Simulated Dynamic Response of a Servovalve Controlled Hydraulic Actuator

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Abstract

A general purpose math model of a servovalve controlled hydraulic actuator system is derived. The system consists of a linear actuator with unequal piston areas, a single stage servovalve, a gas charged hydraulic accumulator, and the interconnecting piping. The state equations are integrated using the Advanced Continuous Simulation Language (ACSL) for determining the system's dynamic response characteristics. Using this generalized hydraulic actuator system model, response characteristics were determined for various servovalve commands.

Nomenclature

Variables

\[ A \] area

\[ B \] fluid bulk modulus

\[ C \] viscous damping

\[ DP \] differential pressure

\[ f \] servovalve bandwidth

\[ F_{st} \] static force

\[ F_{stk} \] sticking force

\[ F_{col} \] coulomb friction force

\[ K \] pressure loss coefficient

\[ m \] fluid mass
\[ M \] total mass of piston and load

\[ P \] pressure

\[ Q \] volumetric flow

\[ S \] laplace operator

\[ t \] time

\[ V \] volume

\[ W_N \] frequency

\[ x \] actuator displacement

\[ y \] servovalve spool displacement

\[ \gamma \] ratio specific heats

\[ \tau \] servovalve time constant

\[ \rho \] fluid density

\[ \xi \] damping

Subscripts

\[ \text{acc} \] accumulator

\[ \text{act} \] actuator

\[ c \] actuator cap side

\[ g \] gaseous

\[ r \] actuator rod side

\[ \text{cmd} \] command

\[ \text{in} \] initial condition

\[ l \] leakage

\[ lq \] liquid

\[ rt \] return side

\[ sp \] supply side

\[ \text{tot} \] total

\[ 2 \]
1.0 Introduction

Many dynamic systems use linear or rotary hydraulic actuators to generate large forces for obtaining high speed response. To satisfy design requirements for such systems, it is necessary to accurately predict load position, velocity, acceleration and system stability.

A generalized hydraulic actuator system was modeled utilizing the Advanced Continuous Simulation Language (ACSL) computer code to solve the system of nonlinear time-dependent ordinary differential equations. Model parameters are easily changed for purposes of component and system evaluation. Control strategies for particular hardware components may be evaluated by assessing the effect on system performance. For a given operating condition and controller gain setting, ACSL evaluates the poles of the system transfer function, thus providing a method to assess the stability of the system.

Three simulations were performed using typical system parameters; a step command to the servovalve, a steep ramp command, and a shallow ramp command. Results of the simulations are discussed with selected variables plotted.

2.0 Governing Equations

Shown in Figure 1 is a schematic of a typical servovalve controlled hydraulic actuator system. The system model consists of an actuator, single stage servovalve, gas charged
accumulator, and interconnecting piping. Presented here is the development of the governing equations for each component. The model of the hydraulic system presented here is an extension of that presented in reference (1) and in addition includes an unequal area piston actuator, Coulomb friction, sticking and pressure losses in the piping system.

2.1 Actuator

The actuator is modeled as a second order spring-mass system with viscous damping, Coulomb friction and sticking. The cap and rod side piston areas are unequal. Piston seal leakage is assumed laminar and given by:

\[ Q_l = K_{act}(P_c - P_r) \]  

(1)

Referring to Figure 1, continuity of mass flow into the cap end of the actuator yeilds:

\[ \frac{dm_c}{dt} + Q_l \rho_l = Q_{vc} \rho_c \]  

(2)

The mass contained in the cap end is given by:

\[ m_c = \rho_c V_c \]  

(3)

Differentiating,

\[ \frac{dm_c}{dt} = \rho_c \frac{dV_c}{dt} + V_c \frac{dp_c}{dt} \]  

(4)

Fluid bulk modulas is defined as:

\[ B = \frac{dP}{d\rho/\rho} \]  

(5)

Volume rate of change is given as:

\[ \frac{dV_c}{dt} = Ac \frac{dx}{dt} \]  

(6)

Substitute (4), (5), and (6) into (2) yeilding:

\[ Q_{vc} = \frac{V_c dP_c}{B \frac{dx}{dt} + Ac \frac{dx}{dt} + Q_l} \]  

