Effect of Contrast on the Perception of Direction of a Moving Pattern

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Ames Research Center, Moffett Field, California

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SUMMARY

We performed a series of experiments examining the effect of contrast on the perception of moving plaids to test the hypothesis that the human visual system determines the direction of a moving plaid in a two-staged process: decomposition into component motion followed by application of the intersection of constraints rule. Although there is recent evidence that the first tenet of the hypothesis is correct, i.e., that plaid motion is initially decomposed into the motion of the individual grating components, the nature of the second-stage combination rule has not yet been established. We found that when the gratings within the plaid are of different contrast the perceived direction is not predicted by the intersection-of-constraints rule. There is a strong (up to 20°) bias in the direction of the higher-contrast grating. A revised model, which incorporates a contrast-dependent weighting of perceived grating speed as has been observed for one-dimensional patterns, can quantitatively predict most of our results. We then discuss our results in the context of various models of human visual motion processing and of physiological responses of neurons in the primate visual system.

INTRODUCTION

Deducing the direction of motion of a pattern as a whole from the motion of oriented components within that pattern is a challenge for all models of human visual motion processing. Adelson and Movshon (1982) studied the problem using moving plaids, the sum of two drifting gratings of different orientations. They proposed that the human visual system determines the direction of a moving pattern using a two-step procedure: first, the velocities of oriented components within the pattern are estimated, then at a later stage they are recombined to calculate the motion of the pattern as a whole.

Their hypothesis was formulated to explain the psychophysical finding that, in order for the two components to cohere (to move together as a plaid), the gratings must be similar in spatial frequency. They concluded from this finding that the human visual system analyzes plaid motion by first decomposing it into the motion of the grating components (fig. 1(a)). They suggested that this decomposition is the natural consequence of having orientation and spatial-frequency tuned sensors at the front end of the system (for a review, see DeValois and DeValois, 1980). They also proposed that, at the second stage (fig. 1(b)), the component velocities are recombined using the intersection of perpendicular constraints (Fennema and Thompson, 1979) to yield a measure of the motion of the plaid as a whole.

When plaid motion is plotted in velocity space (fig. 1(b)), the motion of each grating component within the plaid is ambiguous: consistent with a family of velocities lying along a constraint line (thick lines). Adelson and Movshon proposed that plaid velocity is recovered as the unique vector defined by the intersection of both constraint lines. The plaid-velocity vector is thus consistent with the rigid motion of both of the individual gratings and is therefore a measure of the motion of the coherent plaid. The lack of coherence for gratings of widely differing spatial frequencies was explained by assuming that the second stage only combines information from sensors with similar spatial-frequency tuning.

They found support for their hypothesis in the discovery of two types of motion-sensitive neurons in the monkey visual cortex: one sensitive to component motion and one, at a higher level within the
Figure 1.— The Adelson-Movshon model. (a) Basic two-stage framework where plaid motion is decomposed into the motion of the grating components, then reconstructed at a second stage. (b) The intersection of constraints rule is demonstrated by showing the motion of a plaid in velocity space. The direction of plaid motion ($\alpha$), a function of the speed of the grating components ($V_1$ and $V_2$) and of the plaid angle ($\theta$), is given by equation (4).
cortex, sensitive to the motion of the plaid as a whole (Movshon et al., 1986). Furthermore, a recent
study has found that speed discrimination for moving-plaid stimuli is consistent with the two-staged
approach that Adelson and Movshon proposed (Welch, 1989). However, the second-stage recombination
rule proposed by Adelson and Movshon has recently been challenged (Ferrera and Wilson, 1988, 1989).

In this study, we extend the investigation of how the brain determines the direction of motion. In
particular, we examine the effect of contrast on the perceived direction of a moving plaid. It has been
shown that the perceived speed of a single grating is a function of contrast (Thompson, 1982). At tempo-
rnal frequencies below 8 Hz, a low-contrast grating appears to move more slowly than a standard higher-
contrast grating moving at the same physical speed. If this contrast-dependent distortion in the perceived
speed of the components is passed on to the second stage of the model in figure 1, then a significant
contrast-dependent distortion in the perceived direction of motion of the plaid as a whole should result.
We confirmed this prediction: making the contrast of the individual components within the plaid
unequal results in errors in judgment of direction. The perceived direction of motion can differ by
up to 20° from that predicted by the model in figure 1.

We therefore propose a revised model that incorporates Thompson’s finding as a contrast-dependent
distortion of component speed. Because the proposed contrast dependence in the revised model is a
function of the component contrast in threshold units, we first measured the detection threshold of
moving gratings in the presence of a moving grating mask of different orientation, with the geometric
arrangement the same as that of the plaid stimuli. Simulations of the revised model show that, in most
cases, if the contrast-distorted estimate of grating speed, rather than the true grating speed, is the input to
the second stage of processing, then the observed errors in perceived direction can be quantitatively
predicted. Preliminary results have been presented elsewhere (Stone, Mulligan, and Watson, 1988a,b).

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physiological data.

GENERAL METHODS

The stimulus used in this study was a vignetted plaid, the sum of two sinusoidal gratings of different
orientations viewed through a two-dimensional (2-D) Gaussian window. Figure 2 shows an example of
such a stimulus. We generated moving plaids on a Mitsubishi 19-in. high-resolution monochrome
monitor (model M-6950) using an Adage RDS 3000 image display system. The luminance output of
the monitor was calibrated and corrected for its gamma nonlinearity using a lookup table procedure
described elsewhere (Watson et al., 1986). A detailed account of the animation procedure that was used
to generate moving plaids can be found in Mulligan and Stone (1989).

