{fc} \quad$ Crossflow wall friction coefficient (intr.) $2\tau_c/\left(\rho e U_e^2\right)$

$QW \quad Q_w \quad$ Wall heat flux

$ST \quad S_T \quad$ Stanton number $\left(Q_w/(T_a-T_w)\right)$

$TWAD/TFS \quad T_a/T_w \quad$ Adiabatic wall temperature ratio

$UTE \quad U_{Te} \quad$ Total freestream velocity

$ALPW \quad \alpha_w \quad$ Limiting streamline flow angle (intr.)

$BET1 \quad \beta_1 \quad$ Characteristic directions (intr.)

$BET2 \quad \beta_2 \quad$

$CP \quad C_p \quad$ Pressure coefficient

$V1E \quad V_{1e} \quad$ V1 velocity component (Cart.)
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>V2E</td>
<td>Y2 velocity component (Cart.)</td>
</tr>
<tr>
<td>BETAE</td>
<td>Boundary layer edge flow direction (Cart.)</td>
</tr>
<tr>
<td>BETAW</td>
<td>Limiting wall streamline direction (Cart.)</td>
</tr>
<tr>
<td>YEDGE</td>
<td>Boundary thickness</td>
</tr>
<tr>
<td>DELS</td>
<td>Streamwise displacement thickness (intr.)</td>
</tr>
<tr>
<td>DELC</td>
<td>Crossflow displacement thickness (intr.)</td>
</tr>
<tr>
<td>DELUS</td>
<td>Streamwise velocity thickness (intr.)</td>
</tr>
<tr>
<td>DELUC</td>
<td>Crossflow velocity thickness (intr.)</td>
</tr>
<tr>
<td>THETSS</td>
<td>Streamwise momentum thickness (intr.)</td>
</tr>
<tr>
<td>THETCC</td>
<td>Crossflow momentum thickness (intr.)</td>
</tr>
<tr>
<td>THETSC</td>
<td>Uc AU_s momentum thickness (intr.)</td>
</tr>
<tr>
<td>THETCS</td>
<td>U_s AU_c momentum thickness (intr.)</td>
</tr>
<tr>
<td>THETHS</td>
<td>Streamwise enthalpy thickness (intr.)</td>
</tr>
<tr>
<td>THETHC</td>
<td>Crosswise enthalpy thickness (intr.)</td>
</tr>
<tr>
<td>THETDS</td>
<td>Streamwise dissipation thickness (intr.)</td>
</tr>
<tr>
<td>THETDC</td>
<td>Crosswise dissipation thickness (intr.)</td>
</tr>
<tr>
<td>U1E</td>
<td>X1 component of edge velocity</td>
</tr>
<tr>
<td>U2E</td>
<td>X2 component of edge velocity</td>
</tr>
<tr>
<td>TW/TFS</td>
<td>Wall temperature ratio</td>
</tr>
<tr>
<td>IEDGE</td>
<td>Index for boundary layer edge</td>
</tr>
</tbody>
</table>
**Calculated profiles at the point \((L,K)\)**

The following variables are referenced to the intrinsic coordinate system and are normalized to the local boundary layer edge conditions.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>ZETA3</td>
<td>(\xi_3)</td>
</tr>
<tr>
<td>X3/L</td>
<td>(X_3)</td>
</tr>
<tr>
<td>US/UTE</td>
<td>(U_S/U_{Te})</td>
</tr>
<tr>
<td>UC/UTE</td>
<td>(U_C/U_{Te})</td>
</tr>
<tr>
<td>UT/UTE</td>
<td>(U_T/U_{Te})</td>
</tr>
<tr>
<td>ALPC</td>
<td>(\alpha_c)</td>
</tr>
<tr>
<td>T/TE</td>
<td>(T/T_e)</td>
</tr>
<tr>
<td>VIS</td>
<td>((\rho \mu)/(\rho_e \mu_e))</td>
</tr>
</tbody>
</table>
5.3 Input/Output Data Files

The input data files are units 10, 11, 12 which are read by the main program MAIN. The output data files are units 13, 15, and 16. Unit 20 serves as both an input and output temporary file. The data on units 10, 11, 12 are written by the SETUP code or the user may setup this data independently. The data on units 13, 15, 16, and 20 are written by subroutine ROUTPT. A detailed description of these files are given below.

Unit 10 (IDRM1) Metric Data

The first set of data on this file is the number of points in the computational mesh. FORMAT(3I5)

IE                  Number of points in the X3 direction
IXEND               (No. of pts.) - 1 in the X1 direction
IWEND               (No. of pts.) - 1 in the X2 direction

The second set of data is IXEND X1 coordinate differences and IWEND X2 coordinate differences. Format(7E14.7)

DXV(L),L=1,IXEND     X1 coordinate difference
DWV(K),K=1,IWEND     X2 coordinate difference

The final set of data consists of the metric data for each mesh point (L,K) having a FORMAT(7E14.7/7E14.7). This data is arranged to be read by a DO K LOOP nested within a DO L LOOP. At each mesh point (L,K) the following data is read.
Unit 11 (IDRM2) Boundary Layer Edge Data

The data on this file consists of the boundary layer edge conditions for each computational point (L,K). This data, like the data above, is read by a DO K LOOP nested in a DO L LOOP. At each mesh point (L,K) the following data is read. FORMAT(7E14.7/1E14.7).

U(K) \( U_{le} \) X1 velocity component
V(K) \( U_{2e} \) X2 velocity component
PP(K) \( P \) Static pressure
DUDW(K) \( \partial U_{le}/\partial X_2 \) D(U1)/DX2
Unit 12 (IDRM3) Direction Cosine Data

The data on this file consists of the direction cosines for each computational point (L,K). This data is read by a DO K LOOP nested in a DO L LOOP. At each mesh point the following data is read. FORMAT(7E14.7/5E14.7).

<table>
<thead>
<tr>
<th>Y1</th>
<th>Y1 Cartesian coordinate or</th>
</tr>
</thead>
<tbody>
<tr>
<td>S1</td>
<td>S1 arc length along X1</td>
</tr>
<tr>
<td>Y2</td>
<td>Y2 Cartesian coordinate or</td>
</tr>
<tr>
<td>S2</td>
<td>S2 arc length along X2</td>
</tr>
<tr>
<td>Y3</td>
<td>Y3 Cartesian coordinate</td>
</tr>
</tbody>
</table>

((GAM(I,J,K),J=1,3),I=1,3) Direction cosines

Unit 13 (IDRM4) Crossection Plotting Data

The following data is output for each mesh point (L,K) by a DO K LOOP nested in a DO L LOOP. FORMAT(2I3,9E12.5).

<table>
<thead>
<tr>
<th>K</th>
<th>X2 index</th>
</tr>
</thead>
<tbody>
<tr>
<td>L</td>
<td>X1 index</td>
</tr>
<tr>
<td>Y1(K)</td>
<td>Y1 Cartesian coordinate or</td>
</tr>
<tr>
<td>S1(K)</td>
<td>S1 arc length</td>
</tr>
<tr>
<td>VCAP</td>
<td>U1e X1 edge velocity</td>
</tr>
<tr>
<td>CVCAP</td>
<td>U2e X2 edge velocity</td>
</tr>
</tbody>
</table>
RP5-956834-1

CP $C_p$ Static pressure coefficient
DELS $\delta_s^*$ Streamwise displacement thickness
DELC $\delta_c^*$ Crossflow displacement thickness
THETSS $\theta_{ss}$ Streamwise momentum thickness
THETCC $\theta_{cc}$ Crossflow momentum thickness
ST $S_T$ Stanton number

**Unit 15 (IDRM5) Contour and Vector Plotting Data**

The following data is output for each mesh point (L,K) by a DO K LOOP nested in a DO L LOOP. FORMAT(2l3,9E12.5)

K X2 index
L X1 index
Y1 $Y_1$ Y1 Cartesian coordinate or
S1 $S_1$ S1 arc length along X1
Y2 $Y_2$ Y2 Cartesian coordinate or
S2 $S_2$ S2 arc length along X2
Y3 $Y_3$ Y3 Cartesian coordinate
CFS $C_{fs}$ Streamwise friction coefficient
CFC $C_{fc}$ Crossflow friction coefficient
U1E $U_{1e}$ Y1 Cartesian component of velocity or
V1E $V_{1e}$ X1 component of velocity
U2E $U_{2e}$ Y2 Cartesian component of velocity or
V2E $V_{2e}$ X2 component of velocity
EPS1W $\varepsilon_{1w}$ Y1 Cartesian component of strain or
F2N(1) $e_{1w}$ X1 component of strain
EPS2W E210 Y2 Cartesian component of strain or
G2N(1) e2w X2 component of strain

Unit 16 (IDRM6) Special Crosssection data

The following data is output for each mesh point (L,KPT) where KPT is an
input parameter. FORMAT(2I3,9E12.5).

K X2 index
L X1 index
Y1 Y1 Y1 Cartesian coordinate or
S1 S1 S1 arc length along X1
CFS Cfs Streamwise friction coefficient
ST St Stanton number
TW Tw Wall temperature
TWAD Ta Adiabatic wall temperature
STE Ste Local Stanton number

Unit 20 (IDRM7) Wall Temperature Data

The following data is output/input for each mesh point (L,K) in a DO K LOOP
nested in a DO L LOOP. If QW = 0, The wall temperature is the adiabatic wall
temperature and is output onto file 20. If QW > 0, the adiabatic wall
temperature is read from file 20. FORMAT(E12.5).

TW,TWAD Ta Adiabatic wall temperature
5.4 Diagnostics

A number of checks are made during the course of the calculation. If a minor error occurs, a DIAGNOSTIC message is printed and the calculation is continued. If a serious error occurs, a DIAGNOSTIC message is printed and the calculation stops. A description of the DIAGNOSTIC messages is given below.

1) NEGATIVE TEMPERATURE DETECTED IN MOLVIS AT K=

where K is the spanwise station where the error is detected. This error is detected in subroutine MOLVIS and indicates that a negative temperature is calculated in MOLVIS. This negative temperature only occurs if the iteration at the (L,K) mesh point does not converge. The usual problem is that negative spanwise velocities occur at this spanwise station producing instabilities. The calculation is continued by indexing L to the next streamwise station.

5.5 Sample Input

A sample input to the BL3D code is given below card by card as described in Sect. 5.1. To assist the user in setting up a new case comments are inserted between blocks of data in lower case letters. These comments of course should not be on the input cards.
Card 1 Title card (load 72 alphanumeric characters)
GAS TURBINE CASCADE - ROTATING PRESSURE SURFACE

Card 2 Option Card (6I2,8X,3F10.0)
1 1 1 0 020 .0001 1.05 0.10

Card 3 Gas Properties (5F10.0)
1716.0 1.4 0.72 0.95 198.6

Card 4 Flow Conditions (4F10.0)
.0985114 519.0 2117.0 0.9233

Card 5 Virtual origin/heat flux conditions (4F10.0)
00.1000 .000 1.0 000.0

Card 6 Transition points (3F10.0)
00.1002 00.1003 1.0

Card(s) 7 Print output station numbers (16I5)
1 5 18 29 39 40
1 10 20 30 40
6.0 DESCRIPTION OF SETUP CODE

6.1 SETUP Main Program

The main program for the SETUP code opens and closes all input and output files and calls the subroutines which execute the primary tasks depending on the input options IOPT1 through IOPT12. An overall view of the SETUP code is shown on the Global Tree Structure Chart shown on the following pages. This tree structure is arranged by tasks and labeled as they appear in the main program SETUP. Column 1 shows the main program which calls the subroutines in column 2. Each subroutine in column 2 executes a major task and calls the subroutine in column 3. For any given calculation not all branches of the tree are called.
## Chart I Global Tree Structure by Task

<table>
<thead>
<tr>
<th>SETUP</th>
<th>1.0 Read Input Data</th>
<th>INPDAT</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>2.0 Setup Reference Conditions</td>
<td>REFCON</td>
</tr>
<tr>
<td></td>
<td>3.0 Setup Pressure Distribution</td>
<td>ROTORP</td>
</tr>
<tr>
<td></td>
<td>4.0 Calculate Rotor Inlet Conditions</td>
<td>RINLET</td>
</tr>
<tr>
<td></td>
<td>5.0 Smooth Pressure Distribution Data</td>
<td>SMTHD</td>
</tr>
<tr>
<td></td>
<td></td>
<td>INTR1D</td>
</tr>
<tr>
<td></td>
<td></td>
<td>INTR2D</td>
</tr>
<tr>
<td></td>
<td>6.0 Echo Input Data</td>
<td>OPTDAT</td>
</tr>
<tr>
<td></td>
<td>7.0 Compute Metric Data and B. L. Edge Conditions</td>
<td>SOLVE</td>
</tr>
<tr>
<td></td>
<td></td>
<td>INTRB</td>
</tr>
<tr>
<td></td>
<td></td>
<td>INTRC</td>
</tr>
<tr>
<td></td>
<td></td>
<td>METCO</td>
</tr>
<tr>
<td></td>
<td></td>
<td>DIRCOS</td>
</tr>
<tr>
<td></td>
<td></td>
<td>ROTOR</td>
</tr>
<tr>
<td></td>
<td></td>
<td>INTRD</td>
</tr>
<tr>
<td></td>
<td></td>
<td>BLEDGE</td>
</tr>
<tr>
<td></td>
<td></td>
<td>LAG4PT</td>
</tr>
<tr>
<td></td>
<td></td>
<td>LAG4PT</td>
</tr>
<tr>
<td></td>
<td></td>
<td>SPLINE</td>
</tr>
<tr>
<td></td>
<td></td>
<td>EVAL</td>
</tr>
<tr>
<td></td>
<td></td>
<td>INTR1D</td>
</tr>
<tr>
<td></td>
<td></td>
<td>INTR3D</td>
</tr>
<tr>
<td></td>
<td></td>
<td>INTREK</td>
</tr>
<tr>
<td></td>
<td></td>
<td>INTREL</td>
</tr>
<tr>
<td></td>
<td></td>
<td>UI TER</td>
</tr>
</tbody>
</table>
6.2 SETUP COMMON Block Variables

