Final Report

submitted to

NATIONAL AERONAUTICS AND SPACE ADMINISTRATION
GEORGE C. MARSHALL SPACE FLIGHT CENTER, ALABAMA 35812

September 30, 1992

for Contract NAS8 - 38609

Delivery Order 13

titled

Fingerprinting of Materials
Technical Supplement

by

Gary L. Workman Ph.D.
Principal Investigator

Materials Processing Laboratory
Center for Automation & Robotics
University of Alabama in Huntsville
Huntsville, Alabama 35899
Foreword

This supplement to the Guidelines for Maintaining and a Chemical Fingerprinting Program has been developed to assist NASA personnel, contractors, and sub-contractors in defining the technical aspects and basic concepts which can be used in chemical fingerprinting programs. This material is not meant to be totally inclusive to all chemical fingerprinting programs; but merely to present current concepts. Each program will be tailored to meet the needs of the individual organizations using chemical fingerprinting to improve their quality and reliability in the production of aerospace systems.
# Table of Contents

## 1.0 Instrumentation

1.1 Chromatography  
1.2 Spectroscopy and Spectrometry  
1.3 Microanalytical  
1.4 Surface Science  
1.5 Thermal Mechanical Techniques  
1.6 Strategy for Instrument Heirarchy

## 2.0 Chemometrics

2.1 Basic Statistics  
2.2 Design of Experiments  
2.3 Multivariate Analysis

## 3.0 References
1.0 INSTRUMENTATION

Modern instrumental analysis laboratories utilize a variety of chemical analysis instrumentation. This chapter describes the most commonly used analytical instruments, the principles behind the corresponding analytical techniques, and the applications and requirements of these techniques.

1.1. Chromatography

Chromatography is used to separate the components of a mixture. A chromatographic system consists of two mutually immiscible phases: a mobile phase which can be a gas or a liquid, and a stationary phase which is either a solid or a liquid supported on a solid within a column. The mixture is introduced into the mobile phase which flows through the stationary phase. Chemical species within the sample interact with both the mobile and stationary phases. The extent of interaction depends upon the chemical and physical properties of each component. Each component of the mixture partitions, or distributes itself between the two phases based on properties such as polarity, charge, or molecular size. With proper selection of mobile and stationary phases, the component species are gradually separated into distinct volumes or bands within the mobile phase. Separated components are eluted from the column in order of increasing interaction with the stationary phase. A detector placed at the end of the column responds to the eluted species, and its signal is plotted as a function of time. The resulting plot, called a chromatogram, consists of a series of peaks. The location of a peak along the time axis can be used to identify the component, and the area under each peak provides a quantitative measure of the component.

Chromatographic techniques can be broadly classified according to the physical state of the mobile phase (Figure 1.1). Gas chromatography (GC) refers to a technique in which the mobile phase is a gas, whereas in liquid chromatography (LC) the mobile phase is a liquid.

![Figure 1.1. Classification of Chromatographic Techniques](image)
Chromatographic methods can be further categorized according to the stationary phase's physical state or its mode of interaction with the sample. When the separation involves partitioning between a gaseous mobile phase and a liquid stationary phase, the method is called gas-liquid chromatography (GLC). In gas-solid chromatography (GSC), separation is based on size exclusion or adsorption of sample components onto the surface of a solid stationary phase. Liquid-liquid chromatography (LLC) and liquid-solid chromatography (LSC) refer to the analogous methods using liquid mobile phases. Two additional liquid chromatographic methods are commonly used. In size exclusion chromatography (SEC), species are separated based on molecular size due to differential permeation of a porous stationary phase. In ion-exchange chromatography (IEC) ionic species are separated by selective exchange of counter ions with an ion-exchange resin.

Recently, supercritical fluids have been used as chromatographic mobile phases with both liquid and solid stationary phases. Supercritical fluids exhibit properties intermediate between gases and liquids, and supercritical fluid chromatography (SFC) can be described as a hybrid of GC and LC. Although SFC has advantages over both GC and LC in certain applications, it cannot replace either method. SFC is infrequently used in industrial laboratories and will not be discussed further in this handbook.

