On the Structure of Pressure Fluctuations in Simulated Turbulent Channel Flow

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April 1989

NASA Technical Memorandum 101084
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Pressure fluctuations in a turbulent channel flow are investigated by analyzing a database obtained from a direct numerical simulation. Detailed statistics associated with the pressure fluctuations are presented. Characteristics associated with the rapid (linear) and slow (nonlinear) pressure are discussed. It is found that the slow pressure fluctuations are larger than the rapid pressure fluctuations throughout the channel except very near the wall, where they are about the same magnitude. This is contrary to the common belief that the nonlinear source terms are negligible compared to the linear source terms. Probability density distributions, power spectra, and two-point correlations are examined to reveal the characteristics of the pressure fluctuations. The global dependence of the pressure fluctuations and pressure-strain correlations are also examined by evaluating the integral associated with Green's function representations of them. In the wall region where the pressure-strain terms are large, most contributions to the pressure-strain terms are from the wall region (i.e., local), whereas away from the wall where the pressure-strain terms are small, contributions are global. Structures of instantaneous pressure and pressure gradients at the wall and the corresponding vorticity field are examined.

1. Introduction

The pressure fluctuations in turbulent flows are of considerable interest in many engineering applications. Pressure fluctuations on aerodynamic surfaces of airplanes and turbine blades, for example, contribute to noise generation and often lead to undesirable structural vibrations. Understanding the nature of the pressure fluctuations is essential to alleviate such problems. In addition, because pressure at a given point in turbulent flows is related to global information of the associated velocity field, it may be possible to obtain such information by examining local pressure fluctuations. The pressure fluctuations are also intimately related to vorticity fluctuations, although the governing equations for the evolution of the vorticity fluctuations do not explicitly contain pressure fluctuations. The gradients of surface-pressure fluctuations, for example, are equal to the flux of vorticity from the wall. A better understanding of the surface-pressure fluctuations could lead to a better understanding of the vorticity dynamics in the wall region. From a turbulence modeling point of view, the pressure-strain correlations that appear in the Reynolds-averaged, Navier-Stokes equations are of significant interest because these terms are responsible for intercomponent energy transfer. In the Reynolds shear-stress budget equation, the pressure-strain term is, in fact, one of the two dominant terms. Existing
models for the pressure-strain terms, however, are not satisfactory and are regarded as one of the major deficiencies in the Reynolds stress closure. Refer to Mansour et al. (1988) for a recent assessment of the existing turbulence models based on databases obtained direct numerical simulations.

A great deal of experimental and theoretical work on pressure fluctuations has been performed during the past several decades. Willmarth (1975) provides a comprehensive review on the subject, and Eckelmann (1988) gives an updated review of our knowledge on pressure fluctuations. In spite of the considerable efforts evidenced in the literature, progress in our understanding of the pressure fluctuations has been very slow because of inadequate measurements of pressure fields in turbulent flows. This is because we do not yet have a reliable measurement technique for turbulent pressure fluctuations within turbulent flow comparable to the modern measurement techniques for turbulent velocity fluctuations. Consequently, most measurements reported to date have been performed only on the surface using a surface-mounted pressure transducer. Furthermore, many of the earlier surface-pressure measurements suffered from inadequate spatial resolution because of the large size of pressure transducers employed in the experiments. The errors involved turned out to be significant (Blake 1970; Willmarth 1975; Schewe 1983). Bradshaw (1967) also emphasized the importance of small-scale pressure fluctuations. He argued that the "active" universal velocity fluctuations in the wall region would lead to surface-pressure spectra containing a $k^{-1}$ slope up to the wave number range inversely proportional to the sublayer thickness. Most pressure transducers used in the earlier works were an order of magnitude larger than the sublayer thickness. Schewe (1983) also reported the effect of inadequate spatial resolutions of the pressure transducer on the measured power spectra. For example, he showed that the exponential decay exhibited in some of the measured power-spectra was due to the inadequate spatial resolution.

Most theoretical works in which attempts were made to compute the pressure fluctuations and the power spectra — Kraichnan (1956), Lilley (1964), and Panton & Linebarger (1974), to name a few — also suffered from the lack of accurate information to guide their analyses. The analyses were based on the earlier measurements with the poor spatial resolution. Also, most of the theoretical work assumed that the contribution from the linear source term in the Poisson equation for pressure, representing the interaction of turbulence with the mean shear, is much larger than that from the nonlinear source terms representing interactions of the turbulence with itself. Corcos (1964), however, claimed that the nonlinear source terms should be of the same order of importance as the linear source term after analyzing the data of Willmarth & Wooldridge (1962). Willmarth (1975) later argued that Corcos' conclusion may not necessarily be valid because the data used in the analysis did not satisfy the compatibility condition discussed by Phillips (1956).

The objective of this paper is to document detailed statistics and turbulence structures associated with pressure fluctuations in a wall-bounded turbulent shear flow. The database used in the present work was obtained from a direct numerical simulation of turbulent channel flow by Kim, Moin & Moser (1987, in short, KMM henceforth). The physical realism and accuracy of the computed flow fields have been established by detailed comparison with existing experimental results. Many of the results presented in this paper include new information that cannot be validated directly by comparing it with
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experimental data, unlike most of the statistics and turbulence structures of the corresponding velocity field. However, the pressure fields considered in the present work are obtained from the same velocity fields whose validity has been thoroughly examined, and there is little doubt that the pressure information presented here is as valid as the velocity field. Also, although the Reynolds number considered is very low — $Re_b \approx 3300$ based on the centerline velocity and the channel half-width — because of the enormous amount of computational time necessary for high Reynolds number simulations, most of the computed statistics, as well as turbulence structures of the velocity fields, were essentially the same as those obtained in higher Reynolds number experiments. It is expected that the essential characteristics of the pressure field presented in this paper also would differ only slightly from those of higher Reynolds number flows, except for some features observable only for high Reynolds number flows such as the inertial subrange in the power spectra of the pressure fluctuations.

In § 2, a brief description of numerical procedures and splitting of pressure according to its source terms is presented. Detailed statistics of pressure fluctuations are discussed in § 3. In § 4, Green's function representation for the pressure fluctuations is presented. In § 5, the structure of instantaneous pressure fields and its association with the corresponding velocity and vorticity fields will be discussed. A brief summary is given in § 6.