PARAMETERS

LPL   (101)   Max. no. $X_1$ mesh points
KPL   (61)    Max. no. $X_2$ mesh points
LBL   (51)    Max. no. input $X_1$ boundary points
KBL   (51)    Max. no. input $X_2$ boundary points
LSL   (51)    Max. no. input $X_1$ surface points
KSL   (51)    Max. no. input $X_2$ surface points
LDL   (21)    Max. no. input $X_1$ inflow points
KDL   (21)    Max. no. input $X_2$ inflow points
IDRM1 8   Output unit for metric data
IDRM2 9   Output unit for edge conditions
IDRM3 10  Output unit for transformation variables
IDRM4 11  Output unit for length scales
IDRM5 12  Output unit for setup code

COMMON /INTV/ Integer Variables

LPLAST   No. input $X_1$ mesh points
KPLAST   No. input $X_2$ mesh points
LSLAST   No. input $X_1$ surface points
KSLAST   No. input $X_2$ surface points
LBLAST   No. input $X_1$ boundary points
KBLAST   No. input $X_2$ boundary points
LDLAST   No. output $X_1$ $C_p$ data points
KDLAST  No. output $X_2 C_p$ data points
LULAST  No. input $X_1$ inflow points
KULAST  No. input $X_2$ inflow points
LILAST  No. input $X_1 C_p$ data points
KILAST  No. input $X_2 C_p$ data points

COMMON /IOPT/ Input Options

IOPT1  Surface geometry option
IOPT2  Grid boundary option
IOPT3  Pressure data input option
IOPT4  Mesh distribution option
IOPT5  Inflow option
IOPT6  Print option
IOPT7  Pressure smoothing option
IOPT8  Rotor/Stator option
IOPT9  Coordinate output option
IOPT10 Relative eddy option
IOPT11 Upstream inflow option
IOPT12 Not used

COMMON /INDV/ Independent Variables

$X_1(L)$ $X_1^L$ $X_1$ coordinate array
$X_2(K)$ $X_{2,K}$ $X_2$ coordinate array
DX1(L) $\Delta X_1^L$ $X_1$ step size

DX2(K) $\Delta X_{2,K}$ $X_2$ step size

X1P $X_1$ $X_1$ coordinate

X2P $X_2$ $X_2$ coordinate

**COMMON /SURFC/ 2D Coordinate Surface Variables**

YY(LK) $Y_1^L$ or $Y_2^L,K$ $Y_1$ or $Y_2$ Cartesian coordinates

YY3(LK) $Y_3^L,K$ $Y_3$ Cartesian coordinate

**COMMON /SMIX/ 3D Coordinate Surface Variables**

Y1M(L) $Y_1^L$ $Y_1$ Cartesian coordinate of surface

Y2M(K) $Y_2^L,K$ $Y_2$ Cartesian coordinate of surface

Y3M(L,K) $Y_3^L,K$ $Y_3$ Cartesian coordinate of surface

**COMMON /ARCL/ Arc Length Variables**

SS1(K) $S_1,K$ $X_1$ arc length array

HS1(K) $H_{1,K}$ $X_1$ metric coefficient array

SL1 $S_1$ $X_1$ arc length

SL2 $S_2$ $X_2$ arc length

SS10 $S_{10}$ $X_1$ arc length start

**COMMON /COMB/ Computational Boundary Variables**

Y10X2(K),Y20X2(K) Side 1 input boundary

Y1X11(L),Y2X11(L) Side 2 input boundary

Y11X2(K),Y21X2(K) Side 3 input boundary

Y1X10(L),Y2X10(L) Side 4 input boundary
COMMON /TRANSV/ Transformation Variables

Y1P, Y2P, Y3P, Y1, Y2, Y3 Cartesian coordinates

DY11 \( \frac{\partial Y_1}{\partial x_1} \) First partial derivatives

DY12 \( \frac{\partial Y_1}{\partial x_2} \) of Cartesian coordinates

DY21 \( \frac{\partial Y_2}{\partial x_1} \) with respect to surface coordinates

DY22 \( \frac{\partial Y_2}{\partial x_2} \)

DY31 \( \frac{\partial Y_3}{\partial x_1} \)

DY32 \( \frac{\partial Y_3}{\partial x_2} \)

D2Y111 \( \frac{\partial^2 Y_1}{\partial x_1 \partial x_1} \) Second partial derivatives

D2Y112 \( \frac{\partial^2 Y_1}{\partial x_1 \partial x_2} \) of Cartesian coordinates

D2Y122 \( \frac{\partial^2 Y_1}{\partial x_2 \partial x_2} \) with respect to surface coordinates

D2Y211 \( \frac{\partial^2 Y_2}{\partial x_1 \partial x_1} \)

D2Y212 \( \frac{\partial^2 Y_2}{\partial x_1 \partial x_2} \)

D2Y222 \( \frac{\partial^2 Y_2}{\partial x_2 \partial x_2} \)

D2Y311 \( \frac{\partial^2 Y_3}{\partial x_1 \partial x_1} \)

D2Y312 \( \frac{\partial^2 Y_3}{\partial x_1 \partial x_2} \)

D2Y322 \( \frac{\partial^2 Y_3}{\partial x_2 \partial x_2} \)

COMMON /METRIC/ Metric variables

GL11, GL12, GL13

GL21, GL22, GL23 \( G_{ij} \) Covariant metric tensor components

GL31, GL32, GL33

GU11, GU12, GU13

GU21, GU22, GU23 \( g^{ij} \) Contravariant metric tensor components

GU31, GU32, GU33
DG  \[ g \]  Determinate of metric tensor

HH1, HH2, HH3  \[ H_1, H_2, H_3 \]  Metric scale coefficients

DH11  \[ \frac{\partial H_1}{\partial x_1} \]  Derivatives of metric scale coeff.

DH12  \[ \frac{\partial H_1}{\partial x_2} \]  

DH21  \[ \frac{\partial H_2}{\partial x_1} \]  

DH22  \[ \frac{\partial H_2}{\partial x_2} \]  

DG121  \[ \frac{\partial G_{12}}{\partial x_1} \]  Derivatives of metric tensor

DG122  \[ \frac{\partial G_{12}}{\partial x_2} \]  

COMMON /DIRC/ Direction cosines

GAM(I,J)  \[ \gamma_{ij} \]  Direction cosines

GAMI(I,J)  \[ \gamma^{-1}_{ij} \]  Inverse of direction cosines

COMMON /INPEDG/ Pressure Distributions Variables

Y1D(L)  \[ Y^L_1 \]  Output Y coordinate

Y2D(K)  \[ Y^L_{2,K} \]  Output Y coordinate

Y3D(L,K)  \[ C^L_{P,K} \]  Output pressure coeff.

Y1I(L)  \[ \hat{Y}^L_1 \]  Input Y coordinate

Y2I(K)  \[ \hat{Y}^L_{2,K} \]  Input Y coordinate

Y3I(L,K)  \[ \hat{C}^L_{P,K} \]  Input pressure coeff

COMMON /BLEDGE/ Boundary Edge Variables

U1E  \[ U_{1e} \]  \[ X_1 \] Edge velocity

U2E  \[ U_{2e} \]  \[ X_2 \] Edge velocity
### Edge static pressure

\[ P \]

### Edge velocity gradients

\[
\begin{align*}
\Delta U_1 & = \frac{\partial U_1}{\partial x_1} \\
\Delta U_2 & = \frac{\partial U_2}{\partial x_2}
\end{align*}
\]

### Static pressure coefficient

\[ C_P \]

### Static pressure gradients

\[
\begin{align*}
\Delta C_P & = \frac{\partial C_P}{\partial x_1} \\
\Delta C_P & = \frac{\partial C_P}{\partial x_2}
\end{align*}
\]

### Explicit velocity gradients

\[
\begin{align*}
\Delta U_1 & = \frac{\partial U_1}{\partial x_1} \\
\Delta U_2 & = \frac{\partial U_2}{\partial x_2}
\end{align*}
\]

### Edge rothalpy

\[ I \]

### Inflow Conditions

- Side 1 input inflow velocity \( U_2e \)
- Side 4 input inflow velocity \( U_2e \)
- Side 1 input coordinate \( Y_1 \)
- Side 4 input coordinate \( Y_1 \)

### Stored arrays

- \( U_1e \)
- \( U_2e \)
- \( C_P \)
- \( I \)

### Common Blocks

- **/INFLO/**
- **/UBLED/**
### COMMON /GASP/ Constants

<table>
<thead>
<tr>
<th>Variable</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>GASR</td>
<td>( R )</td>
</tr>
<tr>
<td>GAMM</td>
<td>( \gamma )</td>
</tr>
<tr>
<td>TI</td>
<td>0.01745329</td>
</tr>
<tr>
<td>PI</td>
<td>3.1415926</td>
</tr>
</tbody>
</table>

### COMMON /FLOWI/ Input Flow Conditions

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>PINFI</td>
<td>Reference static pressure ( P_\infty )</td>
</tr>
<tr>
<td>TINFI</td>
<td>Reference free stream static temperature ( T_\infty )</td>
</tr>
<tr>
<td>ROINFI</td>
<td>Reference density ( \rho_\infty )</td>
</tr>
<tr>
<td>UINFI</td>
<td>Reference velocity ( u_\infty )</td>
</tr>
<tr>
<td>XMINFI</td>
<td>Reference mach number ( M_\infty )</td>
</tr>
<tr>
<td>BET1I</td>
<td>Not used ( \beta_1^{\infty} )</td>
</tr>
<tr>
<td>XLREF</td>
<td>Reference length ( \ell )</td>
</tr>
</tbody>
</table>

### COMMON /FLOW/ Output Flow Conditions

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>PINF</td>
<td>Reference static pressure ( P_\infty )</td>
</tr>
<tr>
<td>TINF</td>
<td>Reference freestream static temperature ( T_\infty )</td>
</tr>
<tr>
<td>TREF</td>
<td>Reference temperature ( T_{\text{ref}} )</td>
</tr>
<tr>
<td>HINF</td>
<td>Reference enthalpy ( H_\infty )</td>
</tr>
<tr>
<td>PINFL</td>
<td>Rotor inlet static pressure ( P_L )</td>
</tr>
<tr>
<td>HRINFL</td>
<td>Rotor inlet enthalpy ( I_L )</td>
</tr>
<tr>
<td>DHINF</td>
<td>Side 4 delta enthalpy ( \Delta H )</td>
</tr>
<tr>
<td>ALP1I</td>
<td>Not used ( \alpha_{100} )</td>
</tr>
</tbody>
</table>
COMMON /FLOW/ Output Flow Variables

PTABSF \( P_{T\infty} \) Absolute total pressure
HTABSF \( T_{T\infty} \) Absolute total enthalpy
PTABSL \( P_{TL} \) Absolute rotor inlet total pressure

COMMON /ROTOR/ Input Rotor Parameters

VBTI \( V_{Bt} \) Rotor tip velocity
G01,G02,G03 \( \gamma_{0i} \) Direction cosines for vorticity vector
RADHI,RADTI \( R_H, R_T \) Hub/Tip radius
YRADHI,YRADTI \( Y_H, Y_T \) Hub,Tip coordinates
GAPI \( G \) Rotor midspan gap

COMMON /ROTOR1/ Output Rotor Parameters

OMEG1,OMEG2,OMEG3 \( \Omega_i \) Vorticity components in Cartesian coor.
RAD \( R \) Radius
DRAD1 \( \partial R / \partial X_1 \) Derivatives
DRAD2 \( \partial R / \partial X_2 \)

COMMON /ROTOR2/ Rotor Inlet Parameters

VBINF \( Y_{B\infty} \) Rotor blade reference velocity
UPINF \( U_{\phi\infty} \) Rotor reference tangential velocity
VBINFL \( V_{BL} \) Rotor blade inlet velocity
UPINFL \( U_{\phi L} \) Rotor inlet tangential velocity
SGNR \( (+/-)_U \) Sign on radius vector
SGNU \( (+/-)_L \) Sign on rotor tangential velocity
DELCp \( \Delta C_p \) Rotor CP correction
**COMMON /UPSTR1/ Input Upstream Flow Variables**

- **Y2RI(K)** \( Y_2, K \) \( Y_2 \) input coordinate
- **PTRI(K)** \( p_T, K \) Upstream absolute total pressure
- **TTRI(K)** \( T_T, K \) Upstream absolute total temperature

**COMMON /UPSTR2/ Input Upstream Flow Variables**

- **UZRI(K)** \( U_z, K \) Upstream axial velocity
- **BTRI(K)** \( \beta_{1, K} \) Upstream relative flow angle

**COMMON /UPSTR3/ Output Upstream Flow Variables**

- **U1A(K)** \( u_{1, K} \) Absolute total velocity
- **UPA(K)** \( u_{\phi, K} \) Absolute tangential velocity
- **ULR(K)** \( U_{1, K} \) Relative total velocity
- **UPR(K)** \( u_{\phi, K} \) Relative tangential velocity
- **U2S(K)** \( U_{2s, K} \) Est. initial rotor spanwise velocity

**COMMON /UPSTR4/ Output Upstream Flow Variables**

- **UZA(K)** \( U_z, K \) Absolute axial velocity
- **VBB(K)** \( V_B, K \) Rotor velocity
- **BTA(K)** \( \beta_K \) Absolute inlet flow angle
- **OMS(K)** \( \Omega_{S, K} \) Ratio relative vorticity/rotor speed
- **RDK(K)** \( R_K \) Rotor radius
COMMON /UPSTR5/ Output Upstream Flow Variables

- PS(K) P_K Rotor inlet static pressure
- TS(K) T_K Rotor inlet static temperature
- HTA(K) H_K Absolute inlet total enthalpy
- PTA(K) P_T,K Absolute inlet total pressure
- TTA(K) T_T,K Absolute inlet total temperature
6.3 Description of SETUP Subroutines

BLEDGE
Integrate boundary layer edge eqs.

