Propulsive-Jet Flow Field Analysis Using The Three-Dimensional Navier-Stokes Equations


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Contract A30142C (MSB)

October 1988

NASA
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Velocity Vectors Near the Jet Computed for the Jet-in-Crossflow Test Case
A critical aspect of advanced aircraft design is the effect of exhausting hot, high-velocity gas into the flow field adjacent to the aircraft. Jet-entrainment produced when a propulsive-jet is exhausted straight back from a fighter-type aircraft can account for up to 25% of the total airplane drag. Exhausting the hot gas in any direction other than straight back, such as in propulsive-lift or thrust-reversing, can have a significant, and sometimes devastating, impact on the aircraft performance. To date, these effects have only been determined through extensive wind tunnel testing. Computational models of these flows have not been available because of the complexity of the flow fields and because of the extensive computer resources required. But now, with new numerical algorithms and high capability computers, advancements can be made in the development of viscous, 3-D analysis procedures for propulsive-jet flow fields.

Several approaches have been taken to determine the characteristics of high velocity jets exhausting into a relatively slower crossflow. Adler and Baron (reference 1) use an integral method to predict the characteristics of a circular turbulent jet in crossflow. Baker and Orzechowski
(reference 2) have used a parabolized Navier-Stokes solver along with a rather complicated start-up procedure to analyze a jet in a crossflow. Numerous others have also attempted solutions of this type. These are summarized in reference 2. The current approach is to model flow fields containing propulsive-jets by solving the 3-D time-dependent Navier-Stokes equations. Although more expensive, this method should have a much wider range of applicability.

This report summarizes the work carried out to test and validate a propulsive-jet flow field analysis method which is based on the 3-D Navier-Stokes equations.
In 1983, an effort was initiated within General Dynamics to develop a propulsive-jet flow field analysis capability using the 3-D Navier-Stokes equations. Because of General Dynamic's experience in using the code for inlet analysis, the full 3-D time-dependent Navier-Stokes (N-S) code developed by J. S. Shang (reference 3) was selected as the baseline code to build on. Some very preliminary results were obtained for a cylindrical body with a sonic jet exiting normal to a subsonic freestream. Although these results indicated that much work was yet to be done, they were encouraging and allowed confidence to be placed in the N-S code's ability to model propulsive-jet problems.

In late 1983, a cooperative program was initiated with the NASA Ames Research Center to continue the 3-D N-S code work. Under this program, NASA Ames supplied both computer resources and jet-in-crossflow test data. After numerous code modifications, the NASA flat plate plume model test case (reference 4) was analyzed. A schematic of this test case is shown in Figure 1. The results were much more encouraging and indicated a well defined plume within the flow field. Figure 2 shows the results for a velocity ratio of 3.66 and a zero-gradient upstream boundary condition.
Figure 1  Schematic of the NASA Flat-Flat Plume Model
Figure 2  Computational Results for the NASA Flat-Plate Plume Model, $\frac{V_4}{V_\infty} = 3.66$, Zero-Gradient Upstream Boundary Condition
No test data were available for this case, however, the results were compared with the empirical jet path equation of reference 5. Although the computational results do not match the empirical jet path, they do indicate that the 3-D N-S code can model highly vectored propulsive jets. In a later test case, a problem was discovered in using a zero-gradient upstream boundary condition. As a temporary solution to this problem, the velocities were specified on the upstream boundary. This type of boundary condition is more consistent mathematically, though still not an exact modeling of the physics. Figure 3 shows the results using a specified upstream velocity and a jet-to-freestream velocity ratio of 8.0. Again, the results are compared to the empirical jet path equation of reference 5. Laser doppler velocimeter (LDV) test data were available for this case and are qualitatively compared to the computationally derived data in Figure 4. The results from these test cases are very encouraging and reinforce our confidence in the ability of the 3-D N-S code to model these complex flow regions.
Figure 3  Computational Results for the NASA Flat-Plate Plume Model, $V_4/V_\infty = 8.0$, Specified Upstream Boundary Condition
Figure 4  Comparison of Computed and Experimental Results for the NASA Flat-Plate Plume Model
EXPERIMENTAL TEST CASE

In order to test and validate the computational analysis methodology a suitable test case was necessary. Under contract to General Dynamics, the Israel Institute of Technology (Technion) has tested a series of jet-in-crossflow cases. At a freestream Mach number of 0.3 and a jet Mach number of 1.5, flow field surveys were made at various injection angles. The case with an injection angle of $90^\circ$ was chosen as the current test case. A schematic of the wind tunnel test set-up is shown in figure 5. Figure 6 shows how data was taken in several planes which are normal to the jet-plume trajectory. Figures 7 and 8 show sample data at a location six jet-exit diameters downstream along the jet-plume centerline.
Figure 5 Schematic of the GD/Technion Jet-in-Crossflow Test Case
Figure 6  The GD/Technion Jet-in-Crossflow test data was taken in planes perpendicular to the jet centerline.
Figure 7  Mach Number Contours for the GD/Technion Jet-in-Crossflow Wind Tunnel Test at Z/D = 6
COMPUTATIONAL MODEL AND RESULTS

A 70 x 46 x 50 grid (161,000 grid points) was set up for the General Dynamics/Technion 90 degree jet case. To alleviate as many boundary condition problems as possible, the grid included the entire wind tunnel test section. The grid was basically Cartesian; however, it was clustered in the vicinity of the jet. Figure 9 shows how the grid was set-up.

