The University of Alabama in Huntsville

Final Report

MICROGRAVITY LIQUID PROPELLANT MANAGEMENT

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Abstract

The requirement to settle or to position liquid fluid over the outlet end of a spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem. Resettlement or reorientation of liquid propellant can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion for the space fluid management under microgravity environment. The purpose of the present study is to investigate most efficient technique for propellant resettling through the minimization of propellant usage and weight penalties. Both full-scale and sub-scale liquid propellant tank of Space Transfer Vehicle have been used to simulate flow profiles for liquid hydrogen reorientation over the tank outlet. In sub-scale simulation, both constant and impulsive resettling acceleration have been used to simulate the liquid flow reorientation. Comparison between the constant reverse gravity acceleration and impulsive reverse gravity acceleration to be used for activation of propellant resettlement, it shows that impulsive reverse gravity thrust is superior to constant reverse gravity thrust for liquid reorientation in a reduced gravity environment.
(I) Statement of Problems

Behavior of liquid propellant becomes fairly uncertain when the gravity environment reduces to the order of $10^{-6}$ g$_0$ level. The requirement to settle or to position liquid fuel over the outlet end of the spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem. Retromaneuvers of spacecraft, such as Orbital Maneuvering Vehicle (OMV) and Space Transfer Vehicle (STV)\cite{11} taking a flight from high earth orbit to low earth orbit, require settling or reorientation of propellant prior to main engine firing. Cryogenic liquid propellant is required to position over the tank outlet by using small auxiliary thrusters which provide a thrust parallel to the tank's major axis in the direction of flight. During the reorientation process, the liquid flows in an annular sheet along the tank wall, with the gas or ullage bubble "rising" centrally into the liquid. This motion would also clear the tank vent of liquid so that venting of vapor is possible.

An efficient propellant settling technique should minimize propellant usage and weight penalties. This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion.

Time-dependent dynamical behaviors of fluids in a microgravity environment have been investigated by numerically computing full set of Navier-Stokes equation\cite{12-15}. 

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(II) Problems Attempted

Liquid propellant (hydrogen) tank is 168 inch in diameter, has a square root of 2 domes and a 48 inch long barrel section. Figure 1 shows the size and dimension of hydrogen tank. A settling acceleration, ranging from $1.5 \times 10^{-3}$ to $3.0 \times 10^{-3} \text{g}_0$, has been assumed to be produced by idle-mode thrust from the main engine. Settling of propellant prior to main engine start is defined to be required at two tanks with fill percentages of 30% and 70%.

To provide conservative settling conditions, the liquid is assumed to be initially oriented at the top of the tank. If the spacecraft has been coasting for a long time, aligned with its direction of motion, the most significant force, drag would be axial.

Axisymmetric representation of the tank, with a cylindrical coordinate system is assumed. The settling acceleration is assumed to be parallel to by the axial direction, and the liquid is initially oriented symmetrically at the top of the tank.

Numerical simulations have been carried out for both full-scale and sub-scale of liquid hydrogen propellant tanks for the Space Transfer Vehicle (STV).

(III) Full-Scale Simulation for Liquid Reorientation and Resettlement

The following four cases have been accomplished for the cases of full-scale STV propellant tank liquid fluid reorientation: (A) Liquid filled level of 30% and settling acceleration of $1.5 \times 10^{-3} \text{g}_0$; (B) Liquid filled level of 30% and settling acceleration of $3.0 \times 10^{-3} \text{g}_0$; (C) Liquid filled level of 70% and settling acceleration of $1.5 \times 10^{-3} \text{g}_0$. (D)
Liquid Hydrogen and Vapor

Figure 1 Size and Diameter of Space Transfer Vehicle
10^{-3} \, g_0; \text{ and (D) Liquid filled level of 70\% and settling acceleration of } 3.0 \times 10^{-3} \, g_0.

Figures 2 to 11 show the time evolution of liquid hydrogen reorientation for liquid filled level of 30\% and settling acceleration of 1.5 \times 10^{-3} \, g_0. \text{ Figure 12 to 21 illustrate the time evolution of liquid hydrogen reorientation for liquid filled level of 30\% and resettling acceleration of } 3.0 \times 10^{-3} \, g_0. \text{ Figure 22 to 31 show the time evolution of liquid hydrogen reorientation of liquid hydrogen for liquid filled level of 70\% and resettling acceleration of } 1.5 \times 10^{-3} \, g_0. \text{ Figure 32 to 41 illustrate the time evolution of liquid hydrogen for liquid filled level of 70\% and resettling of } 3.0 \times 10^{-3} \, g_0.$
(A) Full-Scale Simulation

Liquid Filled: 30%

Settling Acceleration: $1.5 \times 10^{-2} \text{ g}_0$
Liquid Hydrogen and Vapor

Liquid Filled = 30\% \quad t = 0.00 \text{s}

\( g = -1.50 \times 10^{-3} \text{g} \)

Figure 2
Liquid Hydrogen and Vapor
liquid filled=30%  t= 2.81×10^1s
g=−1.50×10^3\,g_s
Liquid Hydrogen and Vapor

Liquid Filled = 30%, t = 5.61 x 10^5 s

g = -1.50 x 10^-3 g
Liquid Hydrogen and Vapor
Liquid Filled=30% \text{ t}=8.82 \times 10^1 \text{s}
g=-1.50 \times 10^{-3} \text{g}

Figure 5
Liquid Hydrogen and Vapor
Liquid Filled=30%  t = 1.20x10^2 s
g = -1.50x10^{-3} g
Liquid Hydrogen and Vapor

Liquid Filled = 30%  \( t = 1.24 \times 10^2 \) s
\( g = -1.50 \times 10^{-3} \) g.
Liquid Hydrogen and Vapor
Liquid Filled = 30%  \( t = 1.28 \times 10^2 \text{s} \)
g = \(-1.50 \times 10^{-3} \text{g} \)
Liquid Hydrogen and Vapor

Liquid Filled = 30%  \( t = 1.36 \times 10^2 \) s
\( g = -1.50 \times 10^{-3} \) g
\( f = 0.00 \) Hz

Figure 9
Liquid Hydrogen and Vapor

Liquid filled = 30%  \( t = 1.52 \times 10^2 \text{s} \)

\( g = -1.50 \times 10^{-3} \text{g} \)
Liquid Hydrogen and Vapor

Liquid Filled=30%  t= 1.80×10^2 s  
g=−1.50×10^3 g
(B) Full-Scale Simulation

Liquid Filled: 30%

Settling Acceleration: $3.0 \times 10^{-3} \, g_o$
Liquid Hydrogen and Vapor
Liquid Filled = 30%  \( t = 0.00 \text{s} \)
g = \(-3.00 \times 10^{-3} \text{g}_0\)
Liquid Hydrogen and Vapor

Liquid Filled = 30% \quad t = 2.88 \times 10^5 \text{s}

g = -3.00 \times 10^{-3} \text{g}
Liquid Hydrogen and Vapor

Liquid Filled=30%, t = 5.77 x 10^3 s

g = -3.00 x 10^-3 g₀

Figure 14

HEIGHT (CM)

RADIUS (CM)
Liquid Hydrogen and Vapor

Liquid Filled = 30%  \( t = 6.59 \times 10^1 \text{s} \)
\( g = -3.00 \times 10^{-3} \text{g}_0 \)

Figure 15
Liquid Hydrogen and Vapor

Liquid Filled = 30% \[ t = 8.24 \times 10^3 \text{s} \]
\[ g = -3.00 \times 10^{-3} \text{g}_0 \]

Figure 16
Liquid Hydrogen and Vapor

Liquid Filled=30%  \( t = 8.57 \times 10^1 \)s
\( g = -3.00 \times 10^{-3} \)g.
Liquid Hydrogen and Vapor

Liquid Filled = 30%  \( t = 9.39 \times 10^1 \text{s} \)
\( g = -3.00 \times 10^{-3} \text{g} \)

Figure 18
Liquid Hydrogen and Vapor

Liquid Filled = 30% \( t = 9.72 \times 10^1 \) s
\( g = -3.00 \times 10^{-3} \) g.
Liquid Hydrogen and Vapor

Liquid Filled = 30%  \( t = 1.17 \times 10^2 \) s
\( g = -3.00 \times 10^{-3} \) g

Figure 20
Liquid Hydrogen and Vapor

Liquid Filled = 30%  \( t = 1.33 \times 10^2 \text{s} \)

\( g = -3.00 \times 10^{-3} g_0 \)
(C) Full-Scale Simulation

Liquid Filled: 70%

Settling Acceleration: $1.5 \times 10^{-3} \, g_0$
Liquid Hydrogen and Vapor
Liquid Filled=70%  t = 0.00s
\(g = -1.50 \times 10^{-3} g_0\)
Liquid Hydrogen and Vapor
Liquid filled = 70%  \[ t = 2.20 \times 10^1 \text{s} \]
\[ g = -1.50 \times 10^{-3} \text{g}_0 \]
\[ f = 0.00 \text{Hz} \]

![Figure 23]
Liquid Hydrogen and Vapor
Liquid Filled = 70%  \( t = 6.60 \times 10^4 \text{s} \)
\( g = -1.50 \times 10^{-3} \text{g} \)
Liquid Hydrogen and Vapor

Liquid Filled = 70%  \( t = 8.71 \times 10^1 \) s
\( g = -1.50 \times 10^{-3} \) \( g_0 \)
Liquid Hydrogen and Vapor

Liquid Filled = 70%  \[ t = 1.01 \times 10^2 \text{s} \]
\[ g = -1.50 \times 10^{-3} g \]
Liquid Hydrogen and Vapor
Liquid filled=70\% \ t = 1.06 \times 10^2 s
\ g = -1.50 \times 10^{-3} g_0
Liquid Hydrogen and Vapor

Liquid Filled=70%  \( t = 1.14 \times 10^2 \text{s} \)
\( g = -1.50 \times 10^{-3} \text{g} \)

Figure 28
Liquid Hydrogen and Vapor

Liquid filled = 70% \text{, } t = 1.72 \times 10^2 \text{s}

g = 1.50 \times 10^3 \text{ g}
Liquid Hydrogen and Vapor

Liquid Filled = 70%  \( t = 1.98 \times 10^2 \text{s} \)
\( g = -1.50 \times 10^{-3} \text{g} \)
Liquid Hydrogen and Vapor

Liquid Filled = 70%, t = 2.20 x 10^4 s,
\[ g = 1.50 \times 10^{-3} \, g, \]
\[ f = 0.0012 \, Hz. \]

\[ V_{max} = 7.73 \times 10^{-1} \, \text{cm/sec} \]

Figure 31

Height (CM)
(D) Full-Scale Simulation

Liquid Filled: 70%

Settling Acceleration: $3.0 \times 10^{-3} \, g_0$
Liquid Hydrogen and Vapor

Liquid Filled-70%  \( t = 0.00 \text{s} \)
\( g = -3.00 \times 10^{-3} \text{g} \)

Figure 32
Liquid Hydrogen and Vapor

Liquid Filled=70%  \( t = 1.40 \times 10^1 \text{s} \)
\( g = -3.00 \times 10^{-3} \text{g} \)
Liquid Hydrogen and Vapor

Liquid filled = 70%  t = 3.74 × 10^4 s

\( g = -3.00 \times 10^{-3} \, g \)
Liquid Hydrogen and Vapor

Liquid Filled = 70%  t = 4.21 \times 10^1 \text{s}

g = -3.00 \times 10^{-3} \text{g}_0
Liquid Hydrogen and Vapor

Liquid filled = 70%  \( t = 5.14 \times 10^4 \) s

\( g = -3.00 \times 10^{-3} \) g
Liquid Hydrogen and Vapor

Liquid Filled = 70%  t = 8.39 \times 10^4 s

g = -3.00 \times 10^{-3} g_o

![Diagram of liquid and vapor distribution](image)
Liquid Hydrogen and Vapor
Liquid Filled=70%  t=8.86\times10^4\text{s}
g=-3.00\times10^{-3}\text{g}
Liquid Hydrogen and Vapor

Liquid Filled=70%  \( t = 1.45 \times 10^2 \) s
\( g = -3.00 \times 10^{-3} \) g
Liquid Hydrogen and Vapor
Liquid Filled=70\% \ t=1.73\times10^2 s
\ g=-3.00\times10^{-3} \ g_0

Figure 40
Liquid Hydrogen and Vapor
Liquid Filled=70%  \( t = 1.87 \times 10^2 \text{s} \)
\( g = -3.00 \times 10^{-3} \text{g} \)

\( V_{\text{max}} = 9.90 \times 10^{-1} \text{cm/sec} \)
(IV) Sub-Scale Simulation for Liquid Reorientation and Resettlement

In the sub-scale STV propellant tank liquid hydrogen reorientation we have accomplished the following four cases of numerical simulation: (E) Cryogenic liquid hydrogen reorientation activated by constant settling acceleration of geyser initiation; (F) Cryogenic liquid hydrogen reorientation activated by low frequency impulsive settling acceleration of geyser initiation; (G) Cryogenic liquid hydrogen reorientation activated by medium frequency impulsive settling acceleration of geyser initiation; and (H) Cryogenic liquid hydrogen reorientation activated by high frequency impulsive settling acceleration of geyser initiation.
(E) Cryogenic Liquid Hydrogen Reorientation
Activated by Constant Settling Acceleration
of Geyser Initiation
Abstract

A key objective of the cryogenic fluid management of the spacecraft propulsion system is to develop the technology necessary for acquisition or positioning of liquid outflow or vapor venting. In this paper, numerical simulation of positive liquid acquisition is attempted by introducing reverse gravity acceleration, resulting from the propulsive thrust of auxiliary engines, which exceeds critical value for the initiation of geyser. Based on the computer simulation of flow fields during the course of fluid reorientation, six dimensionless parameters resulted in this study. It shows that these parameters hold near constant values through the entire ranges of liquid filled levels, from 30% to 80%, during the course of fluid reorientation.
Nomenclature

\( a_g \) = geyser initiation acceleration (cm/s\(^2\))

\( a_m \) = scale flow acceleration associated with maximum velocity (cm/s\(^2\)), defined by Eq (5)

\( D \) = diameter of propellant tank (cm)

\( f \) = frequency of impulsive thrust (Hz)

\( g_i \) = geyser initiation gravity-level (\( g_0 \))

\( g_0 \) = normal Earth gravitational acceleration = 9.81 m/s\(^2\)

\( \bar{h} \) = average liquid height (cm)

\( h_m \) = maximum liquid height (cm)

\( L \) = height of propellant tank (cm)

\( L_m \) = scale length of maximum liquid height (cm/s), defined by Eq (4)

STV = Space Transfer Vehicle

\( \bar{t}_f \) = average free fall time (s)

\( t_m \) = time for observing maximum flow velocity (s)

\( t_R \) = liquid reaching tank bottom time (s)

\( V_{fm} \) = free fall velocity from maximum liquid height (cm/s), defined by Eq (3)

\( \bar{V}_f \) = average free fall velocity (cm/s), defined by Eq (2)

\( V_m \) = maximum flow velocity (cm/s)
I. Introduction

In spacecraft design, the requirements for a settled propellant are different for tank pressurization, engine restart, venting, or propellant transfer. Prepressurization requires that heat and mass transfer effects be minimized; otherwise, a process of chill down of tank, venting of noncondensing gases, etc., may have to carry out for the cryogenic system. For engine restart, it is necessary to have the liquid settle with no bubbles near the tank outlet so that the initial flow of propellant will not carry vapor to the pump or engine. The slosh wave amplitude should be relatively low to keep the center of mass shifts within an acceptable range and wave motion low enough to avoid pressure collapse caused by interface agitation.

Bubble and globule formation as a result of liquid impact with the aft end of the tank could lead to propellant loss for the spacecraft during venting. Globules could be entrained in the vented ullage gas or bubbles rising through the liquid and expanding because of the decreasing tank pressure could cause a spray of globules to be vented. Liquid level rise, vent liquid loss, fluid freezing, and vehicle dynamics are all affected by the microgravity levels.

A key objective of the cryogenic fluid management of spacecraft propulsion system, such as a Space Transfer Vehicle\(^1\) (STV), is to develop the technology necessary for acquisition or positioning of liquid and vapor within a tank in reduced gravity to enable liquid outflow or vapor venting. Liquid acquisition techniques can be divided into two general categories: (1) Active liquid acquisition by the creation of a positive acceleration environment resulting from
the propulsive thrust of small auxiliary engines, and (2) Passive liquid acquisition utilizing the liquid capillary forces provided by using solid baffles of liquid traps made of fine mesh screen material. In this study, active liquid acquisition is aimed for numerically simulating the resettlement of cryogenic liquid hydrogen. Liquid hydrogen, which, in general, poses more severe technical challenges than liquid oxygen, is used as the test bed working fluid in this study.

Recently Leslie\textsuperscript{2} was able to measure and to numerically compute the bubble shapes at various ratios of centrifugal force to surface tension force in the microgravity environment. Hung and Leslie\textsuperscript{3} extended Leslie's work\textsuperscript{2} to rotating free surfaces influenced by gravity with higher rotating speeds when the bubble intersects with both the top and bottom walls of the cylinder. Hung et al.\textsuperscript{4,5} further extended the work to include rotating speeds which resulted with bubbles intersecting and/or without intersecting the top, bottom and side walls of the cylinder.

An analysis of time-dependent dynamical behavior of surface tension on partially-filled rotating fluids in both low gravity and microgravity environments was carried out by numerically solving the Navier-Stokes equations subjected to the initial and the boundary conditions\textsuperscript{4,6}. The initial condition for the bubble profiles was adopted from steady-state formulations developed by Hung and Leslie\textsuperscript{3}, and Hung et al.\textsuperscript{6} for rotating cylinder tank; and by Hung et al.\textsuperscript{5,7} for the dewar-shaped container to be used in the Gravity Probe-B Spacecraft\textsuperscript{8}. Some of the steady-state formulations of bubble
shapes, in particular for bubbles intersecting at the top wall of the cylinder, were compared with the experiment carried out by Leslie in a free-falling aircraft (KC-135) with an excellent agreement.

An efficient propellant settling technique should minimize propellant usage and weight penalties. This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion.

Production of geyser during the propellant reorientation is not a desirable motion for the space fluid management. It is because geyser is always accompanied by the vapor entrainment and globule formation. Geyser is observed at reverse gravity acceleration greater than certain critical values of acceleration during the course of liquid reorientation. In other words, geyser will not be observed at very low reverse gravity level, and it will be detected when the reverse gravity level is greater than the certain critical level. In this paper, numerical simulation of positive liquid acquisition is attempted by introducing reverse gravity acceleration, resulting from the propulsive thrust of small auxiliary engines which exceeds the critical value for geyser initiation. The reverse gravity acceleration is starting with a small value and increases gradually till the initiation of geyser is detected in the computer simulation for the liquid reorientation of propellant tank with various liquid-filled levels.

In this study, time-dependent computations have been carried out
to investigate the dynamical behavior of fluid reorientation or resettling of propellant prior to main engine firing for spacecraft restart at the net reverse gravity acceleration which is great enough to initiate geyser during the liquid reorientation. The computation extends to the study of the characteristics of fluid resettlement due to the reversal of lowest artificial gravity fields which is great enough to initiate geyser with and without various frequencies of impulsive acceleration. This frequency of impulsive acceleration is generally termed "gravity jitters". Gravity jitters are produced by spacecraft attitude motion, machinery (turbine, pump, engine) vibrations, thruster firing, thruster shutdown, etc. Positioning of liquid propellant over the tank outlet can be carried out by using small auxiliary thrusters which provide a thrust parallel to the tank's major axis in the direction of flight.