CUBA
See subroutine CUBTWO

CUBB
See subroutine CUBTWO

CUBTWO
Calculate two dimensional cubic spline fit

DIRCOS
Calculate direction cosines and inverse

EVAL
Evaluate function and derivatives of spline fit

INPDAT
Read input data

INTRB
Establish the mapping of the boundaries

INTRC
Establish surface geometry

INTRD
Calculate pressure coeff. and derivatives

INTREK
Interpolate inflow velocity on L=1 boundary

INTREL
Interpolate inflow velocity on K=1 boundary

INTR1D
Linear interpolation on 1d grid

INTR3D
Linear interpolation on 2d grid

LAG4PT
Lagrangian 4 point interpolation

MATRIX
See subroutine CUBTWO

METCO
Calculate metric data

OPEC
Calculate one sided proximate end conditions

OPTDAT
Echo input data

PERM
See subroutine CUBTWO
<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>REFCON</td>
<td>Setup reference conditions</td>
</tr>
<tr>
<td>RINLET</td>
<td>Calculate rotor inlet conditions</td>
</tr>
<tr>
<td>ROTOR</td>
<td>Estimate upstream total enthalpy and pressure</td>
</tr>
<tr>
<td>ROTORP</td>
<td>Setup pressure distribution for relative eddy approx.</td>
</tr>
<tr>
<td>SETUP</td>
<td>Main program</td>
</tr>
<tr>
<td>SMTHD</td>
<td>Smooth input CP data</td>
</tr>
<tr>
<td>SOLVE</td>
<td>Compute metric data and b. l. edge conditions</td>
</tr>
<tr>
<td>SPLINE</td>
<td>Setup derivatives on boundary for surface spline fit</td>
</tr>
<tr>
<td>UIITER</td>
<td>Iteration algorithm for U1E, U2E</td>
</tr>
</tbody>
</table>
Subroutine BLEDGE(L,K)

Object

This subroutine integrates the boundary layer edge equations using the input pressure (CP) distribution. The boundary layer edge equations are solved at the point X1, X2 for the velocities U1;e, U2;e and the enthalpy HE for the given input static pressure.

Options

IOPT3 = 0 No pressure data
       = 1 CP = CP(X1,X2)
       = 2 CP = CP(Y1,Y2)
       = 3 CP = CP(Y1,X2)
       = 4 CP = CP(X1,Y2)
       = 5 Analytical pressure data

IOPT5 = 0 U2E = 0.0 ; U1E calculated from the Euler equation
       = 1 U2E(0,X2) = 0.0 ; U2E(X1,0) = 0.0
       = 2 U2E(0,X2) = 0.0 ; U2E(X1,0) input
       = 3 U2E(0,X2) input ; U2E(X1,0) = 0.0
       = 4 U2E(0,X2) input ; U2E(X1,0) input

List of Symbols

A0 to A10 Coefficients of edge equations
Ci to C6 Coefficients of edge equations
D1 to D6 Coefficients of Euler equations
E1 to E3 Coefficients of energy equation
L, K Index for X1 and X2
Theory

The basic equations are described in Sect. 3.11 of Ref 1. This subroutine first calculates the coefficients of the differential equations. Then it determines if the point \( L, K \) is on an inflow boundary (\( L=1 \) or \( K=1 \)) or an interior point.

\[
\begin{align*}
\text{If } L=1 \text{ and } IOPT5 &= 1 \text{ or } 2 \quad ; U2E = 0 \\
\text{If } L=1 \text{ and } IOPT5 &= 1 \text{ or } 2 \quad ; U2E \text{ is interpolated from the input data using subroutine INTREK} \\
\text{If } K=1 \text{ and } IOPT5 &= 3 \text{ or } 4 \quad ; U2E = 0 \\
\text{If } K=1 \text{ and } IOPT5 &= 3 \text{ or } 4 \quad ; U2E \text{ is interpolated from the input data using subroutine INTREL} \\
\text{IF } L>1 \text{ and } K>1 & \quad ; U2E \text{ and } U2E \text{ are calculated by integrating the boundary layer edge equations}
\end{align*}
\]

After \( U1E, U2E \) and \( HE \) are calculated, all the remaining boundary edge variables required by the BL3D code are then calculated.

References

Subroutine CUBTWO(Arg. List)

Object

This subroutine performs a two dimensional cubic spline fit to unequally spaced data.

Options

None

List of Symbols

- \( N \) : Max. X array size
- \( M \) : Max. Y array size
- \( X(I) \) : Input Y1 coordinate
- \( Y(J) \) : Input Y2 coordinate
- \( U(I,J) \) : Input Y3 coordinate
- \( P(I,J) \) : \( \frac{DY_3}{DY_1} \)
- \( Q(I,J) \) : \( \frac{DY_3}{DY_2} \)
- \( R(I,J) \) : \( \frac{D^2Y_3}{DY_1/DY_2} \)
- \( A(I,J,K,L) \) : Spline coefficients
- \( CDX \) : Work arrays
- \( DY \)
- \( ZX \)
- \( ZY \)
- \( ORD \)
- \( UNB \)
- \( F \)
Theory

This subroutine performs a two-dimensional cubic spline fit to the input blade surface using the theory of Ref. 1. This subroutine is called by subroutine SPLINE, and calls subroutines PERM, MATRIX, CUBA, and CUBB.

References

Subroutine DIRCOS

Object

This subroutine calculates the direction cosine tensor and the inverse of the direction cosine tensor for the transformation from the computational to the Cartesian coordinates.

Options

None

List of Symbols

See COMMON blocks

Theory

The theory for calculating the direction cosine tensor is given in Sect. 3.10 by Anderson (Ref. 1).

References

Subroutine EVAL(Arg. List)

Object

This subroutine evaluates \( Y_3, DY_3/DY_1, DY_3/DY_2, D^2Y_3/DY_1/DY_1, D^2Y_3/DY_2/DY_2, - D^2Y_3/DY_1/DY_2 \) at the point \((Y_1P, Y_2P)\) using the Spline coefficients calculated in subroutine SPLINE.

Options

None

List of Symbols

- \( A(I,J,K,L) \): Spline coefficients
- \( LL1 \): No. \( Y_1 \) input points
- \( KK1 \): No. \( Y_2 \) input points
- \( LSI \): Corner point \( Y_1 \) index
- \( KSI \): Corner point \( Y_2 \) index
- \( DY3Y1 \): \( DY_3/DY_1 \) First derivatives
- \( DY3Y2 \): \( DY_3/DY_2 \)
- \( DY3Y11 \): \( D^2Y_3/DY_1/DY_1 \)
- \( DY3Y12 \): \( D^2Y_3/DY_1/DY_2 \)
- \( DY3Y22 \): \( D^2Y_3/DY_2/DY_2 \)

Theory

The function and its derivatives are evaluated using the formulas derived in Ref. 1. For the function we have:

\[
Y_3 = \sum_{k=1}^{4} \sum_{i=1}^{4} A_{ijkl} (Y_1 - Y_{1i})^k (Y_2 - Y_{20k})^l
\]  

(1)
The partial derivatives are evaluated by analytically differentiating Eq. (1).

References

Subroutine INPDAT

Object

This subroutine reads all input data for the SETUP code according to the
input options IOPT1 through IOPT12

Options

IOPT4 = 0 Uniform (X1,X2) computational grid calculated
IOPT2 = 0 Uniform (Y1,Y2) Cartesian grid calculated
         = 1 Skewed (Y1,Y2) grid calculated
         = 2 One dimensional mapping using sides 1 and 3
         = 3 One dimensional mapping using sides 2 and 4
         = 4 Two dimensional mapping

List of Symbols

See COMMON blocks

Theory

This subroutine reads all input data required by the SETUP code and cal-
lculates certain grids by default since they do not require all the input data for
general grids. See Options List.
Subroutine INTRB

Object

This subroutine establishes the mapping of the physical boundaries to the computational boundaries.

Options

None

List of Symbols

See COMMON block variables

Theory

The theory for this calculation is given by Anderson (Ref. 1). The physical boundaries are known from the input data as ordered pairs of points for the four sides of the physical boundary as shown on Fig. 1. These are given by:

\[
\begin{align*}
Y_1(0,X_2P), Y_2(0,X_2P) & \quad \text{KBLAST points for Side 1} \\
Y_1(X_1P,1), Y_2(X_1P,1) & \quad \text{LBLAST points for Side 2} \\
Y_1(1,X_2P), Y_2(1,X_2P) & \quad \text{KBLAST points for Side 3} \\
Y_1(X_1P,0), Y_2(X_1P,0) & \quad \text{LBLAST points for Side 4}
\end{align*}
\]

where

\[
\begin{align*}
0.0 < X_1P < 1.0 \\
0.0 < X_2P < 1.0
\end{align*}
\]
Then considering Side 1, we note that the boundary is only a function of $X_2P$. Thus the Side 1 boundary can be written in parametric form as a function of $X_2P$ by establishing an array $X_2B(KB) \quad KB=1,KBLAST$ at equal increments $0.0 < X_2B < 1.0$ so that there is a one to one correspondence of points. The same procedure follows for the other three sides. With the boundaries established in parametric form, the Cartesian coordinates $(Y_1,Y_2)$ of the of the boundary is known as a function of the computational coordinates $(X_1P,X_2P)$. Given the computational coordinate $(X_1P,X_2P)$, the corresponding Cartesian coordinates of the boundary on the four sides is obtained by interpolation using the four point Lagrangian interpolation formulas contained in subroutine LAG4PT.

The interior Cartesian coordinate point $(Y_1P,Y_2P)$ corresponding to the computational coordinate point $(X_1P,X_2P)$ is obtained by the transfinite mapping of Gordon and Thiel (Ref. 2) as shown in Sect. 3.10 of Ref. 1. With the mapping established, the derivatives of $Y_1$ and $Y_2$ with respect to $X_1$ and $X_2$ are obtained by analytically differentiating the algebraic mapping formula. Subroutine LAG4PT also returns the first and second derivatives of the Cartesian coordinates $Y_1$ and $Y_2$ of the boundaries with respect to the appropriate computational coordinate $X_1$ or $X_2$ so that the first and second partial derivatives can be obtained.
References


Subroutine INTRC

**Object**

This subroutine establishes the complete surface geometry by calculating the first and second partial derivatives of the surface coordinate $Y_3$ with respect to $Y_1$ and $Y_2$.

**Options**

- $IOPT_1 = 0$  
  $Y_3 = 0.0$
- $IOPT_1 = 1$  
  $Y_3 = Y_3(Y_1)$
- $IOPT_1 = 2$  
  $Y_3 = Y_3(Y_2)$
- $IOPT_1 = 3$  
  $Y_3 = Y_3(Y_1, Y_2)$

**List of Symbols**

See COMMON blocks

**Theory**

The Cartesian coordinate of the surface $Y_3$ and the partial derivatives of $Y_3$ with respect to $Y_1$ and $Y_2$ are obtained by interpolation.

- $IOPT_1 = 0$  
  $Y_3$ and all derivatives are zero.
- $IOPT_1 = 1$  
  $Y_3$ and its derivatives are obtained by interpolation using a four point Lagrangian interpolation contained in subroutine LAG4PT.
- $IOPT_1 = 2$  
  $Y_3$ and its derivatives are obtained using a surface spline interpolation contained in subroutine EVAL.
  The spline coefficients are calculated first when $L=1$ and $K=1$ by calling subroutine SPLINE.
Subroutine INTRD

Object

Calculate pressure coefficient \( CP \) and derivatives.

Options

\[
\begin{align*}
\text{IOPT3} = 0 & \quad \text{No CP data} \\
\text{IOPT3} = 1 & \quad CP = CP(X_1, X_2) \\
\text{IOPT3} = 2 & \quad CP = CP(Y_1, Y_2) \\
\text{IOPT3} = 3 & \quad CP = CP(Y_1, X_2) \\
\text{IOPT3} = 4 & \quad CP = CP(X_1, Y_2) \\
\text{IOPT3} = 5 & \quad CP \text{ Analytical function}
\end{align*}
\]

List of symbols

- \( AX \) Logical variable (if TRUE \( X_1P \) lies on grid line)
- \( AY \) Logical variable (if TRUE \( X_2P \) lies on grid line)
- \( ONED \) Logical variable (If TRUE \( X_1P \) or \( X_2P \) lies on grid line)

Theory

The pressure coefficient \( CP \) and its derivatives with respect \( X_1 \) and \( X_2 \) are calculated in this subroutine. If \( X_1 \) or \( X_2 \) lie on a grid line, then \( CP \) and its derivatives with respect to the input variables \( (X_1 \text{ or } Y_1) \) and \( (X_2 \text{ or } Y_2) \) are calculated using a one dimensional interpolation contained in subroutine INTR1D. If \( X_1 \) and \( X_2 \) do not lie on a grid line, then \( CP \) and its derivatives with respect to the input variables \( (X_1 \text{ or } Y_1) \) and \( (X_2 \text{ or } Y_2) \) are calculated using a linear two dimensional interpolation contained in subroutine INTR3D. Then depending on the option \( \text{IOPT3} \), the partial derivatives with respect to the coordinates are calculated.
Subroutine INTREK

Object

This subroutine interpolates for the inflow velocities along the X1 = 0.0 boundary.

