Dynamic Measurements of Gear Tooth Friction and Load

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1. INTRODUCTION

The dynamic forces at the point of tooth contact are of considerable interest to the designers of high-speed, lightweight gearing. Accurate prediction of the dynamic loads can assist in minimizing the size and weight of a transmission. In a helicopter application, where the transmission is a significant fraction of vehicle weight, such a reduction would be an important factor in overall vehicle performance.

A program to experimentally and theoretically study fundamental mechanisms of gear dynamic behavior is being undertaken at the NASA Lewis Research Center in support of a joint research program between NASA and the U.S. Army. This paper presents the results of dynamic tooth-fillet strain gage measurements from the NASA gear-noise rig, and it introduces a technique for using these measurements to separate the normal and tangential (friction) components of the load at the tooth contact. Resolution of the contact force is desirable for several reasons. Two of these reasons are the following:

(1) A primary output of analytical models of gear dynamic behavior is typically the normal force at the point of contact (e.g., [1] and [2]).

(2) The measurement of dynamic friction of meshing gears does not appear to have yet been carried out successfully. An interesting trial was carried out by Benedict and Kelly [3], but it was discontinued because of dynamic response problems. Anderson and Lowenthal [4] computed overall losses due to friction and found good agreement between theoretical predictions and experimental data. Krantz and Handschuh [5] applied a similar technique to an epicyclic gear rig, obtaining good correlation at low oil temperatures, but poorer correlation at higher oil temperatures. However, this technique cannot detect the variation in friction during the tooth engagement cycle. There is also the problem of separating the power loss due to gear tooth friction from power losses due to other sources such as bearings, windage, and so forth.

Extensive measurements of lubrication conditions at a sliding-rolling contact have been carried out on disk machines [6]. These experiments are of considerable value in confirming the existence of elastohydrodynamic lubrication and in identifying the separate regimes of lubrication that prevail under the various slide-to-roll ratios. However, the usefulness of the modes of behavior and friction coefficients in predicting lubrication conditions at an actual tooth contact, where the degree of sliding changes throughout the tooth engagement cycle (typical duration, 250 µsec), needs to be verified. In this short period of time, large changes occur in the lubricant temperature, shear, and viscosity at pressures up to 1.4 GPa (200 000 lbf-in.'). Dyson [7] reported temperatures up to 400 °C and oscillatory shear rates up to 107 sec'. These conditions cannot readily be produced outside of an actual tooth mesh.

Visiting scientist from Australian Aeronautical Research Laboratory.
Friction at the tooth contact is important for determining not only power loss and efficiency, but also for understanding gear-tooth scoring and wear. An important parameter in scoring is the friction coefficient [3]. Friction greatly affects the heat input to the lubricant when sliding velocities are high.

This report presents dynamic, gear-tooth strain measurements from low-contact-ratio spur gears tested in the NASA gear-noise rig. The technique used to convert the strain in the lubricant into normal and tangential (friction) tooth loads is described. Plots of normal and tangential forces, for both static and dynamic conditions, are presented for a representative range of loads and speeds. The normal force and dynamic strain data have been used to verify a gear dynamics code in another related report [8].

2. APPARATUS

2.1 Test Facility

These tests were conducted in the NASA Lewis gear-noise rig (Fig. 1). This rig comprises a simple gearbox powered by a 150-kW (200-hp) variable speed electric motor, with an eddy-current dynamometer that loads the output shaft. The gearbox can be operated at speeds up to 6000 rpm. The rig was built to carry out fundamental studies of gear noise and of dynamic behavior of gear systems. It was designed to allow testing of various configurations of gears, bearings, dampers, and supports.

A poly-V belt drive served as a speed increaser between the motor and input shaft. A soft coupling was installed on the input shaft to reduce input torque fluctuations caused by a nonuniformity of the belt at the splice. Test gear parameters are shown in Table 1, test rig parameters in Table 2, and gear tooth profile traces in Fig. 2. The tooth surface roughness was measured by using an involute-gear-checking machine with a diamond stylus of approximately 10-µm (0.0003-in.) radius. The surface roughness varied along the length of the tooth, with the region near the root appearing to be lightly polished. The maximum surface roughness was estimated to be 1.34 µm (34 µm) peak-to-peak, or an average of 0.43 µm (11 µm) (Fig. 3). The gear rig was operated at an oil fling-off temperature of 54±2 °C (130±5 °F). At the mean temperature of 54 °C, the viscosity of the synthetic oil (Table 2) used in the tests was 14 cSt (11.6 cP). Natural frequencies from a four degrees-of-freedom eigensolution [8] are also shown in Table 2.