II. Numerical Simulation of Liquid Hydrogen Reorientation at the Reverse Gravity Acceleration of Geyser Initiation

Propellant tank of liquid-filled levels of 30, 50, 65, 70 and 80% are considered in this study. Time-dependent axial symmetry mathematical formulation are adopted. Detailed description of mathematical formulation, initial and boundary conditions suitable for the analysis of cryogenic fluid management under microgravity environment are given in our earlier studies. The initial profiles of liquid-vapor interface are determined from computations based on algorithms developed for the steady state formulation of microgravity fluid management.

A staggered grid for the velocity components is used in this
computer program. The method was first developed by Harlow and Welch\textsuperscript{13} for their MAC (marker and cell) method of studying fluid flows along free surface. The finite difference method employed in this numerical study was the "Hybrid Scheme" developed by Spalding.\textsuperscript{14} The formulation for this method is valid for any arbitrary interface location between the grid points is not limited to middle point interfaces.\textsuperscript{15} An algorithm for semi-implicit method\textsuperscript{16} was used as the procedure for modeling the flow field. The time step is determined automatically based on the size of the grid points and the velocity of flow fields. Detailed description of the computational algorithm applicable to microgravity fluid management are illustrated in our earlier studies.\textsuperscript{4,6,10-12} Fig 1(A) shows the distribution of grid points in the radial-axial plane of cylindrical coordinates.

For the purpose of facilitating easy comparison between computational results and experimental measurement, a model of 0.01 size prototype is adopted in the computer simulation. Fig 1(B) shows a model size for computation. The size of prototype is height, $L = 166.8$" (423.672 cm), and diameter, $D = 168$" (426.72 cm). Model size is $L = 4.23672$ cm and $D = 4.2672$ cm, as shown in Fig 1(B). If the spacecraft had been coasting for a long time, aligned with its direction of motion, the most significant force, drag, would be axial and with acceleration of $10^{-4}g_0$ along upward direction. The hydrogen vapor is, thus, originally positioned at the bottom of the tank. The requirement to settle or to position liquid fuel over the outlet end of the spacecraft propellant tank prior to main engine restart poses a
microgravity fluid behavior problem. Retromaneuvers of spacecraft, such as STV, require settling or reorientation of the propellant to main engine firing. Cryogenic liquid propellant shall be positioned over the tank outlet by using auxiliary thrusters (or idle-mode thrusters from the main engine) which provide a thrust parallel to the tank's major axis in the direction of flight. In the present study of computer simulation, a small value of reverse gravity acceleration (downward direction) is provided by the propulsive thrust of small auxiliary engine to initiate the reorientation of liquid propellant. This small value of reverse gravity acceleration of propulsive thrust increases gradually till reaching the critical value on which initiation of geyser is detected during the time period of fluid resettlement. We term this reverse gravity acceleration of propulsive thrust, which is capable to initiate geyser, as "geyser initiation gravity-level". This geyser initiation gravity level has been investigated through the method of trial and error for the various liquid-filled levels of propellant tank as a base to simulate following cases of reduced gravity fluid behaviors during the reorientation: (A) constant reverse gravity acceleration, (B) impulsive reverse gravity acceleration with a frequency of 0.1 Hz, (C) impulsive reverse gravity acceleration with a frequency of 1.0 Hz, and (D) impulsive reverse gravity acceleration with a frequency of 10 Hz. Cases (B) to (D) for the impulsive reverse gravity acceleration with various frequencies will be discussed in the subsequent papers. Liquid filled level of 30, 50, 65, 70 and 80% have been considered in this study. Cryogenic liquid hydrogen at temperature of 20K is
considered. Hydrogen density of 0.071 g/cm³; surface tension coefficient at the interface between liquid hydrogen and hydrogen vapor of 1.9 dyne/cm; hydrogen viscosity coefficient of 1.873 \times 10^{-3} cm²/s; and contact angle of 0.5⁰ are used in the computer simulation.

Reorientation of cryogenic liquid hydrogen activated by geyser initiation reverse gravity acceleration produced by propulsive thrust has been investigated for various liquid filled levels of propellant tank. It is found that these geyser initiation gravity levels are 5.5 \times 10^{-2}, 6.52 \times 10^{-2}, 6.6 \times 10^{-2}, 6.7 \times 10^{-2} and 8.2 \times 10^{-2}g₀ for liquid filled levels of 30, 50, 65, 70, and 80%, respectively. To illustrate some examples Figs 2 and 3 show the selected sequences of time evolution of fluid reorientation for cryogenic hydrogen with liquid filled levels of 30, and 80%, respectively. Each figure contains four sub-figures. Subfigure (A) is initial profile of liquid-vapor interface at the moment of the starting of fluid reorientation at time t = 0; subfigure (B), the flow profile during the course of fluid reorientation before the initiation of geysering motion; subfigure (C), the flow profile with geysering motion; and subfigure (D), the flow profile after the ending of geysering motion.

Figs 2 and 3 illustrate following flow behaviors: (1) The liquid starts to flow in an annular sheet along the solid wall of tank and gradually pushes the vapor toward the central portion of the lower dome of tank as the net acceleration, reversing the direction of gravity field, which is applied toward the downward direction of tank’s major axis, by using small auxiliary thrusters; (2) As the
downward fluid annular sheet along the tank wall reaches the central bottom dome side of the tank, a geysering flow is observed; and (3) The vapor is thus pushed upward centrally into the liquid and the geysering disappears.

Table 1 shows the characteristics of cryogenic liquid hydrogen resettlement activated by reverse gravity acceleration at geyser initiation gravity level. Average liquid height $\bar{h}$, and maximum liquid height $h_m$ are shown in Fig 1(B). Average free fall velocity $\bar{V}_f$, average free fall time $\bar{t}_f$, and free fall velocity from maximum liquid height $V_{fm}$ are computed from the following equations:

$$\bar{V}_f = (2g_i\bar{h})^{1/2}$$  \hspace{1cm} (1)

$$\bar{t}_f = \left(\frac{2\bar{h}}{g_i}\right)^{1/2}$$  \hspace{1cm} (2)

$$V_{fm} = (2g_i h_m)^{1/2}$$  \hspace{1cm} (3)

where $g_i$ denotes geyser initiation reverse gravity acceleration. Values of maximum flow velocity $V_m$, time for observing maximum flow velocity $t_m$, and time for reorienting liquid flowing down and reaching the bottom of propellant tank $t_r$, are obtained from the numerical computation of flow field. Scale length of maximum flow velocity $L_m$, and scale flow acceleration associated with maximum velocity $a_m$, are computed from the following parameters:

$$L_m = V_m t_m$$  \hspace{1cm} (4)
Following dimensionless parameters are introduced: $\frac{V_m}{V_f}$, $\frac{t_m}{t_f}$, $\frac{a_m}{a_g}$, $\frac{L_m}{h}$ and $\frac{V_m}{V_f m}$ where $a_g$ stands geyser initiation acceleration (cm/s$^2$) for corresponding geyser initiation gravity level $g_i$.

Figs 4 to 6 show the variations of dimensionless parameters in terms of liquid filled levels. Denominators of these six dimensionless parameters are either predetermined from the geometry of liquid fill levels or can be deduced from the corresponding calculations associated with the geyser initiation gravity levels. Characteristics of these near constant values dimensionless parameters can provide a good understanding of the physics of microgravity fluid behaviors, in particular the active category of liquid acquisition or positioning, and also the design criteria of on-orbit spacecraft propulsion system at the critical value of reverse gravity acceleration of propulsive thrust which is capable to initiate geyser.

Fig 4(A) shows the ratio of maximum flow velocity to average free fall flow velocity $\frac{V_m}{\bar{V}_f}$ and its associated parameters of $V_m$ and $\bar{V}_f$ in terms of liquid filled levels. It shows that the ratio of $V_m/\bar{V}_f$ varies in the range of 4.3 to 4.9 in the entire liquid filled levels while $V_m$ and $\bar{V}_f$ vary from 62.0 to 73.6 cm/s (decreasing with increasing liquid filled levels) and from 12.5 to 17.0 cm/s (also decreasing with increasing liquid filled levels), respectively. As $\bar{V}_f$ can be predetermined from geyser initiation gravity level and average liquid
height, shown in Eq (1), one can make an approximate prediction of maximum flow velocity during the liquid reorientation for the various liquid filled levels.

Fig 4(B) shows the ratio of liquid reaching bottom time to average free fall time $t_R/\bar{t}_f$ and its associated parameters of $t_R$ and $\bar{t}_f$ in terms of liquid filled levels. It shows that the ratio of $t_R/\bar{t}_f$ varies in the range of 1.21 to 1.30 in the entire liquid filled levels while $t_R$ and $\bar{t}_f$ vary from 0.20 to 0.40 s (decreasing with increasing liquid filled levels) and from 0.15 to 0.32 s (also decreasing with increasing liquid filled levels), respectively. As $\bar{t}_f$ can be predetermined from geyser initiation gravity level and average liquid height, shown in Eq (2), one can predict the time reorienting liquid fluid flowing down from the original position and reaching the bottom of propellant tank for the various liquid filled levels at the reverse gravity acceleration capable for the initiation of geyser.

Fig 5(A) shows the ratio of time for observing maximum flow velocity to average free fall time $t_m/\bar{t}_f$ and its associated parameters of $t_m$ and $\bar{t}_f$ in terms of liquid filled levels. It shows that the ratio of $t_m/\bar{t}_f$ varies in the range of 1.2 to 1.3 in the entire liquid filled levels while $t_m$ and $\bar{t}_f$ vary from 0.20 to 0.42 s (decreasing with increasing liquid filled levels) and from 0.15 to 0.32 s (also decreasing with increasing liquid filled levels), respectively. As we indicated in 4, $\bar{t}_f$ can be predetermined, one can predict the time for observing maximum flow velocity for various liquid filled levels at the reverse gravity acceleration capable for the initiation of geyser.
Fig 5(B) shows the ratio of scale flow acceleration associated with maximum velocity to geyser initiation acceleration for corresponding geyser initiation gravity level $a_m/a_g$ and its associated parameters of $a_m$ and $a_g$ in terms of liquid filled levels. It shows that the ratio of $a_m/a_g$ varies in the range of 3.3 to 3.9 in the entire liquid filled levels while $a_m$ and $a_g$ vary from 175 to 310 cm/s$^2$ (increasing with increasing liquid filled levels) and from 53.9 to 80.4 cm/s$^2$ (also increasing with increasing liquid filled levels), respectively. As $a_g$ can be predetermined from geyser initiation gravity level, one can make an approximate prediction of scale flow acceleration associated with maximum velocity, which is defined in Eq (5), at the reverse gravity acceleration capable for the initiation of geyser.

Fig 6(A) shows the ratio of scale length of maximum flow velocity to average liquid height $L_m/h$ and its associated parameters of $L_m$ and $h$ in terms of liquid filled levels. It shows that the ratio of $L_m/h$ varies in the range of 11.6 to 13.0 in the entire liquid filled levels while $L_m$ and $h$ vary from 12.4 to 30.9 cm (decreasing with increasing liquid filled levels) and from 0.93 to 2.67 cm (also decreasing with increasing liquid filled levels), respectively. As $h$ can be predetermined from the geometry of liquid filled levels, one can make an approximate prediction of scale length of maximum flow velocity, which is defined in Eq (4), at the reverse gravity acceleration capable for the initiation of geyser.

Fig 6(B) shows the ratio of maximum flow velocity to free fall velocity from maximum liquid height $V_m/V_{f_m}$ and its associated
parameters of $V_m$ and $V_{fm}$ in terms of liquid filled levels. It shows that the ratio of $V_m/V_{fm}$ varies in the range of 3.8 to 4.0 in the entire liquid filled levels while $V_m$ and $V_{fm}$ vary from 62.0 to 73.6 cm/s (decreasing with increasing liquid filled levels) and from 16.4 to 19.2 cm/s (also decreasing with increasing liquid filled levels), respectively. As $V_{fm}$ can be predetermined from geyser initiation gravity level and maximum liquid height, shown in Eq (3), one can make an approximate prediction of maximum flow velocity at the reverse gravity acceleration capable for the initiation of geyser.

Six dimensionless parameters presented in this study show that the parameters hold near constant values through the entire ranges of liquid filled levels during the course of reorientation of liquid hydrogen activated by the reverse gravity acceleration which is great enough to initiate geysering flow. As the denominators of these six dimensionless parameters are either predetermined from the geometry of liquid filled levels or can be deduced from the corresponding calculations associated with the geyser initiation gravity levels, one can predict the flow parameters from these relations.

III. Discussion and Conclusions

The efficient management of subcritical cryogenic propellants is one of the key technology drivers for the on-orbit spacecraft. Cryogenic liquids are essential for the spacecraft as reactants, coolants, and propellants. The requirement to settle or to position liquid fuel over the outlet end of the spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem. Retromaneuvers of spacecraft require settling or
reorientation of the propellant prior to main engine firing. Cryogenic liquid propellant is positioned over the tank outlet by using small auxiliary thrusters (or idle-mode thrusters from the main engine) which provide a thrust parallel to the tank’s major axis in the direction of flight.

The results of the study of fluid reorientation have to be evaluated in terms of how well they can be managed efficiently. An efficient propellant settling technique should minimize propellant usage and weight penalties through the operation of small thrusters (or idle-mode thrusters from the main engine). This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion.

Production of geyser during the propellant reorientation is not a desirable motion for the space fluid management under microgravity environment. In this paper, numerical simulation of positive liquid acquisition is attempted by introducing reverse gravity acceleration, resulting from the propulsive thrust of auxiliary engines, which exceeds critical value for the initiation of geyser.

Flow profile simulations, in particular the time evolution of liquid-vapor interface during the course of fluid reorientation, for the selected various liquid filled levels are shown in Figs 2 and 3. Table 1 and Figs 4 to 6 show the characteristics of dimensionless flow parameters and their associated flow fields during the course of fluid reorientation with geyser initiation. Computer simulation of flow
fields disclose the following results: (1) Geyser initiation gravity level is high (low) for high (low) liquid filled level; (2) Average liquid height is high (low) for low (high) liquid filled level; (3) Average free fall flow velocity is high (low) for low (high) liquid filled level; (4) Maximum flow velocity is high (low) for low (high) liquid filled level; (5) Average free fall time is longer (shorter) for low (high) liquid filled level; (6) Time for liquid falling from original position to liquid reaching bottom time is longer (shorter) for low (high) liquid filled level; (7) Time for observing maximum flow velocity is longer (shorter) for low (high) liquid filled level; (8) Scale length of maximum flow velocity is longer (shorter) for low (high) liquid filled level; (9) Scale flow acceleration associated with maximum velocity is low (high) for low (high) liquid filled level; (10) Maximum liquid height is high (low) for low (high) liquid filled level; and (11) Free fall velocity from maximum liquid height is high (low) for low (high) liquid filled level.

Based on the computer simulation of flow fields during the course of fluid reorientation, six dimensionless parameters are presented in this study. It is shown, in Figs 4 to 6, that these parameters hold near constant values through the entire ranges of liquid filled levels during the course of fluid reorientation activated by the reverse gravity acceleration great enough to initiate geyser. As the denominators of these dimensionless parameters are either predetermined from the geometry of liquid filled levels or can be deduced from the corresponding calculations associated with the
geyser initiation gravity levels, one can predict the values of these flow parameters from the relationship shown in Eqs (1) to (5).

Any fluid capable of motion relative to the spacecraft will be subject to an acceleration relative to the mass center of the spacecraft that arises from the gravity gradient of the Earth\textsuperscript{17,18}. In addition to the Earth's gravitational force, the interaction between the particle mass of fluids and the spacecraft mass due to gravity gradient accelerations\textsuperscript{17} have also been taken into consideration in this microgravity fluid management study.

To conclude, we have demonstrated that, the computer algorithm presented, can be used to simulate fluid behavior in a microgravity environment, in particular the development of technology necessary for acquisition or positioning of liquid and vapor within a tank to enable liquid outflow or vapor venting through active liquid acquisition by the creation of a positive acceleration environment resulting from propulsive thrust. Better understanding of the full pictures of flow fields during the course of fluid reorientation can provide the proper design techniques for handling and managing the cryogenic liquid propellants to be used in on-orbit spacecraft propulsion.

**Acknowledgement**

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Reference


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<th>Liquid Filled Level (%)</th>
<th>30</th>
<th>50</th>
<th>65</th>
<th>70</th>
<th>80</th>
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<td>Geyser Initiation Gravity-Level, ( g_1 ) (10(^{-2}) ( g_0 ))</td>
<td>5.5</td>
<td>6.52</td>
<td>6.6</td>
<td>6.7</td>
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<td>53.9</td>
<td>63.9</td>
<td>64.7</td>
<td>65.7</td>
<td>80.4</td>
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<td>Average Liquid Height, ( \bar{h} ) (cm)</td>
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<td>1.35</td>
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<td>17.0</td>
<td>16.2</td>
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<td>72.6</td>
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<td>62.0</td>
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<td>( V_m/V_f )</td>
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<td>4.5</td>
<td>4.8</td>
<td>4.9</td>
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<td>Average Free Fall Time, ( t_f ) (s)</td>
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<td>( t_R/t_f )</td>
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<td>1.21</td>
<td>1.25</td>
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<td>30</td>
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<td>Time for Observing Maximum Flow Velocity, ( t_m ) (s)</td>
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<td>Scale Length of Maximum Flow Velocity, ( L_m ) (cm) ( (= V_m t_m ) )</td>
<td>30.9</td>
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<td>19.2</td>
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<td>( L_m / H )</td>
<td>11.6</td>
<td>11.6</td>
<td>12.4</td>
<td>12.3</td>
<td>13.0</td>
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<td>( t_m / t_f )</td>
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<td>1.2</td>
<td>1.3</td>
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<td>1.3</td>
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<td>175</td>
<td>232</td>
<td>244</td>
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<td>( a_m / a_g )</td>
<td>3.3</td>
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<td>Maximum Liquid Height, ( h_m ) (cm)</td>
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<td>Free Fall Velocity from Maximum Liquid Height ( V_{fm} ) (cm/s)</td>
<td>19.2</td>
<td>18.9</td>
<td>17.1</td>
<td>16.6</td>
<td>16.4</td>
</tr>
<tr>
<td>( V_m / V_{fm} )</td>
<td>3.9</td>
<td>3.8</td>
<td>4.0</td>
<td>3.9</td>
<td>3.8</td>
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Figure Captions

Fig 1. (A) Distribution of grid points in the radial-axial plane of cylindrical coordinate for propellant tank, and (B) Model size propellant tank adopted for numerical simulation with geometrical description.

Fig 2. Selected sequences of time evolution of fluid reorientation with liquid filled level of 30%, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Fig 3. Selected sequences of time evolution of fluid reorientation with liquid filled levels of 80%, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Fig 4. (A) Ratio of $\frac{V_m}{\bar{V}_f}$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $\frac{t_r}{\bar{t}_f}$ and its associated parameters in terms of liquid filled levels.

Fig 5. (A) Ratio of $\frac{t_m}{\bar{t}_f}$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $\frac{a_m}{a_g}$ and its associated parameters in terms of liquid filled levels.

