A Model for the Space Shuttle Main Engine High Pressure Oxidizer Turbopump Shaft Seal System

Daniel E. Paxson
Lewis Research Center
Cleveland, Ohio

Prepared for the
Second Annual Conference on Health Monitoring for Space Propulsion Systems
sponsored by the University of Cincinnati
Cincinnati, Ohio, November 14-15, 1990
A Model for the Space Shuttle Main Engine
High Pressure Oxidizer Turbopump Shaft Seal System

Daniel E. Paxson
National Aeronautics and Space Administration
Lewis Research Center
Cleveland, Ohio 44135

Abstract

A simple static model is presented which solves for the flow properties of pressure, temperature, and mass flow in the Space Shuttle Main Engine High Pressure Oxidizer Turbopump Shaft Seal System. This system includes the Primary and Secondary Turbine Seals, the Primary and Secondary Turbine Drains, the Helium Purge Seals and Feed Line, the Primary Oxygen Drain, and the Slinger/Labyrinth Oxygen Seal Pair. The model predicts the changes in flow variables that occur during and after failures of the various seals. Such information would be particularly useful in a post flight situation where processing of sensor information using this model could identify a particular seal that had experienced excessive wear. Most of the seals in the system are modeled using simple one dimensional equations which can be applied to almost any seal provided that the fluid is gaseous. A failure is modeled as an increase in the clearance between the shaft and the seal. Thus, the model does not attempt to predict how the failure process actually occurs (e.g. wear, seal crack initiation, etc.). The results presented herein were obtained using a FORTRAN implementation of the model running on a VAX computer. Solution for the seal system properties is obtained iteratively; however, a further simplified implementation (which does not include the Slinger/Labyrinth combination) has also been developed which provides fast and reasonable results for most engine operating conditions. Results from the model compare favorably with the limited redline data available.
Nomenclature

c ..................... clearance between shaft and seal (radial) in inches
CD ..................... discharge coefficient
C1 ..................... experimental coefficient
d ..................... diameter of shaft in inches
G ..................... geometric factor depending upon slinger dimensions
h ..................... fluid enthalpy in btu/lbm
ks ..................... smooth side slip coefficient
kv ..................... vaned side slip coefficient
L ..................... seal length in inches
M1 ..................... mach number at the end of the inlet nozzle
M2 ..................... mach number at the end of the channel
rh ..................... flow rate in lbm/sec
N ..................... number of teeth in labyrinth seal
Po ..................... pressure at origin or inlet of a seal in psi
Pe ..................... pressure seal exit in psi
R ..................... real gas constant for a specific gas in ft·lbf/lbm·°R
r ..................... radial position in inches
8t ..................... flow resistance in sec²/in⁵
To ..................... temperature at origin or inlet of a seal in degrees Rankine
γ ..................... ratio of specific heats
μ ..................... fluid viscosity in Reynolds
ρ ..................... fluid density in lbm/ft³
ω ..................... shaft rotational speed in rpm
Introduction

Seal failures have been recognized as an important potential failure mode in reusable rocket engines [1,2,3]. Seals are critical for the operation of many major components and appear in many forms throughout the engine. However, despite their varied appearance many of these seals function in a similar fashion and thus lend themselves to a generalized representation. Unfortunately, to the author's knowledge, no reliable model is readily available in the literature today. In an effort to eliminate this void, the present investigation was undertaken and resulted in the model to be described below.

Before describing the model itself it is worthwhile to discuss the nature of failure modelling in general and its relation to the approach taken in this investigation. There are two basic approaches which seem to be espoused in the field. The first is a true first principles approach in which one asks, "what are the dynamics of the failure?" An attempt is made to actually link together the fluid mechanical and structural interactions which lead to a given component failure. This is a bold and difficult approach which has yet to yield fruitful results, however; if successful, it will give the most valuable information. The second approach proceeds along the lines of asking, "suppose a certain failure does occur, what are the effects on the rest of the engine?" This is a purely pragmatic line of thinking in which the only goal is detection and isolation of a failure. No consideration is given to its cause. It is this approach which was taken in the present work and which will now be discussed.