2.2 Instrumentation

General-purpose, constantan foil, resistance strain gages (gage length, 0.38 mm (0.015 in.)) were installed in the tooth-root fillets on both the loaded (tensile) and unloaded (compression) side of two adjacent teeth on the output (driven) gear (Fig. 4). To measure maximum tooth bending stress, the gages were placed at the 30° position (roll angle) the torque was applied to the input shaft to measure roll angle and hence determine load location; the position of the encoder was adjusted so it would produce 1 pulse/revolution at a known roll angle.

3. TEST PROCEDURE

3.1 Calibration

Calibration of the strain gages on the instrumented (driven) gear was conducted to provide a matrix of strain output versus applied load. Before commencing the strain gage calibration, the gears were demagnetized. This demagnetization reduced the apparent strain resulting from the gages moving through the magnetic field of the adjacent gear. At normal gear operating speeds, magnetic effects can induce an error signal in the gage.

For calibration, the instrumented gear was meshed with a special gear whose adjacent teeth had been ground away; this permitted loading of a single tooth only. The calibration was carried out for each of the two instrumented teeth for roll angles ranging from 12° to 30°. At each test position (roll angle) the torque was applied at three levels - 45 percent, 88.5 percent, and 132 percent of the nominal value of 71.8 N-m (635 in.-lb). At each of these load levels the sliding direction was reversed (by reversing roll direction), and a linear curve was fit to the data for each sliding direction. By reversing the roll direction, the instrumented gear was effectively tested as both the driven gear (output) and driving gear (input). In each instance the gear was rotated a small angle (approximately 1°) in the intended direction of roll until the desired roll angle was reached, so as to definitely establish a sliding direction.

The strain gage calibration apparatus is shown in Fig 5. The results of the calibration for gages 1 to 4 are given in Figs. 6 and 7, for loading on tooth 1. The arrows indicate roll direction. The results for loading on tooth 2 were very similar.
TABLE 1. - TEST GEAR PARAMETERS

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gear type</td>
<td>standard involute, full-depth tooth</td>
</tr>
<tr>
<td>Number of teeth</td>
<td>28</td>
</tr>
<tr>
<td>Module, mm (diametrical pitch in.)</td>
<td>3.175(8)</td>
</tr>
<tr>
<td>Face width, mm (in.)</td>
<td>6.35 (0.25)</td>
</tr>
<tr>
<td>Pressure angle, deg</td>
<td>20</td>
</tr>
<tr>
<td>Nominal (100-percent) torque, N·m (in.-lb)</td>
<td>71.77 (635.25)</td>
</tr>
<tr>
<td>Theoretical contact ratio</td>
<td>1.64</td>
</tr>
<tr>
<td>Driver modification amount, mm (in.)</td>
<td>0.023 (0.0009)</td>
</tr>
<tr>
<td>Driven modification amount, mm (in.)</td>
<td>0.025 (0.0010)</td>
</tr>
<tr>
<td>Driver modification start, deg</td>
<td>24</td>
</tr>
<tr>
<td>Driven modification start, deg</td>
<td>24</td>
</tr>
<tr>
<td>Tooth root radius, mm (in.)</td>
<td>1.35 (0.053)</td>
</tr>
<tr>
<td>Average surface roughness, µm (µin.)</td>
<td>0.43 (11)</td>
</tr>
</tbody>
</table>
TABLE II. — TEST RIG PARAMETERS

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input inertia, $J_i$, kg-m$^2$</td>
<td>0.0237</td>
<td>(lb-sec$^2$-in.)</td>
</tr>
<tr>
<td>Gear inertia, $J_1$, $J_2$, kg-m$^2$</td>
<td>0.0000364</td>
<td>(lb-sec$^2$-in.)</td>
</tr>
<tr>
<td>Load inertia, $J_L$, $J_3$, kg-m$^2$</td>
<td>0.085</td>
<td>(lb-sec$^2$-in.)</td>
</tr>
<tr>
<td>Input stiffness, $K_i$, N-m/rad</td>
<td>341</td>
<td>(lb-in./rad)</td>
</tr>
<tr>
<td>Gearbox stiffness, $K_0$, N-m/rad</td>
<td>6158</td>
<td>(lb-in./rad)</td>
</tr>
<tr>
<td>Load stiffness, $K_L$, N-m/rad</td>
<td>12,700</td>
<td>(lb-in./rad)</td>
</tr>
<tr>
<td>Synthetic turbine oil</td>
<td>MIL-L-23699B</td>
<td></td>
</tr>
<tr>
<td>Viscosity at 130 °C, cSt, (cP)</td>
<td>14</td>
<td></td>
</tr>
<tr>
<td>Natural frequencies (eigensolution), Hz</td>
<td>6.56, 52.5, 1220</td>
<td></td>
</tr>
</tbody>
</table>

Figure 2.—Test gear profile traces.