Briefly, the plaid stimulus was a 512 pixel by 512 pixel 8-bit/pixel image created using both locally
developed programs and the HIPS image-processing software package (Landy, Cohen, and Sperling,
1984). First, four 2-D sinusoidal gratings were generated (sine- and cosine-phase components of gratings
with two different orientations symmetric with respect to the vertical axis). These four images were then
Figure 2.— The standard plaid stimulus. The two gratings were 1.5 c/d, oriented 60° symmetrically from vertical, and viewed through a Gaussian window. The halftoning for this figure was not that used for the actual stimulus. For a detailed discussion of the halftoning used to display our stimuli see Mulligan and Stone (1989).

multiplied by a 2-D Gaussian (x and y standard deviations of 90.5 pixels). This procedure eliminated the sharp edges at the boundaries of the stimulus. The images were then halftoned using a modified error-diffusion method (Floyd and Steinberg, 1975; Mulligan, 1986). The resulting four bit-mapped images were then loaded into the four lower-order bit-planes. A 3 pixel by 3 pixel white fixation cross was drawn into a fifth bit-plane in the center of the image. The remaining three bit-planes were blank. The image could be loaded into the framebuffer within a few seconds. Then, by varying the color lookup table on a frame-by-frame basis (at 60 Hz), we modulated the contrast of the sine- and cosine-phase components of each grating in temporal quadrature so that they appeared as a single drifting grating. In this way, we had complete control over the speed and contrast of both gratings within the plaid without having to load new images into the framebuffer. Furthermore, the initial spatial phases of the gratings within the plaid were randomized so that position cues could not be used to assess motion.
There were small, but measurable, departures from linearity of spatial summation in our display monitor, which conflict with one of the basic assumptions underlying halftoning techniques. However, using a technique described elsewhere (Mulligan and Stone, 1989), for a stimulus of 40% total contrast, we estimated the contrast of the largest artifact to be less than 0.2% and, in particular, those artifacts harmonically related to the stimulus were even smaller.

The standard plaid stimulus consisted of two 1.5 cycle/degree (c/d) gratings whose normal vectors were oriented symmetrically ±60° from the vertical axis (fig. 2). We defined the plaid angle as the angle between the normal vector defining each grating and the bisecting axis or half the angle between the normal vectors (θ in fig. 1(b)). It was therefore 60° for the standard plaid. This arbitrary definition was chosen because it simplifies the equations presented below. The grating contrasts were 10% each. For a pair of sinusoidal gratings, the total contrast is simply the sum of the grating contrasts or 20%. The speed of the coherent plaid was held constant at 2°/sec. In some experiments, the spatial frequency was 0.75 or 3.0 c/d, the plaid angle was 45° or 30°, the total contrast was 5, 10, or 40%, and the plaid speed was increased to 6.0°/sec.

Subjects viewed the screen binocularly through natural pupils from a distance of 273 cm. This distance made the image subtend 5.4° by 5.4° (20 pixels/cm) and made the high-frequency halftoning noise invisible except at the highest contrast level (40% total contrast). The mean luminance of the image was 100 cd/m². The stimulus presentation lasted 300 msec. The contrast rose with a Gaussian time course (standard deviation of 0.71 frames), reached full contrast after 50 msec (3 frames), stayed at full contrast for 200 msec, then fell with the same Gaussian time course during the final 50 msec. We used four male observers (three of whom were unaware of the purpose of the experiment) between 16 and 30 years old.

**Experiment 1: Detection Threshold for Moving Plaid Components**

Before performing the main experiment of this study, we measured the detection threshold of our subjects for each of the components within the plaid. This was to ensure that both gratings within the plaid were above threshold in experiment 2 and to convert absolute contrast into threshold units which were needed for the simulations.

**Methods**—We determined the threshold for detecting the presence of a moving sinusoidal grating (signal) in the presence of a second moving grating (mask) of higher contrast and different orientation using an unconventional procedure: we held total contrast (mask plus signal) constant (at 5, 10, 20, or 40%) to allow easy comparison with the data from experiment 2. The signal and mask were both 1.5 c/d sinusoidal gratings oriented either +60° or -60° from the vertical axis and moving at 1°/sec. The choice of which of the two gratings was signal and which was mask was made randomly before each trial. Threshold was determined using a two-interval, forced-choice protocol. The signal contrast level was chosen from a finite set which varied from 2.5% to 0.025% in fifteenth of a log unit steps. A trial consisted of two stimulus intervals (300 msec each separated by a 500-msec blank interval) presented in random order: one in which both signal and mask were present at a fixed total contrast and another in which only the mask was present. Thus, although the mask varied from trial to trial, it was identical in both intervals within a single trial. The signal contrast on a given trial was determined by one of two
independent, randomly interleaved staircases. Within each staircase, contrast was reduced after two correct responses and increased after a single incorrect response.

Subjects were instructed to watch the screen and to fixate the small cross which appeared for 500 msec immediately before the onset of each stimulus, and was extinguished while the moving stimulus was displayed. They were then asked to indicate whether the signal was in the first or second interval. The resulting proportion correct (P) versus signal contrast (x) was fit with the best-fitting Weibull function (Watson, 1979; Weibull, 1951)

\[ P = \min\left(0.99, 1 - 0.5 e^{-(x/T)^{3.5}}\right) \]

where \( T \) is detection threshold. Thus, threshold was defined as the signal contrast at which the observer distinguished correctly 82% of the time between a weak "signal" grating moving within a moving plaid (i.e., in the presence of a "mask" grating) and the moving mask grating alone.