A schematic of the High Pressure Oxidizer Turbopump (HPOTP) seal system on the Space Shuttle Main Engine (SSME) is shown in Figure 1. Generally, its purpose is to prevent the leakage of any fluids in down the shaft and in particular, to prevent the mixing of hot Hydrogen rich turbine gases on one side of the pump from combining with Oxygen from the other side. Also shown in the figure are the points at which pressure and temperature sensors reside in the actual HPOTP. There are five static seals, that is seals which have no moving parts, and a dynamic seal, often referred to as a slinger, which depends upon shaft rotation in order to function. Proceeding from right to left, the first two seals are referred to as the primary and secondary turbine seals. These separate the hot turbine gases from the Helium purge gases. The second set of seals are referred to collectively as the Purge seals. These serve to separate hot gas which has leaked through the turbine seals from gaseous oxygen which has leaked through the slinger/labyrinth seal combination on the left of the figure (often called the Primary Oxidizer Seal). Gaseous, inert Helium is forced through the purge seal pair from high pressure tanks on board the shuttle. This gas then mixes with the hot turbine gas and gaseous oxygen on either side of the seal pair and exits through separate drain lines which are also shown in Figure 1. The constant flow of Helium thus provides a barrier between the two gases (Hydrogen rich turbine gas and gaseous oxygen) which if combined would be extremely volatile. The labyrinth seal, in combination with the slinger, serves to stem the flow of oxygen leaking from the high pressure LOX pump. Like the other seals mentioned, it provides high resistance to through flow by maintaining a small clearance between the seal face and the shaft. The labyrinth differs from the
others however, in that it is composed of many thinner seal faces, or teeth, instead of just one thick face. Thus, there is a relatively small drop in pressure across each of the labyrinth teeth, but the accumulated pressure drop across the entire seal is quite large. Finally, the slinger seal is a dynamic seal (e.g. has moving parts) which serves two purposes. First, it restricts the flow. Secondly, it gasifies the liquid oxygen which does leak through by doing work on it. Many papers have been written on the slinger seal [4,5,6,7] and details of the principles of operation will not be presented here. Suffice it to say that generally speaking, a slinger is conceptually the same as a pump in which the pressure gradient that it must overcome is too great and the fluid flows backward. The shortcoming of this analogy is that unlike most pumps, the slinger has the added complexity of a gas/liquid interface.

Model Description

Annular Seals

The Turbine seals and the two seals which compose the Purge seal are all simple annular clearance seals thus, a general description of them was sought. It was found that they could be well modeled by considering each to be composed of a nearly isentropic entrance nozzle attached to a one dimensional channel with frictional losses through which perfect gases flowed. This is shown in Figure 2. Several implications are embedded in this model. First, the clearance of the seal is presumed to be much less than the radius of the shaft. Second, the fluid velocities associated with axial flow through the seal are assumed much greater than those in the circumferential direction caused by the rotation of the shaft. This is a reasonable assumption since seals typically operate at or near a choked condition, and the speed of sound in the gases is significantly larger than the characteristic circumferential speed which is the shaft angular rotation rate multiplied by the shaft radius. Thirdly, it is supposed that fluid velocities inside the seal proper are much greater than those outside so that the fluid on either side of the seal is nearly stagnant. Finally, it is assumed that heat transfer effects are negligible. That is, that the flow is adiabatic. The information necessary to calculate the flow through the seal includes the pressure drop across the seal, the seal clearance, and length, the fluid viscosity, ratio of specific heats, and real gas constant and the coefficient of discharge for the entrance nozzle. For the nozzle region, the equation for the flow rate may be written as

\[ \dot{m} = \pi d c_d P_o \sqrt{\frac{\gamma}{R T_o}} \left[ \frac{M_1^2}{1 + \frac{\gamma - 1}{2} M_1^2} \right]^{\gamma - 1} \left[ \frac{\gamma + 1}{\gamma - 1} \right]^{1/2} \]

