Modification of the SHABERTH Bearing Code To Incorporate RP–1 and a Discussion of the Traction Model

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Summary

Recently developed traction data for Rocket Propellant 1 (RP-1), a hydrocarbon fuel of the kerosene family, were used to develop the parameters needed by the bearing code SHABERTH in order to include RP-1 as a lubricant choice. As an aid to future additions, a review of the procedure for inputting data for a new lubricant choice is presented. In particular, the fluid traction model used by SHABERTH is discussed, and issues concerning it are presented. In the process of fitting the RP-1 traction data to the model, certain assumptions and simplifications were necessary. The error resulting from making these simplifications is discussed.

A slight error was detected in the traction equations that are in the SHABERTH program, but a lack of traction data on the original lubricants prevented immediate correction of the error. However, the error was judged insignificant to the traction prediction for RP-1. A temperature dependency that is not accounted for by the model was found in a particular traction coefficient for RP-1. The maximum traction coefficients that were predicted by using temperature-averaged coefficients errored by an average of 12 percent, whereas those predicted by using the discrete coefficients at the two temperature conditions errored by an average of 4 percent. Currently, the temperature-averaged coefficients are being used. The model of the pressure-viscosity coefficient as a function of temperature was modified for RP-1 by using pressure-viscosity data valid for RP-1.

Background

The introduction of reusable engines for space launch vehicles has made necessary the development of more rigorous design methodologies for long-life bearings in launch vehicle turbopump applications. Considerations of weight and simplicity require that the working fuel and oxidizer be used as the turbopump coolant and lubricant; however, there is currently a lack of data on the rheological properties of the types of fluids used in these applications at the conditions present in a bearing contact (i.e., high pressures and potentially high shear rates).

One fuel that has been considered for use in future launch vehicles (e.g., the advanced launch system (ALS)) is Rocket Propellant 1 (RP-1), a type of kerosene. Though RP-1 has been used in the past to cool and lubricate the bearings of expendable launch vehicles, such as Titan, only a small amount of data on its rheological properties has been collected (refs. 1 to 3).

In order to design long-life bearings to be run in RP-1, the bearing behavior needs to be theoretically analyzed. One of the most widely used rolling-element-bearing design and analysis tools is the computer code SHABERTH (Shaft Bearing Thermal Analysis, ref. 4). SHABERTH simulates the thermomechanical performance of a load support system consisting of up to five ball, cylindrical, or tapered-roller bearings. Transient or steady-state temperatures can be calculated by using a lumped-mass thermal model that takes into account free convection, forced convection, conduction, radiation, and mass transport heat transfer.

Since the SHABERTH code takes into account the influence of the lubricating fluid on bearing behavior, it requires certain empirical rheological data for the particular fluid. The SHABERTH code currently contains hard-coded rheological data on a number of lubricants. These data consist of density, thermal coefficient of expansion, thermal conductivity, the relationships of viscosity and temperature, and pressure-viscosity coefficient and temperature at ambient pressure; and the characteristics of fluid traction as a function of shear rate.

The rheological properties of RP-1, a low-viscosity fuel, differ greatly from those of the lubricating oils currently in the program as lubricant choices: therefore, the SHABERTH code had to be modified to include RP-1. The density, thermal expansion, and thermal conductivity, as well as data for viscosity with respect to temperature and for the pressure-viscosity coefficient as a function of temperature were available. The characteristics of traction force as a function of shear rate, however, needed to be established. Once all of the rheological data were established, they had to be fit to the various rheological models used by the code; this determined the inherent parameters that needed to be hard-coded into the SHABERTH code.

Introduction

The purposes of this report are (1) to review the general procedure for inputting data for a new lubricant choice into the SHABERTH bearing code and to describe the theoretical traction model used by SHABERTH, (2) to describe the fitting of the experimental RP-1 fluid traction data to the model, and
(3) to present results and quantify the error due to making certain assumptions. All RP-1 parameters needed by SHABERTH to run the program are specified.

As previously mentioned, in order to predict the behavior of a bearing being lubricated and cooled by a specific fluid, the SHABERTH bearing code requires empirically derived rheological data on the fluid (viscosity-temperature relationship, density, thermal expansion, thermal conductivity, pressure-viscosity coefficient, and traction force as a function of shear rate). The experimental data must be fit to various rheological models that the code uses to determine the values of specific parameters for that fluid. These values must then be hard-coded. A review of the entire procedure is presented to aid in future lubricant additions. This review utilizes material from references 4 to 6. In particular, the fluid traction model used by the SHABERTH code is discussed in detail.

Experimental viscosity-temperature, density, thermal expansion, and thermal conductivity data for RP-1 were obtained from reference 7. The experimental characteristics of traction force as a function of shear rate needed to be established. The traction force in a bearing contact is dependent not only on shear rate (or sliding velocity) but also on the maximum Hertzian contact pressure, the rolling velocity, and the temperature of the fluid in the contact. An effort was made to obtain experimental data on the traction coefficient as a function of sliding velocity for RP-1 fuel at various conditions of maximum contact pressure, rolling velocity, and temperature. The work was conducted on a twin disk traction tester by using side slip to produce the traction. Further information on the testing can be found in reference 8, where RP-1 data pertaining to the pressure-viscosity coefficient at ambient pressure as a function of temperature, which was used to modify the SHABERTH code, can also be found.

Fitting the experimental data to the rheological models is straightforward for all but the fluid traction model. Therefore, only the fitting of the RP-1 fluid traction data to the fluid traction model will be discussed in detail. The necessary parameters for all of the models will be specified.

In the process of fitting the RP-1 traction data to the traction model that exists in the code, certain assumptions and simplifications were necessary. The error due to making these simplifications is quantified by comparing theoretical predictions of traction force with and without the simplifications to each other and to the experimental data.

**Review and Discussion of the SHABERTH Rheological Models**

**Fluid Property Models**

This section describes the density, thermal conductivity, viscosity and temperature, and pressure-viscosity and temperature models already in the SHABERTH code (see ref. 6). Values for the parameters within the models for RP-1 are listed in appendix A.

Although the SHABERTH code requires the user input file to be in SI units and furnishes the output in SI units, the internal calculations are all done in English units. Also, some of the models used are based on empirical equations that were developed by using a mixture of SI and English units. Therefore, some variation occurs in the system of units required for each piece of property data that must be hard-coded. The proper units for each piece of information are specified. All symbols are defined in appendix B.

**Density, thermal expansion coefficient, and thermal conductivity.**—The SHABERTH code assumes a linear relationship between fluid density and temperature, with the thermal expansion coefficient being the slope. The necessary parameters are the fluid density \( \rho \) (in g/cm\(^3\) at 60 °F) and the thermal expansion coefficient \( \alpha \) (in (g/cm\(^3\))/°C), which can be obtained as the slope of the line of the specific gravity plotted as a function of temperature \( T \). The code internally converts \( G \) to degrees Fahrenheit and calculates density using

\[
\rho T = \rho \text{ (at 60 °F)} - G (T - 60 °F)
\] (1)

The thermal conductivity of the fluid \( K' \), which must be expressed in the code in watts/meter °C, is assumed to be constant with temperature. In actuality, it varies slightly with temperature, so the user must choose the specific temperature at which to take the thermal conductivity data.

**Viscosity as a function of temperature.**—The kinematic viscosity \( \nu \) in centistokes (cSt) at atmospheric pressure is calculated as a function of temperature from Walther's relation (ref. 6)

\[
\log_{10} \left[ \log_{10} (\nu + 0.6) \right] = A - B \log_{10} (T + 459.7)
\] (2)

\( A \) and \( B \) are lubricant-dependent constants determined by substituting into equation (2) the experimental data of kinematic viscosity \( \nu \) (in cSt) as a function of temperature \( T \) (in °F).

SHABERTH calculates the absolute viscosity at ambient pressure \( \eta_0 \) in centipoise (cP) using

\[
\eta' = \nu \rho
\] (3)

The necessary parameters for the code are \( A, B, \) and \( \nu \) at both 100 and 210 °F, in cSt.

An auxiliary temperature-viscosity coefficient \( \beta \) (in 1/°R), which is needed for use in a film-thickness thermal reduction factor, is found by calculating

\[
\beta = 0.00909 \ln \frac{\eta_0 \text{ (at 100 °F)}}{\eta_0 \text{ (at 210 °F)}}
\] (4)
Pressure-viscosity coefficient as a function of temperature.—The SHABERTH code calculates the value of the pressure-viscosity coefficient \( \alpha \) (in\(^2/\text{lb}\)) at atmospheric pressure and a given temperature by using the following relationship developed by Fresco (ref. 6):

\[
\alpha = (2.303 \times 10^{-4}) \left( C_r + D_r \log_{10}(\nu) + E_r \left( \log_{10}(\nu) \right)^2 \right)^{1/2}
\]

where

- \( TF = 560/(T + 459.7) \)
- \( \nu = \nu T \)
- \( C_r, D_r, E_r \) constants determined by Fresco
- \( T \) temperature, °F

The values of \( C_r, D_r, \) and \( E_r \) are constant for all lubricant types, so no further data are needed for the particular fluid. However, whether this model will adequately predict pressure-viscosity coefficients for fluids that differ greatly from the original lubricating oils in the code is questionable. This will be discussed in the section Pressure-Viscosity Coefficient for RP-1.

**Traction**

In this section, the traction curve is defined and the SHABERTH traction model is described. All symbols are defined in appendix B.