(7)
Similarly for the rod end:

\[ Q_{vr} = \frac{V_r}{B} \frac{dP_r}{dt} - A_r \frac{dx}{dt} - Q_l \]  

(8)

A force balance on the actuator yields:

\[ M \frac{d^2x}{dt^2} = P_cA_c - P_rA_r - C \frac{dx}{dt} - (F_{st} + F_{stk} + F_{col}) \]  

(9)

At the point of zero actuator velocity, the fluid pressure must overcome the breakout or sticking force, \( F_{stk} \), before motion is established. At that time a constant force due to Coulomb friction, \( F_{col} \), opposes the direction of motion. These non-linear terms have the effect of increasing system damping.

2.2 Servovalve

The servovalve spool actuator is modeled as a first order system with response given as:

\[ \tau \frac{dy}{dt} + y = Y_{cmd} \]  

(10)

with

\[ \tau = 1/(2\pi f) \]

Servovalve bandwidth, \( f \), is typically specified by the manufacturer. The oil flow of the servovalve is a function of the square root of differential pressure across the valve and is given as;

\[ Q_{vc} = K_v(P_{vsp} - P_{vb})^{1/2} \]  

(11)

\[ Q_{vr} = K_v(P_{va} - P_{vrt})^{1/2} \]  

(12)

The variable, \( K_v \), is computed from manufacturer ratings of flow for a given differential pressure. For instance, if the servovalve is rated for 40 gpm at a pressure loss of 1000 psi, \( K_v \) would be calculated as:

\[ K_v = (3.85)(40)/(1000)^{1/2} = 4.87\text{in}^4/(\text{sec(lbf)})^{1/2} \]  

(13)
A servovalve spool may be manufactured with overlap to insure positive shutoff. An overlapped spool results in a deadband about the neutral position and acts to increase system damping. Deadband is modeled with an ACSL command by setting the dependent variable to zero when the independent variable lies between a specified lower and upper bound. (ref. 2)

2.3 Accumulator

The accumulator is charged with gas which is assumed to behave isentropically. Accumulator pressure is shown to be:

\[ P_{accin}(V_{gin})^\gamma = P_{acc}(V_g)^\gamma \]  \hspace{1cm} (14)

\[ V_g = V_{tot} - V_{lq} \]  \hspace{1cm} (15)

\[ \frac{dV_{lq}}{dt} = Q_{sp} \]  \hspace{1cm} (16)

\[ V_{lq} = \int Q_{sp} dt \]  \hspace{1cm} (17)

\[ P_{acc} = P_{accin}[V_{gin}/(V_{tot} - \int Q_{sp} dt)]^\gamma \]  \hspace{1cm} (18)

2.4 Piping

Pressure losses in the innerconnection piping is modeled by use of pressure loss coefficients. There are four significant sections of piping; the accumulator to servovalve, servovalve to return, and servovalve to rod and cap ends of the actuator cylinder. These equations are defined as:

\[ DP_{sp} = K_{sp}(Q_{sp})^2 \]  \hspace{1cm} (19)

\[ DP_{c} = K_{c}(Q_{c})^2 \]  \hspace{1cm} (20)

\[ DP_{r} = K_{r}(Q_{r})^2 \]  \hspace{1cm} (21)

\[ DP_{rt} = K_{rt}(Q_{rt})^2 \]  \hspace{1cm} (22)
2.5 Transfer Function

The system of equations for the generalized hydraulic actuator system may be linearized by making the following assumptions.

1. Coulomb friction and sticking are negligible
2. Pressure losses in the piping system are negligible
3. Supply pressure remains constant
4. Zero servovalve overlap

Incorporating these assumptions, a block diagram of the linearized system is shown in Figure 2. The block diagram may be reduced to yield the system transfer function:

\[
\frac{X}{Y_{cmd}} = \frac{BK_v \sqrt{\frac{P_{sp}}{2}} \left( \frac{A_r}{V_r} + \frac{A_c}{V_c} \right)}{S(\tau S + 1) \left[ S^2 + \frac{C}{M} S + \frac{B}{M} \left( \frac{A_r^2}{V_r} + \frac{A_c^2}{V_c} \right) \right]} \quad (23)
\]