This equation assumes that the nozzle flow is unchoked, however; it may be shown that, when the nozzle is joined to a constant area duct with friction, choking can occur only in the duct. In the duct region the relation between the entrance and exit mach numbers (regions 1 and 2 respectively in
where a friction factor corresponding to laminar boundary layer flow on a flat plate has been used due to the entry region type flow in the seal annulus. Also, since the flow is assumed adiabatic and the gases are assumed perfect, the stagnation temperature remains constant throughout the seal and, provided the flow is not choked, it is found that

\[
M_2^2 = \frac{1}{\gamma - 1} \left[ -1 + \left( 1 + \frac{2(\gamma - 1)M_1^2}{\gamma + 1} \left( \frac{P_e}{P_o} \right)^{\gamma - 1} \right) \left( \frac{\gamma + 1}{\gamma - 1} \right)^{\gamma - 1} \right]^{-1/2}
\]  

These are three equations and three unknowns (\(M_1\), \(M_2\), and \(\mu\)) which may be solved simultaneously, however; due to their complexity their solution must be obtained iteratively. The procedure is as follows. A guess is made at \(\mu\) and equation 2 is solved for \(M_1\) on the assumption that \(M_2=1.0\) (e.g. choked flow). Equation 3 is then solved for the pressure ratio which corresponds to choking. If the actual pressure ratio \(P_e/P_o\) is less than or equal to the choking value then the actual pressure ratio is irrelevant and the value of \(M_1\) obtained above may be used in equation 1 to find the new \(\mu\). If the actual pressure ratio is greater than the choking value then with \(P_e/P_o\) and \(\mu\) known, 2 may be substituted into 3 and this equation may be solved for \(M_1\) using a technique such as the False Point method. With \(M_1\) known, equation 1 may then be used to find a new guess at \(\mu\). This process is repeated until the new and old mass flow values agree to within a specified tolerance. The above procedure is illustrated clearly using the flowchart shown in Figure 3. Comparisons of this model with data obtained experimentally for several different gases [8] are shown in Figures 4, 5, and 6. The format of Figure 6 is different from the other two because in the experiment several different clearances were used as well as different pressure ratios. Information concerning the graphs can be found in Table 1. Also shown in Figure 6 are the predicted flow values obtained using another program called FLOWCAL described in [8]. As is clearly evident, the present model performed significantly better. The ordinate axis label SCFM refers to Standard Cubic Feet per Minute and is simply the mass flow per minute divided by the density of the gas at standard temperature and pressure.

Labyrinth Seal
The Labyrinth seal, shown in Figure 7, was modeled according to an analysis performed by Martin [9]. Here it is assumed that each seal within the Labyrinth may be treated as an orifice (e.g. the length is negligible) and that the fluid stagnates completely on either side of the seal tooth. Furthermore, it is assumed that the pressure drop across any one tooth is not large. This is a valid assumption for the HPOTP labyrinth since it has seventeen teeth. The equation for the mass flow across the entire seal may be written as

\[ \dot{m} = \pi dc C_D \frac{P_o}{\sqrt{RT_o}} \left[ \frac{1}{N} - \ln \left( \frac{P_e}{P_o} \right) \right]^{1/2} \]  

(4)

This is an established and accepted model and therefore no experimental data is presented here for verification. It is noted however, that modifications exist in the literature [10] which account for residual kinetic energy (non stagnant flow between teeth) and geometrical variations such as teeth which fit into grooves on the shaft instead of the smooth shaft type shown in Figure 7. These modifications were used in the present investigation. For reasons to be explained later it was necessary to solve this equation for the pressure ratio with the flow rate given. This was done by moving the right side of equation 4 to the left and solving for the roots of the resulting equation using the False Point method.

Slinger Seal

The Slinger seal was extremely difficult to model and it is noted at the outset that this aspect of the seal system model is probably the least accurate. At best it is claimed that reasonable qualitative results may be expected. An analysis by Voss [5] provided the starting point for the present model. For reference a schematic drawing of the slinger seal is shown in Figure 8. As shown by the arrows, the fluid flow path originates at the high pressure point just upstream the turbine side bearing set. As it travels radially outward along the smooth side of the slinger there is an increase in the pressure owing to the centrifugal force of rotation. On the other side of the slinger there is a set of vanes. Because of the vanes there is much less fluid slip than on the smooth side. Consequently, the centrifugal effects are multiplied considerably. If both sides of the slinger were filled with liquid it can be seen that for a given radial position the pressure on the vaned side would be less than on the smooth side. Furthermore, this difference increases as one moves closer to the shaft. This is the operating principle of the slinger, however; there is another important feature of this particular system. The vanes also "stir" the fluid like the whisks of a beater. Consequently, work is done on the fluid thereby raising its internal energy. When enough energy has been added, and the proper pressure conditions exist (e.g. at some radial point) the liquid oxygen will turn to vapor. When this
happens the density drops substantially, thereby greatly reducing the centrifugal effects. The vanes however, can continue to heat the gas. On the smooth side of the seal it is assumed that no work is done and that the flow is isentropic. The change in pressure due to the centrifugal force is expressed as