Options

None

List of Symbols

See COMMON Blocks

Theory

The input arrays are Y12U(K) and U2X2(K). Then given Y2, along the X1 = 0.0 boundary, the inflow velocity U2E is interpolated from the input arrays using the four point Lagrangian interpolation contained in subroutine LAG4PT.
Subroutine INTREL

Object

This subroutine interpolates for the inflow velocities along the $X2 = 0.0$ boundary.

Options

None

List of Symbols

See COMMON Blocks

Theory

The input arrays are $YI1U(L)$ and $U2X1(L)$. Then given $Y1$, along the $X2 = 0.0$ boundary, the inflow velocity $U2E$ is interpolated from the input arrays using the four point Lagrangian interpolation contained in subroutine LAG4PT.
Subroutine INTR1D

Object

Interpolates between data points which lie on a gridline.

Options

None

List of Symbols

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>X</td>
<td>Ordinates</td>
</tr>
<tr>
<td>Y</td>
<td>Abscissa</td>
</tr>
<tr>
<td>F</td>
<td>Function F(X,Y)</td>
</tr>
<tr>
<td>L,K</td>
<td>Indices of Interpolation</td>
</tr>
<tr>
<td>XP,YP</td>
<td>Interpolation Point</td>
</tr>
<tr>
<td>FP</td>
<td>F(XP,YP)</td>
</tr>
<tr>
<td>DFDX</td>
<td>d(F(XP,YP))/dx</td>
</tr>
<tr>
<td>DFDY</td>
<td>d(F(XP,YP))/dy</td>
</tr>
<tr>
<td>LD,KD</td>
<td>Dimensions: X(LD), Y(KD), F(LD,KD)</td>
</tr>
<tr>
<td>LL,KK</td>
<td>Actual sizes: X(LL), Y(KK), F(LL,KK)</td>
</tr>
<tr>
<td>AX,AY</td>
<td>Logical: AX = .true. denotes interpolation is along an X gridline. AY = .true. denotes interpolation along a Y gridline.</td>
</tr>
</tbody>
</table>

Theory

The function F is evaluated at the point (XP,YP) using simple divided differences. This routine differs from INTR3D in that interpolation is strictly along a gridline.
Subroutine INTR3D

Object

This subroutine interpolates a function F to a point in between gridlines, using linear interpolation of a first order tensor product approximation of the function F.

Options

None

List of Symbols

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>X</td>
<td>Ordinates</td>
</tr>
<tr>
<td>Y</td>
<td>Abscissa</td>
</tr>
<tr>
<td>F</td>
<td>Function F(X,Y)</td>
</tr>
<tr>
<td>L,K</td>
<td>Indices of Interpolation</td>
</tr>
<tr>
<td>XP,YP</td>
<td>Point of Interpolation</td>
</tr>
<tr>
<td>FP</td>
<td>F(XP,YP)</td>
</tr>
<tr>
<td>DFDX</td>
<td>d(F(XP,YP))/dx</td>
</tr>
<tr>
<td>DFDY</td>
<td>d(F(XP,YP))/dy</td>
</tr>
<tr>
<td>DFDXY</td>
<td>d^2(F(XP,YP))/dy^2</td>
</tr>
<tr>
<td>LL,KL</td>
<td>Dimensions: X(LL) Y(KL) F(LL,KL)</td>
</tr>
</tbody>
</table>
Theory

The function $F$ is locally approximated by the first order tensor product:

$$F = (ax+b)(cy+d) \quad (1)$$

where $a,b,c$ and $d$ are chosen so that the local approximation agrees with the actual function values at the four corners of grid box whose lower lefthand corner has indices $(L,K)$. The returned function value and derivatives are evaluated directly from $F'$. 
Subroutine LAG4PT

Object

This subroutine interpolates the function and the first and second derivatives using a four point Lagrangian interpolation.

Options

None

List of Symbols

- $X(I)$: Input abscissas
- $Y(I)$: Input ordinates
- $XARG$: Output abscissa
- $YARG$: Output ordinate
- $DYDX$: Output first derivative
- $D2YDX$: Output second derivative

Theory

The four point Lagrangian interpolation formula is:

\[
Y = \frac{(X - X(I+1))(X - X(I+2))(X - X(I+3))Y(I)}{(X(I) - X(I+1))(X(I) - X(I+2))(X(I) - X(I+3))} \\
- \frac{(X - X(I))(X - X(I+2))(X - X(I+3))Y(I+1)}{(X(I) - X(I+1))(X(I+1) - X(I+2))(X(I+1) - X(I+3))} \\
+ \frac{(X - X(I))(X - X(I+1))(X - X(I+3))Y(I+2)}{(X(I) - X(I+2))(X(I+1) - X(I+2))(X(I+2) - X(I+3))} \\
- \frac{(X - X(I))(X - X(I+1))(X - X(I+2))Y(I+3)}{(X(I) - X(I+3))(X(I+1) - X(I+3))(X(I+2) - X(I+3))}
\]

The first and second derivatives are obtained by analytically differentiating Eq. (1).
Subroutine METCO

Object

This subroutine calculates the covariant metric tensor components $G_{IJ}$, the contravariant metric tensor components $G^{IJ}$, the metric coefficients $H^{HI}$, and their derivatives.

Options

None

List of Symbols

See COMMON blocks

Theory

Given all the partial derivatives of the transformation calculated in subroutine INTRC, the metric data is then given by:

$$G_{ij} = \frac{dY_K}{dX_i} \frac{dY_K}{dX_j}$$  \hspace{1cm} (1)

$$H_1 = \sqrt{G_{11}}$$  \hspace{1cm} (2)

$$H_2 = \sqrt{G_{22}}$$  \hspace{1cm} (3)

$$H_3 = 1.0$$  \hspace{1cm} (4)

$$G = \det(G_{ij})$$  \hspace{1cm} (5)

$$g^{ij} = \frac{G_{rs}G^{st} - G_{rt}G^{rs}}{G}$$  \hspace{1cm} (6)

where the groups $(i,r,l)$ and $(j,s,t)$ are cyclic permutations. The derivatives are obtained by differentiating Eq. (1).
Subroutine OPEC(X,F,FPA,FPB,NP1)

Object

This subroutine calculates the one sided proximate end conditions for
the surface spline interpolation.

Options

None

List of Symbols

X  Abscissas
F  Ordinates
FPA  Left hand derivative end condition
FPB  Right hand derivative end condition
NP1  Number of ordered pairs of data (NP1>4)

Theory

This subroutine evaluates the derivative boundary conditions for the
cubic spline which is fitted to the input coordinates of the blade surface
using the theory of McCartin (Ref 1.). This subroutine is called by sub-
routine SPLINE.

References

1. McCartin, B. J.: Theory, Computation, and Application of Exponential
Subroutine OPTDAT

Object

This subroutine echo prints the input data.

Options

None

List of Symbols

See COMMON blocks

Theory

This subroutine echo prints the input data, prints the reference conditions calculated in subroutine REFCON, prints the smoothed pressure CP data calculated in subroutine SMTHD, and finally prints the rotor inlet conditions calculated in subroutine RINLET.
Subroutine REFCON

Object

This subroutine calculates the reference conditions to normalize all input variables.

Options

IOPT8 = 0 (Stator) No coriolus forces
IOPT8 = 1 (Rotor) Load pressure data hub to tip
IOPT8 = -1 (Rotor) Load pressure data tip to hub

List of Symbols

See COMMON blocks

Theory

The reference conditions are defined in Ref. 1 as used in the BL3D boundary layer code.

References

Subroutine RINLET

Object

This subroutine calculates the rotor inlet conditions.

Options

IOPT8 = 0 (Stator) Non coriolus forces
IOPT8 = 1 (Rotor) Load pressure data hub to tip
IOPT8 = -1 (Rotor) Load pressure data tip to hub
IOPT11 = 0 Uniform upstream conditions
IOPT11 = 1 Nonuniform upstream conditions
IOPT11 = 2 Approx. upstream cond. for rotor

List of Symbols

DUPDR  Derivative of absolute tangential velocity
GAP    Gap normal to flow direction
HGT    Span
OMEGZ  Axial component of absolute vorticity
        Axial component of relative vorticity
        Steamwise component of relative vorticity
        Average relative vorticity
        Steam function

Theory

The total pressure PTAI(K), total temperature TTAI(K), axial velocity UZAI(K), and rotor inlet relative angle BTRI(K) are known from the input data. Both the relative and absolute velocity components can be calculated from the velocity triangles. Knowing the absolute velocities, the static enthalpy and static pressure can then be calculated.
The relative rotor inlet vorticity and the initial spanwise velocities as estimated using the theory of Dring and Joslyn, Ref. 1. The absolute vorticity is given approximately by

\[ \omega_z = \frac{1}{R} \frac{\partial}{\partial R} (RU) \]  

(1)

and the relative vorticity by

\[ \zeta_z = \omega_z - 2\hat{\Omega} \]  

(2)

The component of vorticity in the streamwise direction is then

\[ \zeta_s = \zeta_z \frac{U_z}{U_1} \]  

(3)

An estimate of the initial spanwise velocity on the rotor blade is obtained by solving Poisson's equation using the area average vorticity.

\[ \nabla^2 \psi = \zeta_{ZA} \]  

(4)

A Fourier series solution of Eq. (4) is given by (Ref. 2) as

\[
\psi = -\frac{\zeta_{ZA}}{2} x (g-x) + \frac{4\zeta_{ZA}R^2}{\pi^3} \sum_{k=1}^{\infty} \sin \left( \frac{k\pi x}{g} \right) \cosh \left( \frac{k\pi (y-h/2)}{g} \right) \cos \left( \frac{k\pi y}{g} \right) \cosh \left( \frac{k\pi h/2}{g} \right)
\]  

(5)

where K is odd. The estimated spanwise velocity at the leading edge is given by
\[ V(0, Y) = g \xi_{SA} \left\{ \frac{1}{2} - \frac{4}{\Pi^2} \sum_{k=1}^{\infty} \frac{\cosh \left[ \frac{k \Pi}{g} \left( Y - \frac{h}{2} \right) \right]}{k^2 \cosh \left[ \frac{k \Pi}{g} \frac{h}{2} \right]} \right\} \]  

References


Subroutine ROTOR

Object

This subroutine calculates the upstream total pressure, total enthalpy (rothalpy) and local vorticity component normal to the surface

Options

IOPT8 = 0 (Stator) Non coriolis forces
IOPT8 = 1 (Rotor) Load pressure data hub to tip
IOPT8 = -1 (Rotor) Load pressure data tip to hub
IOPT11 = 0 Uniform upstream conditions
IOPT11 = 1 Nonuniform upstream conditions
IOPT11 = 2 Approx. upstream cond. for rotor

List of Symbols

See COMMON blocks

Theory

The upstream conditions PTABSI,TTABSI,UZABSI,BETARI, are linearly interpolated from the input data. The velocities are then calculated from the velocity triangles and the relative total enthalpy and rothalpy are given by,

\[ H_T = H - \frac{U_T^2 + V_T^2}{2} \]  \hspace{1cm} (1)

\[ I = \frac{H_T - V_B^2}{2} \]  \hspace{1cm} (2)

The component of vorticity normal to the surface is then

\[ \Omega_3 = \gamma_{13} \Omega_1 + \gamma_{23} \Omega_2 + \gamma_{33} \Omega_3 \]  \hspace{1cm} (3)
Subroutine SMTHD

Object

This subroutine smooths the input CP data

Options

IOPT7 = 0  Do not smooth data

IOPT7 > 0  Smooth data IOPT7 times

List of Symbols

See COMMON blocks

Theory

The input data is first interpolated from the input LILAST*KILAST grid to a LDL*KDL grid. Then the CP data is smoothed by averaging with its neighboring points using the formula

\[ f^L_K = \frac{f^L_{k+1} + f^L_{k-1} + f^L_k + f^L_{k+1}}{8} + \frac{f^L_k}{2} \]  

(1)
Subroutine SOLVE

Object

This subroutine calculates the geometric coordinate data and the boundary layer edge conditions for use by the UTRC boundary layer code.

