Verifying an Interactive Consistency Circuit:  
A Case Study in the Reuse of a Verification Technology

Mark Bickford  
Mandayam Srivas

Odyssey Research Associates, Inc.  
301A Harris B. Dates Drive  
Ithaca, NY 14850.

This talk presented the work done at ORA for NASA-LRC in the design  
and formal verification of a hardware implementation of a scheme for  
attaining interactive consistency (byzantine agreement) among four  
microprocessors. The microprocessors used in the design are an  
updated version of a formally verified 32-bit, instruction-pipelined,  
RISC processor, MiniCayuga. The 4-processor system, which is designed  
under the assumption that the clocks of all the processors are  
synchronized, provides ‘‘software control’’ over the interactive  
consistency operation. Interactive consistency computation is  
supported as an explicit instruction on each of the microprocessors.  
An identical user program executing on each of the processors decides  
when and on what data interactive consistency must be performed.

This exercise also served as a case study to investigate the  
effectiveness of reusing the technology which had been developed  
during the MiniCayuga effort for verifying synchronous hardware  
designs. MiniCayuga was verified using the verification system Clio  
which was also developed at ORA. To assist in reusing this technology  
a computer-aided specification and verification tool was developed.  
This tool specializes Clio to synchronous hardware designs and  
significantly reduces the tedium involved in verifying such designs.  
The talk presented the tool and described how it was used to specify  
and verify the interactive consistency circuit.
Summary

Achievements

1. Formalization of abstract Byzantine agreement algorithm.

2. Use of this algorithm to specify a hardware device.

3. A mechanically checked proof that the device design is correct.

4. The implementation of the device form the low-level design.

Limitations

1. Assumes synchronized behavior of the processes.
Verifying an Interactive Consistency Circuit:
A Case Study in the Reuse of a Verification Technology

Mark Bickford
Mandayam Srivas

Odyssey Research Associates, Inc.
301A Harris B. Dates Drive
Ithaca, NY 14850.
Objectives of the Work

- Design an efficient hardware implementation for a 4-processor architecture
- Use verified MiniCayuga’s in the design
- Verify the design
- Reuse MiniCayuga verification technology
  - A method of modeling synchronous hardware designs in the Clio verification system
  - Formalizing a class of properties most commonly encountered in verifying designs
  - A “standard” proof strategy
Clio: A functional Language Based Verification System

- Caliban: A modern functional language eg., higher order functions, data types, lazy, etc.

\[ \text{least } P \ x = \ x, \ P \ x \]
\[ \text{least } P \ x+1 \]

- Assertion Level: Full FOPE with equality on Caliban terms

\[ \text{Prop} := (\exists) (x) \land \left[ \neg \left( \exists \ x \right) \land \text{`True`} \right] \land \left[ \neg \left( \exists \ x \right) \land \text{`True`} \right] \]

- Interactive Theorem Prover

- rewriting
- Induction
  - structural
  - Fixed Point
- Other FOPE proof Strategies
Presentation Outline

• IC circuit design

• The computer-aided hardware verification tool

• How we verified it

• General observations about the effort
The Hardware Design: Overview
Two new instructions:

**ICOP REG** - initiates and co-ordinates IC computation

**MOVE SREG REG** - moves special REG to general REG

|| check if voter is free
Notfree MOVE STATUS REG1
JIF REG1 Notfree
ICOP REG2

|| check if IC computation is complete
Notready MOVE STATUS REG1
JIF REG1 Notready

|| move the results of IC to general registers
MOVE SREG0 REG3
MOVE SREG1 REG4
MOVE SREG2 REG5
The Hardware Design: Overview

Fault Region 1

Cayuga-FT1

1 2 3

Voter1

V1 V2 V3

Fault Region 2

Cayuga-FT2

1 2 3

Voter2

Fault Region 3

Cayuga-FT3

1 2 3

Voter3

Fault Region 4

Cayuga-FT4

1 2 3

Voter4
• voter separate from processor: modularity

• point-to-point connection: electrical isolation

• serialize data transfers: number of pins Vs. time

• Fault region: processor, voter, and the connections they feed
• no absolute indexing scheme for processors/voters
  – relative indexing scheme: $succ$, $succ^2$, $succ^3$