Results—Figure 3 plots \( \log_{10} \) threshold contrast (T) as a function of \( \log_{10} \) mask contrast (M). The data for all four subjects have a flat region below some critical mask contrast followed by a linear rising slope. This result is similar to the detection threshold results of Legge and Foley (1980) for pairs of stationary gratings of different spatial frequency. To quantify the results, we did a simple piecewise linear fit. For the flat portion, we made the assumption that the mean threshold at 5% total contrast (leftmost data points in fig. 3), was the mean unmasked threshold (c). To measure the linear rising phase, we fit the three clusters of points generated for total contrasts of 10% and higher using linear regression to determine the slope (a) and intercept (b). Although it is arbitrary to include the points generated at 10%
total contrast, any resulting error is probably small. The mean curve, the solid line in figure 3, is given by the following equation:

\[ T = \max \left(10^{(a \log M - b)}, c\right) \]  \hspace{1cm} (2)

with \( a = 0.548 \), \( b = 1.526 \), and \( c = 0.0078 \). Equation (2) is merely a power law with an exponent of 0.548 for mask contrasts above 8.6%. The exponent found here is similar to that for stationary grating masks of different spatial frequency (range: 0.50 to 0.79 in Legge and Foley, 1980) and of different orientation (range: 0.40 to 0.72 in Phillips and Wilson, 1984). (We will use eq. (2) to estimate threshold for the simulations in fig. 11.)

For two subjects, we measured the effect of temporal and spatial frequency on detection threshold (fig. 4). Temporal frequency (speed) had little effect on threshold (fig. 4(a)). However, threshold was very sensitive to changes in spatial frequency (fig. 4(b)): it increased at lower spatial frequency (0.75 c/d) and decreased at higher spatial frequency (3.0 c/d). This is consistent with previous studies of human spatio-temporal contrast sensitivity (Robson, 1966; Koenderink and van Doorn, 1979). (The thresholds for these two observers at these temporal and spatial frequencies, given by eq. (2) with \( a, b, \) and \( c \) as shown in table 1, were used for the simulations in figs. 12 and 13.)

**Experiment 2: Effect of Contrast on the Perceived Direction of Plaid Motion**

These experiments were conducted to measure systematically the effect of the relative contrast of the two gratings within the moving plaid on the perceived direction of motion. They were designed to test the model shown in figure 1 which predicts that changes in contrast will have no systematic effect on the perceived direction of plaid motion.

**Methods**—Subjects were presented with a single stimulus interval and were asked whether the stimulus moved to the left or right of subjective vertical. The true direction of plaid motion was varied by making the appropriate change in the ratio of the speeds of the two gratings (speed ratio) while the speed of the coherent plaid was held constant at 2°/sec. The direction was changed within two interleaved up-down staircases to determine the direction for which subjects chose left or right with equal probability. We call this point *perceived vertical* and, for simplicity, we express it in degrees with respect to true vertical.

While total contrast was held constant at 5, 10, 20, or 40%, the ratio of the contrasts of the two gratings (contrast ratio) was varied in steps of \( \sqrt{2} \). For example, the possible contrast pairs with 40% total contrast are: 20%, 20%; 23.4%, 16.6%; 26.7%, 13.3%; 29.6%, 10.4%, etc., and the symmetric counterparts. The series of stimuli included all possible contrast ratios which were powers of \( \sqrt{2} \) and for which both gratings were above detection threshold. Because these series contained so many conditions, they were split into two interleaved subseries: one with contrast ratios which were even powers of \( \sqrt{2} \) and another with odd powers of \( \sqrt{2} \). The two subseries were presented in separate sessions.

For example, if the contrast of one of the gratings is so low that its perceived speed is half that of its true speed and if perceived rather than true speed feeds into the second stage of the model in figure 1, then the intersection of constraints rule will yield a severe directional bias toward the direction.
Figure 4.– Detection threshold versus mask contrast. These plots contain the thresholds of two subjects at four different total contrasts at two different temporal frequencies (a) and three different spatial frequencies (b). The solid curves are given by equation (2) using the parameters shown in table 1.

### TABLE 1.– THRESHOLD PARAMETERS DEPEND ON TEMPORAL AND SPATIAL FREQUENCY

<table>
<thead>
<tr>
<th>Spatial frequency</th>
<th>Temporal frequency</th>
<th>a slope</th>
<th>b intercept</th>
<th>c unmasked threshold</th>
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<tr>
<td>0.75</td>
<td>1.5</td>
<td>0.536</td>
<td>1.148</td>
<td>0.0148</td>
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<td>1.5</td>
<td>0.554</td>
<td>1.532</td>
<td>0.0080</td>
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<tr>
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<td>1.5</td>
<td>0.448</td>
<td>1.781</td>
<td>0.0054</td>
</tr>
<tr>
<td>1.5</td>
<td>4.5</td>
<td>0.553</td>
<td>1.497</td>
<td>0.0078</td>
</tr>
</tbody>
</table>
of motion of the grating of higher contrast (fig. 5(a)). To quantify this bias, the true direction of plaid motion is altered by varying the speed ratio of the components. When the speed ratio reaches 2 to 1, the plaid will appear to move straight up (fig. 5(b)). Perceived vertical measured this way (bias in fig. 5(b)) is equal and opposite to the bias seen when the plaid is actually moving straight up (bias in fig. 5(a)) assuming the contrast-dependent distortion is a multiplicative speed distortion, which is independent of temporal frequency.

Figure 5.— Measuring the directional bias of a plaid moving straight up but composed of unequal contrast gratings. (a) If Thompson (1982) is correct, the lower-contrast grating (grey) will appear to move more slowly and the intersection-of-constraints rule applied to the perceived grating speeds will predict a bias toward the direction of motion of the higher-contrast grating (black). (b) If the speed ratio is changed until the plaid is perceived to move straight up, then the true direction of plaid motion will have an equal and opposite bias to that in (a).