2. Numerical procedures and splitting of pressure

A direct simulation of fully developed turbulent channel flow — turbulent flow between two parallel plates — has been performed. The numerical algorithm and other details employed to generate the database can be found in KMM. The computation was carried out with about $2 \times 10^6$ grid points ($128 \times 129 \times 128$, in $x$, $y$, and $z$, where $x$, $y$, $z$ indicate streamwise, normal to the wall, and spanwise directions, respectively) for a Reynolds number of about 3300, based on the centerline velocity and channel half-width. The grid spacings in the streamwise and spanwise directions were $\Delta x^+ \approx 17$, and $\Delta z^+ \approx 6$ in wall units.† Nonuniform meshes were used in the normal direction. The first mesh point away from the wall was at $y^+ \approx 0.05$, and the maximum spacing (at the centerline of the channel) was 4.4 wall units. A spectral method — Fourier series in the streamwise and spanwise directions and Chebychev polynomial expansion in the normal direction — was used for the spatial derivatives. The time advancement was carried out by a semi-implicit second-order scheme.

The initial velocity field was obtained from a velocity field of a previous coarse computation (Moin & Kim 1982) by spectrally interpolating the coarse velocity field onto the present collocation points. This reduced the time required to reach a statistically steady state. Once the velocity field reached the steady state, about 100 instantaneous velocity fields (each contains about $8 \times 10^6$ words) at a regular time interval were stored on magnetic tapes for future analyses, from which the present results were obtained.

† The superscript $+$ indicates a nondimensional quantity scaled by the wall variables, e.g., $y^+ = y u_r/\nu$, where $\nu$ is the kinematic viscosity and $u_r = \sqrt{\tau_w/\rho}$ is the wall shear velocity.
The turbulent pressure field for incompressible flows satisfies the following Poisson equation:

\[ \nabla^2 p = -u_{i,j} u_{j,i} \]
\[ \frac{\partial p}{\partial y} (\pm 1) = \frac{1}{Re} \frac{\partial^2 v}{\partial y^2} \]  

(1)

where \( u_i \) \((i = 1, 2, 3)\) or \( u, v, w \) denote the three velocity components in the streamwise, normal to the wall, and spanwise directions, respectively, and \( p \) denotes the kinematic pressure. Here, all the flow variables are nondimensionalized by the friction velocity, \( u_\tau \), and the channel half-width, \( \delta \). The Reynolds number is defined as \( Re = u_\tau \delta / \nu \), and \( y = \pm 1 \) corresponds to the upper and lower walls. Equation (1) is obtained by taking the divergence of the Navier-Stokes equations. The Neumann boundary condition is a result of evaluating the normal component equation at the wall. One can use the Dirichlet boundary condition instead by evaluating the equations for horizontal components at the wall, but it has been demonstrated that any compatible velocity field will produce the same result (Moin & Kim 1980; KMM). The Poisson equation for pressure is solved by the same method as described in KMM for the velocity field: that is, a Fourier/Chebychev-tau method is used to invert the elliptic operator, which involves the inversion of a tridiagonal matrix with one extra full row representing the boundary condition.

The pressure is sometimes split into rapid and slow parts by dividing the source terms in equation (1) into two parts, one containing the mean velocity gradient and the other without it. By decomposing the velocity field into mean and fluctuations as \( u_i = U_i + u'_i \) and noting that the only nonzero mean velocity gradient for the present flow is \( dU/dy \), equation (1) can be written as follows:

\[ \nabla^2 p_r = -2 \frac{dU}{dy} \frac{\partial v'}{\partial x} \]
\[ \frac{\partial p_r}{\partial y} (\pm 1) = 0, \]  

\[ \nabla^2 p_s = -u'_{i,j} u'_{j,i} \]
\[ \frac{\partial p_s}{\partial y} (\pm 1) = \frac{1}{Re} \frac{\partial^2 v'}{\partial y^2} \]  

(2)

where the subscripts \( r \) and \( s \) denote the rapid and slow parts, respectively. The terms “rapid” and “slow” are derived from the fact that only the rapid part responds immediately to a change imposed on the mean field, and the slow part will feel the change through nonlinear interactions. The slow part is sometimes referred to as the “return” term because it is believed by many to be responsible for returning the Reynolds-stress tensor toward isotropy. Sometimes, the rapid and slow pressure are also referred to as linear and nonlinear pressure, respectively, because the corresponding source terms in equation (2) are linear in the fluctuating quantities for the rapid part and nonlinear for the slow part. The above treatment of the boundary conditions, i.e., the homogeneous condition for the rapid pressure and the inhomogeneous condition for the slow pressure, is somewhat arbitrary.
Mansour, Kim & Moin (1988) suggested that the effect of the boundary condition should be treated separately by splitting the pressure into three parts as follows:

\[
\nabla^2 p_r = -2\frac{dU}{dy} \frac{\partial v'}{\partial x} \\
\frac{\partial p_r}{\partial y} (\pm 1) = 0,
\]

\[
\nabla^2 p_s = -u_{i,j}' u_{j,i}' \\
\frac{\partial p_s}{\partial y} (\pm 1) = 0,
\]

\[
\nabla^2 p_{st} = 0 \\
\frac{\partial p_{st}}{\partial y} (\pm 1) = \frac{1}{Re} \frac{\partial^2 v'}{\partial y^2}
\]

where \( p_{st} \) is called the Stokes pressure. The Stokes pressure is solely due to the inhomogeneous boundary condition and one can add the Stokes pressure either into the rapid part or into the slow part. The above triple splitting avoids the arbitrariness in treating the boundary condition, but it takes extra effort to carry the three terms (instead of two) separately in the analysis, and it may not be necessary to do so unless the Stokes pressure becomes significant.

