Reasoning about Real-Time Systems with Temporal Interval Logic Constraints on Multi-State Automata

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Abstract
Models of real-time systems using a single paradigm often turn out to be inadequate, whether the paradigm is based on states, rules, event sequences or logic. In this paper, a model-based approach to reasoning about real-time systems is presented in which a temporal interval logic called TIL is employed to define constraints on a new type of high-level automata. The combination, called "Hierarchical Multi-State (HMS) machines," can be used to model formally a real-time system, a dynamic set of requirements, the environment, heuristic knowledge about planning-related problem solving, and the computational states of the reasoning mechanisms. In this framework, mathematical techniques have been developed for (1) proving the correctness of a representation, (2) planning of concurrent tasks to achieve goals, and (3) scheduling of plans to satisfy complex temporal constraints. HMS machines allow reasoning about a real-time system from a model of how truth arises instead of merely depending on what is true in a system.

1. Introduction
Real-time systems are characterized by unpredictability of inputs and "hard deadline" requirements. In addition, since many real-time systems are utilized in life-critical situations, strict "safety properties" are usually defined for them. A safety property is a state of affairs that must always remain true in a system. Instead of the usual discussion of "liveness properties," it is useful to define other requirements of a real-time system in terms of a set of "conditional goals" defined in terms of (condition, goal) pairs. A condition defines the state of affairs under which the associated goal must be pursued. We assume that deadlines may be associated with goals and that requirements are dynamic so that the pursuit of an active goal may have to be abandoned if certain other conditions become true. Thus, at the specification stage, the main forms of reasoning about a real-time system consists of the verification that (1) safety properties are not violated and (2) conditional goals are achievable. For traditional systems which operate deterministically or stochastically, this is essentially sufficient even though it can be a very complicated process. At the operational stage, two other forms of reasoning arise for "intelligent systems" which are not defined deterministically and require a search or other forms of analysis to instantiate a specific set of responses in a particular situation. First, off-line reasoning can be performed to determine in advance a set of allowable actions to achieve goals. Secondly, on-line reasoning can be employed, where deadlines on the reasoning process itself may have been defined. A key problem in the specification and operation of complex real-time systems is the choice of a representational framework that can provide manageable approaches to specification, verification, and instantiation of behavior.

While numerous formal representational schemes have been proposed for systems in general and real-time systems in particular, most of these are based on one of the following paradigms: state-based...
models, rules, event sequences or logic. Two major examples of state-based models are automata and Petri nets. For real-time systems, traditional automata are inadequate for at least two important reasons: (1) explosion of the state space for non-trivial systems, and (2) absence of a natural mechanism for representing temporal constraints. Petri nets reduce the state space and can represent concurrent activities adequately. However, in Petri nets numerous dummy states are usually necessary to maintain logical consistency and no clear separation is made between precedence and causality [7].

In addition, even timed Petri nets have a limited language for representing temporal relationships among states and events [6]. Specification and verification of complex real-time requirements are also difficult for rule-based systems and event sequences. In particular, it is generally accepted that while rules are appropriate for defining prototypical behavior, they are inadequate for reasoning about novel situations. As far as pure logical formalisms are concerned, temporal logic provides a promising approach, except for two shortcomings. First, certain simple regular properties cannot be expressed in temporal logic [10]. Secondly, in a pure logic-based language a system is represented merely in terms of what is true. This gives a limited understanding of system behavior, since knowledge of how truth arises which is common to state models is not readily available.

The purpose of this paper is to present a brief overview of a comprehensive framework for specifying real-time systems and reasoning about them, called "Hierarchical Multi-State (HMS) machines," that integrates high-level "multi-state" automata and fragments of a temporal interval logic called TIL ([7], [4], [3], [5], [6]). As noted in Figure 1, an HMS machine can be used to define formally the dynamic behavior of a system, its requirements, a model of the environment, heuristic knowledge about planning-related problem solving, and the state of the computational resources used in reasoning. Given such a specification, the system can be simulated, its correctness can be verified formally, and it can be used for both off-line and on-line reasoning to derive operational plans and schedules to respond to the dynamics of a real-time situation.

Section 2 presents an outline of a simple form of HMS machines, with a brief discussion of the method for representing requirements in terms of "policy HMS machines." Section 3 presents an overview of the planning process, plan representation languages, and a scheduling algorithm for plans. Section 4 presents a brief set of conclusions and directions for future work.