Options

IOPT6 Print every IOPT6'th station
IOPT9 = 0 Output coordinates Y1 and Y2
IOPT9 = 1 Output arc lengths S1 and S2

List of Symbols

See COMMON blocks

Theory

This subroutine first calculates the computational step size in both the X1 and X2 directions. A double DO LOOP sweeps through the mesh and calls the subroutines as follows:

INTRB Establish mapping of boundaries
INTRC Establish surface geometry
METCO Calculate metric data
DIRCOS Calculate direction cosines
ROTOR Calculate upstream total enthalpy, total pressure and vorticity component normal to surface
INTRD Interpolate pressure distribution
BLEIDGE Calculate b. l. edge conditions
At each L,K mesh point the following data is written on the output files:

<table>
<thead>
<tr>
<th>IDRM</th>
<th>Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>8</td>
<td>metric data</td>
</tr>
<tr>
<td>4</td>
<td>9</td>
<td>edge conditions</td>
</tr>
<tr>
<td>5</td>
<td>10</td>
<td>transformation variables</td>
</tr>
<tr>
<td>6</td>
<td>11</td>
<td>length scales</td>
</tr>
<tr>
<td>7</td>
<td>12</td>
<td>setup code output</td>
</tr>
<tr>
<td>8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>9</td>
<td></td>
<td></td>
</tr>
<tr>
<td>10</td>
<td></td>
<td></td>
</tr>
<tr>
<td>11</td>
<td></td>
<td></td>
</tr>
<tr>
<td>12</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Subroutine UITER(Arg. List)

Object

This subroutine solves finite difference equations for the boundary layer edge velocities U1E, U2E using an iteration algorithm based on successive substitution.

Options

None

List of Symbols

A0 to A14 Coefficients of edge equations
C1 to C6 Coefficients of edge equations
B1 to B12 Coefficients of algebraic equations
L, K Index for X1 and X2

Theory

This subroutine solves a set of quadratic algebraic equations by successive substitution as described in Sec. 3.8 in Ref. 1.

References

7.0 DESCRIPTION OF BL3D CODE

7.1 BL3D Main Program

The main program for the BL3D code opens and closes all input and output files and calls the subroutines which execute the primary tasks depending on the input options described in Section 5.1. An overall view of the BL3D code is shown on the Global Tree Structure Chart shown on the following pages. This tree structure is arranged by tasks and labeled as they appear in the main program BL3D. Column 1 shows the main program which calls the subroutines in Column 2. Each subroutine in Column 2 executes a major tasks and calls the subroutine in Column 3. For any given calculation not all branches of the tree are called.
Chart II Global Tree Structure by Task

<table>
<thead>
<tr>
<th>MAIN</th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1.0</td>
<td>Open Input/Output File</td>
<td></td>
</tr>
<tr>
<td>PREP</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2.0</td>
<td>Read Input Data</td>
<td></td>
</tr>
<tr>
<td>RINPUT</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3.0</td>
<td>Initialize Parameters and Arrays</td>
<td></td>
</tr>
<tr>
<td>RINIT</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4.0</td>
<td>Start Outer Do Loop (L=1, IXEND)</td>
<td></td>
</tr>
<tr>
<td>4.01</td>
<td>Read Metric Data, Edge Conditions, and Direction Cosines</td>
<td></td>
</tr>
<tr>
<td>5.0</td>
<td>Start Inner Do Loop (K=1, IWEND)</td>
<td></td>
</tr>
<tr>
<td>5.01</td>
<td>Set Boundary Layer Edge Conditions</td>
<td></td>
</tr>
<tr>
<td>EDGE</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.02</td>
<td>Calculate Molecular Viscosity</td>
<td></td>
</tr>
<tr>
<td>MOLVIS</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.03</td>
<td>Calculate Turbulent Viscosity</td>
<td></td>
</tr>
<tr>
<td>TURBL</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5.04</td>
<td>Calculate Coefficients of P.D.E.</td>
<td></td>
</tr>
<tr>
<td>AXCOEF</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6.0</td>
<td>Start Iteration Loop to Calculate Turbulent Viscosity</td>
<td></td>
</tr>
<tr>
<td>MOLVIS</td>
<td></td>
<td></td>
</tr>
<tr>
<td>TURBL</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6.01</td>
<td>Calculate Coefficients of Matrix Equations</td>
<td></td>
</tr>
<tr>
<td>PDICOEF</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Chart II Global Tree Structure by Task (Cont'd)

<table>
<thead>
<tr>
<th>Task Number</th>
<th>Task Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>6.02</td>
<td>Set Boundary Conditions on Matrix Equations</td>
</tr>
<tr>
<td></td>
<td>BNDCND</td>
</tr>
<tr>
<td>6.03</td>
<td>Invert Matrix Equations</td>
</tr>
<tr>
<td></td>
<td>SOLVE</td>
</tr>
<tr>
<td>6.04</td>
<td>Set Solution Arrays on Inflow Plains</td>
</tr>
<tr>
<td></td>
<td>SYMSET</td>
</tr>
<tr>
<td>6.05</td>
<td>Check for Convergence</td>
</tr>
<tr>
<td>6.06</td>
<td>Calculate and Write Output Data</td>
</tr>
<tr>
<td></td>
<td>ROUTPT</td>
</tr>
<tr>
<td>6.07</td>
<td>Reinitialize Solution for Next Point</td>
</tr>
<tr>
<td></td>
<td>NEXTPT</td>
</tr>
<tr>
<td>7.0</td>
<td>End Inner Do Loop</td>
</tr>
<tr>
<td>8.0</td>
<td>End Outer Do Loop</td>
</tr>
<tr>
<td>9.0</td>
<td>Close Input/Output Files</td>
</tr>
<tr>
<td></td>
<td>POSTP</td>
</tr>
</tbody>
</table>
7.2 BL3D COMMON Block Variables

PARAMETERS

NPHI (61) Max. no. $X_2$ mesh points
NXDIM (101) Max. no. $X_1$ mesh points
NORM (201) Max. no. $X_3$ mesh points
IDRM0 (7) Printed output unit
IDRM1 (10) Coordinate and metric data input unit no.
IDRM2 (11) Boundary layer edge data input unit no.
IDRM3 (12) Direction cosines data input unit no.
IDRM4 (13) Contour and vector plot output unit no.
IDRM5 (15) Crosssection plot output unit no.

COMMON /AXCFCB/ Coefficients of Partial Differential Eqs.

AX(I) A Coefficients of partial differential eqs.
Q q Levy - Lees length scale parameter
Q0 $q_0$ Levy - lees length scale parameter at $X_2 = 0.$
GBAR(K) $\bar{\varepsilon}_{ref}$ Reference turbulent/laminar viscosity ratio

COMMON /CNTRL/ Integer Parameters

IE No. $X_3$ mesh points for energy eq.
IM (IE-1) No. $X_3$ mesh points for momentum eq.
IXEND No. $X_1$ mesh points
IWEND No. $X_2$ mesh points
ITURB Turbulence model input option
IGBAR Levy - Lees input option
IENERGY Wall boundary condition on energy eq.
ITC Flag for negative temperature
IFL Pointer for direct access files
KTC K counter for BL3D failure
KTC1 KTC - 1
KSP K counter
KSP1 KSP - 1
KSTOP Max. no. calculated X2 mesh points
NIT Iteration counter
NITCV Max. no. iterations
CONV Convergence criteria
LSTOP Max. no. calculated X1 mesh points
LINIT X1 inflow option
KINIT X2 inflow option

COMMON /EDGECB/ Boundary Layer edge Conditions

U(K) U1e X1 edge velocity
PP(K) Pe Edge static pressure
V(K) U2e X2 edge velocity
R85-956834-1

\[ \begin{align*}
\text{DVDW}(K) & : \frac{\partial u_2}{\partial x_2} \\
\text{DUDW}(K) & : \frac{\partial u_1}{\partial x_2} \\
\text{DUDX}(K) & : \frac{\partial u_1}{\partial x_1} \\
\text{DVDX}(K) & : \frac{\partial u_2}{\partial x_2}
\end{align*} \]

Velocity gradients

\[ \begin{align*}
Y1(K) & : Y_1 & & & \text{Y}_1 \text{ Cartesian coordinate} \\
Y2(K) & : Y_2 & & & \text{Y}_2 \text{ Cartesian coordinate} \\
Y3(K) & : Y_3 & & & \text{Y}_3 \text{ Cartesian coordinate} \\
\text{GAM}(I,J,K) & : \gamma_{ij} & & & \text{Direction cosines} \\
\text{HR}(K) & : H & & & \text{Rothalpy (enthalpy)}
\end{align*} \]

\text{COMMON} /\text{EWINPT}/ \text{ Input Wall Heat Transfer Variables}

\[ \begin{align*}
\text{EWIN}(K,L) & : q_w & & & \text{Wall heat flux array} \\
\text{RHWIN} & : \frac{H_w}{H_\infty} & & & \text{Wall enthalpy ratio} \\
\text{QWSIN} & : q_w & & & \text{Wall heat flux}
\end{align*} \]

\text{COMMON} /\text{FLORF}/ \text{ Reference Conditions Parameters}

\[ \begin{align*}
\text{XMA} & : M_\infty & & & \text{Reference freestream Mach no.} \\
\text{TFS} & : t_\infty & & & \text{Reference freestream static temperature} \\
\text{PFS} & : P_\infty & & & \text{Reference freestream static pressure}
\end{align*} \]
R85-956834-1

UFS $U_\infty$ Reference freestream velocity
ROFS $\rho_\infty$ Reference freestream density
AMUFS $\mu_\infty$ Reference freestream viscosity
TREF $t_{ref}$ Reference temperature
XLREF $\ell$ Reference length scale
AMURF $\mu_\infty$ Reference viscosity
RE $Re$ Reference Reynolds no.
REFS $Re_\infty$ Reference freestream Reynolds no.
R $R$ Gas constant
PR $Pr$ Prandtl number (laminar)
PRT $Pr_T$ Prandtl number (turbulent)
G $\gamma$ Ratio of specific heats
CSTAR $C^*$ Constant in Sutherland's law
R1 Not used
D Constant for isentropic flow
HO $H_{T\infty}$ Reference rothalpy
CPRIME $C'$ Constant
VK Constant
CP $C_p$ Pressure coefficient

COMMON /METCB/ Coordinate Data

H1(K) $H_1$ X metric scale coefficient
H2(K) $H_2$ X metric scale coefficient
Derivatives of metric scale coefficients

\[ \begin{align*}
\text{DH1DX}(K) &= \frac{\partial H_1}{\partial x_1} \\
\text{DH1DW}(K) &= \frac{\partial H_1}{\partial x_2} \\
\text{DH2DX}(K) &= \frac{\partial H_2}{\partial x_1} \\
\text{DH2DW}(K) &= \frac{\partial H_2}{\partial x_2}
\end{align*} \]

Covariant metric component

\[ G_{12} = \frac{\partial G_{12}}{\partial x_1} \]

Derivatives of covariant metric component

\[ \frac{\partial G_{12}}{\partial x_2} \]

Determinant of metric tensor

\[ |G| \]

COMMON /PCOEF/ Matrix Elements

\[ \begin{align*}
\text{AULF}, \text{BU1F}, \text{CU1F}, \text{BU1V}, \\
\text{BU1G}, \text{BU1T}, \text{BU2F}, \text{BU2V}, \\
\text{AU2G}, \text{BU2G}, \text{CU2G}, \text{BU2T}, \\
\text{AEF}, \text{BEF}, \text{CEF}, \text{AEG}, \\
\text{BEG}, \text{CEG}, \text{AET}, \text{BET}, \\
\text{CET}, \text{ACF}, \text{ACG}, \text{BEV}, \\
\text{DUL}, \text{DU2}, \text{DE}, \text{DC}
\end{align*} \]

COMMON /PPROCB/ Print Control Parameters

\[ \begin{align*}
\text{LPRO}(L) &= \text{L Print control array} \\
\text{KPRO}(K) &= \text{K Print control array}
\end{align*} \]
### COMMON /ROTAT/ Rotor Variables

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>RAD(K)</td>
<td>Radius</td>
</tr>
<tr>
<td>DRADX(K)</td>
<td>Derivatives of Radius</td>
</tr>
<tr>
<td>DRADW(K)</td>
<td></td>
</tr>
<tr>
<td>OMEGA</td>
<td>Rotor rotational speed</td>
</tr>
<tr>
<td>OMEGA3(K)</td>
<td>Vorticity component normal to surface</td>
</tr>
</tbody>
</table>

### COMMON /STPSIZ/ Step Size Variables

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>XII(L)</td>
<td>Levy - Lees coordinate in $X_1$ direction</td>
</tr>
<tr>
<td>DXII(L)</td>
<td>Levy - Lees step size in $X_1$ direction</td>
</tr>
<tr>
<td>DXV(L)</td>
<td>Coordinate step size in $X_1$ direction</td>
</tr>
<tr>
<td>XO</td>
<td>Virtual origin for $X_1$ direction</td>
</tr>
<tr>
<td>WV(K)</td>
<td>Coordinate in $X_2$ direction</td>
</tr>
<tr>
<td>DWV(K)</td>
<td>Coordinate step size in $X_2$ direction</td>
</tr>
<tr>
<td>Wo</td>
<td>Virtual origin for $X_2$ direction</td>
</tr>
<tr>
<td>XN(N)</td>
<td>Levy - Lees coordinate in $X_3$ direction</td>
</tr>
<tr>
<td>DN(N)</td>
<td>Levy - Lees step size in $X_3$ direction</td>
</tr>
<tr>
<td>DNI</td>
<td>Initial step size in $X_3$ direction</td>
</tr>
<tr>
<td>AK</td>
<td>Stretching parameter</td>
</tr>
</tbody>
</table>