Discussions of the kinetic processes and physical forces that comprise the theoretical basis of chromatography are beyond the scope of this handbook. However, several definitions and concepts are essential for a practical understanding of chromatographic techniques. Chromatographic separations arise from selective retention of components on the stationary phase. Retention results from interactions between the component and the stationery phase. Four modes of interaction occur in chromatography: partition, adsorption, size exclusion, and ion-exchange. In the partition mode, sample components distribute themselves between the stationary and mobile phases on the basis of the relative phase solubility of the components. Components having differing phase solubilities will spend different amounts of time in the stationary phase, and will be eluted from the column separately. Most GC and LC separations are based on partitioning. In the adsorption mode, components selectively adsorb onto the surface of the stationary phase. At one time, adsorption was the most widely used separation mode in both GC and LC. Although adsorption chromatography sometimes suffers form irreversible adsorption or peak distortion due to slow desorption, it remains the preferred approach in certain applications. In the size exclusion or sieving mode, separation is based on a component's ability to penetrate the pores of the stationary phase. Large molecules that are excluded from the pore structure are rapidly eluted from the column, whereas small molecules permeate the pore structure and remain in the column longer. Size exclusion is used in both LC and GC. Ion-exchange is based on exchange equilibria between ions in the sample solution and ions on the surface of an ion-exchange resin. This mode of separation is applicable only to LC.

Parameters used to describe chromatographic separations can be understood by examining the hypothetical chromatogram in Figure 1.2.
In this example, a sample composed of Species 1 and 2 entered the system at time zero on the chromatogram. Solvents and sample components that do not interact with the stationary phase move through the column at the velocity of the mobile phase, and are eluted from the column at time $t_M$. In this example, species 1 and 2 interact with the stationary phase, with species 2 interacting more than species 1. The retention time, $t_R$, of each component is defined as the time required for the component to elute from the column and be detected. The peak width, $W$, is obtained by drawing tangents to the sides of the peak and measuring the distance between the tangents as they intersect the baseline.

The sample is initially applied to the column as a narrow band on plug. However, as the species present in the sample move through the column and are separated, the bands broaden. Chromatographic peak shapes are similar to the normal, or Gaussian, curve.

Band broadening adversely affects the efficiency or separation capability of a chromatographic system. Band broadening in chromatography can be attributed to mass-transfer processes. One such process is eddy diffusion, which is due to the multitude of pathways a molecule or ion can follow through a packed column. Because these pathways differ in length, molecules or ions of the same species reach the end of the column at different times. A second process that can lead to band broadening is longitudinal diffusion, the migration of a molecule or ion away from the center of a band, where its concentration is highest, to regions of low concentration on the outskirts of the band. Longitudinal diffusion is more significant in gas chromatography due to the relatively high diffusion rates of species through gaseous media. Another process responsible for band broadening is stationary phase mass-transfer. For a liquid stationary phase, this involves the diffusion of a solute through the liquid stationary phase to the stationary phase/mobile phase interface where transfer to the mobile phase occurs. When the stationary phase is a solid, the stationary phase mass-transfer is controlled by the rate at which the solute is adsorbed onto or desorbed from the surface of the stationary phase.

Band broadening can often be minimized by judicious selection of experimental parameters. Improved separation efficiency can be achieved by decreasing the stationary phase particle size, by decreasing the thickness of the immobilized liquid in the case of liquid mobile phases, and by decreasing the viscosity of the mobile phase. In gas chromatography, longitudinal diffusion can be minimized by lowering the temperature of the column and mobile phase.
Three factors control the resolution or quality of a separation: efficiency, capacity, and selectivity. All can be calculated directly from the chromatogram. The efficiency of a chromatographic column is expressed in terms of \( N \), the number or theoretical plates, or \( H \), the height equivalent of a theoretical plate. These parameters are related to each other and to the column length, \( L \).

\[ L = NH \]

Column efficiency is increased as the number of theoretical plates becomes larger or as the column length increases. The number of theoretical plates can be readily calculated from two experimentally measured parameters, \( t_R \) and \( W \):

\[ N = 16 \left( \frac{t_R}{W} \right)^2 \]

Both \( N \) and \( H \) are used by column manufacturers and by analysts as a measure of a chromatographic column's performance. To compare the efficiencies of two columns, it is essential that \( N \) or \( H \) be determined with the same compound and under the same experimental conditions (mobile phase composition and flow rate, temperature, etc.). To compare columns of different length, \( H \) must be used.

The selectivity factor, \( \alpha \), is a measure of the relative retention of two components in a mixture. Selectivity can be calculated as:

\[ \alpha = \frac{t_{R,2} - t_M}{t_{R,1} - t_M} \]

where \( t_{R,2} \) is measured for the more strongly retained component. Selectivity depends on the nature of the mobile and stationary phases and temperature.