Which may be put in the form:

\[
\frac{X}{Y_{cmd}} = \frac{W_N^2 K_v \left( \frac{A_r V_c + A_c V_r}{A_r^2 V_c + A_c^2 V_r} \right) \sqrt{\frac{P_{sp}}{2}}}{S(\tau S + 1) \left[ S^2 + 2\xi W_N S + W_N^2 \right]} \quad (24)
\]

yielding system natural frequency and damping.

\[
W_N^2 = \frac{B}{M} \left( \frac{A_r^2}{V_r} + \frac{A_c^2}{V_c} \right) \quad (25)
\]

\[
\xi = C/(2W_NM) \quad (26)
\]

For the case \(A_r = A_c\) and \(V_r = V_c\), such as a double acting linear actuator operating about midstroke the transfer function would reduce to:

\[
\frac{X}{Y_{cmd}} = \frac{W_N^2 K_v \sqrt{\frac{P_{sp}}{2}}}{S(\tau S + 1) \left[ S^2 + 2\xi W_N S + W_N^2 \right]} \quad (27)
\]

\[
W_N^2 = \frac{2BA^2}{VM} \quad (28)
\]

\[
\xi = C/(2W_NM) \quad (29)
\]
A rotary motor can also be modeled if the mass of the load is replaced with inertia of the rotary motor.

3.0 Method of Solution

A computer model of the above equations (Appendix 7.0) was implemented using the ACSL code. ACSL was written to facilitate the solution of a system of nth order, nonlinear ordinary differential equations which describe a physical system. Special functions are available in addition to standard Fortran commands to provide flexibility in the problem description. The code sorts the commands into an executable sequence such that a variable is calculated before it is used, allowing the system of equations to be inputted in a logical sequence. Nine integration algorithms are available (default is fourth order Runge-Kutta) in addition to a user supplied routine. The code assigns lower order derivatives a variable name then simultaneously solves the system of first order equations and determines the system states.

A post run command invokes a linear analysis which determines the system poles and damping. The linearized forcing matrix is determined for perturbations about a particular operating point. This capability is particularly useful for designing or developing control strategies.

4.0 Results

A typical use for a servovalve controlled hydraulic actuator system would be that of model injection into the test chamber of a supersonic wind tunnel. Table I shows system parameters for such an application. Dynamic behavior for this model was simulated by solving the nonlinear equations described in section 2 using the ACSL code. Results are presented for three different servovalve command functions.
4.1 Case 1, Step Command to Servovalve

Figure 3a-e presents results for a step command to the servovalve. The servovalve was given a step command of 30%, held for 0.5 second than returned to the neutral position. Table I shows the ACSL equation for the step command. Simulated response to this command shows large initial acceleration as the servovalve opens rapidly subjecting the actuator piston to large differential pressure. While the servovalve spool position is held fixed, the actuator piston velocity remains fairly constant, decreasing slightly as accumulator pressure decreases. Upon return of the servovalve spool to the neutral position, the actuator again undergoes large acceleration/deceleration. Oscillation (second order response) of the piston and load occurs due to the compressibility of fluid (fluid bulk modulus). These oscillations are damped by viscous and coulomb friction. The maximum flow for this simulation occurs to the cap end of the actuator, about +15GPM, while the rod end experiences about a −7GPM flow rate (flow in is taken as positive, flow out is negative). The difference in these flow rates is due to the unequal piston area of the rod and cap ends.

4.2 Case 2, Steep Ramp Command to Servovalve

Figure 4a-e presents results for a steep ramp command to the servovalve. The servovalve was given a command of 150%/sec for 0.2 second, then held at 30% for 0.2 second and returned to the neutral position at a rate of −150%/sec. Table I shows the ACSL equation for this ramp command. From these results it is seen that the actuator piston and load is subjected to much lower peak acceleration than in Case 1. Maximum velocity and flows are similar due to the same command hold state. Piston oscillation is much less pronounced and of shorter duration than that of Case 1.
4.3 Case 3, Shallow Ramp Command to Servovalve

Figure 5a-e presents results for a shallow ramp command to the servovalve. The servovalve was given a command of 60%/sec for 0.5 second, then held at 30% for 0.1 second, and then returned to the neutral position at a rate of −60%/sec. Table I shows the ACSL equation for this ramp command. Similar to the results of Case 2, peak acceleration of the piston and load is again reduced with the less abrupt servovalve spool movement. Maximum velocity and flows are again about the same due to the same command hold state as the previous simulations. Piston oscillation is almost non-existent for this case.