\[ P_{r+\Delta r} = P_r + k_s^2 \rho \omega^2 r \Delta r \]  \hspace{1cm} (5)

Here it is assumed that the change in radius is small so that, over the interval, the density may be assumed constant. The slip factor \( k_s \) used in the present study was 0.5. To find conditions at the outer radius of the slinger, it was divided into 20 intervals. At each new radial position the pressure was calculated using equation 5 and the value of density and pressure from the previous position. A new density and temperature were then found using the new pressure and constant entropy. This was accomplished by utilizing a series of software routines known collectively as GASPLUS available on the VAX cluster at NASA [11]. These routines are designed to calculate the properties of many gases and liquids over a wide range of conditions. The process was repeated until the outside of the slinger was reached. On the vaned side equation 5 could again be used, however, this time the direction of travel is inward and the value of the slip factor \( k_v \) was much higher (e.g. less slip). In the present investigation the value was chosen as 0.98 if the fluid was liquid and 0.93 if it was vapor or saturated vapor. An energy balance on a "thin ring" control volume yields

\[ h_{r-\Delta r} = h_r + G C_O \left(1 - k_v\right)^2 \rho \omega^3 r^3 \Delta r \]  \hspace{1cm} (6)

This equation is based on the assumption that the work done per mass on the fluid flowing through the ring is equal to the work rate of the torque. A simple analysis of the torque induced on the slinger vanes is outlined in [12]. The procedure was thus to again divide the vaned side of the slinger into 35 intervals beginning at the outer edge. For each new radial position equations 5 and 6 were used to calculate a new pressure and enthalpy based on the density at the last position. Using the GASPLUS routines the new temperature and density were then found. This process was repeated until the shaft radius was reached. Of course, at some point the liquid would change to a vapor. When this happened the new \( k_v \) for gas was then used to continue the calculations. For this calculation to proceed, the flow rate through the seal, and the state of the LOX on the slinger's smooth side are needed. The result is the conditions at the base of the vaned side just upstream of the Labyrinth seal. Since the Slinger and the Labyrinth seal are in series (Figure 1) it is necessary that the flow through them be the same. This fact was used to solve for the flow through the Slinger/Labyrinth combination. A guess was made at the flow rate, \( \dot{m} \) and equations 5 and 6 were used to find the properties upstream of the Labyrinth seal. With the same flow rate and the known downstream pressure, equation 4 was also used to find the pressure upstream of the Labyrinth. If this pressure matched that calculated with equations 5 and 6 then the flow was solved. If not, a new guess (based on the magnitude of the pressure difference) was made and the cycle was repeated until
the pressures matched. Figures 9 and 10 show the Slinger/Labyrinth mass flow and exit temperature respectively as functions of exit pressure for two different Labyrinth seal clearances. The LOX conditions at the base of the slinger (inlet) as well as the slinger rpm were held constant for these calculations. The inlet conditions are presented for reference in Table 2 following the figures. Note that this is in contrast to the other seals discussed where the exit pressure was held constant and the inlet pressure was varied. The inlet information was obtained from the SSME Power Balance Model. Figure 9 shows an expected trend in that flow rate increases as the exit pressure is dropped and eventually chokes at very low exit pressures. One interesting aspect however, is that the calculations show that it is possible for the exit pressure to exceed the inlet pressure and still maintain positive through flow. In these cases the centrifugal effects on the smooth side remain the same and increase the pressure at the tip of the slinger above the inlet pressure at the base. In the low flow cases however, the work done per unit mass on the gas is large on the vaned side and the interface occurs near the slinger tip. With the gasification of the Oxygen, the centrifugal effect on the vaned side is substantially reduced and the pressure at the base of the slinger on the vaned side can remain higher than that at the inlet. It is noted here that the "waviness" of the data is a result of the rather large finite intervals into which the slinger was divided in order to calculate properties up and down the sides (e.g. the deltas in equations 5 and 6). Smaller divisions lead to better results but far more computing time. Figure 10 is presented because, unlike the annular seals described earlier in which the temperature changes vary little across them, this seal combination shows a fairly strong dependence of exit temperature on the flow rate. This, of course, makes intuitive sense for as the flow rate decreases more work is done to heat the fluid.

