CHARACTERIZATION OF SLOW AND FAST PHASE NYSTAGMUS

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ABSTRACT

A current literature review of the analog and digital processes of vestibular and optical kinetic nystagmus reveals little agreement in the methods used by various laboratories. The strategies for detection of saccade (fast phase velocity component of nystagmus) vary between laboratories, and most of the processes have not been evaluated and validated with a standard database. The purpose of this study is to survey major vestibular laboratories in the U.S. that perform computer analyses of vestibular and optokinetic reflexes to stimuli, and to establish a baseline from which to standardize data acquisition and analysis programs. The vestibular laboratories that cooperated in the evaluation were:

1. UCLA, Los Angeles, CA
2. MIT, Space Laboratory, Cambridge, MA
3. Pittsburgh, PA - Harvard, Cambridge, MA
4. USAF/SAM, Brooks AFB, San Antonio, TX
5. SBRI, JSC (NASA), Houston, TX

The concept of an Error Index was employed as the criterium for evaluating the performance of the vestibular analysis software programs. The performance criterium is based on the detection of saccades and is the average of the percentages of missed detections and false detections. Evaluation of the programs produced results for lateral gaze with saccadic amplitude of one (1), two (2), three (3), five (5) and ten (10) degrees with various signal-to-noise ratios. In addition, results were obtained for sinusoidal pursuit of 0.05 Hz, 0.10 Hz and 0.50 Hz with saccades from one (1) to ten (10) degrees at various signal-to-noise ratios.

Selection of the best program was made from the performance in the lateral gaze with three (3) degrees of saccadic amplitude and in the 0.10 Hz sinusoid with three (3) degrees of saccadic amplitude. The FPID program written for SBRI, NASA and the UCLA SINUXEC were the best overall. The FPID program produced errors less than 5% with signal-to-noise ratios of 2.5 or more, and the SINUXEC program produced errors less than 5% error at signal-to-noise ratios of 4.0 or more.
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CHAPTER I
INTRODUCTION

Although vestibular function tests have been employed for over eighty years, accepted formal standards for manual and computerized clinical evaluation of vestibular dysfunction have yet to be established in the United States. Without standards, vestibular clinics and laboratories perform similar tests with different data processing techniques [1]; therefore, test results from the various vestibular research laboratories are not directly comparable, thereby, hindering the overall process of vestibular dysfunction research. Detailed measurements of nystagmic movements are essential for the evaluation of vestibular and visual oculomotor reflexes [2], and standardization of vestibular function testing and data processing is necessary in order to unify clinical and laboratory vestibular function investigations in the United States.

With the increased usage of computers and digital signal processing techniques, many clinics and research laboratories record and analyze eye movement data with individually tailored software. The objective of this part of the study, entitled "Characterization of Slow and Fast Phase Nystagmus" (NASA Grant NAG 9-303, sponsored by the Space Biomedical Research Institute (SBRI), Space and Life Science Division, Johnson Space Center (JSC), National Aeronautics and Space Administration), is twofold:

1. To evaluate and compare computer programs used in the United States (programs which quantify, characterize, and analyze nystagmus components, i.e., slow phase velocity and saccades); and
2. To develop an automated nystagmus analysis program for NASA.

The scope of this report involves the evaluation of various computer programs used in the U.S. and their ability to analyze simulated and real electro-oculogram (EOG) data and completes Tasks 03 and 04 of the statement of work. Part I, "Survey of Vestibular Laboratories: Baseline for Standardization," which completed Task 01 and Part II, "Vestibular Function Tests
Standardization Proposal,” which completed Task 02, were submitted in 1988 and 1989, respectively. Copies of the Part II report were sent to the CHABA, Office of the National Research Council (NRC) and used in the final NRC Standard for Vestibular Dysfunction.

Evaluation of the various computer algorithms (Part III of the study) was divided into four efforts:

1. obtaining listings of programs currently used by vestibular laboratories in the United States,
2. creating a representative "data base" of ocular movement responses to various visual stimuli,
3. rewriting the various computer programs in FORTRAN 77 for evaluation on a VAX system, and
4. developing the criteria for evaluation and, subsequently, evaluating the various programs.

Vestibular laboratories in the United States, willing to cooperate and participate in the software evaluation phase, are: School of Aerospace Medicine (USAF/SAM), Brooks AFB, San Antonio, TX; UCLA Medical School, Los Angeles, CA; Space Research Laboratory, MIT, Cambridge, MA; Dr. C. Wall's Vestibular Laboratory, Harvard University, Cambridge, MA (C. Wall's program was obtained while he was at the Vestibular Laboratory, Pittsburgh, PA); and SBRI Vestibular Laboratory, JSC (NASA), Houston, TX. For the study conducted at Texas A&M University, these laboratories provided listings of the nystagmus analysis algorithms, along with permission to evaluate their algorithms.

A simulated (synthesized) nystagmus data base was developed and an experimental human subject nystagmus data base was acquired at the physiological signal processing facility, Texas A&M University, College Station, TX. The various nystagmus analysis algorithms, which perform nystagmus identification and characterization, were rewritten in FORTRAN 77 for use with the VAX computer system at Texas A&M and were evaluated on their accuracy in correctly detecting the occurrence of saccadic movements with the simulated and human EOG data sets. Each program was tested with the same sets of artificially generated EOG simulated...
The synthetic data sets simulate different types of eye movement (e.g., midposition gaze or sinusoidal) with and without superimposed nystagmus and random magnitude noise. The data sets generated with superimposed nystagmus have adjustable nystagmus amplitude and fast and slow phase velocities. Random noise is included with some data sets to test the accuracy of the programs in the presence of extraneous events. The intent is to simulate real data acquisition conditions, under which the signal-to-noise ratio (SNR) varies with recording conditions [3]. An Error Index is calculated for each data set tested to evaluate and compare the accuracy of the various programs under different recording conditions. Results from this evaluation logically lead to the second aspect of this study: to develop an automated or interactive ocular nystagmus analysis program for NASA.

In the second half of the study, the best program method or best parts of programs from the participating vestibular laboratories will be selected and modified for application to the SBRI. The Fast Phase Identification (FPID) nystagmus analysis program, which was originally written in FORTRAN by Dr. Charles S. Lessard [4] for use with the SBRI's LSI-11 system, automatically identifies fast phase nystagmus, reconstructs slow phase position and velocity waveforms and computes magnitude and phase of the response to sinusoidal stimulus.

The program FPID described in this report is a modified version of an original FORTRAN program developed for the DEC LSI-11 system. The code was modified to extend its use for personal computers, and the modified FPID is composed of two versions to run on different systems:

1. FPID.FOR: written in FORTRAN 77, for use with VAX, IBM mainframes.

2. FPID.C: written in C (Microsoft v.5.1), for use with IBM personal computers (PC's) or compatible personal computers.

These two different versions of the FPID program should meet the data analysis needs of most clinics or laboratories regardless of the data acquisition and computer system in use.
CHAPTER II
BACKGROUND

Evaluation of vestibular dysfunction is performed by analyzing a patient's eye movements during various test conditions. At the present, electronic methods are most commonly used in vestibular clinics and laboratories for measuring eye movements.

An eye movement measuring system consists of four subsystems: stimulation, detection, signal conditioning, and recording. To elicit eye movements, the stimulation system presents one or more stimuli provided by an array of LED's placed in front of the patient in both the horizontal and vertical directions. The array may be used to present step changes in position or smooth pursuit (sinusoidal) stimuli.

The resulting eye movement is detected by an eye movement detection system, of which the most popular is electro-oculography. The electro-oculography method for acquiring ocular movements relies on the corneo-retinal potential oriented along the long axis of the eye. Consequently, an electrode placed in the vicinity of the eye becomes more positive as the eye rotates toward the electrode and less positive when the eye rotates in the opposite direction [5]. The eye movement signals detected by EOG are small magnitude signals of about 20 μV/degree that require amplification gains of 1000 and lowpass filtering below 60 Hz before recording or displaying. Lowpass filters are used to eliminate high frequency noise due to the high gain of the system while highpass filters eliminate the effects of baseline drift caused by electrode capacitance changes.

Specialized software is often used to analyze eye position data in clinics and research laboratories; therefore, following the signal conditioning circuitry, analog to digital (A/D) conversions are necessary to digitally analyze the eye position data. The accuracy of the data analysis software is affected by the signal conditioning circuitry.

Vestibular dysfunction is characterized by abnormal eye movements commonly referred to
as nystagmus. Nystagmus is separated into two components or phases: fast and slow. The following terms are important in the clinical description of nystagmus [6]:

1. Beat mode
2. Conjugate or disconjugate eye movements
3. Plane of eye movement
4. Direction of fast and slow phases
5. Amplitude
6. Beat frequency
7. Velocity of the fast and slow phases
8. Changes in direction or amplitude
9. Influences of head position or changes of head position.

The parameters most commonly measured and analyzed by software are: direction, duration, peak velocity, average velocity, and beat frequency. Several programs exist for analyzing these parameters; however, each program uses its own method of feature extraction and parameter measurement. Each algorithm uses different criteria for fast and slow phase detection, velocity and duration estimation. Additionally, each algorithm is affected differently by extraneous events such as eye blinks and noise. The quantification of the nystagmus parameters are commonly used to locate and diagnose the cause of vestibular dysfunction. Identification of significant patterns in the eye movement could provide insight about the mechanism involved in the production of nystagmus, as well as the formulation of comprehensive models for nystagmus induced by a variety of stimuli [2]. The consistency and symmetry of saccade accuracy in normal subjects suggests that saccade accuracy measurements can be a sensitive clinical test of the oculomotor control system [7]. It is necessary, therefore, that the parameters be measured accurately and that these parameters be common for comparison. This approach should help standardize vestibular dysfunction testing analysis and facilitate direct comparison between laboratories.
CHAPTER III
EVALUATION CRITERIA

Performance in the detection of saccades formed the basis for development of a criteria by which to quantitatively evaluate the various nystagmus programs. The concept of an error index is employed as the criteria for evaluating the best performing vestibular analysis software program. Two error measures were used to evaluate the detection of saccades. The performance criterium consists of a weighted average of two classes of errors: the error of missed detection of a true saccade, and the error of false detection (detection of an event when a true saccade did not occur).

The method of evaluating the error in detection of a saccade consists of running the test data set through one of the analysis programs, i.e., UCLA, USAF, FPID, etc., and comparing when the program detects a fast phase component (during which samples) to when the fast phase (true saccade) really occurs in the test data. If the sample indices of the detected event were within the sample index interval (±2 samples or ±10 msec at 200 Hz sampling rate) of true saccade, the program was credited with correct detection of the event.

Missed-detection error ($E_1$) is calculated by subtracting the number of correctly detected fast phase components (saccades) from the total number of known true saccades in the record (Equation 1).

$$E_1 = \text{Total number of true saccades} - \text{Number of correctly detected saccades} \quad (1)$$

The percent missed-detection error is obtained by dividing the missed-detection error ($E_1$) by the total number of known true saccades in the test data and multiplying the quotient by 100 (Equation 2).

$$E_1\% = \left(\frac{E_1}{\text{total number of known true saccades}}\right)(100) \quad (2)$$
The false-detection error (E2) is calculated by subtracting the number of correctly detected saccades from the total number of events detected by the program (Equation 3).

\[ E2 = \text{Number of events detected by program} - \text{Number of correctly detected saccades} \] (3)

The percent false-detection error is obtained by dividing the false-detection error (E2) by the total number of events detected by the program and multiplying the quotient by 100 (Equation 4).

\[ E2\% = \left( \frac{E2}{\text{total number of detected saccades}} \right) \times 100 \] (4)

The Error Index (in percentage) is the average value of the missed-detection error and false-detection error percentages (Equation 5).

\[ \text{Error Index}\% = \frac{E1\% + E2\%}{2} \] (5)
Simulated Data Generation

The program, NASDAT, was developed to generate simulated midposition gaze and sinusoidal pursuit EOG data with which to evaluate the various nystagmus analysis computer programs. Fifteen seconds of artificial EOG data were generated for each test run and were stored in files to be read by each nystagmus analysis program. Figure 1 is a flowchart of the test data generation program, NASDAT.

At the beginning of the NASDAT program (Fig. 1), the operator has the option of generating either a simulated midposition gaze EOG data set or a simulated sinusoidal pursuit EOG data set. The program is initialized by entering values for several nystagmus parameters, (i.e., sampling rate, magnitude of saccades, direction of saccades, velocities, thresholds). The sampling rate (SR) is necessary to determine the time interval between data points. The velocity of the nystagmus components may be entered or calculated by dividing the product of the sampling rate and the magnitude of the saccadic jump by the number of points in the respective nystagmus component. For example, in calculation of the fast phase velocity (FPV) component, the denominator (#PTS) is the number of data points in the fast phase component of nystagmus; to determine the slow phase velocity (SPV), the denominator (#PTS) denotes the number of data points in the slow phase component of nystagmus.

Additionally, the data point ratio (DPR) may be entered or obtained by calculating the ratio between the number of fast phase data points and the number of slow phase data points. Simulated EOG data were generated with data point ratios of 1:5, 1:8, 1:10, 1:12, and 1:15.

The initialization subroutine requires data-specific parameters before simulated nystagmus data is generated (e.g., slow phase velocity). An example of the NASDAT program output is presented in Figure 2, where the simulated midposition gaze EOG data without noise resembles
a sawtooth waveform. Note that all fast phase events (saccades) are of equal magnitude and in the same direction. For the simulated sinusoidal pursuit EOG data, initial direction, frequency, and maximum amplitude of the base sinusoid waveform must be entered, as well as the data point ratio (DPR) and the slope difference threshold. The data point ratio is not entered for the gaze data because the parameter is calculated by the program from the fast phase and slow phase velocities entered by the user. The slope difference threshold is entered for simulated sinusoidal pursuit EOG data such that saccadic events do not occur at the maxima or minima of the base sinusoid, a necessary condition if the simulated EOG is to be consistent with human ocular responses during sinusoidal tracking tasks. The value of the slope difference threshold parameter was determined experimentally and set at 0.001 for the frequencies between 0.10 and 0.80 Hz.

After the program is initialized, the operator must decide if the addition of saccades is desired. If the operator desires to superimpose saccades (nystagmus beats) on the simulated base signal (midposition gaze or sinusoid), the operator must enter the desired magnitude of nystagmus beats (AMP) (one, two, three, five or ten degrees); then the desired direction of the nystagmus beat (upward beating or downward beating) is entered.

Normal ocular pursuit responses to sinusoidal stimulus consist of a base sinusoidal waveform with corrective saccades opposite to the direction of ocular movement. This convention assumes that, during normal ocular pursuit, prediction errors occur as subjects overshoot the stimulus. The simulated sinusoidal pursuit EOG data with superimposed saccades contain fast events opposite to the direction of the base sinusoid; therefore, fast events in both directions (upward and downward) occur within one cycle of data as shown in the NASDAT output (Fig. 3). The slow phase velocity is not entered for the simulated sinusoidal EOG data because the velocity can be determined from the knowledge of the frequency of the sinusoid.

Once the base waveform has been generated, the beginning and ending times of each fast phase are determined and the base waveform root-mean square value (BRMS) is calculated.
according to Equation (6):

\[
BRMS = \left( \frac{\sum_{i=1}^{N} (Y_i - \bar{Y})^2}{N} \right)^{0.5}
\]

where \(Y_i\) is the \(i^{th}\) data point and \(\bar{Y}\) is the mean value of the eye position data. The signal-to-noise ratio of the signal is calculated from the ratio of the base waveform RMS value (BRMS) to the RMS value of the added noise (NRMS). If noise is not added to the signal, SNR is arbitrarily set to infinity. After the data has been generated, the data and timing files are created. The data files contain one column of eye position data as well as data parameters, if so desired, at the end. The timing files contain beginning and ending times of each fast phase.

The velocities of the fast and slow phases of the simulated data were constant for each nystagmus amplitude at a given data point ratio. For example, Table I is a list of the slow and fast phase velocities for the 1/10 data point ratio. For more information on the execution of the NASDAT program consult the NASDAT Software User's Manual (Appendix A) before using the program.

**Table I.** Velocity of slow and fast phases as a function of nystagmus amplitude for simulated data with 1/10 data point ratio.

<table>
<thead>
<tr>
<th>Nystagmus Amplitude (°)</th>
<th>Slow Phase Velocity (°/sec)</th>
<th>Fast Phase Velocity (°/sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>6</td>
<td>66</td>
</tr>
<tr>
<td>2</td>
<td>13</td>
<td>133</td>
</tr>
<tr>
<td>3</td>
<td>20</td>
<td>200</td>
</tr>
<tr>
<td>5</td>
<td>33</td>
<td>333</td>
</tr>
<tr>
<td>10</td>
<td>60</td>
<td>666</td>
</tr>
</tbody>
</table>

**Human Subject Data**

Real EOG data were used to verify results obtained with the simulated EOG data. Human EOG data collected at the Texas A&M University Physiologic Signal Acquisition and Processing Laboratory were analyzed with the different programs to evaluate their performance
with human EOG data. Three types of data were analyzed: optokinetic pursuit, sinusoidal pursuit and pseudorandom pursuit. Figures 4A and 4B illustrate a five (5) second segment of the stimulus and optokinetic EOG response. The stimulus was presented at a constant velocity of 29.2 degrees/sec from -15 degrees to +15 degrees. The pattern of saccades followed by smooth pursuit was generated as the subject tried to fixate on the repeatable, unidirectional stimulus appearing in the field of vision at -15 degrees (i.e., entering the field of vision) and disappearing at +15 degrees (i.e., leaving the field of vision). Although the saccades in this data set are not true fast phases, the readily identifiable events make this a suitable data set for analysis. The sinusoidal stimulus had an amplitude of 20 degrees and a frequency of 0.10 Hz. Figure 5 illustrates the sinusoidal pursuit stimulus and response collected during a 10-second period. The pseudorandom stimulus consisted of the sum of eight (8) sinusoidal frequencies ($f_1 = 0.015$ Hz; $f_2 = 0.026$ Hz; $f_3 = 0.050$ Hz; $f_4 = 0.096$ Hz; $f_5 = 0.190$ Hz; $f_6 = 0.378$ Hz; $f_7 = 0.751$ Hz and $f_8 = 1.500$ Hz). Pseudorandom data were collected during a four minute period [8]; however, only six (6) seconds from a pseudorandom data set were analyzed as part of this study. Figures 6A and 6B illustrate the pseudorandom stimulus and EOG response used for program evaluation. The human subject data were low-pass filtered at 45 Hz before sampling at 200 Hz.
CHAPTER V
DESCRIPTION OF PROGRAMS AND RESULTS

Presentation of material in this section is arranged by laboratory. The nystagmus analysis program of each laboratory is briefly described before performance results from synthetically generated data then human subject data, respectively. The order of presentation by laboratory are USAF/SAM, UCLA, MIT, Harvard, and NASA/SBRI laboratories. In all cases, input parameters were set according to instructions from or after discussion with the respective laboratory. Once set, the input parameters were not reset. The rationale for not fine tuning threshold parameters for each run is based on the desire to obtain the dynamic range of operation for each program in a minimum hands-on, automated mode.

U. S. Air Force Nystagmus Analysis Program

The eye movement analysis program obtained from the U. S. Air Force was developed by the Data Science and Clinical Science Division, United States Air Force School of Aerospace Medicine in Brooks Air Force Base, San Antonio, Texas. The flowchart of the overall program, shown in Figure 7, depicts the overall structure of the data analysis program. The program, written to analyze data on-line, consists of a main program, written in FORTRAN, and a number of sub-programs, written in assembly language. The program requires initialization of three parameters, CALSUM, KLIMIT and ILIMIT. The Air Force program consists of a calibration section, a data collection and analysis section, and an exit section. The sub-programs are called by the main program to perform initialization of hardware, clear memory spaces, control the motorized rotational chair, control data collection, and perform fast phase detection. Only the two fast phase detection algorithms (HLOGIC and MLOGIC), pertinent to this study, were converted from assembly language to FORTRAN 77 for evaluation. Other on-line processing algorithms were not re-coded and are not discussed in
this report. A minor modification was made to read test data from a file rather than from an
analog-to-digital (A/D) converter.

**Description of the Algorithm**

**Calibration Subroutine:** The calibration section was written to: 1.) control the
presentation of a constant velocity stimulus to the subject; 2.) calculate the eye velocity to the
eye position conversion factor; and 3.) determine the velocity threshold for fast phase
detection. Thus, in this program the user need not enter any parameter. The calibration
section, which is depicted by the flowchart shown in Figure 8, controls an optokinetic stimulus
to turn clockwise and then counterclockwise at a constant velocity of 30 degree/sec for 10.48
seconds in each direction. When used on-line, the EOG data were filtered by a precision
(3-second time constant), one (1) pole analog RC high-pass filter before digitization [9].

For this study, all simulated data are filtered with an equivalent digital highpass filter which
simulated the one-pole analog RC highpass filter. The filtered and digitized EOG data are read
and processed point by point by two specially designed 31-point, finite impulse response
(FIR), velocity and acceleration digital filters. The output of the velocity digital filter is a
measure of eye velocity, whereas, the output of the acceleration filter is a measure of eye
acceleration. Accordingly, these filters remove the effects of the RC filter and high frequency
noise [9]. The instantaneous eye velocity and eye acceleration are compared to predetermined
corresponding thresholds KLIMIT and ILIMIT, respectively. When either threshold is
exceeded, the eye velocity value is set to zero because it is assumed that a fast phase has been
detected. Then, the processed eye velocity data are separated into the left and the right-going
parts and are further processed to remove overshoots and undershoots caused by the digital
velocity filter. Subsequently, left- and right-going eye velocity calibration data are averaged
individually to obtain the calibrated factor for the person's left- and right-eye movements. An
overall calibration factor, CALSUM, is calculated from the left calibration factor, the right
calibration factor, and an empirically determined factor. The velocity threshold, \( K_{\text{LIMIT}} \), is updated to 2.5 times the value of the right calibration factor. Both the \( \text{CALSUM} \) and the \( K_{\text{LIMIT}} \) are used in the analysis subroutine.

**Analysis Subroutine**: In the analysis section, which is illustrated by the flowchart in Figure 9, the high-pass filtered input data passed through the same digital velocity and acceleration filters used in the calibration section. The instantaneous eye acceleration is compared to the preset acceleration threshold (same as in the calibration section). If the instantaneous eye acceleration is larger than the preset threshold, an event is said to have occurred. The algorithm \( H_{\text{LOGIC}} \) sets a fast phase flag \( ISHIFT \) and maintains \( ISHIFT \) set during the period in which the eye acceleration exceeds the threshold. When the eye acceleration drops below the threshold, the \( ISHIFT \) is kept set by \( M_{\text{LOGIC}} \) for the next five additional input data points. The instantaneous eye velocity is set to zero when the \( ISHIFT \) flag is set or when the eye velocity exceeded the threshold \( K_{\text{LIMIT}} \) (calculated in the calibration section). For example, a probable fast phase is indicated by a series of zeroes in the processed eye velocity data. The locations of zeroes correspond to the non-zero locations of \( ISHIFT \). Thus the values of \( ISHIFT \) are extracted and output to a file for later fast phase identification performance evaluation. The latter part of the analysis program performs the following tasks:

1. Remove fast phases
2. Reconstruct the slow phase waveform
3. Average the reconstructed slow phase
4. Filter the averaged slow phase, and
5. Multiply the final filtered slow phase by the scale correction factor \( \text{CALSUM} \) to scale in degrees.

In addition, the program displays, on CRT, graphs of filtered, scaled slow phase eye position,
and input stimulus. Based upon the eye position data given in the graph, the operator may decide to save the data or to collect another segment of data. Since the functions performed by the latter part of the analysis program, i.e., reconstructing, filtering and scaling, are pertinent to this research, these functions were not evaluated.

Because the U. S. Air Force program does not provide a fast phase indication file, fast phase identification information is extracted and output to a file. The fast phase identification (FPI) data and the nystagmus timing (NI) data are read by a performance evaluation program called "PERFORM." PERFORM aligns timing points of FPI data with the NI data timing by shifting the FPI data 15 data points to correct for the time delay produced by the 31-point digital velocity filter. One additional offset point was allowed between the FPI and NI data. If the FPI data indicates a fast phase event when the NI data does not contain a saccadic jump, then a false detection is said to have occurred; conversely, if the FPI data does not indicate a fast phase event, yet the NI data contains a saccadic jump, then a missed detection is said to have occurred. The Air Force nystagmus analysis program was not evaluated for its accuracy in the timing of fast phases because the program was not written to detect ending points of saccades.

