SAIC has the responsibility for independent test and validation of the SSE. They have been using a mathematical functions library package implemented in Ada to test the SSE IV&V process. The library package consists of elementary mathematical functions and is both machine and accuracy independent. The SSE Ada components evaluation includes code complexity metrics based on Halstead’s software science metrics and McCabe’s measure of cyclomatic complexity. Halstead’s metrics are based on the number of operators and operands on a logical unit of code and are compiled from the number of distinct operators, distinct operands, and total number of occurrences of operators and operands. These metrics give an indication of the physical size of a program in terms of operators and operands and are used diagnostically to point to potential problems. McCabe’s Cyclomatic Complexity Metrics (CCM) are compiled from flow charts transformed to equivalent directed graphs. The CCM is a measure of the total number of linearly independent paths through the code’s control structure. These metrics were computed for the Ada mathematical functions library using Software Automated Verification and Validation System (SAVVAS), the SSE IV&V tool. A table with selected results was shown, indicating that most of these routines are of good quality. Thresholds for the Halstead measures indicate poor quality if the length metric exceeds 260 or difficulty is greater than 190. The McCabe CCM indicated a high quality of software products. The SSE will include the Ada version of SAVVAS that may be used for computing these code complexity metrics.
INITIAL ADA COMPONENTS EVALUATION
MATHEMATICAL FUNCTIONS LIBRARY PACKAGE

- IMPLEMENTED IN ADA BY L. J. GALLAHER, Ph.D

- LIBRARY PACKAGE OF ELEMENTARY
MATHEMATICAL FUNCTIONS
- SIN, COS, SINH, LOG, ETC.

- ROUTINES ARE BOTH MACHINE AND ACCURACY
INDEPENDENT
- ACCURACY DETERMINED WHEN LIBRARY
PACKAGES ARE INTEGRATED INTO USER
PROGRAM

INITIAL ADA COMPONENTS EVALUATION
MATHEMATICAL FUNCTIONS LIBRARY PACKAGE

- SPECIFICATION FOR ELEMENTARY MATH
FUNCTIONS PACKAGE

generic type real is digits < >;
package pac_el_fun is ...
  function exp(x : real) return real;
  function ln(x : real) return real;
  function log10(x : real) return real;
  function sqrt(x : real) return real;
  function cbrt(x : real) return real;
  function sin(x : real) return real;
  function cos(x : real) return real;
  function atan(x : real) return real;
  function cosh(x : real) return real;
  function sinh(x : real) return real;
  function tan(x : real) return real;
  function tanh(x : real) return real;
  function acosh(x : real) return real;
  function asinh(x : real) return real;
  function atan2(y, x : real) return real;
  function root(n : integer; y : real) return real;
end pac_el_fun

120
APPROXIMATIONS CALCULATED DIRECTLY FROM CHEBYSHEV POLYNOMIALS USING A METHOD INTRODUCED BY C. W. CLENSHAW, "CHEBYSHEV SERVICES FOR MATHEMATICAL FUNCTIONS," "NATIONAL PHYSICS LABORATORY MATHEMATICAL TABLES," VOL. 5, HER MAJESTY'S STATIONERY OFFICE, LONDON, 1962

TECHNICAL REPORT ON THE LIBRARY GIVEN BY L. J. GALLAHER, "A LIBRARY OF ELEMENTARY MATH FUNCTIONS IN ADA," IRAD R626, LOCKHEED-GEORGIA COMPANY, MARIETTA, GEORGIA, JANUARY, 1987

INITIAL ADA COMPONENTS EVALUATION SSE IV&V CODE COMPLEXITY METRICS

WHAT ARE THE TYPES OF CODE COMPLEXITY METRICS?

- CODE COMPLEXITY METRICS
  - HALSTEAD'S SOFTWARE SCIENCE METRICS
  - McCabe's Measure of Cyclomatic Complexity

- COMPUTED IN SSE IV&V'S SOFTWARE AUTOMATED VERIFICATION & VALIDATION SYSTEM (SAVVAS)
WHY USE HALSTEAD'S SOFTWARE SCIENCE METRICS?

