Measurements and Predictions of a Liquid Spray From an Air-Assist Nozzle

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Abstract

Droplet size and velocity and gas velocity were measured in a water spray using a two-component Phase/Doppler Particle Analyzer. A complete set of measurements was obtained at axial locations from 5 to 50 cm downstream of the nozzle. The nozzle used was a simple axisymmetric air-assist nozzle. The sprays produced, using the atomizer, were extremely fine. Sauter mean diameters were less than 20 μm at all locations. Measurements were obtained for droplets ranging from 1 to 50 μm. The gas phase was seeded with micron sized droplets, and droplets having diameters of 1.4 μm and less were used to represent gas-phase properties. Measurements were compared with predictions from a multi-phase computer model. Initial conditions for the model were taken from measurements at 5 cm downstream. Predictions for both the gas phase and the droplets showed relatively good agreement with the measurements.

Nomenclature

a acceleration of gravity
Ci constants in turbulence model
Cd drag coefficient
d nozzle diameter
dp droplet diameter
k turbulence kinetic energy
Le dissipation length scale of eddy
mp droplet mass
n number of droplet groups
ni number of droplets per unit time in group i
Re Reynolds number
r radial distance

c source term
Sp source term due to droplets
t time
t_e eddy lifetime
V_v volume of computational cell j
v radial velocity
w angular velocity
x axial distance
X_p droplet position vector
c rate of dissipation of turbulence kinetic energy
u viscosity
u_t turbulent viscosity
ρ density
σ_t turbulent Prandtl/Schmidt number
ϕ generic property
q_X_p relative path length of droplets in an eddy
V_t_p droplet residence time in an eddy

Subscripts:
c centerline quantity
o initial axial location
p droplet property
= ambient condition

Superscripts:
( )' fluctuating quantity
(−) time averaged value
(∗) vector quantity
(~) Favre averaged value

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Introduction

Spray nozzles have many important applications and have been the subject of considerable research. The objective of the present investigation was to obtain measurements of droplet size, velocity, and volume flux and gas velocity in the flowfield of a simple atomizer and compare their values with predictions from a multiphase computer model.

A similar investigation was performed by Dodge and Schwab1 using a pressure swirl atomizer. Most of the initial conditions for their model were estimated, however, predictions were shown not to be very sensitive to initial conditions. For that study, air velocities were very low in comparison to droplet velocities. A single-component Phase/Doppler instrument was used for the measurements. The liquid utilized was an aircraft fuel system calibration fluid (MIL-C-7024 type II). The computer model used for comparison with the data was the FLUENT code. In an earlier study, reported by Solomon, et al.,2 an air-atomizing nozzle operating with nonevaporating vacuum pump oil was investigated. Gas-phase velocities were measured with a standard LDA system. Droplet size and velocities were measured using a double-flash shadow photographic method. Droplet fluxes were measured using an isokinetic sampling probe. Experimental measurements were compared with predictions from three two-phase flow models.

Other experimental spray studies using a Phase/Doppler instrument are reported in Refs. 3 and 4. Measurements are presented for both droplet and gas-phase velocities. Presser and Senerjian6 also report a spray study using an ensemble light scattering technique. No gas-phase measurements are presented. A recent study is reported in Ref. 6 describing Phase/Doppler measurements of a water spray in a swirling flowfield. Both gas phase and droplet measurements are reported.

Experimental Methods

The sprays were directed vertically downward within a large enclosure (1.8 by 1.8 by 2.4 m high). The air-assist nozzle could be traversed vertically within the enclosure while the enclosure and nozzle could be traversed together in two horizontal directions. This arrangement allowed rigid mounting of all optical instrumentation used during the study. The flow downstream impinging upon a screen located 1 m below the measurement plane to remove larger droplets and allow smaller droplets to be used as seeding for the ambient air.