Simulated Data Parameters

Simulated EOG data used to evaluate the US Air Force nystagmus program had a sampling period of approximately 16 msec. (i.e., 62 Hz sampling frequency). Each data file was 400 seconds in length. The simulated midposition gaze and sinusoidal pursuit data were generated with simulated saccadic jumps of one, two, three, five, and ten degrees of magnitude. The simulated sinusoidal pursuit data contained saccades of one two, three, and five degrees superimposed on sinusoids of 0.05, 0.10, 0.50 Hz, and 0.80 Hz. The amplitude of the sinusoidal pursuit data sets was 20 degrees. The data were not filtered through an anti-alias filter.
Results with Simulated Midposition Gaze Data

The results of the simulated midposition gaze test at each of five saccadic amplitudes (one, two, three, five, and ten degrees) with a 1/10 data point ratio, show a decrease in performance of the program with an increase in the magnitude of the nystagmus saccadic jump. As shown in Figure 10, the Air Force program does not produce any errors with simulated data containing saccadic jumps of two (2) degrees until the signal-to-noise ratio (SNR) is less than six. For the simulated data containing saccadic jumps of three (3) and five (5) degrees, the program does not produce detection errors until the SNR is less than 10 and 17, respectively. For saccades of ten (10) degrees, the Error Index remained about 11%, even at a SNR of 100, as shown in Figure 11. Generally, the false-detection errors are larger than the missed-detection errors except for data sets containing saccadic jumps of five (5) and ten (10) degrees at SNR above six (6) and 12, respectively. The reversal of missed-detection and false-detection error magnitudes for five (5) degrees and ten (10) degrees is attributed to the use of fixed thresholds to detect fast phases. When random noise is superimposed on a large magnitude saccade, the period during which the velocity and acceleration thresholds are exceeded becomes increasingly longer as larger magnitude noise is added. HLOGIC, which is used to keep track of the period during which the eye acceleration exceeds the acceleration threshold, maintains the fast phase flag ILIMIT in the valid state for an extended period. At the end of this period, only one count of fast phase detection is credited toward the program; whereas, several fast phases may have occurred during this period, and are considered being "missed detected." Thus, the false detection counts decrease; however, the number of missed detections increases as the magnitude of random noise increases. The combined error curves for the various magnitudes of saccade are shown in Figure 12. The general trend of degradation in performance as the saccadic magnitude increased from two (2) to ten (10) degrees is also the consequence of fixed velocity and acceleration thresholds. Analysis of the one (1) degree data indicates a high percentage of missed-detection error and is not illustrated in
Results with Simulated Sinusoidal Pursuit Data

The U. S. Air Force program was evaluated with simulated sinusoidal pursuit EOG data at five magnitudes (one, two, three, five, and ten degrees), four frequencies (0.05, 0.10, 0.50 and 0.80 Hz), and a data point ratio of 1/10. Results of 0.8 Hz sinusoid with two (2) degree saccades (Fig. 13) indicate that the program was not designed for sinusoids at 0.8 Hz since the maximum velocity of the slow phase at 0.8 Hz is larger than the velocity threshold set by the program. The fixed velocity threshold causes the HLOGIC to set the fast phase flag at wrong locations and/or for extended periods of time; thus, results at 0.8 Hz are considered to be erroneous and questionable.

The percentage of missed-detection and false-detection errors in the USAF program is illustrated in Figure 13. This figure, typical of the error profile for all the nystagmus amplitudes tested, indicates that at SNR greater than 20 the performance of the USAF/SAM nystagmus analysis program is good, i.e., detection errors of 5% or less. The performance decreases (greater detection errors) as the magnitude of the saccadic jumps is increased from two (2) to ten (10) degrees for the same value of SNR (Fig. 15). The false-detection errors are larger than the missed-detection errors as the amplitude of the noise is increased (decrease in SNR). A decrease in the false-detection error, shown in Figure 14, occurs at SNR less than five (5) when the HLOGIC maintains the fast phase flag for an extended period of time.

The Error Index for the frequencies tested (Figs. 15 - 18) indicates that the program is consistent and independent of sinusoidal frequencies between 0.05 Hz and 0.50 Hz. The performance degrades about 10% at 0.50 Hz when compared to either 0.05 or 0.10 Hz for the larger magnitude saccades (five and ten degrees). The "zigzagging" nature of errors when the SNR is less than nine (9) is an indication that the program performance is inconsistent or unreliable at low SNR. The Error Index profiles shown in Figures 15 through 18 indicate that
the program performance is better with small amplitude saccades (two degrees) and large amplitudes of noise (i.e., small SNR) than with large amplitude saccades (ten degrees). The best overall performance of the program occurs with the 0.10 Hz sinusoidal waveform with three degree saccades. The results for the one (1) degree of saccadic jump at all frequencies are erratic and unreliable. The frequency limitation of the US Air Force program at 0.80 Hz is illustrated in Figure 18.

Results with Human Subject Data

Optokinetic, sinusoidal pursuit, and pseudorandom pursuit data collected from human subjects were analyzed with the USAF/SAM nystagmus program. The human subject data were collected at 200 Hz; however, as the Air Force program uses a sampling rate of 61.445 Hz [10], a sampling rate conversion was performed on the data to bring the effective sampling rate to 62 Hz. The time marks identified by hand-scoring subject data with a sampling rate of 200 Hz were adjusted to the corrected sampling rate of 62 Hz before the program was evaluated. Fast phase timing information is not included in the output as the Air Force program does not provide timing information.

Table II summarizes the fast phase detections of the program with corresponding magnitude of saccade. For the optokinetic data set, five (5) saccades were missed, resulting in 38.46% missed-detection error; and 13 saccades were falsely identified, resulting in 61.9% false-detection error. The Error Index for the optokinetic data set is 51.18%.

Results with the sinusoidal pursuit data set (0.10 Hz) indicate very high false-detection errors and high missed-detection errors. The results are summarized in Table III. The USAF/SAM program identified 36 fast phases; two of the five true fast phases were detected, resulting in 60.0% missed-detection error, and 34 fast phases were falsely detected, resulting in 94.44% false-detection error. The Error Index for the human sinusoidal pursuit data is 77.22%.
Table II. Results from the analysis of human optokinetic data by USAF/SAM Program.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Amplitude (°)</th>
<th>Detection Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>8.0</td>
<td>detected</td>
</tr>
<tr>
<td>2</td>
<td>15.6</td>
<td>detected</td>
</tr>
<tr>
<td>3</td>
<td>18.0</td>
<td>missed</td>
</tr>
<tr>
<td>4</td>
<td>5.6</td>
<td>detected</td>
</tr>
<tr>
<td>5</td>
<td>18.0</td>
<td>detected</td>
</tr>
<tr>
<td>6</td>
<td>14.2</td>
<td>detected</td>
</tr>
<tr>
<td>7</td>
<td>12.4</td>
<td>detected</td>
</tr>
<tr>
<td>8</td>
<td>14.6</td>
<td>detected</td>
</tr>
<tr>
<td>9</td>
<td>13.6</td>
<td>detected</td>
</tr>
<tr>
<td>10</td>
<td>16.2</td>
<td>missed</td>
</tr>
<tr>
<td>11</td>
<td>19.2</td>
<td>missed</td>
</tr>
<tr>
<td>12</td>
<td>20.2</td>
<td>missed</td>
</tr>
<tr>
<td>13</td>
<td>5.4</td>
<td>missed</td>
</tr>
</tbody>
</table>

Table III. Results from the analysis of human sinusoidal pursuit data by USAF/SAM Program.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Amplitude (°)</th>
<th>Detection Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3.0</td>
<td>missed</td>
</tr>
<tr>
<td>2</td>
<td>3.0</td>
<td>detected</td>
</tr>
<tr>
<td>3</td>
<td>3.0</td>
<td>detected</td>
</tr>
<tr>
<td>4</td>
<td>3.0</td>
<td>missed</td>
</tr>
<tr>
<td>5</td>
<td>4.0</td>
<td>missed</td>
</tr>
</tbody>
</table>

Results with the pseudorandom data indicate equal percentages of missed-detection and false-detection errors. Table IV summarizes the results of the pseudorandom data analysis. A total of 14 fast phases were identified by the program; six (6) were false detections, resulting in a 42.85% false-detection error, and eight (8) were correct identifications (i.e., six (6) fast phases were missed), again resulting in 42.85% missed-detection error. The Error Index for the pseudorandom data set is 42.85%. Examination of Table IV for the saccadic amplitude corresponding to missed detection of a fast phase reveals that a greater number of large magnitude fast phases were missed than were small magnitude fast phases, results which are in agreement with those obtained from simulated nystagmus data.
Table IV. Results from the analysis of human pseudorandom data by USAF/SAM Program.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Amplitude (°)</th>
<th>Detection Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3.2</td>
<td>detected</td>
</tr>
<tr>
<td>2</td>
<td>2.7</td>
<td>detected</td>
</tr>
<tr>
<td>3</td>
<td>4.0</td>
<td>detected</td>
</tr>
<tr>
<td>4</td>
<td>4.5</td>
<td>missed</td>
</tr>
<tr>
<td>5</td>
<td>3.7</td>
<td>detected</td>
</tr>
<tr>
<td>6</td>
<td>4.6</td>
<td>detected</td>
</tr>
<tr>
<td>7</td>
<td>5.2</td>
<td>missed</td>
</tr>
<tr>
<td>8</td>
<td>3.8</td>
<td>missed</td>
</tr>
<tr>
<td>9</td>
<td>5.0</td>
<td>missed</td>
</tr>
<tr>
<td>10</td>
<td>4.8</td>
<td>missed</td>
</tr>
<tr>
<td>11</td>
<td>5.3</td>
<td>detected</td>
</tr>
<tr>
<td>12</td>
<td>5.8</td>
<td>missed</td>
</tr>
<tr>
<td>13</td>
<td>5.0</td>
<td>detected</td>
</tr>
<tr>
<td>14</td>
<td>3.0</td>
<td>detected</td>
</tr>
</tbody>
</table>

UCLA Nystagmus Analysis Programs

The University of California at Los Angeles (UCLA) vestibular research laboratory developed two programs (SINUXEC and CALORXEC) to analyze eye movements. The programs identify saccadic eye movements on the basis of minimum velocity and duration criteria, and measure saccadic amplitude, duration, and maximum velocity [11]. The first program analyzes sinusoidal pursuit or rotational test eye position data, and the second program analyzes gaze test eye position data. Because both programs contain several parameter input and plotting subroutines, the fast component identification (FCID) portions of the programs were extracted and analyzed separately.

The UCLA programs were designed to analyze data on-line; therefore, the fast component identification is performed at the assembly language level as the data is collected. The assembly language code was developed with the PDP-11 computer (Digital Equipment Corporation) [12]. To test the FCID portions of the programs, the algorithms were converted to FORTRAN so that the VAX system at Texas A&M University could be used to evaluate the analysis algorithms. The assembly language commands were converted on a one-to-one basis.
to equivalent fortran commands. Parameters, necessary for the programs to run, are entered by the user before each program run. Both programs analyze one data point at a time from an input eye position data file. The necessary parameters are checked, updated, and written to an output data file.

**SINUXEC Program**

**Description of the Algorithm**

The sinusoidal pursuit execution (SINUXEC) program is used with eye position data created during the pursuit or rotational test. The program initializes the following fast component (FC) parameters:

1. FC direction (IDIREC)
2. Minimum FC duration (MINDUR)
3. Maximum FC duration (MAXDUR)
4. Minimum FC amplitude (MINAMP)
5. Minimum peak velocity (MINPKV)
6. Minimum FC velocity (MINVEL).

Because the program analyzes each data point during data collection, the FC parameters are scaled by the sampling rate (SR) to obtain the parameters in terms of the number of samples rather than the timing of each sample.

The flowchart for the SINUXEC program is shown in Figures 19A and 19B. The SINUXEC program begins execution by calculating the difference between the \( n^{th} \) and \( n^{th} + 2 \) sample points (derivative function with a two-point central difference equation). The absolute value of this difference is stored, and the direction flag set to 1 if the difference is positive (right) or to -1 if the difference is negative (left). Then the program determines if a FC has started, and if not, the start time, start amplitude, and direction are stored. The FC duration counter is incremented, and the current difference compared to the maximum difference for that
FC. If the current difference is greater than the maximum difference, the current difference is stored; otherwise, the program processes the next data point.

The program checks the direction of the fast component (FC) difference with the previous difference. If the directions are not the same, the end of a FC may have occurred; then the program checks the current FC parameter values with the limit values entered by the user. If the directions are the same and the pursuit test performed, the current difference is compared to MINVEL. If the current difference is less than MINVEL, the program branches and checks the FC parameters against the limit values entered by the user. If it is not a pursuit test or the current difference is greater than MINVEL - the SINUXEC program increments the FC duration counter, stores the value of the maximum difference, and returns to process the next data point.

If an end to a FC is identified, the FC duration counter is compared to MINDUR and MAXDUR. If the duration counter is greater than MINDUR and less than MAXDUR, the maximum difference is compared to MINPKV. If the difference is greater than MINPKV, the starting amplitude is subtracted from the ending amplitude and the absolute difference is compared to MINAMP. If the difference is greater than MINAMP and the direction is the same as IDIREC, the program stores the following parameters [11]:

1. Starting time
2. Starting position
3. Ending time
4. Ending position
5. Maximum difference (maximum velocity).

The maximum difference is converted back to maximum velocity and stored in an output file with the other parameters; then the program clears the parameters. If any of the comparisons failed, the program clears the FC duration counter, the maximum difference register and returns to process the next data point.
Simulated Data Parameters

The simulated data analyzed by the SINUXEC program had a sampling period of 5 msec. (i.e., 200 Hz sampling frequency) and the length of each data file was 15 seconds. The simulated midposition gaze data were generated with saccades of one, two, three, five, and ten degrees. The simulated sinusoidal pursuit data contained saccades of one, two, three, and five degrees superimposed on sinusoids of 0.05, 0.10, and 0.50 Hz. The amplitude of the sinusoidal pursuit data sets was 20 degrees. The data were filtered with a simulated anti-alias digital filter with cutoff at 40 Hz.

Results with Simulated Midposition Gaze Data

The SINUXEC program is very consistent in analyzing the simulated midposition gaze data. Figure 20 illustrates the missed- and false-detection errors and the Error Index for the midposition gaze data with one (1) degree nystagmus. The missed-detection error ratio is low (less than 5%) for all SNR, but the false-detection error ratio increases as the SNR is decreased below four (4). The false detection-error ratio is responsible for the Error Index profiles illustrated in Figure 21. Figures 21 and 22 illustrate the consistency of the SINUXEC program in its detection capability as a function of SNR and amplitude of saccades. Figure 22 shows that the majority of errors are false detections of saccades in the analysis of midposition gaze data.

Results with Simulated Sinusoidal Pursuit Data

The results from the analysis of the simulated sinusoidal pursuit data are not as clear as those from the analysis of midposition gaze data. Apparently, the accuracy of the analysis is dependent on the frequency of the sinusoid and the amplitude of nystagmus. Figure 23 illustrates the results of the analysis of sinusoidal pursuit data at a frequency of 0.50 Hz. The plot shows the high Error Index for the data set with one (1) degree nystagmus with a decrease
in the Error Index as nystagmus amplitude is increased. High incidence of missed and false
detections is observed at all frequencies for the one (1) degree nystagmus data set. For all
other amplitudes as previously observed with the midposition gaze data; however, the results
show a high number of false detections with a low number of missed detections. Figures 24
and 25 summarize the Error Index performance of SINUXEC for sinusoidal pursuit data at
0.05 Hz and 0.10 Hz, respectively. In summary, the performance of the SINUXEC program
in analyzing sinusoidal pursuit data, as with midposition gaze data, is consistent in producing
low missed-detection errors but high false-detection errors (Fig. 26).

Results with Human Subject Data

The SINUXEC program requires the user to input several nystagmus parameters prior to
analyzing the data. With results from the simulated data analysis and a priori knowledge of the
stimulus parameters used in collecting the human data, the input parameters for the SINUXEC
are:

1. Minimum saccadic amplitude- 3 degrees
2. Minimum saccadic duration- 0.015 sec.
3. Maximum saccadic duration- 0.050 sec.
4. Minimum peak saccadic velocity- 150 degrees/sec.
5. Minimum slow component velocity- optokinetic: 30 degrees/sec.,
sinusoidal: 8 degrees/sec., pseudorandom: 6 degrees/sec.

The optokinetic data set generates high missed-detection and false-detection errors. Table
V summarizes the results of the analysis of the human optokinetic data with the SINUXEC
program. Nine (9) saccades out of 13 were missed, resulting in a 69.23% missed-detection
error; and eight (8) events were falsely identified as saccades, resulting in 66.67% false-
detection error. The combined Error Index for the optokinetic data set is 67.95%.
Table V. Results from the analysis of human optokinetic data by SINUXEC Program.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Start</th>
<th>End</th>
<th>Amplitude</th>
<th>Start</th>
<th>End</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.350</td>
<td>0.380</td>
<td>8.0</td>
<td>0.360</td>
<td>0.395</td>
</tr>
<tr>
<td>2</td>
<td>0.850</td>
<td>0.900</td>
<td>15.6</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>3</td>
<td>1.735</td>
<td>1.790</td>
<td>18.0</td>
<td>1.750</td>
<td>1.800</td>
</tr>
<tr>
<td>4</td>
<td>2.155</td>
<td>2.185</td>
<td>5.6</td>
<td>2.165</td>
<td>2.195</td>
</tr>
<tr>
<td>5</td>
<td>2.710</td>
<td>2.775</td>
<td>18.0</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>6</td>
<td>3.580</td>
<td>3.650</td>
<td>14.2</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>7</td>
<td>4.495</td>
<td>4.550</td>
<td>12.4</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>8</td>
<td>5.635</td>
<td>5.705</td>
<td>14.6</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>9</td>
<td>6.580</td>
<td>6.640</td>
<td>13.6</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>10</td>
<td>7.790</td>
<td>7.865</td>
<td>16.2</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>11</td>
<td>8.975</td>
<td>9.035</td>
<td>19.2</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>12</td>
<td>10.125</td>
<td>10.190</td>
<td>20.2</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>13</td>
<td>10.665</td>
<td>10.695</td>
<td>5.4</td>
<td>10.675</td>
<td>10.710</td>
</tr>
</tbody>
</table>

Table VI summarizes the results from the analysis of the sinusoidal data from human subjects which indicate low false-detection error and high missed-detection error. The SINUXEC program did not detect any fast phases in the sinusoidal pursuit data set, resulting in 100% missed-detection error, 0% false-detection error, and an overall 50% Error Index for the human sinusoidal pursuit data. The results from the subject data analysis differ from the results of the analysis of 0.10 Hz simulated sinusoidal data, where the false-detection error is higher than the missed-detection error (Fig. 26).

Table VI. Results from the analysis of human sinusoidal pursuit data by SINUXEC Program.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Start</th>
<th>End</th>
<th>Amplitude</th>
<th>Start</th>
<th>End</th>
<th>SNR</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2.855</td>
<td>2.870</td>
<td>3.0</td>
<td>-</td>
<td>-</td>
<td>1.67</td>
</tr>
<tr>
<td>2</td>
<td>5.125</td>
<td>5.145</td>
<td>3.0</td>
<td>-</td>
<td>-</td>
<td>1.93</td>
</tr>
<tr>
<td>3</td>
<td>7.100</td>
<td>7.120</td>
<td>3.0</td>
<td>-</td>
<td>-</td>
<td>1.50</td>
</tr>
<tr>
<td>4</td>
<td>9.425</td>
<td>9.445</td>
<td>3.0</td>
<td>-</td>
<td>-</td>
<td>1.61</td>
</tr>
<tr>
<td>5</td>
<td>9.545</td>
<td>9.570</td>
<td>4.0</td>
<td>-</td>
<td>-</td>
<td>2.03</td>
</tr>
</tbody>
</table>

The pseudorandom EOG data set has higher SNR than does the sinusoidal EOG data set; therefore, the performance of the SINUXEC program improved. Table VII summarizes the results of the pseudorandom data analysis. Only two (2) saccades were missed, and no false
detections recorded, resulting in a 14.28% missed-detection error, a 0% false-detection error, and an overall 7.14% Error Index for the human pseudorandom data.

Table VII. Results from the analysis of human pseudorandom data by SINUXEC Program.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Hand-scored Start</th>
<th>Hand-scored End</th>
<th>Computer Start</th>
<th>Computer End</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.603</td>
<td>0.650</td>
<td>3.2</td>
<td>0.640</td>
</tr>
<tr>
<td>2</td>
<td>0.865</td>
<td>0.885</td>
<td>2.7</td>
<td>-</td>
</tr>
<tr>
<td>3</td>
<td>1.150</td>
<td>1.175</td>
<td>4.0</td>
<td>1.160</td>
</tr>
<tr>
<td>4</td>
<td>1.465</td>
<td>1.490</td>
<td>4.5</td>
<td>1.475</td>
</tr>
<tr>
<td>5</td>
<td>1.710</td>
<td>1.730</td>
<td>3.7</td>
<td>1.720</td>
</tr>
<tr>
<td>6</td>
<td>2.505</td>
<td>2.525</td>
<td>4.6</td>
<td>2.515</td>
</tr>
<tr>
<td>7</td>
<td>2.710</td>
<td>2.735</td>
<td>5.2</td>
<td>2.725</td>
</tr>
<tr>
<td>8</td>
<td>3.005</td>
<td>3.030</td>
<td>3.8</td>
<td>3.015</td>
</tr>
<tr>
<td>9</td>
<td>3.725</td>
<td>3.755</td>
<td>5.0</td>
<td>3.740</td>
</tr>
<tr>
<td>10</td>
<td>4.065</td>
<td>4.090</td>
<td>4.8</td>
<td>4.075</td>
</tr>
<tr>
<td>11</td>
<td>4.295</td>
<td>4.325</td>
<td>5.3</td>
<td>4.305</td>
</tr>
<tr>
<td>12</td>
<td>4.975</td>
<td>5.005</td>
<td>5.8</td>
<td>4.985</td>
</tr>
<tr>
<td>13</td>
<td>5.205</td>
<td>5.235</td>
<td>5.0</td>
<td>5.220</td>
</tr>
<tr>
<td>14</td>
<td>5.750</td>
<td>5.775</td>
<td>3.0</td>
<td>-</td>
</tr>
</tbody>
</table>

**CALORXEC Program**

**Description of the Algorithm**

The gaze test execution program (CALORXEC) analyzes eye position data produced during the midposition gaze test. The flowchart for the CALORXEC program is shown in Figures 27A and 27B. The program begins by initializing the following fast component identification (FCID) parameters used by the FCID portion of the CALORXEC program:

1. Minimum duration (DURMIN), expressed in number of samples
2. Minimum amplitude (MINAMP)
3. Fast Component direction (DIRFC).

Similar to the SINUXEC program, the CALORXEC program is an on-line analysis program that analyzes the eye position data, point-by-point as the data is sampled. The program stores the absolute difference of the \(n\)th and \((n+1)\)th data points and sets the direction flag to one (1) if the difference is positive (right) and to minus one (-1) if the difference is negative (left). Subsequently, the program checks for the start of a fast component (FC) and,
if a fast component has started, the program branches to compare the previous direction with the current direction. If a fast component has not started, the program stores the start time, the current amplitude, and the current direction before comparing the previous direction to the current direction. If the previous direction is the same as the current direction, the FC duration counter is incremented and the current difference is compared to the maximum difference for the current FC. If the current difference is greater than the maximum difference, the current difference is stored as the new maximum difference. The program then returns to process the next data point.