  – IC vectors will be stored in the processors in the order of their successors

• Underlying assumption: clocks are synchronized with at most a bounded skew

  – hold sender’s signal stable for one phase longer than needed
IC System Design Behavior

- **Initiate**: draw the attention of voter (1)
- **Load**: transfer private values (2)
- **Exchange**: exchange received values (6)
- **Compute**: compute and store IC vector (3)
Controller State Machine
MiniCayuga Processor: Summary

- Inspired by Cayuga (Cornell University)

- 32-bit RISC processor

- Design characteristics
  - 32 general purpose registers
  - small and simple instruction set
  - 3-stage instruction pipeline: fetch, compute, writeback
  - delayed jump, pipeline stalling, internal forwarding
  - interrupt
What do we prove?

Assuming

- every Cayuga-FT is about to execute an ICOP,
- every Voter is ready to vote, and
- there is at most one faulty region,

then, 12 cycles later the system state will satisfy the following conditions:

- The IC vectors in the processors are identical "up to rotation."
- The IC vectors are correct w.r.t. to the processor private values 12 cycles earlier.
A Computer-Aided Verification Tool

- Specializes Clio to the domain of *finite state controller systems*

- Design specification generation

- Verification condition formulation

- Automatic proof support
The Voter Circuit

Controller State Machine
Finite State Controller Systems (FSCS)

- Central Controller + Data Path components

- Component behavior is specified as a set of actions

- Controller is specified as an FSM which schedules a set of actions on the components.

- Timing Model
  - Every transition corresponds to a clock cycle (with multiple phases)
  
  - An action may have zero or more units (phases) of delay

  - Actions are synchronized with state transitions
Specification technology reused

- a method of formalizing the intended operational model of an FSCS in Caliban/Clio

\[
\text{designspecgen} ::
\begin{align*}
\text{data-path-structure} & \rightarrow \\
\text{controller-structure} & \rightarrow \\
\text{controller-schedule} & \rightarrow \\
\text{actions-behavior} & \rightarrow \text{design-spec}
\end{align*}
\]

\[
\text{Execute} :: \text{STATE} \rightarrow \text{STATE}
\]

"single clock cycle behavior of design"
Proof technology shared

- Form of the most commonly proved conditions
  - Invariant conditions

  ![Diagram of invariant conditions]

  - Advance conditions

  ![Diagram of advance conditions]

- Proof strategy: "controlled symbolic evaluation (rewriting) with selective case-splits"
The Specification Hierarchy

ICNet

Step

Voter

Execute

Majority

Step

Execute

Actions

Reg

ByteReg

ALU

Register decoder Reg

...
Rationale for the hierarchy

- Decompose proofs into manageable units

- Need for the black level
  - introduce "error" actions
  - type of Execute is different from that of action

- Implication of intermediate levels
  - pro: proof can take "bigger" steps
  - con: must come up with intermediate abstract specification
Top Level Specification

IcNetState ::~ <<(INDEX -> FTCstate),
INDEX -> Voterstate), Interrupts>>

IcNetStep <<ftc,vtr, int:rest>> =
<<newftc,newvtr ,rest>>
where newftc index
    = fault_ftc_step index ftc (ftcinp index)
newvtr index
    = fault_vtr_step index vtr (vtrinp index)
ftcinp index
    = make_ftc_in (select_int index int)
        (fault_to_proc index ftc vtr)
vtrinp index
    = Voterinput index ftc vtr
        (ftcinp index )

fault_ftc_step index s in =
    FtCayugaStep (s index) in , ~(faulty index)
    byzCayugaStep (s index) in

fault_vtr_step index s =
    voterstep (s index) , ~(faulty index)
    byzstep (s index)

...
Formal Statement of Correctness

MainTheorem :=
    Preconditions 's' => ResultConsistent 's'

ResultConsistent 's' :=
    Consistent 'icvec s (Iterate #12 IcNetStep s)'