Figure 3.—Surface roughness measurements of driven gear.

Figure 4.—Strain gage installation and location on test gear.
3.2 Data Acquisition

3.2.1 Static strain data. - Strain data were recorded under static (nonrotating) conditions for the gear set assembled in its normal (running) configuration with the standard running gear replacing the calibration gear. The measurements were made for two reasons: first, as a check on the accuracy of the method used to resolve tooth force into normal and tangential components; and second, to provide information on load sharing characteristics of the gear assembly. A strain gage bridge circuit was used to record strains for roll angles from 12° to 40° relative to tooth 2. Torque levels of 37, 88, 100, and 132 percent were applied, but unlike the single-tooth case, linear curve-fitting of these data was not appropriate because of the kinematic nonlinearities introduced by load sharing when more than one pair of teeth are in contact. As for the single-tooth case, these measurements were carried out for the instrumented gear acting as both the driven and driving gear, thus reversing the sliding direction.

3.2.2 Dynamic strain data. - Dynamic strains were recorded for the 4 gages, for a speed-load matrix of 28 points: 4 speeds (800, 2000, 4000, and 6000 rpm) and 7 torque levels (16, 31, 47, 63, 79, 94, and 110 percent of the nominal value of 71.8 N-m (635 in.-lb)). The data were recorded by 14-bit data recorders via a slip-ring assembly. Sample rates used were 50,000 Hz per channel for the 2000-, 4000-, and 6000-rpm speeds, and 20,000 Hz per channel for the 800-rpm speed. A continuous record, consisting of 10,000 data scans, was made at each speed so as to give a record length of 0.2 sec at 50,000 Hz, and 0.5 sec at 20,000 Hz. Because of the interest in comparing tensile and compressive strains on each tooth, data from these two gages were simultaneously recorded along with the encoder signal. This procedure was repeated for the second instrumented tooth.

The data were then digitally resampled, by using linear interpolation, at either 1000 or 2000 samples per revolution (depending on speed) and synchronously averaged. Time domain synchronous averaging, a technique now in wide use in gear diagnostics [10], was used here to reduce noise effects (especially from the torque fluctuation caused by the belt drive). Its implementation requires two data channels—one for timing signal data and one for strain data. The timing signal data provided resample intervals for exactly one revolution.

4. ANALYSIS

For a single tooth, measurement of the strain outputs $S_r$ and $S_t$ of gages mounted on the compressive and tensile sides of the tooth respectively (Fig. 4) will, in principle, enable resolution of the tooth forces $F_n$ (normal) and $F_t$.
(tangential), provided that the response of these two gages to the two forces is linearly independent. The response of the gages can then be expressed as

\[ S_c = a_{11}F_n + a_{12}F_f \]  
(4.1)

\[ S_s = a_{21}F_n + a_{22}F_f \]  
(4.2)

or simply as

\[ \{S\} = [a]\{F\} \]  
(4.3)

where \[ \{S\} = \begin{bmatrix} S_c \\ S_s \end{bmatrix} \]

\[ \{F\} = \begin{bmatrix} F_n \\ F_f \end{bmatrix} \]

and \( a_{ij} \) is the strain influence coefficient; that is, the strain at \( i \) due to a unit normal force \( (j = 1) \) or a unit friction force \( (j = 2) \).

