A Brief Review of Some Mechanisms Causing Boundary Layer Transition at High Speeds

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SUMMARY

In high-speed flight, the state of the boundary layer can strongly influence the design of vehicles through its effect on skin friction drag and aerodynamic heating. The major mechanisms causing boundary layer transition on high-speed vehicles are briefly reviewed and some empirical relations from the unclassified literature are given for the transition Reynolds numbers.

INTRODUCTION

An understanding of the mechanisms which cause transition of the boundary layer from laminar to turbulent flow remains the most complex problem in fluid mechanics. At hypersonic speeds, turbulent boundary layer heating can be several times greater than laminar heating. Therefore, it is essential that some reliable means of predicting transition be available to avoid the penalties that result from overly conservative design. Because transition is influenced by many factors, the engineer must rely on empirical relations derived from test data. However, none of the ground test facilities can simulate most of the parameters of interest; in fact, the operating characteristics of many test facilities have been found to influence the data strongly. In the following sections, some examples of test data will be discussed and a few correlation charts and formulas will be presented.

NOMENCLATURE

\[ k \quad \text{surface roughness element height} \]
\[ L \quad \text{total body length} \]
\[ M \quad \text{Mach number} \]
\[ r \quad \text{radius} \]
\[ Re \quad \text{Reynolds number (boundary layer edge value, except in fig. 3)} \]
\[ T \quad \text{temperature} \]
\[ w \quad \text{crossflow velocity} \]
\[ x \quad \text{distance along surface} \]
\[ \delta \quad \text{boundary layer velocity thickness} \]
\[ \mu \quad \text{coefficient of viscosity} \]
\[ \rho \quad \text{density} \]

Subscripts

\[ b_{tr} \text{ or } tr \quad \text{beginning of transition} \]
\[ e \quad \text{boundary layer edge value} \]
\[ n \quad \text{vehicle nose} \]
\[ r \quad \text{recovery or adiabatic wall value} \]
\[ sw \quad \text{swallowing of high-entropy gas layer} \]
\[ w \quad \text{wall condition} \]
\[ \theta \quad \text{boundary layer momentum thickness} \]
MEASUREMENTS

It has long been known that among the important parameters influencing transition are the boundary layer edge Reynolds number and Mach number. The results of plotting measurements of the Reynolds number calculated at the beginning of transition against Mach number are shown in figure 1 for flow on cones. At first glance, figure 1 appears to be a shotgun pattern of data points with transition Reynolds numbers varying from about 1 million to 30 million. However, even within this jumble of data there are some definite trends. First, note that the flight data give the highest transition Reynolds numbers and the wind tunnel data give the lowest values. The ballistic range points fall, more or less, in the middle.

The occurrence of early transition in many wind tunnels has been widely observed (refs. 1 and 2) and correlated by Dougherty and Fisher (ref. 2) with the intensity and, to some extent, the frequency of the free-stream disturbances in the facilities. The problems encountered in wind tunnel test measurements of transition have encouraged the use of ballistic ranges (refs. 3, 4, and 5). However, ballistic range experiments are affected by the small scale of the models which are, typically, on the order of a few centimeters in size. At that scale, microscopic surface irregularities and, possibly, dust particles suspended in the air can trigger transition. More recently, the development and use by Beckwith (ref. 6), of a low-disturbance, high Reynolds number, supersonic wind tunnel has yielded valuable data (refs. 7 and 8). For example, Chen et al. (ref. 8), measured similar transition Reynolds numbers at a Mach number of 3.5, on flat plates and slender cones with adiabatic walls. In high-noise wind tunnel tests at supersonic speeds, the transition Reynolds numbers on flat plates were only half as large as the values measured on cones (ref. 8), implying that the flat plate boundary layer was more sensitive to free-stream disturbances.

Many other phenomena can destabilize the laminar boundary layer. Among these are surface roughness, mass injection, positive pressure gradients, and wall heating or cooling (depending on the Mach number), as will be shown. In fact, any phenomenon which causes an inflection point to form in the boundary layer velocity profile is destabilizing (ref. 9). In contrast, boundary layer suction and negative pressure gradients have a stabilizing influence. While sucking hot air through the vehicle surface is highly impractical, it usually yields negative pressure gradients. One exception to the latter can occur when shock waves produced by different parts of the vehicle intersect. The resulting pressure rise can cause transition.

Although numerical calculations, using linear theory, have recently been made for simple shapes in high-speed flow (refs. 10 and 11), empirical correlations continue to be widely used, by necessity. Data have been collected and correlated with varying degrees of success for the phenomena causing boundary layer transition, and some examples will be discussed next.

EMPIRICAL CORRELATIONS

Despite the data scatter in figure 1, there is a discernible trend of increasing transition Reynolds number with rising Mach number. The same trend is shown more clearly in figure 2, which is based on references 12 and 13 for sharp cones tested primarily in wind tunnels. Note that the ballistic range measurements are, again, above most of the wind tunnel data. The high stability of the laminar boundary layer to disturbances at hypersonic edge Mach numbers has been observed by other researchers (ref. 14) and lends credence to the trend shown in figure 2. The data in figure 2 are for sharp cones. However, in practice
all bodies have finite amounts of nose bluntness. The nose bluntness introduces a second length scale, in addition to body size, into the transition problem.

