NETRA—A PARALLEL ARCHITECTURE FOR INTEGRATED VISION SYSTEMS I: ARCHITECTURE AND ORGANIZATION

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NETRA - A Parallel Architecture for Integrated Vision Systems I:  
Architecture and Organization

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1. Introduction

Computer vision has been regarded as one of the most complex and computationally intensive problems. The algorithms involved employ a very broad spectrum of techniques from several areas such as signal processing, advanced mathematics, graph theory, and artificial intelligence. These algorithms are, in general, characterized by massive parallelism. For low level processing, spatial decomposition of image provides a natural way of generating parallel tasks. For higher level processing operations, parallelization may also be based on other image characteristics. The multi-dimensional divide-and-conquer paradigm [3] is an attractive mechanism for providing parallelism in both of the above cases.

There is no general definition of an Integrated Vision System (IVS). However, an application dependent definition of an IVS is possible. For example, an object recognition, system that takes an image (or a set of images) of an object as input and produces as an output a description of the object can be considered an IVS. However, a system (or an algorithm) that takes an image input and produces its Discrete Fourier Transform (DFT) is not considered an IVS though computing DFT itself may be a part of an IVS. Therefore, IVS can be viewed as a system which employs a number of vision algorithms in a systematic way to produce a specified output. In this paper we are interested in an IVS from the viewpoint of complexity and execution of the necessary computations. An architecture for vision must be powerful as well as general enough to efficiently execute algorithms for any given computer vision problem. Researchers in vision and architecture communities are recognizing the need for architectures that are suited for IVSs rather than those architectures that are good for a few applications but are too rigid to perform any other applications efficiently. In [4] Weems et al. present an integrated image understanding benchmark that consists of algorithms that may comprise an object recognition system.

The advent of VLSI technology has provided architects to produce high performance chips for specific applications. But these special purpose chips can only be used in an IVS as accelerators of specific algorithms (e.g., convolution chips or FFT chips). Another use of VLSI technology has been to create massively parallel Single Instruction Multiple Data (SIMD) processors for vision and other applications. Massively parallel SIMD processors are well suited for low level and well structured vision algorithm that exhibit spatial parallelism at pixel level. However, such architectures are not well suited for high level vision algorithm because high level vision algorithms require non-uniform processing, more complex data structures and data dependent decision making capabilities. Furthermore, mapping a parallel algorithm on such architectures becomes really inefficient when the problem size does not
match with the available processor size and when its communication requirements do not match with the underlying interconnection structure of the parallel processor machine.

Meshes, array processors, hypercubes and pyramids are some of the most common SIMD parallel processors proposed for image analysis and processing. In meshes, the processing elements are arranged in a square array. Examples of mesh connected computers include CLIP4 [5,6,7], and the MPP [8,9,10]. In [11], Ahuja and Swamy proposed multiprocessor pyramid architecture of the divide-and-conquer based approach model of computation. Such pyramids are, therefore, natural candidates for executing divide-and-conquer algorithms that closely mirror the flow of information in these algorithms. Example of other pyramid architectures include PAPIA [12], SPHINX [13], MPP pyramid [14], and HCL Pyramid [15,16]. However, design of an integrated vision system requires a greater flexibility, partitionability, and reconfigurability than is offered by regular array, mesh connected or pyramid structures as discussed in [1]. For this reason other multiprocessor architectures and parallel algorithms have been proposed [17,18,19,20], some of which discuss the flexibility, partitionability, and reconfigurability issues. CMU Warp processor [21,22,23,24] is another machine proposed and built for image understanding. The machine has a programmable systolic array of linearly connected cells. The array can perform low level and high level vision algorithms in systolic mode for low level operations and in MIMD mode for high level operations. There are unique features in the Warp processor that are not present in other architectures. The machine can be reconfigured in several modes [25]. The UMass image understanding architecture is based on Content Addressable Array Parallel Processor for low level vision and a MIMD parallel processor for high level vision [26].

The effectiveness and performance of architectures such as pyramid, array processors, and meshes is limited as architectures for integrated vision systems due to several reasons. First, they are mostly suitable for SIMD type of algorithms which only constitute low level vision operations. Secondly, the architectures are inflexible due to the rigid interconnections. Third, the number of processors needed to solve a problem of reasonable size is thousands. Such a large number of processors is not only cost prohibitive, but the processors themselves cannot be very powerful and can have only limited features due to technological limitations. Fourth, it is normally assumed that the problem size exactly matches the number of processors available. Most of the time it is not clear how to adapt algorithms so that problems of different sizes can be solved using the same number of processors. Finally, the problem of input-output of data and fault-tolerance is rarely addressed in any of these architectures. It is important to note that no matter how fast or powerful a particular architecture is, its utilization can be limited by the bandwidth of the
I/O. Furthermore, a failure normally either results in a breakdown of the entire system or the performance degrades tremendously. It is important that the architecture provide for graceful degradation. Graceful degradation can be achieved by providing flexibility in the interconnection and a capability for dynamic reconfiguration and partitioning of the architecture.

In this paper, we present a parallel architecture called NETRA for IVSs which is intended to provide the above flexibility. The architecture was originally proposed by Sharma, Patel and Ahuja [1]. NETRA is a recursively defined tree-type hierarchical architecture each of whose leaf nodes consists of a cluster of processors connected with a programmable crossbar with selective broadcast capability. The internal nodes are scheduling processors whose function is task scheduling, load balancing, and global memory management. All the scheduling processors and the cluster processors are connected to a global memory through a multistage circuit switched network. The processors in clusters can operate in SIMD, MIMD or systolic mode, and therefore, are suitable for both low level as well as high level vision algorithms.

In Section 2 we propose a model of computation for integrated vision systems. The model is discussed from the parallel processing perspective. Using the model we derive desired features and capabilities of a parallel architecture for IVSs. Section 3 presents the architecture of NETRA and describes its components and their functions in detail. Then the architecture is critically examined with respect to the IVS requirements. In Section 4 we present methods to map parallel algorithms on NETRA. We also discuss the alternative communication strategies in NETRA and present a qualitative evaluation of the strategies. The algorithms are classified according to their computation and communication requirements for parallel processing. Section 5 presents analysis of alternative inter-cluster communication strategies in NETRA and discusses a methodology to evaluate a parallel algorithm which has been mapped across clusters. Finally, a summary is presented in Section 6.