If the current direction differs from the previous direction, a possible end of the current FC may have occurred; then, the program branches and compares the FC duration counter to DURMIN. If the FC duration is not greater than DURMIN, the program clears the FC duration counter and maximum difference register before returning to process the next data point. Otherwise, the program branches and calculates the absolute FC amplitude from the difference between the starting amplitude and the current amplitude. Before comparing the current FC amplitude to MINAMP, the program determines if the current FC is consistent with DIRFC. If the current amplitude is not greater than MINAMP or if the directions are not consistent, the program clears the FC duration counter and maximum difference register before returning to process the next data point. Otherwise, the program increments the variable NSAC (the number of saccades) and then compares the value in NSAC to the maximum number of saccades allowed per data record. If NSAC is less than the maximum, the program stores the following FC parameters to a data file:

1. Starting time
2. Starting amplitude
3. Ending time
4. Ending amplitude
5. Maximum difference.
After storing the current FC parameters or if NSAC is greater than the maximum, the program clears the FC duration counter and returns to the next data point.

**Simulated Data Parameters**

The simulated data analyzed by the CALORXEC program had a sampling period of 5 msec. \( (i.e., 200 \text{ Hz sampling frequency}) \), and the length of each data file was 15 seconds. The simulated midposition gaze data were generated with saccades of one, two, three, five, and ten degrees in magnitude. The simulated sinusoidal pursuit data, which was filtered with an anti-alias filter \( f_c = 40 \text{ Hz} \), contained saccades of one, two, three, five, and ten degrees superimposed on sinusoids of 0.05, 0.10, and 0.50 Hz. The amplitude of the sinusoidal pursuit data sets was 20 degrees.

**Results with Simulated Mid-position Gaze Data**

The CALORXEC nystagmus analysis program was initially evaluated with simulated midposition gaze data. No errors, \( i.e., 0\% \) Error Index, are observed for the gaze data without noise at the five saccadic amplitudes (one, two, three, five, and 10 degrees) and different data point ratios, \( i.e., \) number of fast phase data points to slow phase data points (1:5, 1:8, 1:10, 1:12, and 1:15).

Figure 28 shows the effect of adding noise to midposition gaze data containing the five amplitudes of saccade. The best results are obtained for 10-degree saccades for SNR's less than 20. The program produces significant errors for one (1) degree saccades. Acceptable results (Error Index of 5% or less) are obtained for saccadic amplitudes greater than one degree with signal-to-noise ratios greater than 33. Figure 29 shows that the reason for the high Error Index is the high value of missed-detection error.
Results with Simulated Sinusoidal Pursuit Data

The next test series evaluated the performance of the UCLA CALORXEC Program with simulated sinusoidal pursuit data without noise. Data with three different ratios of fast phase to slow phase data points (1:5, 1:10, and 1:15) were analyzed.

For the sinusoidal pursuit data with 3 degrees nystagmus at 0.05 Hz and 0.10 Hz, the CALORXEC program produces 100% missed-detection errors, which are caused by the inability of the program to differentiate between the slow and the fast phases at these frequencies (Fig. 30). Figure 31 illustrates the results of the analysis of sinusoidal pursuit data with 3 degrees nystagmus at the three sinusoidal frequencies. The high Error Indexes at 0.05 Hz and 0.10 Hz are caused by the high frequency of missed-detection errors shown in Figure 30.

Results with Human Subject Data

Comparison of the two UCLA programs, SINUXEC and CALORXEC, by Schmidt [13] showed that for every test condition the SINUXEC program always produces significantly better results than the CALORXEC program. Therefore, only the UCLA SINUXEC program was evaluated with actual human data.

MIT Program (M2MI86)

The Massachusetts Institute of Technology nystagmus analysis programs M2MI86 and M2DETE were developed by Mohammad-Ali Massoumnia under contract NAS-W-3651, NASA (Washington) and contract NAS-9-15343, NASA (Houston). The only difference between M2MI86 and M2DETE is that the M2MI86 program reads and writes the data word by word, whereas the latter program reads and writes 256 words at a time; thus, the M2DETE program is faster [14]. Because speed is not of primary concern for the performance
evaluation, the M2MI86 program was chosen to be evaluated. The M2MI86 program is written in FORTRAN. Changes to the program have been minor input/output modifications allowing the program to read from and write to data files.

Description of the Algorithm

Before execution of the program, several parameters must be entered by the user. The parameters include:

1. Starting point of the data file
2. Ending point of the data file
3. Sampling rate
4. Minimum acceleration threshold (MAT)
5. A/D scale factor.

The data is copied to a scratch file for processing.

The M2MI86 algorithm detects fast movements of the eye on the basis of the eye's velocity and pseudo acceleration. The flowchart for the M2MI86 program is shown in Figures 32A and 32B. The algorithm uses digital finite impulse response (FIR) filters to calculate the velocity and pseudo acceleration of the eye. Once an event is detected, it is classified as either a saccade, a fast phase of nystagmus, or "other" type of fast movement. Simultaneously, the program produces the following outputs:

1. One point per beat slow phase velocity
2. Slow phase velocity
3. Pseudo-acceleration
4. Event indicator flag
5. Cumulative slow phase position.

The detection of fast components is based on the sign and magnitude of the instantaneous velocity and acceleration of the eye. The beginning of a fast phase is the point where the
absolute magnitude of acceleration is larger than a starting threshold \(T_s\), the sign of velocity and acceleration is the same, and the absolute magnitude of acceleration is increasing. The starting threshold \(T_s\) is based on the root-mean-square (RMS) value of the acceleration signal. Velocity is not compared with \(T_s\) because the mean value of the velocity signal is not zero; whereas, the mean value of the acceleration signal is zero [14]. The ending point of a fast phase is the point where the absolute magnitude of acceleration drops below an ending threshold \(T_e\), and the signs of velocity and acceleration are different from their respective signs during the onset of the fast phase.

Following the detection of an event, the event is classified as a saccade if the velocity of the slow phase preceding the event is less than 2 degrees/sec. The event is classified as a fast phase if the fast movement preceding the current event has the same direction [14]. If the preceding slow phase does not meet any of the criteria, it is classified as "other" type of fast movement.

The M2MI86 program calculates the acceleration of the eye using a 3-point double differentiator. Because the two opposite peaks of the acceleration waveform are the points of interest, the output of the noise sensitive double differentiator is lowpass filtered to attenuate the spectral peaks often associated with wideband differentiation. The combination of filters produce a 9-point pseudo-acceleration filter (PAF). The 3-point double differentiator, based on the Stirling interpolation formula, is accurate at low frequencies but has limited bandwidth. The filter is a 7-point lowpass filter with the cutoff frequency \(\omega_c\) and filter coefficients based on the sampling frequency. The cutoff frequency and sampling frequency \(\omega_s\) are related by Equation 7.

\[
\omega_c \leq \omega_s + 2.
\]  

For each run of the program, the unit sample responses (USR) of the 9-point PAF and the
7-point lowpass filter are calculated. The unit sample response of the PAF is used to calculate the acceleration output.

An optimal 9-point differentiator is used to find the derivative of the eye position signal. The USR of this filter is fixed to reduce ringing in the output caused by the frequency of damped oscillation \( f_d \) created by the Butterworth antialiasing filter used during sampling [14]. The velocity filter is band limited to a frequency lower than \( f_d' \) as described by Equations 8 and 9.

\[
f_d = 0.707 \times f_c \quad (8)
\]

\[
f_c \leq f_s + 2 \quad (9)
\]

where \( f_c \) is the cutoff frequency below 20 Hz and \( f_s \) the sampling frequency.

The acceleration thresholds determining the beginning and the ending of a fast movement are calculated as follows. The root-mean-square (RMS) value of the pseudo-acceleration filter is calculated during the next \( N \) sample points (where \( N = f_s \)). The RMS value is a measure of activity in the acceleration signal; therefore, when there are too many spikes in the acceleration signal, the RMS value increases [14]. Combining the RMS value with a constant minimum acceleration threshold (MAT) entered by the user reduces the sensitivity of the adaptive threshold. The minimum acceleration threshold varies according to the SNR of the eye position data. The linear combination of RMS and MAT determines the starting threshold \( T_s \), which is calculated using Equation 10.

\[
T_s = \text{RMS} + 0.5 \times \text{MAT} \quad (10)
\]

Multiplying \( T_s \) by a constant with magnitude less than unity, as described by Equation 11, produces the ending threshold \( T_e \).

\[
T_e = 0.7 \times T_s \quad (11)
\]

Convolving the eye position data in the scratch file with the USR's of the PAF and velocity filters produces the acceleration and velocity outputs. Outputs from the filters are stored in separate ring buffers. After the buffers are filled, the program searches for an event.
If a fast phase (or saccade) is not detected, the program branches to the slow phase processing section, where the event indicator flag is set to zero, and the slow phase velocity and other outputs are written to their respective files [14]. Before the slow phase velocity is stored, it is further smoothed with the 7-point lowpass filter used for the PAF.

Following the detection of an event, the program searches forward for the end of the event. After finding the end point, the velocity during the event is computed by averaging the velocity before and after the event. The detected event is classified and the saccade indicator set to an appropriate magnitude. The classifications and corresponding magnitudes are:

\[
\begin{align*}
0 &= \text{a data point not belonging to a fast event} \\
\pm 100 &= \text{a data point from a fast component which is in the direction of the previous slow component} \\
\pm 200 &= \text{a data point from a fast component which is in the opposite direction of the previous slow component} \\
\pm 300 &= \text{a data point belonging to an unidentified fast event.}
\end{align*}
\]

The sign identifies the direction of the component, positive for right-going fast components, negative for left-going fast components. The data process indicator advances the length of the event while the necessary outputs are written to their files.

The output available from the program includes one point per beat slow phase velocity, slow phase velocity, acceleration, saccade indicator, and cumulative slow phase velocity. The cumulative slow phase velocity is the position that the eyeball would reach if it could rotate without restrain in the socket, and it is obtained by removing the fast phase segments from the nystagmus record and piecing together the slow phase segments. The one point per beat slow phase velocity is a plot of time versus the average of slow phase velocity per slow phase beat. [14].

**Simulated Data Parameters**

The simulated data analyzed by the M2M186 program had a sampling period of 5 msec.
(i.e., 200 Hz sampling frequency), and the length of each data file was 15 seconds. The simulated midposition gaze data were generated with saccades of one, two, three, five, and ten degrees. The simulated sinusoidal pursuit data, which was filtered with an anti-alias filter \( f_c = 35 \, \text{Hz} \), contained saccades of one, two, three, and five degrees superimposed on sinusoids of 0.05, 0.10, and 0.50 Hz. The amplitude of the sinusoidal pursuit data sets was 20 degrees. The type of saccade determined by the program was not considered in the analysis of the data. The only criteria for detection were the approximate timing and the direction of the fast event.

**Results with Simulated Mid-position Gaze Data**

The performance of the M2M186 program in analyzing the simulated midposition data is contradictory. Figure 33 illustrates the results of the analysis of midposition gaze data with 1 degree nystagmus. This figure illustrates the typical profile of the error ratios and Error Index for midposition gaze data with all the nystagmus amplitudes tested (one, two, three, five and ten degrees). The missed-detection error ratio is less than 5% for SNR greater than seven (7) and remains close to 5% for SNR less than six (6). However, the false-detection error ratio increases exponentially at SNR less than ten (10) and is as high as 30% at SNR of five (5). The error profiles illustrated in Figure 33 are also observed for the other nystagmus amplitudes; false-detection errors increase at a high rate as the SNR falls below five (5) while the missed-detection errors remain relatively constant (Fig. 34). The interesting feature of the results from the analysis of midposition gaze data is the increase in the number of false detections as nystagmus amplitude increases. For the three degree nystagmus data the false-detection error ratio is 38% at a SNR of five (5), but for the data with five (5) degree nystagmus the false-detection error ratio increases to 43% at a SNR of five (5). The increase in false-detection errors as a function of SNR and nystagmus amplitude is responsible for the Error Index profiles illustrated in Figure 35. This figure shows how the performance of the M2M186 program deteriorates as the signal-to-noise ratio (SNR) decreases.
Results with Simulated Sinusoidal Pursuit Data

The most common errors in the analysis of sinusoidal pursuit data with the M2MI86 program are false detections (as observed in the analysis of the midposition gaze data). Figure 36 illustrates the consistently low missed-detection errors contrasted by exponentially increasing false-detection errors for sinusoidal data at 0.50 Hz. As nystagmus amplitude increases, more false detections are recorded, but missed detections remain relatively constant. Figures 37 through 39 illustrate the Error Index of the simulated sinusoidal pursuit data at 0.05, 0.10, and 0.50 Hz, respectively. These figures indicate that the program performs better at 0.50 Hz with smaller magnitudes of saccadic jump, i.e., one and two degrees, than at the lower frequencies, 0.05 and 0.10 Hz. At all the frequencies tested, the false-detection errors cause the increase in the Error Index as SNR decreases. It should be noted that program parameters were not reset or optimized for any particular run. The best performance of the program, 5% Error Index with SNR of seven (7), appears to be with two (2) degrees of saccadic amplitude and a sinusoidal frequency of 0.50 Hz. For the 0.05 and 0.10 Hz sinusoidal data, the errors become significant at a SNR of approximately 12.

Results with Human Subject Data

The form of the output of the M2MI86 program makes it impossible to accurately determine the timing information of the saccades in the human EOG data sets. Figure 40 is a graph of the output from M2MI86 for the optokinetic EOG data set. This output, as well as the output from the sinusoidal and pseudorandom data sets, was evaluated by expanding sections of the graph, determining the approximate timing of the saccadic events from the index on the graph, and correlating this information with the timing of the true saccades in each data set determined by manually. The results in tabular format are not presented.

The analysis of the optokinetic data set indicates few missed-detection errors; only two (2) fast events are missed, resulting in a 15.38% missed-detection error. However, false
detections are numerous; 58 events are falsely identified, resulting in a 84.06% false-detection error. The Error Index for the human optokinetic data set is 49.72%.

As with the other programs evaluated, the signal-to-noise ratio of the sinusoidal EOG data set caused problems. The results of the analysis of simulated data show that for the 0.10 Hz sinusoidal data with SNR lower than 10, false detections recorded by M2M186 increase exponentially and are as high as 50% (Fig. 41). For the human sinusoidal pursuit data set, no fast events are missed (0% missed-detection error); however, 119 events are falsely identified, resulting in a 95.97% false-detection error. The Error Index for the human sinusoidal pursuit data is 47.98%.

The pseudorandom EOG generated fewer false detections. Only one (1) fast event is missed, resulting in a 7.14% missed-detection error; and 22 events are falsely identified, resulting in a 62.86% false-detection error. The Error Index for the pseudorandom data set is 35.0%.

Harvard Program

The nystagmus algorithms were developed originally for the Raymond E. Jordan Human Vestibular Clinical Laboratory of the Eye and Ear Hospital, Pittsburgh, PA, by Conrad Wall III, Ph.D., who subsequently moved his vestibular laboratory projects to the Massachusetts Eye and Ear Infirmary Vestibular Laboratory, Harvard Medical School, Boston, MA. These algorithms were developed for off-line analysis of nystagmus. The program consists of two major components: 1.) a saccade/slow component identification, and 2.) modeling. Only the fast phase detection algorithm portion of the first component of the program was used in this study. The program was recoded into FORTRAN 77 for use in the VAX system at Texas A&M University. Minor modifications of the input/output algorithms of the program were made in order to read from and write to data files on hard disk rather than magnetic tape.
Description of the Algorithm

The algorithm used by the Harvard laboratory [15] performs an identification of extrema by scanning the data for occurrences of amplitude maxima and minima [11][12][16]. A synthetic nystagmus representation is obtained by straight line connections of extrema. The synthetic nystagmus is used to identify the fast phase segments. A preset parameter called "peak detection" is used to identify extreme points. The program identifies an event as a fast phase component of nystagmus if a segment between a maxima and a minima has a slope greater than a preset minimum slope threshold and a time duration greater than a preset minimum time limit.

A major disadvantage of the program is that these three parameters are in counts of A/D units not in physical units. Thus, the parameters depend upon the sampling interval, the A/D resolution (12-bit, etc.), and the amplification factor. This requires an operator with more than nominal knowledge. In general, this approach is by trial-and-error.

Once a fast phase is identified, the fast phase portion is removed from slow phase eye position and replaced with a first order (straight line) extrapolation. Then, the vertical displacements of the extrapolation and the fast phase segment are added to provide an overall positional offset in reconstructing the slow phase nystagmus, which is referred to as the "estimated cumulative slow phase" [15]. A simple first difference (central difference equation) is calculated from the cumulative slow phase position to obtain the slow phase velocity. The slow phase velocity is fitted with a sinusoidal least squares fit rather than a Fast Fourier Transform.

A flowchart of the fast phase identification portion of the program is shown in Figure 42. Before the program can be executed, the operator must initialize the program by presetting four parameters: window width (IDEL), minimum slope threshold (SLIM), minimum amplitude displacement threshold (TLIM), and maximum amplitude displacement threshold (DISMAX). These parameters are important because they affect the accuracy of fast phase detection and slow phase reconstruction. The parameters are set by an operator with either a priori
knowledge of the data or by trial-and-error. A priori knowledge must take into account: the type of data set, the sampling rate, and the amplification factor. The program uses a moving window search based on the preset value IDEL to scan the EOG data and detects peaks in the data (i.e., maxima and minima) as points which are higher or lower in amplitude than the adjacent points. A flag is set to one (1) if the extremum is a maximum or set to minus one (-1) if the extremum is a minimum. Information on the points of extrema is stored in two arrays. The flags, which specify each extremum as a maximum or minimum, are stored in an array, MXMNI. A second array, MXMN, stores the coordinates that represent time and magnitude of each extrema. Values of slope (or average velocity) are calculated from each maximum peak and the next neighboring minimum peak value. When the program finds a positive value of one (maximum) in the array MXMNI, the absolute value of the slopes of the segment to the left and to the right of the present maximum is computed. The line segment with the largest absolute value between right slope and left slope is selected as a fast phase candidate. Subsequently, slope and displacement magnitudes of the segment are compared with the preset threshold values (i.e., the slope magnitude is compared with the minimum slope threshold (SLIM)), and the amplitude displacement is compared to the displacement value between the minimum amplitude displacement threshold (TLIM) and the maximum amplitude displacement threshold (DISMAX). If the selected segment meets the fast phase detection criteria, the segment is marked as a fast phase and the actual magnitude values are stored in the array CON. The elements that do not belong to a fast phase are stored as zeros in the array CON. Finally, the program outputs starting times of the detected fast phases.

Other algorithms of the program include: rejection of fast component, extrapolation of the slow component position, computation of slow component velocity, and calculation of gain and phase from the relationship between slow component velocity response and the stimulus.

Proper adjustments of the input parameters to the Harvard program were made before analyzing the data. Window width, IDEL, is set to 1 so that the extrema search would go
through all eye position data points to detect maximum and minimum amplitude. The slope limit (SLIM), minimum amplitude (TLIM) and maximum amplitude (DISMAX) are set empirically after determining the initial value that provided the best fast phase detection. Because the Harvard program provides only the starting time of the identified fast phase, the accuracy of the ending point timing of the fast phase was not evaluated. Starting times of the fast phases produced by the program are compared to the timing information of the artificial data (nystagmus timing data) being tested. If the timing data from the program indicates a fast phase when the data does not contain a fast phase, it is counted as a false detection. If the data indicates a fast phase, but the program does not, then the event is counted as a missed detection.

**Simulated Data Parameters**

The simulated data analyzed by the Harvard program had a sampling period of 10 msec. (i.e., 100 Hz sampling frequency), and the length of each data file was 15 seconds. The simulated midposition gaze data were generated with saccades of one, two, three, five, and ten degrees. The simulated sinusoidal pursuit data contained saccades of one, two, three, five, and ten degrees superimposed on sinusoids of 0.05, 0.10, and 0.50 Hz. The amplitude of the sinusoidal pursuit data sets was 20 degrees. The simulated data were not filtered with an anti-alias filter.

**Results with Simulated Midposition Gaze Data**

The Harvard program produces no errors in the analysis of the artificial midposition gaze data without noise. The effects of adding noise to the midposition gaze data at the five nystagmus amplitudes are shown in Figure 43. As indicated in Figure 43, when the SNR is less than 5, the Error Index is greater than 50% for any amplitude of nystagmus. The Error Index is about 30% with ten degrees of nystagmus amplitude at a SNR of seven (7).
Significant errors above 70% result at any amplitude of nystagmus when the SNR is less than four (4). In general, the missed-detection errors are larger than the false-detection errors (Fig. 44).

**Results with Simulated Sinusoidal Pursuit Data**

The analysis of simulated sinusoidal pursuit data without noise with the Harvard program produces no errors, *i.e.*, 0% Error Index. Figures 45 through 48 show the results of adding noise at three sinusoidal frequencies, 0.05, 0.10 and 0.50 Hz, for the five different nystagmus amplitudes. Figure 45 shows the results of adding noise to the 0.05 Hz sinusoidal nystagmus pursuit waveform. The results indicate that the Error Index is greater than 50% when the SNR is less than six (6). Figures 45 through 47 show that the program appears to be more efficient (*i.e.*, small Error Index) at the smaller saccadic displacements of one (1) and two (2) degrees. The worst performance at the 0.05 and 0.10 Hz sinusoids occurs with nystagmus amplitudes of five (5) degrees (Fig. 45 and 46). As the frequency of the sinusoidal base waveform is increased to 0.50 Hz, the performance of the program improves (Fig. 47). In general, the ability of the program to detect fast phases decreases as the nystagmus amplitude increases. Figure 47 shows that the best results (10% Error Index) at the 0.50 Hz sinusoid occur with two (2) degrees of nystagmus amplitude and a SNR of eight (8) or more. For the 0.50 Hz sinusoid, the Error Index exceeds 50% at a nystagmus amplitude of ten (10) degrees and a SNR less than five (5).

In summary, missed-detection errors are generally greater than false-detection errors (Fig. 48). The program produces better results at the higher frequency (0.50 Hz) and smaller amplitude of nystagmus. At SNR less that five (5), significant errors result at all frequencies and nystagmus amplitudes.
Results with Human Data

The Harvard program, as written, uses data collected at a sampling rate of 100 Hz. Sampling rate conversion was performed on the human data to modify the sampling rate from 200 Hz to 100 Hz. The Harvard program threshold parameters were set on the basis of the hand-scored data. The values of the threshold parameters are listed in Table VIII.

Table VIII. List of the presetting parameters for the Harvard program.

<table>
<thead>
<tr>
<th>Type of the test data</th>
<th>SLIM</th>
<th>TLIM</th>
<th>DISMAX</th>
</tr>
</thead>
<tbody>
<tr>
<td>Optokinetic</td>
<td>0.18</td>
<td>5.4</td>
<td>20.2</td>
</tr>
<tr>
<td>Sinusoidal Pursuit</td>
<td>0.14</td>
<td>3.0</td>
<td>4.0</td>
</tr>
<tr>
<td>Pseudorandom Pursuit</td>
<td>0.12</td>
<td>2.7</td>
<td>5.8</td>
</tr>
</tbody>
</table>

For the optokinetic data set, 13 events are manually identified as saccades; but, the Harvard program identifies 20 events as fast phases. Table IX summarizes the fast phase detection results with corresponding magnitude. Out of the twenty detected events, ten are false detections, resulting in a 50% false-detection error. Three (3) true events are missed detections, resulting in a 23% missed-detection error. The Error Index for the optokinetic data set is 37%.

Table IX. Results from the analysis of human optokinetic data by Harvard Program.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Amplitude (°)</th>
<th>Detection Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>8.0</td>
<td>detected</td>
</tr>
<tr>
<td>2</td>
<td>15.6</td>
<td>detected</td>
</tr>
<tr>
<td>3</td>
<td>18.0</td>
<td>missed</td>
</tr>
<tr>
<td>4</td>
<td>5.6</td>
<td>detected</td>
</tr>
<tr>
<td>5</td>
<td>18.0</td>
<td>detected</td>
</tr>
<tr>
<td>6</td>
<td>14.2</td>
<td>detected</td>
</tr>
<tr>
<td>7</td>
<td>12.4</td>
<td>detected</td>
</tr>
<tr>
<td>8</td>
<td>14.6</td>
<td>missed</td>
</tr>
<tr>
<td>9</td>
<td>13.6</td>
<td>detected</td>
</tr>
<tr>
<td>10</td>
<td>16.2</td>
<td>detected</td>
</tr>
<tr>
<td>11</td>
<td>19.2</td>
<td>detected</td>
</tr>
<tr>
<td>12</td>
<td>20.2</td>
<td>detected</td>
</tr>
<tr>
<td>13</td>
<td>5.4</td>
<td>missed</td>
</tr>
</tbody>
</table>
Table X summarizes the results of the evaluation of the human sinusoidal data set. The sinusoidal pursuit data set contains only five (5) fast phases. The Harvard program identified seven (7) events as fast phases of which six (6) are false detections and 4 are missed detections, resulting in 86% false-detection error and 80% missed-detection error. The Error Index for the sinusoidal data set is 83%, which is very high when compared to other types of data sets, i.e., optokinetic and pseudorandom.