Nose bluntness can have a very strong influence on transition as shown in figure 3 from reference 15. Note that the slopes of the lines change drastically at a value corresponding to about \( r_w/x_w = 10^{-2} \) for slender cones with half-angles of less than 10°. Therefore, the line labeled “small bluntness” is for very small amounts of nose blunting. The nose bluntness effect is caused by the action of the hot, high-entropy gas that has passed through the blunt portion of the bow shock. When the bluntness is “large,” the shear layer produced by the entropy gradient in the inviscid part of the flow destabilizes the boundary layer. In contrast, if the nose blunting is very small, the thin high-temperature gas layer is “swallowed” much sooner (closer to the nose) by the boundary layer. As the gas flows downstream over the cone, the hot layer becomes progressively thinner and moves closer to the wall. This process increases the heating of the wall which can be stabilizing in hypersonic flow.

The effect of wall heating on slightly blunted slender cone transition was correlated in reference 5 using ballistic range data for cone half-angles from 3° to 9°. Subsequently, it was shown in reference 16 that flight measurements made on a 22° half-angle cone confirmed the slender cone ballistic range results (fig. 4) that wall heating stabilizes the hypersonic boundary layer, at least for surfaces that are well below the adiabatic wall temperature.

Unlike the hypersonic boundary layer, the thin subsonic and transonic one existing on the blunt noses of high-speed flight vehicles is easily tripped by surface roughness. The mechanism has been extensively studied and correlations have been published (refs. 17-19). Since strong pressure gradients exist on the blunt noses, the correlations use Reynolds numbers based on boundary layer momentum thickness rather than the body lengths used for sharp cones and flat plates. A formula suggested by Laderman (ref. 18) is

\[
\text{Re}_{\theta_{\text{er}}} = 215 / \left( \frac{k T_e}{\theta T_w} \right)^{0.7}
\]

where \( k/\theta \) is the ratio of roughness element height to local momentum thickness. (Charts of momentum thickness in high-speed flight for bodies with various amounts of nose bluntness can be found in ref. 20.) Another correlation for surface-roughness-induced transition is presented by Amirkabirian et al. (ref. 21) for the Shuttle orbiter and is shown in figure 5. Although the Shuttle tiles’ surfaces are very smooth, the “roughness” results from misaligned tiles and the gaps that can form between tiles. Again, the majority of the flight data points are well above the shaded band which is based on wind tunnel tests.

It is valid to use local Reynolds numbers that are based on momentum thickness in preference to body length to correlate transition measurements on surfaces with pressure gradients. An approximate correlation for supersonic, or hypersonic, boundary layer edge velocities is (ref. 21)

\[
\text{Re}_{\theta} / M_e = \text{const.}
\]

where the constant varies from 150 to 350 depending on the ratio of roughness height to momentum thickness, etc. Another rationale for equation 2 is that it appears to yield a better correlation, with less data scatter, than using length Reynolds number, \( \text{Re}_x \). However, the above reasoning is faulty. For example, for the incompressible flow over a flat plate \( \text{Re}_{\theta} \sim \text{Re}_{x}^{0.5} \), or \( \theta \sim \theta^{2} \). Therefore, using either \( \text{Re}_{\theta} \) or \( \text{Re}_{x} \) will result in approximately the same uncertainty in the location of the beginning of transition on a flat plate.
One source of surface roughness is ablation of the heat shield. Another byproduct of ablation which destabilizes the boundary layer is gaseous mass addition. The effect of mass addition by transpiration of gases through a porous surface on transition on blunt bodies is presented in reference 22.

Some transition data are also available for configurations of practical interest, such as blunted cones at angle of attack (ref. 23), and swept-wing leading edges (ref. 24) where crossflow occurs. Crossflow can trigger transition by causing the formation of an inflection point in the inviscid shock layer velocity profile. A crossflow, boundary layer edge Reynolds number, which is approximately independent of Mach number, can be used to correlate transition, when written as

\[ Re = \frac{\rho_\infty w_\infty \delta}{\mu_\infty} \approx 350 \]  

In equation 3, \( w_\infty \) is the maximum crossflow velocity and \( \delta \) is the boundary layer velocity thickness. The remaining terms in the equation are evaluated at the boundary layer edge. The crossflow velocity, \( w \), must be computed using three-dimensional flow field codes, or it can be measured, although with difficulty. The constant of 350 is based on transonic and supersonic flight test data (refs. 25-27) and is supported by measurements made in the quiet supersonic wind tunnel (ref. 7) at Mach 3.5. In contrast, tests conducted in standard ("noisy") wind tunnels yielded values of 175 to 200 for the crossflow transition Reynolds number. These low values indicate that test-facility-generated disturbances can also cause early crossflow-induced transition.

CONCLUDING REMARKS

The major mechanisms causing boundary layer transition are briefly discussed and some empirical relations are given for the transition Reynolds numbers. The effects on transition of local Mach number, nose bluntness, wall temperature, surface roughness, mass injection, and crossflow are covered. It is shown that transition is significantly delayed as local Mach number increases. However, despite the high transition Reynolds numbers which may occur at hypersonic speeds, many large vehicles will still experience turbulent boundary layers over much of their surfaces.
REFERENCES


Figure 1. Typical transition data—cones.

Figure 2. Sharp-cone transition local Reynolds number as a function of local Mach.
Figure 3. Transition Reynolds number (free-stream) on blunt cones in hypersonic flow.

Figure 4. Effect of wall temperature on transition at hypersonic speeds.
Figure 5. Shuttle orbiter flight values of the transition parameters (from ref. 21; reprinted with permission of the American Institute of Aeronautics and Astronautics).
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