3. Pressure statistics

Throughout the present paper, all quantities are nondimensionalized by the wall-shear velocity, \( u_r \), and the channel half-width, \( \delta \), unless otherwise stated. In some cases, the viscous length scale, \( \nu/u_r \), is used when it appears to be more appropriate. One could use the following global parameters to convert from one form of nondimensionalization to others, if necessary:

\[
Re_r = \frac{u_r \delta}{\nu} = 179 \\
Re_c = \frac{U_c \delta}{\nu} = 3251 \\
\frac{U_c}{u_r} = 18.2 \\
\frac{U_m}{u_r} = 15.6 \\
\frac{\delta^*}{\delta} = 0.141 \\
\frac{\theta}{\delta} = 0.087
\]

where \( U_c, U_m, \delta^*, \) and \( \theta \) denote the centerline velocity, mass-averaged velocity, displacement thickness, and momentum thickness, respectively.
3.1 Rms pressure fluctuation and probability density distribution

The profiles of the root-mean-square (rms) fluctuation resulting from the triple splitting (equation (3)) across the channel are shown in figure 1. These results are obtained from a single realization (one pressure field) to examine the relative importance of each term. It is quite clear that the Stokes part is negligible compared to other two parts throughout the channel, including the near-wall region, where the Stokes part has its maximum. Thus, it would make little difference where we include the inhomogeneous boundary condition. For many practical purposes, one could use the homogeneous boundary condition for both the rapid and slow pressure and simply ignore the Stokes pressure as far as the rms fluctuation is concerned. It should be noted, however, that this does not imply that the presence of the wall is not affecting the pressure fluctuations. Rather, it indicates that most of the influence from the presence of the wall is already built into the source terms through the no-slip boundary conditions (i.e., the source terms themselves are already affected by the no-slip boundary conditions on the velocities), and the explicit influence through the boundary condition to the Poisson equation is not significant. Because of the negligible contribution of the Stokes pressure to the total rms fluctuation, we use the conventional splitting (equation (2)) in the present paper unless otherwise stated.

The profiles of the rms fluctuation of the rapid, slow, and total pressure obtained by averaging over five velocity fields are shown in figure 2. We note that the slow part is substantially larger than the rapid part except very close to the wall ($y^+ < 15$ or $y/\delta < 0.1$), contrary to the common belief that the rapid part would be the dominant one. Both the rapid and slow parts contribute approximately 75% of the total rms pressure at the wall (or about 55% of the total mean-square fluctuation). The two are negatively correlated, with the correlation coefficient about -0.1 at the wall. Throughout the channel, the correlation between the rapid and slow pressure is negligible; the magnitude of the correlation coefficient is less than 0.1. To investigate whether this particular behavior is a characteristic peculiar to a low Reynolds number flow, pressure fluctuations from a higher Reynolds number flow — $Re_r \approx 400$ or $Re_\varepsilon \approx 7800$ compared to $Re_r \approx 180$ or $Re_\varepsilon \approx 3300$ of the present case — have been examined (Kim 1988, unpublished work), and it showed basically the same trend (figure 3). For the high Reynolds number case, the rapid and slow rms pressure contribute approximately 70% each to the total rms fluctuations at the wall. The rms wall-pressure fluctuations reported here are smaller than previously reported values, but they are increasing with the Reynolds number — 1.4 for $Re_r = 180$ and 1.9 for $Re_r = 400$ — which is consistent with the analyses by Bradshaw (1967) and Townsend (1976). From his numerical simulations of turbulent boundary layers, Spalart (1988) reported the same trend of the wall-pressure fluctuations.

To obtain further insight into the pressure splitting, the source terms that appear in equation (2) are examined. The profiles of the mean-square linear, nonlinear, and total source terms are shown in figure 4. Figure 4a shows that the nonlinear source term is much larger than the linear source term throughout the channel. This is because even though the mean shear is large in the wall region, $\partial u' / \partial x$ is rather small (zero at the wall where the shear is the highest, and the mean shear drops significantly where $\partial v' / \partial x$ becomes finite away from the wall). Further breakdown of the nonlinear source terms — there are six different terms — is shown in figure 4b, and it is found that $(\partial v' / \partial z)(\partial w' / \partial y)$ has the
largest mean-square value. Note that the magnitude of \((\partial v'/\partial x)(\partial w'/\partial y)\) would be large at the core of streamwise vortices, and indeed it has a local peak at about \(y^+=20\), where the centers of streamwise vortices are located on the average (KMM). Note also that the locations of the maxima for each source terms approximately coincide with the location of the maximum \(r_{ms}\) pressure fluctuation.

The probability density distribution function (pdf) of the pressure fluctuations at three different \(y\)-locations is shown in figure 5. The pdf at the wall shows an excellent agreement with the result obtained by Schewe (1983) in a turbulent boundary layer at Reynolds number, \(Re_\theta = 1400\) (\(Re_\theta = 280\) in a channel, for the present result). The data points of Schewe shown in the figure correspond to the values obtained from the smallest transducer with its diameter equal to 19 viscous units. Results obtained from larger transducers by Schewe (not shown here) showed a considerable dependence of pdf on the transducer size: smaller transducers measured more high-intensity fluctuations. To examine fractional contributions to the mean-square fluctuation, the integrand of

\[
\overline{p^2} = \int_{-\infty}^{\infty} \eta^2 f(\eta) \, d\eta
\]

where \(f(\eta)\) is the probability density function, is computed, and is shown in figure 6. The area under the curve is equal to the mean-square fluctuation, which has been normalized to be one. For comparison, the same quantity corresponding to the streamwise velocity fluctuations is also included in the figure. It is clear that relatively large contributions to the mean-square fluctuation are from high-intensity fluctuations, especially from the negative fluctuations, compared to the streamwise velocity fluctuations. For instance, at \(y^+ = 12\), only 1% of the data points exceed \(\pm 3 \, \overline{p_{rm\delta}}\), but they contribute to about 42% of the total \(\overline{p_{rm\delta}}\). Corresponding contribution to the streamwise velocity fluctuations, on the other hand, is negligible. While the mean-square streamwise velocity fluctuation takes larger contributions from the positive fluctuations (associated with the sweep-like events) near the wall \((y^+ < 15)\) and from the negative fluctuations away from the wall \((y^+ > 15)\), the mean-square pressure fluctuation takes its contributions about the same from both sides near the wall and more from the negative fluctuations away from the wall.

The skewness and flatness factors, \(\overline{p^3}/(\overline{p^2})^{3/2}\) and \(\overline{p^4}/(\overline{p^2})^2\), respectively, computed from the pdfs were presented in KMM and are shown in figure 7. The wall values of the skewness and flatness factors, - 0.1 and 5.0, respectively, are comparable to Schewe's results of - 0.2 and 4.9. Moving away from the wall region, pdf becomes more negatively skewed with a higher flatness factor (more intermittent) indicating the presence of localized and very low pressure regions. Robinson et al. (1988), in their analysis of the data of Spalart (1988), noticed a strong correspondence between low-pressure regions and streamwise vortices. It is likely that the intermittent occurrence of low-pressure fluctuations in the pdf is associated with the vortices present in the flow. The joint probability density distribution between pressure fluctuations and streamwise vorticity fluctuations is examined to find out whether this is the case. The joint pdfs at \(y^+ \approx 30\) and 100 (figure 8) indicate that large streamwise vorticity fluctuations are indeed more likely associated with large negative pressure fluctuations. It should be noted, however, that the reverse is not true.
Large negative pressure fluctuations are not necessarily associated with the large streamwise vorticity fluctuations, suggesting that additional information is required in identifying organized vortical structures.