Table X. Results from analysis of human sinusoidal pursuit data by Harvard Program.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Amplitude (°)</th>
<th>Detection Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3.0</td>
<td>detected</td>
</tr>
<tr>
<td>2</td>
<td>3.0</td>
<td>missed</td>
</tr>
<tr>
<td>3</td>
<td>3.0</td>
<td>missed</td>
</tr>
<tr>
<td>4</td>
<td>3.0</td>
<td>missed</td>
</tr>
<tr>
<td>5</td>
<td>4.0</td>
<td>missed</td>
</tr>
</tbody>
</table>

Table XI summarizes the results of the pseudorandom data set analysis. For the pseudorandom pursuit data set, 14 events are identified as true fast phases based on the

Table XI. Results from analysis of human pseudorandom data by Harvard Program.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Amplitude (°)</th>
<th>Detection Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3.2</td>
<td>detected</td>
</tr>
<tr>
<td>2</td>
<td>2.7</td>
<td>missed</td>
</tr>
<tr>
<td>3</td>
<td>4.0</td>
<td>missed</td>
</tr>
<tr>
<td>4</td>
<td>4.5</td>
<td>detected</td>
</tr>
<tr>
<td>5</td>
<td>3.7</td>
<td>missed</td>
</tr>
<tr>
<td>6</td>
<td>4.6</td>
<td>detected</td>
</tr>
<tr>
<td>7</td>
<td>5.2</td>
<td>detected</td>
</tr>
<tr>
<td>8</td>
<td>3.8</td>
<td>detected</td>
</tr>
<tr>
<td>9</td>
<td>5.0</td>
<td>missed</td>
</tr>
<tr>
<td>10</td>
<td>4.8</td>
<td>detected</td>
</tr>
<tr>
<td>11</td>
<td>5.3</td>
<td>detected</td>
</tr>
<tr>
<td>12</td>
<td>5.8</td>
<td>detected</td>
</tr>
<tr>
<td>13</td>
<td>5.0</td>
<td>missed</td>
</tr>
<tr>
<td>14</td>
<td>3.0</td>
<td>detected</td>
</tr>
</tbody>
</table>

manually scored data. Four (4) events of the thirteen events detected by the Harvard program are false detections, resulting in a 30% false-detection error. Five (5) of the true fast phases are
missed detections, for a missed-detection error of 36%. The resulting Error Index for the pseudo-random pursuit data is 33%.

Both the simulated data and human data analyses show the inconsistency and high error percentages in the Harvard fast phase detection algorithm. One may argue about initial threshold settings not being optimized, but this implies that the program is not user friendly or automatic.

**NASA Nystagmus Analysis Program (FPID)**

The FPID program was created to automatically detect and eliminate fast phases from the EOG so that the slow phase characteristics of the EOG could be analyzed independently. For this study, modifications to the NASA FPID program included: 1.) output of timing information, and 2.) calculation of fast phase amplitude. Two versions of FPID were developed in order to meet the computing demands of research and clinical vestibular laboratories. The first version, FPID.FOR, is written in FORTRAN 77; the second version, FPID.C, is written in C for use on IBM or compatible personal computers with the Microsoft C Compiler version 5.1 (Microsoft Crop., Redmond, WA). The algorithm for EOG analysis is the same for the two versions; however, the format of the program output varies from system to system such that the code is not fully transportable. The FORTRAN version was developed with a VAX mainframe computer but could be compiled on any other FORTRAN compiler adhering to the VAX (DEC) standards. The C version was developed on an IBM-AT compatible computer. Several commands in FPID.C are not ANSI standard; therefore, users of compilers other than Microsoft C must consult the **FPID Software User's Manual** (Appendix B) before using the program. In both versions, FPID.FOR and FPID.C, fast phase timing information is saved on a formatted file. For additional information on the operation of the programs, consult the **FPID Software User's Manual** in the appendix.
Description of the Algorithm

Figure 49 is a flowchart of the algorithm for the analysis of the EOG. The data analysis algorithm, which is the same for all versions, has three main components: data processing, fast phase identification, and slow phase reconstruction. The data processing component consists of:

1. DC removal
2. Moving average smoothing, and
3. Digital filtering.

Initially, the user may choose to eliminate the DC component from the data by subtracting the mean of the data from each data point. Immediately following the removal of the DC offset, the data is smoothed with a five (5) point weighted moving average. Smoothing serves to low-pass filter the data and reduce incorrect identification of fast phases [4]. As illustrated in Table XII, the attenuation of the signal by the weighted moving average is negligible; the difference between the manual and computer calculations of saccadic amplitude is less than one (1) degree. After the five-point smoother, a 15-point, FIR low-pass filter is applied to the signal. The filter coefficients in the original version of FPID were designed for a sampling rate of 120

<table>
<thead>
<tr>
<th>Hand-Calculation (°)</th>
<th>Computer-Calculation (°)</th>
<th>Difference (°)</th>
</tr>
</thead>
<tbody>
<tr>
<td>8.0</td>
<td>7.15</td>
<td>0.85</td>
</tr>
<tr>
<td>15.6</td>
<td>15.34</td>
<td>0.26</td>
</tr>
<tr>
<td>18.0</td>
<td>17.15</td>
<td>0.85</td>
</tr>
<tr>
<td>5.6</td>
<td>5.95</td>
<td>0.35</td>
</tr>
<tr>
<td>18.0</td>
<td>17.56</td>
<td>0.44</td>
</tr>
<tr>
<td>14.2</td>
<td>13.76</td>
<td>0.44</td>
</tr>
<tr>
<td>12.4</td>
<td>12.23</td>
<td>0.17</td>
</tr>
<tr>
<td>14.6</td>
<td>14.51</td>
<td>0.09</td>
</tr>
<tr>
<td>13.6</td>
<td>12.90</td>
<td>0.70</td>
</tr>
<tr>
<td>16.2</td>
<td>15.70</td>
<td>0.50</td>
</tr>
<tr>
<td>19.2</td>
<td>18.56</td>
<td>0.64</td>
</tr>
<tr>
<td>20.2</td>
<td>19.27</td>
<td>0.93</td>
</tr>
<tr>
<td>5.4</td>
<td>5.03</td>
<td>0.37</td>
</tr>
</tbody>
</table>
Hz (θ = π/2) [4]. Even though these coefficients were not recalculated for the 200 Hz
sampling rate, the higher filter cutoff did not affect the results significantly.

Following the digital processing of the EOG data, the fast phase identification process is
performed. The algorithm for fast phase identification includes:

1. First difference
2. Velocity threshold-crossing detection, and

The filtered EOG is differentiated with a fourth-order, first difference algorithm to get the
velocity profile of the EOG data. Spikes in the velocity signal suggest the presence of a fast
phase. A velocity threshold for detection of fast phases is determined from the root-mean-
square (RMS) value of the velocity signal. The value of the threshold is twice the RMS value
of the first derivative. The algorithm searches for threshold-crossing data points as a means of
detecting the fast events in the data. Once the threshold-crossing point is determined, the
previous zero-crossing data point is searched to determine the beginning of a fast phase. The
zero-crossing data point following the threshold-crossing data point is then searched to
determine the end of the fast phase. The algorithm also determines the direction of the fast
phase, up- or down-beating. By convention, right-beating saccades in the horizontal EOG are
considered to be positive, and left-beating saccades are considered to be negative. The fast
phase amplitude is also calculated at this stage. Previous studies have employed the same
algorithm to accurately detect fast phases from human EOG data [4].

The third, and last, portion of the FPID program is the slow phase reconstruction. Slow
phase reconstruction consists of:

1. Least-squares estimation
2. Height correction, and
3. Moving average smoothing.
Once the starting and ending times of each phase are determined, least-squares estimates of the slope and y-intercept are calculated from the ten points immediately preceding the fast phase. The estimates are then used to re-calculate the previously eliminated fast phase data points by linear fit. After completing the reconstruction, but before continuing the search for subsequent fast phases, a height correction factor is implemented to concatenate the remaining part of the signal to the reconstructed portion of the EOG at the correct amplitude. Once all the points in the signal have been analyzed, the reconstructed data may be further smoothed with the same five (5) point moving average previously employed. Fast phase timing information and amplitude are stored on file in a tabular format after the data set has been completely analyzed. Also stored on file is the reconstructed EOG.

Although FPID is an automatic EOG analysis program, it is dependent on data acquisition parameters such as sampling rate. The software code must provide flexibility and/or be easily modified; therefore, it may be used for data analysis in any laboratory. Flexibility has been achieved by implementation of subroutines and functions and portability of code. Flexibility allows users to implement the program without modifying the code. Unfortunately, some signal processing algorithms (e.g., digital filtering) depend on parameters set during data collection. In this case, a code that is easily modified is absolutely necessary. In addition to the documentation of the program, the modular code in FPID, implemented through subroutines and functions, is easy to follow and simplifies the process of modifying the code.

**Simulated Data Parameters**

The simulated data analyzed by the FPID program had a sampling period of 5 msec. (i.e., 200 Hz sampling frequency), and the length of each data file was 15 seconds. The simulated midposition gaze data were generated with saccades of one, two, three, five, and ten degrees. The simulated sinusoidal pursuit data also contained saccades of one, two, three, five, and ten degrees superimposed on sinusoids of 0.05, 0.10, and 0.50 Hz. The amplitude of the
sinusoidal pursuit data sets was 20 degrees. The data were not filtered with an anti-alias filter.

Results with Simulated Mid-position Gaze Data

The analysis with simulated EOG data was a comprehensive study of the performance of the program (i.e., fast phase detection capability) as a function of SNR. Simulated mid-position gaze and sinusoidal pursuit data were generated using the NASDAT program developed for the study. The highest signal-to-noise ratio for the data was approximately 14; the lowest SNR was approximately 1.5. Table XIII illustrates the noise levels (in degrees) with the corresponding SNR for data sets with one (1) degree nystagmus. Initially, data sets with SNR as high as 80 were analyzed; however, the results did not show an improvement in the fast phase detection capability of FPID.

**TABLE XIII.** Noise amplitude and SNR for artificial data with one (1) degree saccades.

<table>
<thead>
<tr>
<th>Noise (°)</th>
<th>SNR</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0</td>
<td>∞</td>
</tr>
<tr>
<td>0.1</td>
<td>13.43</td>
</tr>
<tr>
<td>0.2</td>
<td>6.75</td>
</tr>
<tr>
<td>0.3</td>
<td>4.52</td>
</tr>
<tr>
<td>0.4</td>
<td>3.38</td>
</tr>
<tr>
<td>0.5</td>
<td>2.72</td>
</tr>
<tr>
<td>1.0</td>
<td>1.34</td>
</tr>
</tbody>
</table>

The typical fast phase detection capability of FPID for midposition gaze data with all the nystagmus amplitudes tested is illustrated in Figure 50. As shown, the Error Index is zero for SNR greater than four (4) and increases exponentially as the SNR falls below four. As illustrated in Figure 51, saccadic amplitude does not affect the detection capability of FPID. Individual missed-detection and false-detection errors, shown in Figure 52, further illustrate the independence of the fast phase identification algorithm from nystagmus magnitude. The results from the midposition gaze analysis show the remarkable consistency in fast phase detection by the FPID program.
**Results with Simulated Sinusoidal Pursuit Data**

In order to compare the results from simulated midposition gaze and simulated sinusoidal pursuit trials, the amplitude of the base sinusoid was not included in calculation of the SNR. The signal-to-noise ratio of the simulated sinusoidal pursuit data was calculated in the same manner as for the simulated midposition gaze data. Simulated midposition gaze and sinusoidal pursuit data were generated with the same saccadic amplitude and noise levels (i.e., same SNR) to allow for comparison of results.

The results from the analysis of sinusoidal pursuit data are slightly different from those of gaze data. The analysis of sinusoidal data illustrates the effect of frequency and saccadic amplitude on the fast phase detection capability of FPID (Figs. 53 - 55). Missed and false-detection errors (individual errors) in the 0.50 Hz data are high when the saccadic amplitude is less than three (3) degrees (Figure 53). Although not depicted in Figure 53, individual errors in the 0.50 Hz data without noise (one and two degree nystagmus) are also very high. The individual errors decrease sharply for saccadic amplitudes greater than two (2) degrees.

The apparent inability of FPID to detect fast phases of small amplitude in the simulated 0.50 Hz sinusoidal data stems from a discrepancy between the velocity of the fast phases and the average velocity of the sinusoid. The FPID program uses a velocity threshold to detect fast phases; therefore, the program's capability to detect fast phases is dependent on the magnitude of the velocity of nystagmus and the RMS value of the velocity signal, not on nystagmus amplitude or sinusoid frequency. Results from the 0.05 Hz and 0.10 Hz data show that the individual errors and the Error Index profile are consistent. Figures 54 and 55 show exponentially increasing Error Index as the SNR falls below four (4). The average velocities of the slow phases in the 0.05 Hz and 0.10 Hz sinusoidal data were much slower than the fast phase velocities; therefore, the velocity threshold algorithm was capable of detecting fast phases of fast phase velocity of the nystagmus beats.

The analysis of simulated EOG data shows that FPID is very accurate and consistent in
detecting fast phases in midposition gaze data. The results from the sinusoidal data analysis suggest a discrepancy between simulated sinusoidal data with one (1) and two (2) degrees nystagmus beats and real EOG data. The simulated sinusoidal pursuit data with one (1) and two (2) degree nystagmus at 0.50 Hz indicates that the fast phase velocity was not much higher than the slow phase velocity, giving rise to high missed-detection errors.

Results with Human Subject Data

The three types of EOG data were analyzed using FPID: optokinetic, sinusoidal and pseudo-random pursuit. The summary of the results of the analysis of optokinetic data is presented in Table XIV. The results show that FPID does not miss any saccades, a 0% missed-detection error ratio, but falsely detects one (1) saccade, resulting in a 7.69% false-detection error ratio. The Error Index for this data set is 3.85%. The event falsely identified as a saccade by FPID is relatively large in amplitude, 5.2 degrees, with a low average velocity of 115 degrees/sec.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Start</th>
<th>End</th>
<th>Amplitude</th>
<th>Start</th>
<th>End</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.350</td>
<td>0.380</td>
<td>8.0</td>
<td>0.360</td>
<td>0.395</td>
</tr>
<tr>
<td>2</td>
<td>0.850</td>
<td>0.900</td>
<td>15.6</td>
<td>0.860</td>
<td>0.910</td>
</tr>
<tr>
<td>3</td>
<td>1.735</td>
<td>1.790</td>
<td>18.0</td>
<td>1.745</td>
<td>1.795</td>
</tr>
<tr>
<td>4</td>
<td>2.155</td>
<td>2.185</td>
<td>5.6</td>
<td>2.135</td>
<td>2.200</td>
</tr>
<tr>
<td>5</td>
<td>2.710</td>
<td>2.775</td>
<td>18.0</td>
<td>2.725</td>
<td>2.780</td>
</tr>
<tr>
<td>6</td>
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<td>3.650</td>
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<td>5.715</td>
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<td>6.580</td>
<td>6.640</td>
<td>13.6</td>
<td>6.595</td>
<td>6.650</td>
</tr>
<tr>
<td>10</td>
<td>7.790</td>
<td>7.865</td>
<td>16.2</td>
<td>7.800</td>
<td>7.865</td>
</tr>
<tr>
<td>11</td>
<td>8.975</td>
<td>9.035</td>
<td>19.2</td>
<td>8.985</td>
<td>9.045</td>
</tr>
<tr>
<td>12</td>
<td>10.125</td>
<td>10.190</td>
<td>20.2</td>
<td>10.140</td>
<td>10.190</td>
</tr>
<tr>
<td>13</td>
<td>10.665</td>
<td>10.695</td>
<td>5.4</td>
<td>10.675</td>
<td>10.705</td>
</tr>
</tbody>
</table>

Results of the sinusoidal pursuit analysis are summarized in Table XV. The program performs poorly: three saccades are missed, resulting in a 60% missed-detection error, and 56 saccades are falsely identified, resulting in a 95.24% false-detection error. The Error Index for
the human sinusoidal data set is 77.62%.

Table XV. Results from the analysis of human sinusoidal pursuit data by FPID Program.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Hand-scored</th>
<th>Computer</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Start</td>
<td>End</td>
</tr>
<tr>
<td>1</td>
<td>2.855</td>
<td>2.870</td>
</tr>
<tr>
<td>2</td>
<td>5.125</td>
<td>5.145</td>
</tr>
<tr>
<td>3</td>
<td>7.100</td>
<td>7.120</td>
</tr>
<tr>
<td>4</td>
<td>9.425</td>
<td>9.445</td>
</tr>
<tr>
<td>5</td>
<td>9.545</td>
<td>9.570</td>
</tr>
</tbody>
</table>

A likely explanation for the high Error Index for the human sinusoidal pursuit EOG is the low SNR of the signal with respect to the amplitude of the saccades. The noise on the sinusoidal EOG was extracted by subtracting the 0.10 Hz base sinusoid from the signal, and the average RMS value of the remaining noise, shown in Figure 56, was calculated. The amplitude of the sinusoid subtracted from the EOG was determined according to the amplitude of the EOG after the DC shift on the EOG was eliminated. The root-mean-square value of each saccade was calculated to determine the SNR of each saccade using Equation 12:

$$\text{SNR}_{\text{saccade}} = \frac{\text{RMS}_{\text{saccade}}}{\text{RMS}_{\text{noise}}}$$ \hspace{1cm} (12)

In the analysis of simulated sinusoidal pursuit data at 0.10 Hz, a signal-to-noise ratio of four (4) or less generates an Error Index higher than 30% (Fig. 55). The highest SNR of the fast phases in the sinusoidal data set is 2.03 (Table XV); therefore, the high noise level with respect to the nystagmus beats was responsible for the high Error Index observed in the subject data sinusoidal EOG.

The pseudorandom data test set contained less noise than the sinusoidal pursuit test data set; and the results were much better than those from the sinusoidal data. The results summarized in Table XVI reflect much lower error ratios; one (1) saccade is missed, resulting in a 7.14% missed-detection error, and no false identifications occur (0% false-detection error). The Error...
Index for the pseudorandom data set is 3.57%.

The results from simulated data analysis prove the consistency of FPID in detecting fast phases under controlled conditions; however, the results from the subject data analysis illustrate the complexities of automatic EOG analysis using computers. The human data contains nystagmus of varying amplitude and velocity, which, when coupled with artifact, generate higher than expected errors. It seems that the sensitivity of the automatic velocity threshold technique for fast phase detection depends on the type of data being analyzed.

Table XVI. Results from the analysis of human pseudorandom data by FPID Program.

<table>
<thead>
<tr>
<th>Fast Phase #</th>
<th>Hand-scored</th>
<th>Computer</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Start</td>
<td>End</td>
</tr>
<tr>
<td>1</td>
<td>0.603</td>
<td>0.650</td>
</tr>
<tr>
<td>2</td>
<td>0.865</td>
<td>0.885</td>
</tr>
<tr>
<td>3</td>
<td>1.150</td>
<td>1.175</td>
</tr>
<tr>
<td>4</td>
<td>1.465</td>
<td>1.490</td>
</tr>
<tr>
<td>5</td>
<td>1.710</td>
<td>1.730</td>
</tr>
<tr>
<td>6</td>
<td>2.505</td>
<td>2.525</td>
</tr>
<tr>
<td>7</td>
<td>2.710</td>
<td>2.735</td>
</tr>
<tr>
<td>8</td>
<td>3.005</td>
<td>3.030</td>
</tr>
<tr>
<td>9</td>
<td>3.725</td>
<td>3.755</td>
</tr>
<tr>
<td>10</td>
<td>4.065</td>
<td>4.090</td>
</tr>
<tr>
<td>11</td>
<td>4.295</td>
<td>4.325</td>
</tr>
<tr>
<td>12</td>
<td>4.975</td>
<td>5.005</td>
</tr>
<tr>
<td>13</td>
<td>5.205</td>
<td>5.235</td>
</tr>
<tr>
<td>14</td>
<td>5.750</td>
<td>5.775</td>
</tr>
</tbody>
</table>
CHAPTER VI
DISCUSSION - COMPARISON OF RESULTS

Evaluation of the various software used in detection of saccades (fast phase component of nystagmus) included recoding nystagmus analysis programs from six vestibular laboratories in the United States to FORTRAN computer language, generating a simulated EOG data base, and evaluating each program with an Error Index criteria as a function of SNR. The concept of an Error Index was employed as the criterium for evaluating the vestibular analysis software program with the best performance, i.e., the smallest percentage of Error Index at the lowest SNR.

Figures 21 and 51 indicate that the UCLA SINUXEC AND NASA FPID programs are extremely consistent in detecting midposition gaze saccades and that the percent Error Index is independent of the magnitude of saccadic jump. Both programs appear to have comparable performances, i.e., less than a 5% Error Index for a SNR of four (4), although the UCLA SINUXEC program (Fig. 22) has a low missed-detection error (less than 2% missed detection at a SNR of 3.5) but a high false-detection error (8% false detection at a SNR of 3.5) while the NASA FPID program (Fig. 52) has equal detection errors (missed and false detections) of 4.0% error at a SNR of 2.5.

For the simulated midposition gaze test, Figure 12 shows that the USAF/SAM program performs best with two (2) and three (3) degree of saccadic jumps, but the performance deteriorates (larger Error Index) as the saccadic jump increases from five (5) to ten (10) degrees. Similar to the NASA program, the missed-detection error equals the false-detection error for the same value of saccadic jump. The midposition gaze test results from the MIT program (Fig. 35) show a consistent percent Error Index of about 5% at a SNR of eight (8) at saccadic jumps of one, two, three, five, and ten degrees. Similar to the UCLA program, the MIT program (Fig. 34) performance had less than a 2% missed-detection error with SNR
greater than four at all saccadic jump magnitudes but had a high false-detection error rate at SNR less than ten (10). The low missed-detection error coupled with a high false-detection error in both the UCLA SINUXEC and MIT M2MI86 programs may be attributed to low settings of threshold values. As a threshold is decreased more events are detected, which results in less missed detections of true events, but at the expense of an increase in detection of false events.

In contrast to the UCLA and MIT programs, the Harvard program midposition gaze test results (Fig. 44) show a lower false-detection error than missed-detection error. This indicates that perhaps threshold settings may be decreased.

Figure 57 shows the Error Index for the midposition gaze test at three (3) degrees of saccadic jump for five of the programs evaluated in this study. As illustrated by this figure, the NASA FPID and the UCLA SINUXEC programs have comparable performance; whereas, the USAF/SAM and the MIT programs perform comparably but not as good as the UCLA and NASA programs.

The results of the nystagmus analysis programs with simulated sinusoidal tests performed at 0.05, 0.10 and 0.50 Hz for the various saccadic jump/magnitudes (one, two, three, five, and ten degrees) show patterns similar to results obtained with the simulated gaze data. The USAF/SAM (Figs. 15 - 17), UCLA SINUXEC (Figs. 23 - 25), and NASA FPID (Figs. 53 - 55) programs show better performance (lower Error Index as a function of SNR) at the lower frequencies (0.05 and 0.10 Hz) than at the higher frequency (0.50 Hz). In contrast, the MIT M2MI86 (Figs. 37 - 39) and the Harvard programs (Figs. 45 - 47) perform better at the higher frequency (0.50 Hz) than at the lower frequencies (0.05 and 0.10 Hz). The variation in performance as the sinusoidal frequency varies is probably due to the digital or optimal filter designs used in the various programs and the parameters of the simulated sinusoidal data. The USAF/SAM and the Harvard programs perform better with small saccadic jump magnitudes of two (2) and three (3) degrees than at larger saccadic magnitudes of five (5) and ten (10)
degrees. The performance of the UCLA SINUXEC, the MIT M2MI86 and NASA FPID programs are consistent and independent of the saccadic jump magnitude, except at 0.50 Hz, when the fast phase and slow phase velocities are approximately the same value and less than 100 deg./sec. (i.e., one (1) degree saccadic jumps have a maximum average velocity of 66 deg./sec. and the slow phase component of the 0.50 Hz sinusoid has maximum average velocity of approximately 46 deg./sec.). The NASA/FPID program (Fig. 53) shows poor performance with simulated sinusoidal pursuit data at 0.50 Hz and saccadic jumps of one (1) and two (2) degrees. The decreased performance may be the result of the average fast phase velocity of the simulated nystagmus being approximately the same as the average velocity of the slow component. The fast phase velocity of the one (1) and two (2) degree nystagmus beats in the simulated data may not be high enough for adequate detection by programs that employ velocity filters or any other type of fast phase detection based on the velocity of the EOG. This situation is not likely to happen with real EOG data because the fast phase of nystagmus beats during sinusoidal pursuit will generally have much greater velocity than the slow phase. The fast phase velocities of the three, five and ten degree nystagmus beats are considerably higher than the average velocity of the slow component of the 0.05, 0.10, and 0.50 Hz sinusoids (Table I) and did not generate as many errors as the data sets with lower magnitude saccadic jumps.