The air-assist nozzle is shown in Fig. 1. The inside diameter of the liquid tube was 0.39 mm and the orifice for the nozzle was 3.18 mm. This nozzle was selected because it is relatively simple and does not utilize a swirler for atomization. Water was used for the liquid spray and was supplied using a tank pressurized with nitrogen to provide a steady flowrate without pressure oscillations. Liquid flowrates were measured using a mass flowmeter. Air flowrates were measured using a 1.27 mm diameter critical-flow orifice. The air flowrate was controlled by regulating upstream pressure of the air. The atomizing air was seeded with micron sized droplets supplied from a Norgren lubricator. The fluid used for the seeding was Rosco fog fluid, typically used for smoke generators. The average measured drop size in the jet using only the seeder was 1.5 μm. For the results reported in the present paper, the air and water flowrates were 2.25 and 0.49 g/s, respectively.

All measurements were performed using a two-component Phase/Doppler Particle Analyzer. Previous studies describing this instrument have been reported in Refs. 7 and 8. The configuration chosen for the present experiment utilized a 2-W argon laser, frequency shifting for both channels using rotating diffraction gratings, a 500 mm focal length focusing lens, and a 450 mm focal length receiving lens. Light was collected 30° off-axis in the forward direction and focused onto a slit. For measurements at 5 and 10 cm downstream of the nozzle, a 50 μm wide slit was used. The remainder of the measurements used a 100 μm wide slit. Generally, 64,000 total samples were taken at each measurement location. The number of validated samples varied from about 90 to 20 percent of the total, depending on the region of the flowfield where measurements were being obtained. Measurements in locations near the center of the spray close to the injector exit where number densities were extremely high and velocities were also high showed the largest number of signal rejections. Regions downstream of the nozzle where the spray was not as dense and velocities lower had much higher validation rates. Droplet diameters ranging from 1 to 50 μm were measured. Velocity measurements are reported for droplet diameters of 4, 11, 18, and 25 μm. Gas-phase velocities are obtained from measurements of droplets with diameters of 1.4 μm or less. A traverse across the entire spray was performed at each axial measurement station.

Theoretical Methods

The analysis is limited to steady, axisymmetric, dilute, nonevaporating, droplet-laden, non-swirling, turbulent jets in an infinite stagnant medium. The boundary-layer approximations are adopted in conjunction with a k-ε turbulence model for closure. The assumptions for the continuous phase are identical to those reported in Ref. 9. Favre-averaged equations (equivalent to time-averaged in this case) govern the variation of mean axial and radial velocities, turbulent kinetic energy, and rate of dissipation of turbulent kinetic energy. With these assumptions, the governing equations for the gas phase can be expressed in the following general form:

\[ \frac{\partial}{\partial x}\left( \rho \vec{u} \cdot \vec{v} \right) + \frac{1}{r} \frac{\partial}{\partial r} \left( \rho v \vec{v} \right) = \frac{1}{r} \frac{\partial}{\partial r} \left[ \left( \mu + \mu_t \right) \frac{\partial \vec{v}}{\partial r} \right] - S_\phi + S_{\rho \phi} \] (1)

The parameters \( \phi \) and \( S_\phi \) appearing in Eq. (1), as well as empirical constants used, are listed in Table 1.

The turbulent viscosity \( \mu_t \) was calculated as:

\[ \mu_t = C_\mu \frac{k^2}{\varepsilon} \] (2)

Boundary conditions for Eq. (1) are:
\[ r = 0, \ \frac{\partial r}{\partial t} = 0; \ \ r = \infty, \ \ \phi = \phi_0 \]  

Initial conditions were obtained from the measurements obtained at 5 cm downstream of the nozzle. \( e_0 \) was calculated from the definition of a turbulent length scale and is given as follows:

\[ e_0 = C \mu \frac{k^{3/2}}{L} \]  

where \( L \) was taken as 8 percent of the flow width at that axial location. Initial values of \( w' \) were assumed to be equal to measured values of \( v' \).