Our staircase method yielded typical psychometric curves (fig. 6). We fit the data for each condition with a cumulative Gaussian using a weighted least-squares procedure (Mulligan and MacLeod, 1988) based on probit analysis (Finney, 1971). The standard deviation of the best-fitting cumulative Gaussian was defined as the precision in the observer’s direction judgments. The location of the inflection point represents a bias which we refer to as the perceived vertical (the direction of motion that is perceived as pure vertical).
Figure 6.— Raw psychometric curves for plaid direction discrimination. This figure plots the percentage of stimulus presentations that were perceived as leftward versus the true direction of motion of the stimulus, for a single subject, for three runs at the three different contrast ratios indicated above the curves. Positive angles indicate leftward motion.

Results— For the standard plaid with a contrast ratio of 1, table 2 shows the mean precision of four subjects averaged over three runs and the standard deviation. Observers were apparently able to determine the direction of plaid motion to around ±4°. Although there seems to be some idiosyncratic variability, on average, there is no bias in the mean perceived vertical which indicates that there was little or no systematic bias.

<table>
<thead>
<tr>
<th>Subject</th>
<th>Perceived vertical, deg</th>
<th>Precision, deg</th>
</tr>
</thead>
<tbody>
<tr>
<td>L.S.</td>
<td>-0.7 ±1.3</td>
<td>4.0 ±1.0</td>
</tr>
<tr>
<td>L.L.</td>
<td>0.5 ±0.4</td>
<td>3.4 ±0.4</td>
</tr>
<tr>
<td>E.P.</td>
<td>-3.4 ±3.7</td>
<td>5.5 ±1.6</td>
</tr>
<tr>
<td>C.F.</td>
<td>4.0 ±2.6</td>
<td>2.7 ±0.7</td>
</tr>
<tr>
<td>Mean</td>
<td>0.1</td>
<td>4.0</td>
</tr>
</tbody>
</table>

Figure 6 shows raw data for naive observer C.F. The psychometric curves shift along the x-axis for different contrast ratios: perceived vertical goes from 14.9° rightward for a contrast ratio of 0.125, to 1.1° rightward at equal contrast, and finally to 10.3° leftward for a contrast ratio of 8. However, the precision for the three conditions remained nearly unchanged at 3.4°, 3.4°, and 2.5°, respectively. This illustrates, at the raw-data level, that there are systematic changes in perceived vertical that occur as a function of contrast ratio and which cannot be explained by changes in precision.
A complete analysis of the performance of all four subjects shows that varying the contrast ratio away from 1 produced large distortions in the perceived direction of motion. Figure 7 plots perceived vertical in degrees away from true vertical as a function of \( \log_2 \) contrast ratio at total contrasts of 5, 10, 20, and 40% for all four subjects. (Typical standard deviations are plotted for 40% contrast.) When the gratings were of unequal contrast, the perceived direction of motion was shifted toward that of the higher-contrast grating. The effect increased systematically with increased contrast ratio, although it varied for different total contrasts. All four subjects showed the same qualitative behavior.

Figure 7. Perceived vertical versus contrast ratio. (a)-(d) This figure plots perceived vertical for all four subjects at four different total contrasts (5, 10, 20, and 40%). Error bars indicate standard deviations. Positive values indicate biases to the left of actual vertical.

The precision of the direction judgments was insensitive to changes in contrast except at extreme contrast ratios. Figure 8 plots precision as a function of \( \log_2 \) contrast ratio at four different total contrasts for all four subjects. Although subjects varied in their overall sensitivity to the direction of motion, there were no systematic effects of contrast ratio on precision.
A Revised Model

The Adelson-Movshon model, as shown in figure 1, fails to explain the results of experiment 2, because it tacitly implies that the speeds of the components are accurately determined regardless of contrast. In this section, we amend the model to incorporate the finding of Thompson (1982) that the perceived speed of moving gratings is a function of contrast. The revised model is then tested with a variety of moving plaid stimuli.

Theory—Figure 9 shows the revised model. The modification is that the second stage is passed a contrast-distorted version of grating speed (for convenience, hereafter called perceived speed) rather than actual grating speed. We construct perceived speed by multiplying actual speed by \( f \), the contrast-dependent weighting function. For each grating, \( f \) is a function of the grating’s contrast in threshold
A revised model. A contrast-dependent nonlinearity is added to each channel in the Adelson-Movshon model. The nonlinearity is a function of the contrast in threshold units of the input grating for the particular channel. Because threshold will be altered in the presence of the other grating (masking), the nonlinearity actually becomes a function of the contrast of both gratings.

units \((C_T)\), determined by dividing absolute contrast by threshold calculated using equation (2) with the other grating acting as the mask. Figure 10 shows the contrast-dependent weighting function that we used for the simulations that follow. We chose a Weibull function (Weibull, 1951) which goes to zero at threshold and which rises rapidly to just about 1 for contrasts exceeding 10 threshold units. The explicit formula was:

\[
f = 1 - e^{-\left(\frac{C_T - 1}{k_1}\right)^{k_2}} \quad \text{for } C_T \geq 1
\]

\[
= 0 \quad \text{for } C_T < 1
\]

with \(k_1 = 1.99\) and \(k_2 = 0.76\) (by a least-squares fit of the data in fig. 11).
Figure 10.—The contrast-dependent weighting function. This rapidly saturating function given by equation (3) was derived by choosing $k_1$ and $k_2$ such that the mean squared error between the simulated and actual data was minimized.