The performance of the six programs may be compared for the 0.10 Hz sinusoid with saccadic amplitude of three (3) degrees (Fig. 58). The NASA FPID, UCLA SINUXEC and USAF/SAM programs have comparable performances.

The results of program performance with three types of data acquired from subject EOG responses to optokinetic, sinusoidal pursuit, and pseudorandom test stimuli are summarized in Table XVII. As indicated in the table, the NASA FPID program had the best performance, or lowest Error Index, 3.8% for the optokinetic test and 3.6% for the pseudorandom test. The UCLA SINUXEC had a 7.1% Error Index for the pseudorandom test. All programs
performed poorly with the sinusoidal pursuit test data. An examination of the signal-to-noise ratio indicated that the SNR was about two (2) when the RMS value of the saccade was compared to the RMS value of the noise. Results with the simulated sinusoidal data indicated that a high percentage of Error Index can be anticipated when the signal-to-noise ratio is less than four (4).

**Table XVII. Comparison of the Program Performance with Subject Data**

<table>
<thead>
<tr>
<th>PROGRAM</th>
<th>DATA TYPE</th>
<th>OPTOKINETIC</th>
<th>SINUSOIDAL</th>
<th>PSEUDORANDOM</th>
</tr>
</thead>
<tbody>
<tr>
<td>USAF/SAM</td>
<td>MDE</td>
<td>FDE</td>
<td>EI</td>
<td>MDE</td>
</tr>
<tr>
<td>UCLA (SINUXEC)</td>
<td>38.5</td>
<td>61.9</td>
<td>51.2</td>
<td>60.0</td>
</tr>
<tr>
<td>MIT (M2M86)</td>
<td>69.2</td>
<td>66.7</td>
<td>68.0</td>
<td>100</td>
</tr>
<tr>
<td>HARVARD</td>
<td>15.4</td>
<td>84.1</td>
<td>49.7</td>
<td>0</td>
</tr>
<tr>
<td>NASA (FPID)</td>
<td>23.0</td>
<td>50.0</td>
<td>37.0</td>
<td>80.0</td>
</tr>
</tbody>
</table>

MDE: Missed Detection Error; FDE: False Detection Error; EI: Error Index. All values are in percentage.
CHAPTER VII
CONCLUSIONS

The objective of this study was to evaluate the performance of six nystagmus analysis programs. The programs were evaluated on their ability to detect the occurrence of saccadic (fast phase) movements. An Error Index was used to evaluate and compare the accuracy of the nystagmus analysis programs. The conclusions of this study are:

1. The NASA-FPID and the UCLA-SINUXEC programs have the most consistent performance.
2. The performance (smallest Error Index at the lowest signal-to-noise ratio) of the NASA-FPID and UCLA-SINUXEC programs is less than 5% error in index for signal-to-noise ratios greater than four (4).
3. Both programs perform better with sinusoidal pursuit frequencies less than 0.50 Hz than at frequencies greater than or equal to 0.50 Hz.
4. The NASA-FPID and UCLA-SINUXEC programs had the best performance of the six (6) programs when tested with pseudorandom EOG data from human subjects.
CHAPTER VIII
RECOMMENDATIONS

The traditional approach used in the analysis of a system is to determine the system's transfer function by observing the system response to a predetermined deterministic excitation. Knowledge of the system's transfer function permits prediction of the system response to other deterministic excitations. Although linear systems analysis is the most popular and useful analytical method used to evaluate explicit mathematical models, i.e., the transfer function of a biological system, the method applies only to systems that are linear.

The most commonly used excitation signals in systems analyses are single frequency sinusoid, step, and impulse functions. The use of other than deterministic input signals did not fully develop until computers with a large number handling capacity became available. The Wiener method, nonlinear system identification by observation of a system's response to zero-mean Gaussian white noise, enables one to predict the response (linear and nonlinear) of the system to any input; however, the method is not without problems.

A pseudorandom input stimulus lies between the simple single frequency sinusoid and the complex random Gaussian white noise; but, according to Victor and Shapley [17] can produce results similar to the Wiener method. An excellent description of the sum of sinusoids method capability for both linear and nonlinear analyses in the frequency domain was presented by Victor and Shapley. The crux of the method is the use of a modulation signal that is a sum-of-sine waves and the measurement of nonlinear response of the system as cross-talk between the input frequencies. Thus, the sum-of-sinusoids method uses a deterministic rather than random Gaussian noise input stimulus, is not restricted to a small signal regime like the harmonic input method, and is different from the use of a single sinusoid method. The difference is based on the response to a sum-of-sinusoids stimulus which may contain the nonlinear interaction terms, i.e., the sum and difference frequency terms which are the intermodulation of cross-talk.
frequencies.

Expansion of the automated analysis of optokinetic and vestibular responses from linear system analysis to nonlinear analysis using the sum-of-sinusoids technique is recommended.
CHAPTER IX

REFERENCES


APPENDIX A

SOFTWARE USER'S MANUAL:

SYNTHETIC DATA GENERATION PROGRAM (NASDAT.FOR)
I. INTRODUCTION

The NASDAT.FOR program has been developed to generate 15 seconds of simulated EOG data. The source code was written in FORTRAN 77 for a VAX computer system (8650), but the code is transportable to other systems with adequate memory capacity. Two types of EOG data are generated, midposition gaze and sinusoidal pursuit. The program is designed to:

1. generate data containing fast phases of variable amplitude;
2. generate data with variable slow phase to fast phase data point ratio; and
3. add white noise with fixed maximum amplitude.

The data point ratio is defined as the ratio of the number fast phase points to the number slow phase points in each nystagmus beat, which determines the length of the nystagmus beats in the simulated data. The time interval between sample points in the simulated EOG data is determined by the sampling rate selected by the user.

The simulated EOG data is generated in a three step process:

1. generation of the base wave;
2. superposition of nystagmus beats; and
3. addition of noise.

The first step is always completed because data may be generated without superimposed nystagmus. It is important to note that midposition gaze data without nystagmus is a straight line at zero (0) degrees. The second step is completed if nystagmus beats are to be superimposed on the base wave. In this case the amplitude of nystagmus and the average fast phase velocity must be entered by the user. The third step is completed only if noise is to be superimposed on the base wave. If noise is added to the data, the user must enter the maximum amplitude of noise. If noise is added to the data, an option is provided to select a simulated anti-alias filter is provided. The three lowpass filters with cutoff frequencies at 33 Hz, 45 Hz and 80 Hz are implemented with recursive digital filters designed for a 200 Hz sampling rate. If the user selects a different sampling rate (f_s), the cutoff frequency of these filters will be changed by a factor (f_s) described in Equation (1)
\[ ef = 200 + f \]  

If a sampling rate other than 200 Hz is selected the new cutoff frequency \((f_{cn})\) of the simulated anti-alias filter will change according to Equation 2.

\[ f_{cn} = f_c + ef \]  

II. SOFTWARE REQUIREMENTS

The software and data files required for generation of simulated electro-oculogram (EOG) data are listed below:

1. NASDAT.FOR: Source code for generation of simulated data
2. FREQ.DAT: Random frequency data file
3. MGxx.DAT: Noise amplitude data files (xx=maximum amplitude of noise)

The source code, NASDAT.FOR, is listed in this report. The random frequency data file, FREQ.DAT, is required to ensure the whiteness of the noise added to the signal. The noise amplitude data files contain noise data with maximum amplitude determined by the xx suffix. Table A1 lists the available noise amplitudes and their corresponding file names.

<table>
<thead>
<tr>
<th>Noise Amplitude (°)</th>
<th>Filename</th>
<th>Noise Amplitude (°)</th>
<th>Filename</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>MG0_2.DAT</td>
<td>3.0</td>
<td>MG3.DAT</td>
</tr>
<tr>
<td>0.2</td>
<td>MG0_1.DAT</td>
<td>4.0</td>
<td>MG4.DAT</td>
</tr>
<tr>
<td>0.3</td>
<td>MG0_3.DAT</td>
<td>5.0</td>
<td>MG5.DAT</td>
</tr>
<tr>
<td>0.4</td>
<td>MG0_4.DAT</td>
<td>6.0</td>
<td>MG6.DAT</td>
</tr>
<tr>
<td>0.5</td>
<td>MG0_5.DAT</td>
<td>7.0</td>
<td>MG7.DAT</td>
</tr>
<tr>
<td>1.0</td>
<td>MG1.DAT</td>
<td>8.0</td>
<td>MG8.DAT</td>
</tr>
<tr>
<td>1.5</td>
<td>MG1_5.DAT</td>
<td>9.0</td>
<td>MG9.DAT</td>
</tr>
<tr>
<td>2.0</td>
<td>MG2.DAT</td>
<td>10.0</td>
<td>MG10.DAT</td>
</tr>
<tr>
<td>2.5</td>
<td>MG2_5.DAT</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

III. INPUT REQUIREMENTS

Data parameters common to both types of data (midposition gaze and sinusoidal) are entered by the user at the beginning of the program. This input determines:
1. type of data to generate;

2. sampling rate of data collection (used to determine the time interval between data points);

3. if nystagmus is to be added to the data, the amplitude of nystagmus,

4. if noise is to be added to the data, the maximum amplitude of noise; and

5. if anti-alias filtering is to be simulated, the cutoff of the lowpass digital filter.

Before the data is generated the user must enter the following information:

1. the name of the data file and fast phase timing file,

2. the format of the data file
   a. formatted or unformatted
   b. sequential or direct access
   c. time index or EOG data only

3. if input data parameters are to be included with the EOG data file.

The user can select the format of the EOG data files such that the data can be analyzed by any data analysis program; however, timing files are formatted with sequential access. The input parameters are included at the end of the EOG data files for user reference. A detailed description of the operation of the program appears in the text this report (Chapter IV). The input parameters specific to the type of data being generated (i.e., midposition gaze or sinusoidal pursuit) are discussed in the following.

A. Midposition Gaze

Before midposition gaze data can be generated the user must input the average slow phase velocity and the direction of the fast phases. The slow phase velocity (in deg./sec.) is necessary to determine the slope of the slow phase. The user also selects the direction of the fast phases (upward or downward). The user can select upward saccades or downward saccades. The direction of the fast phases is constant in each midposition gaze data file; therefore, the direction of the slow phase is always opposite to the direction of the fast phase. Tables A2 and A3 are examples of the prompts and responses required for generating
midposition gaze data.

Table A2. Prompts and Responses for generating midposition gaze with one (1) degree nystagmus without noise (Fig. A1).

1. MIDPOSITION GAZE
2. SINUSOIDAL PURSUIT
3. EXIT
(ALWAYS USE CAPITAL LETTERS)

ENTER TEST NUMBER FOR DATA TO BE GENERATED: 1
ENTER SAMPLING RATE (SAMPLES/SECOND): 200
ENTER 1 FOR SUPERIMPOSED NYSTAGMUS: 1
ENTER NYSTAGMUS AMPLITUDE (DEGREES): 1
ENTER FAST PHASE VELOCITY (DEGREES/SECOND): 400
ENTER SLOW PHASE VELOCITY (DEGREES/SECOND): 40
ENTER 1 IF RIGHT (UP)- OR 0 IF LEFT- (DOWN)-BEATING: 1
ENTER HORIZONTAL MIDPOSITION DATA FILE NAME
(IN APOSTROPHES AND NO MORE THAN 10 CHARACTERS): 'NYS50.DAT'
ENTER FORM OF OUTPUT FILES (FORMATTED OR UNFORMATTED)
(IN APOSTROPHES): 'FORMATTED'
ENTER ACCESS OF OUTPUT FILES (DIRECT OR SEQUENTIAL)
(IN APOSTROPHES): 'SEQUENTIAL'
DO YOU WANT A HEADER PRINTED WITH THE OUTPUT FILE
(Y OR N IN APOSTROPHES): 'Y'
DO YOU WANT TIME INCLUDED IN THE OUTPUT FILE
(Y OR N IN APOSTROPHES): 'N'
DO YOU WANT SUPERIMPOSED RANDOM NOISE
(Y OR N IN APOSTROPHES): 'N'
ENTER OUTPUT NYSTAGMUS TIME FILENAME
(IN APOSTROPHES): 'NYS10.TIM'

B. Sinusoidal Pursuit

The input parameters necessary before generating sinusoidal pursuit data are:
1. amplitude of the sinusoid;
2. frequency of the sinusoid;
3. initial direction of the sinusoid (upward or downward);
4. slope difference threshold; and
5. the data point ratio.

The amplitude of the sinusoid, in degrees, is determined by the user. The frequency of the sinusoid, in Hz, is important because it allows the user to evaluate the frequency dependency of the EOG analysis program. The program is not limited to any specific frequency range such that the user may select any frequency. However, the user needs to generate at least one full
Table A3. Prompts and responses required for generating midposition gaze data with one (1) degree nystagmus with 0.5 degrees (maximum amplitude) noise (Fig A2).

1. MIDPOSITION GAZE

2. SINUSOIDAL PURSUIT

3. EXIT

(ALWAYS USE CAPITAL LETTERS)

ENTER TEST NUMBER FOR DATA TO BE GENERATED: 1
ENTER SAMPLING RATE (SAMPLES/SECOND): 200
ENTER 1 FOR SUPERIMPOSED NYSTAGMUS: 1
ENTER NYSTAGMUS AMPLITUDE (DEGREES): 5
ENTER FAST PHASE VELOCITY (DEGREES/SECOND): 400
ENTER SLOW PHASE VELOCITY (DEGREES/SECOND): 40
ENTER 1 IF RIGHT (UP) OR 0 IF LEFT (DOWN) BEATING: 1
ENTER HORIZONTAL MIDPOSITION DATA FILE NAME (IN APOSTROPHES AND NO MORE THAN 10 CHARACTERS): 'NYS505.DAT'
ENTER FORM OF OUTPUT FILES (FORMATTED OR UNFORMATTED) (IN APOSTROPHES): 'FORMATTED'
ENTER ACCESS OF OUTPUT FILES (DIRECT OR SEQUENTIAL) (IN APOSTROPHES): 'SEQUENTIAL'
DO YOU WANT A HEADER PRINTED WITH THE OUTPUT FILE (Y OR N IN APOSTROPHES): 'Y'
DO YOU WANT TIME INCLUDED IN THE OUTPUT FILE (Y OR N IN APOSTROPHES): 'N'
DO YOU WANT SUPERIMPOSED RANDOM NOISE (Y OR N IN APOSTROPHES): 'Y'
ENTER OUTPUT NYSTAGMUS TIME FILENAME (IN APOSTROPHES): 'NYS10.TIM'
DO YOU WANT THE LOWPASS NOISE FILTER (Y OR N IN APOSTROPHES) (ONLY GOOD FOR 200 HZ SAMPLING RATE): 'N'
ENTER UPPER MAGNITUDE BOUND: 0.5
ENTER RANDOM NOISE FREQUENCY FILENAME (IN APOSTROPHES): 'FREQ.DAT'
ENTER RANDOM NOISE MAGNITUDE FILENAME (IN APOSTROPHES): 'MAG05.DAT'

The cycle of data and keep in mind that the data files are 15 seconds in length when selecting the frequency of the sinusoid. The user may select the initial direction of the sinusoid (upward or downward), but, in this case, the direction of the fast phases cannot be selected by the user because fast phases are automatically generated by the program in a direction opposite to the direction of the slow phase of the sinusoid. The slope difference threshold is necessary to avoid generating nystagmus beats at the maxima and minima of the sinusoid (an adequate value for the slope difference threshold is 0.001). An expanded description of the slope difference threshold is presented in the description of the operation of the program in Chapter IV. The
data point ratio must be entered so that the appropriate location of the fast phases can be
determined. Since the slow phase in a sinusoidal pursuit task can occur in either direction
(upward and downward), the data point ratio is used to determine where and in which direction
a fast phase will occur. As with midposition data, sinusoidal data are generated in tenths of
degrees. Tables A4 and A5 are examples of the prompts and responses required for generating
sinusoidal pursuit data.

Table A4. Prompts and responses required for generating sinusoidal pursuit data with one (1)
dergree nystagmus without noise (Fig. A3).

1. MIDPOSITION GAZE
2. SINUSOIDAL PURSUIT
3. EXIT
   (ALWAYS USE CAPITAL LETTERS)

ENTER TEST NUMBER FOR DATA TO BE GENERATED: 2
ENTER SAMPLING RATE (SAMPLES/SECOND): 200
ENTER 1 FOR SUPERIMPOSED NYSTAGMUS: 1
ENTER NYSTAGMUS AMPLITUDE (DEGREES): 5
ENTER FAST PHASE VELOCITY (DEGREES/SECOND): 400
ENTER SINUSOID MAGNITUDE (DEGREES): 20
ENTER FREQUENCY (HERTZ): .5
ENTER HORIZONTAL MIDPOSITION DATA FILE NAME
   (IN APOSTROPHES AND NO MORE THAN 10 CHARACTERS): 'SIN505.DAT'
ENTER FORM OF OUTPUT FILES (FORMATTED OR UNFORMATTED)
   (IN APOSTROPHES): 'FORMATTED'
ENTER ACCESS OF OUTPUT FILES (DIRECT OR SEQUENTIAL)
   (IN APOSTROPHES): 'SEQUENTIAL'
DO YOU WANT A HEADER PRINTED WITH THE OUTPUT FILE
   (Y OR N IN APOSTROPHES): 'Y'
DO YOU WANT TIME INCLUDED IN THE OUTPUT FILE
   (Y OR N IN APOSTROPHES): 'N'
DO YOU WANT SUPERIMPOSED RANDOM NOISE
   (Y OR N IN APOSTROPHES): 'N'
ENTER DATA POINT RATIO (INT >1): 10
ENTER THE SLOPE DIFFERENCE THRESHOLD: .001
ENTER OUTPUT NYSTAGMUS TIME FILENAME
   (IN APOSTROPHES): 'SIN101.TIM'
Table A5. Prompts and responses required for generating sinusoidal pursuit data with one (1) degree nystagmus with 0.5 degrees (maximum amplitude) noise (Fig. A4).

1. MIDPOSITION GAZE
2. SINUSOIDAL PURSUIT
3. EXIT
(ALWAYS USE CAPITAL LETTERS)

ENTER TEST NUMBER FOR DATA TO BE GENERATED: 2
ENTER SAMPLING RATE (SAMPLES/SECOND): 200
ENTER 1 FOR SUPERIMPOSED NYSTAGMUS: 1
ENTER NYSTAGMUS AMPLITUDE (DEGREES): 5
ENTER FAST PHASE VELOCITY (DEGREES/SECOND): 400
ENTER SINUSOID MAGNITUDE (DEGREES): 20
ENTER FREQUENCY (HERTZ): .5
ENTER HORIZONTAL MIDPOSITION DATA FILE NAME
(IN APOSTROPHES AND NO MORE THAN 10 CHARACTERS): 'SIN505.DAT'
ENTER FORM OF OUTPUT FILES (FORMATTED OR UNFORMATTED)
(IN APOSTROPHES): 'FORMATTED'
ENTER ACCESS OF OUTPUT FILES (DIRECT OR SEQUENTIAL)
(IN APOSTROPHES): 'SEQUENTIAL'
DO YOU WANT A HEADER PRINTED WITH THE OUTPUT FILE
(Y OR N IN APOSTROPHES): 'Y'
DO YOU WANT TIME INCLUDED IN THE OUTPUT FILE
(Y OR N IN APOSTROPHES): 'N'
DO YOU WANT SUPERIMPOSED RANDOM NOISE
(Y OR N IN APOSTROPHES): 'Y'
ENTER DATA POINT RATIO (INT >1): 10
ENTER THE SLOPE DIFFERENCE THRESHOLD: .001
ENTER OUTPUT NYSTAGMUS TIME FILENAME
(IN APOSTROPHES): 'SIN501.TIM'
DO YOU WANT THE LOWPASS NOISE FILTER
(Y OR N IN APOSTROPHES): 'N'
DO YOU WANT THE LOWPASS NOISE FILTER
(Y OR N IN APOSTROPHES)
(ONLY GOOD FOR 200 HZ SAMPLING RATE): 'N'
ENTER UPPER MAGNITUDE BOUND: 0.5
ENTER RANDOM NOISE FREQUENCY FILENAME
(IN APOSTROPHES): 'FREQ.DAT'
ENTER RANDOM NOISE MAGNITUDE FILENAME
(IN APOSTROPHES): 'MAGO5.DAT'

IV. PROGRAM OUTPUT
A. Midposition Gaze

The program automatically creates two data files, a timing file and a simulated EOG data file. The timing file contains the timing information (in seconds) of the fast events in the EOG file. The output is in tabular form with the number of the fast event, the slow phase starting times listed in one column and the fast phase starting times listed in a second column. The
timing information is in seconds, and the magnitude of the midposition data is in tenths of degrees. If the user selected the inclusion of the data parameters with output file, these parameters are appended to the EOG data file. Figure A1 is a sample output of simulated midposition gaze data with one (1) degree nystagmus without noise. Figure A2 is a sample output of simulated midposition gaze data with one (1) degree nystagmus with 0.5 degrees (maximum amplitude) noise.

B. Sinusoidal Pursuit

As with the midposition data, timing and simulated sinusoidal pursuit data files are automatically generated by the NASDAT program. The timing file contains a column with the slow phase ending time and another column with the fast phase ending time. The occurrence of nystagmus beats in the simulated sinusoidal pursuit data is different from that in the midposition gaze data, since fast phases in the sinusoidal data are opposite in direction to the slow phases, and fast phases occur in either upward or downward directions. Figure A3 is a sample of simulated sinusoidal pursuit data with (1) degree nystagmus without noise, and Figure A4 is a sample of simulated sinusoidal pursuit data with one (1) degree nystagmus with 0.5 degrees (maximum amplitude) noise.
APPENDIX B

SOFTWARE USER'S MANUAL:

FAST PHASE IDENTIFICATION PROGRAM (FPID)
I. INTRODUCTION

The following instructions will guide users of the Fast Phase Identification Program, version FPID.FOR or FPID.C. The FPID.FOR program is written in FORTRAN 77 for a VAX computer system (8650); whereas, the FPID.C program is written in C for an IBM-AT compatible machine (Packard Bell ISVT-286) with the Microsoft C Compiler (version 5.1). Although the hardware requirements are different for each version, the algorithm for fast phase identification and slow phase reconstruction is the same. A complete description of the operation of the program appears in the text of this report.

II. SOFTWARE REQUIREMENTS

Compilation of the source code is required before implementation. FPID.FOR is written in FORTRAN 77 such that any FORTRAN compiler adhering to this standard can be used to compile and run the program. The code in FPID.C is not fully transportable and, as written, requires compilation with the Microsoft C Compiler (version 5.1 or higher) (Microsoft Corp., Redmond, WA). Other compilers may be used after minor modifications to the source code of FPID.C.

One software requirement common to both versions of the FPID program is the format of the input EOG data files. Data files must contain only EOG data in a single column arrays. Also, the data to be analyzed by FPID must be floating point numbers (i.e., real). Timing data or data point index should not be included in the data file. If a data file does not meet these criteria, the data must be transformed for the FPID program to operate properly. Two data acquisition parameters are necessary so that the data can be read properly. The user must enter the sampling rate and the length of the sample record to be analyzed (in seconds). The sampling rate is used to determine the time interval between data points and, in conjunction with the length of the sample record, to determine how many data points from the EOG data file are to be analyzed. The total number of points to be analyzed must be less than or equal to
the total number of points in the file. The EOG data files must be in the same directory where the FPID is stored.