Drain Lines

The seal drain lines, of which there are three (see Figure 1), and the helium purge feed line were all modeled using a simple resistance type equation based upon an incompressible flow analysis. Some allowance was made for compressibility by using an average density for the flow in the drains based upon inlet and exit pressures and the inlet temperature (assumed constant throughout the drain). Although the flows in the seals were not, in fact incompressible, it was assumed that in the drain lines, where velocities and mach numbers are relatively low, the assumption was nearly valid. According to this analysis, the flow rate may be expressed in the form

\[ \dot{m} = \frac{P_o^2 - P_e^2}{\sqrt{2RT_o R}} \]  

(7)

The resistances (R's) for the various drain lines were obtained either through discussions with MSFC personnel [13] or by matching experimental flow rates with known pressure differences.
The System

The final step in the modelling process was simply to put all of the various smaller models described above into one complete representation of the seal system. This was accomplished using iterations on the equations of continuity. Figure 11 is a redrawing of Figure 1, however; here the system has been broken into three sections. Also shown in the figure are the points at which the fluid properties and flow rates are calculated. The procedure begins by guessing at the pressure at point 3. With this pressure know, all of the flow quantities in region III may be found. Next a guess is made at the pressure at point 6. With this known, the flow through the oxygen drain (7) and the Labyrinth/Slinger may be found. The Pressure at point 4 may then be adjusted until the net flow into point 6 is zero. Hence, all flow quantities in region I become known. With the pressure at point 4 known, the net flow into point 3 may then be found. If this is zero, the iteration is complete. If not, a new guess must be made for the pressure at point 3 (e.g. using the false point method) and the procedure is repeated. This process is done until the net flows into points 1, 4, and 6 are all zero.