The traction curve.—Tevaarwerk (ref. 9) defines traction as “the ability of a fluid film, trapped under high pressure in the elastically deformed region of two loaded curved elements, to transmit a tangential force from one element to the other.” The characteristics of traction variation with shear rate for a fluid have an important effect on the behavior of the contacting bodies separated by the fluid, both in the motion of the bodies and in the amount of heat generated between them. When two contacting rolling elements that are separated by a fluid have different surface speeds, tangential forces develop at the area of contact. These forces, which arise from the shearing of the fluid layer, are a function of the rate of shear of the fluid. They are also a function of the type of fluid and of the maximum Hertzian contact pressure, rolling velocity, and fluid temperature within the contact area. Therefore, the traction characteristics of a fluid must be determined experimentally for each fluid. This can be done by rotating two disks against one another and introducing a measurable amount of slip between them while using the fluid in question as the lubricant. Curves of traction force as a function of sliding rate can be obtained at various conditions of maximum contact pressure \( P_m \), rolling velocity \( V \), and fluid temperature \( T \). Figure 1 shows a rolling-element contact shearing a fluid film of thickness \( h \). The variable \( P \) is the idealized Hertzian pressure distribution across the contact. Shear stresses \( \tau _s \), which develop because of the difference in surface speeds, affect the heat generation and the tangential forces acting on the rolling elements.

In an actual contact, the shear stress and the shear rate vary across the thickness of the film. It is common practice, however, to treat the problem as if the shear takes place at one plane of the film, with the fluid entrained by disk 1 traveling at surface speed \( U_1 \) and the fluid entrained by disk 2 traveling at surface speed \( U_2 \). Therefore, the relationship of shear stress to shear rate can be characterized by measuring the total traction force as a function of measurable values of sliding speed \( u_s \), or slip, where

\[
u = U_1 - U_2
\]

The entrainment, or rolling, velocity \( V \) of the fluid is taken to be

\[
V = \frac{U_1 + U_2}{2}
\]

Figure 2 shows the typical shape of the curve for traction as a function of sliding speed. Traction force is expressed in terms of a traction coefficient \( \mu \) where

\[
\mu = \frac{\text{traction force}}{\text{normal load}}
\]

Three distinct regions can be identified on this curve. The initial low-slip region of the curve is linear and is thought to be isothermal in nature. At some sliding speed the traction behavior becomes nonlinear, though still increasing. This region is also thought to be isothermal. In the third region, the heat generated by dissipative shearing of the fluid is no longer negligible. This region is characterized by either decreasing traction with further increases in sliding velocity or a flattening of the curve towards a horizontal asymptotic line.

The magnitude of a traction curve at particular conditions can be characterized by the maximum traction coefficient reached on the curve. Again, this is a function of maximum
contact pressure, rolling velocity, and fluid temperature. The maximum traction coefficient is denoted by \( \mu^* \), and the sliding velocity at which \( \mu^* \) occurs is denoted by \( u_s^* \).

**The SHABERTH traction model.**—This discussion applies to the SHABERTH/SKF traction model, not the SHABERTH/NASA model. The differences between the two are discussed in reference 4. The complete SHABERTH/SKF traction model comprises an asperity traction model and a fluid-film traction model. The lubricant traction characteristics are required only for the fluid traction model. SHABERTH calculates \( h/a \), that is, the ratio of film thickness \( h \) to composite surface roughness \( a \). For \( h/a < 0.4 \), traction is modeled as purely asperity contact. For \( h/a > 0.4 \), the traction model is purely lubricant-dependent. For \( 0.4 < h/a < 3.0 \), the model is a combination of the asperity and fluid-film models (ref. 6).

The development of the SHABERTH fluid traction model is explained in reference 5. Since English-system units are used in the reference material, they are used here to describe the model and to fit data to it. Basically, the energy and momentum equations were developed in order to find the governing dimensionless terms. Such terms for heat conduction and convection, slide-to-roll ratio, and the speed-viscosity product \( U = \eta_0 V \alpha/R_v \) are included in these equations. The total thermal effect was assumed to be a multiplicative power function of the individual thermal dimensionless terms, for which the exponents were unknown. Adding a viscoelastic correction to the effective viscosity term produced a relationship between a nondimensional traction coefficient term \( \mu^* \) and a nondimensional sliding-speed term \( \psi_1^{1/2} \). (Further explanation of the nondimensionalization process can be found in ref. 5.) The exponents of the thermal terms were determined by using Johnson and Cameron’s experimental data for a mineral oil, Shell Turbo 33 (ref. 10). The ensuing curve of \( \mu^* \) as a function of \( \psi_1^{1/2} \) is constant over all maximum contact pressures, rolling velocities, and temperatures, for all choices of lubricants; it is the curve to which data for all other lubricant choices for the program are fit. The maximum nondimensional traction coefficient term on the curve is designated by \( \mu^*(1) \). and \( \psi_1^{1/2} \) is the nondimensional sliding-speed term at which \( \mu^* \) occurs. These values which were obtained by using the Johnson-Cameron data, are constant:

\[
\mu^*(1) = 0.235 \quad \text{and} \quad \psi_1^{1/2} = 8.75 \times 10^{-5} \quad (9)
\]

From these values an equation is obtained for the maximum traction coefficient \( \mu^* \) at particular conditions, and for the associated sliding speed \( u_s^* \) as a function of those conditions (ref. 5), as follows:

\[
0.235 = \mu^* (K/\eta_0)^{1/2} (h/b)^{0.28} \left( \frac{h/b}{K/\eta_0} \right)^{0.11} \left( \frac{\eta_0 V \alpha}{R_v} \right)^{0.02}
\]

and

\[
8.75 \times 10^{-5} = \left( \frac{u_s^*}{V} \right) \left( \frac{h/b}{K/\eta_0} \right)^{0.28} \left( \frac{\eta_0 V \alpha}{R_v} \right)^{0.7}
\]

Four other lubricants have been added to the SHABERTH code. They are a polyphenyl ether (SP4E), MIL-L-7808 oil, MIL-L-23699 oil, and a fluorinated polyester (Freon E-1).

**Calculation of the Fluid Traction Parameters for SHABERTH**

In this section, the procedure for finding the fluid traction parameters is described. Thereafter, a discussion of concerns with the model and with the potential difficulties that can be encountered in fitting the data is presented.

There are three basic steps involved in fitting fluid traction data to the SHABERTH fluid traction model: (1) traction data obtained for an elliptical contact must first be transformed into equivalent traction data that would occur over a rectangular contact at the same conditions; (2) the parameters that govern the values of \( \mu^* \) and \( u_s^* \) must be determined from the transformed values of the experimental data; and (3) parameters governing the shape of the curve of \( \mu \) as a function of \( u_s \) are determined from the transformed data.

**Transformation from elliptical- to line-contact data.**—The SHABERTH traction model was developed on the basis of a rectangular, or “line,” contact (ref. 5). When analyzing an elliptical contact, the SHABERTH code divides the contact into discrete rectangular strips, the length of the strips being in the rolling (x) direction as in figure 3. SHABERTH then calculates a traction force for each strip and integrates the traction force over the elliptical contact. Experimental traction data obtained over an elliptical contact must be transformed to the equivalent traction data that would occur over a line contact at the same contact conditions. McCool et al. (ref. 5) developed a method for this transformation.
The pressure distribution over a line contact is assumed to be constant in the rolling direction and to vary semielliptically (as shown in Fig. 1) along the semimajor (y) axis; that is, strip to strip. If the pressure distribution and geometry of the equivalent line contact, and the traction force-pressure relationship are known, the traction force over the contact can be calculated. The traction force-pressure relationship, which varies with rolling velocity, temperature, and sliding velocity, can be found from the experimental elliptical traction data.

The measured total traction force $T_R$ is divided by the length $2a$ of the elliptical contact in the $y$-direction to obtain an average traction force per unit length $T_{tr}$. Then a relationship must be found between $T_R$ and $P_n$; this is possible with the assumption that a polynomial relationship can reasonably model the data for $T_R$ as a function of $P_n$, while remaining easy to integrate analytically. Therefore, a general relationship of the form

$$T_R = d_0 + d_1 P_n + d_2 P_n^2 + d_3 P_n^3 + d_4 P_n^4$$  \hspace{1cm} (12)

where

- $d_0, d_1, d_2, \ldots$ are polynomial coefficients to be determined
- $T_R$ measured traction force
- $P_n$ contact semimajor length
- $a$ contact semimajor length

was integrated over the line contact to obtain an expression for equivalent average traction per unit length, over a line contact, as a function of $P_n$. From this integrated expression and the original polynomial of equation (12), the following relationship between the elliptical-and the line-contact traction coefficients was obtained (it requires only the polynomial coefficients $d_0, d_1, \ldots$, and the maximum Hertzian pressure of the particular elliptical contact):

$$
\frac{\mu_{\text{line}}}{\mu_{\text{elliptical}}} = \left( \frac{4}{3\pi} \right) \frac{G_0 + G_1 P_n + G_2 P_n^2 + G_3 P_n^3 + G_4 P_n^4}{d_0 + d_1 P_n + d_2 P_n^2 + d_3 P_n^3 + d_4 P_n^4} \hspace{1cm} (13)
$$

where

- $G_0 = (\pi/2)d_0$
- $G_1 = 2d_1$
- $G_2 = (3\pi/4)d_2$
- $G_3 = (8/3)d_3$
- $G_4 = (15\pi/16)d_4$

For a particular fluid, at each condition of rolling velocity, temperature, and sliding velocity, the experimental data for average traction force $T_R$ as a function of maximum contact pressure $P_n$ are fit to equation (12) in order to find the polynomial coefficients. These coefficients and the particular contact pressure of interest are substituted into equation (13), whereby equivalent traction coefficient data over a line contact are determined.