3.2 Power spectra and two-point correlations

The power spectra and two-point correlations in the streamwise direction at three different y-locations are shown in figures 9 and 10. Because of the low Reynolds number considered here, we do not expect to see the distinct power-law behaviors for different wave-number ranges. For example, neither the $k^{-1}$-range of Bradshaw (1967) nor the inertial subrange can be differentiated in figure 9 except for very narrow bands whose tangents are parallel to the expected slopes (one can show from a dimensional argument that the rapid pressure should decay as $k^{-11/3}$ while the slow pressure should decay as $k^{-7/3}$).

To compare the present wave-number spectra with the measured frequency spectra, we invoke Taylor's hypothesis with a convection velocity of pressure at the wall to yield:

$$\omega^+ = \omega \frac{\nu}{u_r^2} = 2\pi \frac{V \nu}{\lambda u_r^2} = 2\pi \frac{V^+}{\lambda^+} = k \delta \frac{V^+}{Re_r}$$

where $k$ and $\lambda$ denote the corresponding wave number and wavelength, respectively, and $V$ denotes the convection velocity of pressure. In the above conversion, $V^+=13$ is used at the wall, which was obtained from the space-time correlation of pressure fluctuations at the wall. This will be discussed in § 3.3. The nondimensional frequencies are indicated in figure 9.

The power spectra at the wall (figure 9a) display no big difference between the rapid and slow parts, indicating no difference in length scales associated with the two pressures. This is somewhat surprising because one would expect a large contribution to the rapid pressure from low wave numbers and to the slow pressure from high wave numbers. Durbin (1978), using the rapid distortion theory (Townsend 1976), predicted that the effect of wall on the rapid pressure is to increase the amplitude of the spectra associated with the low wave numbers. The present results do not bear out this effect. The power spectra obtained from the smallest transducer by Schewe (1983) indicated a small region of $\omega^{-7/3}$ for $0.4 \leq \omega^+ \leq 0.8$ (other data obtained from larger transducers had a steeper fall-off, indicating the insensitivity of large-size transducers to high-frequency fluctuations). Figure 9a also indicates a small region of $k^{-7/3}$ at about the same frequency range. The power spectra at the centerline (figure 9c) show a different behavior between the two pressures more consistent with the expected behavior. That is, most of the energy of the rapid pressure resides in low wave numbers, while that of the slow pressure spreads over to small wave numbers. They both show a trace of the expected behavior of the inertial subrange: $k^{-11/3}$ for the rapid pressure and $k^{-7/3}$ for the slow pressure.
The peak in the power spectra of the rapid pressure, distinct at the centerline, but slightly noticeable at the wall, persists throughout the channel, indicating that this is related to a global phenomenon. The corresponding wavelength is about 750 viscous units or about 4δ. The same convection velocity used above gives $\omega^+ = 0.11$. It is interesting to note that this value is not too far from the bursting frequency reported in Luchik & Tiederman (1987), in which they used the quadrant analysis of velocity fluctuation to detect the bursting process: $T_b^+ = 90$ of their nondimensional bursting period gives $\omega_b^+ = 2\pi/T_b^+ = 0.07$. The spectrum of the total pressure at the wall, however, has a maximum at the wave number and frequency corresponding to $\lambda^+ = 330$ and $\omega^+ = 0.26$.

Two-point correlations in the streamwise direction at the wall shown in figure 10a again indicate little difference between the two pressures. The two-point correlations at the centerline, however, show a marked difference between the two; one can see that the rapid pressure is correlated over a much longer distance. The dominance of the length scale associated with $\lambda^+ = 750$ discussed above is also obvious in the two-point correlation of the rapid pressure at the centerline. The fact that the correlations for the rapid pressure have negative excursions for all $y$-locations is a direct consequence of the presence of $\partial v/\partial x$ in the source term. It can be easily shown that the area under the two-point correlations in the streamwise directions must be zero. Two-point correlations in the spanwise directions (not shown) do not have such negative excursions. Also included in figure 10a are the results obtained by Lee (1988, private communication), who used the rapid distortion theory to study the effect of wall on turbulence. The two-point correlation predicted by the linear theory is normalized such that the streamwise location where it crosses zero would be the same as that of the present result. As shown in the figure, the rapid pressure of the present result and that predicted by the linear theory are in good agreement.

Two-point correlations with streamwise and spanwise separations, $R_{pp}(\Delta z, \Delta z)$, at three different $y$-locations are shown in figure 11. The contours of constant correlations at the wall are slightly elongated in the streamwise direction, but they become more elongated in the spanwise direction away from the wall. This is quite a contrast to contours of other quantities, which are generally elongated in the streamwise direction in the wall region and become less so away from the wall. For comparison, contours of constant two-point correlations of the streamwise velocity fluctuations are shown in figure 12. Two-point correlations of the streamwise velocity fluctuations near the wall (figure 12a) illustrate the presence of the familiar streaky structures elongated in the streamwise direction alternating in the spanwise direction with the mean spanwise spacing — estimated by twice the distance of the negative peak — about 100 wall units. The streamwise elongation becomes less pronounced away from the wall (figure 12b and 12c). The two-point correlations of the wall pressure shown in figure 11a are similar to those obtained by Bull (1967), but there are some differences. Bull’s results showed that contours for the high correlations were round, and become oval shapes at low correlations, but the present results do not show the oval shape at lower correlations. The contours at the centerline of the present results (figure 11c) are more like Bull’s results at the wall.

Contours of constant two-point correlations of pressure as a function of streamwise and normal separations, $R_{pp}(\Delta z, y, y')$, at three different $y'$-locations are shown in figure 13. For comparison, the same contours for the streamwise velocity fluctuations are also shown.
in figure 14. Note that in figures 13 and 14, the y-coordinate is stretched by a factor of about two and the domain extends to the other wall. Unlike the correlations of streamwise velocity fluctuations, the maximum correlation of the pressure fluctuations is approximately aligned along the normal direction to the wall. Note that contours of streamwise velocity fluctuations illustrate the presence of inclined structure with the maximum correlation aligned along a line inclined about 20° to the wall (figure 14b). Two-point correlations along the normal direction with zero separations in the streamwise and spanwise directions are shown in figure 15, and indicate that the correlation length for the pressure along the normal direction is much larger than for the other quantities.