There are two types of parallelism available in vision tasks. First, Spatial Parallelism, in which the same operation is applied to all parts of the image data. That is, the data is divided into many granules and distributed to different subtasks which may execute on different processors in parallel. Most low level vision algorithms exhibit this type of parallelism. However, different tasks may be performed sequentially in time on the same granules of data. Each such task operates on the output data of the previous task. Therefore, the type of data, data structures, etc.,
may be different for each task in the system but each form of data can be partitioned into several granules, to be processed in parallel. For example, consider one IVS that performs object recognition. The input image is smoothed using some filtering operation, then on the smoothed image an operator is applied for feature extraction, features with similar characteristics are grouped, then matching with the models is performed. Each of these tasks takes the output of the previous tasks as its input and produces an output which becomes the input for the next task.

Second form of parallelism called *Temporal Parallelism* is available when these tasks are repeated on a time sequence of images or on different resolutions of images. For example, the system in which the motion of a moving object is estimated from an image sequence performs the same set of computation on all image frame(s) in the sequence. The processing of each frame or sets of frames can be done in parallel.

Figure 1 shows a computational model of IVS which incorporates the above mentioned characteristics. Each pipeline shows a number of tasks applied to a set of inputs. Each block in the pipeline represents one task. The input to the first task in a pipeline is the image, and the input to the rest of the tasks is the output of the previous task. Entire pipeline of tasks is repeated at different images in time and/or resolution. Each task is decomposed into subtasks to be performed in parallel. For example, $T_1$ is one task, and $T_1(d_1)$ is a subtask of $T_1$ operating on data granule $d_1$. The figure shows $m$ tasks in the pipeline. The number of subtasks depends on the amount of data in a granule and number of available processors. $D_{i,i+1}$ represents data transfer from task $T_i$ to task $T_{i+1}$ in the pipeline.

2.1. Data Dependencies

Existence of spatial and temporal parallelism may also result in two types of data dependencies, namely, *spatial data dependency* and *temporal data dependency*. The spatial data dependency can be classified into intratask data dependency and intertask data dependency. Intratask data dependency arises when a set of subtasks need to exchange data in order to execute a task in parallel. The exchange of data may be needed during the execution of the algorithm, or to combine their partial results, or both. Therefore, each task itself is a collection of subtasks which may be represented as a graph with nodes representing the subtasks and edges representing communication between subtasks. Intertask data dependency denotes the transfer and reorganization of data to be passed onto the next task in the pipeline. This may be done by exchanging data between subtasks of the current tasks and the subtasks of the next task, or by collection and reorganization of the output data of current task and then redistribution of the data.
Figure 1: A Computational Model of an Integrated Vision System

The choice and method depends on the underlying parallel architecture and mapping of the algorithms. Temporal data dependency is similar to spatial data dependency except that some form of output generated by tasks executed on the previous image frames may be needed by one or more tasks executing on the current image frames. A simple example of such a dependency is the system for motion estimation in which features from the previous image frames are needed in the processing of the current image frames so that features can be matched to establish correspondences between features of different time frames.
The total computation to execute one pipeline includes time to input data, time to output data and results, sum of the times to execute all tasks in the pipeline (which includes computation time of subtasks and communication time between subtasks) and, data transfer and reorganization time between two successive tasks. Let's denote $t_{cp}$ as computation time for a subtask, $t_{comm}$ as total communication time for a task, $t_{in}$ as data input time, $t_{out}$ as data output time, and $t_d$ as data transfer and reorganization time. Then the time to complete task $i$, denoted as $\tau_i$, is given by

$$\tau_i = \max_{1s/2s} t_{cp}(T_i(d_j)) + t_{comm}(T_i)$$

(1)

Total time to execute one pipeline including the input and output of the data is given by

$$t_{tot} = \sum_{i=1}^{i=m} \tau_i + \sum_{i=1}^{i=m-1} t_d(D_{i,i+1}) + t_{in} + t_{out}$$

(2)

Let us now consider some characteristics of the algorithms involved in IVS, and using the above model determine the desired features and capabilities of a multiprocessor architecture suitable for IVS. First, an IVS involves algorithms from all levels of processing, i.e., an IVS normally includes low, intermediate and high level vision algorithms. Typically, the first few tasks of the pipeline require low level algorithms and last few require high level algorithms. The low level algorithms are well understood and well defined. They are normally data independent, have regular structure, and spatial parallelism is mostly available at pixel level. They are well suited for both SIMD and MIMD type of processing. If communication between processors is fast enough, almost linear speedups are possible by using multiple processors. Therefore, an architecture for IVS should be capable of efficiently executing low level algorithms and algorithms suited for SIMD type of processing. Also, data I/O should not be a bottleneck because otherwise, speedups through parallelism can be nullified. Examples of low level algorithms include various transforms, filtering algorithms, convolution algorithms etc.

High level algorithms are not well catalogued. They are normally global data dependent, involve more complex data structures (compared to pixel representation), and need varying amount of communication for parallel processing. These type of algorithms are better suited for MIMD type of processing. Hence, the architecture should be capable of executing MIMD algorithms efficiently.
2.2. Desired Features and Capabilities of Parallel Architectures for IVS

(1) Reconfigurability: From the model and the above discussion it is clear that the architecture should be capable of executing both SIMD and MIMD type of algorithms efficiently. That is, it should be possible to reconfigure the architecture such that each algorithm can be implemented efficiently using the most suited mode of computation.

(2) Flexible Communication: The communication requirements vary for different algorithms. The communication pattern between processors executing subtasks of a larger task depends on the algorithm involved in the task. If the connectivity between processors is too rigid then the communication overhead of intratask and intertask communication may become prohibitive. Therefore, it is desirable that the communication be flexible in order to provide most efficient communication with low overhead.

(3) Resource Allocation and Partitionability: As we discussed earlier, there are several tasks with vastly different characteristics and computational requirements in an IVS. These tasks need to exist simultaneously in the system. Therefore, the system should be partitionable into many independently controlled subsystems to execute each task. Since the high level algorithms exhibit varying level of parallelism and data dependent performance, it should be possible to allocate resources (such as processors, memory) dynamically to meet the performance requirements.

(4) Load Balancing and Task Scheduling: Load balancing and task scheduling are very important, specially for high level vision algorithms. High level vision algorithms are data dependent, and therefore, in order to obtain better utilization of resources and better speedups, dividing the computation equally among the processor is critical [27]. The underlying architecture on which load balancing is done and the type of algorithm(s) involved contribute significantly to how well load balancing can be achieved. In low level algorithms since the computations are data independent, partitioning data equally among the processors normally balances the load among the processors. However, for high level algorithms more sophisticated load balancing and scheduling strategies are needed. The architecture should include features such that it is easy to perform load balancing and task scheduling and that the overhead of doing so is minimal.