### COMMON /TURBCB/ Turbulent Flow Variables

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>E1(K)</td>
<td>Ratio turbulent/laminar viscosity $X_1$ momentum eq.</td>
</tr>
<tr>
<td>E2(K)</td>
<td>Ratio turbulent/laminar viscosity $X_2$ momentum eq.</td>
</tr>
<tr>
<td>Symbol</td>
<td>Description</td>
</tr>
<tr>
<td>--------</td>
<td>--------------------------------------------------</td>
</tr>
<tr>
<td>E3(K)</td>
<td>$1 + \frac{P_r}{P_T} \frac{E}{\nu}$ Ratio turbulent/laminar viscosity energy eq.</td>
</tr>
<tr>
<td>EM(K)</td>
<td>$\frac{E}{\nu}$ Ratio eddy/laminar viscosity</td>
</tr>
<tr>
<td>XT1</td>
<td>$X_{T1}$ Start of transition</td>
</tr>
<tr>
<td>XT2</td>
<td>$X_{T2}$ End of transition</td>
</tr>
<tr>
<td>CISO</td>
<td>$C_{S0}$ Ratio $E_2/E_1$</td>
</tr>
<tr>
<td>XTRAN</td>
<td>$X_T$ Transition coordinate length</td>
</tr>
</tbody>
</table>

**COMMON /VELL/ Boundary Layer Edge Parameters**

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>VCAP</td>
<td>$U_{1e}$ $X_1$ edge velocity</td>
</tr>
<tr>
<td>TCAP</td>
<td>$T_e$ Edge static temperature</td>
</tr>
<tr>
<td>CVCAP</td>
<td>$U_{2e}$ $X_2$ edge velocity</td>
</tr>
<tr>
<td>PCAP</td>
<td>$P_e$ Edge static pressure</td>
</tr>
<tr>
<td>DTCDX</td>
<td>$\partial T_e/\partial x_1$ Derivatives of edge temperature</td>
</tr>
<tr>
<td>DTCDW</td>
<td>$\partial T_e/\partial x_2$ Derivatives of edge temperature</td>
</tr>
<tr>
<td>DVCDX</td>
<td>$\partial U_{1e}/\partial x_1$ Derivatives of $X_1$ edge velocity</td>
</tr>
<tr>
<td>DVCDW</td>
<td>$\partial U_{1e}/\partial x_2$ Derivatives of $X_1$ edge velocity</td>
</tr>
<tr>
<td>DCCDX</td>
<td>$\partial U_{2e}/\partial x_1$ Derivatives of $X_1$ edge velocity</td>
</tr>
<tr>
<td>DCCDW</td>
<td>$\partial U_{2e}/\partial x_2$ Derivatives of $X_1$ edge velocity</td>
</tr>
<tr>
<td>DPCDX</td>
<td>$\partial c_p/\partial x_1$ Derivatives of static pressure</td>
</tr>
<tr>
<td>DPCDW</td>
<td>$\partial c_p/\partial x_2$ Derivatives of static pressure</td>
</tr>
<tr>
<td>VR</td>
<td>$U_{ref}$ Reference edge velocity</td>
</tr>
<tr>
<td>DVRDX</td>
<td>$\partial U_{ref}/\partial x_1$ Derivatives of reference edge velocity</td>
</tr>
<tr>
<td>DVRDW</td>
<td>$\partial U_{ref}/\partial x_2$ Derivatives of reference edge velocity</td>
</tr>
</tbody>
</table>
R85-956834-1

HE $H_{Te}$ Edge rothalpy

DHEDX $\frac{\partial H_{Te}}{\partial X_1}$ Derivatives of edge rothalpy

DHEDW $\frac{\partial H_{Te}}{\partial X_2}$

ROCAP $\rho_e$ Edge density

ROMU $L$ Edge Levy - Lees parameter

AMUE $\frac{\mu_e}{u_{ref}}$ Edge viscosity

DCCDWX $\frac{\partial^2 U_2 e}{\partial X_1 \partial X_2}$ Limiting derivative at symmetry boundary

COMMON /VISC/ Dependent Variables

VIS(N) $L$ Levy - Lees stretching function

V2(N) $V_{I K}^L$ Normal velocity ratio

V3(N) $V_{I K-1}^L$ Normal velocity ratio

F3N(N) $(\frac{\partial F}{\partial \xi_3})_{K-1}^L$ Derivative of $X_1$ velocity ratio

G3N(N) $(\frac{\partial G}{\partial \xi_3})_{K-1}^L$ Derivative of $X_2$ velocity ratio

F2(N) $F_{I K}^L$ $X_1$ velocity ratio

G2(N) $G_{I K}^L$ $X_2$ velocity ratio

T2(N) $T_{I K}^L$ Static temperature ratio

F2N(N) $(\frac{\partial F}{\partial \xi_3})_K^L$ Derivative of $X_1$ velocity ratio

G2N(N) $(\frac{\partial G}{\partial \xi_3})_K^L$ Derivative of $X_2$ velocity ratio

F1(N) $F_{I K}^{L-1}$ $X_1$ velocity ratio

G1(N) $G_{I K}^{L-1}$ $X_2$ velocity ratio
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F_1(N)$</td>
<td>$(\partial F/\partial \xi_3)_K^{L-1}$ Derivative of $X_1$ velocity ratio</td>
</tr>
<tr>
<td>$G_1(N)$</td>
<td>$(\partial G/\partial \xi_3)_K^{L-1}$ Derivative of $X_2$ velocity ratio</td>
</tr>
<tr>
<td>$Y(N)$</td>
<td>$Y_3$                               Distance from wall</td>
</tr>
<tr>
<td>$F_3(N)$</td>
<td>$F_{s,K-1}^L$                        $X_1$ velocity ratio</td>
</tr>
<tr>
<td>$G_3(N)$</td>
<td>$G_{s,K-1}^L$                        $X_2$ velocity ratio</td>
</tr>
<tr>
<td>$TT_1(N)$</td>
<td>$H_{s,k}^{L-1}$                      Total enthalpy ratio</td>
</tr>
<tr>
<td>$TT_2(N)$</td>
<td>$H_{s,k}^L$                          Total enthalpy ratio</td>
</tr>
<tr>
<td>$TT_3(N)$</td>
<td>$H_{s,K-1}^L$                        Total enthalpy ratio</td>
</tr>
<tr>
<td>$TT_1(N)$</td>
<td>$(\partial H/\partial \xi_3)_K^{L-1}$ Derivative of total enthalpy ratio</td>
</tr>
<tr>
<td>$TT_2(N)$</td>
<td>$(\partial H/\partial \xi_3)_K^L$   Derivative of total enthalpy ratio</td>
</tr>
<tr>
<td>$TT_3(N)$</td>
<td>$(\partial H/\partial \xi_3)_{s,K-1}^L$ Derivative of total enthalpy ratio</td>
</tr>
<tr>
<td>$TT_4(N)$</td>
<td>$(\partial H/\partial \xi_3)_{s,K+1}^{L-1}$ Derivative of total enthalpy ratio</td>
</tr>
<tr>
<td>$F_4(N)$</td>
<td>$F_{s,K+1}^L$                        $X_1$ velocity ratio</td>
</tr>
<tr>
<td>$G_4(N)$</td>
<td>$G_{s,K+1}^L$                        $X_2$ velocity ratio</td>
</tr>
<tr>
<td>$V_4(N)$</td>
<td>$V_{s,K+1}^{L-1}$                    Normal velocity ratio</td>
</tr>
</tbody>
</table>
7.3 Description of BL3D Subroutines

AXCOEF Calculate coefficients of differential eqs.

BNDCND Set boundary conditions for matrix eqs.

EDGE Set boundary layer edge conditions

MAIN Main program

MOLVIS Calculate Levy-Lees function

NEXTPT Reinitialize solution arrays for next point

PDCOEF Calculate coefficients of matrix equations

POSTP Close input/output files

PREP Open input/output files

RINIT Initialize parameters and arrays

RINPUT Read input data

ROUTPT Calculate and write output data

SOLVE Invert matrix equations

SYMSET Set solution arrays at starting planes

TURBL Calculate turbulent viscosity

VII-13
Subroutine BNDCND(Arg. List)

Object

This subroutine sets the boundary conditions on the matrix equations.

Options

KINIT = 0  Local similarity start at X2 = 0.0
KINIT = 1  Plane of symmetry start at X2 = 0.0
IERNGY = 0  Specify wall temperature
IERNGY = 1  Specify wall heat flux

List of Symbols

EIE  Edge value of total enthalpy function
EW  Wall value of total enthalpy function
EWP  Wall value of enthalpy derivative function
FIE  Edge value of X1 velocity function
GIE  Edge value of X2 velocity function
L , K  Index for X1 and X2 respectively

Theory

The boundary conditions are given Sect. 3.6 of Ref. 1. At the edge of the boundary layer the conditions are:

\[ F_e = 1.0 \]  (1)

\[ H_e = 1.0 \]  (2)

\[ G_e = \frac{U_3}{U_{ref}} \]  (3)
At the wall the conditions are

\[ G_e = 1.0 \quad \text{if } KINIT=1 \text{ and } K=1 \]  
\[ H_e = (T_w/T_\infty)H_{T\infty}/H_{Te} \quad \text{if } IENERGY=0 \]

\[ \frac{\partial H}{\partial \xi_e} = \frac{-\alpha_w \xi_e^2 \sqrt{2 \xi_e/R_e}}{H_{T\infty} U_\infty^2 \left( \frac{\rho_w u_w}{\rho_e u_e} \left( \rho_e u_e \right)^2 \right)^{1/2}} \quad \text{if } IENERGY = 1 \]

References

Subroutine EDGE(Arg. List)

Object

This subroutine sets the boundary layer edge conditions.

Options

LINIT = 0  Local similarity start at X1 = 0.0
LINIT = 1  Flat plate similarity start at X1 = 0.0
LINIT = 2  Stagnation point similarity start at X1 = 0.0
LINIT = 3  Input profiles (not programmed)
KINIT = 0  Local similarity start at X2 = 0.0
KINIT = 1  Plane of symmetry start at X2 = 0.0
KINIT = 2  Input profiles (not programmed)

List of Symbols

See COMMON blocks

Theory

Given $U_{1e}$, $U_{2e}$, $I_e$, and $P_e$, the remaining edge conditions are given as follows

$$V_B = R\Omega$$  \hspace{1cm} (1)

$$H_{Te} = I_e + \frac{V_B^2}{2}$$  \hspace{1cm} (2)

$$U_e^2 = U_{1e}^2 + U_{2e}^2 + 2U_{1e}U_{2e}G_{12}/(H_1H_2)$$  \hspace{1cm} (3)

$$T_e = \frac{\gamma - 1}{\gamma} [H_{Te} - \frac{U_e^2}{2}]$$  \hspace{1cm} (4)

$$P_e = P_e/T_e$$  \hspace{1cm} (5)
where the derivatives of the edge conditions are obtained by differentiating Eqs. 1 through 5. The reference conditions are set as follows:

\[ U_{\text{ref}} = U_{1e} \quad \text{KINIT=1} \quad (6) \]

\[ U_{\text{ref}} = U_{2e} \quad \text{KINIT=1, K=1} \quad (7) \]

The edge viscosity is obtained from Sutherland's law.

\[ \mu_e = T_e^{3/2} \left( \frac{1 + C'}{T_e + C'} \right) \quad (8) \]
Object

This subroutine calculates the Levy-Lees variable and the static temperature.

Options

None

List of Variables

UTESQ $u_e^2$ Velocity squared

X Not used

Theory

The total velocity is given by:

$$U_e^2 = (U_{1e} F)^2 + (U_{ref} G)^2 + 2(U_{1e} F)(U_{ref} G) \frac{G_{12}}{(H_1 H_2)} \tag{1}$$

Then the static temperature is given by

$$\Xi = \frac{\gamma - 1}{Y} \frac{1}{T_e} \left[H_{Te} H - U_e^2/2\right] \tag{2}$$

and the Levy-Lees function is calculated from Sutherland's viscosity law where the static pressure is constant in the boundary layer

$$L = \frac{\partial w}{\partial \rho_e u_e} = \zeta^{1/2} \frac{1 + \zeta}{\zeta + \zeta}$$

A check is made on the static temperature during the iteration.

If $\Xi > 0.0$ then $ITC = 0$

If $\Xi < 0.0$ then $ITC = 1$
Subroutine NEXTPT(K,L,IFLAG)

Object

This subroutine reinitializes the solution arrays for the next point.

Options

IFLAG = 0 The solution has converged
IFLAG = 1 The solution has not converged
KINIT = 1 Plane of symmetry start on X2 = 0.0

List of Symbols

KSP K
KTC K counter for convergence failure
KTCl KTC - 1
KSP1 KSP - 1
IFL Record counter

Theory

This subroutine writes the current solution on Unit 8 and reads the appropriate record from Unit 8 to set up the solution arrays at the next point. The record counter IFL is reset to IFL=1 each time L is indexed. Let us define the following vector arrays each representing one record.

\[
\begin{align*}
\mathbf{f}(L,K-1) &= \left( H(N), F(N), G(N), V(N) \right)_{K-1}^{L} \quad N=1,IE \\
\mathbf{f}(L,K) &= \left( H(N), F(N), G(N), V(N) \right)_{K}^{L} \quad N=1,IE \\
\mathbf{f}(L-1,K) &= \left( H(N), F(N), G(N), V(N) \right)_{K}^{L-1} \quad N=1,IE \\
\mathbf{f}(L-1,K+1) &= \left( H(N), F(N), G(N), V(N) \right)_{K+1}^{L-1} \quad N=1,IE
\end{align*}
\]

The Unit contains the following records (see Fig. 1):

\[
\begin{align*}
\text{for IFL} = 1,K & \quad \left\{ \mathbf{f}(L,K) \right\} \\
\text{for IFL} = K+1,KSP & \quad \left\{ \mathbf{f}(L-1,K) \right\}
\end{align*}
\]
where KSP < IWEND. Hence to update the arrays we have:

\[
\begin{align*}
    f_1 &= f_2 = f(IFL) \\
    f_3 &= f(IFL+1) \quad 1 < K < KSP \\
    f_4 &= f(IFL+2) \\
    f_1 &= \text{not needed} \\
    f_3 &= f(1) \quad K = 1 \\
    f_4 &= f(2)
\end{align*}
\]

After the new arrays are set, the normal derivative of the dependent variables are calculated numerically.
Subroutine PDCOEF(L,K,PR)

Object
This subroutine calculates the coefficients of the matrix equations.