Traction parameters governing the maximum traction coefficient and the sliding velocity of maximum traction. The traction parameters needed by SHABERTH to find the values of $\mu^*$ and $u^*$ at particular contact conditions are those dealing with the viscoelastic relationship and some proportionality constants.

The viscoelastic relationship defines an effective fluid viscosity $\eta_e$ at contact conditions, as a function of ambient fluid viscosity $\eta_0$, contact pressure $P_n$, and fluid entrainment velocity $V$. The viscoelastic model in SHABERTH is of the form

$$\eta_e = \eta_0 f(P_n) \left( \frac{V}{V_0} \right)^{-\lambda_0} \hspace{1cm} (14)$$

where $f(P_n)$ and $(V/V_0)^{-\lambda_0}$ are viscoelastic corrections for the pressure and the entrainment velocity, respectively. The viscoelastic parameters that must be found for each new lubricant are $f(P_n)$ and $\lambda_0$.

The exponent $\lambda_0$ is obtained by fitting the experimental data for $\mu^*$ as a function of $V$ at constant temperature and pressure, to a relationship of the form

$$\mu^* = C_m V^{\gamma_3} \hspace{1cm} (15)$$

where $C_m$ is a constant of proportionality and by defining $\gamma_3$ as

$$\gamma_3 = a_3 + 0.5\lambda_0(a_1 + a_2) - \lambda_0 - c_1 + n_2(a_2 - 1) + 0.5a_2 \hspace{1cm} (16)$$
where
\[ a_1 = 0.236 \]
\[ a_2 = 0.55 \]
\[ a_3 = 0.22 \]
\[ c_1 = 0.022 \]

The coefficients \( a_1, a_2, a_3, c_1 \) were developed from the Johnson-Cameron data. The term \( n_1 \) is the exponent of the rolling speed from the film thickness relationship. With a value of \( n_1 = 0.7 \) taken for a typical unstarved contact, the equation reduces to
\[ \lambda_0 = \frac{0.165 - \gamma_3}{0.607} \quad (17) \]

The function \( f(P_o) \) is found by using equation (10) and the experimental contact conditions and traction data to calculate values of \( \eta_r \) as a function of \( P_o \). From the viscoelastic relationship,
\[ f(P_o) = \left( \frac{\eta_r}{\eta_0} \right) \left( \frac{V}{V_0} \right)^{\lambda_0} \quad (14) \]

\( f(P_o) \) can be found as a function of \( P_o \) since \( \lambda_0 \) has been calculated previously. The constant \( V_0 \) will be discussed shortly.

The SHABERTH model for \( f(P_o) \) was developed from the Johnson-Cameron data. Figure 4 shows the relationship obtained from these data plotted on log-log coordinates. This figure shows not only that the relationship is exponential but also that the value of the exponent changes at a certain pressure. Therefore, the relationship is modeled as a function of the form
\[ f(P_o) = C_n \left( \frac{P_o}{P_1} \right)^{A_1} \quad (18) \]

where
\[ A_1 = A_1, \text{ for } P_o < P_1 \]
\[ A_1 = A_2, \text{ for } P_o \geq P_1 \]

and \( A_1, P_1, \) and \( C_n \) are lubricant-dependent constants.

The value of \( P_1 \) is chosen as the pressure (in lb/in^2 \times 10^{-5}) at which the slope of the log-log plot of \( f(P_o) \) as a function of \( P_o \) changes. The value of \( A_1 \) is chosen from the best-fit value of the exponent \( A \) over all conditions prior to \( P_1 \), and \( A_1 \) is the best-fit exponent at pressures greater than or equal to \( P_1 \). The value of \( C_n \) need not be determined from this data fit because it is combined with other constants to form general proportionality constants \( C_1 \) and \( C_2 \), which are determined after all of the specific parameters are found.

By substituting the viscoelastic relationship into equations (10) and (11) and by grouping the fluid property constants into general proportionality constants, the following equations, relating \( \mu^* \) and \( u^*_r \) to \( P_o, V, \eta_0, \) and \( h \), are obtained:
\[ \mu^* = (C_1)P_o^{-0.14} \left( \frac{P_o}{P_1} \right)^{0.61A_1} \eta_0^{-0.59}V^{0.48-0.61A_1} \eta^{-0.45} \quad (19) \]

and
\[ u^*_r = (C_2)P_o^{-0.14} \left( \frac{P_o}{P_1} \right)^{-0.44A_1} \eta_0^{-1.1}V^{0.44A_1-0.09} \eta^{-0.85} \quad (20) \]

where
\[ A_1 = A_1, \text{ for } P_o < P_1 \]
\[ A_1 = A_2, \text{ for } P_o \geq P_1 \]

By substituting experimental values of \( \mu^* \) and \( u^*_r \), at the specific test conditions, into equations (19) and (20), best-fit values of \( C_1 \) and \( C_2 \) can be determined. These equations are used in the SHABERTH code, along with lubricant-specific values of \( \lambda_0, P_1, A_1, A_2, C_1, \) and \( C_2 \), to predict values of \( \mu^* \) and \( u^*_r \).

The constant \( V_0 \), which serves as a rolling velocity normalization factor, is not a required parameter in the SHABERTH code. It is used only when a relationship between \( f(P_o) \) and...
$P_o$ is fitted by using equation (14). For each of the oils discussed in reference 5, the value chosen for $V_0$ was that of the lowest rolling velocity condition in the particular test matrix. However, for the model of $f(P_o)$ shown in equation (18) (an exponential relationship), the value of $V_0$ has no effect on the relevant parameters that are being determined (i.e., the values of $A_1$, $A_2$, and $P_1$); its only effect is to shift the curve of $\log[f(P_o)]$ as a function of $\log[P_o]$ by a constant factor. The values of the proportionality constants $C_1$ and $C_2$ are determined from equations (19) and (20), which do not include the constant $V_0$.

**Modeling the shape of the traction curve.**—Once the theoretical value of $\mu^*$ has been determined by SHABERTH for certain contact conditions, the shape of the curve of the traction coefficient as a function of sliding velocity is needed to determine $\mu$ at a particular sliding velocity. Experimentally derived traction curves are of two basic types (see fig. 5). For both types, $\mu$ increases linearly at low sliding speeds and then becomes nonlinear, increasing at a slower rate. The curve shown in figure 5(a) reaches the value of $\mu^*$ and then slowly decreases with increasing sliding speed. The curve shown in figure 5(b) increases continuously to an asymptotic value of $\mu^*$. SHABERTH uses the continuously increasing, asymptotic model; the other model created convergence problems in the program.

Values must be found for the coordinates where the linearly increasing portion of the asymptotic curve ends. These values are dependent on the contact conditions. However, the experimental data for all contact conditions falls on a single curve of $(\mu/\mu^*)$ as a function of $(u_s/u_s^*)$. Therefore, SHABERTH models the shape of the traction curve on the basis of one set of coordinates, $(X_B, Y_B)$, where the linear portion of the experimental curve of $(\mu/\mu^*)$ as a function of $(u_s/u_s^*)$ ends (see fig. 6). The SHABERTH code then calculates values of $\mu$ using

$$\frac{\mu}{\mu^*} = \left(\frac{Y_B}{X_B}\right) \left(\frac{u_s}{u_s^*}\right) \quad 0 \leq \frac{u_s}{u_s^*} \leq X_B$$

and

$$\frac{\mu}{\mu^*} = Y_B \left(1 + \frac{X_D Y_B}{Y_D X_B + Y_B X_D}\right) \quad \frac{u_s}{u_s^*} > X_B$$

where

$$Y_D \text{ and } Y_B$$

and $X_D (u_s/u_s^*) = X_B$.

### Issues Concerning the SHABERTH Fluid Traction Model

Issues relevant to the SHABERTH fluid traction model and the problems that can arise during the fitting of the experimental traction data and the extraction of the parameters are discussed.

**Transformation from elliptical- to line-contact data.**—Care must be taken when fitting a polynomial to the elliptical-contact data of $T_R$ as a function of $P_o$. As previously discussed, the resulting polynomial models the relationship between $T_R$ and $P$ as it varies over a rectangular (line) contact. Equation (13) was developed by integrating a general form of the polynomial across incremental strips of a line-contact area for which the pressure is $P_o$ at the center strip and decreases semielliptically toward the edge of the contact in the y-direction. Therefore the polynomial for each set of contact conditions must be valid down to pressures below $P_o$.

Figure 7 shows a possible example of a polynomial fit to experimental data. The points $A$, $B$, $C$, and $D$ represent
such that geometric relationship to the data of pressures still well within the contact ellipse has a profound as shown in figure 7. The erroneous increase of for these cases were examined, they exhibited behavior such as shown in figure 7. The erroneous increase of $T_R$ at pressures still well within the contact ellipse has a profound effect on the resulting $\mu_{\text{line}}/\mu_{\text{elliptical}}$ values.

A method was found to solve this problem. First, fit a geometric relationship to the data of $T_R$ as a function of $P_\nu$ such that

$$T_R = b_1(P_\nu^{b_2})$$

(22)

where $b_1$ and $b_2$ are coefficients of the geometric fit.

An advantage of this relationship is that $T_R$ goes to zero as $P_\nu$ goes to zero, which is in keeping with physical reality. By using equation (22), values of $T_R$ at pressures below the lowest test matrix $P_\nu$ were predicted. Then the original and predicted data for $T_R$ as a function of $P_\nu$ were used together to fit a polynomial of the form of equation (12). The resulting set of polynomial coefficients ($a_{01}$, etc.) were used in equation (13) to obtain final values of $\mu_{\text{line}}/\mu_{\text{elliptical}}$. For 5P4E the results of this method were in good agreement with the original transformed line-contact data listed in reference 5 for all conditions. Another method was also tried, using an exponential relationship of the form $T_R = b_1(P_\nu^{b_2})$ in place of equation (22), but these results did not agree as well with the original 5P4E data. Therefore, the method that uses equation (22) is recommended.