(5) Topology and Data Size Independent Mapping: For a system as complex as an IVS, if the underlying architecture is rigid such that the problem size that can be solved on it dependent on the size of the architecture, the effectiveness of the architecture for an IVS will diminish.
Input-Output of Data: It is most often the case that an architecture is able to perform very well on some algorithms and high speedups are obtained but input-output (I/O) of data is inefficient. I/O is an integral part of a system and if it is a bottleneck then performance of the system will be limited.

Fault-Tolerance: Fault-tolerance is an important part of a system of such complexity. A failure in a processor or communication structure should not affect the performance drastically which is normally the case when rigid interconnections are present between processors. The architecture should provide for graceful degradation in case of failures.

3. Architecture of NETRA

In this section we describe the architecture of NETRA and its features. We examine and evaluate the characteristics of the architecture using the criteria developed in the previous section.

Figure 2 shows the architecture of "NETRA" for integrated vision systems. The architecture consists of the following components:-

(1) A large number (1000 - 10000) of Processing Elements (PEs), organized into clusters of 16 to 64 PEs each.

(2) A tree of Distributing-and-Scheduling-Processors (DSPs) that make up the task distribution and control structure of the multiprocessor.

(3) A parallel pipelined shared Global Memory and a Global Interconnection that links the PEs and DSPs to the Global Memory.

3.1. Processor Clusters

The clusters consist of, 16 to 64 PEs, each with its own program and data memory. They form a layer below the DSP-tree, with a leaf DSP associated with each cluster. PEs within a cluster also share a common data memory. The PEs, the DSP associated with the cluster, and the shared memory are connected together with a crossbar switch. The crossbar switch permits point-to-point communications as well as selective broadcast by the DSP or any of the PEs. Figure 3 shows the cluster organization. A 4x4 crossbar is shown as an example of the implementation of the crossbar switch. The crossbar design consists of pass transistors connecting the input and output data lines. The switches are controlled by control bits indicating the connection pattern. If a processor of DSP needs to broadcast then all the control bits in its row are made one. In order to connect processor $P_i$ to processor $P_j$, control bit $(i,j)$ is
Clusters can operate in an SIMD mode, a systolic mode, or an MIMD mode. Each PE is a general purpose processor with a high speed floating point capability. In an SIMD mode, PEs in a cluster execute identical instruction streams from private memories in a lock-step fashion. In the systolic mode, PEs repetitively execute an instruction or set of instruction on data streams from one or more PEs. In both cases, communication between PEs is synchronous. In the MIMD mode PEs asynchronously execute instruction streams resident in their private memories.
The streams may not be identical. In order to synchronize the processors in a cluster, a synchronization bus is provided which is used by processors to indicate to the DSP that a processor(s) has finished its computation or a processor wants to change the communication pattern. The DSP can either poll the processors or the processors can interrupt the DSP using the synchronization bus.
3.1.1. Crossbar Design

There is no arbitration in the crossbar switch. That is, the interconnection between processor has to be programmed before processors can communicate with each other. Programming a crossbar requires writing a communication pattern into the control memory of the crossbar. A processor can alter the communication pattern by updating the control memory as long as it does not conflict with the existing communication pattern. The DSP associated with the cluster can write into the control memory to alter the communication pattern. The most common communication patterns such as linear arrays, trees, meshes, pyramids, shuffle-exchanges, cubes, broadcast, can be stored in the memory of the crossbar. These patterns need not be supplied externally. Therefore, switching to a different pattern in the crossbar can be fast because switching only requires writing the patterns into the control bits of the crossbar switches from its control memory.

The advantages of such a crossbar design are the following: first, since there is no arbitration, the crossbar is relatively faster than one which provides arbitration because switching and arbitration delays are avoided. Secondly, it is easier to design and implement the crossbar because arbitration is absent, and therefore, switches are simple. Furthermore, it is possible to implement systolic algorithms using the crossbar because it can transfer data at the same or greater speed than required by the systolic computation. Such a crossbar is easily scalable. Unlike other interconnections (such as cubes, shuffle-exchanges etc.), the scalability need not be in power of 2. A unit scalability is possible. Furthermore, due to the same reason, it is easy to provide fault-tolerance because one spare processor can replace any failed processor, and one extra crossbar link can replace any failed link. This is possible because there is no inherent structure that connects the processor and each processor (link) is topologically equivalent to any other processor (link).

3.1.2. Scalability of Crossbar

Figure 4(a) depicts a 1 bit 4×4 crossbar switch. In order to obtain byte or word parallel crossbar, the crossbar switches can be stacked together as shown in figure 4(b). The control, address and communication pattern information is exactly the same in all the stacked switches. Figure 4(c), (d) and (e) illustrate the size scalability. Figure 4(c) shows how a 4×8 crossbar can be obtained from two 4×4 crossbars. Similarly, figure 4(d) and (e) illustrate how 8×4 and 8×8 crossbars can be obtained respectively. Note that the smallest switch need not be a bit crossbar. Depending on the technology and availability of the I/O pins, it can be of any size (such as 4 bit or a byte). Further-
more, depending on the available pins, it can be a 16x16 or 32x32 bit crossbar. Finally, sizes of the crossbar need not be a multiple of two but can be any arbitrary.

3.2. The DSP Hierarchy

The DSP-tree is an n-tree with nodes corresponding to DSPs and edges to bi-directional communication links. Each DSP node is composed of a processor, a buffer memory, and a corresponding controller.

The tree structure has two primary functions. First it represents the control hierarchy for the multiprocessor. A DSP serves as a controller for the subtree structure under it. Each task starts at a node on an appropriate level in the tree, and is recursively distributed at each level of the sub-tree under the node. At the bottom of the tree, the sub-tasks are executed on a processor cluster in the desired mode (SIMD or MIMD) and under the supervision of the leaf DSP.

![Figure 4: Scalability of Crossbar](image-url)
The second function is that of distributing the programs to leaf DSPs and the PEs. Vision algorithms are characterized by a large number of identical parallel processes that exploit the spatial parallelism and operate on different data sets. It would be highly wasteful if each PE issued a separate request for its copy of the program block to the global memory because it would result in large unnecessary traffic through the interconnection network. Under the DSP-hierarchy approach, one copy of the program is fetched by the controlling DSP (the DSP at the root of the task subtree) and then broadcast down the subtree to the selected PEs. Also, DSP hierarchy provides communication paths between clusters to transfer control information or data from one cluster to others. Finally, the DSP-tree is responsible for Global Memory management.