Fig 6. (A) Ratio of $\frac{L_m}{\bar{h}}$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $\frac{V_m}{V_{f_m}}$ and its associated parameters in terms of liquid filled levels.
A. Liquid Hydrogen and Vapor  
Liquid Filled=30%  \( t = 0.00 \) s  
\( g = -5.50 \times 10^{-3} \) g  
\( f = 0.00 \) Hz

B. Liquid Hydrogen and Vapor  
Liquid Filled=30%  \( t = 3.00 \times 10^{-1} \) s  
\( g = -5.50 \times 10^{-3} \) g  
\( f = 0.00 \) Hz

C. Liquid Hydrogen and Vapor  
Liquid Filled=30%  \( t = 5.27 \times 10^{-1} \) s  
\( g = -5.50 \times 10^{-3} \) g  
\( f = 0.00 \) Hz

D. Liquid Hydrogen and Vapor  
Liquid Filled=30%  \( t = 9.47 \times 10^{-1} \) s  
\( g = -5.50 \times 10^{-3} \) g  
\( f = 0.00 \) Hz

Fig 2
A. Liquid Hydrogen and Vapor
Liquid Filled - 50%  \( t = 0.00\) s
\( g = -6.52 \times 10^2 \) g.
\( f = 0.00\) Hz

B. Liquid Hydrogen and Vapor
Liquid Filled - 50%  \( t = 2.40 \times 10^1\) s
\( g = -6.52 \times 10^2 \) g.
\( f = 0.00\) Hz

C. Liquid Hydrogen and Vapor
Liquid Filled - 50%  \( t = 4.04 \times 10^1\) s
\( g = -6.52 \times 10^2 \) g.
\( f = 0.00\) Hz

D. Liquid Hydrogen and Vapor
Liquid Filled - 50%  \( t = 5.24 \times 10^1\) s
\( g = -6.52 \times 10^2 \) g.
\( f = 0.00\) Hz

Fig 3
A. Liquid Hydrogen and Vapor  
Liquid Filled-65%  \( t = 0.00 \) s  
\( g = -6.60 \times 10^{-3} \) g  
\( f = 0.00 \) Hz  

B. Liquid Hydrogen and Vapor  
Liquid Filled-65%  \( t = 2.40 \times 10^{-1} \) s  
\( g = -6.60 \times 10^{-3} \) g  
\( f = 0.00 \) Hz

C. Liquid Hydrogen and Vapor  
Liquid Filled-65%  \( t = 4.61 \times 10^{-1} \) s  
\( g = -6.60 \times 10^{-3} \) g  
\( f = 0.00 \) Hz

D. Liquid Hydrogen and Vapor  
Liquid Filled-65%  \( t = 7.61 \times 10^{-1} \) s  
\( g = -6.60 \times 10^{-3} \) g  
\( f = 0.00 \) Hz

Fig 4
A. Liquid Hydrogen and Vapor
Liquid Filled=70% $t=0.00s$
g=-6.70x10^{-2}g$
f=0.00Hz

B. Liquid Hydrogen and Vapor
Liquid Filled=70% $t=1.80x10^{-1}s$
g=-6.70x10^{-3}g$
f=0.00Hz

C. Liquid Hydrogen and Vapor
Liquid Filled=70% $t=2.84x10^{-1}s$
g=-6.70x10^{-2}g$
f=0.00Hz

D. Liquid Hydrogen and Vapor
Liquid Filled=70% $t=1.18x10^{0}s$
g=-6.70x10^{-3}g$
f=0.00Hz

Fig 5
A. Liquid Hydrogen and Vapor
Liquid Filled-80% $t = 0.00s$
$g = -8.20 \times 10^{-3} g_s$
f = 0.00Hz

B. Liquid Hydrogen and Vapor
Liquid Filled-80% $t = 1.80 \times 10^{-1}s$
$g = -8.20 \times 10^{-3} g_s$
f = 0.00Hz

C. Liquid Hydrogen and Vapor
Liquid Filled-80% $t = 2.77 \times 10^{-1}s$
$g = -8.20 \times 10^{-3} g_s$
f = 0.00Hz

D. Liquid Hydrogen and Vapor
Liquid Filled-80% $t = 7.57 \times 10^{-1}s$
$g = -8.20 \times 10^{-3} g_s$
f = 0.00Hz

Fig 6
Fig 7(A,B)

(A) AVERAGE FREE FALL FLOW VELOCITY, $V_f$ (cm/sec)

(B) MAXIMUM FLOW VELOCITY, $V_m$ (cm/sec)

(B) LIQUID REACHING BOTTOM TIME, $t_r$ (sec)

(C) $t_r/t_f$
Fig 8 (A, B)
(A) AVERAGE LIQUID HEIGHT, \( h \) (cm)

(B) SCALE LENGTH OF MAXIMUM FLOW VELOCITY, \( L_m \) (cm)

Fig 9 (A, B)
(F) Cryogenic Liquid Hydrogen Reorientation
Activated by Low Frequency Impulsive Settling
Acceleration of Geyser Initiation
ABSTRACT

The requirement to settle or to position liquid fluid over the outlet end of spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem. Resettlement or reorientation of liquid propellant can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion for the space fluid management under microgravity environment. The purpose of present study is to investigate most efficient technique for propellant resettling through the minimization of propellant usage and weight penalties. Comparison between the constant reverse gravity acceleration and impulsive reverse gravity acceleration to be used for the activation of propellant resettlement, it shows that impulsive reverse gravity thrust is superior to constant reverse gravity thrust for liquid reorientation in a reduced gravity environment.
I. Introduction

In spacecraft design, the requirements for a settled propellant are different for tank pressurization, engine restart, venting, or propellant transfer. Prepressurization requires that heat and mass transfer effects be minimized; otherwise, a process of chill down of tank, venting of noncondensing gases, etc., may have to carry out for the cryogenic system. For engine restart, it is necessary to have the liquid settle with no bubbles near the tank outlet so that the initial flow of propellant will not carry vapor to the pump or engine. The slosh wave amplitude should be relatively low to keep the center of mass shifts within an acceptable range and wave motion low enough to avoid pressure collapse caused by interface agitation. For venting, it is probably necessary that virtually all bubbles be displaced from the bulk liquid so that a two-phase mixture is not vented. Propellant transfer requires that the liquid be completely settled with virtually no bubbles. Outflow of a liquid near the tank outlet can result in the premature ingestion of gas while a significant amount of liquid is still in the tank under microgravity environment. This phenomenon is termed "suction dip". Slosh wave motion must be minimal because the combination of "suction dip" and sloshing could cause gas pull-through to occur more readily in microgravity than if the surface were essentially quiescent.

During the prepressurization of a cryogenic propellant in microgravity, significant heat and mass transfer will occur if the liquid interface is disturbed. Interface disturbances may result from (a) impingement of the gas on the liquid surface at a mass flow
rate sufficient to cause Kelvin-Helmholtz instability, (b) globule formation from breaking waves caused by wave motion over baffles or internal hardware, (c) globule and surface froth formation resulting from movement of bubbles through the liquid to the surface, and (d) surface froth formation because of gas impingement.

Bubble and globule formation as a result of liquid impact with the aft end of the tank could lead to propellant loss for the spacecraft during venting. Globules could be entrained in the vented ullage gas or bubbles rising through the liquid and expanding because of the decreasing tank pressure could cause a spray of globules to be vented. Liquid level rise, vent liquid loss, fluid freezing, and vehicle dynamics are all affected by the microgravity levels.

A key objective of the cryogenic fluid management of spacecraft propulsion system, such as a Space Transfer Vehicle (STV), is to develop the technology necessary for acquisition or positioning of liquid and vapor within a tank in reduced gravity to enable liquid outflow or vapor venting. Liquid acquisition techniques can be divided into two general categories: (1) Active liquid acquisition by the creation of a positive acceleration environment resulting from the propulsive thrust of small auxiliary engines, and (2) Passive liquid acquisition utilizing the liquid capillary forces provided by using solid baffles of liquid traps made of fine mesh screen material. In this series of study, active liquid acquisition is aimed for numerically simulating the resettlement of cryogenic liquid hydrogen. Liquid hydrogen, which, in general, poses more severe technical challenges than liquid oxygen, is used as the test bed
working fluid in this study.

Recently Leslie\textsuperscript{2} was able to measure and to numerically compute the bubble shapes at various ratios of centrifugal force to surface tension force in 2, 4 and 6.3 cm deep cylinders in the microgravity environment. The results showed excellent agreement between model computation and measurements. Hung and Leslie\textsuperscript{3} extended Leslie's work\textsuperscript{2} to rotating free surfaces influenced by gravity with higher rotating speeds when the bubble intersects with both the top and bottom walls of the cylinder. Hung et al.\textsuperscript{4,5} further extended the work to include rotating speeds which resulted with bubbles intersecting and/or without intersecting the top, bottom and side walls of the cylinder.

An analysis of time-dependent dynamical behavior of surface tension on partially-filled rotating fluids in both low gravity and microgravity environments was carried out by numerically solving the Navier-Stokes equations subjected to the initial and the boundary conditions\textsuperscript{4,6}. At the interface between the liquid and the gaseous fluids, both the kinematic surface boundary condition, and the interface stress conditions for components tangential and normal to the interface, were applied. The initial condition for the bubble profiles was adopted from steady-state formulations developed by Hung and Leslie\textsuperscript{3}, and Hung et al.\textsuperscript{6} for rotating cylinder tank; and by Hung et al.\textsuperscript{5,7} for the dewar-shaped container to be used in the Gravity Probe-B Spacecraft\textsuperscript{8}. Some of the steady-state formulations of bubble shapes, in particular for bubbles intersecting at the top wall of the cylinder, were compared with the experiment carried out by
Leslie in a free-falling aircraft (KC-135). Comparisons of time-dependent results between numerical computations and experiments were unavailable. This was because the calibration of the recordings of time-dependent gravity variations in a KC-135 aircraft during the short time periods of microgravity environment is very difficult. There was also an unavailability of accelerometer data for measuring the actual levels of microgravity during the experiment.

An efficient propellant settling technique should minimize propellant usage and weight penalties. This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion.

Production of geyser during the propellant reorientation is not a desirable motion for the space fluid management. It is because geyser is always accompanied by the vapor entrainment and globule formation. Geyser is observed at reverse gravity thrust greater than certain critical values of acceleration during the course of liquid reorientation. In other words, geyser will not be observed at very low reverse gravity level, and it will be detected when the reverse gravity level is greater than the certain critical value. In this series of study, numerical simulation of positive liquid acquisition is attempted by introducing reverse gravity acceleration, resulting from the propulsive thrust of small auxiliary engines which exceeds the critical value for geyser initiation. The reverse gravity acceleration is starting with a small value and increases gradually.
till the initiation of geyser is detected in the computer simulation for the liquid reorientation of propellant tank with various liquid-filled levels.

In this series of studies, time-dependent computations have been carried out to investigate the dynamical behavior of fluid reorientation or resettling of propellant prior to main engine firing for spacecraft restart at the net reverse gravity acceleration which is great enough to initiate geyser during the liquid reorientation. First paper of present study (Paper I)\(^9\) investigates the characteristics of fluid resettlement due to the reversal of lowest constant reverse gravity acceleration which is great enough to initiate geyser without any impulsive acceleration. The frequency of impulsive acceleration is generally termed "gravity jitters". Gravity jitters are produced by spacecraft attitude motion, machinery (turbine, pump, engine) vibrations, thruster firing, thruster shutdown, impulsive engine acceleration, etc.\(^{10}\) Positioning of liquid propellant over the tank outlet can be carried out by using small auxiliary thrusters which provide a thrust parallel to the tank's major axis in the direction of flight.

Computer simulation of flow field based on Paper I\(^9\) during the course of fluid reorientation induced by constant reverse gravity acceleration show that six dimensionless parameters are obtained in the study. These parameters hold near constant values through the entire ranges of liquid filled levels during the course of fluid reorientation activated by the reverse gravity acceleration great enough to initiate geyser. As the denominators of these
dimensionless parameters are either predetermined from the geometry of liquid filled levels or can be deduced from the corresponding calculations associated with the geyser initiation gravity levels. One can predict the values of these flow parameters. These predictable parameters include maximum flow velocity \( V_m \), time for observing maximum flow velocity \( t_m \), time for reorienting liquid flowing down and reaching the bottom of propellant tank \( t_R \), scale length of maximum flow velocity \( L_m \), and scale flow acceleration associated with maximum velocity \( a_m \).

Instead of applying constant reverse gravity acceleration as we described in Paper I\(^9\), this paper adopts impulsive reverse gravity acceleration with a low frequency of 0.1 Hz for the activation of fluid reorientation with liquid filled levels of 30, 50, 65, 70 and 80%.

II. Numerical Simulation of Liquid Hydrogen Reorientation with Geyser Initiation at Low Frequency Impulsive Reverse Gravity Acceleration of 0.1 Hz

The present study examines time-dependent fluid behaviors, in particular the dynamics of liquid hydrogen and hydrogen vapor reorientation induced by reverse gravity acceleration which is great enough to introduce geyser initiation. As in Paper I\(^9\), time-dependent axial symmetry mathematical formulation are adopted. Detailed description of mathematical formulation, initial and boundary conditions suitable for the analysis of cryogenic fluid management under microgravity environment are given in our earlier
studies. The initial profiles of liquid-vapor interface are determined from computations based on algorithms developed for the steady state formulation of microgravity fluid management. Detailed description of computational algorithm applicable to microgravity fluid management are illustrated in Paper I and our earlier studies. As we have indicated in Paper I, for the purpose of facilitating easy comparison between computational results and experimental measurement, a model of 0.01 size prototype is adopted in the computer simulation. Model size is height L = 4.23672 cm and diameter D = 4.2672 cm. If the spacecraft had been coasting for a long time, aligned with its direction of motion, the most significant force, drag, would be axial and with acceleration of \(10^{-4}g_0\), along upward direction. The hydrogen vapor is, thus, originally positioned at the bottom of the tank. The requirement to settle or to position liquid fuel over the outlet end of the spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem. Retromaneuvers of spacecraft, such as STV, require settling or reorientation of the propellant prior to main engine firing. Cryogenic liquid propellant shall be positioned over the tank outlet by using auxiliary thrusters (or idle-mode thrusters from the main engine) which provide a thrust parallel to the tank's major axis in the direction of flight. Similar to Paper I, a small value of reverse gravity acceleration (downward direction) is provided by the propulsive thrust of small auxiliary engine to initiate the reorientation of liquid propellant. This small value of reverse gravity acceleration of propulsive thrust increases
gradually till reaching the critical value on which initiation of geyser is detected during the time period of fluid resettlement. We term this reverse gravity acceleration of propulsive thrust, which is capable to initiate geyser, as "geyser initiation gravity-level". This geyser initiation gravity level has been investigated through the method of trial and error for the various liquid-filled levels as a base to simulate impulsive reverse gravity acceleration with frequencies of 0.1, 1.0 and 10 Hz. As we have indicated in Paper I, cryogenic liquid hydrogen at temperature of 20K is considered. Hydrogen density of 0.071 g/cm$^3$; surface tension coefficient at the interface between liquid hydrogen and hydrogen vapor of 1.9 dyne/cm; hydrogen viscosity coefficient of 1.873 x 10$^{-3}$ cm$^2$/s; and contact angle of 0.5$^\circ$ are used in the computer simulation.

In this paper, among three categories of impulsive reverse gravity acceleration with frequencies of 0.1, 1.0 and 10 Hz, reorientation of cryogenic liquid hydrogen activated by geyser initiation impulsive reverse gravity acceleration with a low frequency of 0.1 Hz produced by propulsive thrust will be investigated for various liquid filled levels of propellant tank. Paper I shows that these geyser initiation gravity levels are 5.5 x 10$^{-2}$, 6.52 x 10$^{-2}$, 6.6 x 10$^{-2}$, 6.7 x 10$^{-2}$ and 8.2 x 10$^{-2}$g$_0$ for liquid filled levels of 30, 50, 65, 70, and 80%, respectively.

Table 1 shows some basic geometries and characteristics of cryogenic liquid hydrogen resettlement activated by reverse gravity acceleration at geyser initiation gravity level. Average liquid height $\bar{h}$, and maximum liquid height $h_m$ are shown in Figure 1. Average
free fall velocity \( \bar{V}_f \), average free fall time \( \bar{t}_f \), and free fall velocity from maximum liquid height \( V_{fm} \) are computed from the following equations:

\[
\bar{V}_f = (2g_{io}h)^{1/2}
\]

\[
\bar{t}_f = \left( \frac{2h}{g_{io}} \right)^{1/2}
\]

\[
V_{fm} = (2g_{io}h_m)^{1/2}
\]

where \( g_{io} \) denotes geyser initiation reverse gravity acceleration.

To show examples of the selected sequences of time evolution of fluid reorientation for cryogenic hydrogen, Figures 2, 3, 4, 5, and 6 show time evolution of fluid reorientation activated by geyser initiation impulse reverse gravity acceleration with a frequency of 0.1 Hz for liquid filled levels of 30, 50, 65, 70 and 80 %, respectively. Each figure contains four sub-figures. Subfigure (A) is initial profile of liquid-vapor interface at the moment of the starting of fluid reorientation at time \( t = 0 \); subfigure (B), the flow profile during the course of fluid reorientation before the initiation of geysering motion; subfigure (C), the flow profile with geysering motion; and subfigure (D), the flow profile after the ending of geysering motion.

Examples of selected sequences of time evolution of fluid reorientation illustrate following flow behaviors: (1) The liquid starts to flow in an annular sheet along the solid wall of tank and gradually pushes the vapor toward the central portion of the lower dome of tank as the net acceleration, reversing the direction of gravity field, which is applied toward the downward direction of the
tank's major axis, by using small auxiliary thrusters; (2) As the downward fluid annular sheet along the tank wall reaches the central bottom dome side of the tank, a geysering flow is observed; and (3) The vapor is thus pushed upward centrally into the liquid and the geysering disappears.

Based on the computer simulation of flow field values of maximum flow velocity \( V_m \), time for observing maximum flow velocity \( t_m \), and time for reorienting liquid flowing down and reaching the bottom of propellant tank \( t_R \), are obtained and illustrated in Table 2 for reverse gravity acceleration with impulsive frequency of 0.1 Hz. Scale length of maximum flow velocity \( L_m \), and scale flow acceleration associated with maximum velocity \( a_m \), can be computed from the following parameters:

\[
L_m = V_m t_m \tag{4}
\]

\[
a_m = \frac{V_m}{t_m} \tag{5}
\]

Following dimensionless parameters are introduced: \( V_m/\bar{V}_f, t_R/\bar{t}_f, t_m/\bar{t}_f, a_m/a_g, L_m/\bar{h} \) and \( V_m/V_{fm} \) where \( a_g \) stands geyser initiation acceleration \((\text{cm/s}^2)\) for corresponding geyser initiation gravity level \( g_{i0} \). Impulsive reverse gravity acceleration, \( g_i \) with frequency \( f \) Hz is defined as follows:

\[
g_i = g_{i0} \left( 1 + \frac{1}{2} \sin 2\pi ft \right) \tag{6}
\]

Figures 7 to 9 show the variations of dimensionless parameters in terms of liquid filled levels for impulsive acceleration with frequency of 0.1 Hz. Denominators of these six dimensionless
parameters are either predetermined from the geometry of liquid fill levels or can be deduced from the corresponding calculations associated with the geyser initiation gravity levels. Characteristics of these near constant values dimensionless parameters can provide a good understanding of the physics of microgravity fluid behaviors, in particular the active category of liquid acquisition or positioning, and also the design criteria of on-orbit spacecraft propulsion system at the critical value of reverse gravity acceleration of propulsive thrust which is capable to initiate geyser.

An efficient propellant settling technique should minimize propellant usage and weight penalties. This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion. In particular, it is important to study how well the impulsive acceleration can provide higher efficient propellant settling technique than the constant acceleration thrust technique. Also, what is the most optimal choice of impulsive frequency which can achieve the best fluid acquisition management being the goal of our research.