The computation of the liquid phase is based on the solution of Lagrangian equations of motion for a statistically significant number of representative droplet groups. Major assumptions for the droplet trajectory calculations are: quasi-steady gas phase, no droplet-droplet interaction, and use of a solid-sphere drag law. With these assumptions, the position and velocity of each droplet group can be found by integrating:

\[ \frac{dx_{ij}}{dt} = u_{pi} \]  

\[ \frac{du_{pi}}{dt} = \left( \frac{3\pi C_D}{4 \rho_p \pi L} \right) (u_{pi} - u_p) \left| \frac{\partial}{\partial x_{ij}} + \frac{\partial}{\partial y_{ij}} \right| + a_i \]  

where \( i = 1, 2, 3 \) for each one of the Cartesian coordinates and the velocities shown in these equations are instantaneous velocities. The drag coefficient was calculated as follows:

\[ C_D = \frac{24}{Re(1 + Re^{2/3})}, \ \ Re < 1000; \]  

\[ C_D = 0.44, \ \ Re \geq 1000 \]  

The effects of turbulent gas phase fluctuations on droplet trajectory are incorporated using a stochastic separated-flow (SSF) model. The interaction between turbulence and droplets is considered by using a random-walk technique. Each group of droplets interacts with a succession of turbulent eddies. The interaction time is taken to be the minimum of either the eddy lifetime or the transit time for the droplet to cross the eddy. Properties of each eddy are found by making a random selection from the pdf of velocity. Instantaneous eddy velocity is calculated assuming velocity fluctuations are isotropic with a Gaussian pdf having a most probable value found from the local mean velocity and a variance of \( 2k/3 \). Details of the procedure can be found in Refs. 2 and 10. The interaction between the droplets and the gas phase yields source terms in the governing equations for conservation of momentum. They are found by computing the net change in momentum as each droplet group passes through a computational cell \( j \) and is given as follows:

\[ S_{p,u_j} = v_j^{-1} \sum_{i=1}^{n} S_{p,u_i}\left( u_{p,i_{in}} - u_{p,i_{out}} \right) \]  

where, \( n_i \) is the number of particles per unit time in each group. The calculations for the continuous phase were performed using a modified version of Genmix.11 The computational grid utilized has 33 cross-stream grid nodes and streamwise step size was limited to 2 percent of the current flow width or an entrainment increase of 2 percent - whichever was smaller. For the droplet calculations, 19 200 droplet groups were tracked through the flowfield.

**Results and Discussion**

**Axial Profiles**

The variation of centerline values with axial distance are illustrated in Fig. 2(a) to (e). Both measurements and predictions are presented for axial velocities of both gas and liquid phases. As illustrated in Fig. 2(a) to (d), axial velocities at 5 cm downstream of the nozzle are fairly high, ranging from 80 m/s for the gas phase to 93 m/s for the 25 \( \mu \)m drops. As measured, the droplets had higher velocities than the gas at this axial location. Axial velocities decay very quickly from 5 to 20 cm downstream of the nozzle for both the gas and the three droplet sizes shown. Results for the 4 \( \mu \)m droplets were almost identical to the gas phase and are not shown. Even though the droplet size is relatively small, larger droplets possess higher axial velocities at distances less than 20 cm from the nozzle. At distances greater than about 20 cm, velocity differences between droplet sizes are considerably reduced. As illustrated in Fig. 2, predictions from the model for axial centerline velocities are in reasonably good agreement with the measurements. At downstream distances of 5 and 10 cm, the centerline measurements presented for the 25 \( \mu \)m droplets are based on less than 50 samples, consequently they should be used with caution. Sample sizes for the 18 \( \mu \)m and smaller drops were adequate at all downstream locations. At larger downstream distances, centerline measurements for the 25 \( \mu \)m droplets are based on at least 2000 samples. Figure 2(e) presents the axial centerline profile of turbulence kinetic energy for the gas phase, normalized by the local centerline axial velocity. For the experimental values, only \( u' \) and \( v' \) were measured. It was assumed that \( w' \) was equal to \( v' \). The increase of normalized turbulent kinetic energy with axial distance is initially overpredicted, however, predictions show better agreement with the measurements at increasing axial distances from the injector. No attempt was made to account for the modification of the gas-phase turbulence by the droplets.