These simulations indicate that the acceleration of the piston and load are determined by the rate of change of the servovalve command. The magnitude of the servovalve command determine piston and load slew rate.

5.0 Conclusion

A general purpose math model of a servovalve controlled hydraulic actuator system is derived for use with the Advanced Continuous Simulation Language (ACSL). Parameters typical of a hydraulic system were input and the model exercised. The math model is of a general hydraulic actuator system which can be easily changed. This allows for quick assessment of alternate system hardware or control strategy.
6.0 References/Acknowledgement


Acknowledgement is extended to Mr. J. F. Watson Jr. of NASA Langley Research Center. Mr. Watson provided the author with an ACSL model and schematic of a hydraulic injection system which became the basis of this memorandum. Appendix 7.0 contains the code listing and revisions incorporated into the model.
Table I Example Simulation Parameters

Actuator

<table>
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<th>Value</th>
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<td>Cylinder Length</td>
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<tr>
<td>Stroke</td>
<td>15</td>
</tr>
<tr>
<td>Mass of Piston &amp; Load</td>
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<td>Cylinder I.D.</td>
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<td>Rod Diameter</td>
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<td>$K_{q_{act}}$</td>
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<tr>
<td>$F_{stk}$</td>
<td>75</td>
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<tr>
<td>$F_{col}$</td>
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Servo Valve

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<td>Bandwidth</td>
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<tr>
<td>Max Flow @ 1000 psid</td>
<td>40 GPM</td>
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<td>Deadband</td>
<td>+/−2 %</td>
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Accumulator and Piping

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<td>Initial Gas Charge</td>
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<td>Supply Pressure</td>
<td>3000 psig</td>
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<tr>
<td>Return Pressure</td>
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<td>$K_{q_{sup}}$</td>
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<tr>
<td>$K_{q_{ret}}$</td>
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<tr>
<td>$K_{q_{cap}}$</td>
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</tr>
<tr>
<td>$K_{q_{rod}}$</td>
<td>0.0125 Lbf sec²/in⁸</td>
</tr>
</tbody>
</table>

Command to Servo Valve

Case 1. (Figure 3), Step Command

$$Y_{cmd} = 30(\text{step}(0.2) - \text{step}(0.7))$$

Case 2. (Figure 4), Steep Ramp Command

$$Y_{cmd} = 150(\text{ramp}(0.2) - \text{ramp}(0.4) - \text{ramp}(0.6) + \text{ramp}(0.8))$$

Case 3. (Figure 5), Shallow Ramp Command

$$Y_{cmd} = 60(\text{ramp}(0.1) - \text{ramp}(0.6) - \text{ramp}(0.7) + \text{ramp}(1.2))$$
Figure 1. Schematic of Servovalve Controlled Hydraulic Actuator System.
Note: $P_{sup} =$ Supply pressure; Return pressure assumed zero

Transfer function:

$$\frac{X}{Y_{CMD}} = \frac{BK \sqrt{\frac{P_{sup}}{2}} \left( \frac{A_r}{V_r} \cdot \frac{A_c}{V_c} \right)}{S(\tau S + 1) \left[S^2 + \frac{C}{M} S + \frac{B}{M} \left( \frac{A_r^2}{V_r} \cdot \frac{A_c^2}{V_c} \right) \right]}$$

For $A_r = A_c = A$ and $V_r = V_c = V$
Transfer function reduces to:

$$\frac{X}{Y_{CMD}} = \frac{2A BK \sqrt{2 P_{sup}} / (VM)}{S(\tau S + 1) \left[S^2 + \frac{C}{M} S + 2BA^2 / (VM) \right]}$$

Figure 2. Block Diagram of Linearized Servovalve Controlled Hydraulic Actuator System for Small Perturbations.
Figure 3a. Servovalve Command (YCMD) and Actuator Position (X) Versus Time for a Step Command to the Servovalve.

Figure 3b. Actuator Velocity (XDOT) and Acceleration (XG) Versus Time for a Step Command to the Servovalve.
Figure 3c. Cap Side Flow (QCAPG) and Pressure (PCAP) Versus Time for a Step Command to the Servovalve.