Figure 7(A) shows the ratio of maximum flow velocity to average free fall flow velocity $\frac{V_m}{\bar{V}_f}$ and its associated parameters of $V_m$ and $\bar{V}_f$ in terms of liquid filled levels for impulsive acceleration with frequency of 0.1 Hz. It shows that the ratio of $V_m/\bar{V}_f$ varies in the range of 5.0 to 5.1 in the entire liquid filled levels while $V_m$ and $\bar{V}_f$
vary from 64.0 to 85.3 cm/s (decreasing with increasing liquid filled levels) and from 12.5 to 17.0 cm/s (also decreasing with increasing liquid filled levels), respectively. As \( \bar{V}_f \) can be predetermined from geyser initiation gravity level and average liquid height, shown in Equation (1), one can make an approximate prediction of maximum flow velocity during the liquid reorientation for the various liquid filled levels. In comparison between impulsive acceleration with frequency of 0.1 Hz and constant thrust acceleration, it shows that impulsive acceleration can produce higher maximum flow velocity (\( V_m/\bar{V}_f = 5.0 \) to 5.1) than that of constant thrust acceleration (\( V_m/\bar{V}_f = 4.3 \) to 4.9).

Figure 7(B) shows the ratio of liquid reaching bottom time to average free fall time \( t_R/\bar{t}_f \) and its associated parameters of \( t_R \) and \( \bar{t}_f \) in terms of liquid filled levels for impulsive acceleration with frequency of 0.1 Hz. It shows that the ratio of \( t_R/\bar{t}_f \) varies in the range of 1.1 to 1.2 in the entire liquid filled levels while \( t_R \) and \( \bar{t}_f \) vary from 0.19 to 0.36 s (decreasing with increasing liquid filled levels) and from 0.15 to 0.32 s (also decreasing with increasing liquid filled levels), respectively. As \( \bar{t}_f \) can be predetermined from geyser initiation gravity level and average liquid height, shown in Equation (2), one can predict the time reorienting liquid fluid flowing down from the original position and reaching the bottom of propellant tank for the various liquid filled levels at the reverse gravity acceleration capable for the initiation of geyser. In comparison between impulsive acceleration with frequency of 0.1 Hz and constant thrust acceleration, it shows that impulsive
acceleration activate the flow which takes shorter time for flow to reach the tank bottom \( \left( \frac{t_R}{\bar{t}_f} = 1.1 \text{ to } 1.2 \right) \) than that of constant thrust acceleration \( \left( \frac{t_R}{\bar{t}_f} = 1.21 \text{ to } 1.30 \right) \).

Figure 8(A) shows the ratio of time for observing maximum flow velocity to average free fall time \( \frac{t_m}{\bar{t}_f} \) and its associated parameters of \( t_m \) and \( \bar{t}_f \) in terms of liquid filled levels for impulsive acceleration with frequency of 0.1 Hz. It shows that the ratio of \( \frac{t_m}{\bar{t}_f} \) varies in the range of 1.2 to 1.3 in the entire liquid filled levels while \( t_m \) and \( \bar{t}_f \) vary from 0.18 to 0.39 s (decreasing with increasing liquid filled levels) and from 0.15 to 0.32 s (also decreasing with increasing liquid filled levels), resectively. As we indicated in Figure 7(B), \( \bar{t}_f \) can be predetermined, one can predict the time for observing maximum flow velocity for various liquid filled levels at the reverse gravity acceleration capable for the initiation of geyser. In comparison between impulsive acceleration with frequency of 0.1 Hz and constant thrust acceleration, it shows that impulsive acceleration can activate higher maximum flow velocity within a shorter period of time (0.18 to 0.39 s) than that of constant thrust acceleration (0.20 to 0.425).

Figure 8(B) shows the ratio of scale flow acceleration associated with maximum velocity to geyser initiation acceleration for corresponding geyser initiation gravity level \( \frac{a_m}{a_g} \) and its associated parameters of \( a_m \) and \( a_g \) in terms of liquid filled levels for impulsive acceleration with frequency of 0.1 Hz. It shows that the ratio of \( \frac{a_m}{a_g} \) varies in the range of 4.1 to 4.4 in the entire liquid filled levels while \( a_m \) and \( a_g \) vary from 218 to 355 \( \text{cm/s}^2 \) (increasing
with increasing liquid filled levels) and from 53.9 to 80.4 cm/s² (also increasing with increasing liquid filled levels), respectively. As \(a_g\) can be predetermined from geyser initiation gravity level, one can make an approximate prediction of scale flow acceleration associated with maximum velocity, which is defined in Equation (5), at the reverse gravity acceleration capable for the initiation of geyser. In comparison between impulsive acceleration with frequency of 0.1 Hz and constant thrust acceleration, it shows that impulsive acceleration can produce higher scale flow acceleration associated with maximum flow velocity \((a_m/a_g = 4.1 \text{ to } 4.4)\) than that of constant thrust acceleration \((a_m/a_g = 3.3 \text{ to } 3.8)\).

Figure 9(A) shows the ratio of scale length of maximum flow velocity to average liquid height \(L_m/\bar{h}\) and its associated parameters of \(L_m\) and \(\bar{h}\) in terms of liquid filled levels for impulsive acceleration with frequency of 0.1 Hz. It shows that the ratio of \(L_m/\bar{h}\) varies in the range of 12.3 to 12.6 in the entire liquid filled levels while \(L_m\) and \(\bar{h}\) vary from 11.5 to 33.2 cm (decreasing with increasing liquid filled levels) and from 0.93 to 2.67 cm (also decreasing with increasing liquid filled levels), respectively. As \(\bar{h}\) can be predetermined from the geometry of liquid filled levels, one can make an approximate prediction of scale length of maximum flow velocity, which is defined in Equation (4), at the reverse gravity acceleration capable for the initiation of geyser. In comparison between impulsive acceleration with frequency of 0.1 Hz and constant thrust acceleration, it shows that impulsive acceleration can produce longer scale length of maximum flow velocity \((L_m = 11.5 \text{ to } 33.2 \text{ cm})\) than that
of constant thrust acceleration \( (L_m = 12.4 \text{ to } 30.9) \).

Figure 9(B) shows the ratio of maximum flow velocity to free fall velocity from maximum liquid height \( V_m/V_{fm} \) and its associated parameters of \( V_m \) and \( V_{fm} \) in terms of liquid filled levels for impulsive acceleration with frequency of 0.1 Hz. It shows that the ratio of \( V_m/V_{fm} \) varies in the range of 4.0 to 4.4 in the entire liquid filled levels while \( V_m \) and \( V_{fm} \) vary from 64.0 to 85.3 cm/s (decreasing with increasing liquid filled levels) and from 16.4 to 19.2 cm/s (also decreasing with increasing liquid filled levels), respectively. As \( V_{fm} \) can be predetermined from geyser initiation gravity level and maximum liquid height, shown in Equation (3), one can make an approximate prediction of maximum flow velocity at the reverse gravity acceleration capable for the initiation of geyser. In comparison between impulsive acceleration with frequency of 0.1 Hz and constant thrust acceleration, it shows that impulsive acceleration can produce higher maximum velocity \( (V_m/V_{fm} = 4.0 \text{ to } 4.4) \) than that of constant thrust acceleration \( (V_m/V_{fm} = 3.8 \text{ to } 4.0) \).

As we have illustrated in Paper 1\(^9\), six dimensionless parameters presented in this study show that the parameters hold near constant values through the entire ranges of liquid filled levels during the course of reorientation of liquid hydrogen activated by the reverse gravity acceleration which is great enough to initiate geysering flow. As the purpose of present study is to investigate an efficient propellant settling technique which is able to minimize propellant usage and weight penalties, comparison of flow parameters between impulsive acceleration with frequency of 0.1 Hz and that of constant
thrust acceleration have been made toward this objective. It shows that the operation of auxiliary engine with impulsive acceleration of 0.1 Hz frequency is better than that of constant thrust acceleration in terms of introducing a higher maximum flow velocity, a shorter time period to reach maximum flow velocity, a shorter time period for flow to reach the tank bottom (tank outlet) for resettling, a longer scale length of maximum flow velocity, and a higher flow acceleration associated with maximum flow velocity.

IV. Discussion and Conclusions

The requirement to settle or to position liquid fluid over the outlet end of the spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem. Retromaneuvers of spacecraft require settling or reorientation of the propellant prior to main engine firing. Cryogenic liquid propellant is positioned over the tank outlet by using small auxiliary thrusters (or idle-mode thrusters from the main engine) which provide a thrust parallel to the tank’s major axis in the direction of flight.

The results of the study of fluid reorientation have to be evaluated in terms of how well they can be managed efficiently. An efficient propellant settling technique should minimize propellant usage and weight penalties through the operation of small thrusters (or idle-mode thrusters from the main engine). This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion.
Production of geyser during the propellant reorientation is not a desirable motion for the space fluid management under microgravity environment. It is because geyser is always accompanied by the vapor entrainment and globule formation. Geyser is observed at reverse gravity acceleration greater than certain critical values of acceleration during the course of liquid reorientation. In this paper, numerical simulation of positive liquid acquisition is attempted by introducing reverse gravity acceleration, resulting from the propulsive thrust with high impulsive frequency of 0.1 Hz auxiliary engine, which exceeds critical value for the initiation of geyser.

Evaluation of performance is based on how efficient the impulsive reverse gravity with 0.1 Hz frequency in comparison with constant thrust acceleration can activate following flow parameters at the same background thrust accelerations: (A) a higher maximum flow velocity, (B) a shorter time period for flow to reach maximum velocity, (C) a shorter time period for flow to reach tank bottom (tank outlet) for fluid resettling, (D) a larger length scale of maximum flow velocity, and (E) a higher flow acceleration associated with maximum flow velocity. Comparison between the results of present study for impulsive thrust with 0.1 Hz frequency and that of constant thrust, shown in Paper I, it shows that impulsive thrust is superior than the constant reverse thrust in terms of efficient operation of fluid reorientation.

Based on the computer simulation of flow fields during the course of fluid reorientation, six dimensionless parameters are presented.
It is shown that these parameters hold near constant values through the entire ranges of liquid filled levels during the course of fluid reorientation activated by the reverse gravity acceleration in both constant and impulsive thrusts great enough to initiate geyser. As the denominators of these dimensionless parameters are either predetermined from the geometry of liquid filled levels, as shown in Table 1, or can be deduced from the corresponding calculations associated with the geyser initiation gravity levels, one can predict the values of these flow parameters. Present study can greatly enhance our understanding in the behaviors of cryogenic fluid resettlement under reduced gravity environment. This is particularly important for liquid acquisition technique to be used in on-orbit spacecraft design.

Any fluid capable of motion relative to the spacecraft will be subject to an acceleration relative to the mass center of the spacecraft that arises from the gravity gradient of the Earth\textsuperscript{14,15}. In addition to the Earth's gravitational force, the interaction between the particle mass of fluids and the spacecraft mass due to gravity gradient acceleration\textsuperscript{14} have also been taken into consideration in this microgravity fluid management study.

To conclude, we have demonstrated that, the computer algorithm presented, can be used to simulate fluid behavior in a microgravity environment, in particular the development of technology necessary for acquisition or positioning of liquid and vapor within a tank to enable liquid outflow or vapor venting through active liquid acquisition by the creation of a positive acceleration environment.
resulting from propulsive thrust. Better understanding of the full pictures of flow fields in both constant and impulsive thrusts, during the course of fluid reorientation can provide the proper design techniques for handling and managing the cryogenic liquid propellants to be used in on-orbit spacecraft propulsion. It is important to emphasize that impulsive reverse gravity thrust is superior to constant reverse gravity thrust for the activation of liquid necessary for the resettlement of liquid in a reduced gravity environment.

Acknowledgement

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Reference


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<th>65</th>
<th>70</th>
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<tr>
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<td>4.4</td>
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Figure Captions

Figure 1. (A) Distribution of grid points in the radial-axial plane of cylindrical coordinate for propellant tank, and (B) Model size propellant tank adopted for numerical simulation with geometrical description.

Figure 2. Selected sequences of time evolution of fluid reorientation with liquid filled level of 30% for impulsive acceleration with frequency of 0.1 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 3. Selected sequences of time evolution of fluid reorientation with liquid filled level of 50% for impulsive acceleration with frequency of 0.1 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 4. Selected sequences of time evolution of fluid reorientation with liquid filled level of 65% for impulsive acceleration with frequency of 0.1 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 5. Selected sequences of time evolution of fluid reorientation with liquid filled level of 70% for impulsive acceleration with frequency of 0.1 Hz, (A)
initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 6. Selected sequences of time evolution of fluid reorientation with liquid filled levels of 80% for impulsive acceleration with frequency of 0.1 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 7. (A) Ratio of $V_m/V_f$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $t_R/t_f$ and its associated parameters in terms of liquid filled levels.

Figure 8. (A) Ratio of $t_m/t_f$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $a_m/a_g$ and its associated parameters in terms of liquid filled levels.

Figure 9. (A) Ratio of $L_m/h$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $V_m/V_{fm}$ and its associated parameters in terms of liquid filled levels.
A. Liquid Hydrogen and Vapor
Liquid Filled=30% t = 0.00s
$g = 5.50 \times 10^{-2} \text{g}$
f = $1.00 \times 10^{4} \text{Hz}$

B. Liquid Hydrogen and Vapor
Liquid Filled=30% t = 2.40 x $10^{3}$s
$g = 5.50 \times 10^{-2} \text{g}$
f = $1.00 \times 10^{4} \text{Hz}$

C. Liquid Hydrogen and Vapor
Liquid Filled=30% t = 5.27 x $10^{3}$s
$g = 5.50 \times 10^{-2} \text{g}$
e = 0.00 rpm
f = $1.00 \times 10^{4} \text{Hz}$

D. Liquid Hydrogen and Vapor
Liquid Filled=30% t = 8.27 x $10^{3}$s
$g = 5.50 \times 10^{-2} \text{g}$
f = $1.00 \times 10^{4} \text{Hz}$

Fig 2
A. Liquid Hydrogen and Vapor
Liquid Filled=50% t= 0.00s
$g=-6.52 \times 10^{-2} \text{g}_s$
$f=1.00 \times 10^{-1} \text{Hz}$

B. Liquid Hydrogen and Vapor
Liquid Filled=50% t= 2.40 \times 10^{-1} \text{s}
$g=-6.52 \times 10^{-2} \text{g}_s$
$f=1.00 \times 10^{-1} \text{Hz}$

C. Liquid Hydrogen and Vapor
Liquid Filled=50% t= 4.58 \times 10^{-1} \text{s}
$g=-6.52 \times 10^{-2} \text{g}_s$
$f=1.00 \times 10^{-1} \text{Hz}$

D. Liquid Hydrogen and Vapor
Liquid Filled=50% t= 1.90 \times 10^{0} \text{s}
$g=-6.52 \times 10^{-2} \text{g}_s$
$f=1.00 \times 10^{-1} \text{Hz}$

Fig 3
A. Liquid Hydrogen and Vapor
Liquid Filled-65% t = 0.00s
g = 6.60 \times 10^{-3} \text{g.s}^{-1}
f = 1.00 \times 10^{11} \text{Hz}

B. Liquid Hydrogen and Vapor
Liquid Filled-65% t = 2.40 \times 10^{-1} \text{s}
g = 6.60 \times 10^{-3} \text{g.s}^{-1}
f = 1.00 \times 10^{11} \text{Hz}

C. Liquid Hydrogen and Vapor
Liquid Filled-65% t = 3.90 \times 10^{-1} \text{s}
g = 6.60 \times 10^{-3} \text{g.s}^{-1}
f = 1.00 \times 10^{11} \text{Hz}

D. Liquid Hydrogen and Vapor
Liquid Filled-65% t = 7.50 \times 10^{-1} \text{s}
g = 6.60 \times 10^{-3} \text{g.s}^{-1}
f = 1.00 \times 10^{11} \text{Hz}

Fig 4
A. Liquid Hydrogen and Vapor
Liquid Filled=70% t= 0.00s
\( g = -7.00 \times 10^{-2} \text{g} \)
\( f = 1.00 \times 10^{-1} \text{Hz} \)

B. Liquid Hydrogen and Vapor
Liquid Filled=70% t= 1.80 \times 10^{-1}s
\( g = -7.00 \times 10^{-2} \text{g} \)
\( f = 1.00 \times 10^{-1} \text{Hz} \)

C. Liquid Hydrogen and Vapor
Liquid Filled=70% t= 3.35 \times 10^{-1}s
\( g = -7.00 \times 10^{-2} \text{g} \)
\( f = 1.00 \times 10^{-1} \text{Hz} \)

D. Liquid Hydrogen and Vapor
Liquid Filled=70% t= 8.75 \times 10^{-1}s
\( g = -7.00 \times 10^{-2} \text{g} \)
\( f = 1.00 \times 10^{-1} \text{Hz} \)

Fig 5
A. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 0.00s
$g = -8.20 \times 10^2 \text{g}$
$f = 1.00 \times 10^4 \text{Hz}$

B. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 1.80 \times 10^1 s
$g = -8.20 \times 10^2 \text{g}$
$f = 1.00 \times 10^4 \text{Hz}$

C. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 3.32 \times 10^1 s
$g = -8.20 \times 10^2 \text{g}$
$f = 1.00 \times 10^4 \text{Hz}$

D. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 6.92 \times 10^1 s
$g = -8.20 \times 10^2 \text{g}$
$f = 1.00 \times 10^4 \text{Hz}$

Fig 6
Fig 7 (A, B)
Fig 8 (A, B)
(G) Cryogenic Liquid Hydrogen Reorientation
Activated by Medium Frequency Impulsive Settling
Acceleration of Geyser Initiation
ABSTRACT

The requirement to settle or to position liquid fluid over the outlet end of spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem. Resettlement or reorientation of liquid propellant can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion for the space fluid management under microgravity environment. The purpose of present study is to investigate most efficient technique for propellant resettling through the minimization of propellant usage and weight penalties. Comparison between the constant reverse gravity acceleration and impulsive reverse gravity acceleration to be used for the activation of propellant resettlement, it shows that impulsive reverse gravity thrust is superior to constant reverse gravity thrust for liquid reorientation in a reduced gravity environment. Comparison among impulsive reverse gravity thrust with 0.1, 1.0 and 10 Hz frequencies for liquid filled level in the range between 30 to 80 %, it shows that the selection of 1.0 Hz frequency impulsive thrust over the other frequency ranges of impulsive thrust is most proper based on the present study.
Nomenclature

\( a_g = \) geyser initiation acceleration (cm/s\(^2\))

\( a_m = \) scale flow acceleration associated with maximum velocity (cm/s\(^2\)), defined by Equation (5)

\( D = \) diameter of propellant tank (cm)

\( f = \) frequency of impulsive thrust (Hz)

\( g_i = \) impulsive reverse gravity acceleration, defined by Equation (6)

\( g_{i0} = \) geyser initiation gravity-level (\(g_0\))

\( g_0 = \) normal Earth gravitational acceleration = 9.81 m/s\(^2\)

\( \bar{h} = \) average liquid height (cm)

\( h_m = \) maximum liquid height (cm)

\( L = \) height of propellant tank (cm)

\( L_m = \) scale length of maximum liquid height (cm/s), defined by Equation (4)

\( \text{STV} = \) Space Transfer Vehicle

\( t_f = \) average free fall time (s)

\( t_m = \) time for observing maximum flow velocity (s)

\( t_R = \) liquid reaching tank bottom time (s)

\( V_{fm} = \) free fall velocity from maximum liquid height (cm/s), defined by Equation (3)

\( \bar{V}_f = \) average free fall velocity (cm/s), defined by Equation (2)

\( V_m = \) maximum flow velocity (cm/s)
I. Introduction

In spacecraft design, the requirements for a settled propellant are different for tank pressurization, engine restart, venting, or propellant transfer. Prepressurization requires that heat and mass transfer effects be minimized; otherwise, a process of chill down of tank, venting of noncondensing gases, etc., may have to carry out for the cryogenic system. For engine restart, it is necessary to have the liquid settle with no bubbles near the tank outlet so that the initial flow of propellant will not carry vapor to the pump or engine. The slosh wave amplitude should be relatively low to keep the center of mass shifts within an acceptable range and wave motion low enough to avoid pressure collapse caused by interface agitation. For venting, it is probably necessary that virtually all bubbles be displaced from the bulk liquid so that a two-phase mixture is not vented. Propellant transfer requires that the liquid be completely settled with virtually no bubbles. Outflow of a liquid near the tank outlet can result in the premature ingestion of gas while a significant amount of liquid is still in the tank under microgravity environment. This phenomenon is termed "suction dip". Slosh wave motion must be minimal because the combination of "suction dip" and sloshing could cause gas pull-through to occur more readily in microgravity than if the surface were essentially quiescent.