3.3. Global Memory

The multiport global memory is a parallel-pipelined structure as introduced in [28]. Given a memory(chip)-access-time of $T$ processor-cycles, each line has $T$ memory modules. It accepts a request in each cycle and responds after a delay of $T$ cycles. Since an $L$-port memory has $L$ lines, the memory can support a bandwidth of $L$ words per cycle.

Data and programs are organized in memory in blocks. Blocks correspond to "units" of data and programs. The size of a block is variable and is determined by the underlying tasks and their data structures and data requirements. A large number of blocks may together constitute an entire program or an entire image. Memory requests are made for blocks. The PEs and DSPs are connected to the Global Memory with a multistage interconnection network.

The global memory is capable of queueing requests made for blocks that have not yet been written into. Each line (or port) has a Memory-line Controller (MLC) which maintains a list of read requests to the line and services them when the block arrives. It maintains a table of tokens corresponding to blocks on the line, together with their length, virtual address and full/empty status. The MLC is also responsible for virtual memory management functions.

Two main functions of the global memory are input-output of data and program to and from the DSPs and processor clusters, and to provide intercluster communication between various tasks as well as within a task if a task is mapped onto more than one cluster.
3.4. Global Interconnection

The PEs and the DSPs are connected to the Global Memory using a multistage circuit-switching interconnection network. Data is transferred through the network in pages. A page is transferred from the global memory to the processors which is given in the header as a destination port address and the header also contains the starting address of the page in the global memory. When the data is written into the global memory, only starting address needs to be stated. In each case, end-of-page may be indicated using an extra flag bit appended to each word.

We are evaluating an alternative strategy to connect DSPs, clusters and the global memory using a high speed bus. In this organization one port of each cluster will be connected to the high speed bus. Also, each DSP will be connected to the bus. Processors that need to communicate with processors in other clusters use explicit messages to send and receive data from the other processors. Figure 5 illustrates this method. A processor \( P_i \) in cluster \( C_i \) can send data to a processor \( P_j \) in cluster \( C_j \) as shown in the figure. \( P_i \) sends the data to the \( DSP_i \) which sends the data to \( DSP_j \) in a burst mode. \( DSP_j \) then sends the data to the processor \( P_j \). We are evaluating both alternatives for intercluster communication.

![Figure 5: An Alternative Strategy for Inter-Cluster Communication](image)
3.5. IVS Computation Requirements and NETRA

In the following discussion we examine NETRA's architecture in the light of requirements for an IVS discussed in the previous section.

Reconfigurability (Computation Modes)

The clusters in NETRA provide SIMD, MIMD and systolic capabilities. As we discussed earlier, it is desirable to have these modes of operations in a multiprocessor system for IVS so that all levels of algorithms can be executed efficiently. For example, consider matrix multiplication operation. We will show how it can be performed in SIMD and systolic modes. Let us assume that the computation requires obtaining matrix $C = A \times B$. For simplicity, let's assume that the cluster size is $P$ and the matrix dimensions are $P \times P$. Note that this assumption is made to simplify the example description. In general, any arbitrary size computation can be performed independent of the data or cluster size.

SIMD Mode

The algorithm can be mapped as follows. Each processor is assigned a column of the $B$ matrix, i.e., processor $P_i$ is assigned column $B_i$. Then the DSP broadcasts each row to the cluster processor which compute the inner product of the row with their corresponding column in lock-step fashion. Note that the elements of the $A$ matrix can be continuously broadcast by DSP, row by row without any interruptions, and therefore, efficient pipelining of data input, multiply, accumulate operations can achieved. Figure 6(a) illustrates a SIMD configuration of a cluster. The following pseudo code describes the DSP and processor ($P_k$'s program, $0 \leq k \leq P - 1$) program.

**SIMD Computation**

<table>
<thead>
<tr>
<th>DSP</th>
<th>$P_k$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. FOR $i=0$ to $i=P-1$ DO</td>
<td>1.</td>
</tr>
<tr>
<td>2. connect(DSP, $P_i$)</td>
<td>2.</td>
</tr>
<tr>
<td>3. out(column $B_i$)</td>
<td>3. in(column $B_i$)</td>
</tr>
<tr>
<td>4. END_FOR</td>
<td>4.</td>
</tr>
<tr>
<td>5. connect(DSP, all)</td>
<td>5.</td>
</tr>
<tr>
<td>6. FOR $i=0$ to $i=P-1$ DO</td>
<td>6. $c_{ik} = 0$</td>
</tr>
<tr>
<td>7. FOR $j=0$ to $j=P-1$ DO</td>
<td>7. FOR $j=0$ to $j=P-1$ DO</td>
</tr>
<tr>
<td>8. out($a_{ij}$)</td>
<td>8. in($a_{ij}$)</td>
</tr>
<tr>
<td>9. END_FOR</td>
<td>9. $c_{ik} = c_{ik} + a_{ij} \times b_{jk}$</td>
</tr>
<tr>
<td>10. END_FOR</td>
<td>10. END_FOR</td>
</tr>
</tbody>
</table>
In the above code, the computation proceeds as follows. In first three lines, the DSP connects with each processor through the crossbar and writes the column on the output port. That column is input by the corresponding processor. In statement 5, the DSP connects with all the processors in a broadcast mode. Then from statement 6 onwards, the DSP broadcasts the data from matrix A in row major order and each processor computes the inner product with each row. Finally, each processor has a column of the output matrix. It should be mentioned that the above code describes the operation in principal and does not exactly depict the timing of operations.

Systolic Mode

The same computation can be performed in a systolic mode. The DSP can reconfigure the cluster in a circular linear array after distributing columns of matrix B to processors as before. Then DSP assigns row Ai of matrix A to processor Pi. Each processor computes the inner product of its row with its column and at the same time writes the element of the row on the output port. This element of the row is input to the next processor. Therefore, each processor receives the rows of matrix A in a systolic fashion and the computation is performed in the systolic fashion. Note that the computation and communication can be efficiently pipelined. In the code, it is depicted by statements 7-10. Each element of the row is used by a processor and immediately written on to the output port, and at the same time, the processor receives an element of the row of the previous processor. Therefore, every P cycles a processor computes new element of the C matrix from the new rows it receives every P cycles. Again, note that the code describes only the logic of the computation and does not include the timing information. Figure 6(b) illustrates a systolic configuration of a cluster.