The strain influence coefficients \( a_{ij} \) are evaluated by alternately setting \( F_n \) and \( F_f \) in equations (4.1) and (4.2) to zero. In practice, neither \( F_n \) nor \( F_f \) can actually be zero because a normal force between the teeth is a prerequisite for a sliding force to develop. However, because strain values were recorded for both directions of sliding (that is, for the instrumented gear acting as both driving and driven gear) at each roll angle value, we inferred that the average of these two strain values is equivalent to the frictionless case, and that the effect of friction alone will be one-half the difference between the two values. Thus, the coefficients \( a_{1j} \) and \( a_{2j} \) (which relate to friction) are evaluated from half the difference between the driving gear and driven gear curves of Fig. 6. Likewise, the strain coefficients \( a_{ij} \) and \( a_{2j} \) (which relate to normal force) are evaluated from the average of these two curves. The solution for \( F_n \) and \( F_f \) is found by premultiplying both sides of equation (4.3) by \([a]^{-1}\); hence

\[ \{F\} = [a]^{-1}\{S\} \]  
(4.4)

The analysis presented above ignores the influence on strains \( S_c \) and \( S_s \) due to loading on adjacent teeth. In the case of thin-rim gears [11], this effect can be on the order of 12 percent. For the thick-rim gears used here, however, the influence from adjacent teeth is at most 3 percent (compare Figs. 6 and 7). In the data presented in this paper, the influence of adjoining teeth has been included. The computational procedure is outlined in the Appendix.

5. RESULTS AND DISCUSSION

5.1 Calibration

Tooth-fillet strains for 100-percent torque were evaluated by fitting a linear curve to the calibration data for the three torque levels. These strains at gages 1 to 4 are plotted in Figs. 6 and 7 as a function of roll angle, for loading of tooth 1. Notable from these curves is the significant influence of static friction on strain output; the tensile gage (see Fig. 6(a)) shows a difference in strain between the driving- and driven-gear cases (when sliding direction reverses) that is 27 percent of the mean strain reading. The significance of this is twofold: first, it is difficult to establish a "no-friction" curve; and second, and possibly more important, these curves (particularly the tensile curve) illustrate the effect that tooth friction has on the results. It is apparent from Fig. 6 that the compressive gage is much less influenced by friction and, thus, would be expected to give the best indication of normal force if only one gage were used. This is further confirmed by the tooth strain influence coefficients (see Appendix).

5.2 Static Meshing

Measured strain is plotted in Fig. 8 as a function of roll angle for static meshing of the gears (i.e., for multiple-tooth contact). This figure shows the average strain (mean of driving- and driven-gear values) for 37-, 88-, 100-, and 132-percent torque. Figure 9 shows in greater detail the tooth-fillet strains for
gages 1 to 4 at 100-percent torque, with
the instrumented gear acting as both driven
and driving gear. The curves of Fig. 9 are
the averaged result of three trials. From
the results of Fig. 9, and the influence
coefficient matrix previously described,
plots of normal and friction forces
(Fig. 10) have been derived from the static
data for the 100-percent-torque case.

The total normal force between the
one- or two-tooth pairs in mesh should be
equal to 1718 N (386 lbf). This value is
the torque divided by the base circle
radius. The normal-force component of the
plots shows agreement within 1.5 percent of
the expected value.

An absolute value for the friction
force cannot be determined during calibra-
tion since the coefficient of friction at
the tooth contact point is unknown. If an
arbitrary value of unity is assigned to the
maximum frictional force developed at
100-percent torque, then the friction value
should be either +1 or -1 (depending on the
direction of sliding) in the single-tooth
contact region. This ideal is nearly
achieved in the static measurements for
tooth 1 in Fig. 10(b). For tooth 2, the
friction force is offset by about -0.4 from
the +1 values. Outside the single-tooth
contact region, the friction force
decreases in approximately linear fashion
with the normal tooth load. This implies a
constant friction coefficient under these
static meshing conditions.

It is interesting to note the location
of the zero-crossing of the friction force
in Fig. 10 when tooth sliding changes di-
rection. This zero-crossing differs from
the pitch point by nearly 1° of roll. Some
of this difference may be due to deflection
of the gear shaft, which causes a shift in
the operating pitch point.

5.3 Dynamic Case

The dynamic tooth strains for the 28
speed-load conditions are shown in Fig. 11.
To allow direct comparison, the compressive
strain data are inverted (shown as posi-
tive) and overlayed on the tensile curves.
Notable features of these curves include
the peak tooth strain corresponding with
the high point of single-tooth contact
(which occurs at about 23° roll angle), a
dip or notch in the tensile tooth strain
curves near the pitch point (where the
sliding force reverses), and dynamic
effects becoming apparent at higher speeds.

The dynamic effect is particularly
notable in the curves for 4000 rpm at the
lowest torque (16 percent). Here, the
force vanishes, thereby indicating tooth
separation occurs. By contrast, at 110-
percent torque there is very little dynamic
effect, as evidenced by little difference
among the curves for the four speeds (800,
2000, 4000, and 6000 rpm).