3.3 Space-time correlation and convection velocity.

Space-time correlations of the total pressure as a function of streamwise separation and time delay, \( R_{pp}(\Delta x, \Delta t) \), are computed from 50 consecutive pressure fields, which were obtained from 50 consecutive velocity fields stored at an interval of \( \Delta t^+ = 3 \). Figure 16 shows the space-time correlation at the wall. It shows basically the same characteristics as the one measured by Willmarth & Wooldridge (1962) in a turbulent boundary layer. The maximum correlation is along the first (or third by the symmetry) quadrant in the \((\Delta z, \Delta t)\)-plane, indicating that the pressure eddies are propagating downstream. They lose their correlations as they propagate downstream, and there is a slight increase in the slope of \( d\Delta z/d\Delta t \), suggesting that the propagation speed of large eddies is higher than that of small eddies because only large eddies retain their coherence at large time separations.

There are several ways to determine propagation velocity† using the space-time correlations (see Wills 1964, for example). In the present work, we used the propagation velocity determined by

\[
V_p = \frac{\Delta x_{\text{max}}}{\Delta t}
\]

(6)

\( \Delta x_{\text{max}} \) is the streamwise separation where the space-time correlation, \( R_{pp}(\Delta x, \Delta t) \), is maximum for a given \( \Delta t \). \( V_p \) determined this way will be a function of \( \Delta t \) used in equation (6), but their variation is rather small as indicated in figure 16, where the ridge of the maximum correlations forms approximately a straight line. \( \Delta t^+ = 18 \) was used for the present work.‡ The propagation velocity determined as such was \( V_p = 0.72 U_c \) or \( V_p = 13 u_r \) at the wall, and there was little difference among the rapid, slow, and total pressure. Willmarth & Wooldridge (1962) found that \( V_p \) varied from 0.56 \( U_\infty \) to 0.83 \( U_\infty \) in a turbulent boundary layer depending on the probe separation used. Schewe (1983) reported \( V_p = 0.53 U_\infty \) or \( V_p = 11.9 u_r \), but it was determined by sampling only high amplitude fluctuations. A further discussion of the propagation speeds for velocity, pressure, and vorticity fluctuations, including their dependence on eddy sizes, will be reported elsewhere (Hussain & Kim 1989). The propagation velocity of the pressure at the wall is larger than that of each velocity or vorticity component at the wall. For all three velocity and

† Strictly speaking, it is “propagation velocity,” but the term “convection velocity” has been used in the literature. We use them interchangeably in the present paper.

‡ The dependence of the propagation velocity on \( \Delta t \) was examined and it was found that \( V_p \) varied from 0.7 \( U_c \) to 0.8 \( U_c \) for \( 9 \leq \Delta t^+ \leq 27 \).
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vorticity components, the wall convection velocities determined by space-time correlations were about the same, at 0.53 \( U_c \) and 9.6 \( u_r \).

Schewe (1983) estimated the location of the "effective" source terms for the pressure by the distance from the wall where the mean velocity was equal to the propagation velocity of the pressure at the wall. For the present work, this corresponds to \( y^+ \approx 23 \) with \( U = 13 \ u_r \), which compares well with Schewe's \( y^+ = 21 \). It is interesting to note that the location of the effective source terms determined this way coincides approximately with the location where the mean-square source term has its maximum (figure 4a), of which most contributions are from the vortex-like structures (see § 3.1). This suggests that the wall-pressure fluctuations can be regarded as a signature connected to vortex structures present near \( y^+ \approx 20 \). This is consistent with Alfesson et al. (1988) who reported a large pressure peak underneath the internal shear-layer structure responsible for much of turbulence production in the wall region.

4. Green's function representation for the pressure fluctuations

In this section, to gain a further insight into which part of the channel in the \( y \)-direction contributes most to the local pressure fluctuations, we represent the pressure fluctuations in terms of Green's function. For the purpose of this section only, we use the homogeneous boundary condition for both the rapid and slow pressure. That is, we are using the triple splitting according to equation (3), but we neglect the Stokes part; this is justified because the contribution from the Stokes part is negligible, as discussed in § 3.1. We first take the Fourier transform of equation (3) in the homogeneous directions to give

\[
\frac{d^2}{dy^2} - (k_z^2 + k_x^2) \hat{p}(k_z, y, k_x) = \hat{f}(k_z, y, k_x)
\]

where \( k_z \) and \( k_x \) denote the nondimensional wave number normalized by \( \delta \) in the streamwise and spanwise directions, respectively, and \( \hat{p} \) and \( \hat{f} \) represent the pressure and source terms in the Fourier space. It can be shown that Green's function to equation (7) is

\[
\hat{G}(k, y, y') = -\frac{\cosh[k(y'-1)]\cosh[k(y+1)]}{2k \cosh(k) \sinh(k)} \quad \text{for} \quad y < y'
\]

\[
\hat{G}(k, y, y') = -\frac{\cosh[k(y'+1)]\cosh[k(y-1)]}{2k \cosh(k) \sinh(k)} \quad \text{for} \quad y > y'
\]

for \( k \neq 0 \), where \( k = \sqrt{k_x^2 + k_z^2} \), and

\[
\hat{G}(y, y') = 0.5 (y' - y) \quad \text{for} \quad y < y'
\]

\[
\hat{G}(y, y') = 0.5 (y - y') \quad \text{for} \quad y > y'
\]

\( \dagger \) For the velocity and normal vorticity at the wall, whose values are zero there, we use limiting values of the propagation velocities, all of which are constant in the region \( y^+ < 10 \).
for \( k = 0 \). The solution to equation (7) can now be written as

\[
\hat{p}(k_x, y, k_z) = \int_{-1}^{1} \hat{G}(k_x, y, k_z) \hat{f}(k_x, y', k_z) \, dy'
\]

(10)

The Green's functions at the wall, \( \hat{G}(k_x, y = -1, y') \), corresponding to three different wave numbers are shown in figure 17. The Green's functions corresponding to high wave numbers diminish rather quickly away from the source location, but those corresponding to the small wave numbers decay very slowly. This implies that the source terms associated with long streamwise and spanwise wave lengths will influence the pressure far away from the location of the source terms. Inverse Fourier transform of equation (10) gives

\[
p(z, y, z) = \int_{-1}^{1} G * f(z, y, y', z) \, dy'
\]

(11)

where the convolution \( G * f(z, y, y', z) \) represents the inverse Fourier transform of \( \hat{G}(k_x, y, y') \hat{f}(k_x, y', k_z) \). Equation (11) gives an expression for pressure at a given point in terms of contributions from various \( y \)-locations. An example is given in figure 18 in which contributions to instantaneous pressure at an arbitrary location at the wall are shown. It illustrates that the source terms near one wall contribute significantly to the total and slow pressure at the other wall; the contribution to the rapid pressure from near the other wall is negligible. Obviously the slowly decaying Green's function for low wave numbers (figure 17) induces such global dependence. Note that the Green's functions considered here are independent of the Reynolds number, and this nonlocal dependence would be the same for high Reynolds number flows unless the source terms change drastically such that the low wave number contents of the source terms diminishes significantly.