Once $f$ is determined for each grating, human performance can be simulated. The simple intersection-of-constraints rule illustrated in figure 1(b) predicts that the perceived direction of motion ($\alpha$) is given by the following equation (Stone, 1988):

$$\alpha = \arctan \left[ \cotan \theta \left( \frac{V_1 - V_2}{V_1 + V_2} \right) \right]$$

(4)

where $V_1$ and $V_2$ are the speeds of the two grating components and $\theta$ is the plaid angle. Note that, when $V_1 = V_2 = V$, $\alpha$ is zero and the plaid is perceived to move straight up. If, however, perceived rather than true speed is the input to the intersection-of-constraints stage and the perceived speed of the $i$th grating is $f_i V$, then the perceived direction of motion when the plaid is actually moving straight up is

$$\alpha = \arctan \left[ \cotan \theta \left( \frac{f_1 - f_2}{f_1 + f_2} \right) \right]$$

(5)

Equation (5) allows us to simulate human perception of the direction of motion and to compare the result with the data in figure 7.

Results—Figure 11(a) plots the average bias of the four observers as a function of log$_2$ contrast ratio for four different total contrasts by condensing the data presented in figure 7. Because the performance of all four subjects was qualitatively the same and because there is an inherent symmetry in the series of contrast ratios (i.e., the curves in fig. 7 are nearly antisymmetric), we collapsed the data over symmetric pairs of data points and averaged it over all subjects. We defined the contrast-dependent bias
for a given contrast ratio (and its inverse) as the difference in perceived vertical for symmetric contrast ratio pairs divided by two. Figure 11(b) plots the simulated output of the model (using eqs. (2), (3), and (5)) under the same conditions. Using the simplex method of nonlinear curve fitting (Press et al., 1988), we selected the only two floating parameters of the model (k₁ and k₂ of eq. (3)) such that simulations of equation (5) optimally (least-squared error) fit the data shown in fig. 11(a). Both the actual and simulated data show systematic shifts in the perceived direction of motion up to about 20° toward the direction of the higher-contrast grating.

Figure 11.— Simulated versus actual bias. (a) Plot of the same data as that in figure 7 averaged over subjects and over symmetric contrast-ratio pairs. (b) Simulations of the model in figure 9 under the same conditions as (a).

The model in figure 9 also qualitatively predicts the effect of changing the spatial and temporal frequency of the stimulus. Figure 12(a) plots the average bias of two observers as a function of $\log_2$ contrast ratio at three different spatial frequencies. Figure 12(b) plots the output of our model under the same conditions. The model qualitatively predicts that the bias will be larger at 0.75 c/d and smaller at 3.0 c/d. This prediction results from the changes in threshold as a function of spatial frequency (fig. 4(b)): changes in the threshold parameters (table 1) produce changes in $C_T$ (through eq. (2)) which via equations (3) and (5) yield changes in the simulated bias. There is, however, a significant quantitative discrepancy between the data and the simulations. Specifically, at 3.0 c/d, there is a small decrease in threshold so $C_T$ is slightly larger and therefore $f$ is slightly closer to 1. This leads to a small decrease in the simulated bias. However, there is a large decrease in the actual bias seen by our two observers. Similarly, at 0.75 c/d, although there is a large increase in threshold and, therefore, a large increase in the simulated bias, there is only a small increase in the actual bias seen by our two observers.

Increasing the temporal frequency had little effect on the perceived direction of plaid motion. Figure 13(a) shows the average data for the same two observers at mean temporal frequencies of 1.5 Hz and 4.5 Hz (plaid speeds of 2 and 6°/sec). Figure 13(b) shows the simulation of the model under the same
Figure 12.— Effect of spatial frequency. (a) Plot of the bias of two subjects at three spatial frequencies averaged over symmetric contrast-ratio pairs. (b) Simulations of the model in figure 9 under the same conditions as (a).

Figure 13.— Effect of temporal frequency. (a) Plot of the bias of two subjects at two temporal frequencies averaged over symmetric contrast-ratio pairs. (b) Simulations of the model in figure 9 under the same conditions as (a).

time conditions (using table 1 and eqs. (2), (3), and (5)). Temporal frequency changes had little effect on threshold (fig. 4(a)) and therefore had little effect on the simulated bias.
Our revised model does not appear robust to changes in the plaid angle. When the plaid angle is decreased to 30°, some subjects show a bias toward the direction of motion of the lower-contrast grating. Figure 14 shows the biases of two different observers at three different plaid angles. Decreasing the plaid angle affected the two subjects differently. The subject in figure 14(a) showed a reduced bias for a plaid angle of 45° and, at 30°, a reversal of the bias toward the motion of the lower-contrast grating. The model in figure 9 does not predict this reversal. However, the subject in figure 14(b) did not show this reversal.

![Figure 14](image)

Figure 14.—Effect of plaid angle. (a)-(b) Plots of the biases of two subjects at three different plaid angles.

**DISCUSSION**

**Perception of Motion for Unequal Contrast Plaids**

The results presented here and recent results by others (Kooi, DeValois, and Wyman, 1988) clearly show that the simple intersection-of-constraints rule model proposed by Adelson and Movshon (1982) cannot account for the perceived direction of motion of plaids when the components are of unequal contrast. However, a simple modification of their model, which takes into consideration the fact that the perceived speed of a moving grating is dependent on its contrast (Thompson, 1982), can, in most circumstances, account for the perceived direction of a moving plaid.