**Viscoelastic parameters.**—The model of $f(P_\nu)$ as a function of $P_\nu$ shown in equation (18) was developed from experimental data that exhibited a change in the value of $A_i$ at a pressure $P_i$ within the experimental test matrix; it is embedded in the final traction equations used in the SHABERTH code. Therefore, values for $A_1$, $A_2$, and $P_i$ must be obtained for each new lubricant.

However, it is not clear what procedure should be used to determine values for $P_i$ and $A_2$ when they do not occur within the pressure range over which the experimental data were taken. The $f(P_\nu)$ data shown in reference 5 for the 5P4E and the MIL-L-7808 oils indicate that in neither case is there a change in the value of $A_i$ at any place in the experimental pressure range. However, values of $P_i$ and $A_2$ were selected.

On the basis of the behavior of other fluids under high pressure (refs. 10 and 11), it is reasonable to assume that there is a pressure $P_i$ at which the value of the exponent $A_i$ decreases from $A_1$ to some $A_2$. The data in reference 11 show that the pressure-viscosity coefficient $\alpha$, normally associated with the simple power law $\eta = \eta_0 P^{-\alpha}$, decreases to $\beta' < \alpha$ at some pressure. The pressure-viscosity model of equation (18) is somewhat different than this one, but since equation (18) is still a power law, it would also be expected to exhibit a decrease in the value of the exponent $A_i$ at some pressure.

It is impossible to know the exact value of $P_i$ without experimental data. A value should be chosen that gives some weight to the experimentally derived value of $A_i$; that is, a value which extends, somewhat, the range at which $A_i$ is valid beyond the highest pressure in the test matrix. However, the value chosen for $P_i$ should not be too much higher than the experimental range, since the error due to using $A_i$ at pressures where the actual behavior follows $A_2$ has exponential effects on the predicted values of viscosity. For the 5P4E and the MIL-L-7808 oils respectively, values of

---

**Figure 7.**—Example of a polynomial fit through four points representing experimental data.
$P_1$ were chosen that were 14 and 20 percent greater than the highest experimental contact pressure. This seems reasonable. The only data available on which to base a choice of the value of $A_1$ are those of Johnson and Cameron for Shell Turbo 33. The most reasonable recourse seems to be to choose a value of $A_2/A_1$ based on $A_2/A_1$ for Shell Turbo 33 and then find $A_1$ from the value of $A_1$ for the particular fluid. For Shell Turbo 33, $A_2/A_1 = 0.635$.

In choosing a value of $A_2/A_1$ for other fluids, a more conservative prediction of viscosity is obtained by erring on the low side of the actual $A_2$ than by erring by the same amount on the high side, because of the exponential effect. Therefore, a value of less than 0.635 is recommended for $A_2/A_1$.

For the other original lubricants in the SHABERTH code, the following $A_2/A_1$ values were used: 5P4E, 0.456; MIL-L-7808, 0.363; and MIL-L-23699, 0.5.

**Final fluid traction equations.**—Equations (19) and (20) show the final equations used by the SHABERTH code to predict $\mu^*$ and $u^*$ as functions of $P_o$, $\eta_i$, $V$, and $h$. However, a slight error has been detected in these formulas. In the original traction equations developed by McCool, et al. (ref. 5)

$$\mu^* = C_n P_o^{-1} b^{-0.28} h^{-0.45}$$

where

$C_n$ proportionality constant

$b = 2\pi R_1 (P_o)/(E')$

$h = C_g (\alpha \eta_i V)^{0.7} P_o^{-0.3}$ for typical unstarved contact

Substituting the expression for $b$ into equation (23) gives the relation

$$\mu^* = C_n P_o^{1.28} h^{-0.45}$$

The $-1.28$ value of the $P_o$ exponent is that value for which $h$ is still a separate variable in the equation. To find the total relationship between $\mu^*$ and $P_o$, the film thickness term $h$ was broken up to give

$$\mu^* = C_n P_o^{1.14}$$

Here, the $-1.14$ value of the $P_o$ exponent is that for which $h$ is no longer a variable in the equation.

In equations (19) and (20), however, $h$ has been reintroduced as a variable. The exponents associated with $\eta_i$ and $V$ are the appropriate ones since the film thickness term includes contributions of $\eta_i$ and $V$. The exponent of $P_o$, on the other hand, has been left as $-1.14$.

The corrected equations should read

$$\mu^* = (C_1) P_o^{-0.128} \left( \frac{P_o}{P_1} \right)^{0.14} \eta_0^{0.58} V^{0.48} h^{0.45}$$

and

$$u^* = (C_2) P_o^{-0.28} \left( \frac{P_o}{P_1} \right)^{-0.14} \eta_0^{-1.14} V^{0.48} h^{-0.45}$$

where

$A_1 = A_1$, for $P_o < P_1$

$A_1 = A_2$, for $P_o \geq P_1$

The exponent of $P_o$ cannot be easily changed in the program for the following reason: once $A_1$, $A_2$, $\lambda_0$, and $P_1$ have been determined from equations (17) and (18), the traction data are used to determine the values of $C_1$ and $C_2$ for each lubricant. The hard-coded values of $C_1$ and $C_2$ for the existing choices were calculated by using $P_o^{1.14}$. Without the original traction data for these lubricants, the values of $C_1$ and $C_2$ associated with $P_o^{-1.28}$ cannot be calculated. The difference in traction prediction between the two sets of equations for the RP-1 data at the experimental conditions will be shown to be negligible.

**Development of the SHABERTH Fluid Traction Parameters for RP-1**

In this section, the experimental traction data for RP-1, a modified model of the pressure-viscosity coefficient for RP-1, and the fitting of the data to the SHABERTH fluid traction model are discussed.

**Experimental Traction Data for RP-1**

After a description of the RP-1 traction test matrix, the effect of transforming the experimental elliptical-contact traction data to equivalent line-contact traction data is shown. General trends of the transformed RP-1 data are also presented.

**Test matrix conditions.**—A twin disk tester generated data for traction force as a function of sliding speed for RP-1 fuel. An elliptical contact under various conditions of Hertzian pressure, rolling speed, and temperature (ref. 8) was used. The transverse radius of curvature of the lower disk was infinity: the upper disk was a toroid, the curvature of which produced the desired contact geometry. The traction data were generated with side slip, which can be produced by skewing the toroid about the normal to the horizontal plane. The slide-to-roll ratio $u/V$ can be controlled and measured via the skew angle. The test matrix is listed in table 1. Figure 8 shows a typical set of curves for experimental traction coefficient $\mu$ as a function of $u/V$ for elliptical contact. This particular set of curves shows the variation of traction with rolling velocity at one condition of pressure and temperature. In general, traction decreases with increasing rolling velocity, increases with increasing pressure, and decreases with increasing temperature.
TABLE I. TARGET TEST MATRIX CONDITIONS

<table>
<thead>
<tr>
<th>Hertzian pressure, GPa (kpsi)</th>
<th>1.01 (147)</th>
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<tr>
<td></td>
<td>1.27 (185)</td>
</tr>
<tr>
<td></td>
<td>1.60 (233)</td>
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<tr>
<td></td>
<td>1.92 (279)</td>
</tr>
<tr>
<td>Rolling velocity, m/sec (in./sec)</td>
<td>10 (390)</td>
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<td></td>
<td>30 (1200)</td>
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<td></td>
<td>50 (2000)</td>
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<td>Temperature, °C (°F)</td>
<td>40 (104)</td>
</tr>
<tr>
<td></td>
<td>65 (149)</td>
</tr>
</tbody>
</table>

*All parameters were tested.*

Figure 8.—Experimental traction coefficient as a function of slide-to-roll ratio for RP-1 at varying values of rolling velocity. Contact pressure, 279 kpsi; temperature, 111 °F.

The conditions shown in table I represent the maximum capabilities of the test rig. The upper limits extend above those of the original lubricants. For example, the Johnson-Cameron data had the highest Hertzian pressure condition at 225 000 psi ($V_{max} = 1000$ in./sec), and the MIL-L-7808 data included the highest rolling speed at 1820 in./sec ($P_{max} = 150 000$ psi). Values of Hertzian stress greater than the maximum in the RP-1 matrix would result in $h/\sigma$ values that would trigger the asperity-contact-only traction model. Therefore, the test matrix shown in table I is quite adequate for the purpose of modeling the traction behavior of RP-1.

Transformation from elliptical-to line-contact data.—The RP-1 data were transformed from elliptical-to line-contact data by the method previously described. Since there were only four conditions of pressure in the fit, second-order polynomials were used. Figure 9 shows a comparison of the RP-1 curve of $\mu$ as a function of $u_*/V$ for elliptical contact to that for the equivalent transformed line contact for RP-1 at one set of conditions. The elliptical-and line-contact curves at other conditions compare similarly. The equivalent line-contact data always exceed the elliptical-contact data, the greatest amount of difference being in the nonlinear region of low $u_*/V$. The line-to-elliptical ratio then decreases at increasing $u_*/V$. Also, the value of $u_*$, the sliding velocity at which $\mu^*$ occurs, tends to be lower for the line-contact data than for the elliptical data. The behavior of the transformed data is typical of that for other oils.