From equation (11), one can write a similar expression for the mean-square fluctuations as follows:

\[
p^2(y) = \int_{-1}^{1} \overline{p(y)} \, G * f(y, y') \, dy'
\]

\[= \int_{-1}^{1} \int_{-1}^{1} \overline{G * f(y, \eta) \, G * f(y, y')} \, d\eta \, dy'
\]

\[= \int_{-1}^{1} h(y, y') \, dy'
\]

(12)

where the overbar denotes an average over the \( x \) and \( z \) directions. Contributions to the mean-square wall-pressure fluctuation are shown in figure 19, which indicates that most contributions are from the wall region. It appears that even though the instantaneous pressure at one wall is strongly affected by the source terms from the other side of the channel (figure 18), their net effects are not correlated to give a significant contribution to the mean-square fluctuation.

In turbulence modeling, much effort has been directed toward developing models for the pressure-strain terms, \( \overline{p \sigma_{ij}} = \overline{p(u_i,j + u_j,i)} \). This is because not only are these terms responsible for redistributing the kinetic energy among the three components, but also
\( p_s \) is one of the two dominant terms in the budget of the Reynolds shear-stress equation — the other is the production term (see Mansour et al. 1988, for details). It has been of significant interest to modelers to know how local these terms are in order to make certain approximations in developing models for them. Using equation (11), one can write

\[
\overline{p(y) s_{ij}(y)} = \int_{-1}^{1} s_{ij}(y) G * f(y, y') dy'
\]  

(13)

The pressure-strain terms that appear in \( u'^2, v'^2, w'^2, \) and \( u'v' \) at two different \( y \)-locations — one near the wall where they are large and the other away from the wall where they are relatively small (Mansour et al. 1988) — are shown in figure 20. It is clear from the figures that the pressure-strain correlations in the wall region (figure 20a-20c) take their largest contributions from the wall-region (contributions are local), but away from the wall the pressure-strain terms at a given \( y \)-location take their contributions from wide ranges of \( y \)-locations (global). This nonlocal character of the pressure-strain terms would make them hard to model in terms of local variables.

5. Structures of instantaneous pressure fluctuations.

In this section we examine the characteristics associated with instantaneous pressure fields. Instantaneous pressure and other relevant quantities are presented in terms of contours of constant values. The domain shown in the following figures is a fraction of the total computational domain: the total domain was \( 4\pi \delta \) (or \( 2260 \nu/u_r \)) and \( 4\pi \delta/3 \) (or \( 750 \nu/u_r \)) in the streamwise and spanwise directions, respectively. In all cases, the solid lines denote positive quantities and the dashed lines denote negative quantities with respect to the plane-averaged mean value.

Contours of constant rapid, slow, and total pressure at two different \( y \)-locations are shown in figures 21 and 22. Contours at the wall (figure 21) show that there is little difference in associated length scales between the rapid and slow pressure as discussed in § 3.2. Contours for the total pressure at the wall (figure 21c) are very similar to those obtained experimentally by Emmerling (see figure 9 of Willmarth 1975). Contours at the centerline (figure 22) show a marked difference between the rapid and slow pressure. Contours of constant, rapid pressure at the centerline also indicate the presence of the length scale, \( \lambda^+ \approx 750 \), mentioned in § 3.2. It is also discernible from the contours at the centerline that they are more elongated along the spanwise direction. It should be noted that it is the pressure gradient rather than the pressure itself that appears in the Navier-Stokes equation. In other words, fluid motions are not affected by pressure; they respond to the imposed pressure gradients. Hence, it is more interesting to examine contours of constant pressure gradients. Such contours at the wall and the centerline of the channel are shown in figures 23-24. It is somewhat surprising to note that the contours of \( \partial p/\partial z \) do not show any streamwise elongation, whereas those of \( \partial p/\partial y \) and \( \partial p/\partial z \) do. Recall that it is the eddy associated with the streamwise velocity fluctuations that is mostly elongated in the streamwise direction. The magnitudes of instantaneous pressure gradients are quite large. For example, the maximum and minimum streamwise pressure gradients at the wall shown in figure 23a are 96 and -49, respectively, compared to the mean pressure gradient of -1 for the fully developed channel flow considered here.
The instantaneous pressure gradient at the wall is related to the vorticity flux at the wall (Lighthill 1963), which can be obtained by evaluating the Navier-Stokes equations at the wall. That is,

$$\frac{\partial p}{\partial z} = \frac{\partial}{\partial y} \omega_z$$
$$\frac{\partial p}{\partial z} = \frac{\partial}{\partial y} \omega_z.$$  (14)

The streamwise and spanwise components of vorticity are diffused into the surrounding fluid according to equation (14) at the wall, and then they are convected (and diffused) from the wall region. They will subsequently interact with (and modify) turbulence structures responsible for the source terms that created the pressure gradients at the wall. The new, modified source terms will create new pressure gradients at the wall, which in turn determine the flux of vorticity at the wall, and so on. From equation (11) and figure 18, we also note that the vorticity flux at the wall is determined globally. Even the source term on the other side of the channel will influence the flux of vorticity at one side of the channel by affecting the instantaneous pressure, and hence, the instantaneous pressure gradient. In some transitional flows, the pressure gradients at the wall and source terms away from the wall — usually located just above the critical layer — work together in phase to contribute to flow instability (Morkovin 1988, private communication). Also, Kim (1983) and Johansson et al. (1988) showed a strong link between a turbulence structure responsible for intense turbulence production and a localized pressure peak at the surface. This suggests a possibility that one can modify the structure of turbulence by artificially modifying the pressure gradient at the wall, and hence the turbulence production in the boundary layer.