In Fig. 12 the computed normal and
friction forces are shown for four speeds
at the highest torque (110 percent). Note
the very good agreement with expected
results at the low speed of 800 rpm
(Fig. 12(a)), where we would expect to
approach a static case. Here, the normal
force is very close to the static normal
value (a function of the torque divided by
the base circle radius). The friction
results show a marked transition in force
from negative to positive as the tooth con-
tact passes through the pitch point, where
there is pure rolling. Also the friction coefficient appears to be less than that of the static calibration case, as can be seen by comparing Fig. 10(a), where the friction force has a value of unity for a normal force of 386 lbf, and Fig. 12(a), where the friction force is a maximum of approximately 0.75.

5.4 Accuracy

The results obtained herein for the static and dynamic tests indicate the feasibility of using multiple gages to separate the tooth friction and normal forces. The results of the static case are particularly encouraging. The value for the normal force is generally within 1.5 percent of the expected value. The friction force, whilst at times much less accurate, nonetheless demonstrates the trends we expected to see — that is, the friction force is proportional to the normal load, and a reversal in sign occurs at about the pitch point. The good results for the static case are believed to be partly due to using instrumentation that was identical to that used for the static calibration (i.e., the Wheatstone bridge circuit). Assessing the accuracy for the dynamic case is more difficult, since we do not fully know what to expect. However, dynamic operation could introduce the following problems:

1. There could be some change in sensitivity due to the change in signal conditioners (i.e., constant current amplifiers operating through slip rings).
2. Resistance variations of the slip rings and other electrical noise can contaminate dynamic data. This was minimized here by the use of synchronous averaging, as described in the test procedure for dynamic data.
3. Other dynamic effects such as gear body vibration can also produce unwanted

![Figure 11.—Dynamic tooth strains at four speeds and seven torque levels. Compressive strains are shown as positive for comparison with tensile data.](image)
the summing of the strain magnitudes, as is the case for normal force (see Appendix). Various techniques can be used to minimize errors—synchronous averaging, as carried out here, and possibly, an adjustment (compensation) of the friction curve to bring about zero friction at the pitch point. The dc offset of the strain signal is critical. Figure 13 shows the superimposed curves of normal and friction forces for four successive revolutions of the gear, using nonaveraged data. Each curve is based on the corresponding tensile and compressive strains for that particular revolution. A significant variation in friction estimation is evident from one revolution to the next; this cannot be ascribed to the expected small torque fluctuations caused by the belt drive.

Differences in profile between the single-tooth calibration gear and the operating gear result in the tooth contact point being slightly displaced along the tooth profile, thereby causing an error in the measured roll angle. This error has been estimated to be of the same order (0.25°) as the error in setting the roll angle for calibration. The friction force results obtained herein were necessarily qualitative. A logical next step would be to calibrate the gages with a known friction force. A device similar to that of Benedict and Kelly [3] (Fig. 14) could be used for this purpose. In their application, dynamic effects prevented Benedict and Kelly from obtaining useful results from this device. If the device were used only for static calibration, this restriction would be removed. Alternatively, with only slight modification this setup could be used to apply a known force in the friction force direction while the tooth contact position was held constant.

Figure 13.—Computed dynamic load and friction superimposed for four successive revolutions at 4000 rpm and 110-percent torque.

Figure 12.—Computed dynamic load and friction at four speeds and 110-percent torque.

Figure 12.—Computed dynamic load and friction at four speeds and 110-percent torque.
6. SUMMARY OF RESULTS

Tooth-fillet strains were recorded for 28 operating conditions on the NASA gear-noise rig. A method was introduced that used the tensile and compressive tooth-fillet strains to transform these strain measurements into the normal and frictional loads on the tooth. This technique was applied to both the static and dynamic strain data. The results demonstrated that this technique was viable, and in particular they showed the following:

1. For the static case, the normal force closely agreed (within 1.5 percent) with expected results. The frictional results were much more variable, but they exhibited expected trends.

2. In the dynamic case, the estimation of normal force was good, the friction results, less so. However, the friction force results showed expected trends; that is, the dynamic friction coefficient was less than the static coefficient, and the friction reversed direction near the pitch point. Further refinement of measurement techniques will be required to produce more accurate results.

3. The influence of sliding friction was particularly marked on the tension tooth-fillet gage. The compression gage was affected by friction to a much lesser degree.