During the prepressurization of a cryogenic propellant in microgravity, significant heat and mass transfer will occur if the liquid interface is disturbed. Interface disturbances may result from (a) impingement of the gas on the liquid surface at a mass flow
rate sufficient to cause Kelvin-Helmholtz instability, (b) globule formation from breaking waves caused by wave motion over baffles or internal hardware, (c) globule and surface froth formation resulting from movement of bubbles through the liquid to the surface, and (d) surface froth formation because of gas impingement.

Bubble and globule formation as a result of liquid impact with the aft end of the tank could lead to propellant loss for the spacecraft during venting. Globules could be entrained in the vented ullage gas or bubbles rising through the liquid and expanding because of the decreasing tank pressure could cause a spray of globules to be vented. Liquid level rise, vent liquid loss, fluid freezing, and vehicle dynamics are all affected by the microgravity levels.

A key objective of the cryogenic fluid management of spacecraft propulsion system, such as a Space Transfer Vehicle\(^1\) (STV), is to develop the technology necessary for acquisition or positioning of liquid and vapor within a tank in reduced gravity to enable liquid outflow or vapor venting. Liquid acquisition techniques can be divided into two general categories: (1) Active liquid acquisition by the creation of a positive acceleration environment resulting from the propulsive thrust of small auxiliary engines, and (2) Passive liquid acquisition utilizing the liquid capillary forces provided by using solid baffles of liquid traps made of fine mesh screen material. In this series of study, active liquid acquisition is aimed for numerically simulating the resettlement of cryogenic liquid hydrogen. Liquid hydrogen, which, in general, poses more severe technical challenges than liquid oxygen, is used as the test bed
working fluid in this study.

Recently Leslie's work was able to measure and to numerically compute the bubble shapes at various ratios of centrifugal force to surface tension force in 2, 4 and 6.3 cm deep cylinders in the microgravity environment. The results showed excellent agreement between model computation and measurements. Hung and Leslie's work extended Leslie's work to rotating free surfaces influenced by gravity with higher rotating speeds when the bubble intersects with both the top and bottom walls of the cylinder. Hung et al.'s further extended the work to include rotating speeds which resulted with bubbles intersecting and/or without intersecting the top, bottom and side walls of the cylinder.

An analysis of time-dependent dynamical behavior of surface tension on partially-filled rotating fluids in both low gravity and microgravity environments was carried out by numerically solving the Navier-Stokes equations subjected to the initial and the boundary conditions. At the interface between the liquid and the gaseous fluids, both the kinematic surface boundary condition, and the interface stress conditions for components tangential and normal to the interface, were applied. The initial condition for the bubble profiles was adopted from steady-state formulations developed by Hung and Leslie, and Hung et al. for rotating cylinder tank; and by Hung et al. for the dewar-shaped container to be used in the Gravity Probe-B Spacecraft. Some of the steady-state formulations of bubble shapes, in particular for bubbles intersecting at the top wall of the cylinder, were compared with the experiment carried out by
Leslie\textsuperscript{2} in a free-falling aircraft (KC-135). Comparisons of time-dependent results between numerical computations and experiments were unavailable. This was because the calibration of the recordings of time-dependent gravity variations in a KC-135 aircraft during the short time periods of microgravity environment is very difficult. There was also an unavailability of accelerometer data for measuring the actual levels of microgravity during the experiment.

An efficient propellant settling technique should minimize propellant usage and weight penalties. This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion.

Production of geyser during the propellant reorientation is not a desirable motion for the space fluid management. It is because geyser is always accompanied by the vapor entrainment and globule formation. Geyser is observed at reverse gravity thrust greater than certain critical values of acceleration during the course of liquid reorientation. In other words, geyser will not be observed at very low reverse gravity level, and it will be detected when the reverse gravity level is greater than the certain critical value. In this series of study, numerical simulation of positive liquid acquisition is attempted by introducing reverse gravity acceleration, resulting from the propulsive thrust of small auxiliary engines which exceeds the critical value for geyser initiation. The reverse gravity acceleration is starting with a small value and increases gradually.
till the initiation of geyser is detected in the computer simulation for the liquid reorientation of propellant tank with various liquid-filled levels.

In this series of studies, time-dependent computations have been carried out to investigate the dynamical behavior of fluid reorientation or resettling of propellant prior to main engine firing for spacecraft restart at the net reverse gravity acceleration which is great enough to initiate geyser during the liquid reorientation. First paper of present study (Paper I)\(^9\) investigates the characteristics of fluid resettlement due to the reversal of lowest constant reverse gravity acceleration which is great enough to initiate geyser without any impulsive acceleration. The frequency of impulsive acceleration is generally termed "gravity jitters". Gravity jitters are produced by spacecraft attitude motion, machinery (turbine, pump, engine) vibrations, thruster firing, thruster shutdown, impulsive engine acceleration, etc.\(^{10}\) Positioning of liquid propellant over the tank outlet can be carried out by using small auxiliary thrusters which provide a thrust parallel to the tank's major axis in the direction of flight.

Computer simulation of flow field based on Paper I\(^9\) during the course of fluid reorientation induced by constant reverse gravity acceleration show that six dimensionless parameters are obtained in the study. These parameters hold near constant values through the entire ranges of liquid filled levels during the course of fluid reorientation activated by the reverse gravity acceleration great enough to initiate geyser. As the denominators of these
dimensionless parameters are either predetermined from the geometry of liquid filled levels or can be deduced from the corresponding calculations associated with the geyser initiation gravity levels. One can predict the values of these flow parameters. These predictable parameters include maximum flow velocity $V_m$, time for observing maximum flow velocity $t_m$, time for reorienting liquid flowing down and reaching the bottom of propellant tank $t_R$, scale length of maximum flow velocity $L_m$, and scale flow acceleration associated with maximum velocity $a_m$.

Instead of applying constant reverse gravity acceleration as we described in Paper I, this paper adopts impulsive reverse gravity acceleration with a medium frequency of 1.0 Hz for the activation of fluid reorientation with liquid filled levels of 30, 50, 65, 70 and 80%.

II. Numerical Simulation of Liquid Hydrogen Reorientation with Geyser Initiation at Medium Frequency Impulsive Reverse Gravity Acceleration of 1.0 Hz

The present study examines time-dependent fluid behaviors, in particular the dynamics of liquid hydrogen and hydrogen vapor reorientation induced by reverse gravity acceleration which is great enough to introduce geyser initiation. As in Paper I, time-dependent axial symmetry mathematical formulation are adopted. Detailed description of mathematical formulation, initial and boundary conditions suitable for the analysis of cryogenic fluid
management under microgravity environment are given in our earlier studies. The initial profiles of liquid-vapor interface are determined from computations based on algorithms developed for the steady state formulation of microgravity fluid management.

Detailed description of computational algorithm applicable to microgravity fluid management are illustrated in Paper I and our earlier studies. As we have indicated in Paper I, for the purpose of facilitating easy comparison between computational results and experimental measurement, a model of 0.01 size prototype is adopted in the computer simulation. Model size is height \( L = 4.23672 \) cm and diameter \( D = 4.2672 \) cm. If the spacecraft had been coasting for a long time, aligned with its direction of motion, the most significant force, drag, would be axial and with acceleration of \( 10^{-4}g_0 \) along upward direction. The hydrogen vapor is, thus, originally positioned at the bottom of the tank. The requirement to settle or to position liquid fuel over the outlet end of the spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem. Retromaneuvers of spacecraft, such as STV, require settling or reorientation of the propellant prior to main engine firing. Cryogenic liquid propellant shall be positioned over the tank outlet by using auxiliary thrusters (or idle-mode thrusters from the main engine) which provide a thrust parallel to the tank's major axis in the direction of flight. Similar to Paper I, a small value of reverse gravity acceleration (downward direction) is provided by the propulsive thrust of small auxiliary engine to initiate the reorientation of liquid propellant. This small value of
reverse gravity acceleration of propulsive thrust increases gradually till reaching the critical value on which initiation of geyser is detected during the time period of fluid resettlement. We term this reverse gravity acceleration of propulsive thrust, which is capable to initiate geyser, as "geyser initiation gravity-level". This geyser initiation gravity level has been investigated through the method of trial and error for the various liquid-filled levels as a base to simulate impulsive reverse gravity acceleration with frequencies of 0.1, 1.0 and 10 Hz. As we have indicated in Paper I, cryogenic liquid hydrogen at temperature of 20K is considered. Hydrogen density of 0.071 g/cm³; surface tension coefficient at the interface between liquid hydrogen and hydrogen vapor of 1.9 dyne/cm; hydrogen viscosity coefficient of 1.873 x 10⁻³ cm²/s; and contact angle of 0.5° are used in the computer simulation.

In this paper, among three categories of impulsive reverse gravity acceleration with frequencies of 0.1, 1.0 and 10 Hz, reorientation of cryogenic liquid hydrogen activated by geyser initiation impulsive reverse gravity acceleration with a frequency of 1.0 Hz produced by propulsive thrust will be investigated for various liquid filled levels of propellant tank. Paper I shows that these geyser initiation gravity levels are 5.5 x 10⁻², 6.52 x 10⁻², 6.6 x 10⁻², 6.7 x 10⁻² and 8.2 x 10⁻²g₀ for liquid filled levels of 30, 50, 65, 70, and 80%, respectively.

Table 1 shows some basic geometries and characteristics of cryogenic liquid hydrogen resettlement activated by reverse gravity acceleration at geyser initiation gravity level. Average liquid
height \( h \), and maximum liquid height \( h_m \) are shown in Figure 1. Average free fall velocity \( \bar{V}_f \), average free fall time \( \bar{t}_f \), and free fall velocity from maximum liquid height \( V_{f m} \) are computed from the following equations:

\[
\bar{V}_f = (2g_{i_0} \bar{h})^{1/2} \tag{1}
\]

\[
\bar{t}_f = \left( \frac{2h}{g_{i_0}} \right)^{1/2} \tag{2}
\]

\[
V_{f m} = (2g_{i_0} h_m)^{1/2} \tag{3}
\]

where \( g_{i_0} \) denotes geyser initiation reverse gravity acceleration.

To show examples of the selected sequences of time evolution of fluid reorientation for cryogenic hydrogen, Figures 2, 3, 4, 5, and 6 show time evolution of fluid reorientation activated by geyser initiation impulse reverse gravity acceleration with a frequency of 1.0 Hz for liquid filled levels of 30, 50, 65, 70 and 80 %, respectively. Each figure contains four sub-figures. Subfigure (A) is initial profile of liquid-vapor interface at the moment of the starting of fluid reorientation at time \( t = 0 \); subfigure (B), the flow profile during the course of fluid reorientation before the initiation of geysering motion; subfigure (C), the flow profile with geysering motion; and subfigure (D), the flow profile after the ending of geysering motion.

Examples of selected sequences of time evolution of fluid reorientation illustrate following flow behaviors: (1) The liquid starts to flow in an annular sheet along the solid wall of tank and gradually pushes the vapor toward the central portion of the lower dome of tank as the net acceleration, reversing the direction of
gravity field, which is applied toward the downward direction of the tank's major axis, by using small auxiliary thrusters; (2) As the downward fluid annular sheet along the tank wall reaches the central bottom dome side of the tank, a geysering flow is observed; and (3) The vapor is thus pushed upward centrally into the liquid and the geysering disappears.

Based on the computer simulation of flow field values of maximum flow velocity $V_m$, time for observing maximum flow velocity $t_m$, and time for reorienting liquid flowing down and reaching the bottom of propellant tank $t_R$, are obtained and illustrated in Table 2 for reverse gravity acceleration with impulsive frequency of 1.0 Hz. Scale length of maximum flow velocity $L_m$, and scale flow acceleration associated with maximum velocity $a_m$, can be computed from the following parameters:

\[ L_m = V_m t_m \]  
\[ a_m = \frac{V_m}{t_m} \]  

Following dimensionless parameters are introduced: $V_m/\bar{V}_f$, $t_R/\bar{t}_f$, $t_m/\bar{t}_f$, $a_m/a_g$, $L_m/\bar{h}$ and $V_m/\bar{V}_f$ where $a_g$ stands geyser initiation acceleration (cm/s$^2$) for corresponding geyser initiation gravity level $g_{i0}$. Impulsive reverse gravity acceleration, $g_i$ with frequency $f$ Hz is defined as follows:

\[ g_i = g_{i0} \left(1 + \frac{1}{2} \sin 2\pi ft \right) \]  

Figures 7 to 9 show the variations of dimensionless parameters in terms of liquid filled levels for impulsive acceleration with...
frequency of 1.0 Hz. Denominators of these six dimensionless parameters are either predetermined from the geometry of liquid fill levels or can be deduced from the corresponding calculations associated with the geyser initiation gravity levels. Characteristics of these near constant values dimensionless parameters can provide a good understanding of the physics of microgravity fluid behaviors, in particular the active category of liquid acquisition or positioning, and also the design criteria of on-orbit spacecraft propulsion system at the critical value of reverse gravity acceleration of propulsive thrust which is capable to initiate geyser.

An efficient propellant settling technique should minimize propellant usage and weight penalties. This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion. In particular, it is important to study how well the impulsive acceleration can provide higher efficient propellant settling technique than the constant acceleration thrust technique. Also, what is the most optimal choice of impulsive frequency which can achieve the best fluid acquisition management being the goal of our research.

Figure 7(A) shows the ratio of maximum flow velocity to average free fall flow velocity $V_m/\bar{V}_f$ and its associated parameters of $V_m$ and $\bar{V}_f$ in terms of liquid filled levels for impulsive acceleration with frequency of 1.0 Hz. It shows that the ratio of $V_m/\bar{V}_f$ varies in the
range of 6.6 to 6.7 in the entire liquid filled levels while $V_m$ and $V_f$ vary from 82.5 to 112.2 cm/s (decreasing with increasing liquid filled levels) and from 12.5 to 17.0 cm/s (also decreasing with increasing liquid filled levels), respectively. As $V_f$ can be predetermined from geyser initiation gravity level and average liquid height, shown in Equation (1), one can make an approximate prediction of maximum flow velocity during the liquid reorientation for the various liquid filled levels. In comparison between impulsive acceleration with frequency of 1.0 Hz and with frequencies of 0.1 and 10 Hz, it shows that the former case of thrust can activate higher maximum flow velocity ($V_m/V_f = 6.6$ to 6.7) than that of the latter two cases of thrust accelerations ($V_m/V_f = 5.0$ to 5.2 for $f = 0.1$ Hz; and = 5.1 to 5.3 for $f = 10$ Hz).

Figure 7(B) shows the ratio of liquid reaching bottom time to average free fall time $t_R/t_f$ and its associated parameters of $t_R$ and $t_f$ in terms of liquid filled levels for impulsive acceleration with frequency of 1.0 Hz. It shows that the ratio of $t_R/t_f$ varies in the range of 1.1 to 1.2 in the entire liquid filled levels while $t_R$ and $t_f$ vary from 0.19 to 0.35 s (decreasing with increasing liquid filled levels), respectively. As $t_f$ can be predetermined from geyser initiation gravity level and average liquid height, shown in Equation (2), one can predict the time for reorienting liquid fluid flowing down from the original position and reaching the bottom of propellant tank for the various liquid filled levels at the reverse gravity acceleration capable for the initiation of geyser. In comparison between impulsive acceleration with frequency of 1.0 Hz and with
frequencies of 0.1 and 10 Hz, it shows that the former case of thrust can activate the flow which takes slightly shorter time period for flow to reach the tank bottom \( t_R = 0.19 \) to \( 0.35 \) s than that of the latter two cases of acceleration \( t_R = 0.19 \) to \( 0.36 \) s for \( f = 0.1 \) Hz; and \( = 0.18 \) to \( 0.37 \) s for \( f = 10 \) Hz).

Figure 8(A) shows the ratio of time for observing maximum flow velocity to average free fall time \( t_m/t_f \) and its associated parameters of \( t_m \) and \( t_f \) in terms of liquid filled levels. It shows that the ratio of \( t_m/t_f \) varies in the range of 1.1 to 1.2 in the entire liquid filled levels while \( t_m \) and \( t_f \) vary from 0.18 to 0.35 s (decreasing with increasing liquid filled levels) and from 0.15 to 0.32 s (also decreasing with increasing liquid filled levels), respectively. As we indicated in Figure 7(B), \( t_f \) can be predetermined, one can predict the time for observing maximum flow velocity for various liquid filled levels at the reverse gravity acceleration capable for the initiation of geyser. In comparison between impulsive acceleration with frequency of 1.0 Hz and with frequencies of 0.1 and 10 Hz, it shows that the former case of thrust can produce higher maximum flow velocity with a slightly shorter period of time \( t_m = 0.18 \) to \( 0.35 \) s than that of the latter two cases of acceleration \( t_m = 0.18 \) to \( 0.39 \) s for both \( f = 0.1 \) and \( 10 \) Hz).

Figure 8(B) shows the ratio of scale flow acceleration associated with maximum velocity to geyser initiation acceleration for corresponding geyser initiation gravity level \( a_m/a_g \) and its associated parameters of \( a_m \) and \( a_g \) in terms of liquid filled levels for impulsive acceleration with frequency of 1.0 Hz. It shows that the
The ratio of $a_m/a_g$ varies in the range of 5.7 to 6.1 in the entire liquid filled levels while $a_m$ and $a_g$ vary from 320 to 458 cm/s$^2$ (increasing with increasing liquid filled levels) and from 53.9 to 80.4 cm/s$^2$ (also increasing with increasing liquid filled levels), respectively. As $a_g$ can be predetermined from geyser initiation gravity level, one can make an approximate prediction of scale flow acceleration associated with maximum velocity, which is defined in Equation (5), at the reverse gravity acceleration capable for the initiation of geyser. In comparison between impulsive acceleration with frequency of 1.0 Hz and with frequencies of 0.1 and 10 Hz, it shows that the former case of thrust can activate higher scale flow acceleration associated with maximum flow velocity ($a_m/a_g = 5.7$ to 6.1) than that of the latter two cases of acceleration ($a_m/a_g = 4.1$ to 4.4 for $f = 0.1$ Hz; and $= 4.2$ to 4.3 for $f = 10$ Hz).