Contours of constant streamwise and spanwise vorticity at the wall are shown in figure 25. A striking similarity exists between the spanwise pressure gradient at the wall (figure 23c) and the streamwise vorticity at the wall (figure 25a), but the correlation between the streamwise pressure gradient at the wall (figure 23a) and spanwise vorticity (figure 25b) is not discernible at all. It is not clear what causes this difference.

6. Summary and discussions

Turbulence statistics associated with pressure fluctuations in a turbulent channel flow are studied by analyzing the database obtained from a direct numerical simulation (Kim et al. 1987). The pressure is split into the rapid (linear) and slow (nonlinear) parts corresponding to the linear and nonlinear source terms in the Poisson equation. Contrary to the common belief that the rapid pressure is the dominant component, it is found that the slow pressure is comparable near the wall and larger away from the wall. The corresponding source terms also show the same trend. Among the nonlinear source terms, it is found that \((\partial v/\partial z)(\partial w/\partial y)\), which is large in the core of streamwise vortices, is the most dominant term. The mean-square of the nonlinear source terms, \((\partial v/\partial z)(\partial w/\partial y)\) in particular, peak at about \(y^+ \approx 20\), and the major contribution to the mean-square wall-pressure fluctuations comes from this region. The convection velocity of the wall pressure

\[\frac{\partial}{\partial y} = -\frac{\partial \omega_z}{\partial x} - \frac{\partial \omega_y}{\partial z}.\]

\[\frac{\partial}{\partial y} = -\frac{\partial \omega_z}{\partial x} - \frac{\partial \omega_y}{\partial z}.\]
measured from the space-time correlation of the wall-pressure fluctuation is also found to be equal to the local mean velocity at about the same y-location, indicating that the coherent part of the wall pressure can be regarded as a footprint connected to flow structures present at about \( y^+ \approx 20 \). This view is consistent with Kim (1983) and Alfresson et al. (1988) who observed that the internal shear-layer structures responsible for a major portion of turbulence production were associated with a high localized wall-pressure peak. This, in turn, suggests that one can interfere with the flow structures responsible for turbulence production either by directly modifying the wall pressure or by manipulating other flow variables at the wall to control wall-bounded turbulent flows.

The probability density distribution illustrates that the pressure fluctuations are much more intermittent than velocity fluctuations, and high negative fluctuations provide a substantial contribution to the mean-square fluctuation. Much of these negative fluctuations are correlated with high vorticity fluctuations. Robinson et al. (1988) showed that it was easier to identify a vortical structure using low pressure as a detecting criterion than the velocity or vorticity itself. Using low pressure as a diagnostic tool in identifying vortical structures is promising, but it should be used with some caution because not all low pressure regions are associated with organized vortical structures, although the reverse is generally true.

The power spectra and two-point correlations show that there is little difference between the rapid and the slow pressure near the wall, but they differ considerably from each other away from the wall. The behavior of the two-point correlation of the rapid pressure at the wall is in good agreement with that obtained by using the rapid distortion theory, suggesting the usefulness of the linear theory. Other aspects on the effect of the wall on turbulence can be studied using the linear theory, which is much less costly and simple to analyze.

Green's function representation is used to demonstrate the global dependence of pressure fluctuations. It is shown that instantaneous pressure at one wall is influenced significantly by the source terms from near the other wall. However, the same representation for the mean-square fluctuation illustrates that although the instantaneous pressure has a global dependence, most contributions to the mean-square fluctuation are local, indicating that the influence from far away is averaged out with small net effects. Contributions to the pressure-strain correlations are local near the wall, but global away from the wall. This nonlocal character of the contributions to the pressure-strain correlations raises an important question of whether one can model them in terms of local variables as is done currently.

Contours of constant pressure gradients show that those associated with \( \partial p / \partial y \) and \( \partial p / \partial z \) are somewhat elongated in the streamwise direction, but not those associated with \( \partial p / \partial z \). Examination of vorticity and pressure gradients at the wall, which control the diffusion of vorticity from the wall, shows a strong correlation between \( \omega_z \) and \( \partial p / \partial z \), but it shows no apparent correlation between \( \omega_z \) and \( \partial p / \partial x \). Further study is required to explain this interesting but puzzling observation.

Acknowledgment

I am grateful to Dr. Nagi N. Mansour for many discussions during the course of this
work, and to Professor P. Bradshaw and Drs. Philippe R. Spalart and Sanjiva Lele for helpful comments on a draft of this manuscript.

REFERENCES


Figure 1. Root-mean-square fluctuation for each pressure according to equation (3): 
---, rapid; ----, slow; ---, Stokes.
Figure 2. Root-mean-square fluctuation for each pressure according to equation (2): ----- , rapid; ---- , slow; ------ , total.
Figure 3. Root-mean-square fluctuation for $Re_r = 400$: ——, rapid; -----, slow; ———, total.
Figure 4. Profiles of the mean-square source terms. (a) ———, linear; ———, nonlinear; ———, total. (b) Profiles of the mean-square nonlinear terms: ———, $(\partial u'/\partial x)^2$, ———, $(\partial u'/\partial y)(\partial v'/\partial x)$; ———, $(\partial u'/\partial z)(\partial w'/\partial x)$; ———, $(\partial v'/\partial y)^2$; ———, $(\partial v'/\partial z)(\partial w'/\partial y)$; ———, $(\partial w'/\partial z)^2$. 
Figure 5. Probability density distribution of the total pressure-fluctuations: computation; , Gaussian distribution; , Schewe (1983). The abscissa is normalized by the local $\text{rms}$ pressure fluctuations and the ordinate is normalized such that the area under the curve is equal to one: (a) $y^+ = 0$; (b) $y^+ = 12$; (c) $y^+ = 100$. 
Figure 6. Fractional contributions to the mean-square fluctuation: ———, \( u' \); ———, \( p' \). The abscissa is normalized by the corresponding local \( rms \) fluctuations and the ordinate is normalized such that the area under the curve is equal to one: (a) \( y^+ = 0 \) for \( p \) and \( y^+ = 5 \) for \( u \); (b) \( y^+ = 12 \); (c) \( y^+ = 100 \).
Figure 7. (a) Skewness and (b) flatness factors of the velocity and pressure fluctuations: 

--- , u; -----, v; -----, w; ------ , p.
Figure 8. Joint probability density distribution between $p'$ and $w'_x$: (a) $y^+ = 0$; (b) $y^+ = 30$; (c) $y^+ = 100$. The axes are normalized by the corresponding $rms$ fluctuations.
Fig. 9  Power spectra of the rapid (----), slow (-----), and total (---) pressure in the streamwise direction: (a) $y^+ = 0$; (b) $y^+ = 50$; (c) $y^+ = 180$. 