<table>
<thead>
<tr>
<th>Systolic Computation</th>
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<tbody>
<tr>
<td><strong>DSP</strong></td>
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<tr>
<td>11.</td>
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</tbody>
</table>
In a companion paper we present several examples of mapping different algorithms in different modes on the clusters as well as their performance evaluation.

Partitioning and Resource Allocation

There are several tasks with vastly different characteristics in an IVS, and therefore, the number of processors needed for each task may be different and may be needed in different computational modes. Hence, partitionability and dynamic resource allocation are keys to high performance. Partitioning in NETRA can be achieved as follows. When a task is to be allocated, the set of subtrees of DSPs is identified such that the required number of PEs is available at their leaves. One of the subtrees is chosen on the basis of characteristics of the task. The chosen DSP represents the root of the control hierarchy for the task. Together with the DSPs in its subtree, it manages the execution of the task. Note that partitioning is only virtual. The PEs are not required to be physically isolated from the rest of the system. Once the subtree is chosen, the processes may execute in SIMD, MIMD or systolic mode. The following are some of the advantages of such a scheme. Firstly, only one copy of the programs needs to be fetched thereby reducing the traffic through the global interconnection network. Secondly, simple load balancing techniques may be employed while allocating tasks (examples are discussed in a companion paper). The tasks of global memory management can be distributed over the DSP tree by assigning it to the DSP at the root of the subtree executing the subtask. Finally, locality is maintained within the control hierarchy, which limits the intratask

![Diagram of SIMD and Systolic Modes](image-url)

**Figure 6**: An Example of SIMD and Systolic Modes of Computation in a Cluster
communication to within the subtree.

Load Balancing and Task Scheduling

Two levels of load balancing need to be employed, namely, global load balancing and local load balancing. Global load balancing aids in partitioning and allocating the resources for tasks as discussed earlier. Local load balancing is used to distribute computations (or data) to processors executing subtasks of a larger task. Local load balancing can be either static or dynamic or a combination of both. With static load balancing, given a task, its associated data and the number of processors allocated for the task, the data is partitioned in such a way that each processor gets equal or comparable amounts of computation [27]. In dynamic load balancing, the subtasks are dynamically assigned to the processors as and when they finish the previously assigned tasks. In NETRA when a task is assigned to a subtree, the DSPs involved perform the local load balancing functions.

Using the information from local load balancing and other measures of computation, global load balancing can be achieved hierarchically by using the DSP hierarchy. In this scheme, each controller DSP sends its measure of load to its parent DSP and the root DSP receives the load information for the entire system. The root DSP then broadcasts the measure of load of the entire system to the DPSs. When a task is to be allocated, these measures can be used to select a subtree for its execution as follows: If any subtree corresponding to the child of the current DSP has an adequate number of processors then the task is transferred to a child DSP with the lowest load, else if the current subtree has enough resources and the load is not significantly greater than the average system load then the task is allocated to the current subtree, else the current DSP transfers the task to the parent DSP.

Flexible Communication

Availability of flexible communication is critical to achieving high performance. For example, when a partition operates in SIMD mode there is a need to broadcast the programs. When a partition operates in MIMD mode, where processors in the partition cooperate in the execution of a task, one or more programs need to be transferred to the local memories of the processors. Performing the above justifies the need for selective broadcast capability. In order to take advantage of spatial parallelism in vision tasks processors working on neighboring data need to communicate fast amongst themselves for high performance. The programmability and flexibility of the crossbar provide fast local communication. Most common vision algorithms such as FFTs, filtering, convolution, counting, transforms, etc., need a broad range of processor connectivities for efficient execution. These connectivities include
arrays, pipelines, several systolic configurations, shuffle-exchanges, cubes, meshes, pyramids etc. Each of these connectivities may perform well for some tasks and badly for others. Therefore, using a crossbar with a selective broadcast capability, any of the above configurations can be achieved, and consequently, optimal performance can be achieved at the clusters.

Several techniques for implementing reconfigurability between a set of PEs were studied [29, 30]. It was discovered that using a crossbar switch to connect all PEs was simpler than any other schemes. The popular argument that crossbar switches are expensive was easily thwarted. When designing communication networks in VLSI, the primary constraint is the number of pins and not the chip area. The number of pins is governed by the number of ports on the network and is independent of the type of network. Furthermore, it was realized that a crossbar with a selective broadcast capability was not only very powerful and flexible structure, but was also simpler, scalable and less expensive.

The need for global communication is relatively low and infrequent. Global communication is needed for intertask communication, i.e., from one task to another in the IVS pipeline. It is also needed to input and output data, to transfer data within a subsystem when a task is executed on more than one cluster, and finally, it is needed to load the programs. The most important issue in global communication is that the network speed should be matched with the crossbar speed as well as with the processors speed. The global communication is performed through the global memory using the interconnection network, or using the DSP hierarchy. Another alternative we consider is connecting all the clusters and DSPs to a global bus. Since the DSPs perform most control functions and loading of programs and data, the responsibility of intertask communication does not lie with hierarchy. In a Section 5 we present an extensive analysis of the global communication networks in NETRA. Then using the analysis developed here we present performance of several algorithms in a companion paper.

4. Mapping Parallel Algorithms

There are two main considerations in mapping the parallel algorithms. First, mapping individual tasks or algorithms, and the second, integration of various tasks. Mapping individual tasks involves efficient division of the task(s) on the available processors, intratask communication, load balancing and, input and output of data. If the task is mapped onto more than one processor cluster then the mapping will require both intra-cluster as well as inter-cluster communication. Integration of algorithms involves intertask communication, data transfer between
tasks, formatting the data for the next task, and global load balancing.

The methodology we use for mapping parallel algorithms is multi-dimensional divide-and-conquer with medium to large grain parallelism. An individual task (in the following discussion task and algorithm are used interchangeably) can be efficiently mapped using spatial parallelism because most of the vision algorithms are performed on two dimensional data. However, integration of tasks involves exploiting both spatial as well as temporal parallelism. Temporal parallelism can be exploited by recognizing intertask data dependencies. In NETRA, by providing virtual partitioning of processors, reconfigurability, flexibility of communication and distributed control, it is possible with much ease to exploit temporal parallelism available in integrated vision systems. Furthermore, temporal parallelism can be improved by making data available to the next task in the pipeline as soon as it is produced by the previous task. This is achieved using the macro data flow approach between tasks.

4.1. Classification of Common Vision Algorithms

We can classify some of the common vision algorithms according to their communication requirements when mapped onto parallel processors. The classification provides an insight to the performance of an algorithm depending on its communication requirements.