Figure (9A) shows the ratio of scale length of maximum flow velocity to average liquid height $L_m/h$ and its associated parameters of $L_m$ and $h$ in terms of liquid levels for impulsive acceleration with frequency of 1.0 Hz. It shows that the ratio of $L_m/h$ varies in the range of 14.7 to 15.9 in the entire liquid filled levels while $L_m$ and $h$ vary from 14.8 to 39.3 cm (decreasing with increasing liquid filled levels) and from 0.93 to 2.67 cm (also decreasing with increasing liquid filled levels), respectively. As $h$ can be predetermined from the geometry of liquid filled levels, one can make an approximate prediction of scale length of maximum flow velocity, which is defined in Equation (4), at the reverse gravity acceleration capable for the initiation of geyser. In comparison between impulsive acceleration
with frequency of 1.0 Hz and with frequencies of 0.1 and 10 Hz, it shows that the former case of thrust can activate larger scale length of maximum flow velocity \( \left( \frac{L_m}{h} = 14.7 \text{ to } 15.9 \right) \) than that of the latter two cases of acceleration \( \left( \frac{L_m}{h} = 12.3 \text{ to } 12.6 \text{ for } f = 0.1 \text{ Hz and } 12.1 \text{ to } 13.1 \text{ for } f = 10 \text{ Hz} \right) \).

Figure 9(B) shows the ratio of maximum flow velocity to free fall velocity from maximum liquid height \( \frac{V_m}{V_{fm}} \) and its associated parameters of \( V_m \) and \( V_{fm} \) in terms of liquid filled levels for impulsive acceleration with frequency of 1.0 Hz. It shows that the ratio of \( \frac{V_m}{V_{fm}} \) varies in the range of 5.2 to 5.8 in the entire liquid filled levels while \( V_m \) and \( V_{fm} \) vary from 82.5 to 112.2 cm/s (decreasing with increasing liquid filled levels) and from 16.4 to 19.2 cm/s (also decreasing with increasing liquid filled levels), respectively. As \( V_{fm} \) can be predetermined from geyser initiation gravity level and maximum liquid height, shown in Equation (3), one can make an approximate prediction of maximum flow velocity at the reverse gravity acceleration capable for the initiation of geyser. In comparison between impulsive acceleration with frequency of 1.0 Hz and with frequencies of 0.1 and 10 Hz, it shows that the former case of thrust can activate higher maximum flow velocity \( \left( \frac{V_m}{V_{fm}} = 5.2 \text{ to } 5.8 \right) \) than that of the latter two cases of acceleration \( \left( \frac{V_m}{V_{fm}} = 4.0 \text{ to } 4.4 \text{ for } f = 0.1 \text{ Hz; and } 3.9 \text{ to } 4.6 \text{ for } f = 10 \text{ Hz} \right) \).

As we have mentioned in Paper 19, six dimensionless parameters presented in this study show that the parameters hold near constant values through the entire ranges of liquid filled levels during the course of reorientation of liquid hydrogen activated by the reverse
gravity acceleration with impulsive thrust frequency of 1.0 Hz, which is great enough to initiate geysering flow. As the purpose of present study is to investigate an efficient propellant settling technique which is able to minimize propellant usage and weight penalties, comparison of flow parameters between impulsive acceleration with frequency of 1.0 Hz and that of 0.1 and 10 Hzs have been made toward this objective. It shows that the operation of auxiliary engine with impulsive acceleration of 1.0 Hz frequency is better than that of 0.1 and 10 Hz frequency impulsive thrust acceleration in terms of introducing a higher maximum flow velocity, a shorter time period for flow to reach maximum flow velocity, a shorter time period for flow to reach the tank bottom (tank outlet) for fluid resettling, a larger scale length of maximum flow velocity, and a higher flow acceleration associated with maximum flow velocity. It is shown that the impulsive acceleration with frequencies of 0.1 and 10 Hz can provide a higher efficient propellant resettling technique than that of the constant thrust acceleration based on same arguments mentioned earlier. It can be ranked in the order of efficiency that the impulsive acceleration with frequency of 1.0 Hz, followed by that with impulsive frequencies of 0.1 and 10 Hz which are about the same order, and then by constant thrust acceleration based on priority of selecting higher efficient propellant resettling technique.

IV. Discussion and Conclusions

The requirement to settle or to position liquid fluid over the outlet end of the spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem. Retromaneuvers
of spacecraft require settling or reorientation of the propellant prior to main engine firing. Cryogenic liquid propellant is positioned over the tank outlet by using small auxiliary thrusters (or idle-mode thrusters from the main engine) which provide a thrust parallel to the tank's major axis in the direction of flight.

The results of the study of fluid reorientation have to be evaluated in terms of how well they can be managed efficiently. An efficient propellant settling technique should minimize propellant usage and weight penalties through the operation of small thrusters (or idle-mode thrusters from the main engine). This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion.

Production of geyser during the propellant reorientation is not a desirable motion for the space fluid management under microgravity environment. It is because geyser is always accompanied by the vapor entrainment and globule formation. Geyser is observed at reverse gravity acceleration greater than certain critical values of acceleration during the course of liquid reorientation. In this paper, numerical simulation of positive liquid acquisition is attempted by introducing reverse gravity acceleration, resulting from the propulsive thrust with impulsive frequencies of 0.1, 1.0 and 10 Hz auxiliary engines, which exceeds critical value for the initiation of geyser.

Evaluation of performance is based on how efficient the
impulsive reverse gravity with various frequencies can activate following flow parameters at the same background thrust accelerations: (A) a higher maximum flow velocity, (B) a shorter time period for flow to reach maximum velocity, (C) a shorter time period for flow to reach tank bottom (tank outlet) for fluid resettling, (D) a larger length scale of maximum flow velocity, and (E) a higher flow acceleration associated with maximum flow velocity.

In summary, it is shown that impulsive reverse gravity with various frequencies is the most efficient choice for the reverse thrust to be operated at auxiliary engine for the purpose of fluid reorientation. Comparison between the results of present study for impulsive thrust with various frequencies and that of constant thrust, shown in Paper 19, it shows that impulsive thrust, regardless of frequency range, is always superior than the constant reverse thrust in terms of efficient operation of fluid reorientation.

Based on the computer simulation of flow fields during the course of fluid reorientation, six dimensionless parameters are presented both in Paper 19 and this study. It is shown that these parameters hold near constant values through the entire ranges of liquid filled levels during the course of fluid reorientation activated by the reverse gravity acceleration in both constant and impulsive thrusts great enough to initiate geyser. As the denominators of these dimensionless parameters are either predetermined from the geometry of liquid filled levels, as shown in Table 1, or can be deduced from the corresponding calculations associated with the geyser initiation gravity levels, one can predict
the values of these flow parameters. Present study can greatly enhance our understanding in the behaviors of cryogenic fluid resettlement under reduced gravity environment. This is particularly important for liquid acquisition technique to be used in on-orbit spacecraft design.

Any fluid capable of motion relative to the spacecraft will be subject to an acceleration relative to the mass center of the spacecraft that arises from the gravity gradient of the Earth\textsuperscript{14,15}. In addition to the Earth's gravitational force, the interaction between the particle mass of fluids and the spacecraft mass due to gravity gradient acceleration\textsuperscript{14} have also been taken into consideration in this microgravity fluid management study.

To conclude, we have demonstrated that, the computer algorithm presented, can be used to simulate fluid behavior in a microgravity environment, in particular the development of technology necessary for acquisition or positioning of liquid and vapor within a tank to enable liquid outflow or vapor venting through active liquid acquisition by the creation of a positive acceleration environment resulting from propulsive thrust. Better understanding of the full pictures of flow fields in both constant and impulsive thrusts, during the course of fluid reorientation can provide the proper design techniques for handling and managing the cryogenic liquid propellants to be used in on-orbit spacecraft propulsion. It is important to emphasize that impulsive reverse gravity thrust is superior to constant reverse gravity thrust for the activation of liquid necessary for the resettlement of liquid in a reduced gravity
environment. It is also worthwhile to mention that the selection of 1.0 Hz frequency impulsive thrust over the other frequency ranges is most proper based on the present study.

Acknowledgement

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Reference


7. Hung, R. J., Tsao, Y. D., Hong, B. B., and Leslie F. W., "Axisymmetric Bubble Profiles in a Slowly Rotating Helium..."


**TABLE 1** SOME BASIC GEOMETRIES AND CHARACTERISTICS
OF CRYOGENIC LIQUID HYDROGEN REORIENTATION

<table>
<thead>
<tr>
<th>Liquid Filled Level (%)</th>
<th>30</th>
<th>50</th>
<th>65</th>
<th>70</th>
<th>80</th>
</tr>
</thead>
<tbody>
<tr>
<td>Geyser Initiation Gravity-Level, $g_{i0}(10^{-2} g_0)$</td>
<td>5.5</td>
<td>6.52</td>
<td>6.6</td>
<td>6.7</td>
<td>8.2</td>
</tr>
<tr>
<td>Geyser Initiation Acceleration, $a_g$ (cm/s²)</td>
<td>53.9</td>
<td>63.9</td>
<td>64.7</td>
<td>65.7</td>
<td>80.4</td>
</tr>
<tr>
<td>Average Liquid Height, $\bar{h}$ (cm)</td>
<td>2.67</td>
<td>2.05</td>
<td>1.52</td>
<td>1.35</td>
<td>0.93</td>
</tr>
<tr>
<td>Average Free Fall Flow Velocity, $\bar{v}_f$ (cm/s)</td>
<td>17.0</td>
<td>16.2</td>
<td>14.0</td>
<td>13.3</td>
<td>12.5</td>
</tr>
<tr>
<td>Maximum Liquid Height, $h_m$ (cm)</td>
<td>3.41</td>
<td>2.79</td>
<td>2.26</td>
<td>2.09</td>
<td>1.67</td>
</tr>
<tr>
<td>Free Fall Velocity from Maximum Liquid Height $V_{fm}$ (cm/s)</td>
<td>19.2</td>
<td>18.9</td>
<td>17.1</td>
<td>16.6</td>
<td>16.4</td>
</tr>
<tr>
<td>Liquid Filled Level (Z)</td>
<td>30</td>
<td>50</td>
<td>65</td>
<td>70</td>
<td>80</td>
</tr>
<tr>
<td>-------------------------</td>
<td>----</td>
<td>----</td>
<td>----</td>
<td>----</td>
<td>----</td>
</tr>
<tr>
<td>Maximum Flow Velocity, $V_m$ (cm/s)</td>
<td>112.2</td>
<td>107.0</td>
<td>94.8</td>
<td>89.5</td>
<td>82.5</td>
</tr>
<tr>
<td>$V_m/\overline{V_f}$</td>
<td>6.6</td>
<td>6.6</td>
<td>6.7</td>
<td>6.7</td>
<td>6.6</td>
</tr>
<tr>
<td>Liquid Reaching Bottom Time, $t_R$ (s)</td>
<td>0.35</td>
<td>0.28</td>
<td>0.24</td>
<td>0.22</td>
<td>0.19</td>
</tr>
<tr>
<td>$t_R/\overline{t_f}$</td>
<td>1.1</td>
<td>1.1</td>
<td>1.1</td>
<td>1.1</td>
<td>1.2</td>
</tr>
<tr>
<td>Time for Observing Maximum Velocity, $t_m$ (s)</td>
<td>0.35</td>
<td>0.30</td>
<td>0.24</td>
<td>0.22</td>
<td>0.18</td>
</tr>
<tr>
<td>Scale Length of Maximum Flow Velocity, $L_m$ (= $V_m\cdot t_m$) (cm)</td>
<td>39.3</td>
<td>32.1</td>
<td>22.8</td>
<td>19.7</td>
<td>14.8</td>
</tr>
<tr>
<td>$L_m/\overline{H}$</td>
<td>14.7</td>
<td>15.6</td>
<td>15.0</td>
<td>14.6</td>
<td>15.9</td>
</tr>
<tr>
<td>$t_m/\overline{t_f}$</td>
<td>1.1</td>
<td>1.2</td>
<td>1.1</td>
<td>1.1</td>
<td>1.2</td>
</tr>
<tr>
<td>Scale Flow Acceleration Associated with Maximum Velocity, $a_m$ (= $V_m/t_m$) (cm/s²)</td>
<td>320</td>
<td>356</td>
<td>395</td>
<td>407</td>
<td>458</td>
</tr>
<tr>
<td>$a_m/a_g$</td>
<td>5.9</td>
<td>5.7</td>
<td>6.1</td>
<td>6.1</td>
<td>5.7</td>
</tr>
<tr>
<td>$V_m/V_{fm}$</td>
<td>5.8</td>
<td>5.7</td>
<td>5.6</td>
<td>5.6</td>
<td>5.2</td>
</tr>
</tbody>
</table>
Figure Captions

Figure 1. (A) Distribution of grid points in the radial-axial plane of cylindrical coordinate for propellant tank, and (B) Model size propellant tank adopted for numerical simulation with geometrical description.

Figure 2. Selected sequences of time evolution of fluid reorientation with liquid filled level of 30% for impulsive acceleration with frequency of 1.0 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 3. Selected sequences of time evolution of fluid reorientation with liquid filled level of 50% for impulsive acceleration with frequency of 1.0 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 4. Selected sequences of time evolution of fluid reorientation with liquid filled level of 65% for impulsive acceleration with frequency of 1.0 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 5. Selected sequences of time evolution of fluid reorientation with liquid filled level of 70% for impulsive acceleration with frequency of 1.0 Hz, (A)
initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 6. Selected sequences of time evolution of fluid reorientation with liquid filled levels of 80% for impulsive acceleration with frequency of 1.0 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 7. (A) Ratio of $V_m/V_f$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $t_r/t_f$ and its associated parameters in terms of liquid filled levels.

Figure 8. (A) Ratio of $t_m/t_f$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $a_m/a_g$ and its associated parameters in terms of liquid filled levels.

Figure 9. (A) Ratio of $L_m/h$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $V_m/V_{fm}$ and its associated parameters in terms of liquid filled levels.
A. Liquid Hydrogen and Vapor
Liquid Filled=30%  \( t = 0.00 \text{s} \)
\( g = -5.50 \times 10^2 \text{g} \)
\( f = 1.00 \times 10^8 \text{Hz} \)

B. Liquid Hydrogen and Vapor
Liquid Filled=30%  \( t = 3.00 \times 10^1 \text{s} \)
\( g = -5.50 \times 10^2 \text{g} \)
\( f = 1.00 \times 10^8 \text{Hz} \)

C. Liquid Hydrogen and Vapor
Liquid Filled=30%  \( t = 5.13 \times 10^1 \text{s} \)
\( g = -5.50 \times 10^2 \text{g} \)
\( f = 1.00 \times 10^8 \text{Hz} \)

D. Liquid Hydrogen and Vapor
Liquid Filled=30%  \( t = 9.93 \times 10^1 \text{s} \)
\( g = -5.50 \times 10^2 \text{g} \)
\( f = 1.00 \times 10^8 \text{Hz} \)
A. Liquid Hydrogen and Vapor
Liquid Filled-50% $t = 0.00\,\text{s}$
g$=-6.52\times10^2\,\text{g}$
f$= 1.00\times10^6\,\text{Hz}$

B. Liquid Hydrogen and Vapor
Liquid Filled-50% $t = 2.40\times10^1\,\text{s}$
g$=-6.52\times10^2\,\text{g}$
f$= 1.00\times10^6\,\text{Hz}$

C. Liquid Hydrogen and Vapor
Liquid Filled-50% $t = 3.22\times10^1\,\text{s}$
g$=-6.52\times10^2\,\text{g}$
f$= 1.00\times10^6\,\text{Hz}$

D. Liquid Hydrogen and Vapor
Liquid Filled-50% $t = 6.17\times10^1\,\text{s}$
g$=-6.52\times10^2\,\text{g}$
f$= 1.00\times10^6\,\text{Hz}$

Fig 3
A. Liquid Hydrogen and Vapor
Liquid Filled-70% \( t = 0.00 \) s
\( g = -7.00 \times 10^{-3} \) g,
\( f = 1.00 \times 10^6 \) Hz

B. Liquid Hydrogen and Vapor
Liquid Filled-70% \( t = 1.80 \times 10^{-1} \) s
\( g = -7.00 \times 10^{-3} \) g,
\( f = 1.00 \times 10^6 \) Hz

C. Liquid Hydrogen and Vapor
Liquid Filled-70% \( t = 3.20 \times 10^{-1} \) s
\( g = -7.00 \times 10^{-3} \) g,
\( f = 1.00 \times 10^6 \) Hz

D. Liquid Hydrogen and Vapor
Liquid Filled-70% \( t = 8.00 \times 10^{-1} \) s
\( g = -7.00 \times 10^{-3} \) g,
\( f = 1.00 \times 10^6 \) Hz

Fig 4
A. Liquid Hydrogen and Vapor
Liquid Filled-65% \( t = 0.00\) s
\( g = -6.60 \times 10^2 \) g
\( f = 1.00 \times 10^5 \) Hz

B. Liquid Hydrogen and Vapor
Liquid Filled-65% \( t = 1.80 \times 10^3 \) s
\( g = -6.60 \times 10^2 \) g
\( f = 1.00 \times 10^5 \) Hz

C. Liquid Hydrogen and Vapor
Liquid Filled-65% \( t = 3.86 \times 10^3 \) s
\( g = -6.60 \times 10^2 \) g
\( f = 1.00 \times 10^5 \) Hz

D. Liquid Hydrogen and Vapor
Liquid Filled-65% \( t = 7.46 \times 10^3 \) s
\( g = -6.60 \times 10^2 \) g
\( f = 1.00 \times 10^5 \) Hz

Fig 5
A. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 0.00 s
\( g = -8.20 \times 10^3 \) g,
\( f = 1.00 \times 10^6 \) Hz

B. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 1.80 x 10^7 s
\( g = -8.20 \times 10^3 \) g,
\( f = 1.00 \times 10^6 \) Hz

C. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 2.68 x 10^7 s
\( g = -8.20 \times 10^3 \) g,
\( f = 1.00 \times 10^6 \) Hz

D. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 8.08 x 10^7 s
\( g = -8.20 \times 10^3 \) g,
\( f = 1.00 \times 10^6 \) Hz

Fig 6
Fig 7 (A, B)
Fig 8 (A,B)
Fig 9 (A, B)
(H) Cryogenic Liquid Hydrogen Reorientation
Activated by High Frequency Impulsive
Acceleration of Geyser Initiation
Abstract

The requirement to settle or to position liquid fluid over the outlet end of spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem. Resettlement or reorientation of liquid propellant can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion for the space fluid management under microgravity environment. The purpose of present study is to investigate most efficient technique for propellant resettling through the minimization of propellant usage and weight penalties. Comparison between the constant reverse gravity acceleration and impulsive reverse gravity acceleration to be used for the activation of propellant resettlement, it shows that impulsive reverse gravity thrust is superior to constant reverse gravity thrust for liquid reorientation in a reduced gravity environment.
I. Introduction

In spacecraft design, the requirements for a settled propellant are different for tank pressurization, engine restart, venting, or propellant transfer. Prepressurization requires that heat and mass transfer effects be minimized; otherwise, a process of chill down of tank, venting of noncondensing gases, etc., may have to carry out for the cryogenic system. For engine restart, it is necessary to have the liquid settle with no bubbles near the tank outlet so that the initial flow of propellant will not carry vapor to the pump or engine. The slosh wave amplitude should be relatively low to keep the center of mass shifts within an acceptable range and wave motion low enough to avoid pressure collapse caused by interface agitation. For venting, it is probably necessary that virtually all bubbles be displaced from the bulk liquid so that a two-phase mixture is not vented. Propellant transfer requires that the liquid be completely settled with virtually no bubbles. Outflow of a liquid near the tank outlet can result in the premature ingestion of gas while a significant amount of liquid is still in the tank under microgravity environment. This phenomenon is termed "suction dip". Slosh wave motion must be minimal because the combination of "suction dip" and sloshing could cause gas pull-through to occur more readily in microgravity than if the surface were essentially quiescent.