Consistent 'array' :=
    'faulty index'='False' =>
        IndexConsistent 'array' 'index'

IndexConsistent 'array' 'index' :=

    ('faulty (succ index)'='False' =>
        '(array index).succ'='array (succ index)')

    & ('faulty (succ2 index)'='False' =>
        '(array index).succ2'='array (succ2 index)')

    & ('faulty (succ3 index)'='False' =>
        '(array index).succ3'='array (succ3 index)')
Preconditions 's' :=
   Proper_icnet 's' & Sync 'LDP1' 's' & All_go 's'

Sync 'cs' '<<ftc,vtr,inlist>>' :=
   ('faulty ONE' = 'False' =>
      'control (vtr ONE)'='cs')
& ('faulty TWO' = 'False' =>
      'control (vtr TWO)'='cs')
& ('faulty THREE' = 'False' =>
      'control (vtr THREE)'='cs')
& ('faulty FOUR' = 'False' =>
      'control (vtr FOUR)'='cs')

All_go 's' :=
   ('faulty ONE'='False' =>
      ('go_of (vtr s ONE)'='False' & 'go_signal s ONE'='GO')
& ('faulty TWO'='False' =>
      ('go_of (vtr s TWO)'='False' & 'go_signal s TWO'='GO')
& ('faulty THREE'='False' =>
      ('go_of (vtr s THREE)'='False' & 'go_signal s THREE')
& ('faulty FOUR'='False' =>
      ('go_of (vtr s FOUR)'='False' & 'go_signal s FOUR'='GO')

21
Preconditions 's' :=
  Proper_icnet 's' & Sync 'LDP1' 's' & All_go 's'

Sync 'cs' '<<ftc,vtr,inlist>>' :=
  ('faulty ONE' = 'False' =>
   'control (vtr ONE)'='cs')
& ('faulty TWO' = 'False' =>
   'control (vtr TWO)'='cs')
& ('faulty THREE' = 'False' =>
   'control (vtr THREE)'='cs')
& ('faulty FOUR' = 'False' =>
   'control (vtr FOUR)'='cs')

All_go 's' :=
  ('faulty ONE'='False' =>
   ('go_of (vtr s ONE)'='False' & 'go_signal s ONE'='GO'))
& ('faulty TWO'='False' =>
   ('go_of (vtr s TWO)'='False' & 'go_signal s TWO'='GO'))
& ('faulty THREE'='False' =>
   ('go_of (vtr s THREE)'='False'
    & 'go_signal s THREE'='GO'))
& ('faulty FOUR'='False' =>
   ('go_of (vtr s FOUR)'='False'
    & 'go_signal s FOUR'='GO'))
The proof strategy reused

"controlled symbolic execution of design"

1. Instantiate the states of components and inputs with appropriate symbolic constants.

2. Add all the conditions on the constants implied by the preconditions of the theorem as hypothesis.


4. Try case-splitting on all the conditionals automatically.

5. If either of the previous two steps seem to take too long, then case-spilt on the controller states and inputs before symbolic evaluation (step 3).
New technology needed

- Modeling faulty behavior

- Specification
  - determining the right hierarchy
  - writing intermediate "abstract" spec
  - defining abstraction function (ABS)

- Proof: "design level properness" implies "abstract level properness"
General Observations

- An engineering-oriented verification experience
  Lilith → MiniCayuga → IC circuit

- Methodology: top-down + bottom-up

- Level of effort: 1 man year
  - building the tool
  - developing designs
  - verification
Verification Effort Milestones

- formulated a top level correctness statement

- designed and verified a simple voter circuit

- specified voter and processor for a continuous voting scheme

- designed and verified second voter design
• discovered continuous voting scheme was "hard to synchronize"

• respecified voter and processor for a voting-on-demand scheme

• redesign and reverify voter

• verified overall system

• verified processor
• To integrate theorem proving based verification technology into the design process we need:
  
  – more machine assistance
  
  – domain specialization

• The next step?
  
  – A useful way of reporting failed proof attempts
  
  – Interaction with motivated and patient engineering design teams and projects