The capacity factor, \( k' \), is a measure of the time a component spends in the stationary phase compared to the time it spends in the mobile phase. This parameter is important because it is an indication of the column's ability to retain a solvent. The capacity factor can be calculated from the chromatogram:

\[ k' = \frac{t_R - t_M}{t_M} \]

Values of \( k' \) between 1.5 and 4 are desired for adequate retention and reasonable analysis times.

Efficiency, selectivity, and capacity factors together control the resolution, \( R \), between two peaks:

\[ R = \left( \frac{N^{1/2}}{4} \right) \left( \frac{a-1}{a} \right) \left( \frac{k'}{1+k'} \right) \]
Resolution can also be calculated directly from the chromatogram:

\[ R = \frac{t(R_2) - t(R_1)}{0.5 (W_2 + W_1)} \]

A resolution of 1.5 corresponds to 0.2% overlap of peak areas and is adequate for most separations. Figure 1.3 demonstrates the effect of selectivity, capacity factor, and efficiency on the resolution of the separation.

![Figure 1.3 Chromatographic Resolution](image)

Many similarities exist between GC and LC. The definitions and basic concepts discussed above apply to both techniques. In addition, all instruments used for either GC or LC include the following basic components: a mobile phase reservoir and delivery device, a sample introduction device, the chromatographic column, a detector, and a readout device. However, the types of samples analyzed by each technique, and the exact nature of the individual instrumental components required by each technique are different. Because of these differences, these techniques will now be discussed separately.

1.1.1 Gas Chromatography

Gas chromatography (GC) is used to separate thermally stable volatile substances. In GC, a vaporized sample is carried through a column by an inert carrier (mobile phase) gas. Components of the sample are separated due to differences in vapor pressure and affinity for the stationary phase. As each component is eluted from the column, its presence is sensed by a detector and a response is displayed on a recording device. The major components of a GC system are shown in Figure 1.4.
The samples are usually introduced into the system by direct injection. The sample is injected by a microsyringe through a septum into a heated sample port where it is vaporized and carried into the column. Use of automatic samplers increases precision and frees the analyst for other duties. The carrier gas must be chemically inert and pure. Helium, nitrogen, and hydrogen are the most commonly used mobile phases in GC. Because contaminants such as water or oxygen can cause deterioration of column or detector performance, purity is essential.

Two types of columns are commonly used: the packed column and the open tubular or capillary column. Packed columns can accommodate much larger sample volumes and are usually easier to use. Open tubular columns give much better resolution and are preferred for separations of complex mixtures. Packed columns are constructed from glass or metal tubing. Column inner diameters range from 1 to 10 millimeters, and lengths range from 2 to 3 meters. For gas-liquid chromatography, the columns are packed with a solid support material (125 to 250 \( \mu \text{m} \) diameter) that has been coated with an organic liquid layer immobilized by adsorption or chemical bonding. For gas-solid chromatography, the packing may be a porous organic polymer or molecular sieves. Open tubular columns are usually constructed from fused silica. These columns have an internal diameter of 0.1 to 0.5 millimeter, and a length of 10 to 100 meters. Wide-bore capillary columns made of glass have an inner diameter of 0.75 mm. The inner surface of the column is coated with a liquid stationary phase, 1 to 5 micrometers thick.

The selection of the stationary phase is a crucial step in method development. Hundreds of materials have been proposed as stationary phases for gas-liquid chromatography. The ideal stationary phase will be thermally stable, chemically inert, and non-volatile. Selection of a suitable stationary phase for a specific application is based on the selectivity and polarity of the stationary phase. Non-polar stationary phases are used to separate components having significantly different boiling points. A stationary phase that will selectively interact with one or several of the components should be selected when the mixture contains components having similar boiling points.

The most frequently used liquid stationary phases are the silicone polymers. Poly(dimethylsiloxane) is a nonpolar stationary phase used for separations of nonpolar compounds based on boiling point. By replacing some of the methyl groups with phenyl groups, slightly polar phases capable of separating olefins, aromatics, and other unsaturated
species are obtained. Replacement of the silicone's methyl groups with even more polar functionalities (such as cyanopropyl or trifluoropropyl) gives a more polar or more selective stationary phase. Most chromatographic supply catalogues offer excellent advice on the selection of stationary phases. Some common stationary phases, and their applications, are listed in Table 1.5.