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Figure 10. Two-point correlations of the rapid (— ), slow (--- ), and total (--- ) pressure in the streamwise direction: (a) $y^+ = 0$; (b) $y^+ = 50$; (c) $y^+ = 180$. The symbols represent the results obtained by Lee (1989) using the rapid distortion theory.
Fig. 11 Contours of constant two-point correlations of the total pressure fluctuations, $R_{pp}(r_x, r_z)$: (a) $y^+ = 0$; (b) $y^+ = 50$; (c) $y^+ = 180$. The contour level '1' corresponds to 0.1 and higher levels are incremented by 0.1, and the tick marks in the axes represent 50 wall units.
Figure 12. Contours of constant two-point correlations of the streamwise velocity fluctuations, $R_{uu}(\Delta x, \Delta z)$: (a) $y^+ = 0$; (b) $y^+ \approx 50$; (c) $y^+ = 180$. The contour level '1' corresponds to 0.1 and higher levels are incremented by 0.1, and the tick marks in the axes represent 50 wall units.
Figure 13. Contours of constant two-point correlations of the total pressure fluctuations, \( R_{pp}(\Delta x, y, y') \): (a) \( y'^+ = 0 \); (b) \( y'^+ = 50 \); (c) \( y'^+ = 180 \). Note that \( \Delta y/\delta = 0.2 \) corresponds to \( \Delta y'^+ = 36 \), and the \( y \)-coordinate is stretched by a factor of about two.
Figure 14. Contours of constant two-point correlations of the streamwise velocity fluctuations, $R_{uu}(\Delta x, y, y')$: (a) $y'^+ = 10$; (b) $y'^+ = 50$; (c) $y'^+ = 180$. Note that $\Delta y/\delta = 0.2$ corresponds to $\Delta y^+ = 36$, and the $y$-coordinate is stretched by a factor of about two.
Fig. 15 Two-point correlations in the normal direction, $R_{ii}(y)$: $\ldots$, $R_{uu}$; $\ldots$, $R_{vv}$; $\ldots$, $R_{ww}$; $\ldots$, $R_{pp}$. (a) $y^+ = 0$; (b) $y^+ = 50$; (c) $y^+ = 180$. 
Fig. 16  Space-time correlation of the wall-pressure fluctuations, $R_{pp}(r_z, r_t)$. 

Fig. 17  Green's function for three different wave numbers: --- , \( k_x \delta = 2\pi/(\lambda_x/\delta) = 0.5 \) and \( k_x \delta = 2\pi/(\lambda_x/\delta) = 1.5 \); ------ , \( k_x \delta = 5 \) and \( k_x \delta = 15 \); ------ , \( k_x \delta = 25 \) and \( k_x \delta = 75 \). Each Green's function is normalized such that its maximum value is equal to one.
Fig. 18 Contribution to instantaneous wall pressure, \( p(x = 0, y = -1, z = 0) \), from across the channel: \(-\cdot\cdot\cdot\) rapid pressure; \(-\cdot\cdot\cdot\) slow pressure; \(-\cdot\cdot\cdot\) total pressure. The ordinate is normalized such that the maximum value is equal to one.

Fig. 19 Contribution to the mean-square wall-pressure fluctuation from across the channel: \(-\cdot\cdot\cdot\) rapid pressure; \(-\cdot\cdot\cdot\) slow pressure; \(-\cdot\cdot\cdot\) total pressure. The ordinate is normalized such that the maximum value is equal to one.
Fig. 20 Contributions to the pressure-strain correlations: \( - - - - , 2p(\partial u/\partial x) \); \( - - - - - - - - \), \( 2p(\partial v/\partial y) \); \( - - - - \), \( 2p(\partial w/\partial z) \); \( \cdots \cdots \cdots \cdots \), \( p(\partial u/\partial y + \partial v/\partial z) \). The ordinate is normalized such that the maximum value of the four terms is equal to one. (a) rapid, (b) slow, and (c) total pressure-strain at \( y^+ \approx 10 \);
Fig. 20 - continued  (d) rapid, (e) slow, and (f) total pressure-strain at $y^+ \approx 100$. 
Fig. 21 Contours of constant (a) rapid, (b) slow, and (c) total pressure at the wall. The mean flow direction is from left to right, and the tick marks denote 50 wall units.
Fig. 22  Contours of constant (a) rapid, (b) slow, and (c) total pressure at the centerline. The mean flow direction is from left to right, and the tick marks denote 50 wall units.
Fig. 23  Contours of constant (a) $\partial p/\partial x$, (b) $\partial p/\partial y$, and (c) $\partial p/\partial z$ at the wall. The mean flow direction is from left to right, and the tick marks denote 50 wall units.
Fig. 24 Contours of constant (a) $\partial p/\partial x$, (b) $\partial p/\partial y$ and (c) $\partial p/\partial z$ at the centerline. The mean flow direction is from left to right, and the tick marks denote 50 wall units.
Fig. 25  Contours of constant (a) streamwise and (b) spanwise vorticity at the wall.
Pressure fluctuations in a turbulent channel flow are investigated by analyzing a database obtained from a direct numerical simulation. Detailed statistics associated with the pressure fluctuations are presented. Characteristics associated with the rapid (linear) and slow (nonlinear) pressure are discussed. It is found that the slow pressure fluctuations are larger than the rapid pressure fluctuations throughout the channel except very near the wall, where they are about the same magnitude. This is contrary to the common belief that the nonlinear source terms are negligible compared to the linear source terms. Probability density distributions, power spectra, and two-point correlations are examined to reveal the characteristics of the pressure fluctuations. The global dependence of the pressure fluctuations and pressure-strain correlations are also examined by evaluating the integral associated with Green’s function representations of them. In the wall region where the pressure-strain terms are large, most contributions to the pressure-strain terms are from the wall region (i.e., local), whereas away from the wall where the pressure-strain terms are small, contributions are global. Structures of instantaneous pressure and pressure gradients at the wall and the corresponding vorticity field are examined.