The modified model is robust in that it qualitatively predicts changes (or lack thereof) in perceived direction as a function of spatial and temporal frequency. The quantitative discrepancy between the predicted and actual effect of changing spatial frequency (fig. 13) can be explained if one postulates that f, the contrast-dependent weighting function, is itself a function of spatial frequency. In all of our simulations, f was defined by equation (3) as determined by fitting the data for a 1.5 c/d stimulus. If one allows the two floating parameters to vary with spatial frequency, one can quantitatively account for the data in figure 13(a).
Our results cannot be explained by incoherent plaid motion. Our standard stimulus (with a plaid angle of 60°) subjectively appeared to move coherently for all subjects even at contrast ratios as high as \(8\sqrt{2}\). This is not inconsistent with previous observations on coherence (Movshon et al., 1986). Furthermore, an objective measure of the coherence of our standard stimulus is the fact that the precision of the direction judgment is nearly independent of contrast ratio (fig. 8).

An important caveat when interpreting our results and those of others (Adelson and Movshon, 1982; Movshon et al., 1986; Ferrera and Wilson, 1988, 1989; Kooi et al., 1988; Welch, 1989), is that moving plaids are strong stimuli for optokinetic eye movements and that eye movements may contribute to the perception of plaid motion. In this study, the brief stimulus duration (300 msec) makes it unlikely that eye-movement contamination dominates the percept.

The fact that small plaid angles can cause a bias in the direction of the low-contrast grating cannot be explained by our revised model. However, there are at least two possible explanations for this discrepancy. First, because our moving plaids appeared less coherent at low plaid angles, it is possible that tracking behavior is different. If eye movements preferentially track the high-contrast grating, then the resulting retinal motion would be biased in the direction of the low-contrast grating, thus explaining the reversed bias seen in figure 14(a). Furthermore, if coherence threshold varies for different subjects then this could explain the intersubject variability as well. Second, the high-contrast grating might alter the perceived direction of the the low-contrast grating (Levinson and Sekuler, 1976). This directional masking would act to reduce the bias and, if it were large enough, could cause a reversal of the bias. It is logical to assume that directional masking would be more severe for small plaid angles because the component directions are more nearly equal, although the intersubject variability is still puzzling. The issue of the effect of plaid angle remains unresolved.

Finally, our success in salvaging the Adelson-Movshon hypothesis should not be construed as proof that the hypothesis is correct. Recently, Welch (1989) provided strong support for the first tenet of the hypothesis: that the motion of the plaid is first decomposed into the motion of the individual components. However, Ferrera and Wilson (1988, 1989) have found evidence that the intersection-of-perpendicular-constraints rule is not always used at the second stage of processing. Explaining our data with the revised Adelson-Movshon model should not be viewed as an endorsement of the intersection-of-constraints rule. It is likely that our data could be explained using a different second-stage rule. However, a contrast-dependent nonlinearity would still be required.

**Contrast-Dependent Effects in Motion Processing**

The contrast-dependent weighting function (fig. 10), determined by a least-squares, two-parameter fit to our bias data in figure 11, saturates at very low contrast (reaches 0.5 at 2.3 times threshold or below 2% contrast). Low-contrast saturation is associated with many psychophysical phenomena involving moving stimuli. Figure 15(a) replots \(f\) versus \(\log_{10}\) contrast (in threshold units) together with psychophysical measurements made in four different studies. As stated above, Thompson (1982) directly
Figure 15.— Comparison of our contrast-dependent nonlinearity with normalized contrast response functions found in the literature. (a) This panel replots the same function $f$ found in figure 10 on a log-scale plot together with data from four different psychophysical studies. The studies looked at the effect of contrast on perceived grating speed (filled squares), on detection of grating displacements (open squares), on motion after-effect duration (filled circles) and initial speed (open circles), and on perceived rotational frequency (filled triangles). (b) This panel replots $f$ as a function of absolute contrast with the data from three different physiological studies: MT, V1 (squares), and LGN data are from Sclar et al. (1989), V1 data (diamonds) are from Abrecht and Hamilton (1982), and retinal ganglion-cell data are from Kaplan and Shapley (1986). All of the physiological contrast response functions were plotted using the mean or median best-fitting hyperbolic function normalized to their response at 100% contrast. For the ganglion cells, the exponent of the hyperbolic function was fixed at 1.

measured the perceived speed of gratings as a function of contrast and found that low-contrast gratings appear to move more slowly than a high-contrast reference moving at the same speed. The closed squares plot the mean perception of two subjects as the ratio of perceived speed of a test grating to that of a standard grating of 25% contrast, assuming a detection threshold contrast of 0.5%. A higher detection threshold would shift the curve to the left and would therefore improve overlap with $f$. In Thompson’s study, the contrast effect appears to saturate slower, but he used a stimulus that differed slightly in spatial (his 2 c/d versus our 1.5 c/d) and temporal (his 2 Hz versus our 1.5 Hz) frequency, in mean luminance (his 32 cd/m² versus our 100 cd/m²), and greatly in duration (his 2.5 sec versus our 0.3 sec). In addition, from his data, it is difficult to assess the precision and possible bias associated with his matching technique. We assumed that a test grating of 25% matched the standard perfectly. All of these factors may explain the small quantitative differences between the $f$ measured in this study and Thompson’s results.

Nakayama and Silverman (1985) measured the effect of contrast on the minimum displacement of a sinusoidal grating that can be discriminated (leftward or rightward motion of a vertical grating). The
minimum displacement (in degrees of phase) necessary for discrimination decreases to 5-10° as contrast increases to about 3%, then remains nearly constant. The open squares in figure 15(a) plot what the authors called the normalized “effective contrast” of the stimulus (mean of the best-fitting hyperbolic functions for two subjects assuming again that threshold was 0.5%). Their effect saturates at nearly the same rate (reaches 0.5 at about 2.1 times threshold or around 1% contrast) as the contrast effect in this study.