**Radial Profiles**

Radial profiles of spray properties at 10 cm downstream are illustrated in Fig. 3(a) to (f). Results are presented for the 18 \( \mu \)m diameter droplets and the continuous phase. Radial profiles for the other droplet sizes were similar except for the fluctuating quantities, which will be discussed later. Gas phase radial profiles of mean axial velocity, \( k \), and \( u'v' \) are shown in Fig. 3(a) to (c). Centerline axial velocity has decayed to about 43 m/s and is underpredicted by about 30 percent. Centerline \( k \) and peak values of \( u'v' \) are
somewhat overpredicted at this axial location, how-
ever the jet width is fairly well predicted. Pred-
dicted and measured radial profiles of mean axial
velocity, and fluctuating axial and radial veloc-
ties of 18 μm diameter droplets are illustrated in
Fig. 3(d) to (f). Again, the peak axial velocity
is underpredicted, but only by about 10 percent.
Fluctuating axial velocities are substantially
greater than fluctuating radial velocities at this
axial location. Predicted values of fluctuating
axial velocity show lower values than the measure-
ments, while fluctuating radial values agree reason-
ably well with the measurements. This is due to
the assumption of isotropic fluctuating velocities
in the model, while measured axial fluctuating
velocities were larger than radial fluctuating
velocities. The predicted values show some scatter
in the profiles. Predictions for the 18 μm droplets
were obtained using 4800 droplet groups. Increasing
the number of droplet groups would result in
smoother radial profiles. Larger droplets showed
larger fluctuating axial velocities than smaller
droplets near the centerline at this axial location.
However, this may be due to the fact that fewer
larger droplets were found at the center of the spray
and the sample size may not be large enough. An
examination of the complete data set showed that
larger droplets consistently showed lower fluctuat-
ing radial velocities across the entire width of
the spray than smaller droplets. This was also
shown by the predictions. Fluctuating radial
velocities are important for turbulent dispersion of
the droplets since they are larger than the mean radial
velocities in the present spray.

Radial profiles at 20 cm downstream of the nozzle
are illustrated in Fig. 4(a) to (f). Results
are again presented for the gas phase and 18 μm
diameter droplets. Figure 4(a) to (c) presents gas
phase measurements and predictions of mean axial
velocity, k, and u'v'. The centerline gas veloc-
ity has decayed to about 22 m/s from the value of
80 m/s measured at 5 cm downstream of the nozzle.
The predictions agree reasonably well with the meas-
urements; the centerline is underpredicted by about
6 percent. Radial profiles of k and also u'v'
show fairly good agreement with the measurements
at this axial location, although k is underpredicted.
Radial profiles of the 18 μm droplets are presented
in Fig. 4(d) to (f). Even at 20 cm downstream of
the nozzle, mean axial velocities of the droplets
are slightly, but consistently, larger than the gas
phase. Peak centerline velocity is underpredicted
by about 4 percent, however values elsewhere show
very good agreement with the measurements. Fluctu-
ating axial and radial velocities of the 18 μm drop-
lets again show effects of anisotropic velocity
fluctuations, but are reduced here compared to val-
ues observed at 10 cm downstream of the nozzle.
Predicted radial fluctuating velocities agree with
the measurements, while axial fluctuating veloc-
ities are still lower than the measurements.

Profiles at 30 cm downstream are shown in
Fig. 5(a) to (f) for both the gas phase and the 18
μm droplets. Gas phase axial centerline velocity
has decayed to about 14 m/s. Predictions of mean
axial velocity show excellent agreement with the
measurements at this location. Gas phase k and
u'v' are also shown, where some scatter is evident
in the u'v' data. The reason for the scatter is
probably due to a measurement inaccuracy at this
location. Droplet profiles at this axial location
are also presented for the 18 μm droplets. Predic-
tions for mean axial velocity and fluctuating
radial velocity show quite good agreement with the
measurements. Predictions of fluctuating axial
velocity again are lower than the measurements, how-
ever, the differences are decreasing as axial dis-
tance increases and axial velocity decreases.