- COMPiled FROM THE NUMBER OF DISTINCT OPERATORS, DISTINCT OPERANDS, AND TOTAL NUMBER OF OCCURRENCES OF OPERATORS AND OPERANDS
- GIVES AN INDICATION OF THE PHYSICAL SIZE OF A PROGRAM IN TERMS OF OPERATORS AND OPERANDS. VARIOUS SIZE METRICS ARE GIVEN
- USED DIAGNOSTICALLY TO POINT TO POTENTIAL PROBLEMS

HALSTEAD'S SOFTWARE SCIENCE METRICS

- BASED ON THE NUMBER OF OPERATORS AND OPERANDS ON A LOGICAL UNIT OF CODE
- OPERATORS INCLUDE ARITHMETIC OPERATORS, BOOLEAN OPERATORS, DELIMITERS
- OPERANDS ARE VARIABLES AND CONSTANTS
- FOR EACH UNIT OF CODE LET:

\[
\begin{align*}
n_1 &= \text{THE NUMBER OF DISTINCT OPERATORS} \\
n_2 &= \text{THE NUMBER OF DISTINCT OPERANDS} \\
N_1 &= \text{THE TOTAL NUMBER OF OCCURRENCES OF THE OPERATORS} \\
N_2 &= \text{THE TOTAL NUMBER OF OCCURRENCES OF THE OPERANDS}
\end{align*}
\]
INITIAL ADA COMPONENTS EVALUATION
SSE IV&V CODE COMPLEXITY METRICS

- LENGTH: \( N = N_1 + N_2 \)
- VOCABULARY: \( W = n_1 + n_2 \)
- VOLUME: \( V = N \times \log_2 W \)
- LEVEL: \( L = \frac{2 \times n_2}{n_1 \times N_2} \)
- DIFFICULTY: \( D = \frac{1}{L} \)
- EFFORT: \( E = \frac{V}{L} \)
- ERROR ESTIMATE: \( B = \frac{E^{2/3}}{E_0}; E_0 = 3000 \)
  \( B = \text{NO. OF BUGS IN A PROGRAM} \)

- INTERPRETATION OF HALSTEAD'S METRICS

  THE LENGTH \( N \) SERVES AS A MEASURE OF MODULARITY. A LENGTH OF GREATER THAN 260 INDICATES POOR QUALITY CODE. THE CODE SHOULD (PROBABLY) BE REDUCED TO MORE AND SMALLER MODULES

  THE VOLUME \( V \) REPRESENTS THE SIZE (IN BITS) OF A LOGICAL UNIT OF CODE

  THE LEVEL \( L \) IS A MEASURE THAT RELATES TO THE EFFORT OF WRITING, PROPENSITY (INCLINATION) FOR ERROR, AND EASE OF UNDERSTANDING OF A LOGICAL UNIT OF CODE
INITIAL ADA COMPONENTS EVALUATION
SSE IV&V CODE COMPLEXITY METRICS

THE DIFFICULTY $D$, THE RECIPROCAL OF LEVEL, INDICATES THE DIFFICULTY IN UNDERSTANDING AND MAINTAINING THE CODE. A DIFFICULTY GREATER THAN 190 TENDS TO INDICATE A POOR QUALITY OF CODE.

THE EFFORT $E$ IS A MEASURE OF THE RELATIVE AMOUNT OF WORK INVOLVED IN PRODUCING A PIECE OF CODE.

THE ERROR ESTIMATE $B$ (BUGS) IS THE ESTIMATED NUMBER OF ERRORS IN THE CODE.

---

**Operator Parameters**

<table>
<thead>
<tr>
<th>Operator</th>
<th>$j$</th>
<th>$f_{1,j}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>;</td>
<td>1</td>
<td>9</td>
</tr>
<tr>
<td>:=</td>
<td>2</td>
<td>6</td>
</tr>
<tr>
<td>( ) or BEGIN...END</td>
<td>3</td>
<td>5</td>
</tr>
<tr>
<td>IF</td>
<td>4</td>
<td>3</td>
</tr>
<tr>
<td>=</td>
<td>5</td>
<td>3</td>
</tr>
<tr>
<td>/</td>
<td>6</td>
<td>1</td>
</tr>
<tr>
<td>-</td>
<td>7</td>
<td>1</td>
</tr>
<tr>
<td>x</td>
<td>8</td>
<td>1</td>
</tr>
<tr>
<td>RETURN</td>
<td>9</td>
<td>1</td>
</tr>
<tr>
<td>EXIT</td>
<td>10</td>
<td>1</td>
</tr>
</tbody>
</table>

$n_1 = 10 \quad N_1 = 31$
INITIAL ADA COMPONENTS EVALUATION
SSE IV&V CODE COMPLEXITY METRICS

Operand Parameters

<table>
<thead>
<tr>
<th>Operand</th>
<th></th>
<th>j</th>
<th>( |_{2,j} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>B</td>
<td>1</td>
<td>6</td>
<td></td>
</tr>
<tr>
<td>A</td>
<td>2</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>O</td>
<td>3</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>R</td>
<td>4</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>G</td>
<td>5</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>GCD</td>
<td>6</td>
<td>2</td>
<td></td>
</tr>
</tbody>
</table>

\( n_2 = 6 \) \quad \text{AND} \quad n_2 = 21

WHY USE McCabe's Cyclomatic Complexity Metrics?