Solid materials used as GC stationary phases include the molecular sieves and porous polymers. Molecular sieves are porous alkali metal aluminosilicates. Pore size is uniform and depends on the cation present. Porous polymer packings are made from styrene divinyl benzene copolymers. Molecules smaller than the pore dimension penetrate the particles and are adsorbed. Therefore, separation is based on molecular size and shape. Gases and low boiling point liquids can be separated on these solid stationary phases.

Because column temperature must be controlled to within \( \pm 1^\circ C \) for precise work, GC columns are coiled and housed in a thermostated oven. Column temperature is selected based on the boiling range of the sample. If the sample components boil over a narrow range, it may be possible to achieve the separation in a single isothermal run at a temperature near the average boiling point of the sample components. If the sample boils over a broad range, it may be necessary to use temperature programming, i.e., to continuously or incrementally increase the column temperature during the separation. The column temperature is initially set below the boiling point of the lowest boiling component. The final temperature is near the boiling point of the highest boiling component (but within the thermal limit of the stationary phase). Thermal programming shortens the retention time of the later eluting components, decreasing both the band broadening of the later peaks and the total analysis time.

The detector senses the presence of the separated components as they elute from the column. Dozens of detectors have been used for GC. The five types described below are the most frequently used. Figure 1.5 illustrates the range over which the most popular detectors are used, while a guide for detector selection is given in Figure 1.31 on page 66.

![Linear Response Range](image)

Figure 1.5. Useful ranges for Gas Chromatographic Detectors
Thermal conductivity detectors (TCD) display universal response and are rugged, relatively inexpensive, and nondestructive of sample. The TCD is based on changes in the thermal conductivity of the gas stream emerging from the GC column. The sensing element of the TCD consists of a metal block container and a filament that is electrically heated. When gas flows over the filament, heat is transported from the filament to the metal block. Heat loss from the filament results in decreased temperature and electrical resistance. Because the thermal conductivities of helium and hydrogen are six to ten times greater than those of most organic compounds, even small levels of organics in the column effluent cause large decrease changes in thermal conductivity and a marked increase in filament temperature and resistance. A change in filament resistance signals the emergence of a sample component from the column.

Flame ionization detectors (FID) display nearly universal response, high sensitivity, wide linear response range, and excellent reliability. Compared to the TCD, the FID is approximately 1000 times more sensitive, but also more complicated, more expensive, and destructive. In the FID, combustible sample components are burned in a hydrogen/air flame, generating free ions and electrons. The flame in the FID is located between two electrodes. Ions and free electrons present in the pure flame give rise to a small current when a potential is applied across the electrodes. As a carrier gas containing combustible sample components passes through the flame, additional ions and free electrons are generated and the current markedly increases. Response is proportional to the number of reduced carbons in the sample component. Oxidized carbons (present in functional groups such as carbonyl, alcohol, carboxylic acid, ether and their sulfur analogs) produce little or no response. Because the FID does not respond at all to water or to the permanent gases (N2, O2, CO, CO2, etc.), it is ideal for trace analysis in aqueous solutions and air samples.

Thermionic emission detectors (TED) respond only to compounds that contain nitrogen or phosphorus. The TED is similar to the FID except that the flame temperature and electrode polarity are optimized to enhance ionization of nitrogen and phosphorus containing compounds, and to suppress ionization of other compounds. The TED is 500 times more sensitive for nitrogen, and 50 times more sensitive for phosphorus than the FID. The TED is frequently referred to as the nitrogen-phosphorus detector (NPD).

Electron capture detectors (ECD) respond selectively to molecules containing electronegative functional groups such as halogens, nitrate, nitrite, and peroxide. The ECD also responds to unsaturated compounds such as polynuclear aromatics. In the ECD, the chromatographic effluent passes between two polarized electrodes, one of which is coated with a radioisotope that emits beta particles. The beta particles bombard the carrier gas, producing a burst of electrons and current flow between the electrodes. The presence of electron-capturing species is detected as a decrease in current.

Mass spectrometers are used as highly specific and highly sensitive GC detectors. Combined gas chromatography/mass spectrometry (GC/MS) can be used to quantitate and identify the components of a mixture. Mass spectrometers operate under high vacuum. The gas flow rates from capillary columns is usually low enough to permit direct connection between the column and the mass spectrometer. With packed columns, an interface system must be used to remove
most of the carrier gas. Two frequently used interfaces are the jet separator and the membrane separator. The jet separator takes advantage of the faster diffusion rate of the carrier gas compared to analyte. When column effluent is forced through a fine nozzle into a vacuum chamber it rapidly expands. The carrier gas expands more rapidly than the analyte. An orifice aligned with the nozzle collects the core of the effluent stream which is now enriched in analyte. The membrane separator is based on differences between the abilities of the carrier gas and analyte molecules to permeate a silicone membrane separating the column effluent from the mass spectrometer. Organic analyte molecules pass more readily through the membrane and into the mass spectrometer.