(1) **Local Fixed** - In these algorithms, the output depends on a small neighborhood of input data in which the neighborhood size is normally fixed. Sobel edge detection, image scaling and, thresholding are examples of such algorithms.

(2) **Local Varying** - Like the local fixed algorithms, the output at each point depends on a small neighborhood of input data. However, the neighborhood size is an input parameter and is independent of the input image size. Convolutions, edge detection and most other filtering and smoothing operations are examples of such algorithms.

(3) **Global Fixed** - In such algorithms each output point depends on the entire input image. However, the computation is normally input data independent (i.e., computation does not vary with the type of image and only depends on the size of the image). Two Dimensional Discrete Fourier Transform and Histogram computation are examples of such algorithms.

(4) **Global Varying** - Unlike global fixed algorithms, in these algorithms the amount of computation and communication depends on the image input as well as its size. That is, the output may depend on the entire image or
may depend on a part of image. In other words, the computation is data dependent. Hough Transform and, Connected Component Labeling are examples of such algorithms. In an image, a connected component may span only a small region, or in the worst case the entire image may be one connected component (a spiral). Similarly, in case of the Hough transform for detecting lines, a line may span across image (meaning its votes must come from distant pixels or edges) or it may be localized.

4.2. Mapping an Algorithm on One Cluster

Mapping a task on one cluster means that intratask communication will only involve communication between processors of the same clusters. Figure 7 shows how a parallel algorithm is mapped on a cluster. Let us assume that there are $P$ processors in a cluster. As shown in figure 7, first program and data are loaded onto the processor cluster. Both in case of SIMD or MIMD mode, the program is broadcast onto the cluster processors. The data division depends on the particular algorithm. If algorithms are mapped in SIMD or systolic mode then the compute and communication cycles will be intermixed. If the algorithms are mapped in MIMD mode then each processor computes its partial results and then communicates with others to exchange or merge data.

Let us assume that an algorithm is mapped on one cluster with $P$ processors. The total processing time in such a mapping consists of the following components. Program load time onto the cluster processors ($t_{pl}$), data load and partitioning time ($t_{dl}$), computation time of the divided subtasks on the processors ($t_{cp}$) which is the sum of the maximum processing time on a processor $P_i$ and intra-cluster communication time ($t_{comm}$), and the result report time ($t_{rr}$). $t_{dl}$ consists of three components: 1) data read time from the global memory ($t_r$) by the cluster DSP, 2) crossbar switch setup time ($t_{sw}$) and, 3) the data broadcast and distribution time onto the cluster processors ($t_{br}$).

The total processing time $\tau(P)$ of the parallel algorithm is given by

$$\tau(P) = t_{pl} + t_{dl} + t_{cp} + t_{rr}$$

where,

$$t_{dl} = t_r + t_{setup} + t_{br}$$

and if the computation and communication do not overlap then,

$$t_{cp} = \max_{1 \leq i \leq P} (t_{pi}) + t_{comm}$$

else if computation and communication can completely overlap then,
In the above equations $t_r$ depends on the effective bandwidth of the global interconnection network.

4.3. Mapping an Algorithm on More than one Cluster

If an algorithm is mapped on more than one cluster then the communication consists of intra-cluster communication as well as inter-cluster communication. Since the cost of inter-cluster communication is more than that of intra-cluster communication, the inter-cluster communication should be minimized while mapping a parallel algorithm on more than one cluster. Figure 8 shows how a typical algorithm will be mapped onto two clusters.

Figure 5 shows how processor $P_i$ in cluster $C_i$ will communicate with processor $P_j$ in cluster $C_j$ using the global bus. The communication will be performed explicitly by messages. Processor $P_i$ will send the data and the identification of the receiving processor to its DSP ($DSP_i$). The DSP then will forward the message to the corresponding DSP in the other cluster ($DSP_j$). $DSP_j$ will send the data to $P_j$. A processor $P_i$ in cluster $C_i$ will communicate with a processor $P_j$ in cluster $C_j$ using the global memory as shown in figure 9. Processor $P_i$ will
write the data into a specified memory location in the global memory using its port connected to the multistage interconnection network. Processor $P_j$ will request for the data from the Memory Line Controller on its port connected to the interconnection network. The basic difference between the two approaches is the available bandwidth through the global interconnection. In case of the bus, the effective bandwidth will be much lower compared to the effective bandwidth of the multistage interconnection network because only one processor or DSP can access the bus at a time.

The performance of the algorithm mapped on more than one cluster depends on how much inter-cluster communication is required and by how many processors, which in turn depends on the type of algorithm. Figure 9 illustrates various ways in which an algorithm can be mapped on two or more clusters. However, in the figure we only
show two clusters. Case a) represents the best case in which a parallel algorithm can be mapped such that only one or no processors need to communicate with any processor in the other cluster. This is obtained by partitioning the data in such a way that only one processor in each cluster gets the boundary data and the algorithm is such that communication is only exchanging boundary values. Example of such algorithms include local fixed and local varying algorithms.

In an average case, some of the processors in one cluster are required to communicate with processors in the other cluster. Case b) in Figure 9 illustrates such a case. The figure shows that data processed by a few processors is needed by corresponding processors in the other cluster. However, the figure does not show how the transfer of the data will take place. That depends on the chosen global interconnection network and how the algorithm is mapped. Global varying algorithms may need this type of communication. For example, the connected component labeling algorithm can be mapped in such a way that only those processors need to communicate across clusters which have boundary components.

![Figure 9: Types of Intercluster Communication](image-url)
The third case (c) represents the worst case. The worst case means that data produced by each processor is required by at least one processor in another cluster. Global fixed and some global varying algorithms need this type of communication.

Now, let us discuss how inter-cluster communication is incorporated in the performance of an algorithm. Let us assume that an algorithm is mapped on \( C \) clusters. The total computation time for an algorithm (EQ. 5) is now given by

\[
t_{cp} = \max_{i \leq j \leq C} (\max_{0 \leq s \leq P} (t_{pi})) + t_{comm}
\]

(7)

now, \( t_{comm} \) is given by

\[
t_{comm} = t_{cl} + t_{icl}
\]

(8)

where, \( t_{cl} \) represents the intra-cluster communication time and, \( t_{icl} \) denotes the inter-cluster communication time. \( t_{icl} \) not only depends on the type of algorithm, how it is mapped, how many clusters it is mapped on but also depends on the effective bandwidth of the global interconnection. The effective bandwidth depends on the communication requirements of the other tasks in the system which may be executing on other clusters. Let us assume that \( t_{icl} \) denotes the communication time when there is no interference in the interconnection network, that is, \( t_{cl} \) denotes the data write and read time given that the network is available whenever inter-cluster communication is needed. Then the actual inter-cluster communication will be degraded by a factor \( w \) which depends on the traffic intensity in the network and the interference by communication of other tasks in the system. Therefore, instead of \( t_{icl} \), the inter-cluster communication time will be \( w \times t_{icl} \).