Options
None

List of Symbols
AU1F,BU1F,CU1F, Coeff. of X1 momentum eq.
BU1V,BU1G,BU1T,
DU1

BU2F,BU2V,AU2G, Coeff. of X2 momentum eq.
BU2G,CU2G,BU2T,
DU2

AEF,BEF,CEF, Coeff. of energy eq.
BEV,AEG,BEG,
CEG,AET,BET
CEG,DE

ACF,ACG,DC Coeff. of continuity eq.

Theory
In this subroutine the equations of motion are quasi-linearized and
discretized to form a set of matrix equations as outlined in Section 3.9 of Ref.
1.

References
1. Anderson, O. L.: Assessment of a 3-D Boundary Layer Code to Predict Heat
Subroutine POSTP

Object

This subroutine closes all input/output files.

Options

None

List of Symbols

See COMMON blocks

Theory

See Sect. 5.3 for a description of all input/output files for the three dimensional boundary layer code.
Subroutine PREP

Object

This subroutine opens all input/output files.

Options

None

List of Symbols

See COMMON blocks

Theory

See Sect. 5.3 for a description of all input/output files for the three
dimensional boundary layer code.
From Sutherland's law we have

\[ \nu_{\text{ref}} = 2.27 \times 10^{-8} \frac{t_{\text{ref}}}{(t_{\text{ref}} + C^*)} \]  
\[ \nu_\infty = 2.27 \times 10^{-8} \frac{t_\infty}{(t_\infty + C^*)} \]  

The reference total temperature and total enthalpy are

\[ t_{T\infty} = t_\infty \left[ 1 + \frac{\gamma - 1}{2} \frac{M_\infty^2}{t_\infty} \right] \]  
\[ H_{T\infty} = \frac{\gamma}{\gamma - 1} \frac{t_\infty}{t_{\text{ref}}} \]  

and the reference Reynolds numbers are given by

\[ R_{\text{e}} = U_\infty \rho_\infty l / \nu_{\text{ref}} \]  
\[ R_{\text{e}_\infty} = U_\infty \rho_\infty l / \nu_\infty \]
Subroutine RINPUT

Object

This subroutine reads input parameters and flow conditions.

Options

None

List of Symbols

See COMMON blocks

Theory

See Sect. 5.1 for input variables used.
Subroutine ROUTPT

Object

This subroutine calculates output data in an intrinsic coordinate system aligned to the freestream flow direction.

Options

IERNGY = 0  Specify wall temperature
IERNGY = 1  Specify wall heat flux

List of Symbols

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>US(N)</td>
<td>$U_s$</td>
</tr>
<tr>
<td>UC(N)</td>
<td>$U_c$</td>
</tr>
<tr>
<td>UN(N)</td>
<td>$U_n$</td>
</tr>
<tr>
<td>UT(N)</td>
<td>$U_T$</td>
</tr>
<tr>
<td>ALPC(N)</td>
<td>$\alpha_c$</td>
</tr>
<tr>
<td>ES(N)</td>
<td>$e_s$</td>
</tr>
<tr>
<td>EC(N)</td>
<td>$e_c$</td>
</tr>
<tr>
<td>EN(N)</td>
<td>$e_T$</td>
</tr>
<tr>
<td>TS(N)</td>
<td>$\tau_s$</td>
</tr>
<tr>
<td>TC(N)</td>
<td>$\tau_c$</td>
</tr>
<tr>
<td>ALP(N)</td>
<td>$\alpha$</td>
</tr>
<tr>
<td>THE</td>
<td>$\theta$</td>
</tr>
<tr>
<td>UT1E</td>
<td>$U_{T1e}$</td>
</tr>
<tr>
<td>UN1E</td>
<td>$U_{N1e}$</td>
</tr>
<tr>
<td>ALPE</td>
<td>$\alpha_e$</td>
</tr>
<tr>
<td>-------</td>
<td>-----------</td>
</tr>
<tr>
<td>UTE</td>
<td>$U_{Te}$</td>
</tr>
<tr>
<td>UT1</td>
<td>$U_{T1}$</td>
</tr>
<tr>
<td>UN1</td>
<td>$U_{N1}$</td>
</tr>
<tr>
<td>E13</td>
<td>$e_{13}$</td>
</tr>
<tr>
<td>E23</td>
<td>$e_{23}$</td>
</tr>
<tr>
<td>ET1</td>
<td>$e_{T1}$</td>
</tr>
<tr>
<td>EN1</td>
<td>$e_{N1}$</td>
</tr>
<tr>
<td>ET</td>
<td>$e_T$</td>
</tr>
<tr>
<td>ALPEE</td>
<td>$\alpha_{ee}$</td>
</tr>
<tr>
<td>ALPEC</td>
<td>$\alpha_{ec}$</td>
</tr>
<tr>
<td>T13</td>
<td>$\tau_{13}$</td>
</tr>
<tr>
<td>T23</td>
<td>$\tau_{23}$</td>
</tr>
<tr>
<td>TAUT1</td>
<td>$\tau_{T1}$</td>
</tr>
<tr>
<td>TAUN1</td>
<td>$\tau_{N1}$</td>
</tr>
<tr>
<td>TAU</td>
<td>$\tau$</td>
</tr>
<tr>
<td>ALPT</td>
<td>$\alpha_T$</td>
</tr>
<tr>
<td>ALPC</td>
<td>$\alpha_c$</td>
</tr>
<tr>
<td>DY3</td>
<td>$\Delta Y_3$</td>
</tr>
<tr>
<td>Symbol</td>
<td>Definition</td>
</tr>
<tr>
<td>--------</td>
<td>-----------------------------------------------</td>
</tr>
<tr>
<td>DELS</td>
<td>$\delta_s/\ell$ Streamwise displacement thickness</td>
</tr>
<tr>
<td>DELC</td>
<td>$\delta_c/\ell$ Crossflow displacement thickness</td>
</tr>
<tr>
<td>DELUS</td>
<td>$\delta_{us}/\ell$ Streamwise velocity thickness</td>
</tr>
<tr>
<td>DELUC</td>
<td>$\delta_{uc}/\ell$ Crossflow velocity thickness</td>
</tr>
<tr>
<td>THETSS</td>
<td>$\theta_{ss}/\ell$ Streamwise momentum thickness</td>
</tr>
<tr>
<td>THETCC</td>
<td>$\theta_{cc}/\ell$ Crossflow momentum thickness</td>
</tr>
<tr>
<td>THETSC</td>
<td>$\theta_{sc}/\ell$ $U_c \Delta U_s$ momentum thickness</td>
</tr>
<tr>
<td>THETCS</td>
<td>$\theta_{w}/\ell$ $U_s \Delta U_c$ momentum thickness</td>
</tr>
<tr>
<td>THETHS</td>
<td>$\theta_{HS}/\ell$ Streamwise enthalpy thickness</td>
</tr>
<tr>
<td>THETHC</td>
<td>$\theta_{HC}/\ell$ Crosswise enthalpy thickness</td>
</tr>
<tr>
<td>THETDS</td>
<td>$\theta_{DS}/\ell$ Streamwise dissipation thickness</td>
</tr>
<tr>
<td>THETDC</td>
<td>$\theta_{DC}/\ell$ Crosswise dissipation thickness</td>
</tr>
<tr>
<td>HSS</td>
<td>$H_{SS}$ Shape factor</td>
</tr>
<tr>
<td>YEDGE</td>
<td>$\delta$ Edge of boundary layer</td>
</tr>
<tr>
<td>CFS</td>
<td>$C_{fs}$ Streamwise wall friction coefficient</td>
</tr>
<tr>
<td>CFC</td>
<td>$C_{fc}$ Crossflow wall friction coefficient</td>
</tr>
<tr>
<td>QW</td>
<td>$Q_w$ Wall heat flux</td>
</tr>
<tr>
<td>ST</td>
<td>$S_t$ Stanton number</td>
</tr>
<tr>
<td>TWAD</td>
<td>$T_a$ Adiabatic wall temperature</td>
</tr>
<tr>
<td>TW</td>
<td>$T_w$ Wall temperature</td>
</tr>
<tr>
<td>RECFAC</td>
<td>$R_{ec}$ Recovery factor</td>
</tr>
</tbody>
</table>
VIE, V2E $V_1, V_2$ Cartesian components of edge velocity

BETAE $\beta_e$ Flow angle at the edge relative to $Y_1$

BETAW $\beta_w$ Flow angle at the wall relative to $Y_2$

EPS1W $\epsilon_{1W}$ $Y_1$ component of wall rate of strain

EPS2W $\epsilon_{2W}$ $Y_2$ component of wall rate of strain

E131 $\epsilon_{13W}$ E13 at the wall

E231 $\epsilon_{23W}$ E23 at the wall

BET1, BET2 $\beta_1, \beta_2$ Characteristic directions

**Theory**

Consider a vector $\mathbf{A}$ in a nonorthogonal coordinate system $(X_1, X_2, X_3)$ with the corresponding unit vectors $(\hat{n}_1, \hat{n}_2, \hat{n}_3)$. Then, neglecting the normal component, we have for the contravariant components:

$$\mathbf{A} = A^1 \hat{n}_1 + A^2 \hat{n}_2 + 0 \hat{n}_3$$

(1)

The angle between $A^1$ and $A^2$ is given by

$$\cos \theta = G_{12} / (H_1 H_2)$$

(2)

Let use now resolve the vector in components tangent to $\hat{n}_1$ and normal to $\hat{n}_1$.

$$\mathbf{A} = A_T \hat{n}_1 + A_N (\hat{n}_1 \times \hat{n}_3) + 0 n$$

(3)

Clearly as shown in Fig. 1 we have:

$$A_T = A^1 + A^2 \cos \theta$$

(4)

$$A_N = (A^2 + \sin \theta)$$

(5)
\[
|\vec{A}| = (A_T^2 + A_N^2)^{1/2}
\]  
(6)

\[
\alpha = \tan \left( \frac{A_N}{A_T} \right)
\]  
(7)

Let us now define an intrinsic coordinate system referenced to the freestream direction. Then applying the above formulas for \( \vec{A} = \vec{U} \) we have:

\[
U_{Te} = U_{le} + U_{2e} \cos \theta
\]  
(8)

\[
U_{Ne} = U_{2e} \sin \theta
\]  
(9)

\[
U_{e} = (U_{T}^2 + U_{N}^2)^{1/2}
\]  
(10)

\[
\alpha_{e} = \tan \left( \frac{U_{Ne}}{U_{Te}} \right)
\]  
(11)

Then for any velocity in the boundary layer we have:

\[
U_{T1} = U_{1} + U_{2} \cos \theta
\]  
(12)

\[
U_{N1} = U_{2} \sin \theta
\]  
(13)

\[
U_{T} = (U_{T1}^2 + U_{N1}^2)^{1/2}
\]  
(14)

\[
\alpha = \tan \left( \frac{U_{N1}}{U_{T1}} \right)
\]  
(15)

Hence the angle between the local flow direction and the free stream flow direction is:

\[
\alpha_c = \alpha - \alpha_{e}
\]  
(16)

and the velocity components tangent and normal to the freestream direction are:
\[ U_s = U_T \cos \alpha_c \] (17)
\[ U_c = U_T \sin \alpha_c \] (18)

For the rate of strain components and rate of stress components we form the vectors

\[ \dot{\lambda} = \dot{E} \circ n_3^* = e_{13} \vec{n}_1 + e_{23} \vec{n}_2 \] (19)
\[ \dot{\lambda} = \vec{\tau} \circ \vec{n}_3 = \tau_{13} \vec{n}_1 + \tau_{23} \vec{n}_2 \] (20)

where the components are given by

\[ C_0 = \sqrt{Re} \rho_e U_{le} H_2 / \sqrt{2} \xi_1 \] (21)
\[ C_1 = C_0 / Re u_0 / u_{ref} \varepsilon_{ref} \xi \] (22)
\[ e_{13} = C_0 U_{le} \rho / \rho_e \partial \Phi / \partial \xi_3 \] (23)
\[ e_{23} = C_0 U_{le} \rho / \rho_e \partial G / \partial \xi_3 \] (24)
\[ \tau_{13} = C_1 U_{le} \varepsilon_{1} / \varepsilon_{ref} \partial \Phi / \partial \xi_3 \] (25)
\[ \tau_{23} = C_1 U_{ref} \varepsilon_{1} / \varepsilon_{ref} \partial G / \partial \xi_3 \] (26)
and apply the same formula. With the flow angles determined, the characteristic directions are given by:

\[ \beta_1 = \text{MAX}(\alpha_c) \]  

\[ \beta_2 = \text{MIN}(\alpha_c) \]  