During the prepressurization of a cryogenic propellant in microgravity, significant heat and mass transfer will occur if the liquid interface is disturbed. Interface disturbances may result from (a) impingement of the gas on the liquid surface at a mass flow
rate sufficient to cause Kelvin-Helmholtz instability, (b) globule formation from breaking waves caused by wave motion over baffles or internal hardware, (c) globule and surface froth formation resulting from movement of bubbles through the liquid to the surface, and (d) surface froth formation because of gas impingement.

Bubble and globule formation as a result of liquid impact with the aft end of the tank could lead to propellant loss for the spacecraft during venting. Globules could be entrained in the vented ullage gas or bubbles rising through the liquid and expanding because of the decreasing tank pressure could cause a spray of globules to be vented. Liquid level rise, vent liquid loss, fluid freezing, and vehicle dynamics are all affected by the microgravity levels.

A key objective of the cryogenic fluid management of spacecraft propulsion system, such as a Space Transfer Vehicle¹ (STV), is to develop the technology necessary for acquisition or positioning of liquid and vapor within a tank in reduced gravity to enable liquid outflow or vapor venting. Liquid acquisition techniques can be divided into two general categories: (1) Active liquid acquisition by the creation of a positive acceleration environment resulting from the propulsive thrust of small auxiliary engines, and (2) Passive liquid acquisition utilizing the liquid capillary forces provided by using solid baffles of liquid traps made of fine mesh screen material. In this series of study, active liquid acquisition is aimed for numerically simulating the resettlement of cryogenic liquid hydrogen. Liquid hydrogen, which, in general, poses more severe technical challenges than liquid oxygen, is used as the test bed.
working fluid in this study.

Recently Lesie\(^2\) was able to measure and to numerically compute the bubble shapes at various ratios of centrifugal force to surface tension force in 2, 4 and 6.3 cm deep cylinders in the microgravity environment. The results showed excellent agreement between model computation and measurements. Hung and Leslie\(^3\) extended Leslie's work\(^2\) to rotating free surfaces influenced by gravity with higher rotating speeds when the bubble intersects with both the top and bottom walls of the cylinder. Hung et al.\(^4,5\) further extended the work to include rotating speeds which resulted with bubbles intersecting and/or without intersecting the top, bottom and side walls of the cylinder.

An analysis of time-dependent dynamical behavior of surface tension on partially-filled rotating fluids in both low gravity and microgravity environments was carried out by numerically solving the Navier-Stokes equations subjected to the initial and the boundary conditions\(^4,6\). At the interface between the liquid and the gaseous fluids, both the kinematic surface boundary condition, and the interface stress conditions for components tangential and normal to the interface, were applied. The initial condition for the bubble profiles was adopted from steady-state formulations developed by Hung and Leslie\(^3\), and Hung et al.\(^6\) for rotating cylinder tank; and by Hung et al.\(^5,7\) for the dewar-shaped container to be used in the Gravity Probe-B Spacecraft\(^8\). Some of the steady-state formulations of bubble shapes, in particular for bubbles intersecting at the top wall of the cylinder, were compared with the experiment carried out by
Leslie\(^2\) in a free-falling aircraft (KC-135). Comparisons of time-dependent results between numerical computations and experiments were unavailable. This was because the calibration of the recordings of time-dependent gravity variations in a KC-135 aircraft during the short time periods of microgravity environment is very difficult. There was also an unavailability of accelerometer data for measuring the actual levels of microgravity during the experiment.

An efficient propellant settling technique should minimize propellant usage and weight penalties. This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion.

Production of geyser during the propellant reorientation is not a desirable motion for the space fluid management. It is because geyser is always accompanied by the vapor entrainment and globule formation. Geyser is observed at reverse gravity thrust greater than certain critical values of acceleration during the course of liquid reorientation. In other words, geyser will not be observed at very low reverse gravity level, and it will be detected when the reverse gravity level is greater than the certain critical value. In this series of study, numerical simulation of positive liquid acquisition is attempted by introducing reverse gravity acceleration, resulting from the propulsive thrust of small auxiliary engines which exceeds the critical value for geyser initiation. The reverse gravity acceleration is starting with a small value and increases gradually.
till the initiation of geyser is detected in the computer simulation for the liquid reorientation of propellant tank with various liquid-filled levels.

In this series of studies, time-dependent computations have been carried out to investigate the dynamical behavior of fluid reorientation or resettling of propellant prior to main engine firing for spacecraft restart at the net reverse gravity acceleration which is great enough to initiate geyser during the liquid reorientation. First paper of present study (Paper I)\(^9\) investigates the characteristics of fluid resettlement due to the reversal of lowest constant reverse gravity acceleration which is great enough to initiate geyser without any impulsive acceleration. The frequency of impulsive acceleration is generally termed "gravity jitters". Gravity jitters are produced by spacecraft attitude motion, machinery (turbine, pump, engine) vibrations, thruster firing, thruster shutdown, impulsive engine acceleration, etc.\(^10\) Positioning of liquid propellant over the tank outlet can be carried out by using small auxiliary thrusters which provide a thrust parallel to the tank’s major axis in the direction of flight.

Computer simulation of flow field based on Paper I\(^9\) during the course of fluid reorientation induced by constant reverse gravity acceleration show that six dimensionless parameters are obtained in the study. These parameters hold near constant values through the entire ranges of liquid filled levels during the course of fluid reorientation activated by the reverse gravity acceleration great enough to initiate geyser. As the denominators of these
dimensionless parameters are either predetermined from the geometry of liquid filled levels or can be deduced from the corresponding calculations associated with the geyser initiation gravity levels. One can predict the values of these flow parameters. These predictable parameters include maximum flow velocity $V_m$, time for observing maximum flow velocity $t_m$, time for reorienting liquid flowing down and reaching the bottom of propellant tank $t_R$, scale length of maximum flow velocity $L_m$, and scale flow acceleration associated with maximum velocity $a_m$.

Instead of applying constant reverse gravity acceleration as we described in Paper 19, this paper adopts impulsive reverse gravity acceleration with a high frequency of 10 Hz for the activation of fluid reorientation with liquid filled levels of 30, 50, 65, 70 and 80%.

II. Mathematical Model

The present study examines time-dependent fluid behaviors, in particular the dynamics of liquid hydrogen and hydrogen vapor reorientation induced by reverse gravity acceleration which is great enough to introduce geyser initiation. As in Paper 19, time-dependent axial symmetry mathematical formulation are adopted.

Consider a closed circular cylinder of radius, $a$, with length, $L$, which is partially filled with a cryogenic liquid hydrogen of constant density $\rho$ and kinematic viscosity $\nu$. Let us use cylindrical coordinates $(r, \theta, z)$, with corresponding velocity components $(u, v, w)$. The gravitational acceleration, $g$, is along the $z$-axis. For the
case of axial symmetry, the $\theta$-dependency vanishes. The governing equations are shown as follows:

(A) Continuity Equation

\[
\frac{1}{r} \frac{\partial}{\partial r} \left( r u \right) + \frac{\partial w}{\partial z} = 0 \quad (2-1)
\]

(B) Momentum Equations

\[
\begin{align*}
\frac{D}{D_{t}} u &= \frac{1}{r} \frac{\partial P}{\partial r} + u \left( \frac{\partial^2 u - \frac{u}{r^2}}{\partial r^2} \right) \quad (2-2) \\
\frac{D}{D_{t}} v &= \frac{1}{r} \frac{\partial P}{\partial r} + v \left( \frac{\partial^2 v - \frac{v}{r^2}}{\partial r^2} \right) \quad (2-3) \\
\frac{D}{D_{t}} w &= -\frac{1}{\rho} \frac{\partial P}{\partial z} - g + \nu \frac{\partial^2 w}{\partial z^2} \quad (2-4)
\end{align*}
\]

where,

\[
D = \frac{\partial}{\partial t} + u \frac{\partial}{\partial r} + w \frac{\partial}{\partial z} \quad (2-5)
\]

\[
\nabla^2 = \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial}{\partial r} \right) + \frac{\partial^2}{\partial z^2} \quad (2-6)
\]

Let the profile of the interface between gaseous and liquid fluids be given by:

\[
\eta (t, r, z) = 0, \text{ or } r = \eta(t, z) \quad (2-7)
\]

The initial condition of the profile of interface between gaseous and liquid fluids at $t = t_0$ is assigned explicitly, and is given by:

\[
\eta(t = t_0, r, z) = 0, \text{ or } r = \eta_0(z) = \eta(t_0, z) \quad (2-8)
\]

A set of boundary conditions has to be supplied for solving the
equations. These initial interface profiles used in this study have been given explicitly through the steady state computations made by Hung and Leslie\(^3\) and Hung et al\(^4\) which were checked by the experiments carried over by Leslie\(^2\). These boundary conditions are as follows:

(1) At the container wall, no-penetration and no-slip conditions assure that both the tangential and the normal components of the velocity along the solid walls will vanish. In the numerical calculation of bubble profiles for ethanol and air, a constant contact angle is present when the free surface of liquid ethanol intersects the container wall.

(2) Along the interface between the liquid and gaseous fluids, the following two conditions apply:

(a) Kinematic surface boundary condition: The liquid (or gaseous) surface moves with the liquid (or gas) which implies

\[
\begin{align*}
\frac{\partial \eta}{\partial t} + u \frac{\partial \eta}{\partial r} + w \frac{\partial \eta}{\partial z} &= 0 \\
\text{on } \eta = \eta(t = t', r, z)
\end{align*}
\]

(b) Interface stress condition: At the interface, the stress must be continuous. These can be decomposed to the components normal and tangential to the interface. For the component tangential
to the interface between liquid and gaseous fluids

\[
\begin{bmatrix}
\tau \cdot n - (n \cdot \tau \cdot n) \\
\end{bmatrix}_{\text{liquid}} = \begin{bmatrix}
\tau \cdot n - (n \cdot \tau \cdot n) \\
\end{bmatrix}_{\text{gas}} \quad (2-10)
\]

must hold. Here

\[
\tau_{ij} = \mu \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} + \frac{2}{3} \frac{\partial u_k}{\partial x_k} \delta_{ij} \right) + \mu \frac{\partial u_k}{\partial x_k} \delta_{ij}
\]

is the viscous stress tensor; \( \mu \), the viscous coefficient of the first kind; \( \gamma \), the viscous coefficient of the second kind; \( n \), the unit vector normal to the interface and \( \delta_{ij} \), the Dirac delta function. For the component normal to the interface between the liquid and gaseous fluids, the expression becomes Laplace's formula which is

\[
P_g - P_l = \frac{\sigma d}{r \ dr} \left[ \frac{r \phi}{(1 + \phi^2)^{1/2}} \right] \quad (2-11)
\]

Here \( P_l \) denotes the liquid pressure at the interface; \( P_g \), the gaseous pressure at the interface; \( \sigma \), the surface tension of the interface; and \( \phi \), the tangent of the interface which is defined by:

\[
\phi = \frac{dz}{dr} \text{ on } \eta_i = \eta(t_i, r, z) \quad (2-12)
\]

Detailed description of computational algorithm applicable to
microgravity fluid management are illustrated in Paper I\textsuperscript{9} and our earlier studies.\textsuperscript{4,6,11-13} As we have indicated in Paper I\textsuperscript{9}, for the purpose of facilitating easy comparison between computational results and experimental measurement, a model of 0.01 size prototype is adopted in the computer simulation. Model size is height $L = 4.23672$ cm and diameter $D = 4.2672$ cm. If the spacecraft had been coasting for a long time, aligned with its direction of motion, the most significant force, drag, would be axial and with acceleration of $10^{-4}g_0$ along upward direction. The hydrogen vapor is, thus, originally positioned at the bottom of the tank. The requirement to settle or to position liquid fuel over the outlet end of the spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem.\textsuperscript{11} Retromaneuvers of spacecraft, such as STV, require settling or reorientation of the propellant prior to main engine firing.\textsuperscript{1,11} Cryogenic liquid propellant shall be positioned over the tank outlet by using auxiliary thrusters (or idle-mode thrusters from the main engine) which provide a thrust parallel to the tank's major axis in the direction of flight. Similar to Paper I\textsuperscript{9}, a small value of reverse gravity acceleration (downward direction) is provided by the propulsive thrust of small auxiliary engine to initiate the reorientation of liquid propellant. This small value of reverse gravity acceleration of propulsive thrust increases gradually till reaching the critical value on which initiation of geyser is detected during the time period of fluid resettlement. We term this reverse gravity acceleration of propulsive thrust, which is capable to initiate geyser, as "geyser initiation gravity-level". 
This geyser initiation gravity level has been investigated through the method of trial and error for the various liquid-filled levels as a base to simulate impulsive reverse gravity acceleration with frequencies of 0.1, 1.0 and 10 Hz. As we have indicated in Paper I, cryogenic liquid hydrogen at temperature of 20K is considered. Hydrogen density of 0.071 g/cm³; surface tension coefficient at the interface between liquid hydrogen and hydrogen vapor of 1.9 dyne/cm; hydrogen viscosity coefficient of $1.873 \times 10^{-3}$ cm²/s; and contact angle of 0.5° are used in the computer simulation.

### III. Numerical Simulation of Liquid Hydrogen Reorientation With Geyser Initiation at High Frequency Impulsive Reverse Gravity Acceleration With Frequency of 10 Hz

In this paper, among three categories of impulsive gravity acceleration with frequencies of 0.1, 1.0 and 10 Hz, reorientation of cryogenic liquid hydrogen activated by geyser initiation impulsive reverse gravity acceleration with a high frequency of 10 Hz produced by propulsive thrust will be investigated for various liquid filled levels of propellant tank. Paper I shows that these geyser initiation gravity levels are $5.5 \times 10^{-2}$, $6.52 \times 10^{-2}$, $6.6 \times 10^{-2}$, $6.7 \times 10^{-2}$ and $8.2 \times 10^{-2}g_0$ for liquid filled levels of 30, 50, 65, 70, and 80%, respectively.

Table 1 shows some basic geometries and characteristics of cryogenic liquid hydrogen resettlement activated by reverse gravity acceleration at geyser initiation gravity level. Average liquid
height $\bar{h}$, and maximum liquid height $h_m$ are shown in Figure 1. Average free fall velocity $\bar{V}_f$, average free fall time $\bar{t}_f$, and free fall velocity from maximum liquid height $V_{fm}$ are computed from the following equations:

$$\bar{V}_f = (2g_{i0}\bar{h})^{1/2} \quad (3-1)$$
$$\bar{t}_f = \left(\frac{2\bar{h}}{g_{i0}}\right)^{1/2} \quad (3-2)$$
$$V_{fm} = (2g_{i0}h_m)^{1/2} \quad (3-3)$$

where $g_{i0}$ denotes geyser initiation reverse gravity acceleration.

To show examples of the selected sequences of time evolution of fluid reorientation for cryogenic hydrogen, Figures 2, 3, 4, 5, and 6 show time evolution of fluid reorientation activated by geyser initiation impulse reverse gravity acceleration with a frequency of 10 Hz for liquid filled levels of 30, 50, 65, 70, and 80%, respectively. Each figure contains four sub-figures. Subfigure (A) is initial profile of liquid-vapor interface at the moment of the starting of fluid reorientation at time $t = 0$; subfigure (B), the flow profile during the course of fluid reorientation before the initiation of geysering motion; subfigure (C), the flow profile with geysering motion; and subfigure (D), the flow profile after the ending of geysering motion.

Examples of selected sequences of time evolution of fluid reorientation illustrate following flow behaviors: (1) The liquid starts to flow in an annular sheet along the solid wall of tank and gradually pushes the vapor toward the central portion of the lower dome of tank as the net acceleration, reversing the direction of
gravity field, which is applied toward the downward direction of the
tank's major axis, by using small auxiliary thrusters; (2) As the
downward fluid annular sheet along the tank wall reaches the central
bottom dome side of the tank, a geysering flow is observed; and (3) The
vapor is thus pushed upward centrally into the liquid and the
geysering disappears.

Based on the computer simulation of flow field values of maximum
flow velocity \( V_m \), time for observing maximum flow velocity \( t_m \), and
time for reorienting liquid flowing down and reaching the bottom of
propellant tank \( t_R \), are obtained and illustrated in Table 2 for
reverse gravity acceleration with impulsive frequency of 10 Hz.
Scale length of maximum flow velocity \( L_m \), and scale flow acceleration
associated with maximum velocity \( a_m \), can be computed from the
following parameters:

\[
L_m = V_m t_m \\
(3-4)
\]

\[
a_m = \frac{V_m}{t_m} \\
(3-5)
\]

Following dimensionless parameters are introduced: \( \frac{V_m}{\bar{V}_f} \), \( \frac{t_R}{\bar{t}_f} \),
\( \frac{t_m}{\bar{t}_f} \), \( \frac{a_m}{a_g} \), \( \frac{L_m}{\bar{h}} \) and \( \frac{V_m}{V_{f_m}} \) where \( a_g \) stands geyser initiation
acceleration (cm/s\(^2\)) for corresponding geyser initiation gravity
level \( g_{i_0} \). Impulsive reverse gravity acceleration, \( g_i \) with
frequency \( f \) Hz is defined as follows:

\[
g_i = g_{i_0} \left(1 + \frac{1}{2} \sin 2\pi ft\right) \\
(3-6)
\]

Figures 7 to 9 show the variations of dimensionless parameters in
terms of liquid filled levels for impulsive acceleration with
frequency of 10 Hz. Denominators of these six dimensionless parameters are either predetermined from the geometry of liquid fill levels or can be deduced from the corresponding calculations associated with the geyser initiation gravity levels. Characteristics of these near constant values dimensionless parameters can provide a good understanding of the physics of microgravity fluid behaviors, in particular the active category of liquid acquisition or positioning, and also the design criteria of on-orbit spacecraft propulsion system at the critical value of reverse gravity acceleration of propulsive thrust which is capable to initiate geyser.

An efficient propellant settling technique should minimize propellant usage and weight penalties. This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion. In particular, it is important to study how well the impulsive acceleration can provide higher efficient propellant settling technique than the constant acceleration thrust technique. Also, what is the most optimal choice of impulsive frequency which can achieve the best fluid acquisition management being the goal of our research.

Figure 7(A) shows the ratio of maximum flow velocity to average free fall flow velocity $V_m/\bar{V}_f$ and its associated parameters of $V_m$ and $\bar{V}_f$ in terms of liquid filled levels for impulsive acceleration with frequency of 10 Hz. It shows that the ratio of $V_m/\bar{V}_f$ varies in the
range of 5.1 to 5.3 in the entire liquid filled levels while \( V_m \) and \( \bar{V}_f \) vary from 63.0 to 89.3 cm/s (decreasing with increasing liquid filled levels) and from 12.5 to 17.0 cm/s (also decreasing with increasing liquid filled levels), respectively. As \( \bar{V}_f \) can be predetermined from geyser initiation gravity level and average liquid height, shown in Equation (3-1), one can make an approximate prediction of maximum flow velocity during the liquid reorientation for the various liquid filled levels. In comparison for impulsive frequency acceleration and constant reverse thrust acceleration in terms of the performance of capability to induce higher maximum flow velocity to accomplish flow reorientation, it shows that impulsive frequency of 10 Hz reverse thrust is better than that of constant thrust acceleration in which the maximum flow velocity induced are in the range of 62.0 to 73 cm/s in the entire liquid filled levels.