A. FPID.FOR

The FORTRAN version of FPID was developed on VAX computer, therefore, the size of the data arrays is not limited as they are in FPID.C. The data arrays used in the program and their description are listed in Table B1. The size of these arrays has been arbitrarily set at 10000 and may be changed according to the user requirements. The FPID.FOR code is standard FORTRAN 77; therefore, the program should be fully transportable.

Table B1. Description of data arrays in FPID.FOR

<table>
<thead>
<tr>
<th>NAME</th>
<th>DESCRIPTION</th>
</tr>
</thead>
<tbody>
<tr>
<td>HEOG</td>
<td>Original EOG data</td>
</tr>
<tr>
<td>YHEOG</td>
<td>DC shifted and smoothed EOG</td>
</tr>
<tr>
<td>FDEOG</td>
<td>First derivative of EOG</td>
</tr>
<tr>
<td>SDEOG</td>
<td>Second derivative of EOG</td>
</tr>
<tr>
<td>SPEOG</td>
<td>Reconstructed EOG</td>
</tr>
<tr>
<td>SPYHEOG</td>
<td>Smoothed reconstructed EOG</td>
</tr>
<tr>
<td>TIME</td>
<td>Timing for each data point</td>
</tr>
</tbody>
</table>

B. FPID.C

The code for FPID.C was translated from the FORTRAN version and modified to take advantage of the modular structure of the C language. The program employs dynamic memory allocation by calling `malloc()` (ANSI standard) from the `get_memory()` function. Dynamic memory allocation is used to increase the size of the data arrays beyond the 32 Kbytes data stack limit. However, the size of the arrays is limited by the memory capability of the system. For a system with 640 Kbytes of memory data arrays are limited to approximately 3000 elements each. For systems with more memory, the size of the EOG data arrays (HEOG, YHEOG, FDEOG, TIMES) may be changed by altering the value of the variable SIZEB in the


#define statement at the beginning of the source file. The timing information arrays (RTBEG, RTEND, LTBEG, LTEND) are initialized in the variable SIZEA in the #define statement at the beginning of the source file. Each of the timing information arrays is initialized to 100 elements, but the value of SIZEA may be changed if an unusual occurrence of saccadic events is observed in the data. Table B2 lists the names and description of the arrays in FPID.C. A complete description of variables used in the program is included at the end of the source code.

Table B2. Description of data arrays in FPID.FOR

<table>
<thead>
<tr>
<th>NAME</th>
<th>DESCRIPTION</th>
</tr>
</thead>
<tbody>
<tr>
<td>HEOG</td>
<td>Original and smoothed EOG data</td>
</tr>
<tr>
<td>YHEOG</td>
<td>DC shifted and filtered EOG</td>
</tr>
<tr>
<td>FDEOG</td>
<td>First derivative of EOG</td>
</tr>
<tr>
<td>TIMES</td>
<td>Timing for data</td>
</tr>
<tr>
<td>RTBEG</td>
<td>Beginning of right-going fast phase</td>
</tr>
<tr>
<td>RTEND</td>
<td>End of right-going fast phase</td>
</tr>
<tr>
<td>LTBEG</td>
<td>Beginning of left-going fast phase</td>
</tr>
<tr>
<td>LTEND</td>
<td>End of left-going fast phase</td>
</tr>
</tbody>
</table>

Screen graphics is available with the FPID.C version. Plotting of data is accomplished by calling graphics functions supplied with the Microsoft Compiler (v.5.1) from the plot() function in FPID.C. Plotting by FPID.C is possible on IBM AT compatible computers with: 1.) an Enhanced Graphics Adapter (EGA) card, and 2.) the Microsoft C Compiler (version 5.1), otherwise the calls to the plot() function must be deleted from the code before compiling.

III. PROGRAM OUTPUT

A. FPID.FOR

The program automatically creates two output data files, a timing file and a reconstructed EOG data file. The timing file contains the timing information (in seconds) of the saccadic
events in the EOG file. The output is in tabular form with the starting and ending times, and the direction of each event listed. The timing file has a .TIM extension (e.g., \textit{filename}.TIM). The reconstructed EOG file contains the EOG slow phases after removal of the fast phases, and the name of the reconstructed data file is the same as that of the original data file with \textquoteleft-R\textquoteright concatenated at the end, \textit{e.g.}, \textit{filename-R}.DAT. The output data file is a single column array of EOG data, neither time nor index information is included in the output EOG file. The format of the timing and reconstructed data files is the default FORTRAN I/O file standard. The timing and reconstructed EOG data files are stored in the directory where FPID.FOR is stored.

B. FPID.C

The program automatically creates two output data files, a timing file and a reconstructed EOG data file. The timing file contains the timing information (in seconds) of the saccadic events in the EOG file. The output is in tabular form with the starting and ending times, and the direction of each event listed. The timing file has a .TIM extension (e.g., \textit{filename}.TIM). The reconstructed EOG file contains the EOG slow phases after removal of the fast phases, and the name of the reconstructed EOG output data file is the same as that of the original data file with \textquoteleft-R\textquoteright concatenated at the end, \textit{e.g.}, \textit{filename-R}.DAT. The reconstructed data file is a single column array of EOG data, neither time nor index information is included in the output EOG file. The timing and reconstructed EOG data files are stored in the directory where FPID.C is stored.

A limitation of the DOS system in which FPID.C was developed is in the length of the filenames. The name of a file must not be longer than eight (8) characters plus a three (3) character extension, \textit{e.g.}, \textit{filename.dat}. Therefore, the name of the original data file should not be longer than six (6) characters, otherwise the filenames of the original data and reconstructed data may be identical. To prevent overwriting data, the program checks for the existence of a file before creating it for saving data. If a file already exists, the user is prompted to authorize
the overwriting of an already existing data file or renaming the file where data will be saved. However, the length of the data files must be limited to the conditions listed above to prevent accidental loss of data.

Graphic output is available to users of FPID.C during different stages of data analysis provided an EGA card and Microsoft C compiler (version 5.1 or higher) are installed. Another feature of FPID.C is immediate printout of the timing file after the data has been analyzed.
APPENDIX C

PROGRAM LISTING: NASDAT.FOR
C PROGRAM NASDAT.FOR

C PROGRAM ARTIFICIALLY GENERATES MIDPOSITION GAZE AND
C SINUSOIDAL PURSUIT EOG DATA

C DEFINE VARIABLES
REAL SR, MAXDEV, MINDEV, NYSAMP, FVEL, SVEL, SINMAG, SINFREQ
INTEGER CHOICE, NYS, DIR

C DETERMINE WHICH TEST DATA TO GENERATE
4 PRINT 5
5 FORMAT ("I- MIDPOSITION GAZE",/,,"2- SINUSOIDAL PURSUIT",/,,
* "T10,3- EXIT",/,,"(ALWAYS USE CAPITAL LETTERS)",/)
7 PRINT *, "ENTER TEST NUMBER FOR DATA TO BE GENERATED: '
READ *, CHOICE

C INPUT THE APPROPRIATE INFORMATION
IF (CHOICE.EQ.3) GOTO 200
PRINT *, "ENTER SAMPLING RATE (SAMPLES/SECOND): '
READ *, SR
IF (CHOICE.EQ.1.OR.CHOICE.EQ.2) THEN
10 PRINT *, "ENTER 1 FOR SUPERIMPOSED NYSTAGMUS: '
READ *, NYS
IF (NYS.LT.0.AND.NYS.NE.1) GO TO 10
IF (NYS.EQ.1) THEN
PRINT *, "ENTER NYSTAGMUS AMPLITUDE (DEGREES): '
READ *, NYSAMP
PRINT *, "ENTER FAST PHASE VELOCITY (DEGREES/SECOND): '
READ *, FVEL
IF (CHOICE.EQ.1) THEN
15 PRINT *, "ENTER 1 IF RIGHT(UP)-DOWNBEATING OR 0 IF
* LEFT(DOWN)-UPBEATING: '
READ *, DIR
IF (DIR.NE.0.AND.DIR.NE.1) GO TO 15
ENDIF
ELSEIF (NYS.EQ.0) THEN
NYSAMP=0
FVEL=0
SVEL=0
DIR=0
ENDIF
IF (CHOICE.EQ.2) THEN
PRINT *, "ENTER SINUSOID MAGNITUDE (DEGREES): '
READ *, SINMAG
PRINT *, "ENTER FREQUENCY (HERTZ): '
READ *, SINFREQ
ENDIF
IF (CHOICE.EQ.1) THEN
CALL MIDPOSITION (SR, NYS, NYSAMP, FVEL, SVEL, DIR)
ELSEIF (CHOICE.EQ.2) THEN
CALL SINUSOID (SR, SINMAG, SINFREQ, NYS, NYSAMP, FVEL, SVEL)
0059 ENDIF
0060 GO TO 4
0061 200 END

FUNCTIONS AND SUBROUTINES REFERENCED

<table>
<thead>
<tr>
<th>Type</th>
<th>Name</th>
<th>Type</th>
<th>Name</th>
</tr>
</thead>
<tbody>
<tr>
<td>MIDPOSITION</td>
<td>SINUSOID</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

0001 C
0002 C
0003 SUBROUTINE MIDPOSITION (SR,NYS,NYSAMP,FVEL,SVEL,DIR)
0004 REAL SR,NYSAMP,FVEL,SVEL,TS,SS,CY,POS(20000),TIME,FD,SD
0005 REAL FR,NOIS MAG,SGRMS,NOISRMS,SNRATIO,NOISFREQ,FTEMP,STEMP
0006 REAL X(-10:20000),Y(-10:20000),U(-10:20000),W(-10:20000),UB
0007 REAL A,B,C
0008 INTEGER NYS,DIR,TOTSAMP,FSAMP,SSAMP,CYCLES,I,J,K,M
0009 CHARACTER MIDHOR*20,MIDVER*20,ND*5,NZ*5,ANS*3,HEAD*3
0010 CHARACTER NOISE*3,FORMT*14,ACC*12,RANDFR*20,RANDMAG*20
0011 CHARACTER SACTIME*20,FI*5,T YPE*10
0012 C
0013 PRINT *, 'ENTER HORIZONTAL MIDPOSITION DATA FILE NAME'
0014 PRINT *, '(IN APOSTROPHES AND NO MORE THAN 10 CHARACTERS): '
0015 READ *, MIDHOR
0016 PRINT *, 'ENTER FORM OF OUTPUT FILES (FORMATTED OR UNFORMATTED)'
0017 PRINT *, '(IN APOSTROPHES): '
0018 READ *, FORMT
0019 PRINT *, 'ENTER ACCESS OF OUTPUT FILES (DIRECT OR SEQUENTIAL)'
0020 PRINT *, '(IN APOSTROPHES): '
0021 READ *, ACC
0022 PRINT *, 'DO YOU WANT A HEADER PRINTED WITH THE OUTPUT FILE'
0023 PRINT *, '(Y OR N IN APOSTROPHES): '
0024 READ *, HEAD
0025 PRINT *, 'DO YOU WANT TIME INCLUDED IN THE OUTPUT FILE'
0026 PRINT *, '(Y OR N IN APOSTROPHES): '
0027 READ *, ANS
0028 PRINT *, 'DO YOU WANT SUPERIMPOSED RANDOM NOISE'
0029 PRINT *, '(Y OR N IN APOSTROPHES): '
0030 READ *, NOISE
0031 OPEN (UNIT=2,FILE=MIDHOR,STATUS='NEW',ACCESS=ACC,
0032 * FORM=FORMT,RECL=65)
0033 TS=15.0*SR
0034 TOTSAMP=INT(TS)
0035 DO 10 I=1,TOTSAMP
0036 POS(I)=0
0037 10 CONTINUE
0038 FD=0
0039 SD=0
0040 IF (NYS.EQ.1) THEN
0041 PRINT *, 'ENTER OUTPUT NYSTAGMUS TIME FILENAME'
0042 PRINT *(IN APOSTROPHES):'
0043 READ *, SACTIME
0044 OPEN
(UNIT=3,FILE=SACTIME,STATUS='NEW',ACCESS='SEQUENTIAL')
0045 FS=(NYSAMP*0.1)/((FVEL*0.1)/SR)
0046 FSAMP=INT(FS)
0047 SS=(NYSAMP*0.1)/((SVEL*0.1)/SR)
0048 SSAMP=INT(SS)
0049 FD=FS/SD
0050 CY=(FSAMP+SSAMP)/FSAMP
0051 CYCLES=INT(CY)
0052 WRITE (3,20)
20 FORMAT (T5,'CYCLE',T15,'SCSTTIME',T25,'FCSTTIME')
0054 20 DO 50 J=1,CYCLES
0055  K=J-1
0056  STEMPE=((1+(K*(SSAMP+FSAMP))/SR)
0057  FTEMP=((1+SSAMP)+(K*(SSAMP+FSAMP))/SR)
0058  WRITE (3,25) J,STEMPE,FTEMP
25 FORMAT (T5,I3,T15,F7.4,T25,F7.4)
0059 DO 30 I=I,SSAMP
0060  M=I+(K*(SSAMP+FSAMP))
0061  POS(M)=(SVEL*0.1*I)/SR
0062  CONTINUE
0063 DO 40 I=I,FSAMP
0064  M=(I+SSAMP)+(K*(FSAMP+SSAMP))
0065  POS(M)=(NYSAMP*0.1)-(FVEL*0.1*I)/SR
0066  CONTINUE
0067 40 CONTINUE
0068 50 CONTINUE
0069 IF (DIR.EQ.1) THEN
0070  DO 60 I=I,TOTSAMP
0071  POS(I)=-POS(I)
0072  CONTINUE
0073 ENDIF
0074 ENDIF
0075 SIGNRMS=0.0
0076 DO 61 I=I,TOTSAMP
0077  SIGNRMS=SIGNRMS+(POS(I)**2.0)
0078 61 CONTINUE
0079 NOISRMS=0.0
0080 IF (NOISE.EQ.'N') THEN
0081  FIL='N'
0082 ELSEIF (NOISE.EQ.'Y') THEN
0083  PRINT *,'DO YOU WANT TO USE THE LOWPASS NOISE FILTER ?'
0084  PRINT *,(Y OR N IN APOSTROPHES)
0085  PRINT *,(ONLY GOOD FOR 200 HZ SAMPLING RATE):'
0086  READ *, FIL
0087 IF (FIL.EQ.'Y') THEN
0088  PRINT *,'DO YOU WANT MIT (35 HZ), UCLA (40 HZ), OR NASA
0089  * (80 HZ) FILTER ?'
0090  PRINT *,(ENTER MIT, UCLA, OR NASA IN APOSTROPHES):'
0091  READ *, TYPE
0092  ENDIF
0093 PRINT *,'ENTER UPPER MAGNITUDE BOUND: '
READ *, UB
PRINT *, 'ENTER RANDOM NOISE FREQUENCY FILENAME'
PRINT *, '(IN APOSTROPHES):'
READ *, RANDFR
OPEN (UNIT=3,FILE=RANDFR,STATUS='OLD')
PRINT *, 'ENTER RANDOM NOISE MAGNITUDE FILENAME'
PRINT *, '(IN APOSTROPHES):'
READ *, RANDMAG
OPEN (UNIT=4,FILE=RANDMAG,STATUS='OLD')
DO 70 I=1,TOTSAMP
   READ (3,68) NOISFREQ
   READ (4,68) NOISMAG
   68 FORMAT (T10,F10.7)
   69 IF (NOISMAG.GT.UB) THEN
      NOISMAG=NOISMAG/10.0
      GOTO 69
   ENDIF
   FR=(I*NOISFREQ*3.14152654)/SR
   X(I)=SIN(FR)*NOISMAG*0.1
   IF (FIL.EQ.'N') THEN
      NOISRMS=NOISRMS+(X(I)**2.0)
      POS(I)=POS(I)+X(I)
   ENDIF
   70 CONTINUE
   IF (FIL.EQ.'Y') THEN
      DO 71 1=-5,0
         X(I)=0.0
         Y(I)=0.0
         U(I)=0.0
         W(I)=0.0
      71 CONTINUE
      DO 72 I=1,TOTSAMP
         IF (TYPE.EQ.'MIT') THEN
            A=3.32588
            B=-2.818231
            C=4.507649
         ELSEIF (TYPE.EQ.'UCLA') THEN
            A=1.784893
            B=-2.180351
            C=3.604542
         ELSEIF (TYPE.EQ.'NASA') THEN
            A=-1.789568
            B=-0.9373096
            C=1.273122
         ENDIF
         Y(I)=(X(I)+2.0*X(I-1)+X(I-2)+A*Y(I-1)+B*Y(I-2))/C
      72 CONTINUE
   ENDIF
   DO 74 I=1,TOTSAMP
      IF (TYPE.EQ.'MIT') THEN
         A=3.32588
         B=-1.355153
         C=5.970727
      ELSEIF (TYPE.EQ.'UCLA') THEN
         A=1.784893
         B=-2.180351
         C=3.604542
      ELSEIF (TYPE.EQ.'NASA') THEN
         A=-1.789568
         B=-0.9373096
         C=1.273122
      ENDIF
      Y(I)=(X(I)+2.0*X(I-1)+X(I-2)+A*Y(I-1)+B*Y(I-2))/C
   74 CONTINUE
B=-0.9469664
C=4.837927
ELSEIF (TYPE.EQ.'NASA') THEN
  A=-1.789568
  B=-0.6464876
  C=1.563944
ENDIF
U(I)=(Y(I)+2.0*Y(I-1)+Y(I-2)+A*U(I-1)+B*U(I-2))/C
74 CONTINUE
DO 76 I=1,TOTSAMP
IF (TYPE.EQ.'MIT') THEN
  A=3.32588
  B=-0.5104444
  C=6.815436
ELSEIF (TYPE.EQ.'UCLA') THEN
  A=1.784893
  B=-0.2348712
  C=5.550022
ELSEIF (TYPE.EQ.'NASA') THEN
  A=-1.789568
  B=-0.4785813
  C=1.73185
ENDIF
W(I)=(U(I)+2.0*U(I-1)+U(I-2)+A*W(I-1)+B*W(I-2))/C
NOISRMS=NOISRMS+(W(I)**2.0)
POS(I)=POS(I)+W(I)
76 CONTINUE
ENDIF
ENDIF
SIGNRMS=(SIGNRMS/TOTSAMP)**(1.0/2.0)
SIGNRMS=10*SIGNRMS
NOISRMS=(NOISRMS/TOTSAMP)**(1.0/2.0)
NOISRMS=10*NOISRMS
IF (NOISE.EQ.'Y') THEN
  SNRATIO=SIGNRMS/NOISRMS
ELSEIF(NOISE.EQ.'N') THEN
  SNRATIO=0.0
ENDIF
IF (DIR.EQ.1) THEN
  ND='RIGHT'
  NZ='UP'
ELSEIF (DIR.EQ.0) THEN
  ND='LEFT'
  NZ='DOWN'
ENDIF
**C THE SIGNAL TO NOISE RATIO IS ',F9.4,/,**
**C WAS THE LOWPASS FILTER USED ?,A,/**
**C ALL DATA IS STORED IN 1/10 DEGREES'/**

```fortran
IF (ANS.EQ.'Y') THEN
  DO 120 I=1,TOTSAMP
  TIME=I/SR
  IF (HEAD.EQ.'Y'.AND.ACC.EQ.'DIRECT') THEN
    WRITE (2,110,REC=I) TIME, POS(I)
  ELSEIF (HEAD.EQ.'N'.AND.ACC.EQ.'DIRECT') THEN
    WRITE (2,110,REC=I) TIME, POS(I)
  ELSEIF (ACC.EQ.'SEQUENTIAL') THEN
    WRITE (2,110) TIME, POS(I)
  ENDIF
  110 FORMAT (T10,F8.4,T25,F10.6)
  120 CONTINUE
ELSEIF (ANS.EQ.'N') THEN
  DO 140 I=1,TOTSAMP
  IF (HEAD.EQ.'Y'.AND.ACC.EQ.'DIRECT') THEN
    WRITE (2,130,REC=I) POS(I)
  ELSEIF (HEAD.EQ.'N'.AND.ACC.EQ.'DIRECT') THEN
    WRITE (2,130,REC=I) POS(I)
  ELSEIF (ACC.EQ.'SEQUENTIAL') THEN
    WRITE (2,130) POS(I)
  ENDIF
  130 FORMAT (T10,F10.6)
  140 CONTINUE
ENDIF
IF (HEAD.EQ.'Y'.AND.ACC.EQ.'DIRECT') THEN
  WRITE (2,90,REC=TOTSAMP+I) SR,NYSAMP,FVEL,SVEL,FD,SD,ND,
  SIGNRMS,NOISRMS,
  * SNRATIO,FIL
ELSEIF (HEAD.EQ.'Y'.AND.ACC.EQ.'SEQUENTIAL') THEN
  WRITE (2,90) SR,NYSAMP,FVEL,SVEL,FD,SD,ND,SIGNRMS,
  * NOISRMS,SNRATIO,FIL
ENDIF
END
```

```
SUBROUTINE SINUSOID
(SR,SINMAG,SINFREQ,NYS,NYSAMP,FVEL,SVEL)
REAL SR,SINMAG,SINFREQ,NYSAMP,FVEL,SVEL,TS,FS,FR,DIFF
REAL POS(0:20000),TIME,SIGNRMS,NOISRMS,SQSIGN,FD,TRESH
REAL NOISMAG,NOIFREQ,SNRATIO,FP(0:500),FMAG
REAL TP,X(-10:20000),Y(-10:20000),PTEMP,NSBG,NSED
REAL U(-10:20000),W(-10:20000),UB,A,B,C
INTEGER NYS,TOTSAMP,FSAMP,SSAMP,CYCLES,I,J,K,M,WEND,EDIR
INTEGER INOIS(-20:5000),RLOPT,IRATIO,ISTART,IEND,NOISEND
CHARACTER SINHOR*20,SINVER*20,ANS*3,HEAD*3,NOISE*3,FIL*5
CHARACTER FORMT*14,ACC*12,RANDFR*20,RANDMAG*20,TYPE*10
CHARACTER SACTIME*20
```
PRINT *, 'ENTER HORIZONTAL PURSUIT DATA FILE NAME'
PRINT *, '(IN APOSTROPHES AND NO MORE THAN 10 CHARACTERS):'
READ *, SINHOR
PRINT *, 'ENTER FORM OF OUTPUT FILES (FORMATTED OR UNFORMATTED):'
READ *, FORMT
PRINT *, 'ENTER ACCESS OF OUTPUT FILES (DIRECT OR SEQUENTIAL):'
READ *, ACC
PRINT *, 'DO YOU WANT A HEADER PRINTED WITH THE OUTPUT FILE'
READ *, HEAD
PRINT *, 'DO YOU WANT TIME INCLUDED IN THE OUTPUT FILE'
READ *, ANS
PRINT *, 'DO YOU WANT THE SINUSOID TO GO RIGHT (UP) OR LEFT (DOWN):'
READ *, RLOPT
PRINT *, 'DO YOU WANT SUPERIMPOSED RANDOM NOISE'
READ *, NOISE
OPEN (UNIT=2, FILE=SINHOR, STATUS='NEW', ACCESS='SEQUENTIAL', FORM=FORMT, RECL=65)
IF (NYS.EQ.1) THEN
PRINT *, 'ENTER THE DATA POINT RATIO (INT.>1):'
READ *, IRATIO
PRINT *, 'ENTER THE SLOPE DIFFERENCE THRESHOLD: '
READ *, TRESH
ENDIF
TS=15.0*SR
TOTSAMP=INT(TS)
DO 10 I=0,TOTSAMP
  POS(I)=0
10 CONTINUE
SQSIGN=0.0
DO 13 I=0,TOTSAMP+1
  FR=(I*SINFREQ*2*3.14152654)/SR
  POS(I)=SIN(FR)*SINMAG*0.1*RLOPT
13 CONTINUE
FD=0
IF (NYS.EQ.1) THEN
PRINT *, 'ENTER OUTPUT NYSTAGMUS TIME FILENAME'
PRINT *, '(IN APOSTROPHES):'
READ *, SACTIME
OPEN (UNIT=3, FILE=SACTIME, STATUS='NEW', ACCESS='SEQUENTIAL', FORM=FORMT, RECL=65)
FS=(NYSAMP*SR)/FVEL
FSAMP=INT(FS)
IF (FS.LT.1.0) FSAMP=1
SSAMP=FSAMP*IRATIO
FD=FSAMP/SR
DO 17 I=1,FSAMP
FP(I)=0.1*I*FVEL/SR
IF (FP(I).GT.NYSAMP) FP(I)=NYSAMP
17 CONTINUE
FMAG=0.0
ISTART=0
IEND=SSAMP
INOIS(0)=0
INOIS(1)=IEND
K=2
WEND=TOTSAMP-FSAMP
18 DO 19 I=ISTART,IEND
POS(I)=POS(I)+FMAG
19 CONTINUE
TP=POS(IEND)-POS(IEND-1)
IF (TP.GT.0) IDIR=-1
IF (TP.LT.0) IDIR=1
IF (ABS(TP).LT.TRESH) THEN
ISTART=IEND+1
IEND=ISTART+SSAMP
INOIS(K-1)=IEND
IF (IEND.GT.WEND) GO TO 22
GOTO Ig
ENDIF
PTEMP=POS(IEND+FSAMP)
DO 20 J=I,FSAMP
I=IEND+J
POS(I)=POS(IEND)+IDIR*FP(J)
20 CONTINUE
ISTART=IEND+FSAMP+1
IEND=ISTART+SSAMP
INOIS(K)=ISTART
INOIS(K+1)=IEND
K=K+2
FMAG=POS(I)-PTEMP
IF (IEND.LE.WEND) GO TO 18
22 DO 24 I=ISTART,TOTSAMP
POS(I)=POS(I)+FMAG
24 CONTINUE
NOISEND=K-1
INOIS(K-1)=TOTSAMP
WRITE (3,30)
30 FORMAT (T5,'CYCLE',T15,'FCSq'rlME',T25,'FCEDTIME')
J=0
DO 40 I=1,NOISEND,2
J=J+1
NSBG=INOIS(I)/SR
NSED=INOIS(I+1)/SR
WRITE (3,35) J,NSBG,NSED
35 FORMAT (T5,I3,T15,F7.4,T25,F7.4)
40 CONTINUE
SIGNRMS=0.0
DO 54 I=1,TOTSAMP
SIGNRMS=SIGNRMS+(POS(I)**2.0)
54 CONTINUE
NOISRMS=0.0
IF (NOISE.EQ.'N') THEN
  FIL='N'
ELSEIF (NOISE.EQ.'Y') THEN
  PRINT *, 'DO YOU WANT TO USE THE LOWPASS NOISE FILTER ?'
  PRINT *, '(Y OR N IN APOSTROPHES)'
  PRINT *, '(ONLY GOOD FOR 200 HZ SAMPLING RATE)'
  READ *, FIL
  IF (FIL.EQ.'Y') THEN
    PRINT *, 'DO YOU WANT MIT (35 HZ), UCLA (40 HZ), OR NASA (80 HZ) FILTER?'
    PRINT *, '(ENTER MIT, UCLA OR NASA IN APOSTROPHES)'
    READ *, TYPE
    ENDIF
  PRINT *, 'ENTER UPPER MAGNITUDE BOUND'
  READ *, UB
  PRINT *, 'ENTER RANDOM NOISE FREQUENCY FILENAME'
  PRINT *, '(IN APOSTROPHES)'
  READ *, RANDFR
  OPEN (UNIT=3,FILE=RANDFR,STATUS='OLD')
  PRINT *, 'ENTER RANDOM NOISE MAGNITUDE FILENAME'
  PRINT *, '(IN APOSTROPHES)'
  READ *, RANDMAG
  OPEN (UNIT=4,FILE=RANDMAG,STATUS='OLD')
  DO 63 I=1,TOTSAMP
    READ (3,61) NOISFREQ
    READ (4,61) NOISMAG
    FORMAT (T10,F10.7)
    IF (NOISMAG.GT.UB) THEN
      NOISMAG=NOISMAG/10.0
      GOTO 62
    ENDIF
    FR=(I*NOISFREQ*2*3.14152654)/SR
    X(I)=SIN(FR)*NOISMAG*0.1
    IF (FIL.EQ.'N') THEN
      NOISRMS=NOISRMS+(X(I)**2.0)
      POS(I)=POS(I)+X(I)
    ENDIF
    63 CONTINUE
    IF (FIL.EQ.'Y') THEN
      DO 64 I=-5,0
        X(I)=0.0
        Y(I)=0.0
        U(I)=0.0
        W(I)=0.0
        64 CONTINUE
      DO 65 I=1,TOTSAMP
        IF (TYPE.EQ.'MIT') THEN
          A=3.32588
          B=-2.818231
          C=-4.507649
        ELSEIF (TYPE.EQ.'UCLA') THEN
A=1.784893
B=-2.180351
C=3.604542
ELSEIF (TYPE.EQ.'NASA') THEN
A=-1.789568
B=-0.9373096
C=1.273122
ENDIF
Y(I)=(X(I)+2.0*X(I-1)+X(I-2)+A*Y(I-1)+B*Y(I-2))/C
DO 65 I=1,TOTSAMP
IF (TYPE.EQ.'MIT') THEN
A=3.32588
B=1.355153
C=5.970727
ELSEIF (TYPE.EQ.'UCLA') THEN
A=1.784893
B=-0.9469664
C=4.837927
ELSEIF (TYPE.EQ.'NASA') THEN
A=-1.789568
B=-0.6464876
C=1.563944
ENDIF
U(I)=(Y(I)+2.0*Y(I-1)+Y(I-2)+A*U(I-1)+B*U(I-2))/C
DO 66 I=1,TOTSAMP
IF (TYPE.EQ.'MIT') THEN
A=3.32588
B=-0.5104444
C=6.815436
ELSEIF (TYPE.EQ.'UCLA') THEN
A=1.784893
B=-0.2348712
C=5.550022
ELSEIF (TYPE.EQ.'NASA') THEN
A=-1.789568
B=-0.4785813
C=1.73185
ENDIF
W(I)=(U(I)+2.0*U(I-1)+U(I-2)+A*W(I-1)+B*W(I-2))/C
NOISRMS=NOISRMS+(W(I)**2.0)
POS(I)=POS(I)+W(I)
ENDIF
SIGNRMS=(SIGNRMS/TOTSAMP)**(1.0/2.0)
SIGNRMS=10*SIGNRMS
NOISRMS=(NOISRMS/TOTSAMP)**(1.0/2.0)
NOISRMS=10*NOISRMS
IF (NOISE.EQ.'Y') THEN
SNRATIO=SIGNRMS/NOISRMS
ELSEIF (NOISE.EQ.'N') THEN
SNRATIO=0.0
0228    ENDIF
0229 70 FORMAT (1X,'THE SAMPLING FREQUENCY IS ',F8.3,' HZ',/,  
0230    '*C THE NYSTAGMUS AMPLITUDE IS ',F4.1,' DEGREES',/,  
0231    '*C THE FAST PHASE VELOCITY IS ',F6.1,' DEGREES/SECOND',/,  
0232    '*C THE FAST PHASE DURATION IS ',F7.4,' SECONDS',/,  
0233    '*C THE SINUSOID MAGNITUDE IS ',F5.1,' DEGREES',/,  
0234    '*C THE SINUSOID FREQUENCY IS ',F8.3,' HZ',/,  
0235    '*C THE SIGNAL RMS VALUE IS ',F9.4,/,  
0236    '*C THE NOISE RMS VALUE IS ',F9.4,/,  
0237    '*C THE SIGNAL TO NOISE RATIO IS ',F9.4,/,  
0238    '*C WAS THE LOWPASS FILTER USED ? ',A,/,  
0239    '*C ALL DATA IS STORED IN 1/10 DEGREES',/)  
0240    IF (ANS.EQ.'Y') THEN  
0241      DO 100 I=1,TOTSAMP  
0242        TIME=I/SR  
0243        IF (HEAD.EQ.'Y'.AND.ACC.EQ.'DIRECT') THEN  
0244          WRITE (2,80,REC=I) TIME, POS(I)  
0245        ELSEIF (HEAD.EQ.'N'.AND.ACC.EQ.'DIRECT') THEN  
0246          WRITE (2,80,REC=I) TIME,POS(I)  
0247        ELSEIF (ACC.EQ.'SEQUENTIAL') THEN  
0248          WRITE (2,80) TIME, POS(I)  
0249        ENDIF  
0250      80 FORMAT (T10,F8.4,T25,F10.6)  
0251    100 CONTINUE  
0252    ELSEIF(ANS.EQ.'N') THEN  
0253      DO 120 I=1,TOTSAMP  
0254        IF (HEAD.EQ.'Y'.AND.ACC.EQ.'DIRECT') THEN  
0255          WRITE (2,110,REC=I) POS(I)  
0256        ELSEIF (HEAD.EQ.'N'.AND.ACC.EQ.'DIRECT') THEN  
0257          WRITE (2,110,REC=I) POS(I)  
0258        ELSEIF (ACC.EQ.'SEQUENTIAL') THEN  
0259          WRITE (2,110) POS(I)  
0260        ENDIF  
0261    110 FORMAT (T10,F10.6)  
0262    120 CONTINUE  
0263    ENDIF  
0264    IF (HEAD.EQ.'Y'.AND.ACC.EQ.'DIRECT') THEN  
0265      WRITE (2,70,REC=TOTSAMP+1) SR,NYSAMP,FVEL,FD,SINMAG,  
0266      * SINFREQ,SIGNRMS,NOISRMS,  
0267      * SNRATIO,FIL  
0268    ELSEIF (HEAD.EQ.'Y'.AND.ACC.EQ.'SEQUENTIAL') THEN  
0269      WRITE (2,70) SR,NYSAMP,FVEL,FD,SINMAG,SINFREQ,  
0270      * SIGNRMS,NOISRMS,SNRATIO,FIL  
0271    ENDIF  
0272    RETURN  
0273 END  