Figure 3d. Rod Side Flow (QRODG) and Pressure (PROD) Versus Time for a Step Command to the Servovalve.
Figure 3e. Supply Pressure (PACC) and Supply Flow (QSUPG) Versus Time for a Step Command to the Servovalve.
Figure 4a. Servovalve Command (YCMD) and Actuator Position (X) Versus Time for a Steep Ramp Command to the Servovalve.

Figure 4b. Actuator Velocity (XDOT) and Acceleration (XG) Versus Time for a Steep Ramp Command to the Servovalve.
Figure 4c. Cap Side Flow (QCAPG) and Pressure (PCAP) Versus Time for a Steep Ramp Command to the Servovalve.

Figure 4d. Rod Side Flow (QRODG) and Pressure (PRODG) Versus Time for a Steep Ramp Command to the Servovalve.
Figure 4e. Supply Pressure (PACC) and Supply Flow (QSUPG) Versus Time for a Steep Ramp Command to the Servovalve.
Figure 5a. Servovalve Command (YCMD) and Actuator Position (X) Versus Time for a Shallow Ramp Command to the Servovalve.

Figure 5b. Actuator Velocity (XDOT) and Acceleration (XG) Versus Time for a Shallow Ramp Command to the Servovalve.
Figure 5c. Cap Side Flow (QCAPG) and Pressure (PCAP) Versus Time for a Shallow Ramp Command to the Servovalve.

Figure 5d. Rod Side Flow (QRODG) and Pressure (PROD) Versus Time for a Shallow Ramp Command to the Servovalve.
Figure 5c. Supply Pressure (PACC) and Supply Flow (QSUPG) Versus Time for a Shallow Ramp Command to the Servovalve.
PROGRAM CYLINDER

SERVOVALVE CONTROLLED HYDRAULIC ACTUATOR SYSTEM ANALYSIS
ORIGINAL VERSION BY J. F. WATSON, FENGD, FACS
REVISED BY
D. A. BABCOCK MAY 1989, FENGD, PSS

THIS UPDATED VERSION OF THE ORIGINAL CODE INCLUDES THE EFFECTS OF
ACTUATOR STICKING AT ZERO VELOCITY; ACTUATOR COULOMB FRICTION;
ACTUATOR LEAKAGE FROM THE HIGH TO LOW PRESSURE PORTS; AND
SERVOVALVE DEADBAND AS A PERCENTAGE OF OVERLAP; THESE NONLINEAR
TERMS INCREASE THE SIMULATED SYSTEM DAMPING

**************************** VARIABLE TABLE ******************************

X LOAD DISPLACEMENT INCH
XDOT LOAD VELOCITY IN/SEC
XDDOT LOAD ACCELERATION IN/SEC**2
IX INITIAL POSITION IN

CYSTK ACTUATOR STROKE LENGTH IN
CYDIA ACTUATOR PISTON DIAMETER IN
RODDIA ACTUATOR ROD DIAMETER IN
WACTR ACTUATOR PISTON AND ROD WEIGHT LB
WLOAD LOAD WEIGHT LB

FCYL CYLINDER GENERATED FORCE LB
KFV VISCOS DAMPING LB-SEC/IN
FVISC VISCOS FRICTION FORCE LB
FSTAT GRAVITY FORCE OF LOAD AND ACTUATOR LB
FSTK ACTUATOR STICKING FORCE LB
FCOL ACTUATOR COULOMB FRICTION FORCE LB
MTOTL TOTAL MASS OF MOVING ITEMS LB-SEC**2/IN

PROD ROD SIDE CYLDR PRESSURE PSIG
PCAP CAP SIDE CYLDR PRESSURE PSIG
DPprod LINE PRESSURE LOSS ROD SIDE PSID
DPpcap LINE PRESSURE LOSS CAP SIDE PSID