![Figure 1. Specification, Verification and Reasoning Framework for Real-Time Systems](image-url)
2. Automata, Temporal Logic, Machines and Real-Time Systems

An automaton consists of a set of "states" and a set of "transitions" that cause changes in states due to the occurrence of certain events such as arrival of inputs. This provides a very general architecture for defining the dynamics of a system, except that, as indicated in the Introduction, it is inadequate for specifying complex real-time systems. Hierarchical Multi-State (HMS) machines [4] are high-level "multi-state automata," in which (1) multiple (hierarchical) states can be true at one moment, (2) multiple transitions can fire simultaneously, and (3) a temporal interval logic, called TIL, is used to define constraints on transitions. This architecture allows the compact definition of the dynamics of complex real-time systems, in which interactions among states and hard deadlines can be defined formally. In addition, a "multi-level" combination of HMS machines [5] provides the capability for formally defining dynamic requirements, giving rise to a model-based reasoning framework for real-time systems. Because of limitations of space, only the non-hierarchical version of HMS machines will be considered here. A formalization of hierarchies can be found in [6].

An HMS machine is a triple $H = (S, \Gamma_D, \Gamma_N)$, where $S$ is a set of "states," $\Gamma_D$ is a set of "deterministic" transitions, and $\Gamma_N$ is a set of "nondeterministic" transitions. Boolean states represent properties that may be true or false about a system. Non-boolean states can represent both properties of multiple entities in a system and properties of data objects. Deterministic transitions denote fixed causal interactions among states, while nondeterministic transitions represent possible or permissible interactions. Nondeterminism, in fact, is the key to the specification of choice in model-based reasoning in the HMS framework.

The constraints or "controls" on transitions in an HMS machine are defined in terms of the temporal interval logic TIL which is obtained by adding the following three operators to propositional logic:

- $O(t)$: At relative time $t$
- $[t_1, t_2]$: Always between times $t_1$ and $t_2$
- $<t_1, t_2>$: Sometime between times $t_1$ and $t_2$

The operators $[t_1, t_2]$ and $<t_1, t_2>$, which allow hard real-time constraints to be defined for HMS machines, are generalizations of the standard temporal logic operators $\Box$ and $\Diamond$, respectively. All times are relative, with the current moment denoted by 0. Figure 2 depicts a simple 2-level example of an HMS machine specification that defines both a nondeterministic "basic machine" $H_1$ and a specification of requirements in terms of the "policy HMS

![Figure 2. A 2-Level HMS Machine Specification of System and Requirements](image-url)
3. Planning, Plan Formalisms and Scheduling of Plans for HMS Machines

A “plan” in the HMS framework consists of a sequence of sets of transitions to be executed in a nondeterministic machine [5]. Conditional goals are specified for an HMS machine in terms of policy transitions of a policy HMS machine such as H2 in Figure 2. The “planning” process then consists of searching the space of eligible nondeterministic transitions in a basic machine such as H1 to derive a plan that causes the goal states of a policy transition
to be reached. The important points to note in this framework are that (1) goals can be defined formally in terms of histories of states that are being modified dynamically, (2) circumstances such as inability to meet a deadline may cause a goal to be dropped from consideration, (3) the states of the computational resources in which planning is being performed may be used as controls on the policy transitions that define goals, and (4) heuristic guidelines for deriving plans can be specified in terms of intermediate policy machines.

Compilation of plans in advance to meet goals with hard deadlines has been proposed by number of authors (see, e.g., [9]). Various representation schemes for plans have also been proposed. For example, in [1] a Petri net model is used to define conditional actions that depend on facts that are true about the environment. The HMS machine framework offers a powerful capability to define complex concurrent plans that depend not only on the current states of the world but also on temporal histories of states. For this purpose, we say that a machine P is a "plan HMS machine" for a nondeterministic machine H, if some of the states of P correspond to the nondeterministic transitions of H and some other states are "dependent" states of the states of H. A dependent state is defined as a state for which (1) truth only depends on a logical combination of the truth or falsehood of other states, and (2) there are certain restrictions on transitions emerging from it and entering it. At each moment of time, the "execution" of P on H then is obtained by (1) firing the transitions of P as in a standard HMS machine, (2) firing the deterministic transitions of H, and (3) firing those nondeterministic transitions of H that are enabled in H and for which a corresponding state in P is true. Thus, for example, the plan machine in Figure 3 describes how the nondeterministic transitions in the machine H1 should be executed. The states containing asterisks are dependent states which, in this case, are simply duplicates of corresponding states in H1, assuming that the state "In a Hurry" is added to H1. The states denoted by dashed rectangles represent transitions in H1. Thus, this machine indicates that in case the state "In a Hurry" is true, one should execute the transition "Climb into Helicopter" from the state "At Office" in H1. On the other hand, if the state "In a Hurry" is false, the transition "Get in Car" should be executed. Also, when the state "In Car" becomes true in H1, the transition "Start Driving to Airport" will be fired if its corresponding state in Figure 3 is true. The latter situation will be true if the state "Going on Trip" has been true sometime earlier.