Keck, Palella, and Pantie (1976) studied the effect of contrast on motion after-effect (MAE) and found that both the duration (closed circles) and perceived initial speed (open circles) of MAE (normalized with respect to that of a 12.5% grating) saturate at low contrast. Their MAE duration data nearly superimpose on the f derived in this study. Their MAE speed data saturate more slowly and at nearly the same rate as Thompson’s data.

Campbell and Maffei (1981) looked at the effect of contrast on perceived rotational speed and found that a rotating low-contrast grating patch was perceived to rotate more slowly than an otherwise identical high-contrast stimulus rotating at the same rate. The closed triangles in figure 15(a) plot the ratio of perceived rotational frequency of a test grating to that of a 20% contrast grating. The effect again saturates at low contrast, although not as rapidly as the effect in this study.

The fact that all of these disparate psychophysical studies seem to saturate similarly at low contrast probably reflects a fundamental property of a shared input stage for human judgments of motion. It is important for contrast responses within the motion-processing system to saturate early to disambiguate signals related to contrast from those related to motion. The interesting finding of this and the other studies is not that there are contrast-dependent misperceptions of motion, but actually that these misperceptions only occur at the extreme low end of the contrast scale.

Examination of the contrast-response properties of neurons within the monkey visual cortex suggests that this shared input is at a higher stage than striate cortex (Albrecht and Hamilton, 1982; Sclar, Maunsell, and Lennie, 1989). Figure 15(b) replots f as a function of log absolute contrast together with the normalized mean contrast response functions of ganglion cells (triangles), lateral geniculate neurons (circles), and neurons within the striate (open squares and diamonds) and extrastriate visual cortex (solid squares) of macaque monkeys. Albrecht and Hamilton found that striate neurons (V1) show a wide range of contrast response functions. Some neurons begin responding at 1% contrast and saturated by 10%. Others do not begin responding until 10% contrast. V1 neurons, on average, reached 50% of their maximal response at 23.9% contrast, with those neurons tuned for 1.5 c/d doing so at around 20%. Similarly, Sclar and colleagues (1989) found that, on average, V1 neurons reached 50% of their maximal response at 31.6%. They also found that neurons within the middle temporal area (MT), an area of extrastriate visual cortex specifically associated with motion processing (Maunsell and Van Essen, 1983; Rodman and Albright, 1987; DeYoe and Van Essen, 1988), saturate at much lower contrast. On average, MT neurons reached 50% of their maximal response at only 7.6% contrast, with some individual neurons reaching 50% saturation at as low as 1.6% contrast. Sclar and colleagues (1989) and Kaplan and Shapley (1986) measured the contrast response functions of neurons at earlier stages in the visual pathway, in the lateral geniculate nucleus (LGN) and retina, respectively. MT neurons have higher contrast sensitivities apparently because they receive a selective input from the magnocellular pathway (solid symbols) beginning at the retina (Kaplan and Shapley, 1986; DeYoe and Van Essen, 1988) and because they receive pooled information from lower-level neurons with smaller receptive fields (Sclar, Maunsell, and Lennie, 1989). On average, LGN neurons and ganglion cells within the magnocellular pathway...
reached 50% of their maximal response at 9.6% and 10.4% contrast, respectively. A separate parvocellular pathway has lower contrast sensitivity with neurons reaching 50% of their maximal response at 36.5% contrast in the LGN and at 38.9% in the retina.\footnote{1}

The psychophysical phenomena described in figure 15(a) still saturate faster than the responses in MT (or responses at earlier stages in the magnocellular pathway) suggesting that either the common input for psychophysical judgments is from a higher cortical level or that the psychophysical judgments use information pooled from several MT neurons. It is also possible that the humans make psychophysical judgments based on inputs from a selective group of MT neurons because a subset appears to saturate as fast as the psychophysics (Sclar et al., 1989).

In neither V1 nor MT does it appear that speed is encoded in the firing rates of individual neurons (Maunsell and Van Essen, 1983; Rodman and Albright, 1987; Orban, Kennedy, and Bullier, 1986; Movshon, 1975). Therefore, it is a reasonable conjecture that the speed of a moving grating is encoded as some integral of the collective output of an ensemble of MT neurons or in some “higher” cortical area that receives pooled input from MT. However, regardless of the specific scheme used to encode speed, at low contrasts, because neuronal activity within MT is affected by both speed and contrast, decrements in firing within the ensemble of neurons caused by reductions of contrast might be misinterpreted as reductions in stimulus speed (which could just as easily have been the cause). This would lead to the psychophysical findings presented here and in Thompson’s study (1982). At higher contrast, changes in the activity of MT neurons only reflect changes in the motion of the stimulus so the perception of speed is veridical.

Implications for Models of Human Motion Processing

The fact that contrast can systematically and dramatically distort the perceived direction of plaid motion puts a constraint on future models of human motion processing. As stated above, it cannot be explained by the schematic model in figure 1 (Adelson and Movshon, 1982), but it can be explained by the simple modification presented in figure 9. However, both the Adelson-Movshon and revised models are mere cartoons that provide an organizational structure for motion processing; they are not true

\footnote{1}When the average response (R) is given by a hyperbolic function of contrast (C), i.e.,

\[
R = \frac{R_{\text{max}} C^n}{C^n + C_\text{50}^n}
\]

it should be emphasized that \( C_{50} \) is not the contrast value which produces half the maximum response. Because \( C \) varies only between 0 and 100\%, \( R_{\text{max}} \) is often the extrapolated maximum, and the true contrast value at half-maximum response is

\[
\frac{100 C_{50}}{\sqrt[100]{100^n + 2C_{50}^n}}
\]

which reduces to \( C_{50} \) for \( C_{50} \approx 100\% \).
models. We now examine the performance of a few, more complete models of visual motion processing to determine if they mimic our psychophysical findings.