- Compiled from flowcharts transformed to equivalent directed graphs, the number of edges of the graphs, the number of nodes of the graphs and the number of separate parts of the graph.

- The McCabe Cyclomatic Complexity Metric (CCM) assists in breaking up a software program to components that have a small CCM < 10.

- Programs with large CCM should have more errors during development.
WHY USE McCABE'S CYCLOMATIC COMPLEXITY METRICS?
(Continued)

- THE CCM MAY BE USED TO DETERMINE THE MINIMUM NUMBER OF PATHS NEEDED.
- THE CCM RELATES ONLY TO LOGICAL COMPLEXITY. THE CCM SHOULD BE USED IN CONJUNCTION WITH OTHER METRICS

McCABE'S CYCLOMATIC COMPLEXITY METRIC

McCABE'S CYCLOMATIC COMPLEXITY METRIC IS A MEASURE OF THE TOTAL NUMBER OF LINEARLY INDEPENDENT PATHS THOUGH THE CODES CONTROL STRUCTURE

TO CALCULATE CYCLOMATIC COMPLEXITY, FLOW-CHARTS ARE TRANSFORMED TO EQUIVALENT DIRECTED GRAPHS
McCABE'S CYCLOMATIC COMPLEXITY METRIC
(Continued)

COMPLEXITY MEASURE OF A PROGRAM IS A FUNCTION OF THE NUMBER OF DECISIONS IN A PROGRAM AND IS GIVEN BY A SINGLE NUMBER KNOWN AS A CYCLOMATIC NUMBER

COMPLEXITY MEASURE IS INDEPENDENT OF THE PHYSICAL SIZE OF THE PROGRAM

DEFINITIONS:

A GRAPH IS A TREE STRUCTURE CONSISTING OF NODES CONNECTED BY BRANCHES

A DIRECTED GRAPH IS A GRAPH IN WHICH A DIRECTION OR FLOW IS ASSOCIATED WITH EVERY BRANCH
DEFINITIONS: (Continued)

A STRONGLY CONNECTED GRAPH IS A GRAPH THAT HAS A UNIQUE ENTRY AND EXIT NODE AND EACH NODE CAN BE REACHED FROM EVERY OTHER NODE

![Strongly Connected Diagram](image1)

![Not Strongly Connected Diagram](image2)

EXAMPLE
CONTROL GRAPH $G$

SOME POSSIBLE PATHS

- abef
- beb
- abea
- acfa
- adcia
- abefa
- 2beb
- abea
DEFINITION:

THE CYCLOMATIC NUMBER $V(G)$ OF A GRAPH $G$ WITH $n$ NODES AND $e$ BRANCHES AND $p$ CONNECTED COMPONENTS IS

$$V(G)=e-n+2p;$$

IN THE EXAMPLE CONTROL GRAPH $G$:

NUMBER OF NODES = 6
NUMBER OF BRANCHES = 10
$V(G) = 10 - 6 + 2(1) = 6$

GRAPH EXAMPLES:

<table>
<thead>
<tr>
<th>CONTROL SEQUENCE</th>
<th>STRUCTURE</th>
<th>CYCLOMATIC COMPLEXITY $V = e - n + 2p$</th>
</tr>
</thead>
<tbody>
<tr>
<td>IF THEN ELSE</td>
<td></td>
<td>$V = 4 - 4 + 2 = 2$</td>
</tr>
<tr>
<td>WHILE</td>
<td></td>
<td>$V = 3 - 3 + 2 = 2$</td>
</tr>
</tbody>
</table>
GRAPH EXAMPLE WITH \( p = \) NO. OF COMPONENTS = 3

SUPPOSE A PROGRAM \( M \) AND TWO CALLED SUBPROGRAMS \( A \) AND \( B \) HAVE THE FOLLOWING CONTROL STRUCTURE:

\[
\begin{align*}
\text{Mt} & \quad \rightarrow \quad A: \quad \rightarrow \quad B: \\
& \quad \downarrow \quad \quad \downarrow \\
& \quad \circ \quad \circ \quad \circ
\end{align*}
\]

THEN \( G = M \cup A \cup B \) AND \( p = 3 \)

THEN \( V(G) = V(M \cup A \cup B) = 13 \cdot 13 + 2 \cdot 3 = 6 \)

NOTE: \( V(M \cup A \cup B) = V(M) + V(A) + V(B) \)

- PROPERTIES OF THE CYCLOMATIC COMPLEXITY

1. \( V(G) \geq 1 \)