COMPILATION STATISTICS  
Run Time: 5.16 seconds  
Elapsed Time: 8.33 seconds  
Page Faults: 1308  
Dynamic Memory: 1248 pages
APPENDIX D

PROGRAM LISTING: FPID.C
/*
EOG Fast Phase identification and Slow Phase Reconstruction.
*/
Code conversion of fpid.for from FORTRAN to C: May 1990.
Converted by: Karen J. Poindexter and Carlos A. Rodriguez-Garcia

/*
EOG Fast Phase identification and Slow Phase Reconstruction.
*/

#include <stdio.h>
#include <stdlib.h>
#include <string.h>
#include <conio.h>
#include <math.h>
#include <graph.h>

/*Global constants*/
#define SIZEA 100
#define SIZEB 3010

/*Global variables*/
FILE *fopen0, *in_file, *out_file;
float *rtbeg, *rtend, *ltbeg, *ltend;
float *heog, *yheog, *fdeog, *times;

main()
{
int n, j, k, i, l, ln, p, ltcnt, rtcnt;
int nco, var, frmt, istep, itlst, istrt, istp, islg, lterm;
int isl, ilf, temp, templ, count, max_count, index=l;
short int yes, rtflag, ltflag, more=l;
float length, xsum, xmean, xlgt, fdrms, fdrmsth, tht, hht,h;
float ssmfd, ssfd, xn, dxsum, xilf, q, denom, slope, yint;
float dysum, dxysum, dxssum, fsample, fpdur, vel, num_pts;
char datafile[15], filenam[15], ext[15], ch;
static char printer[]="PRN";

strcpy(ext,"exit");
printf("\n\n");
message();

do /*while (more != 0)*/
{
system("cls");
}
get_memory();
printf("\n\n\nENTER NAME OF EOG DATAFILE (without .ext) OR EXIT > ") ;
scanf("%s", filenam);
if (!(strcmpi (filenam,"exit")))
{
exit(0);
}
sprintf(datafile, "%s.dat", filenam);
printf("n");
printf("Enter sampling rate (in Hz) > ");
scanf("%f", &fsample);
printf("Enter length of datafile (in seconds) > ");
scanf("%f", &length);
length=length*f sample;

system("cls");
open_read(datafile);
for (n = 0; n <= (int)length-1; n++)
{
    fscanf(in_file, "%f", &heog[n]);
times[n]=(float)n*(1/fsample);
}
printf("Do you want to plot EOG now? (1- Yes) > ");
scanf("%d%c", &yes,&ch);
if (yes)
plot(length,fsample);

/*Computing the mean of the data - removing DC component*/
printf("\n\nDo you want to remove DC? (1- Yes) > ");
scanf("%d%c", &yes,&ch);
if (yes)
{
printf("Removing DC components...\n");
xsum = 0.0;
xlgt = length;
for(i = 1; i <= (int)length; i++)
xsum = xsum + heog[i];
xmean = xsum / length;
for(i = 1; i <= (int)length; i++)
heog[i] = heog[i] - xmean;
/* Averaging the data*/
smooth_data(length);

/*Filtering data*/
filter_data(length);

/* sprintf(datafile, "%s_s.dat", filenam);
open_write(datafile);
*/

for (n=1; n<=(int)length ;n++)
fprintf(out_file, "%f\n", yheog[n]);
fclose(out_file);

for (n=1; n<=(int)length ;n++)
fprintf(out_file, "%f\n", yheog[n]);
fclose(out_file);

/* First derivative*/

istep = 1;
h = (float)istep / fsample;
printf("\nComputing Fourth Order (5 pt.) Central Difference...
");

for (i = 3; i <= (int)length-2; i++)
  fdeog[i] = ((yheog[i-2] - yheog[i+2])
            + (8.0*(yheog[i+1] - yheog[i-1]))) / (h * 12.0);
  fdeog[1] = fdeog[3];
  fdeog[2] = fdeog[3];
  fdeog[(int)length] = fdeog[(int)length-2];
  fdeog[(int)length-1] = fdeog[(int)length-2];

ssfd = 0.0;
for(i = 1; i <= (int)length-20; i++)
  ssfd = ssfd + (fdeog[i] * fdeog[i]);
ssmfd = ssfd / ((length - 20));
fdrms = sqrt(ssmfd);

/* sprintf(datafile, "%s_d.dat", filenam);
open_write(datafile);
*/

/* Identification of fast phases*/

fdrmsth = drms * 2.0;
rtcnt = 0;
ltcnt = 0;
isl = 0;
ht = 0.0;
hht = 0.0;
do /*while(islg < length)*/
{
iterm = (int)length - islg;
j = 1;
do
{
++j;
} while((abs(fdeog[islg+j])) <= (abs(fdrmsth)) && (j <= lterm));
itlsl = j + islg;
if(fdeog[itlsl] >= 0.0)
goto lp1;
/*printf("negative values start\n");*/
for(i = 1; i <= 10; i++)
if (fdeog[itlsl-i] >= 0.0)
goto lp2;
/*printf("positive values start.\n");*/
for(i = 1; i <= 10; i++)
if (fdeog[itlsl-i] < 0.0)
goto lp3;
/*printf("negative values end.\n");*/
istrt = itlsl - 1;
++ltcnt;
ltbeg[ltcnt] = times[istrt+10];
for (k = 1; k <= 30; k++)
if (fdeog[itlsl+k] >= 0.0)
{
istp = itlsl + k;
lend[ltcnt] = times[istp+6];
goto lp4;
} /*end if*/
/*printf("positive values end.\n");*/
isrt = itlsl - 1;
++rtcnt;
rtbeg[rtcnt] = times[istrt+10];
ln = 1;
do
{
++ln;
} while((fdeog[itlsl+ln] >= 0.0) && (ln <= 30));
214  istp = itlst + ln;
215  rtend[rtcnt] = times[istp+6];
216
217  lp4: /*Least Squares Fit*/
218  dxsum = 0.0;
219  dxssum = 0.0;
220  dysum = 0.0;
221  dxysum = 0.0;
222  q = 1.0;
223
224  for (isl = istrt-10; isl < istrt; isl++)
225  {
226      dxsum = dxsum + q;
227      dxssum = dxssum + (q * q);
228      dysum = dysum + yheog[isl];
229      dxysum = dxysum + (q * yheog[isl]);
230      q = q + 1.0;
231  } /*end for*/
232
233  denom = dxssum - (dxsum * dxsum) / 11.0;
234  if (denom != 0)
235      slope = (dxysum - (dxsum * dysum) / 11.0) / denom;
236  else
237      slope = 0.;
238  yint = (dysum / 11.0) - slope * (dxsum / 11.0);
239
240  xilf = 12.0;
241  for (ilf = istrt+1; ilf <= istp; ilf++)
242  {
243      yheog[ilf] = (slope * xilf) + yint;
244      xilf = xilf + 1.0;
245  } /*end for*/
246
247  /*Reconstructing slow phases*/
248  hht = hht + yheog[istp] - yheog[istp+1];
249
250  for(i = islg+1; i <= istp; i++)
251      heog[i] = yheog[i] + tht;
252
253  tht = hht;
254  islg = istp;
255
256  lp5: printf(".");
257  } while(islg < (int)length);
258
259  if (ltflag)
260      ltcnt--;
261  else if (rtflag)
262      rtcnt--;
printf("Number of Fast Phases Detected: %d... HIT [ENTER] TO CONTINUE",ltcnt+rtcnt);

getchar();

system("cls");

printf("Do you want to plot the reconstructed EOG now? (1- Yes) > ");

scanf("%d%c", &yes,&ch);

if (yes)
  plot(length-10,fsample);

/*5-Point Smoother*/

printf("Do you want to smooth reconstructed EOG? (1- Yes) > ");

scanf("%d%c", &yes,&ch);

if (yes)
  smooth_data(length);

printf("Do you want to plot the reconstructed EOG again? (1- Yes) > ");

scanf("%d%c", &yes,&ch);

if (yes)
  plot(length,fsample);

/*Creating timing file*/

sprintf(datafile, "%s.tim", filenam);

open_write(datafile);

write_timing(datafile,rtcnt,ltcnt);

printf("Do you want a hardcopy of timing file now? (1- Yes) ");

scanf("%d%c",&var,&ch);

if (var)
  open_write(printer);

write_timing(datafile,rtcnt,ltcnt);

/*Creating data file*/

sprintf(datafile, "%s-r.dat", filenam);

open_write(datafile);

for (i = 1; i <= (int)length; i++)
  fprintf(out_file, "%f",heog[i]);

fclose(out_file);
system("cls");
free_memory(); /*Freeing memory*/
printf("nRun program again? (1- Yes) > ");
scanf("%d%c", &more,&ch);
printf("n");
} while(more != 0);
/*end main*/

/*Allocate memory needed for the data arrays*/
get_memory()
{
rtbeg = (float *)calloc(SIZEA, sizeof(float));
rtend = (float *)calloc(SIZEA, sizeof(float));
ltbeg = (float *)calloc(SIZEA, sizeof(float));
ltend = (float *)calloc(SIZEA, sizeof(float));
if (lrtbeg II ! rtend II !ltbeg II !ltend)
{
printf("***MEMORY ALLOCATION ERROR A***n");
exit(0);
}
heog = (float *)calloc(SIZEB, sizeof(float));
yheog = (float *)calloc(SIZEB, sizeof(float));
fdeog = (float *)calloc(SIZEB, sizeof(float));
times = (float *)calloc(SIZEB, sizeof(float));
if (!heog II !yheog II !fdeog II !times)
{
printf("***MEMORY ALLOCATION ERROR B***n");
exit(0);
}
/*end get_memory*/

/*Free memory allocated for data arrays*/
free_memory()
{
free(times); free(heog); free(yheog); free(fdeog);
free(rtbeg); free(rtend); free(ltbeg); free(ltend);
}
/*Pause the program until the user hits ENTER*/
message()
{
    printf(" EOG FAST PHASE IDENTIFICATION and SLOW PHASE RECONSTRUCTION")

    printf(" Files Read              Type");
    printf("----------------------

orig_filename.DAT   EOG Data - ASCII");
    printf(" Files Generated          Type");
    printf("----------------------

orig_filename.TIM    Formatted Report - ASCII")
}

printf(" orig_filename_R.DAT   EOG Data (no index)- ASCII I");

printf(" ANY EOG DATA WILL BE SUCCESSFULLY ANALYZED (e.g., fast phases timing) BUT");
printf(" CORRECT VELOCITY CALCULATIONS AND DATA RECONSTRUCTION CAN BE DONE ON SCALED");
printf(" DATA ONLY (e.g., eog=degrees"));
printf(" EOG FILENAME MUST HAVE A .dat EXTENSION");
printf(" EOG FILENAME MUST ALSO BE LESS THAN -10- CHARACTERS IN LENGTH");
printf(" IF YOU HAVE TO RENAME DATASE file EXIT PROGRAM AND RENAME FILE");
printf(" HIT [ENTER] TO CONTINUE...");
getchar();

/*open input datafile*/
open_read (file)
char file[15];
{  
    if((in_file = fopen(file, "r") == NULL)
    {
        printf(" ***ERROR opening data file %s.....BYE\n", file);
        exit (0);
    }

    printf("Opened %s - reading data...\n", file);

open_read Local Symbols

<table>
<thead>
<tr>
<th>Name</th>
<th>Class</th>
<th>Type</th>
<th>Size</th>
<th>Offset</th>
<th>Register</th>
</tr>
</thead>
<tbody>
<tr>
<td>file</td>
<td>...........</td>
<td>param</td>
<td>0004</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
411
412 /*open output datafile*/
413 open_write(file)
414 char file[15];
415 {
416    int ans;
417    char newfile[15];
418    if ((out_file = fopen(file, "r")) != NULL)
419       {
420          printf("FILE ALREADY EXISTS -- DO YOU WANT TO OVERWRITE? (1=Ye
421            s ) ");
422          scanf("%d",&ans);
423          if (ans!=1)
424             {
425                 printf("ENTER NEW FILENAME (without .ext) ");
426                 scanf("%s",newfile);
427                 sprintf(file,"%s.dat",newfile);
428             }
429        }
430    if ((out_file = fopen(file, "w")) == NULL)
431       {
432           printf("***ERROR opening file %s......BYE\n", file);
433           exit(0);
434       }
435    printf("Writing to file %s\n", file);
436    }
437
438 smooth_data(len)
439 float len;
440 {
441    int i;
442
443    printf("5-point smoother...\n");
444    for (i = 3; i <= (int)len-2; i++)
445        yheog[i] = .1*(heog[i-2] + heog[i+2]) + .22*(heog[i-1] + heog[i+1])
446            + .33*heog[i];
447
448    yheog[1] = yheog[3];
449    yheog[2] = yheog[3];
450    yheog[(int)len] = yheog[(int)len-2];
451    yheog[(int)len-1] = yheog[(int)len-2];
452
453    for (i = 1; i <= (int)len; i++)
454        heog[i] = yheog[i];
455
456    }
filter_data(len)
float len;
{
    int i,j,p,n,nco=15;
    float h,sum;
    double COEF[15];

    COEF[1] = .0037165603;
    COEF[2] = .020235427;
    COEF[3] = .013399956;
    COEF[4] = -.040643737;
    COEF[5] = -.066073574;
    COEF[6] = .061152663;
    COEF[7] = .30294424;
    COEF[8] = .43047285;
    for(n = 1; n <= 7; n++)
        COEF[16-n] = COEF[n];

    printf("15-point FIR filter\n");

    for (i = 2; i <= (int)len+nco; i++)
        {
            sum = 0.0;
            for (j = 1; j <= nco; j++)
                {
                    if (j < i)
                        {
                            if (i-j <= (int)len)
                                {
                                    h = COEF[j] * heog[i-j];
                                    sum = sum + h;
                                }
                        }
                }
            yheog[i-1] = sum;
        }

    p = 14;
    for (j = 15; j <= (int)len+p; j++)
        yheog[p+j] = yheog[j];
    for (i = 1; i <= 14; i++)
        yheog[(int)len-i-1] = yheog[(int)len-14];

    write_timing(file,num_rt,num_lt)
    int num_rt,num_lt;
    char file[15];
    {
        int n;
        ..
517  fputs('
014', out_file);
518  fprintf(out_file, "FAST PHASE TIMING INFORMATION FOR: %s\n", file);
519  fprintf(out_file, "LEFT PHASES ARE DOWNWARD PHASES RIGHT PHASES ARE UPWARD PHASES\n\n");
520  fprintf(out_file, "RIGHT PHASE TIMING\n");
521  fprintf(out_file, "PHASE # START END\n");
522  fprintf(out_file, "\n")
523  for (n = 1; n <= num_rt; n++)
524        fprintf(out_file, "%3d %5.3f %5.3f\n", n, rtbeg[n], rtend[n ]

525  };
526  fprintf(out_file, "\n\n")
527  fprintf(out_file, "LEFT PHASE TIMING\n")
528  fprintf(out_file, "PHASE # START END\n")
529  fprintf(out_file, "\n")
530  for (n = 1; n <= num_lt; n++)
531        fprintf(out_file, "%3d %5.3f %5.3f\n", n, ltbeg[n], ltend[n ]

532  };
533  fclose(out_file);
534 
535 
536  
537  
538  
539  plot(len,fs)
540  float len, fs;
541  {
542  int i,n;
543  long unsigned int g;
544  float maxeog,maxtime;
545  short oldcolor;
546  
547  maxeog=0;
548  for (i=1; i<=(int)len ;i++)
549  {
550    if (abs(heog[i]) > maxeog)
551      maxeog=abs(heog[i]);
552  }
553  
554  maxtime=len/fs;
555  for (i=1; i<=(int)len ;i++)
556  {
557    g = (long)i * 560 /long int)len;
558    yheog[i] = heog[i] * 120. / maxeog;
559  }
560 
561 
562  _setvideomode(_ERESCOLOR);
563  _moveto(54, 30);
564  _lineto(614, 30);
565  _lineto(614, 284);
568  _lineto (54, 284);
569  _lineto (54, 30);
570  
571  n=94;
572  do
573  {  
574    _moveto ((short)n, 30);
575    _lineto ((short)n, 284);
576    n=n+40;
577  } while(n<=594);
578  
579  oldcolor=__getcolor();
580  n=55;
581  do
582  {  
583    _moveto (54, (short)n);
584    if (n--=155)
585   setcolor(5);  
586    else
587      _setcolor(oldcolor);
588  _lineto (614, (short)n);
589    n=n+25;
590  } while(n<=255);
591  
592  
593  _setcolor(10);
594  _moveto(54,155);
595  for (i=1; i<=(int)len ;i++)
596  {  
597    g = (long)* 560 /(long int)len;
598    _lineto (54+(short)g, 155-(int)yheog[i]);
599  }
600  
601  _moveto(54,145);
602  printf('_a %-3.2fknkn %-3.2fknkn %-3.2fknkn %-3.2fknkn

/*0
degrees= 155*/
603  0 degrees= 155*/
604  printf("%n-3.2f\n%n-3.2f\n%n-3.2f\n%n-3.2f\n\n", maxe
605  printf("E\nO 0\nG");
606  printf("n%-3.2f\n%-3.2f\n%-3.2f\n%-3.2f\n%-3.2f\n\n", maxeog/5*4, maxeog/5*3, maxeog/5*2, maxeog/5*1);
607  printf("TIME");
608  printf("n


TIME");
609  
610  while (!kbhit());
611  _setvideomode(_DEFAULTMODE);
612  
613  
614  )
Code size = 158a (5514)
Data size = 0aa1 (2721)
Bss size = 0000 (0)

No errors detected

/* VARIABLE DICTIONARY: a listing of all variables used and their function.