Radial profiles at the largest axial downstream
measurement location of 50 cm are presented in
Fig. 6(a) to (f). As illustrated in Fig. 6(a)
to (c), predictions of gas phase radial properties
show fairly good agreement with the measurements
at this location, although k is still underpredicted,
especially near the centerline. The data show
a slight shift to the positive r direction of about
2 mm at this axial location. This is probably due
to a slight misalignment between the nozzle axis
and the gravity vector which is more evident at
larger axial distances. Radial profiles for the 18
μm diameter drops are presented in Fig. 6(d) to
(f). Centerline mean axial droplet velocity has
decayed to slightly less than 10 m/s at this axial
location. Fluctuating radial velocity is still
smaller than fluctuating axial velocity, however,
the flow becomes more isotropic. Predicted values
show the same distribution trends as the measure-
ments, but values are on the order of 20 percent
lower than the measurements.

Radial profiles for the 4, 11, and 25 μm
droplets are not presented. Results for the 4 μm
droplets are almost identical to the gas phase.
The results for the 11 μm droplets are somewhat
between the gas phase and the 18 μm droplets. The
25 μm droplets show larger differences between
the drops and the gas phase, but there are relatively
few of these in the spray, especially near the cen-
ter of the jet near the nozzle.

Conclusions

A complete set of measurements and predictions
of both the gas phase and droplets have been pre-
tended for a water spray spraying downward into
stagnant surroundings. The flow geometry was
kept relatively simple so that an axisymmetric, par-
abolic, computer model could be used. Major conclu-
sions from the study are listed as follows:

1. Axial centerline velocity decay with dis-
tance downstream of the nozzle was reasonably well
predicted for both the gas phase and the droplets.
For the 18 μm diameter droplets, droplet mean axial
velocities decayed from 86 m/s at 5 cm downstream
of the nozzle to 9 m/s at 50 cm downstream. The
gas phase decayed from 80 m/s at 5 cm to 9 m/s at
50 cm downstream of the nozzle.

2. Predicted radial profiles of mean properties
for both the gas phase and the droplets showed rela-
tively good agreement with the measurements at all
axial stations. Better agreement was obtained as
axial distance increased.

3. For the 18 μm droplets, fluctuating axial
velocities were underpredicted while fluctuating
radial velocities generally showed good agreement
with the measurements. This was probably caused by
the isotropic assumption of the SSP model.

4. The spray produced by the nozzle was very
axisymmetric making it useful for comparison with
model predictions.
References


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Figure 1.—Diagram of air-assist nozzle.
Figure 2.—Axial variation of centerline properties.
Figure 3.—Radial profiles at 10 cm downstream of the nozzle.
Figure 4.—Radial profiles at 20 cm downstream of the nozzle.
(a) Gas phase mean axial velocity.

(b) Gas phase turbulence kinetic energy.

(c) Gas phase shear stress.

(d) Mean axial velocity of 18 micron drops.

(e) Fluctuating axial velocity for 18 micron drops.

(f) Fluctuating radial velocity for 18 micron drops.

Figure 5.—Radial profiles at 30 cm downstream of the nozzle.
Figure 6.—Radial profiles at 50 cm downstream of the nozzle.
Measurements and Predictions of a Liquid Spray From an Air-Assist Nozzle

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Abstract

Droplet size and velocity and gas velocity were measured in a water spray using a two-component Phase/Doppler Particle Analyzer. A complete set of measurements was obtained at axial locations from 5 to 50 cm downstream of the nozzle. The nozzle used was a simple axisymmetric air-assist nozzle. The sprays produced, using the atomizer, were extremely fine. Sauter mean diameters were less than 20 microns at all locations. Measurements were obtained for droplets ranging from 1 to 50 microns. The gas phase was seeded with micron sized droplets, and droplets having diameters of 1.4 microns and less were used to represent gas-phase properties. Measurements were compared with predictions from a multi-phase computer model. Initial conditions for the model were taken from measurements at 5 cm downstream. Predictions for both the gas phase and the droplets showed relatively good agreement with the measurements.

Sprays
Multiphase flow