2. \( V(G) \) IS THE MAXIMUM NUMBER OF (LINEARLY) INDEPENDENT PATHS IN \( G \); IT IS THE SIZE OF A BASIS SET (i.e., ALL COMBINATIONS OF PATHS IN THE CODE ARE MADE UP FROM PATHS IN \( G \))

3. INSERTING OR DELETING FUNCTIONAL STATEMENTS TO \( G \) DOES NOT AFFECT \( V(G) \)

4. \( G \) HAS ONLY ONE PATH IF AND ONLY IF \( V(G) = 1 \)
PROPERTIES OF THE CYCLOMATIC COMPLEXITY
(Continued)

5. INSERTING A NEW EDGE IN G INCREASES V(G) BY UNITY

6. V(G) DEPENDS ONLY ON THE DECISION STRUCTURE OF G

V(G) ASSISTS IN BREAKING UP A SOFTWARE PROGRAM TO COMPONENTS THAT HAVE A SMALLER COMPLEXITY NUMBER. McCABE RECOMMENDS THAT EACH COMPONENT G HAS A V(G) LESS THAN 10

SAVVAS-ADA-McCABE'S CCM

0 COUNT THE NUMBER OF "CASE" STATEMENT BRANCHES AND SET THIS NUMBER EQUAL TO m₁

CASE TODAY IS

1) WHEN MON => OPEN_ACCOUNTS;
   => COMPUTE_INITIAL_BALANCE;

1) WHEN TUE..THU => GENERATE_REPORT (TODAY);

1) WHEN FRI => COMPUTE CLOSING_BALANCE;
   => CLOSE_ACCOUNTS:

1) WHEN SAT/SUN => NULL

4 END CASE;

4 BRANCHES
COUNT THE NUMBER OF "IF STATEMENT" BRANCHES AND SET THIS NUMBER TO $m_2$

1) IF WEATHER_CONDITION = RAIN THEN
   COMPUTE_RAINFALL;
1) ELSIF WEATHER_CONDITION = SUNSHINE THEN
   COMPUTE_HUMIDITY;
1) ELSE
   COMPUTE_PRES;
   END IF;

3 3 BRANCHES

COUNT THE NUMBER OF "LOOP BRANCHES" AND SET THIS NUMBER TO $m_3$

1) FOR I IN 1..10 LOOP
1)   FOR J IN 1..20 LOOP
    IF A(I,J) = 0 THEN
      M:=I;
      N:=J;
      EXIT FIND;
    END IF;
   END LOOP;
  END LOOP FIND;

2 LOOP BRANCHES 1 "IF STATEMENT" BRANCHES
3 BRANCHES
CCM=\log_2 m_1+m_2+m_3
## INITIAL ADA COMPONENTS EVALUATION
SAVVAS CCM RESULTS APPLIED TO ADA
MATHEMATICAL FUNCTIONS LIBRARY

<table>
<thead>
<tr>
<th>UNIT NAME</th>
<th>McCabe V(g)</th>
<th>HALSTEAD's Length Metric (260)</th>
<th>HALSTEAD's Difficulty Metric (190)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Average</td>
<td>3</td>
<td>82</td>
<td>16.018</td>
</tr>
<tr>
<td>ln</td>
<td>1</td>
<td>32</td>
<td>5.25</td>
</tr>
<tr>
<td>tanh</td>
<td>3</td>
<td>74</td>
<td>16.7</td>
</tr>
<tr>
<td>t_aux_fun</td>
<td>1</td>
<td>163</td>
<td>25.84</td>
</tr>
<tr>
<td>pac_aux_fun</td>
<td>1</td>
<td>215</td>
<td>32.045</td>
</tr>
<tr>
<td>remainder</td>
<td>4</td>
<td>90</td>
<td>34.833</td>
</tr>
<tr>
<td>pac_el_fun</td>
<td>1</td>
<td>868</td>
<td>19.989</td>
</tr>
</tbody>
</table>

## SUMMARY

- **CCM DIRECTED IV&V APPLIED TO THE SSE ADA MATHEMATICAL FUNCTION LIBRARY PACKAGE INDICATED A HIGH QUALITY OF SOFTWARE PRODUCTS**

- **IN HALSTEAD'S SOFTWARE SCIENCE METRICS, A LENGTH OF GREATER THEN 260 OR DIFFICULTY GREATER THAN 190 TENDS TO INDICATE POOR QUALITY CODE**

- **McCABE HAS SUGGESTED THAT A CYCLOMATIC COMPLEXITY OF 10 SHOULD BE THE UPPER LIMIT FOR V(G) (CYCLOMATIC COMPLEXITY MEASURE FOR A GRAPH G)**

- **THE ADA VERSION OF SAVVAS MAY BE USED FOR COMPUTING CODE COMPLEXITY METRICS**