Results

Although the flow rate was calculated at each of the prescribed points, it will not be presented in any of the results. Flow rate measurements are not currently practical within the small confines of the seal system passages and thus, it is not expected that they would be used in a health monitoring/failure detection capacity. It is noted however, that in the case of a Primary Turbine Seal failure of the magnitude (i.e. clearance) discussed here, the flow rate across the seal is large and amount to approximately 6% of the total flow through the HPOTP turbine. Figures 12 and 13 show the pressure and temperature values respectively at each of the calculation points for four different engine power levels, using the nominal seal clearances listed in Table 3. The calculation points as well as the points where conditions are assumed known are labeled in Figure 11. Also shown in Figures 12 and 13 are the points (marked with asterisks) where actual transducers are located (this is also shown in Figure 1). As mentioned earlier, the information for the known conditions was obtained from the Power Balance Model. The Primary Turbine Seal inlet conditions were taken to be those at the exit of the HPOTP turbine with 400° R subtracted from the temperature. This accounts for the mixing of the gas with some coolant flow from other parts of the pump [13]. Slinger inlet conditions were taken to be those just upstream of the number 4 bearing set. These were estimated as follows. The pressure was assumed that at the HPOTP LOX pump inlet, with an accounting for area change due to the location of the passage and a flat 20 psi added to the pressure to account for the flow over the bearings. Temperature was taken to be that at the inlet to the booster pump. Finally, the exit pressure for all of the drain lines was assumed to be 1 atmosphere or 14.7 psia. It is seen from these figures that the conditions stay relatively constant over most of the engine power levels. The one exception is the 65% level where a sharp drop in pressure is occurs at points 1 and 8 as well as a significant temperature drop at nearly all points. The pressure and
temperature values for a primary turbine seal failure and a secondary turbine seal failure are shown in Figures 14 and 15. The broken line at point 1 for the primary turbine seal failure indicates that the pressure exceeds the maximum value in the figure (it is 728.6 psia). Failures for all the seals were manifested by changing the clearance. The values used for failed seals are shown in Table 3. As expected, a primary turbine seal failure increases the flow through the primary seal drain and thus raises the pressure at points 1 and 2 considerably. With this pressure elevated, the flow through the secondary turbine seal is also increased thereby increasing the flow through the secondary drain and subsequently the pressure at point 3. The increased temperature at point 3 is the result of increased hot gas flow through the drain line. The secondary turbine seal failure results also display expected trends. Here, the pressure at point 1 drops due to the increased flow across the secondary turbine seal and hence reduced flow through the primary seal drain. Similarly, the increased secondary turbine seal flow increases flow through the secondary seal drain and therefore increases pressure and temperature at point 3. It is found that if both primary and secondary turbine seals failed, the redline pressure value of 100 psi is exceeded at point 3 (secondary seal drain cavity). Figures 16 and 17 show the results of purge seal failures. For either purge seal failure a large drop in the pressures at points 4 and 5 are seen. This is explained by the fact that the resistance to flow is greatly reduced as the seal clearance is increased. Thus it takes less pressure difference across the seal to drive more flow. Again it is found that the pressure calculated at point 5 falls below the redline value for a failure of either seal. The remainder of the deviations from the nominal pressures and temperatures throughout the seal system for the purge seal failures may be explained using analogous arguments to those used for the turbine seal failures. Finally, the results of a slinger/labyrinth seal failure are shown in figures 18 and 19. Since a failure of the slinger seal itself is extremely unlikely it was assumed here that failure was brought about by a change in the clearance of the labyrinth seal. It is seen in the figures that a pressure rise occurs at point 6 due to the increased flow through the drain line but that a significant pressure drop occurs at point 8. This drop is due to the fact that increased flow through the slinger decreases the work done per mass of fluid, which in turn moves the interface toward the shaft and hence allows the centrifugal effects to provide a greater pressure drop. Since less work is done on the fluid it is also discharged at a lower temperature which is reflected at point 6, 7, and 8 of Figure 19. Although the results presented above are in qualitative agreement with expectations, the lack of available experimental data makes them difficult to evaluate objectively.

It is interesting to note that if the actual magnitude of the pressure and temperature changes associated with a given failure are ignored and instead only their direction (greater than or less than) away from the nominal values are considered, each failure seems to have a characteristic pattern. This result is illustrated in Tables 4 and 5. In these tables, the respective pressure and temperature deviations of each point from the nominal value (at RPL), are shown as either upward or downward facing arrows for positive or negative deviations, or as a dash indicating no change. These tables suggest that a potential failure detection and isolation scheme for this seal system could rely on more qualitative measurements and still be successful.
Another noteworthy aspect of the results was the reliability of the seal system as a whole. Recall that the main purpose of this system was to keep the Oxygen flow through the pump separate from the hot, Hydrogen rich gas flow through the turbine. From the results presented it appears that this separation is maintained despite the failure of any one of the seals. In fact, when further test were conducted it was found that potential mixing of the two gases exists only when both of the purge seals fail or the Helium supply pressure is reduced to values of under 100 psia. These are highly unlikely occurrances. Thus, from a health monitoring/failure detection standpoint it would seem that monitoring these seal failures during flight is unnecessary. Since a failure is not catastrophic to the engine and, in fact, does not even seem to imply minor damage, it is enough to monitor the condition of the seals in a post flight mode using stored data.

Conclusions

A model of the HPOTP Shaft Seal System for the SSME was successfully developed. The model predicts the fluid properties and flow rates throughout this system for a number of conditions simulating failed seals. The results agree well with qualitative expectations and redline values but cannot be verified with actual data due to the lack thereof. The results indicate that each failure mode results in a unique distribution of properties throughout the seal system and can therefore be individually identified given the proper instrumentation. Furthermore, the detection process can be built on the principle of qualitative reasoning without the use of exact fluid property values. A simplified implementation of the model which does not include the slinger/labyrinth seal combination has been developed and will be useful for inclusion in a real time diagnostic system.
References