5. Inter-cluster Communication in NETRA

Communication between processors within the same cluster is performed using the crossbar connections. Communication between processors in different clusters can be performed in various ways. First, the global memory is used for this purpose as follows. The processor(s) needing to send data to another processor in a different cluster writes the data into designated locations in the memory. This involves setting the appropriate circuit through the global multistage interconnection network to the memory module followed by a data transfer. The data is transferred in block mode. The Memory Line Controller (MLC) updates the information about the destination port(s), the length of the data block, block's starting address and sets a flag indicating the availability of the data. Now, the destination processor can read the data using this information. Note that this method permits out of order requests to be ser-
viced. For example, if the destination processor tries to read the data before it has been written, MLC informs the processor of this situation and when the data is really written into the global memory then the MLC informs the destination processor. This is a block level data-flow approach. The main advantages of this approach are that asynchronous communication is possible, out of order messages can be handled and efficient pipelining of data can be achieved.

The second alternative to perform inter-cluster communication is to use the DSP tree links. However, for distant inter-cluster communications, the tree may not perform well because of the root bottlenecks typical to any tree structure. The main function of the tree structure is to provide control hierarchy for the clusters. Its links are mainly used for program and data broadcast to subtrees, and DSPs use the tree links to send (receive) control information to (from) other DSPs.

The third alternative strategy to perform inter-cluster communication is to use a high speed global bus that connects all DSPs and one port from each cluster. The global memory is also connected to the bus and is accessible to all the clusters via the bus. The communication is done explicitly by messages and synchronously. Figures 10 and 5 show the first and third communication methods. The figures show how a processor $P_i$ of cluster $C_i$ will communicate with processor $P_j$ of cluster $C_j$ using the two strategies.

Inter-cluster communication is needed in the following cases: i) An algorithm is mapped in parallel on more than one cluster and the processors need to communicate to exchange partial results or combine their results, ii) in

![Figure 10: Inter-Cluster Communication Using Global Memory](image-url)
an integrated vision system, output data of a task produced at one or more clusters needs to be transferred to the next
task executing on different clusters and, iii) to perform input and output of data and results.

The extent of inter-cluster communication depends on the type of algorithms, how they are mapped in parallel, frequency of communication and amount of data to be communicated.

5.1. Analysis of Inter-Cluster Communication

There are several parameters that affect the inter-cluster communication time. The architecture dependent parameters are: number of processors (i.e., number of clusters and number of processors in each cluster), number of memory modules, number of processors per port connected to the global interconnection, and the type of interconnection network. Some parameters depend both on the architecture as well as on the type of algorithms, how they are mapped, their communication requirements when mapped onto multiple clusters etc. Furthermore, not only does the communication time depend on the underlying algorithms but also on the network traffic generated by other processors in the system because there may be conflicts in accessing the network as well as memory modules.

We consider an equivalent model of the architecture as shown in figure 11. The model shows \( N \) processors connected to \( M \) memory modules through a global interconnection network. \( N \) is given by \( C \times P_t + N_{dsp} \), where \( C \) is the number of clusters, \( P_t \) is the number of ports in each cluster and \( N_{dsp} \) is the number of DSPs in the system. For simplicity, we assume that each cluster contains equal number of processors. The number of physical processors will be given by \( C \times P_t \times P_p \), where \( P_p \) is the number of processors per port.

![Figure 11: Equivalent Model for Global Communication](image)
The following analysis is based on the analysis presented by Patel in [31, 32]. He developed an analytical model for evaluating alternative processor memory interconnection performance and showed that the analysis is reasonably accurate. Consider execution of a typical parallel algorithm on multiple clusters. The execution will consist of processing, intra-cluster communication and inter-cluster communication. Figure 12 shows the computation and communication phases of an algorithm. The computation time is given by $t_{cp}$, the intra-cluster communication time is given by $t_{icl}$, and the inter-cluster communication time is given by $t_{icl}$ in terms of equivalent processor cycles. However, due to conflicts in the network or in memory modules, a processor may have to wait for $w_a$ cycles before being able to access the network and write to (or read from) the memory. In effect, this can be seen as the communication time being elongated by a factor $w$ for each request, and instead of it being $t_{icl}$, it is now $w \times t_{icl}$ as shown in figure 12. Therefore, if the probability of accessing the global network in each processing cycle is $m$ and for each access the communication time is $t_{icl}$, then the useful computation for $t$ processor cycles takes $t + m \times t \times w \times t_{icl}$, where $t = t_{cp} + t_{cl}$. The fraction of useful work (utilization $U$) is given by

$$U = \frac{t}{t + m \times t \times w \times t_{icl}}.$$  

(9)

The average number of busy memory modules (or fraction of time when the bus is busy when the global interconnection is a bus) is

$$B = \frac{N \times m \times t_{icl} \times t}{t + m \times t_{icl} \times t \times w}$$  

(10)

and in terms of utilization,

\[ \text{No Interference} \]

\[ t_{cp} + t_{cl} \quad t_{icl} \quad t_{cp} + t_{cl} \quad t_{icl} \]

\[ \text{With Interference} \]

\[ t_{cp} + t_{cl} \quad w \times t_{icl} \]

Figure 12: Computation and Communication Activities of a Processor
In [31] it is shown that the utilization primarily depends on the product \( m \times t_{icl} \) rather than \( m \) and \( t_{icl} \) individually. In other words, the processor utilization primarily depends on the traffic intensity and to a lesser extent on the nature of the traffic.

For a particular algorithm, all the parameters are known except \( w \). The probability of accessing the global network is essentially given by the number of times communication is needed per processor cycle and is known when an algorithm is mapped in parallel. The factor \( w \) depends on the algorithm parameters as well as the interference from other processors accessing the global network and the memory, number of processors, number of memory modules, the type of interconnection network and the access rate \( m \).