APPENDIX

TOOTH FORCE INFLUENCE COEFFICIENT MATRIX

The meshing cycle of a tooth on a low-contact-ratio spur gear may be divided into 3 cases: (1) the tooth load is shared with the preceding tooth; (2) the entire load is carried by the tooth; and (3) the load is shared with the following tooth. We have shown earlier that loading on the adjacent (preceeding or following) tooth will produce a small influence on a tooth-fillet strain gage. The normal and frictional components of force on a gear tooth may be computed from equation (4.4), expanded to a six-by-six matrix. To compute the forces on tooth 1, we must know the output of strain gages on the adjacent teeth (designated 0 and 2) due to loading on tooth 1. Although we did not measure the strain on tooth 0, we know that the strain due to loading on adjacent teeth is a small effect. And we assume that the unmeasured strain reading on tooth 0 due to loading on tooth 1 is identical to the strains measured under similar conditions on tooth 1 due to a load applied on tooth 2. Likewise, when we calculate forces on tooth 2, we make the assumption that unmeasured readings from tooth 3 due to loading on tooth 2 are identical to measured readings on tooth 2 due to loading on tooth 1. Equation (4.4) thus becomes

\[
\begin{vmatrix}
F_{0n} & F_{0f} & F_{1n} & F_{1f} & F_{2n} & F_{2f} \\
S_0 & S_0 & S_1 & S_1 & S_2 & S_2 \\
\end{vmatrix}
\]

where \(a_{ij}\) is a function of roll angle. Since there are only one or two teeth in contact at a time, there are only two or four nonzero rows and columns in equation (A1), so the matrix is effectively only of order two or four. Any \(a_{ij}\) corresponding to a tooth outside of the contact region is zero.

To illustrate the significance of the dominant terms in this matrix, for the purposes of this example only, cross-coupling terms are disregarded. The normal force \(F_{1n}\) simplifies to

\[
F_{1n} = a_{33}S_{1c} + a_{34}S_{1t} \quad (A2)
\]

where \(F_{1n}\) = normal force on tooth 1; \(S_{1c}\) = compressive strain on tooth 1; and \(S_{1t}\) = tensile strain on tooth 1.

The coefficients \(a_{33}\) and \(a_{34}\) are plotted in Fig. A1. It is notable that the tension gage has less influence on the computation of normal force than the compressive gage. Indeed, at a roll angle of 28° the coefficient \(a_{33}\) becomes zero; the tensile gage then has no effect on \(F_{1n}\).

Similarly, the friction force (see Fig. A2) is described (again disregarding cross-coupling terms) by

\[
F_{1f} = a_{43}S_{1c} + a_{44}S_{1t} \quad (A3)
\]

where \(F_{1f}\) = normal force on tooth 1.

'Cross-coupling terms will assume a much greater significance in the case of thin-rim gears where the strain at a tooth fillet is significantly affected by the loading on an adjacent tooth.
To aid in the interpretation of these coefficients, it is useful to plot the tooth strain versus roll angle, for the tension and compressive gages. This is given in Fig. A3; the data shown here were obtained from taking the average of the calibration curves in Fig. 6.

The influence coefficients for the friction force show why accuracy is important. Recall that tensile and compressive outputs are similar in magnitude but opposite in sign; therefore the resultant value of friction is a small (approximately 10 percent) difference obtained from the products $a_{33}S_{1c}$ and $a_{44}s_{1t}$ in equation (A3).

8. REFERENCES


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As part of a program to study fundamental mechanisms of gear noise, static and dynamic gear tooth strain measurements were made on the NASA gear-noise rig. Tooth-fillet strains from low-contact-ratio spur gears were recorded for 28 operating conditions. A method is introduced whereby strain gage measurements taken from both the tension and compression sides of a gear tooth can be transformed into the normal and frictional loads on the tooth. This technique was applied to both the static and dynamic strain data. The static case results showed close agreement with expected results. For the dynamic case, the normal-force computation produced very good results, but the friction results, although promising, were not as accurate. Tooth sliding friction strongly affected the signal from the strain gage on the tension side of the tooth. The compression gage was affected by friction to a much lesser degree. The potential of the method to measure friction force has been demonstrated, but further refinement will be required before this technique can be used to measure friction forces dynamically with an acceptable degree of accuracy.

Gears; Gearing; Dynamic load; Dynamic friction; Friction; Dynamics

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