<table>
<thead>
<tr>
<th></th>
<th>Figure 4 Hydrogen</th>
<th>Figure 5 Air</th>
<th>Figure 6 Helium</th>
</tr>
</thead>
<tbody>
<tr>
<td>Downstream Pressure, $P_e$, psia</td>
<td>14.7</td>
<td>14.7</td>
<td></td>
</tr>
<tr>
<td>Upstream Temperature, $T_o$, °R</td>
<td>555.0</td>
<td>530.0</td>
<td>530.0</td>
</tr>
<tr>
<td>Seal length, L in.</td>
<td>0.28</td>
<td>2.0</td>
<td>0.077</td>
</tr>
<tr>
<td>Shaft diameter, d in.</td>
<td>1.97</td>
<td>6.0</td>
<td>1.968</td>
</tr>
<tr>
<td>Radial clearance, c in.</td>
<td>$2.26 \times 10^{-3}$</td>
<td>0.029</td>
<td></td>
</tr>
<tr>
<td>Discharge coefficient, $C_D$</td>
<td>0.6</td>
<td>1.0</td>
<td>1.0</td>
</tr>
<tr>
<td>Viscosity, $\mu$, Reys</td>
<td>$1.21 \times 10^{-9}$</td>
<td>$2.76 \times 10^{-9}$</td>
<td>$2.89 \times 10^{-9}$</td>
</tr>
<tr>
<td>Ratio of specific heats, $\gamma$</td>
<td>1.39</td>
<td>1.40</td>
<td>1.66</td>
</tr>
<tr>
<td>Real gas constant, $R$, ft-lbf/lbm-°R</td>
<td>772.5</td>
<td>53.46</td>
<td>386.0</td>
</tr>
</tbody>
</table>

Table 1 Annular Seal Conditions

<table>
<thead>
<tr>
<th></th>
<th>354.8</th>
<th>191.1</th>
<th>66.41</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inlet pressure, psia</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Inlet temperature, °R</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Inlet density, lbm/ft³</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Shaft Speed, rpm</td>
<td>27210</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Number of Labyrinth teeth</td>
<td>17</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 2 Labyrinth Seal Inlet Conditions
<table>
<thead>
<tr>
<th>Seal Type</th>
<th>Nominal Clearance (in.)</th>
<th>Failed Clearance (in.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Primary Turbine Seal</td>
<td>0.003</td>
<td>0.015</td>
</tr>
<tr>
<td>Secondary Turbine Seal</td>
<td>0.003</td>
<td>0.015</td>
</tr>
<tr>
<td>Hot Gas Side Purge Seal</td>
<td>0.0015</td>
<td>0.015</td>
</tr>
<tr>
<td>Oxygen Side Purge Seal</td>
<td>0.0015</td>
<td>0.015</td>
</tr>
<tr>
<td>Labyrinth</td>
<td>0.005</td>
<td>0.05</td>
</tr>
</tbody>
</table>

Table 3 Seal Clearances

<table>
<thead>
<tr>
<th>Power Level</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
</tr>
</thead>
<tbody>
<tr>
<td>Primary Turbine Seal</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>(!)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Secondary Turbine Seal</td>
<td></td>
<td>(!)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Hot Gas Purge Seal</td>
<td>-</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Oxygen Purge Seal</td>
<td>-</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Slinger/Labyrinth</td>
<td>-</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 4 Direction of Pressure Deviations for Various Seal Failures
Table 5  Direction of Temperature Deviations for Various Seal Failures

Figure 1.—Seal system schematic.
Figure 2.—Step seal model.
Guess initial \( m \)

Solve Eqn. 2 for \( M_1 \) with \( M_2 = 1.0 \) (e.g. choked)

\[
\frac{1}{\gamma} \left[ \frac{1}{M_1^2} - 1 \right] + \frac{\gamma + 1}{2\gamma} \ln \left[ \frac{M_1^2 (1 + \gamma)}{2 + [\gamma-1]M_1^2} \right] = \frac{2.656 \pi \rho c \mu L}{m} 
\]

Solve Eqn. 3 for \( \frac{p_e}{p_o}_{\text{choked}} \) with \( M_2 = 1.0 \)

\[
\frac{p_e}{p_o}_{\text{choked}} = \left[ \frac{4}{\gamma + 1} \frac{M_1^2}{M_1^{\gamma+1}} \frac{2 + [\gamma-1]M_1^2}{2 + [\gamma-1]M_1^2} \right]^{1/2}
\]

Is \( \frac{p_e}{p_o}_{\text{actual}} \) less than \( \frac{p_e}{p_o}_{\text{choked}} \)?