To retain as much generality as possible, a constraint was placed on the initialization to not assume any type of jet-plume shape. This was accomplished by initializing the jet-plume to be straight and allowing the solution procedure to turn the jet-plume to its final location.

The freestream and jet flow conditions are given in Table 1. The inflow boundary conditions were held constant (with an assumed boundary layer profile) well upstream of the jet. The outflow boundary conditions were no-gradient in the flow direction. The lower surface boundary condition was no-slip and the jet boundary conditions were set at a constant velocity, density and energy. The side wall boundary conditions were set to freestream flow and the upper surface boundary condition was no-gradient in the direction normal to the boundary. A mixing-length type turbulence
Figure 9  Computational Grid Set-up for the GD/Technion Jet-in-Crossflow Test Case
model was employed where the mixing-length in the region of the jet-plume was assumed to be constant.

TABLE 1 - FLOW CONDITIONS

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<tr>
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<th>Freestream</th>
<th>Jet Exit</th>
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<tr>
<td>Mach Number</td>
<td>0.3</td>
<td>1.5</td>
</tr>
<tr>
<td>Static Pressure</td>
<td>2116.2 psf</td>
<td>2116.2 psf</td>
</tr>
<tr>
<td>Static Temperature</td>
<td>530.0 deg R</td>
<td>477.2 deg R</td>
</tr>
<tr>
<td>Velocity</td>
<td>338.57 fps</td>
<td>1606.2 fps</td>
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The solution procedure was executed to ten-thousand iterations on the Numerical Aerodynamic Simulator CRAY-2 super computer. The elapsed solution time was approximately equal to the time required for a particle to travel from one end of the domain to the other at the freestream velocity. Approximately forty-three hours of computer time was used.

Figures 10 through 12 are example results of this analysis. Figure 10 shows velocity vectors in the region of
Figure 10  Velocity Vectors Computed for the GD/Technion Jet-in-Crossflow Test Case
Figure 12  Velocity Vectors Near the Jet Computed for the Jet-in-Crossflow Test Case
the jet. (Only vectors for points where the Mach number is greater than 0.5 are shown.) Figure 11 shows Mach number contours on a plane cutting through the jet. The jet-plume expansion and mixing are apparent in this figure. The jet initially overexpands and then shocks back down. Figure 12 shows velocity vectors in a plane parallel to the wind tunnel floor. Notice the reversed flow downstream of the jet and the characteristic kidney shape of the jet-plume.

Comparisons with the wind tunnel data were intended but have not been carried out formally because the trajectory of the experimental data was significantly different from the trajectory of the computational data. There are several factors which could be contributors to the discrepancy between the computational and experimental results.

1. The code used in this study was explicit and therefore was very limited in the maximum allowable time-step. For subsonic flows, a good "rule of thumb" for convergence is to allow enough computational time for a particle to traverse the domain at least three times. The current solution has only allowed enough time for one traverse down the domain. Therefore, it is felt that a longer solution time is required.

2. Despite the relatively large number of grid points, grid resolution remains a problem. Since no initial assumptions were made on the plume trajectory, the grid could
not be packed in the region of the jet-plume.

3. Although our ultimate goal would be to not assume anything about the trajectory of the jet-plume, it is becoming apparent that this goal is impractical. Initialization using a good approximate solution could decrease the time to reach a steady result and allow better grid packing in the region of the jet.

4. The turbulent closure of the current case is far from optimum. The mixing-length model used is not appropriate for boundary-layers and lacks the sophistication to adequately simulate the turbulent activity in a jet-in-crossflow. Though it is probably not the dominate problem in the current analysis, turbulent closure should be considered an important part of any jet-in-crossflow analysis. The turbulence level is the major contributor to mixing between the jet and the freestream. This mixing, in turn, plays a major role in determining not only the jet-plume trajectory but the entire flow field definition.
CONCLUSIONS AND RECOMMENDATIONS

The results of this study tend to point out areas of concern rather than provide definitive answers to the numerous problems associated with propulsive-jet flow field analysis. The computational results were not readily comparable to the experimental data because of significant differences between the two data sets. However, much can be learned from this study and applied to future efforts to use the 3-D Navier-Stokes equations to analyze jets-in-crossflow. Based on the results of this study the following recommendations can be made.

1. A time-accurate implicit Navier-Stokes solver should be used instead of an explicit method. This would allow steady solutions to be reached in a reasonable number of time-steps.

2. A grid which adequately resolves the large gradients between the jet and the freestream should be employed. If an approximation to the jet-plume trajectory can be obtained an appropriate grid would be easier to set-up. In addition, a different grid orientation could provide more points in the jet-plume without packing the less interesting outer flow regions. The optimum would be a self adapting grid tied to the flow solver.
3. A lower order approximate solution should be used to initialize the flow field. This would not only provide a more rapid convergence to a steady solution but also provide the basis for grid set-up.

4. Turbulent closure should be accomplished using a higher-order turbulence model. Lakshminarayana (reference 6) suggests using a two-equation model plus an algebraic Reynold's stress model for 3-D flows with curvature rotation and shock waves. Additional investigations need to be carried out in this area.
REFERENCES


A three-dimensional Navier-Stokes code has been applied to the analysis of flow fields containing propulsive-jets. Specifically, the application was made to a flow field containing a supersonic jet injected at an angle of 90 degrees to a subsonic freestream. Although wind tunnel data were available, the computational results were not readily comparable to the experimental data because of significant differences between the two plume trajectories. Reasons for the differences are suggested in the report and include (1) incomplete convergence, (2) inadequate grid resolution in the high gradient regions, and (3) use of a low-order turbulence closure model.