The boundary layer integral parameters are defined relative to the intrinsic coordinates and are given by:

\[ dY_3 = \frac{1}{C_o} \frac{\rho}{\rho_e} d\xi_e \]  

\[ \frac{\delta_e^*}{\lambda} = \int \left[ 1 - \frac{\rho U_s}{\rho_e U_e} \right] dY_3 \]  

\[ \frac{\delta_c^*}{\lambda} = -\int \left[ \frac{\rho U_c}{\rho_e U_e} \right] dY_3 \]  

\[ \frac{\delta_{US}^*}{\lambda} = \int \left[ 1 - \frac{U_s}{U_e} \right] dY_3 \]  

\[ \frac{\delta_{UC}^*}{\lambda} = -\int \left[ 1 - \frac{U_c}{U_e} \right] dY_3 \]  

\[ \theta_{ss}/\lambda = \int \frac{\rho U_s}{\rho_e U_e} \left[ 1 - \frac{U_s}{U_e} \right] dY_3 \]
\[ \frac{\theta_{cc}}{\ell} = -\int \frac{\rho U_a}{\rho U_e} \frac{U_c}{U_e} \, dY_3 \]  
\[ \frac{\theta_{sc}}{\ell} = \int \frac{\rho U_a}{\rho U_e} \left[ 1 - \frac{U_a}{U_e} \right] \, dY_3 \]  
\[ \frac{\theta_{cs}}{\ell} = \int \frac{\rho U_a}{\rho U_e} \frac{U_c}{U_e} \, dY_3 \]  
\[ \frac{\theta_{HS}}{\ell} = \int \frac{\rho U_a}{\rho U_e} \left[ 1 - \left( \frac{U_a}{U_e} \right)^2 \right] \, dY_3 \]  
\[ \frac{\theta_{HC}}{\ell} = \int \frac{\rho U_a}{\rho U_e} \left( \frac{U_c}{U_e} \right)^2 \, dY_3 \]  
\[ \frac{\theta_{DS}}{\ell} = \int \frac{\tau_s}{\rho U_e} \frac{e_s}{U_e} \, dY_3 \]  
\[ \frac{\theta_{DC}}{\ell} = \int \frac{\tau_c}{\rho U_e} \frac{e_c}{U_e} \, dY_3 \] 

The wall friction coefficients are given by

\[ C_{fs} = 2 \frac{\tau_{sw}}{(\rho U_e)^2} \]  
\[ C_{fc} = 2 \frac{\tau_{cw}}{(\rho U_e)^2} \]
and the Stanton number by

$$S_t = Q_w / (T_a - T_w)$$

(44)

where

$$Q_w = \frac{\gamma - 1}{\gamma} \frac{C_o}{R_e P_r} \left( \frac{\rho_e \mu_e}{\rho_e} \right) H_{Te} \left( \frac{u_e}{u_{ref}} \right) \left( \frac{\partial H}{\partial \xi_3} \right)_w$$

(45)

The projection of the velocity vector on the Y3 plane are:

$$V_{1e} = \gamma_{11} U_{1e} + \gamma_{21} U_{2e}$$

(46)

$$V_{2e} = \gamma_{12} U_{1e} + \gamma_{22} U_{2e}$$

(47)

The limiting wall streamline is defined by

$$\lim_{Y_3 \to 0} \frac{V_{2e}}{V_{1e}} = \frac{\varepsilon_{2w}}{\varepsilon_{1w}}$$

(48)

hence

$$\varepsilon_{1w} = \gamma_{11} \varepsilon_{13w} + \gamma_{21} \varepsilon_{23w}$$

(49)

$$\varepsilon_{2w} = \gamma_{12} \varepsilon_{13w} + \gamma_{22} \varepsilon_{23w}$$

(50)

$$\beta_w = \tan^{-1} \left( \frac{\varepsilon_{2w}}{\varepsilon_{1w}} \right)$$

(51)
Subroutine SOLVE(Arg. list)

Object

Solve a set of three second order and one first order partial differential
equations forming a block tri-diagonal matrix.

Options

IERNGY = 0  Specify wall temperature
IERNGY = 1  Specify wall heat flux

List of Symbols

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>EIE</td>
<td>Edge value of total enthalpy function</td>
</tr>
<tr>
<td>EW</td>
<td>Wall value of total enthalpy function</td>
</tr>
<tr>
<td>EWP</td>
<td>Wall value of enthalpy derivative function</td>
</tr>
<tr>
<td>FIE</td>
<td>Edge value of X1 velocity function</td>
</tr>
<tr>
<td>GIE</td>
<td>Edge value of X2 velocity function</td>
</tr>
<tr>
<td>A1F, B1F, C1F,</td>
<td></td>
</tr>
<tr>
<td>B1V, B1G, B1T,</td>
<td></td>
</tr>
<tr>
<td>D1</td>
<td>Coeff. of X1 momentum eq.</td>
</tr>
<tr>
<td>B2F, B2V, A2G,</td>
<td></td>
</tr>
<tr>
<td>D2</td>
<td>Coeff. of X2 momentum eq.</td>
</tr>
<tr>
<td>AEF, BEF, CEF,</td>
<td></td>
</tr>
<tr>
<td>BEV, AEG, BEG,</td>
<td></td>
</tr>
<tr>
<td>CEG, AET, BET,</td>
<td></td>
</tr>
<tr>
<td>CET, DE</td>
<td>Coeff. of energy eq.</td>
</tr>
<tr>
<td>ACF, ACG, DC</td>
<td>Coeff. of continuity eq.</td>
</tr>
<tr>
<td>PF, QF, RF, SF, TF,</td>
<td></td>
</tr>
<tr>
<td>PG, QG, RG, SG, TG,</td>
<td></td>
</tr>
<tr>
<td>PE, QE, RE, SE, TE</td>
<td>Coeff. of upper triangular matrix</td>
</tr>
</tbody>
</table>
Theory

The block tri-diagonal matrix is reduced to the upper triangular matrix using block factorization in which the continuity equation is eliminated from the matrix reduction by direct substitution. The center block is inverted using Cramer's rule. The reduction process starts at the outer edge \((N = IE)\) where the boundary conditions are known explicitly and continue to \((N=1)\) where the derivative boundary condition is evaluated. In the backward substitution the coefficients for the normal velocity are evaluated from the other coefficients.
Subroutine TURBL(K,L,X,ICNTRL)

Object

This subroutine calculates the turbulent viscosity and the turbulent Levy-Lees parameter.

Options

ICNTRL = 0 Not used at the present time
    = 1
ITURB = 0 Laminar flow
    = 1 Turbulent/transitional flow
IGBAR = 0 Laminar Levy-Lees variables
    = 1 Turbulent Levy-Lees variables

List of Symbols

BET \( X_3 \) \( X_3 \) Distance normal to wall
EMO \( \epsilon_0/\mu \) Eddy viscosity outer layer
L, K \( X_1 \) \( X_1 \) coordinate distance
X \( X_T \) Intermittancy factor

Theory

A detailed description of the turbulence model is given in Sect. 3.7 of Ref. 1. The basic turbulence model is that developed by Cebeci and Smith Ref. 2. Then in Levy-Lees variables we have the distance normal to the wall is given by
The outer layer eddy viscosity is then given by

\begin{equation}
\frac{\varepsilon_0}{\mu} = X \frac{\sqrt{R_e} \left( \sqrt{2} \xi_1 / H_1 \right)}{\left[ \Xi L \left( u_e / u_{ref} \right) \right]} X_3 (\xi)
\end{equation}

where the terms in the brackets are coded as local variables. For the inner layer, the eddy viscosity is

\begin{equation}
\frac{\varepsilon_i}{\mu} = L^2 \left| \frac{dU}{d\xi_3} \right|
\end{equation}

where the mixing length is given by

\begin{equation}
L^2 = \left[ \frac{\Xi^2 (\sqrt{2} \xi_1 / H_1) X_3^2}{\Xi L u_e / u_{ref}} \right] D^2
\end{equation}

and the damping factor by

\begin{equation}
D = 1 - \exp \left\{ \frac{-X_2}{26 \left( \Xi L u_e / u_{ref} \right)} \left[ \sqrt{\frac{\Xi^2 (\sqrt{2} \xi_1 / H_1)}{L u_e u_{ref}}} \left| \frac{dU}{d\xi_3} \right| \right] \right\}
\end{equation}
The Clauser outer layer constant is usually taken to be
\[ \chi = 0.0168 \]  
(6)
and the Prandtl constant by
\[ K = 0.4357 \]  
(7)
The eddy viscosity is then given by
\[ \frac{\varepsilon}{\mu} = \frac{\varepsilon_i}{\mu} X_T \text{ if } \frac{\varepsilon_i}{\mu} < \frac{\varepsilon_o}{\mu} \]
\[ = \frac{\varepsilon_o}{\mu} X_T \text{ if } \frac{\varepsilon_i}{\mu} > \frac{\varepsilon_o}{\mu} \]  
(8)
where \( X_T \) is the intermittancy factor derived from Dhawan and Narasimha, Ref. 3.
\[ X_T = \{ 1 - \exp \left[ -4.6513 \left( \frac{X - X_{i1}}{X_{T2} - X_{T1}} \right)^2 \right] \} \]  
(9)
The turbulent Levy-Lees parameter is then determined by the eddy viscosity in the outer layer
\[ \bar{\varepsilon}_{\text{ref}} = \begin{cases} 1 & \text{IGBAR} = 0 \\ 1 + \frac{\varepsilon_o}{\mu} X_T & \text{IGBAR} = 1 \end{cases} \]  
(10)
References


LIST OF SYMBOLS

\( a_n, c_n \) Coefficients of boundary edge equations

\( A_n, K_n \) Coefficients of boundary layer equations

\( c_p, c_v \) Specific heats

\( C_f \) Wall friction coefficient

\( C_p \) Pressure coefficient

\( \varepsilon_i \) Unit vectors Cartesian coordinates

\( F \) \( X_1 \) velocity ratio \( \left( \frac{u_1}{u_{1e}} \right) \)

\( g_{ij}, G_{ij} \) Covariant metric tensor components \( \left( g_{ij}/l^2 \right) \)

\( G \) \( X_2 \) velocity ratio \( \left( \frac{u_2}{u_{ref}} \right) \)

\( h_i, H_i \) Metric scale coefficients \( \left( \frac{h_i}{l} \right) \)

\( h, H \) Static enthalpy \( \left( \frac{h}{u_\infty^2} \right) \)

\( h_T, H_T \) Total enthalpy \( \left( \frac{h_T}{u_\infty^2} \right) \)

\( H \) Total enthalpy ratio \( \left( \frac{h_T}{h_{Te}} \right) \)

\( i, I \) Rothalpy \( \left( \frac{i}{u_\infty^2} \right) \)

\( k \) Thermal conductivity

\( l \) Reference length

\( L \) Levy - Lees parameter \( \left( \frac{\rho \mu}{\rho_e \mu_e} \right) \)
Mach number

Unit vectors surface coordinates

Static pressure

Total pressure

Prandtl number laminar/turbulent

Levy - Lees length scale parameter

Radius

Reynolds number

Gas constant

Arc length distance

Stanton number

Static temperature

Velocity components surface coor.

Axial velocity

Radial velocity

Tangential velocity

X₂ reference velocity

Velocity components Cartesian coor.

X₃ reduced velocity

Rotor velocity

(\rho/\rho_\infty u_\infty^2)

(p_T/\rho_\infty u_\infty^2)

(c_p \mu/k)

(r/1)

(\rho_\infty u_\infty l/\bar{u})

(s_i/1)

(t/\bar{t})

(u_i/\bar{u})

(u_z/\bar{u})

(u_r/\bar{u})

(u_\phi/\bar{u})

(u_{ref}/\bar{u})

(u_{le} or u_{2e})

(v_i/\bar{u})

(v_{B}/\bar{u}_{B})
\( x_i, X_i \)  
Surface coordinates  
\( (x_i / 1) \)

\( y_i, Y_i \)  
Cartesian coordinates  
\( (y_i / 1) \)

\( \beta_1 \)  
Relative inlet flow angle

\( \gamma \)  
Ratio of specific heats

\( Y_{ij} \)  
Direction cosine tensor components

\( Y_{ij}^{-1} \)  
Inverse tensor components

\( \delta^* \)  
Displacement thickness

\( \varepsilon \)  
Eddy viscosity

\( \bar{\varepsilon} \)  
Viscosity ratio turbulent/laminar

\( \bar{\varepsilon}_{\text{ref}} \)  
Reference viscosity ratio

\( \theta \)  
Momentum thickness

\( \Xi \)  
Static temperature ratio  
\( (t / t_{\text{ref}}) \)

\( \mu \)  
Molecular viscosity

\( \mu_{\text{ref}} \)  
Reference molecular viscosity  
\( \mu(t_{\text{ref}}) \)

\( \xi_i \)  
Levy - Lees transformed coordinates

\( \rho, \Omega \)  
Density  
\( (\rho / \rho_\infty) \)

\( \tau_{ij} \)  
Stress components

\( \omega, \Omega \)  
Rotor speed  
\( (\omega l / u_\infty) \)
Subscripts

e  Edge conditions
h  Hub
L  rotor inlet conditions
t  Tip
T  Total or stagnation conditions
∞  Freestream or reference conditions

Superscripts

~  Absolute rotor reference frame

Tensor Notation

i,j,k  Subscripts covariant tensor components
i,j,k  Superscripts contravariant tensor components
9.0 REFERENCES