Qrod ROD SIDE CYLDR OIL FLOW IN**3/SEC
QCAP CAP SIDE CYLDR OIL FLOW IN**3/SEC
Vrod ROD SIDE CYLDR OIL VOLUME IN**3
VCAP CAP SIDE CYLDR OIL VOLUME IN**3
AROD ROD SIDE AREA IN**2
ACAP CAP SIDE AREA IN**2
<table>
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<td>Servovalve SPOOL DISP</td>
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<td>KQACT</td>
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</tr>
<tr>
<td>B</td>
<td>Fluid Bulk Modulus</td>
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<tr>
<td>GAMM</td>
<td>Ideal Gas Specific Heat Ratio</td>
</tr>
<tr>
<td>ATM</td>
<td>Local Atmos Pressure</td>
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</table>

**CONSTANTS**

- **Servovalve**
  - Constant SERVFL = 40.0, SERVPR = 1000.0
  - Constant DBAND = 0.02, TAU = 0.006

- **Accumulator and Piping**
  - Constant PN2CHG = 1800.0, VOLACC = 5.0, GAMM = 1.4
  - Constant KQSUP = 0.01250, KQRET = 0.01250
  - Constant KQCAP = 0.01250, KQROD = 0.01250

- **Fluid Constants**
  - Constant POILCG = 3000.0, PRET = 25.0, B = 100000.0
CONSTANT CYSTK = 17.0, CYDIA = 2.0, RODDIA = 1.375
CONSTANT WACCTR = 500.0, WLOAD = 2000.0, KFV = 50.0
CONSTANT FSTK = 75.0, FCOL = 50.0, KQACT = 0.01
CONSTANT ALL = 0.5 "$ ACTUATOR LOWER INTEG LIMIT"
CONSTANT AUL = 16.5 "$ ACTUATOR UPPER INTEG LIMIT"

LOGICAL STUCK "$ TRUE IF VELOCITY IS ZERO OTHERWISE FALSE"
CONSTANT TSTRT = 0.0
CONSTANT TSTP = 1.0
CONSTANT ATM = 14.7
CONSTANT PI = 3.1415927
CONSTANT INPGAL = 231.0 "$ IN3 PER GALLON"
CONSTANT CNVRT = 3.85 "$ IN3/SEC TO GPM"
CONSTANT ACCG = 386.4 "$ GRAVITATIONAL CNST IN/SEC**2"
CONSTANT LL = 5.0 "$ LOWER PRES INTEGRATION LIMIT"
CONSTANT UL = 5000.0 "$ UPPER PRES INTEGRATION LIMIT"

INITIAL "$ SET INITIAL CONDITIONS"

VLN20 = VOLACC * INPGAL * PN2CHG / ( POILCG + ATM )
KACCM = ( POILCG + ATM ) * ( VLN20 ** GAMM )

RESET("NOEVAL")
STUCK = XDOT .EQ. 0.0 "$ ACTUATOR STICKS WHEN VELOCITY IS ZERO"
FVISC = 0.0

FSTAT = WACCTR + WLOAD
MTOTL = FSTAT / ACCG

ACAP = (PI / 4.0) * (CYDIA ** 2)
AROD = ACAP - (PI / 4.0) * (RODDIA ** 2)

IPROD = (POILCG * ACAP - FSTAT) / (AROD + ACAP)
IPCAP = POILCG - IPROD
IX = 0.0

SERVOVALVE
KQSER = CNVRT * SERVFL / (SQRT( SERVPR ))

END "$ OF INITIAL"

SERVOVALUE

DYNAMIC DERIVATIVE

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" YCMD = 0.3*(STEP(.2) - STEP(.7))" "$STEP COMMAND"
YCMD = 1.5*(RAMP(.2)-RAMP(.4)-RAMP(.6)+RAMP(.8)) "$RAMP COMMAND"
" YCMD = 0.6*(RAMP(.1)-RAMP(.6)-RAMP(.7)+RAMP(1.2))" "$RAMP COMMAND"

"************************ CONTROLLER SECTION ***************************"
" SERVOVALVE CONTROLLER MAY BE ADDED HERE"

"************************ SERVOVALVE ***************************"

DYNAMIC SECTION

YDOT = (YCMD - YV) / TAU
YV = LIMIT ( YDOT, 0.0, -1.0, +1.0 )
Y = DEAD ( -DBAND, DBAND, YV )