General trends of the RP-1 data.—Figure 10 shows a plot of $\mu^*/\mu^*$ as a function of $u_*/u_*$ for RP-1 for all conditions in the test matrix. Since the SHABERTH model of the traction curve is based on the assumption that $\mu^*/\mu^*$ is a function of $u_*/u_*$ only, it is desirable for the experimental data for $\mu^*/\mu^*$ as a function of $u_*/u_*$ to fall on one curve. In figure 10 the RP-1 data all follow the same general shape, though some scatter is present. The scatter is not deemed large enough to prohibit the use of the SHABERTH traction model.

Figure 11 shows the effect of maximum contact pressure on the values of $\mu^*$ and $u_*$ for RP-1 at one condition of rolling velocity and fluid temperature. The behavior shown is typical over the range of conditions. The value of $\mu^*$ increases with increasing contact pressure, and the value of $u_*$ decreases. In figure 12, the effect of rolling velocity on the values of $\mu^*$ and $u_*$ for RP-1 is shown at one condition of contact pressure and temperature. Again, the behavior shown is typical over the range of conditions. The value of $\mu^*$ decreases with increasing rolling velocity, and the value of $u_*$ increases.

Pressure-Viscosity Coefficient for RP-1

The SHABERTH code calculates a pressure-viscosity value as a function of temperature and lubricant ambient kinematic viscosity by using an expression developed by Fresco (ref. 6). This semiempirical model was developed by using data for fluids other than RP-1, and it accounts for different lubricant types only in the value of the viscosity. The coefficients used in the calculation are constant for all lubricant types. This model was not used in the analysis of the RP-1 data.
Figure 10.—RP-1 experimental data for $\mu/\mu^*$ as a function of $u_s/u_s^*$ for all test matrix conditions of maximum contact pressure, rolling velocity, and fluid temperature.

Figure 11.—Variation of RP-1 experimental maximum traction coefficient and associated sliding velocity with maximum contact pressure. Velocity, 2000 in./sec; temperature, 104 °F.

Figure 12.—Variation of RP-1 experimental maximum traction coefficient and associated sliding velocity with rolling velocity. Pressure, 233 kpsi; temperature, 104 °F.
As part of the effort to measure and analyze the traction data for RP-1, pressure-viscosity data generated by Bridgman for kerosene were obtained (ref. 12). The traction data specific to RP-1 were also used to check the validity of Bridgman's pressure-viscosity data for use with RP-1. By using the Barus pressure-viscosity relationship, that is,

\[ \eta_p = \eta \theta \exp \left[ \left( \frac{B_1}{(\theta + D_p)} \right) P \right] \]  

(28)

where

\[ \eta \theta \] ambient absolute viscosity at inlet temperature, Pa-sec
\[ \theta \] inlet temperature, °C
\[ D_p \] lubricant-dependent pressure solidification temperature, °C
\[ B_1 \] lubricant-dependent constant, °C/Pa
\[ P \] pressure, Pa

and the reference 8 experimental data, the constants \( B_1 \) and \( D_p \) were determined for RP-1 as \( B_1 = 544 \) °C/Pa and \( D_p = 25.6 \) °C (ref. 8). This was the pressure-viscosity calculation used in fitting the RP-1 traction data to the SHABERTH traction model.

The pressure-viscosity coefficient \( \alpha \), which is used by SHABERTH, can be calculated from the Barus model by using

\[ \alpha = \frac{B_1}{\theta + D_p} \]  

(29)

and converting from units of Pascals \(^{-1}\) to square inches per pound.

Figure 13 shows the RP-1 pressure-viscosity coefficient as a function of temperature for both the Fresco and Barus models. The Fresco model predicts a nearly linear relationship between the pressure-viscosity coefficient and temperature, whereas the Barus model predicts a hyperbolic relationship. The difference between the two models' pressure-viscosity values was deemed significant enough to justify changing the SHABERTH code so that it would branch to equation (29) (with the appropriate values of \( B_1 \) and \( D_p \)) instead of using the Fresco model when the lubricant is RP-1.

**Fluid Traction Parameters**

The final values of the SHABERTH fluid traction parameters obtained by fitting the RP-1 traction data to the previously discussed models are listed in appendix A. Also specified are other changes that need to be made to the SHABERTH code to run it with RP-1 as the lubricant choice.

Viscoelastic parameters. —The value of \( \lambda_0 \) was determined from equation (17) after a best-fit value of \( \gamma_3 \) was found. This value was obtained by varying \( \gamma_3 \) from its lowest to highest experimentally derived value, while comparing the predicted \( \mu \) to the transformed experimental \( \mu \) over all conditions, and choosing the \( \gamma_3 \) that gave the lowest average percent error over the pressure and temperature range. The resulting value was \( \gamma_3_{\text{final}} = 0.733 \), which gives \( \gamma_0_{\text{final}} = 0.28 \). The function \( f(P_o) \) was calculated from equations (10) and (14) by using \( \lambda_0 = 0.733 \) and \( V_o = 390 \) in./sec. The relationship between \( f(P_o) \) and \( P_o \) is shown in figure 14 at a particular rolling velocity and temperature: this behavior is typical at all conditions. No change in slope occurs in the plot of \( \log[f(P_o)] \) with respect to \( \log[P_o] \), thereby indicating that the expected decrease in the exponent \( A_1 \) does not occur within the experimental range of maximum contact pressure. This is true at all conditions of speed and temperature in the matrix. However, based on the behavior of other fluids under high pressures (refs. 10 and 11), an assumption can be made that for RP-1, there is a \( P_o \) at which the value of the exponent \( A_1 \) decreases from \( A_1 \) to \( A_2 \). Since \( P_o \) cannot be determined from the present experimental data, the value of \( A_1 \), which was obtained from experimental data, will be assumed to be valid up to a pressure 20 percent higher than the highest maximum contact pressure in the test matrix. This choice gives some weight to the experimentally derived data, while providing a safety value against predicting unreasonably large values for viscosity. Therefore, \( P_o = 340 \) 000 psi.

In order to model \( f(P_o) \) as a function of \( P_o \), the data for \( f(P_o) \) with respect to \( P_o \) for all conditions of rolling velocity and fluid temperature should fall on the same curve. Figure 15 shows the variation of \( f(P_o) \) with \( P_o \), for all of the conditions and shows the best-fit line. Note that a considerable amount of scatter exists.

Figure 16 again shows the variation of \( f(P_o) \) with \( P_o \) for all conditions, but the data sets taken at the two fluid
Maximum contact pressure, \( P_o \), psi

Figure 14. — Variation of viscoelastic function with maximum contact pressure for RP-1. Velocity, 1970 m/sec; temperature, 110 °F.

Figure 15. — Variation of viscoelastic function with maximum contact pressure for RP-1 at all test matrix conditions.

Figure 16. — Data and best-fit lines showing variation of viscoelastic function with maximum contact pressure for RP-1 at two temperatures.

Temperatures are plotted separately and the best-fit line is drawn through each. From this figure, it is apparent that temperature has an effect on the relationship. The value of \( A_1 \) remained constant at both temperatures; only \( C_n \) is a function of temperature. Therefore, \( A_1 \) can be calculated without regard to the effect of temperature. The best-fit value obtained for \( A_1 \) was 3.23.

The value of \( A_2 \) cannot be determined directly from the experimental data since it occurs outside of the test matrix. The best alternative is to choose a value for \( A_2/A_1 \) based on the behavior of other fluids and determine \( A_2 \) from the value of \( A_1 \) for RP-1. The only fluid data in the SHABERTH reference material showing a decrease in \( A_i \) within the experimental test matrix are those for Shell Turbo 33, obtained by Johnson and Cameron (ref. 10). Their data give \((A_2/A_1)_{	ext{Shell Turbo 33}} = 0.635\).

For the same reasons stated in the section Issues Concerning the SHABERTH Fluid Traction Model, \( A_2/A_1 \) for RP-1 was chosen as a lower value than that for Shell Turbo 33. For convenience, the value chosen was \((A_2/A_1)_{\text{RP-1}} = 0.5\), giving \( A_2 = 1.6\).

An additional point can be made here concerning the RP-1 parameters. The particular value chosen for \( A_2 \) is not of critical importance to the traction prediction for RP-1. The range of pressures in which \( A_1 \) is valid should cover all cases in which the fluid traction plays a significant role. At higher contact pressures, the traction force prediction is governed
predominantly by the dry asperity traction model. However, a value for $A_2$ should be coded in case it is required.

There is currently no mechanism in the SHABERTH program to handle a temperature-dependent $f/P_o$. Because there were only two conditions of temperature in the RP-1 experimental matrix, this study describes the error involved in ignoring the temperature dependency, but it does not develop a temperature-dependent algorithm.

**Proportionality constants.**—The temperature-dependent constant $C_n$ in equation (18) is contained in the general proportionality constants $C_1$ and $C_2$, which must be found by fitting the transformed experimental RP-1 $\mu^*$ and $u_*^r$ data to equations (19) and (20), once the viscoelastic parameters have been determined. Therefore, $C_1$ and $C_2$ reflect the temperature dependency encountered in the $f/P_o$ data. The values chosen for these constants are the average of the best-fit values obtained at each temperature. The error resulting from the temperature-averaged values of $C_1$ and $C_2$ will be quantified in the section Results and Comparisons by comparing the traction predicted by using them to the traction predicted by using the values of $C_1$ and $C_2$ obtained at each temperature.