Detectors on mass spectrometers can acquire and display data in several ways. All of the ion currents can be summed and plotted as a function of time to give a total ion current chromatogram. If the analyst is interested in a particular peak the mass spectrum acquired at the time the peak passes through the detector can be plotted. The spectrum can then be used to identify the separated component.

In selective ion monitoring (SIM), the instrumental parameters are adjusted to detect only those ions associated with a particular compound or class of compounds. For example, if α-Methylstyrene were the only analyte of interest, only the 118 and 117 m/z ions would be monitored. SIM gives enhanced sensitivity because the background signal due to other ions is filtered out and because more time can be spent collecting data for the selected ions.

1.1.2 Liquid Chromatography

Liquid chromatography is used to separate mixtures of high molecular weight polyfunctional materials, polymers, thermally unstable compounds, and ionic species. Unlike GC, LC is not limited to thermally stable, volatile materials. LC and GC are complementary techniques.

Liquid chromatography was originally performed in large glass columns up to 5 m long and 5 cm diameter. To minimize mobile phase flow rates, the stationary phase particle diameters as large as 200 μm were used. Even under these conditions, separations required several hours. Attempts to shorten the analysis time by increasing the mobile phase flow rate resulted in decreased separation efficiency. In the 1960s it became possible to produce highly efficient stationary phase packings with particle diameters near 10 μm. These small diameter packings lead to the development of new instrumentation capable of operating at higher pressures. This new technology was called HPLC, high performance liquid chromatography. Except for preparative applications, HPLC has replaced classical glass-column LC.

Figure 1.6 shows the major components of a typical HPLC instrument. The components perform the following functions: delivery of the mobile phase, sample introduction, separation of the mixtures components, and detection of each component.

A liquid chromatographic separation can be performed by isocratic elution, in which a single mobile phase is used, or by gradient elution, in which two or more solvents are used in varying ratios throughout the run. For isocratic elution, the minimal mobile phase delivery system consists of a mobile phase reservoir and a pump. Gradient elution requires a reservoir and
Solvent reservoirs are constructed of glass or stainless steel. The original solvent bottle is often adequate. The mobile phase itself must be free of particulates which may cause blockages and dissolved gases which may be released as bubbles in the detector or in the pump check valves. Particulates are removed by in-line filters placed between the reservoir and the pump. Gases may be removed by sparging, sonicating, vacuum pumping, or by heating and stirring.

Pumps used for HPLC must be able to operate at pressures up to 6000 psi and to produce reproducible and constant flow rates of 0.1 to 10 mL/min. Two types of pumps are used: reciprocating piston and positive displacement. Reciprocating piston pumps are the most popular. In a piston pump, a small (30 or 400 mL) cylindrical chamber is alternately filled and emptied by the back-and-forth motion of a motor-driven piston. Flow direction is controlled by means of check valves. On the backward stroke, the piston pulls solvent from the external mobile phase reservoir. On the forward stroke, mobile phase is pumped to the column. Because no solvent is pumped to the column on the backward stroke, the flow is pulsed, and a pulse damping system should be used. Dual-head (or triple head) pumps consist of two (or three) pistons mechanically coupled so that pumping and filling occur simultaneously. Flow pulsations are greatly reduced, but not eliminated, in the dual head and triple-head pumps. Advantages of reciprocating pumps include unrestricted operating time due to the use of an external reservoir and rapid solvent change over due to the pump's small internal volume. Positive displacement, or syringe, pumps consist of a large (250 to 500 mL) solvent reservoir equipped with a plunger. A stepping motor actuates the plunger through a screw-driven mechanism. Displacement pumps produce a pulse-free flow. However, it suffers from limited solvent capacity, requiring periodic shut-down of the system for refilling.

Two types of gradient mixing devices are used: low-pressure and high-pressure. In a low-pressure system, the gradient is formed ahead of the high pressure pump. A system of proportioning valves accurately measure and deliver up to four solvents to a low volume mixing chamber. In a high pressure system, mixing of the solvents occurs after the pumps. High pressure systems are more costly because they require a separate pump for each solvent used in the gradient. However, they provide more precise control over the gradient composition. In
both types of gradient systems, changes in the mobile phase composition are controlled by a
gradient programmer. Both continuous and step gradients are used. Because the mixing
process can generate heat which can result in gas evolution thorough degassing of each mobile
phase is essential.