Figure 7(B) shows the ratio of liquid reaching bottom time to average free fall time \( t_R/t_f \) and its associated parameters of \( t_R \) and \( t_f \) in terms of liquid filled levels for impulsive acceleration with frequency of 10 Hz. It shows that the ratio of \( t_R/t_f \) varies in the range of 1.1 to 1.2 in the entire liquid filled levels while \( t_R \) and \( t_f \) vary from 0.18 to 0.37 s (decreasing with increasing liquid filled levels), respectively. As \( \bar{t}_f \) can be predetermined from geyser initiation gravity level and average liquid height, shown in Equation (3-2), one can predict the time for reorienting liquid fluid flowing down from the original position and reaching the bottom of propellant tank for the various liquid filled levels at the reverse gravity acceleration capable for the initiation of geyser. In comparison for
impulsive frequency of 10 Hz reverse thrust acceleration and constant thrust acceleration, in terms of the performance of capability to induce the flow which can reach the tank bottom with a minimum time, it shows that the performance for impulsive acceleration with 10 Hz is better than that of constant thrust acceleration in which $t_R$ is in the range of 0.20 to 0.40 s for the entire liquid filled levels.

Figure 8(A) shows the ratio of time for observing maximum flow velocity to average free fall time $t_m/t_f$ and its associated parameters of $t_m$ and $t_f$ in terms of liquid filled levels. It shows that the ratio of $t_m/t_f$ is in a value of 1.2 in the entire liquid filled levels while $t_m$ and $t_f$ vary from 0.19 to 0.39 s (decreasing with increasing liquid filled levels) and form 0.15 to 0.32 s (also decreasing with increasing liquid filled levels), respectively. As we indicated in Figure 7(B), $t_f$ can be predetermined, one can predict the time for observing maximum flow velocity for various liquid filled levels at the reverse gravity acceleration capable for the initiation of geyser. In comparison for impulsive frequency of 10 Hz reverse thrust acceleration and constant thrust acceleration, in terms of performance of capability to induce maximum flow velocity in a short period of time, it shows that the performance for impulsive acceleration with 10 Hz is better than that of constant thrust acceleration in which $t_m$ is in the range of 0.20 to 0.42 s for the entire liquid filled levels.

Figure 8(B) shows the ratio of scale flow acceleration associated with maximum velocity to geyser intiation acceleration for corresponding geyser intiation gravity level $a_m/a_g$ and its associated
parameters of $a_m$ and $a_g$ in terms of liquid filled levels for impulsive acceleration with frequency of 10 Hz. It shows that the ratio of $a_m/a_g$ vary from 4.2 to 4.3 in entire liquid filled levels while $a_m$ and $a_g$ vary from 228.9 to 331.6 cm/s$^2$ (increasing with increasing liquid filled levels) and from 53.9 to 80.4 cm/s$^2$ (also increasing with increasing liquid filled levels), respectively. As $a_g$ can be predetermined from geyser initiation gravity level, one can make an approximate prediction of scale flow acceleration associated with maximum velocity, which is defined in Equation (3-5), at the reverse gravity acceleration capable for the initiation of geyser. In comparison for impulsive frequency of 10 Hz reverse thrust acceleration and constant thrust acceleration, in terms of the performance of capability to induce higher scale flow acceleration associated with maximum flow velocity, it shows that the performance for impulsive acceleration with 10 Hz is better than that of constant thrust acceleration in which $a_m$ is in the range of 175 to 310 cm/s$^2$ for the entire liquid filled levels.

Figure (9A) shows the ratio of scale length of maximum flow velocity to average liquid height $L_m/h$ and its associated parameters of $L_m$ and $h$ in terms of liquid levels for impulsive acceleration with frequency of 10 Hz. It shows that the ratio of $L_m/h$ varies in the range of 12.8 to 13.0 in the entire liquid filled levels while $L_m$ and $h$ vary from 11.9 to 34.8 cm (decreasing with increasing liquid filled levels) and from 0.93 to 2.67 cm (also decreasing with increasing liquid filled levels), respectively. As $h$ can be predetermined from the geometry of liquid filled levels, one can make an approximate
prediction of scale length of maximum flow velocity, which is defined
in Equation (3-4), at the reverse gravity acceleration capable for the
initiation of geyser. In comparison for impulsive frequency of 10 Hz
reverse thrust acceleration and constant thrust acceleration, in
terms of the performance of capability to produce larger scale length
of maximum flow velocity, it shows that the scale length produced by
impulsive acceleration with 10 Hz is longer than that of constant
thrust acceleration in which $L_m$ is in the range of 12.6 to 30.9 cm for
the entire liquid filled levels.

Figure 9 (B) shows the ratio of maximum flow velocity to free fall
velocity from maximum liquid height $V_m/V_{fm}$ and its associated
parameters of $V_m$ and $V_{fm}$ in terms of liquid filled levels for impulsive
acceleration with frequency of 10 Hz. It shows that the ratio of
$V_m/V_{fm}$ varies in the range of 3.9 to 4.6 in the entire liquid filled
levels while $V_m$ and $V_{fm}$ vary from 63.0 to 89.3 cm/s (decreasing with
increasing liquid filled levels) and from 16.4 to 19.2 cm/s (also
decreasing with increasing liquid filled levels), respectively. As
$V_{fm}$ can be predetermined from geyser initiation gravity level and
maximum liquid height, shown in Equation (3-3), one can make an
approximate prediction of maximum flow velocity at the reverse
gravity acceleration capable for the initiation of geyser. In
comparison for impulsive frequency of 10 Hz reverse thrust
acceleration and constant thrust acceleration, in terms of producing
higher maximum flow velocity, it shows that the maximum flow velocity
produced by impulsive acceleration with 10 Hz produce higher maximum
flow velocity than that of the constant thrust acceleration in which
$V_m$ is in the range of 62.0 to 73.6 cm/s for the entire liquid filled levels.

Similar to Paper 1⁹ for constant reverse gravity acceleration, six dimensionless parameters presented in this study show that the parameters hold near constant values through the entire ranges of liquid filled levels during the course of reorientation of liquid hydrogen activated by the reverse gravity acceleration with impulsive thrust frequency of 10 Hz, which is great enough to initiate geysering flow. As the purpose of present study is to investigate an efficient propellant resettling technique which is able to minimize propellant usage and weight penalties, comparison of flow parameters induced by the impulsive acceleration with frequency of 10 Hz and constant thrust acceleration toward these goals have been made. It shows that the operation of auxiliary engine with impulsive thrust acceleration of 10 Hz is better than that of the constant thrust acceleration.

IV. Discussion and Conclusions

The requirement to settle or to position liquid fluid over the outlet end of the spacecraft propellant tank prior to main engine restart poses a microgravity fluid behavior problem. Retromaneuvers of spacecraft require settling or reorientation of the propellant prior to main engine firing. Cryogenic liquid propellant is positioned over the tank outlet by using small auxiliary thrusters (or idle-mode thrusters from the main engine) which provide a thrust parallel to the tank's major axis in the direction of flight.

The results of the study of fluid reorientation have to be evaluated in terms of how well they can be managed efficiently. An
efficient propellant settling technique should minimize propellant usage and weight penalties through the operation of small thrusters (or idle-mode thrusters from the main engine). This can be accomplished by providing optimal acceleration to the spacecraft such that the propellant is reoriented over the tank outlet without any vapor entrainment, any excessive geysering, or any other undesirable fluid motion.

Production of geyser during the propellant reorientation is not a desirable motion for the space fluid management under microgravity environment. It is because geyser is always accompanied by the vapor entrainment and globule formation. Geyser is observed at reverse gravity acceleration greater than certain critical values of acceleration during the course of liquid reorientation. In this paper, numerical simulation of positive liquid acquisition is attempted by introducing reverse gravity acceleration, resulting from the propulsive thrust with high impulsive frequency of 10 Hz auxiliary engine, which exceeds critical value for the initiation of geyser.

Evaluation of performance is based on how efficient the impulsive reverse gravity with 10 Hz frequency in comparison with constant thrust acceleration can activate following flow parameters at the same background thrust accelerations: (A) a higher maximum flow velocity, (B) a shorter time period for flow to reach maximum velocity, (C) a shorter time period for flow to reach tank bottom (tank outlet) for fluid resettling, (D) a larger length scale of maximum flow velocity, and (E) a higher flow acceleration associated with
maximum flow velocity. Comparison between the results of present study for impulsive thrust with 10 Hz frequency and that of constant thrust, shown in Paper I\(^9\), it shows that impulsive thrust is superior than the constant thrust in terms of efficient operation of fluid reorientation.

Based on the computer simulation of flow fields during the course of fluid reorientation, six dimensionless parameters are presented both in Paper I\(^9\) and this study. It is shown that these parameters hold near constant values through the entire ranges of liquid filled levels during the course of fluid reorientation activated by the reverse gravity acceleration in both constant and impulsive thrusts great enough to initiate geyser. As the denominators of these dimensionless parameters are either predetermined from the geometry of liquid filled levels, as shown in Table 1, or can be deduced from the corresponding calculations associated with the geyser initiation gravity levels, one can predict the values of these flow parameters. Present study can greatly enhance our understanding in the behaviors of cryogenic fluid resettlement under reduced gravity environment. This is particularly important for liquid acquisition technique to be used in on-orbit spacecraft design.

Any fluid capable of motion relative to the spacecraft will be subject to an acceleration relative to the mass center of the spacecraft that arises from the gravity gradient of the Earth\(^14\),\(^15\). In addition to the Earth’s gravitational force, the interaction between the particle mass of fluids and the spacecraft mass due to gravity gradient acceleration\(^14\) have also been taken into
consideration in this microgravity fluid management study.

To conclude, we have demonstrated that, the computer algorithm presented, can be used to simulate fluid behavior in a microgravity environment, in particular the development of technology necessary for acquisition or positioning of liquid and vapor within a tank to enable liquid outflow or vapor venting through active liquid acquisition by the creation of a positive acceleration environment resulting from propulsive thrust. Better understanding of the full pictures of flow fields in both constant and impulsive thrusts, during the course of fluid reorientation can provide the proper design techniques for handling and managing the cryogenic liquid propellants to be used in on-orbit spacecraft propulsion. It is important to emphasize that impulsive reverse gravity thrust is superior to constant reverse gravity thrust for the activation of liquid necessary for the resettlement of liquid in a reduced gravity environment.

Acknowledgement

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Reference


### Table 1: Some Basic Geometries and Characteristics of Cryogenic Liquid Hydrogen Reorientation

<table>
<thead>
<tr>
<th>Liquid Filled Level (%)</th>
<th>30</th>
<th>50</th>
<th>65</th>
<th>70</th>
<th>80</th>
</tr>
</thead>
<tbody>
<tr>
<td>Geyser Initiation Gravity-Level, $g_{10} \times 10^{-2} g_0$</td>
<td>5.5</td>
<td>6.52</td>
<td>6.6</td>
<td>6.7</td>
<td>8.2</td>
</tr>
<tr>
<td>Geyser Initiation Acceleration, $a_g$ (cm/s²)</td>
<td>53.9</td>
<td>63.9</td>
<td>64.7</td>
<td>65.7</td>
<td>80.4</td>
</tr>
<tr>
<td>Average Liquid Height, $h$ (cm)</td>
<td>2.67</td>
<td>2.05</td>
<td>1.52</td>
<td>1.35</td>
<td>0.93</td>
</tr>
<tr>
<td>Average Free Fall Flow Velocity, $V_f$ (cm/s)</td>
<td>17.0</td>
<td>16.2</td>
<td>14.0</td>
<td>13.3</td>
<td>12.5</td>
</tr>
<tr>
<td>Maximum Liquid Height, $h_m$ (cm)</td>
<td>3.41</td>
<td>2.79</td>
<td>2.26</td>
<td>2.09</td>
<td>1.67</td>
</tr>
<tr>
<td>Free Fall Velocity from Maximum Liquid Height $V_{fm}$ (cm/s)</td>
<td>19.2</td>
<td>18.9</td>
<td>17.1</td>
<td>16.6</td>
<td>16.4</td>
</tr>
<tr>
<td>Liquid Filled Level (Z)</td>
<td>30</td>
<td>50</td>
<td>65</td>
<td>70</td>
<td>80</td>
</tr>
<tr>
<td>------------------------</td>
<td>----</td>
<td>----</td>
<td>----</td>
<td>----</td>
<td>----</td>
</tr>
<tr>
<td>Maximum Flow Velocity, ( V_m ) (cm/s)</td>
<td>89.3</td>
<td>82.6</td>
<td>74.2</td>
<td>68</td>
<td>63</td>
</tr>
<tr>
<td>( V_m / V_f )</td>
<td>5.25</td>
<td>5.1</td>
<td>5.3</td>
<td>5.1</td>
<td>5.1</td>
</tr>
<tr>
<td>Liquid Reaching Bottom Time, ( t_R ) (s)</td>
<td>0.37</td>
<td>0.29</td>
<td>0.27</td>
<td>0.23</td>
<td>0.18</td>
</tr>
<tr>
<td>( t_R / \overline{t_f} )</td>
<td>1.1</td>
<td>1.1</td>
<td>1.2</td>
<td>1.1</td>
<td>1.2</td>
</tr>
<tr>
<td>Time for Observing Maximum Velocity, ( t_m ) (s)</td>
<td>0.39</td>
<td>0.30</td>
<td>0.27</td>
<td>0.24</td>
<td>0.19</td>
</tr>
<tr>
<td>Scale Length of Maximum Flow Velocity, ( L_m ) (= ( V_m t_m )) (cm)</td>
<td>34.8</td>
<td>24.8</td>
<td>20.0</td>
<td>16.3</td>
<td>11.9</td>
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<tr>
<td>( L_m / \overline{L} )</td>
<td>13.0</td>
<td>12.1</td>
<td>13.1</td>
<td>12.1</td>
<td>12.8</td>
</tr>
<tr>
<td>( t_m / \overline{t_f} )</td>
<td>1.2</td>
<td>1.2</td>
<td>1.2</td>
<td>1.2</td>
<td>1.2</td>
</tr>
<tr>
<td>Scale Flow Acceleration Associated with Maximum Velocity, ( a_m ) (= ( V_m t_m )) (cm/s²)</td>
<td>228.9</td>
<td>274.3</td>
<td>274.8</td>
<td>283.3</td>
<td>331.6</td>
</tr>
<tr>
<td>( a_m / a_B )</td>
<td>4.2</td>
<td>4.3</td>
<td>4.2</td>
<td>4.3</td>
<td>4.2</td>
</tr>
<tr>
<td>( V_m / V_{fm} )</td>
<td>4.6</td>
<td>4.4</td>
<td>4.3</td>
<td>4.1</td>
<td>3.9</td>
</tr>
</tbody>
</table>
Figure Captions

Figure 1. (A) Distribution of grid points in the radial-axial plane of cylindrical coordinate for propellant tank, and (B) Model size propellant tank adopted for numerical simulation with geometrical description.

Figure 2. Selected sequences of time evolution of fluid reorientation with liquid filled level of 30% for impulsive acceleration with frequency of 10 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 3. Selected sequences of time evolution of fluid reorientation with liquid filled level of 50% for impulsive acceleration with frequency of 10 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 4. Selected sequences of time evolution of fluid reorientation with liquid filled level of 65% for impulsive acceleration with frequency of 10 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 5. Selected sequences of time evolution of fluid reorientation with liquid filled level of 70% for impulsive acceleration with frequency of 10 Hz; (A)
initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 6. Selected sequences of time evolution of fluid reorientation with liquid filled levels of 80% for impulsive acceleration with frequency of 10 Hz, (A) initial profile, (B) flow profile before the initiation of geyser, (C) flow profile with geyser, and (D) flow profile after the ending of geyser.

Figure 7. (A) Ratio of $V_m/V_f$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $t_m/t_f$ and its associated parameters in terms of liquid filled levels.

Figure 8. (A) Ratio of $t_m/t_f$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $a_m/a_g$ and its associated parameters in terms of liquid filled levels.

Figure 9. (A) Ratio of $L_m/h$ and its associated parameters in terms of liquid filled levels, (B) Ratio of $V_m/V_{fm}$ and its associated parameters in terms of liquid filled levels.
Fig 1
A. Liquid Hydrogen and Vapor
   Liquid Filled=30%  t = 0.00 s
   g=-5.50 x 10^{-2} g.
   f= 1.00 x 10^1 Hz

B. Liquid Hydrogen and Vapor
   Liquid Filled=30%  t = 3.60 x 10^{-1} s
   g=-5.50 x 10^{-2} g.
   f= 1.00 x 10^1 Hz

C. Liquid Hydrogen and Vapor
   Liquid Filled=30%  t = 5.20 x 10^{-1} s
   g=-5.50 x 10^{-2} g.
   f= 1.00 x 10^1 Hz

D. Liquid Hydrogen and Vapor
   Liquid Filled=30%  t = 8.80 x 10^{-1} s
   g=-5.50 x 10^{-2} g.
   f= 1.00 x 10^1 Hz

Fig 2
A. Liquid Hydrogen and Vapor
Liquid Filled=50% t=0.00s
g=-6.52\times10^{-2}g_s
f=1.00\times10^{1}Hz

B. Liquid Hydrogen and Vapor
Liquid Filled=50% t=2.40\times10^{-1}s
g=-6.52\times10^{-2}g_s
f=1.00\times10^{1}Hz

C. Liquid Hydrogen and Vapor
Liquid Filled=50% t=3.43\times10^{-1}s
g=-6.52\times10^{-2}g_s
f=1.00\times10^{1}Hz

D. Liquid Hydrogen and Vapor
Liquid Filled=50% t=5.23\times10^{-1}s
g=-6.52\times10^{-2}g_s
f=1.00\times10^{1}Hz

Fig 3
A. Liquid Hydrogen and Vapor
Liquid Filled-65% t= 0.00s
\( g=-6.60\times10^{-3} \text{g} \)
\( f=1.00\times10^3\text{Hz} \)

B. Liquid Hydrogen and Vapor
Liquid Filled-65% t= 2.40\times10^1\text{s}
\( g=-6.60\times10^{-3} \text{g} \)
\( f=1.00\times10^3\text{Hz} \)

C. Liquid Hydrogen and Vapor
Liquid Filled-65% t= 3.37\times10^1\text{s}
\( g=-6.60\times10^{-3} \text{g} \)
\( f=1.00\times10^3\text{Hz} \)

D. Liquid Hydrogen and Vapor
Liquid Filled-65% t= 7.57\times10^1\text{s}
\( g=-6.60\times10^{-3} \text{g} \)
\( f=1.00\times10^3\text{Hz} \)
A. Liquid Hydrogen and Vapor
Liquid Filled-70% t = 0.00s
g = -7.00 x 10^3 g,
f = 1.00 x 10^1 Hz

B. Liquid Hydrogen and Vapor
Liquid Filled-70% t = 1.80 x 10^1 s
g = -7.00 x 10^3 g,
f = 1.00 x 10^1 Hz

C. Liquid Hydrogen and Vapor
Liquid Filled-70% t = 3.33 x 10^1 s
g = -7.00 x 10^3 g,
f = 1.00 x 10^1 Hz

D. Liquid Hydrogen and Vapor
Liquid Filled-70% t = 8.73 x 10^1 s
g = -7.00 x 10^3 g,
f = 1.00 x 10^1 Hz

Fig 5
A. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 0.00s
$g = -8.20 \times 10^3 \, g_s$
$f = 1.00 \times 10^1 \, Hz$

B. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 1.80 \times 10^1 \, s
$g = -8.20 \times 10^3 \, g_s$
$f = 1.00 \times 10^1 \, Hz$

C. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 3.60 \times 10^1 \, s
$g = -8.20 \times 10^3 \, g_s$
$f = 1.00 \times 10^1 \, Hz$

D. Liquid Hydrogen and Vapor
Liquid Filled-80% t = 7.80 \times 10^1 \, s
$g = -8.20 \times 10^3 \, g_s$
$f = 1.00 \times 10^1 \, Hz$

Fig 6
Fig 7 (A, B)
Fig 8 (A, B)
Fig 9 (A, B)
References


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