The values of $C_1$ and $C_2$ are also affected by the potential correction to equations (19) and (20), which led to equations (26) and (27). Therefore, in the Results and Comparisons section, the correction to the exponent of $P_o$ will be shown to have a negligible effect on the resulting value of $\mu^*$. Equations (19) and (20) are used in all subsequent calculations to determine values of $C_1$ and $C_2$. The values ultimately chosen for use in the SHABERTH code were the temperature-averaged values found by using the uncorrected equations (19) and (20); that is, $C_1 = 113.450$ and $C_2 = 24.65$.

Table II lists the values of $C_1$ and $C_2$ found for the various cases described above, that is, the temperature-averaged and temperature-dependent values needed for the uncorrected equations (19) and (20) and the corrected equations (26) and (27).

**Traction curve shape parameters.**—As stated previously, the traction curve predicted by SHABERTH follows a fixed mathematical function, increasing linearly at low sliding speeds and then asymptotically approaching the value of $\mu^*$. Values of $X_B$ and $Y_B$ obtained from the nondimensionalized curve of $\mu/\mu^*$ as a function of $u_*/u_*^r$ are used to calculate $\mu$ as a function of $u_*$ from equation (21), once $\mu^*$ and $u_*^r$ are known. The values of $X_B$ and $Y_B$ that were found from the RP-1 data were 0.15 and 0.65 respectively.

### Results and Comparisons

In this section the effect of the correction to the exponent of $P_o$ in equations (19) and (20) will be shown to be negligible. The term “experimental data” will be used to mean the equivalent line-contact data that was transformed from the experimental elliptical data. Figure 17 shows a comparison of curves of $\mu$ as a function of $u_*/V$. These curves were generated by the SHABERTH model at test matrix conditions, using the corrected ((19) and (20)) and uncorrected ((26) and (27)) equations with the appropriate values of $C_1$ and $C_2$ for each. For reference, the experimental curve at the same conditions is also shown. For both SHABERTH curves, the effect of temperature on $f/P_o$ has been neglected (i.e., $C_1$ and $C_2$ are temperature-averaged values). The value of the maximum traction coefficient of the corrected curve exceeds that of the uncorrected curve by 5 percent. Over the range of conditions, the maximum difference in the two predicted values of $\mu^*$ was 5 percent, with an average difference of 3 percent. The percentages for maximum and average differences in the values of $u_*^r$ were comparable to those of $\mu^*$.

In figure 18, which shows corrected and uncorrected curves at an extrapolated condition of pressure (330 kpsi) and rolling velocity (3937 in./sec), the curves differ by 6 percent.

As was stated previously, the values of the proportionality constants $C_1$ and $C_2$ that were hard-coded for the original lubricants would need to be recalculated by using the original traction data if equations (26) and (27) were to be substituted for equations (19) and (20). However, for a 1- to 5-percent difference in the value of $\mu^*$, recalculation does not seem worth the effort.

Neglecting the temperature dependency of $C_1$ and $C_2$, though, has a greater effect on the results. Figures 19 and 20 compare experimental traction curves at various conditions, not only to those predicted by using temperature-averaged values of $C_1$ and $C_2$ but also to those predicted by using temperature-dependent values of $C_1$ and $C_2$.

The curves in figure 19 are all at the lower temperature condition (104 °F). In all cases the temperature-dependent curves predict the value of $\mu^*$ quite well. The errors between the experimental values of $\mu^*$ and those predicted by using temperature-dependent $C_1$ and $C_2$ are, respectively, 2.6, 0.6, 0.3, and 1.2 percent for the four cases shown. Over the range

<table>
<thead>
<tr>
<th>Equations used</th>
<th>Temperature-averaged values</th>
<th>Temperature-dependent values</th>
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</thead>
<tbody>
<tr>
<td></td>
<td>$C_1$</td>
<td>$C_2$</td>
</tr>
<tr>
<td>(19) and (20)</td>
<td>113.450</td>
<td>24.65</td>
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<td>(26) and (27)</td>
<td>629.519</td>
<td>136.40</td>
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</table>

### Table II.—Values of $C_1$ and $C_2$ for Various Cases
Figure 17.—Comparison of SHABERTH predictions for RP-1 using uncorrected and corrected traction equations. Contact pressure, 147 kpsi; velocity, 1181 m/sec; temperature, 95 °F. (Transformed experimental data shown for reference.)
Figure 18.—Comparison of SHABERTH predictions for RP-1 using uncorrected and corrected traction equations at extrapolated conditions. Contact pressure, 330 kpsi; velocity, 3937 in./sec; temperature, 104 °F.
The SHABERTH model with temperature-averaged coefficients

SHABERTH model with temperature-dependent coefficients

(a) Low maximum contact pressure: \( P_m, 147 \text{ kpsi} \) (velocity: 1953 in./sec).
(b) High maximum contact pressure: \( P_m, 279 \text{ kpsi} \) (velocity: 1969 in./sec).
(c) Low rolling velocity: \( V_r, 445 \text{ in./sec} \) \( (P_m, 185 \text{ kpsi}) \).  
(d) High rolling velocity: \( V_r, 1969 \text{ in./sec} \) \( (P_m, 185 \text{ kpsi}) \).

Figure 19.—Traction coefficient of RP-1 as a function of slide-to-roll ratio at 104 °F—comparison of curves from transformed experimental data with those from SHABERTH predictions using temperature-averaged and temperature-dependent coefficients.
of conditions at the lower temperature, the average error was 3.4 percent and the highest error, 8.2 percent. Since the value of \( \mu^* \) decreases with increases in temperature, the use of the temperature-averaged values of \( C_1 \) and \( C_2 \) underpredicts the experimental values at the lower temperature. In the cases shown, the values of \( \mu^* \) from using temperature-averaged \( C_1 \) and \( C_2 \) differ from the experimental ones by 8.2, 9.9, 10.0, and 9.3 percent respectively. The average error in \( \mu^* \) over the range of conditions at the lower temperature was 10.3 percent, and the highest error was 17.9 percent.

Figure 19 also shows that the accuracy with which the shape of the traction curve is predicted varies with contact pressure and rolling velocity. As a result of SHABERTH's asymptotically increasing model of the traction curve, any thermal dissipation effects, that is, decreasing traction at high \( u_s/V \), are completely neglected. Of greater importance, however, is the prediction of the low \( u_s/V \) region, since ball sliding in a bearing occurs predominantly at low \( u_s/V \).

Parts (a) and (b) of figure 19 show curves at conditions of different maximum contact pressures, but of the same rolling velocity. At low contact pressure (fig. 19(a)) the effect of thermal dissipation is small, and the predicted temperature-dependent curve agrees well with the experimental one at high \( u_s/V \). At low \( u_s/V \), however, the SHABERTH curve both overpredicts the initial slope and remains linear up to a higher \( u_s/V \) than does the experimental curve. At high contact pressure (fig. 19(b)) the thermal effect at high \( u_s/V \) is much more pronounced and, thus, not well predicted by SHABERTH. However, the initial portion of the curve is better predicted at the higher contact pressure, almost exactly matching the shape of the experimental curve up to 0.015 \( u_s/V \).

**Figure 20.**—Traction coefficient of RP-1 as a function of slide-to-roll ratio at 149 °F. Comparison of curves from transformed experimental data with those from SHABERTH predictions using temperature-averaged and temperature-dependent coefficients.

- (a) High maximum contact pressure, high rolling velocity: \( P_c \), 279 kpsi; \( V \), 1953 in./sec.
- (b) Low maximum contact pressure: \( P_c \), 185 kpsi (velocity, 1969 in./sec).
- (c) Low rolling velocity: \( V \), 1200 in./sec (\( P_c \), 279 kpsi).

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1. **SHABERTH model with temperature-averaged coefficients.**
2. **SHABERTH model with temperature-dependent coefficients.**
3. **Transformed experimental data.**

![Graph](image-url)
Parts (c) and (d) of figure 19 show the effect of rolling velocity on the shape of the curve at the same contact pressure. At low rolling velocity (fig. 19(c)) the high $u/V$ region is well predicted because of the absence of significant thermal effects, but the initial slope is underpredicted. Also, the predicted curve remains linear up to a higher $u/V$ than does the experimental curve. The high rolling velocity curves in figure 17(d) show that the thermal effect increases with rolling velocity, thereby causing greater discrepancies at high $u/V$. The initial portion of the curve is, however, very well predicted, accurately matching the shape of the curve up to 0.06 $u/V$.

The results at the higher temperature (149 °F) were very similar (see fig. 20). Again, the values of $\mu^*$ obtained by using temperature-dependent $C_1$ and $C_2$ show good agreement with the experimental ones. For the conditions shown in figure 20 parts (a) to (c), the temperature-dependent prediction of $\mu^*$ differs from the experimental prediction by 5.9, 1.5, and 3.9 percent respectively. The average error over the range of conditions at this temperature was 4.1 percent, and the highest error, 9.8 percent. The values of $\mu^*$ determined by using temperature-averaged values of $C_1$ and $C_2$ overpredicted the experimental $\mu^*$ by 21.1, 12.2, and 9.9 percent in figure 20 parts (a) to (c), respectively. The average error was 14.4 percent and the highest, 25.3 percent.

The same trends in ability to predict the shape of the traction curve are seen at the higher temperature as at the lower. Figure 20(a) shows curves at a condition of high contact pressure and high rolling velocity. The initial portion of the curve is very well predicted up to 0.03 $u/V$, whereas the high $u/V$ region is not well predicted because of thermal dissipation effects. At a lower contact pressure and the same rolling velocity (fig 19(b)), the high $u/V$ region is well predicted, but the predicted curve at low $u/V$ remains linear up to a higher $u/V$ ratio than does the experimental one. Figure 20(c) shows curves at the same contact pressure as in figure 20(a) but at a lower rolling velocity. As in the low-temperature case, the initial slope of the curve is underpredicted. There is still a significant thermal effect in this experimental curve because of the high contact pressure.