Global:

SIZEA  constant; the number of elements allocated for rtbeg, rtend,
SIZEB  constant; the number of elements allocated for heog, yheog,
*fopen() a C pointer used to open an outside file;
in file a pointer set to the input EOG file;
*out_file a pointer set first to the output Timing File, then to the
output Data File;
rtnbeg  an array of 100 floating-point elements allocated
dynamically; used to mark the end of the right phases;
*rtend  an array of 100 floating-point elements allocated
dynamically; used to mark the beginning of the right phases;
*ltbeg  an array of 100 floating-point elements allocated
dynamically; used to mark the end of the left phases;
*ltend  an array of 100 floating-point elements allocated
dynamically; used to mark the beginning of the left phases;
*heog  an array of 3100 floating-point elements allocated
dynamically; holds the EOG data, read in from the input
file; stores most of the changes made to the wave and
finally stores the reconstructed slow phase wave;
yheog  an array of 3100 floating-point elements allocated
dynamically; used to temporarily store some of the
changes made to the wave;
fdeog  an array of 3100 floating-point elements allocated
dynamically; holds the first derivative of the wave;
times  an array of 3100 floating-point elements allocated
dynamically; holds the timing information of the wave;
read in from the EOG input file;

Local:

length  the number of points to read; equal to sampling rate*seconds;
read in from the keyboard;
filename array holding the name (with no extension) of the EOG input
file; read in from the keyboard;
datafile array holding the name (including the extension) of the file
to be opened;
more  boolean (0 or 1); set to 1 if the main loop is to be repeated
(run program with another EOG file); set to 0 if main loop
is not to be repeated, either because of an error or by the
user's choice;  
   boolean (0 or 1); set to 1 if the user wants 5-point  
   smoothing and/or another 15-point FIR filter;  
   the mean of the EOG data; used to remove the DC component;  
used in finding the mean of the EOG data;  
the number of the FIR filter being used; equal to 15;  
array of constants; used in filtering the data;  
factor used in the first 15-point FIR filter;  
factor used in the second 15-point FIR filter;  
used to hold the sum in the first 15-point FIR filter;  
used to hold the sum in the second 15-point FIR filter;  
used in Differentiating; equal to 1;  
used in calculating the RMS of the first derivative;  
used in calculating the RMS of the first derivative;  
the RMS of the first derivative;  
holds the first derivative RMS threshold value, 2*fdrms;  
used in Identification of fast phases;  
used in Identification of fast phases;  
used to mark the position in Identification of fast phases;  
used to mark the beginning of a phase;  
used to mark the end of a phase;  
counter used when identifying right phases;  
counter used when identifying left phases;  
used to mark a position in Least Squares Fit;  
used to mark a position in Least Squares Fit;  
factor used in Least Squares Fit; equal to 10;  
factor used in Least Squares Fit;  
factor used in Least Squares Fit;  
the sum of the x values in the Least Squares Fit;  
the sum of the y values in the Least Squares Fit;  
the sum of the x values squared in the Least Squares Fit;  
(the sum of the x values)*(the sum of the y values) in  
the Least Squares Fit;  
the value of the denominator in the Least Squares Fit;  
the value of the slope in the Least Squares Fit;  
the value of the y intercept in the Least Squares Fit;  
used in finding the height correction factor for the  
reconstructed wave;  
the height correction factor for the reconstructed wave;  

n, j, k, i, l, ln, p  counters used throughout the program  
*/
APPENDIX E

PROGRAM LISTING: FPID.FOR
PROGRAM FPID.FOR

INTEGER LENGTH,RTCNT,LTCNT
REAL RTBEG(200),RTEND(200),LTBEG(200),LTEND(200),TIME(10000)
CHARACTER * 20 FILENAM
CHARACTER * 30 INFILE,TIMFILE,OUTFILE
CHARACTER TEXT*5, REXT*5
REAL FSAMPLE, HEOG(10000), XT(10000), COEF(15), YHEOG(10000),
1 SPEOG(10000), SPYHEOG(10000), FDEOG(10000)

COEF(1) = .0037165603
COEF(2) = .020235427
COEF(3) = .013399956
COEF(4) = -.040643737
COEF(5) = -.066073574
COEF(6) = .061152663
COEF(7) = .30294424
COEF(8) = .43047285
DON= 1,7
COEF(16-N) = COEF(N)
END DO

TEXT = '.TIM'
REXT = '-R'
PRINT *,' FPID'
PRINT *, ' EOG FAST PHASE IDENTIFICATION AND'
PRINT , SLOW PHASE RECONSTRUCTION'
PRINT *'
PRINT *,' ENTER EOG DATAFILE ENCLOSED IN APOSTROPHES (no .ext)'
READ *, INFILE
CALL CHARCONCAT(INFILE,TIMFILE,TEXT)
CALL CHARCONCAT(INFILE,OUTFILE,REXT)
PRINT 5, INFILE, OUTFILE, TIMFILE
FORMAT (T5,'INPUT FILE (.dat): ',A,/,T5,'RECONSTRUCTED FILE (.dat): ',A,/)
FORMAT (T5,'TIMING FILE: ',A,/)
PRINT *, ' ENTER SAMPLING RATE (in Hz)'
READ *, FSAMPLE
PRINT *, ' ENTER LENGTH OF FILE (in seconds)'
READ *, LENGTH
LENGTH = LENGTH * FSAMPLE

TYPE *, ' OPENING INPUT DATAFILE'
OPEN (UNIT=2,FILE=INFILE,STATUS='OLD')
TYPE *,' OPENED DATAFILE- READING DATA'
DO N=1,LENGTH
READ (2,*) HEOG(N)
FORMAT (F10.6)
TIME(N) = N / FSAMPLE
END DO
CLOSE (UNIT=2,STATUS='KEEP')
ISTEP = 1
XLGT = FLOAT(LENGTH)

COMPUTE THE MEAN OF THE DATA- REMOVE DC
XSUM = 0.0
DO 58 I = 1, LENGTH
   XSUM = XSUM + HEOG(I)
CONTINUE
XMEAN =XSUM/XLGT
DO 59 I = 1, LENGTH
   HEOG(I) = HEOG(I) - XMEAN
CONTINUE

AVERAGE DATA
DO 500 1 = 3, LENGTH-2
   YHEOG(I) =.11*(HEOG(I-2)+HEOG(I+2))+.22*(HEOG(I-1)+HEOG(I+1))
   + .33*HEOG(I)
CONTINUE
YHEOG(1) = YHEOG(3)
YHEOG(2) = YHEOG(3)
YHEOG(LENGTH) = YHEOG(LENGTH-2)
YHEOG(LENGTH-1) = YHEOG(LENGTH)

FILTERING DATA WITH 15-POINT FIR FILTER!
DO 80 1 = 2, LENGTH+NCO
   SUM =0.0
   DO 70 J = 1,NCO
      L = J
      IF (J .GE. I) GO TO 70
      IF (I-J .GT. LENGTH) GO TO 70
      H = COEF(J) * HEOG(I-J)
      SUM = SUM + H
   CONTINUE
YH OG(I-1) = SUM
CONTINUE
NCO = 15
DO 81 J = 15, LENGTH+J2
   YHEOG(J-J2) = YHEOG(J)
CONTINUE

DO 630 I = 1, 14
YHEOG(LENGTH-I-1)=YHEOG(LENGTH-14)
CONTINUE

H = FLOAT(ISTEP)/FSAMPLE
L = LENGTH
TYPE *, ' COMPUTING FOURTH ORDER FIRST DIFFERENCE'

DO 87 I = 3, L-2
FDEOG(I) = ((YHEOG(I-2) - YHEOG(I+2)) + (8.*(YHEOG(I+1) - YHEOG(I-1))))/(L*12.)
CONTINUE
FDEOG(1) = FDEOG(3)
FDEOG(2) = FDEOG(3)
FDEOG(L) = FDEOG(L-2)
FDEOG(L-1) = FDEOG(L-2)

FDRMS = 0.
SSFD = 0.
DO 700 I = 1, LENGTH-20
SSFD = SSFD + FDEOG(I)**2.
CONTINUE
SSMFD = SSFD/FLOAT(LENGTH-20)
FDRMS = SQRT(SSMFD)
TYPE 725,FDRMS
725 FORMAT (' RMS OF 1ST DERV. =',F8.3)

IDENTIFICATION OF FAST PHASES

FDRMSTH = FDRMS*2.
TYPE 410, FDRMSTH
410 FORMAT (' 1ST DERV. RMS THRESHOLD =',F9.3)

RTCNT = 0
LTCNT = 0
ISLG = 0
THT = 0.
HHT = 0.
LTERM = LENGTH - ISLG
DO 112 J = 1, LTERM
IF (ABS(FDEOG(ISLG+J)) .GT. ABS(FDRMSTH)) GO TO 115
CONTINUE
ITLST = J + ISLG
TYPE 411,ITLST
411 FORMAT (' INDEX TSH EXCD AT I =',I5)
IF (FDEOG(ITLST) .GE. 0.) GO TO 120
C TYPE *, 'NEGATIVE VALUES START'
DO 117 L = 1, 10
   IF (FDEOG(ITLST - L) .GE. 0.) GO TO 124
117 CONTINUE
CC TYPE *, 'POSITIVE VALUES START'
120 DO 122 L = 1, 10
   IF (FDEOG(ITLST - L) .LT. 0.) GO TO 128
122 CONTINUE
CC TYPE *, 'NEGATIVE VALUES END'
124 ISTRT = ITLST - L
CC TYPE 412, ISTRT
126 CONTINUE
DO 126 K = 1, 30
   IF (FDEOG(ITLST + K) .GE. 0.) GO TO 135
126 CONTINUE
CC TYPE *, 'POSITIVE VALUES END'
128 ISTRT = ITLST - L
CC TYPE 414, ISTRT
130 CONTINUE
DO 130 LN = 1, 30
   IF (FDEOG(ITLST + LN) .LT. 0) GO TO 134
130 CONTINUE
   ISTP = ITLST + LN
CC TYPE 415, ISTP
134 ISTP = ITLST + K
CC TYPE 416, ISTP
138 Q = 1.0
140 CONTINUE
DO 140 ISL = ISTRT-10, ISTRT
   DXSUM = DXSUM + Q
   DXSSUM = DXSSUM + Q*Q
   DYSUM = DYSUM + YHEOG(ISL)
   DXYSUM = DXYSUM + Q*YHEOG(ISL)
   Q = Q + 1.0
140 CONTINUE
C
C LEAST SQUARES FIT
XN = 10.
DXSUM = 0.
DXSSUM = 0.
DYSUM = 0.
DXYSUM = 0.
Q = 1.0
C
DO 140 ISL = ISTRT-10, ISTRT
   DXSUM = DXSUM + Q
   DXSSUM = DXSSUM + Q*Q
   DYSUM = DYSUM + YHEOG(ISL)
   DXYSUM = DXYSUM + Q*YHEOG(ISL)
   Q = Q + 1.0
140 CONTINUE
C
DENOM = DXSSUM - (DXSUM*DXSUM) / 11.0
SLOPE = (DXYSUM - (DXSUM*DYSUM) / 11.0) / DENOM
YINT = (DYSUM / 11.0) - SLOPE * (DXSUM / 11.0)

CC TYPE 417, SLOPE, YINT

CC TYPE 417, SLOPE, YINT
FORMAT (' SLOPE = ', F12.5, ' YINT = ', F12.5)

NAME = XILF = 12.0
DO 142 ILF = ISTRT, ISTOP
    YHEOG(ILF) = SLOPE*XILF + YINT
    XILF = XILF + 1.0
CONTINUE

CC TYPE *, 'RECONSTRUCT SLOW PHASE'

HHT = HHT + YHEOG(ISTP) - YHEOG(ISLP+1)

FORMAT (' HEIGHT CORRECTION = ', F12.5)

TYPE 421, ISLP, ISTOP
FORMAT (' STRT SP INDX = ', I7, ' STP SP INDX = ', I7)

DO 145 I = ISLP+1, ISTOP
    SPEOG(I) = YHEOG(I) + THT
CONTINUE

THT = HHT
ISLP = ISTOP

FORMAT (' NEW SEARCH STARTS AT I = ', I4)
CC TYPE *, 'TO CONTINUE TYPE: 1'
CC ACCEPT *, IXS
IF (ISLP .LT. LENGTH) GO TO 10

RTCNT = RTCNT - 1
LTCNT = LTCNT - 1

OPEN (UNIT=3, FILE=TIMFILE, STATUS='NEW')
WRITE (3, 11)
FORMAT (' UPBEATING PHASES'

DO N=1,RTCNT
    WRITE (3, 14) N, RTBEG(N), RTEND(N)

WRITE (3, 16)
FORMAT (' DOWNBEATING PHASES'

DO N=1,KTCNT
    WRITE (3, 17) N, LTPEG(N), LTEND(N)

C TYPE 17, N, LTPEG(N), LTEND(N)

FORMAT (T2, I4,T15,F8.3,T30,F8.3)
**FUNCTIONS AND SUBROUTINES REFERENCED**

**CHARCONCAT**

```
subroutine charconcat(filename,cfilename,ext)
character filename*20,cfilename*30,ext*5
do i= 1,20
  if (filename(i:i).eq.' ') go to 14
  enddo
  cfilename=filename(1:i-1)//ext
return
end
```

**COMPILATION STATISTICS**

- Run Time: 2.27 seconds
- Elapsed Time: 3.95 seconds
- Page Faults: 1023
- Dynamic Memory: 1076 pages
Figure 1A. Flowchart of NASDAT Program.
Figure 1B. Flowchart of NASDAT Program (continued).
Figure 1C. Flowchart of NASDAT Program (continued).
Figure 2. Sample synthetic midposition gaze data with five (5) degrees of saccadic jump (without noise).
Figure 3. Sample synthetic 0.5 Hz sinusoidal pursuit data with five (5) degrees of saccadic jump (without noise).
Figure 4A. Plot of optokinetic stimulus.

Figure 4B. Plot of human optokinetic EOG data set.
Figure 5A. Plot of 0.10 Hz sinusoidal pursuit stimulus.

Figure 5B. Plot of human sinusoidal pursuit EOG data set.
Figure 6A. Plot of pseudorandom stimulus.

Figure 6B. Plot of human pseudorandom EOG data set.
Figure 7. Overall flowchart of US Air Force Program.
Figure 8A. Flowchart of calibration section of US Air Force Program.
Figure 8A. Flowchart of calibration section of US Air Force Program.
Process first 10.48 sec. of velocity data: Zero right-going data

Process second 10.48 sec. of velocity data: Zero left-going data

Calculate left-going average (BSCAL)

Calculate right-going average (USCAL)

\[(USCAL + BSCAL) + 2 \rightarrow \text{CALSUM} \]
\[2.5 \times \text{USCAL} \rightarrow \text{KLIMIT}\]

RETURN

Figure 8B. Flowchart of calibration section of US Air Force Program (continued).
Figure 9A. Flowchart of analysis section of US Air Force Program.
Figure 9B. Flowchart of analysis section of US Air Force Program (continued).
Figure 10. Plot of individual errors by USAF Program for midposition gaze data (maximum SNR of 25).
Figure 11. Plot of individual errors by USAF Program in midposition gaze data (maximum SNR of 200).
Figure 12. Plot of Error Index by USAF Program for midposition gaze data.
Figure 13. Plot of individual errors by USAF Program for sinusoidal pursuit data with two (2) degrees of saccadic jump.
Figure 14. Plot of individual errors by USAF Program for sinusoidal pursuit data with five (5) degrees of saccadic jump.
Figure 15. Plot of Error Index by USAF Program for 0.05 Hz sinusoidal pursuit data.
Figure 16. Plot of Error Index by USAF Program for 0.10 Hz sinusoidal pursuit data.
Figure 17. Plot of Error Index by USAF Program for 0.50 Hz sinusoidal pursuit data.
Figure 18. Plot of Error Index by USAF Program for 0.80 Hz sinusoidal pursuit data.
Figure 19A. Flowchart of UCLA SINUXEC Program.
Figure 19B. Flowchart of UCLA SINUXEC Program (continued).
Figure 20. Plot of individual errors and Error Index by SINUXEC Program for midposition gaze data with one (1) degree of saccadic jump.
Figure 21. Plot of Error Index by SINUXEC Program for midposition gaze data.
Figure 22. Plot of individual errors by SINUXEC Program for midposition gaze data.
Figure 23. Plot of Error Index by SINUXEC Program for 0.50 Hz sinusoidal pursuit data.
Figure 24. Plot of Error Index by SINUPEC Program for 0.05 Hz sinusoidal pursuit data.
Figure 25. Plot of Error Index by SINUXEC Program for 0.10 Hz sinusoidal pursuit data.
Figure 26. Plot of individual errors by SINUXEC Program for 0.10 Hz sinusoidal pursuit data.
Figure 27A. Flowchart of UCLA CALORXEC Program.
Figure 27B. Flowchart of UCLA CALORXEC Program (continued).
Figure 28. Plot of Error Index by CALORXEC Program for midposition gaze data.
Figure 29. Plot of individual errors by CALORXEC Program for midposition gaze data.
Figure 30. Plot of individual errors by CALORXEC Program for sinusoidal pursuit data with 1:5 and 1:15 data point ratios.
Figure 31. Plot of Error Index by CALORXEC Program for sinusoidal pursuit data with 1:5 and 1:15 data point ratios.
Define Modula and Sign Functions

Enter starting and ending point of file; Input file specification

Set up I/O channels

Enter SR, MAT & SCALE FACTOR

Find USR of acceleration, velocity and LP filters

Read data

Function ISGN

Scale input data; Compute velocity & PAF output; Compute moving avg. and RMS of acceleration for previous 0.25 seconds

Buffer full?

Calculate $T_a$ and $T_s$ from RMS of acceleration signal

PAF > $T_a$?

Figure 32A. Flowchart of MIT M2MI86 Program.
Figure 32B. Flowchart of MIT M2MI86 Program (continued).
Figure 33. Plot of individual errors and Error Index by MIT M2MI86 Program for midposition gaze data with one (1) degree of saccadic jump.
Figure 34. Plot of individual errors by MIT M2MI86 Program for midposition gaze data.
Figure 35. Plot of Error Index by MIT M2MI86 Program for midposition gaze data.
Figure 36. Plot of individual errors by MIT M2MI86 Program for 0.50 Hz sinusoidal pursuit data.
Figure 37. Plot of Error Index by MIT M2MI86 Program for 0.05 Hz sinusoidal pursuit data.
Figure 38. Plot of Error Index by MIT M2M86 Program for 0.10 Hz sinusoidal pursuit data.
Figure 39. Plot of Error Index by MIT M2M186 Program for 0.50 Hz sinusoidal pursuit data.
Figure 41. Plot of individual errors by MIT M2MI86 Program for 0.10 Hz sinusoidal pursuit data.
Figure 42A. Flowchart of Harvard Program.
Figure 42B. Flowchart of Harvard Program (continued).
Figure 43. Plot of Error Index by Harvard Program for midposition gaze data.
Figure 44. Plot of individual errors by Harvard Program for midposition gaze data.
Figure 45. Plot of Error Index by Harvard Program for 0.05 Hz sinusoidal pursuit data.
Figure 46. Plot of Error Index by Harvard Program for 0.10 Hz sinusoidal pursuit data.
Figure 47. Plot of Error Index by Harvard Program for 0.50 Hz sinusoidal pursuit data.
Figure 48. Plot of individual errors by Harvard Program for 0.50 Hz sinusoidal pursuit data.
Figure 49A. Flowchart of FPID Program.
Figure 49B. Flowchart of FPID Program (continued).
Figure 50. Plot of individual errors and Error Index by FPID Program for midposition gaze data with one (1) degree of saccadic jump.
Figure 51. Plot of Error Index by FPI Program for midposition gaze data.
Figure 52. Plot of individual errors by FPID Program for midposition gaze data.
Figure 53. Plot of Error Index by FPID Program for 0.50 Hz sinusoidal pursuit data.
Figure 54. Plot of Error Index by FPID Program for 0.05 Hz sinusoidal pursuit data.
Figure 55. Plot of Error Index by FPID Program for 0.10 Hz sinusoidal pursuit data.
Figure 56. Plot of noise on the human sinusoidal pursuit data set.
Figure 57. Plot of Error Index by five (5) of the programs (USAF/SAM, UCLA SINUXEC, MIT M2MI86, Harvard and NASA FPID) for midposition gaze data with three (3) degrees of saccadic jump.
Figure 58. Plot of Error Index by five (5) of the programs (USAF/SAM, UCLA SINUXEC, MIT M2M186, Harvard and NASA FPID) for 0.10 Hz sinusoidal pursuit data with three (3) degrees of saccadic jump.
Figure A1. Plot of simulated midposition gaze data with five (5) degrees of saccadic jump without noise.
Figure A.2. Plot of simulated midposition gaze data with five (5) degrees of saccadic jump with 0.5 degree (maximum amplitude) noise.
Figure A3. Plot of simulated sinusoidal pursuit data with five (5) degrees of saccadic jump without noise.
Figure A4. Plot of simulated sinusoidal pursuit data with five (5) degrees of saccadic jump with 0.5 degree (maximum amplitude) noise.