Consider the processor activities again. A processor needing to access the global memory or the bus submits requests again and again until accepted; on an average this happens for \((w-1)\times t_{icl}\) time units. After the request is granted, the processor has a path to memory for \( t_{icl} \) time units. In other words, the network sees an average of \( w \times t_{icl} \) consecutive requests for unit service time. Therefore, the request rate (for unit service) from a processor as seen by the network is

\[
m' = \frac{m \times w \times t_{icl}}{1 + m \times w \times t_{icl}}.
\]

and in terms of utilization

\[
m' = 1 - U.
\]

For details, the reader is referred to [31].

The model that we analyze is a system of \( N \) sources and \( M \) destinations. Each source generates a request with probability \( m' \) in each unit time. The request is independent, random, and uniformly distributed over all destinations. Each request is for one unit service time. The following is an analysis for a bus and for multistage delta network.

Bus: We know from earlier discussion that

\[
B = N \times m \times t_{icl} \times U
\]

and also, assuming all sources have the same request rate, average amount of time the bus is busy is given by

\[
B = [1 - (1 - m')^N].
\]
The equations 12 and 13 result in a non-linear equation

\[ N \times m \times t_{icl} \times U - \left[ 1 - \left( 1 - m' \right)^N \right] = 0. \]  

(15)

In the above equation, value of \( m' \) can be substituted in terms of \( w \), and hence, value of \( w \) can be computed. If the request rate from sources is not uniform, i.e., if the request rate from source \( N_i \) is \( m_i \) then the above equation becomes

\[ \sum_{j=1}^{N} (m_i \times t_{icl}(j) \times U_j) - \left[ 1 - \prod_{j=1}^{N} (1 - m'_j) \right] = 0. \]  

(16)

When evaluating performance of a parallel algorithm mapped across clusters there will be two request rates, one for the processors taking part in running the algorithm and the other for rest of the processors in the system which will be an input parameter.

**Multistage-Interconnection (Delta)**: A delta network is an \( n \) stage network constructed from \( a \times b \) crossbar switches with a resulting size of \( a^n \times b^n \). Therefore, \( N = a^n \) and \( M = b^n \). For a complete description refer to [32]. Functionally, a delta network is an interconnection network which allows any of \( N \) sources (processors) to communicate with any one of the \( M \) destinations (memory modules). However, two requests may collide in the network even if the requests are made to different memory modules. We use results from [32, 31] to obtain average number of busy main memory modules \( B \), which is given by

\[ B = M \times m_n \]  

(17)

and the following equation in satisfied.

\[ N \times m \times t_{icl} \times U - M \times m_n = 0 \]  

(18)

where,

\[ m_{i+1} = 1 - \left( 1 - \frac{m_i}{b} \right)^a, \quad 0 \leq i < n \]

\[ m_0 = 1 - U. \]

For details, the reader is referred to [31, 32].

These equations are solved numerically to obtain the interference delay factor \( w \) which is used in the performance evaluation of algorithms mapped across multiple clusters.
5.2. Approach to Performance Evaluation of Algorithms

Performance of an algorithm mapped on multiple clusters is governed by various factors. Table 1 summarizes the parameters affecting the performance of a parallel algorithm. The approach to evaluating the performance of an algorithm is as follows. Using the parameters and a particular mapping, computation ($t_{cp}$), intra-cluster communication ($t_{cl}$) and inter-cluster communication time ($t_{icl}$) are determined. The traffic intensity for a processor(s) (or a cluster depending on how an algorithm is mapped) is given by $\frac{t_{icl}}{t_{cp}+t_{cl}}$. Using the traffic intensity values, and using a range of traffic intensity values for interference, the effective bandwidth of the network is determined, that is, the factor $w$ is computed. In a companion paper, we will present performance evaluation of several algorithms using the above method.

Consider a parallel execution of an algorithm across clusters. If the execution time when the algorithm is executed on a single processor is $t_{seq}$ then the speed up in the best case is given by

$$Sp = \frac{t_{seq}}{t_{cp} + t_{cl} + t_{icl}}$$

(19)

That is, assuming there is no interference while accessing the network or the global memory. Under the conditions in which there are conflicts while accessing the network, the inter-cluster communication time will be given by $w \cdot t_{icl}$, and therefore, the speed up will be given by

$$Sp' = \frac{t_{seq}}{t_{cp} + t_{cl} + w \cdot t_{icl}}$$

(20)

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P$</td>
<td>No. of proc. executing an algorithm</td>
</tr>
<tr>
<td>$C$</td>
<td>Cluster size</td>
</tr>
<tr>
<td>$N$</td>
<td>Total no. of proc. in the system</td>
</tr>
<tr>
<td>$D$</td>
<td>Data size</td>
</tr>
<tr>
<td>$P_t$</td>
<td>No. of proc./port</td>
</tr>
<tr>
<td>$M$</td>
<td>No. of memory modules</td>
</tr>
<tr>
<td>GICN</td>
<td>Type of global interconnection</td>
</tr>
<tr>
<td>$m \times t$</td>
<td>Traffic intensity for interference in network and memory accesS by $(N-P)$ processors</td>
</tr>
<tr>
<td>$m_1 \times t_1$</td>
<td>Traffic intensity for network and memory access by partition executing the algorithm</td>
</tr>
</tbody>
</table>
Hence, degradation in speed up with respect to the best case speed up will be

\[
\frac{Sp - Sp'}{Sp} = \frac{(w-1) \times t_{icl}}{t_{cp} + t_{cl} + w \times t_{icl}}.
\]  

(21)

6. Summary

In this paper we presented a model of computation for IVSs. Using the model desired features and capabilities of a parallel architecture for IVSs were derived. Then a multiprocessor architecture suitable for IVS (called NETRA) was presented. The topology of NETRA is recursively defined and, hence is easily scalable from small to large systems. Homogeneity of NETRA permits fault tolerance and graceful degradation under faults. NETRA is a recursively defined tree-type hierarchical architecture whose leaf nodes consist of cluster of processors connected with a programmable crossbar with selective broadcast capability to provide for desired flexibility. We presented a qualitative evaluation is NETRA. Then general schemes were described to map parallel algorithms onto NETRA. Finally, an analysis to evaluate alternative inter-cluster communication strategies in NETRA was presented with a methodology to evaluate performance of parallel algorithms mapped across multiple clusters.

In a companion paper (part II of this paper) we present performance evaluation of several common vision algorithms on NETRA. The paper discusses performance of algorithms on one cluster, their analysis and implementation. Furthermore, the paper includes performance evaluation of alternative communication strategies as well as presents mapping of algorithms across multiple clusters. The effect of interference in the global interconnection network and global memory on the performance of algorithms is also studied.
REFERENCES