Two simpler formalisms for defining HMS machine plans can be defined in terms of the plan languages PL0 and PL1, which can also be considered as languages for describing concurrent event sequences. Words in the language PL0 simply consist of sequences of (1) symbols from the set of transitions of the HMS machine, (2) lists of symbols, (3) words with integer exponents. An individual symbol α denotes the firing of the corresponding transition in the machine. A list of the form (α, β, ..., 8) denotes the simultaneous firings of the transitions α, β, ..., 8. A word of the form w^8 represents the n-fold repetition of firing of the transitions in w. Thus, the plan α (β, γ) (δn)^8 denotes the execution of the fol-

![Figure 3. A Plan Machine for the HMS Machine H1 in Figure 2.](image_url)
lowing transitions in a machine: first fire $\alpha$, then fire $\beta$ and $\gamma$ simultaneously, then fire $\delta$ followed by $\eta$ times. The language $PL_1$ extends $PL_0$ by the introduction of conditional operators and the means for defining alternative choices of actions. Plans in such languages, combined with an underlying HMS machine, provide the capability for both model-based reasoning from basic principles and the ability to respond rapidly to dynamic requirements without the need for searching.

Plan languages also offer the possibility of studying the scheduling of plans as distinct from the planning or plan generation process itself. For example, consider the plan

"Get in Car" "Start Driving to Airport"
"Arrive at Airport in Car"

in the plan language $PL_0$ for the machine $H_1$ of Figure 2. This plan simply lists the sequences of actions that must be performed, in which there is a key missing element: when should the actions be performed. Here, the only missing part is a delay of 45 minutes that must occur between the transitions "Start Driving to Airport" and "Arrive at Airport in Car." If such required delays are incorporated into a plan and it is verified for correctness, then the underlying machine can essentially be ignored during the execution. The important correctness criteria for plans are: (1) no transition is attempted that is not enabled, and (2) the plan will transform the machine from a given initial set of states to the desired final set of goal states.

In [5] a general approach for deriving schedules for plans was introduced that also provides a limited method of verifying the correctness of plans. In this scheme, given a potential plan $p'$, a "variable delay plan" $p$ is generated in which between each pair of terms in $p'$ a parametric delay $\phi^i$ is introduced, where $\phi$ denotes a wait or "no action." Using symbolic execution techniques, then a solution for the exponents of the $\phi$'s can often be found that guarantees the correctness of the plan. In addition, in many cases, misordered plans can be corrected in the process of finding the delays.

4. Conclusions and Future Work

Hierarchical Multi-State (HMS) machines provide a framework for specification, verification and control of complex real-time systems by integrating multi-state automata and temporal interval logic. The major benefits are: (1) significant reduction in state space, (2) convenient mechanisms for specifying both safety properties and conditional goals, including hard deadlines, (3) methods of verifying correctness of specifications, and (4) model-based reasoning approaches for planning and scheduling in dynamic environments.

Three directions for future work have been defined: theory, applications and tools. Theoretical research goals include (1) the extension and formalization of the specification language, (2) investigation of more powerful methods for capturing requirements, (3) verification methods, (4) representation of uncertainty relating to both incomplete knowledge about the world and probabilistic outcome of events, (5) introduction of learning, and (6) efficient planning and scheduling algorithms. Various potential application areas for HMS machine have also been identified. Currently, HMS machines are being applied to the specification of a fragment of a future European command and control system. As far as tool development plans are concerned, work is continuing on the development of a prototype environment for specification of HMS machines, along with the capabilities for interactive simulation, limited forms of animation, and verification.

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References