In general, the error from using temperature-averaged values of $C_1$ and $C_2$ runs approximately 10 percent higher than that from using the discrete, temperature-dependent values. The traction model for RP-1 does very well (1) at predicting the shape of the low $u/V$ region of the traction curve at conditions of high maximum contact pressure and high rolling velocity and (2) at predicting the shape of the high $u/V$ region at conditions in which thermal dissipation does not play a significant role (i.e., low maximum contact pressures and low rolling velocities). At conditions of low contact pressure or low rolling velocity, the initial slope of the traction curve is not well predicted, and the predicted curves remain linear up to higher $u/V$ values than do the experimental curves.

Concluding Remarks

An effort is underway both to provide data on and to develop a bearing design methodology for Rocket Propellant I (RP-1), a hydrocarbon fuel, for possible use in future engine programs. Integral to this effort is the modification of the rolling-element bearing analytic code SHABERTH to incorporate RP-1 as a bearing lubricant. Modification of the code requires that certain specific property data be hard-coded. Of the required data, the only information not previously known for RP-1 were the characteristics of traction force as a function of shear rate; these characteristics must be determined experimentally. The traction data were obtained and fit into the traction model of SHABERTH, thereby providing a set of parameters that were hard-coded.

A slight error was detected in the traction equations that are in the SHABERTH program. However, lack of traction data on the original lubricants prevented immediate correction of the error. The error was found to make an insignificant difference in predicting traction for RP-1. A particular traction coefficient for RP-1 was found to be temperature-dependent: this is not accounted for by the model. Prediction of the maximum traction coefficient by using temperature-averaged coefficients err by an average of 12 percent, whereas prediction by using the discrete coefficients at the two temperature conditions err by an average of 4 percent. Currently, the temperature-averaged coefficients are being used. Future work may include developing and adding a temperature-dependent coefficient into the model. The model of the pressure-viscosity coefficient as a function of temperature was tailored to RP-1 by using RP-1 pressure-viscosity data.

A potential project is the investigation of more recent traction models, with the possible replacement of the present traction model in the SHABERTH code in mind. Much work has been done in the area of traction modeling since the development of the SHABERTH code. It is now possible to reduce the traction data to a few fundamental parameters from which the entire traction curve can be predicted with good accuracy, including the high slide-to-roll region where thermal dissipation can become a significant factor.

One such model, which has shown very good agreement with experimental data on a wide variety of lubricants and which would be a good candidate to replace SHABERTH, is the Johnson-Tevaarwerk model. In addition to its ability to accurately predict fluid traction due to ball sliding, the Johnson-Tevaarwerk model has demonstrated the capability to take into account spin and asperity contact as well. Further experimental work on RP-1, as well as work on the SHABERTH code, would be needed for the spin and asperity options.

Lewis Research Center
National Aeronautics and Space Administration
Cleveland, Ohio. April 17, 1990
Appendix A
Changes to the SHABERTH Code

This appendix describes the changes which must be made to the SHABERTH code in order to incorporate RP-1 as a lubricant choice. It includes the modified portions of the SHABERTH code.

A fifth lubricant choice, Freon E-1, was added to the code in 1986. Some versions of the code may not have this addition. The code listed herein has all of the necessary information for adding both the Freon E-1 and the RP-1 choices.

VISCO2

In the subroutine VISCO2, lines 2, 3, 4, and 11 must be added. The variable NCODE must be added to the input list in both the subroutine statement and the call statements. The following information is contained in these additions:

BB = 544. (constant \( B_f \) in Barus pressure-viscosity relationship, 1/GPa)

DP = 25.6 (pressure solidification temperature \( D_p \) in Barus pressure-viscosity relationship, °C)

VISC02

1 SUBROUTINE VISCO2 ( NCODE,A,B,TEMP,RH060, G, VISCP, ALO, RHO )

2 BB = 544.

3 DP = 25.6

4 TT = (TEMP - 32.)*(5./9.)

5 C = 10.*X

6 EXP = C / ( TEMP + 459.7 )**B

7 VISCS = 10.*EXP - .6

8 RHO = RH060 - G * ( TEMP - 60. )

9 VISCP = RHO * VISCS

10 CALL ALPHA0 ( B*2, VISCS, TEMP+459.7, ALO )

11 IF (NCODE.EQ.6) ALO = (BB/(TT+DP))**6.894E-06

12 RETURN

13 END

EHDSKF

In the subroutine EHDSKF, the following variable values must be added at the end of each appropriate data list in the DATA statement (lines 3 to 8). Also, in line 9, ‘N .LT. 6’ must be changed to ‘N .LT. 7’.

C1 = 113450. (\( C_t \))

C2 = 24.65 (\( C_2 \))

C3 = 0.0329 (0.48 - 0.61\( \lambda_0 \))

C4 = 0.203 (0.4\( \lambda_0 \) - 0.09)

A1 = 3.23 (\( A_1 \))

A2 = 1.6 (\( A_2 \))

P1 = 3.4E5 (\( P_1 \))

SLB = 0.15 (\( X_{nb} \))

FBK = 0.65 (\( Y_{nb} \))

EHDSKF

1 SUBROUTINE EHDSKF( ET, H, V, PO, US, N, UM )

2 DIMENSION C1(6),C2(6),C3(6),C4(6),A1(6),A2(6),P1(6),SLB(6),FBK(6)
DATA C1/4734.5,46293.,68910.,27350.,28000.,113450./, C2/304.848,
1102.58,17.31,124.4226,125.012,24.65/, C3/0.297,-0.093,0.053,
2-0.0873,-0.0881,0.0329/, C4/0.03,0.286,0.19,0.282,0.284,0.203/, A1/
33.42,4.08,3.29,6.88,6.80,3.25/, A2/2.18,1.8,1.5,3.4,3.4,1.6/,
4P1/1.5E5,1.7E5,1.7E5,2.2E5,2.0E5,3.4E5/, SLB/0.1,0.1,0.25,0.15,0.25,
50.25,0.15/, FBK/0.65,0.68,0.65,0.68,0.68,0.65/

IF( N .GT. 0 .AND. N .LT. 7 ) GO TO 10

IF ( PO .LT. 1000. ) RETURN
IF ( PO .LT. P1(N) ) XI = (PO/P1(N)) ** A1(N)
IF( PO .GT. PI(N) ) XI = (PO/PI(N)) ** A2(N)
UMS = C1(N) / PO**1.14 * XI**0.61 * ET**0.59 * VN**C3(N) / H**0.45
USS = C2(N)/PO**0.14/XI**0.4/ET**1.1 * VN**C4(N) * H**0.55
FBREAK = FBK(N)
SVB = SLB(N)
SV = US/USS
UM = UMS * FRIC1N(FBREAK, SVB, SV )
RETURN
END

LUPROP

In the subroutine LUPROP. Text must be added to the DATA list in lines 8 and 9. In line 15, '.600' must be added to the GOTO statement. Lines 82 to 96 must be added. These lines contain the following information:

VIS1 = 1.571 (kinematic viscosity at 100 °F, cSt)
VIS2 = 0.7542 (kinematic viscosity at 210 °F, cSt)
A = 13.98464 (constant in Walther’s equation)
B = 5.26787 (constant in Walther’s equation)
RHO60 = 0.8065 (fluid density at 60 °F, g/cm³)
G = 7.2E-04 (fluid thermal expansion coefficient, 1/°C)
COND = 0.13806 (fluid thermal conductivity, W/m °C)
BETA = 0.007278 (auxiliary temperature-viscosity coefficient, 1/°R)
AKN = 20. (EHD high-contact stress factor—not used with the SKF fluid traction model)
FRIC = 0.070 (Allen friction coefficient—not used with the SKF fluid traction model)

LUPROP

1 SUBROUTINE LUPROP ( NCODE, KK, A, B, BETA, RH060, G, COND, VIS1,
2 $ VIS2, XLUBE, IMET )
3 DIMENSION AL(9,6), XLUBE(9,6)
4 COMMON /FLMDAT/ EMOD(2), AKN, FRIC
DATA AL /'SH','EL','L','TU','RB','O','33','M',
1 'IL','L','-7','80','8G','PL','YP','HN','L','ET',
2 'H','MC','52','93','M','IL','-2','36','99','ET',
3 'SP','EC','IA','L','EL','P','RO','CK',
4 'ET','P','RO','PE','LL','NT','1/

... FILL XLUBE WITH THE APPROPRIATE ALPHERIC LUBRICANT TYPE DATA.
DO 10 I = 1,9
10 XLUBE(I,KK) = AL(I,NCODE)

... DETERMINE THE LUBRICANT TYPE FROM NCODE
GO TO ( 100, 200, 300, 400, 500, 600 ), NCODE

100 CONTINUE
... THE LUBRICANT IS SHELL TURBO 33
VIS1 = 64.
VIS2 = 8.
A = 10.34871
B = 3.672531
RHO60 = .879975
G = 6.336E-4
COND = 0.11614
BETA = 0.01932
AKN = 18.2
FRIC = .075
GO TO 999

200 CONTINUE
... THE LUBRICANT IS A MIL-L 7808G
VIS1 = 12.76
VIS2 = 3.2
A = 10.214494
B = 3.698398
RHO60 = .9526
G = 7.092E-4
COND = 0.15218
BETA = 0.013168
AKN = 18.2
FRIC = .045
GO TO 999