One class of models that would not exhibit the same behavior as our subjects consists of cross-correlation models (e.g., Leese, Novak, and Taylor, 1970). When a plaid with components of unequal contrast moves straight up, a pure cross-correlation technique will show no bias because cross-correlation determines the maximum overlap between two successive frames and overlap is perfect (neglecting noise) for true upward motion. Therefore, our results clearly indicate that the human visual system is not using a full-field, cross-correlation technique. Bulthoff, Little, and Poggio (1989) recently proposed a neural network implementation of a variant of the cross-correlation method. Rather than performing a simple 2-D cross-correlation over the whole image, it does a local cross-correlation over a patch. If this patch is the whole image, the model reduces to a simple cross-correlation model. In response to a plaid whose components are of unequal contrast, it would therefore show no bias. If the patch is small, as compared to the spatial frequency of the gratings, the model will exhibit a spatially nonuniform response: at different points within the image, it will detect either the motion of an individual component or of a node. It is hard to say what the exact response to a plaid whose components were of unequal contrast would be, as it depends critically on the patch size, but it seems likely that it would detect either the true direction of motion or nonrigid motion, but not the systematic biases that we observed empirically.

A second class of models that one would expect to be invariant to changes in contrast comprises those that track the motion of the nodes by tracking the motion of edges (zero-crossings of the second spatial derivative) within the image (e.g., Marr and Ullman, 1981; Hildreth, 1984). The nodes in our stimuli always moved exactly upward, regardless of the contrast ratio and, therefore, should only provide information about the true direction of motion. However, it is not the determination of the edge velocity per se, but how the edge velocities are combined to determine the global motion of the plaid that is important. For example, one model (Perrone, 1989) that identifies moving edges within images and hence, ostensibly, tracks the moving nodes, uses a cosine-weighted voting scheme to determine the global motion. The Perrone model shows a directional bias toward the direction of motion of the higher-contrast grating in response to plaids composed of unequal contrast gratings (Perrone and Stone, 1988), although the biases are twice as large as those found here. The simulated bias occurs because the nodes change shape and become spatially asymmetric for contrast ratios different than 1. This asymmetry causes a shift in the distribution of edge-velocity vectors. The voting scheme then causes a shift in the output of the model. Therefore, models that look at the motion of edges within the image can predict directional biases despite the fact that the features they are tracking are moving in the true direction of motion of the pattern as a whole. However, feature-based models that identify and track the nodes per se would not show such biases.

A third class of motion models consists of those that work directly with the spatial and temporal gradient of the image intensity (e.g., Limb and Murphy, 1975; Horn and Shunk, 1981). Recently, a neural network implementation of this approach has been shown to respond to plaids composed of unequal contrast gratings with directional biases toward the direction of motion of the higher-contrast grating (Koch et al., 1989). The bias is caused by the contrast dependence of their first-stage neurons (U cells) at low contrast, although the asymmetry of the spatial gradient, when the components have unequal contrasts, may also contribute. However, the proposal that the U cells are located in V1 is not
plausible, because the output of U cells is proportional to speed and no such units have been found in either V1 or anywhere else in the primate visual cortex.

A fourth class of models includes those that look at motion in the frequency domain (e.g., Watson and Ahumada, 1983, 1985), those that calculate motion energy (e.g., Adelson and Bergen, 1985), and the related elaborated Reichardt detectors (van Santen and Sperling, 1985). Motion-energy models are expected to be seriously affected by contrast manipulations because motion energy is basically proportional to the square of the contrast. To address this weakness, Heeger (1987) proposed a modified motion-energy model which normalizes the response by dividing the output of each sensor by the total energy for a given orientation. Because of this normalization, Heeger’s model determines the true direction of motion for moving plaids with contrast ratios as high as 1:32, which is inconsistent with our results. Furthermore, the model without contrast normalization will yield larger biases over a wider range of contrasts than the biases observed here. New approaches to reduce the inherent contrast dependence of motion-energy models need to be developed.

Watson and Ahumada (1985) designed their model of human motion processing to be robust to contrast variations. They determine the direction of motion by examining the temporal frequency of the response of linear spatio-temporal filters, a measure which is independent of contrast. Because of this, the Watson-Ahumada model finds the true direction of motion for plaids with contrast ratios as high as 1:10 which is inconsistent with our results. Their model, however, can be modified, as was the Adelson-Movshon model, by incorporating a contrast-dependent nonlinearity.

Our results are therefore inconsistent with the specific versions of a number of current models of human motion processing. In many cases, simple modifications can be made to account for our data. This discussion is not meant to be an exhaustive survey of motion models, but is merely intended to show how our psychophysical results can be used in many cases to refine and, in some cases, to rule out certain models. It is also meant to show how the quantitative comparison of empirical and simulation data is needed for the meaningful analysis of the biological plausibility of existing models of human visual motion processing.
REFERENCES


We performed a series of experiments examining the effect of contrast on the perception of moving plaids to test the hypothesis that the human visual system determines the direction of a moving plaid in a two-staged process: decomposition into component motion followed by application of the intersection-of-constraints rule. Although there is recent evidence that the first tenet of the hypothesis is correct, i.e., that plaid motion is initially decomposed into the motion of the individual grating components, the nature of the second-stage combination rule has not yet been established. We found that when the gratings within the plaid are of different contrast the perceived direction is not predicted by the intersection-of-constraints rule. There is a strong (up to 20°) bias in the direction of the higher-contrast grating. A revised model, which incorporates a contrast-dependent weighting of perceived grating speed as observed for one-dimensional patterns, can quantitatively predict most of our results. We then discuss our results in the context of various models of human visual motion processing and of physiological responses of neurons in the primate visual system.