FLOW SECTION

FLOW0 = 0.0
FLOW1 = Y*KQSER*(SQRT(ABS(PSRVP-PSRUB)))*SIGN(1.,PSRVP-PSRUB)
FLOW2 = Y*KQSER*(SQRT(ABS(PSRUB-PSRUT)))*SIGN(1.,PSRUB-PSRUT)
FLOW3 = -Y*KQSER*(SQRT(ABS(PSRVA-PSRVT)))*SIGN(1.,PSRVA-PSRVT)
FLOW4 = -Y*KQSER*(SQRT(ABS(PSRVP-PSRVA)))*SIGN(1.,PSRVP-PSRVA)
QVR = FCNSW(Y, FLOW4, FLOW0, FLOW3)
QVC = FCNSW(Y, FLOW2, FLOW0, FLOW1)

"************************ ACTUATOR FORCES AND POSITION ******************"

X = LIMIT ( XDOT, IX, ALL, AUL )
XDOT = INTEG ( XDDOT, 0.0)
XDDOT = ( FTOTL + FCF ) / MTOTL

FTOTL = FCYL - FVISC - FSTAT
FVISC = KFV * XDOT
FCYL = PCAP * ACAP - PROD * AROD
FCF = RS14 ( STUCK, -FTOTL, FASF)
FIA = RSN ( STUCK, ABS ( FTOTL ) - FSTK, XDOT )
SCHEDULE STICK .XZ. FIA

"************************ ROD SIDE FLOW AND PRESSURE ******************"

PROD = LIMIT ( PDROD, IPROD, LL, UL )
QROD = AROD * XDOT
PDROD = ( QVR + QROD + QL ) * ( B / VROD )
VROD = AROD * ( CYSTK - X )
DPPROD = ( QROD ** 2 ) * KQROD * SIGN ( 1.0, QROD )
PSRVA = PROD - DPPROD

QL = KQACT * ( PCAP - PROD ) "$ACTUATOR LEAKAGE"

"************************ CAP SIDE FLOW AND PRESSURE ******************"

PCAP = LIMIT ( PDPCAP, IPCAP, LL, UL )
QCAP = ACAP * XDOT

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PDCAP = ( QVC - QCAP - QL ) * ( B / VCAP )
VCAP = ACAP * X
DPPCAP = ( QCAP ** 2 ) * KQCAP * SIGN ( 1.0, QCAP )
PSRVB = PCAP + DPPCAP

"**************** ACCUMULATOR / SUPPLY AND RETURN ******************"

DELVOL = INTEG ( QSUP, 0.0 )
VOLN2 = VLN20 + DELVOL
PACC = KACCM / ( VOLN2 ** GAMM ) - ATM

DPPSUP = ( QSUP ** 2 ) * KQSUP * SIGN ( 1.0, QSUP )
PSRVP = PACC - DPPSUP
QSUP = FCNSW ( Y, -QROD, 0.0, QCAP )

DPPRET = ( QRET ** 2 ) * KQRET * SIGN ( 1.0, QRET )
PSRVT = PRET + DPPRET
QRET = FCNSW ( Y, -QCAP, 0.0, QROD )

END $ "OF DERIVATIVE"

DISCRETE STICK

STUCK = .NOT. STUCK .AND. ABS( FTOTL ) .LT. FSTK
FASF = RSW ( STUCK, 0.0, SIGN( FCOL, -FTOTL ) )
XDOT = 0.0 "$ SET VEL 0 IF STICKING "$ END $ "OF PROCEDURAL"
END $ "OF DISCRETE"

"******************* ENGINEERING VARIABLES *******************"

" CONVERT IN**3 TO GALLON PER MINUTE
QCAPG = QCAP / CNVRT
QRODG = QROD / CNVRT
QSUPG = QSUP / CNVRT
QRETG = QRET / CNVRT

" CONVERT IN/SEC**2 TO G
XG = XDDOT / ACCG

TERMT ( T .GE. TSTP )

END $ "OF DYNAMIC"
END $ "OF PROGRAM"
A general purpose math model of a servovalve controlled hydraulic actuator system is derived. The system consists of a linear actuator with unequal piston areas, a single stage servovalve, a gas charged hydraulic accumulator, and the interconnecting piping. The state equations are integrated using the Advanced Continuous Simulation Language (ACSL) for determining the system's dynamic response characteristics. Using this generalized hydraulic actuator system model, response characteristics were determined for various servovalve commands.