300 CONTINUE
... THE LUBRICANT IS POLY PHENYL ETHER MCS 293
VIS1 = 25.4
VIS2 = 4.13
A = 11.451954
B = 4.112963
RHO60 = 1.2006
G = 7.47E-4
COND = 0.11924
BETA = 0.016798
AKN = 24.9
FRIC = .070
GO TO 999

400 CONTINUE
THE LUBRICANT IS A MIL-L-23699
VIS1 = 28.
VIS2 = 5.1
A = 10.207208
B = 3.655059
RH060 = 1.0102
G = 7.452E-4
COND = 0.15218
BETA = 0.016089
AKN = 18.2
FRIC = .070
GO TO 999

LUBRICANT ADDED FOR CRYOGENIC USE
E.S. ARMSTRONG, LEWIS RESEARCH CENTER, 4-10-86

500 CONTINUE
THE LUBRICANT IS SPECIAL E1
VIS1 = .4370
VIS2 = .4106
A = 17.2097
B = 6.9177
RH060 = 1.564
G = .002826
COND = .06921
BETA = .0180
AKN = 20.
FRIC = .070
GO TO 999

LUBRICANT ADDED - LOW VISCOSITY FUEL
C. M. WOODS, LEWIS RESEARCH CENTER, 10/28/89

600 CONTINUE
THE LUBRICANT IS RP-1
VIS1 = 1.571
VIS2 = .7542
A = 13.98464
B = 5.26787
RH060 = 0.8065
G = 7.2E-04
COND = 0.13806
BETA = 0.007278
AKN = 20.
FRIC = .070

999 CONTINUE

CONVERT TO ENGLISH INITS IF REQUIRED.
IF( IMET .EQ. 1 )  GO TO 1000
RH060 = RH060 * 0.036127
G = G * 0.5555555
VIS1 = VIS1 * 1.55E-3
VIS2 = VIS2 * 1.55E-3
COND = COND * 0.5777

1000 CONTINUE
106    RETURN
107    END
Appendix B

Symbols

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A, B$</td>
<td>constants in Walther's equation</td>
</tr>
<tr>
<td>$A_i$</td>
<td>generic expression for $A_1$ and $A_2$</td>
</tr>
<tr>
<td>$A_1, A_2$</td>
<td>parameters in the viscoelastic relationship</td>
</tr>
<tr>
<td>$a$</td>
<td>semimajor length of Hertzian contact ellipse, in.</td>
</tr>
<tr>
<td>$a_1, a_2, a_3, c_1$</td>
<td>exponents of the nondimensional traction equation</td>
</tr>
<tr>
<td>$B_i$</td>
<td>lubricant-dependent constant in Barus model, °C/Pa</td>
</tr>
<tr>
<td>$b$</td>
<td>semiminor width of Hertzian contact ellipse, in.</td>
</tr>
<tr>
<td>$b_1, b_2$</td>
<td>coefficients in geometric fit</td>
</tr>
<tr>
<td>$b_3, b_4$</td>
<td>coefficients in exponential fit</td>
</tr>
<tr>
<td>$C_1, D_1, E_F$</td>
<td>constants in the Fresco model</td>
</tr>
<tr>
<td>$C_{w}$</td>
<td>general constant of proportionality</td>
</tr>
<tr>
<td>$C_o$</td>
<td>constant in the viscoelastic relationship</td>
</tr>
<tr>
<td>$C_o$</td>
<td>constant in the film thickness relationship</td>
</tr>
<tr>
<td>$C_1, C_2$</td>
<td>constants of proportionality in traction equations</td>
</tr>
<tr>
<td>$C_4, C_3$</td>
<td>constants in traction equation</td>
</tr>
<tr>
<td>$c_i$</td>
<td>specific heat of fluid, Btu/°F-in.$^3$</td>
</tr>
<tr>
<td>$D_p$</td>
<td>pressure solidification temperature in Barus model, °C</td>
</tr>
<tr>
<td>$d_{a_1, d_2, d_3, d_4}$</td>
<td>coefficients in polynomial fit</td>
</tr>
<tr>
<td>$E'$</td>
<td>effective elastic modulus, lb/in.$^2$</td>
</tr>
<tr>
<td>$G$</td>
<td>fluid coefficient of thermal expansion, $1/°C$</td>
</tr>
<tr>
<td>$h$</td>
<td>minimum film thickness, in.</td>
</tr>
<tr>
<td>$K_o, K_o'$</td>
<td>conductivity of fluid film, ft-lb/ft $°F$-sec; W/m °C, respectively</td>
</tr>
<tr>
<td>$n_1$</td>
<td>constant in film thickness relationship</td>
</tr>
<tr>
<td>$P, P'$</td>
<td>pressure, lb/in.$^2$; Pa, respectively</td>
</tr>
<tr>
<td>$P_o$</td>
<td>maximum Hertzian contact pressure, lb/in.$^2$</td>
</tr>
<tr>
<td>$f(P_o)$</td>
<td>function of $P_o$ in viscoelastic relationship</td>
</tr>
<tr>
<td>$P_1$</td>
<td>parameter in the viscoelastic relationship, lb/in.$^2$</td>
</tr>
<tr>
<td>$R_s$</td>
<td>curvature sum in x-direction (rolling direction), in.</td>
</tr>
<tr>
<td>$T$</td>
<td>fluid temperature, °F</td>
</tr>
<tr>
<td>$T_R$</td>
<td>experimental traction force, lb</td>
</tr>
<tr>
<td>$T_R$</td>
<td>average experimental traction force per unit length, lb/in.</td>
</tr>
<tr>
<td>$U, U_1, U_2$</td>
<td>rolling velocity of disk 1 and disk 2, respectively, in./sec</td>
</tr>
<tr>
<td>$u, u_s$</td>
<td>sliding velocity, in./sec</td>
</tr>
<tr>
<td>$u_s, u_s^*$</td>
<td>sliding velocity at which $\mu^*$ occurs, in./sec</td>
</tr>
<tr>
<td>$u_s/\mu_s$</td>
<td>nondimensionalized sliding velocity</td>
</tr>
<tr>
<td>$V$</td>
<td>rolling velocity (entrainment velocity), in./sec</td>
</tr>
<tr>
<td>$V_0$</td>
<td>constant in the viscoelastic relationship, in./sec</td>
</tr>
<tr>
<td>$X_R, Y_R$</td>
<td>shape parameters for the predicted traction curve</td>
</tr>
<tr>
<td>$x$</td>
<td>coordinate in contact plane in direction of rolling, in.</td>
</tr>
<tr>
<td>$x^*$</td>
<td>coordinate of nondimensional curve for $u_s/\mu_s^*$</td>
</tr>
<tr>
<td>$y$</td>
<td>coordinate in contact plane normal to rolling, in.</td>
</tr>
<tr>
<td>$y^*$</td>
<td>coordinate of nondimensional curve for $\mu/\mu^*$</td>
</tr>
<tr>
<td>$z$</td>
<td>coordinate normal to contact plane, in.</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>pressure-viscosity coefficient, in.$^2$/lb</td>
</tr>
<tr>
<td>$\beta$</td>
<td>temperature-viscosity coefficient, $1/°R$</td>
</tr>
<tr>
<td>$\beta'$</td>
<td>secondary pressure-viscosity coefficient, in.$^2$/lb</td>
</tr>
<tr>
<td>$\gamma_1$</td>
<td>exponent in the relationship of $\mu^*$ as a function of $V$</td>
</tr>
<tr>
<td>$\eta_0, \eta_0'$</td>
<td>ambient absolute viscosity at inlet temperature, lb-sec/in.$^2$; cP, respectively</td>
</tr>
<tr>
<td>$\eta_0, \eta_0'$</td>
<td>effective absolute viscosity in contact, lb-sec/in.$^2$; Pa-sec, respectively</td>
</tr>
<tr>
<td>$\eta_0^*</td>
<td>\theta</td>
</tr>
<tr>
<td>$\lambda_0$</td>
<td>fluid inlet temperature, °C</td>
</tr>
<tr>
<td>$\mu$</td>
<td>parameter in the viscoelastic relationship</td>
</tr>
<tr>
<td>$\mu'$</td>
<td>traction coefficient (tractive force/normal load)</td>
</tr>
<tr>
<td>$\mu^*$</td>
<td>nondimensionalized traction coefficient term</td>
</tr>
<tr>
<td>$\mu^*$</td>
<td>maximum traction coefficient</td>
</tr>
<tr>
<td>$\mu^*$</td>
<td>maximum nondimensionalized traction coefficient term</td>
</tr>
<tr>
<td>$\nu$</td>
<td>ambient kinematic viscosity at inlet temperature, cSt</td>
</tr>
<tr>
<td>$\rho, \rho'$</td>
<td>fluid density, g/cm$^3$; lb/in.$^3$, respectively</td>
</tr>
<tr>
<td>$\sigma$</td>
<td>composite surface roughness, in.</td>
</tr>
<tr>
<td>$\tau_s$</td>
<td>fluid shear stress in rolling direction, lb/in.$^2$</td>
</tr>
<tr>
<td>$\psi_0, \psi_0'$</td>
<td>nondimensionalized sliding velocity term</td>
</tr>
<tr>
<td>$\psi_0^*</td>
<td>\psi_0^*$</td>
</tr>
</tbody>
</table>

References

Recently developed traction data for Rocket Propellant 1 (RP-1), a hydrocarbon fuel of the kerosene family, was used to develop the parameters needed by the bearing code SHABERTH in order to include RP-1 as a lubricant choice. The procedure for inputting data for a new lubricant choice is reviewed, and the theoretical fluid traction model is discussed. Comparisons are made between experimental traction data and those predicted by SHABERTH for RP-1. All data needed to modify SHABERTH for use with RP-1 as a lubricant are specified.