If yes

With current \( m \) and \( \frac{p_e}{p_o} \), solve Eqn.'s 2 and 3 simultaneously for \( M_1 \) with \( M_2 \)

\[
\frac{1}{\gamma} \left[ \frac{1}{M_1^2} - \frac{1}{M_2^2} \right] + \frac{\gamma + 1}{2\gamma} \ln \left[ \frac{M_1^2 (2 + [\gamma-1]M_2^2)}{M_2^2 (2 + [\gamma-1]M_1^2)} \right] = \frac{2.656 \pi \rho c \mu L}{m} 
\]

\[
M_2^2 = \frac{1}{\gamma - 1} \left( 1 + \frac{2(\gamma-1)M_1^2}{\sqrt{\left( 1 + \frac{\gamma-1}{2} M_1^{\gamma+1} \right)^{\gamma-1}}} \right)^{1/2} 
\]

Use Eqn. 1 with current \( M_1 \) to find new \( m \)

\[
m_{\text{new}} = \pi \rho c C_p p_o \sqrt{\frac{\gamma}{RT_o}} \left[ \frac{M_1^2}{\left( 1 + \frac{\gamma-1}{2} M_1^{\gamma+1} \right)^{\gamma-1}} \right]^{1/2} 
\]

Is abs(\( m_{\text{new}} - m \)) less than specified tolerance?

If yes

Quit

Figure 3.—Seal flowchart.
Figure 4.—Hydrogen ring seal leakage rate.

Figure 5.—Air ring seal leakage rate.
Figure 6.—Helium purge seal leakage rate.

Figure 7.—Labyrinth seal schematic.
Figure 8.—Slinger seal.

Figure 9.—Slinger/labyrinth seal leakage rate.
Figure 10.—Slinger/labyrinth seal exit temperature.

Figure 11.—Seal system regions and calculation points.
Figure 12.—Pressures throughout seal system for various thrust levels.
Figure 13.—Temperatures throughout seal system for various thrust levels.
Figure 14.—Pressures throughout seal system for primary and secondary turbine seal failures at engine RPL

At Engine RPL
 *=Measured

Pressure Point

1 2* 3* 4 5* 6 7* 8

Pressure (psia)

Nominal
Primary Turbine Seal
Secondary Turbine Seal
Figure 15.—Temperatures throughout seal system for failed primary and secondary turbine seal failures at engine RPL.
Figure 16.—Pressures throughout seal system for failed purge seals at engine RPL.
Figure 17.—Temperatures throughout seal system for failed purge seals.
Figure 18.—Pressures throughout seal system for failed labyrinth seal at engine RPL.
Figure 19.—Temperatures throughout seal system for failed labyrinth seal at engine RPL.
A simple static model is presented which solves for the flow properties of pressure, temperature, and mass flow in the Space Shuttle Main Engine pressure Oxidizer Turbopump Shaft Seal Systems. This system includes the Primary and Secondary Turbine Seals, the Primary and Secondary Turbine Drains, the Helium Purge Seals and Feed Line, the Primary Oxygen Drain, and the Slinger/Labyrinth Oxygen Seal Pair. The model predicts the changes in flow variables that occur during and after failures of the various seals. Such information would be particularly useful in a post flight situation where processing of sensor information using this model could identify a particular seal that had experienced excessive wear. Most of the seals in the system are modeled using simple one dimensional equations which can be applied to almost any seal provided that the fluid is gaseous. A failure is modeled as an increase in the clearance between the shaft and the seal. Thus, the model does not attempt to predict how the failure process actually occurs (e.g. wear, seal crack initiation, etc.). The results presented herein were obtained using a FORTRAN implementation of the model running on a VAX computer. Solution for the seal system properties is obtained iteratively; however, a further simplified implementation (which does not include the Slinger/Labyrinth combination) has also been developed which provides fast and reasonable results for most engine operating conditions. Results from the model compare favorably with the limited redline data available.