The most widely used sample introduction devices are sampling valves. These devices permit
sample introduction at high pressure with minimal interruption of mobile phase flow. Typical
valves can deliver 10 to 500 μL with a few tenths percent precision. Automatic samplers
available for HPLC allow unattended operation of the equipment.

HPLC columns are constructed of smooth-bore stainless steel tubing or glass-lined metal
tubing. Several types of analytical columns are used: standard, short, and narrow bore.
Standard columns are 20 to 30 cm in length with an inner diameter of 4 to 5 mm and stationary
phase particle size of 3 to 10 μm. Short columns that are 3 to 6 cm long and packed with 3 μm
particles give good separations with increased sample throughput and minimal solvent
consumption. These columns are useful for relatively easy separations (N ~ 4000) when speed
is essential as in quality control applications. Narrow-bore (or microbore) columns have small
internal diameters, usually 1 to 2 mm. Narrow-bore columns offer several advantages including
decreased solvent consumption and increased detector response. Disadvantages include a
requirement of special low volume injection valves, detector cells, and pumps.

Guard columns are sometimes placed between the injection valve and the analytical column.
Guard columns are short and packed with a stationary phase similar to that used in the
analytical column, but of larger particle size. Guard columns protect the analytical column by
trapping particulates and sample components that would be permanently retained on the
analytical column.

As mentioned before, there are four modes of liquid chromatography: liquid-liquid (partition),
liquid-solid (adsorption), ion exchange, and size exclusion. Each mode is applicable to
different types of samples and each mode makes use of different types of stationary phases.
Liquid chromatographic techniques are also categorized on the basis of the relative polarities of
the stationary and mobile phases. In normal-phase chromatography, a polar stationary phase is
used with a nonpolar mobile phase. In reverse-phase chromatography, the stationary phase is
less polar than the mobile phase.

Column packings used for partition chromatography are of two types. In the liquid-coated type,
the liquid stationary phase is held on the solid support particles by adsorption. In bonded-phase
packings, the stationary phase is covalently bonded to the support particles. Bonded-phase
packings have almost completely replaced the liquid-coating packings due to their greater
stability. Bonded phase packings are based on rigid silica particles. The organic stationary
phase is bonded to the silica surface through a siloxane linkage:

\[ -\text{Si-O-} \text{Si-R} \]

where R is an organic group. The polarity and selectivity of the stationary phase can be
controlled by varying the organic group. In the most popular bonded phase packings, the alkyl group is an \( \eta \)-octyl (C₈), or an \( \eta \)-octadecyl (C₁₈) group. Both are nonpolar, however, the size of the alkyl group affects retention. The C₈ packing will accomplish the separation faster, but the C₁₈ phase can be used with larger sample sizes. Bonded phases containing phenyl groups are also nonpolar, but more selectivity interact with aromatic and unsaturated hydrocarbons. Phases that contain cyano groups are moderately polar and are used to separate ethers, esters, ketones, aldehydes, and nitro compounds. Amino alkyl bonded phase are highly polar, and are useful in separations involving alcohols, phenols, carbohydrates, and amines.

Column packings used for liquid-solid chromatography are composed of silica, alumina, or carbon. Silica packings are the most frequently used. LSC is primarily used separate nonpolar, water-soluble molecules. LSC can also be used to separate isomeric mixtures.

Size exclusion packings are composed of cross-linked polymers or porous glass or silica. Styrene-divinylbenzene copolymers are frequently used.

In packings used for ion chromatography, a monolayer of small (0.1 to 0.3 \( \mu \)m) polymeric beads are aminated or sulfonated and electrostatically bonded to a relatively large (10 to 30 \( \mu \)m) polymeric or glass bead. The aminated resins are used to separate anions, while the sulfonated material are used for cations.

Liquid chromatography has no detector as sensitive and as universally applicable as the FID and TCD detectors used in gas chromatography. The most commonly used HPLC detectors and their properties are listed in Table 1.1.

<table>
<thead>
<tr>
<th>Detector</th>
<th>Type</th>
<th>Sensitivity (g/mL)</th>
<th>Linearity</th>
</tr>
</thead>
<tbody>
<tr>
<td>UV-Visible absorption</td>
<td>selective</td>
<td>(10^{-10})</td>
<td>(10^5)</td>
</tr>
<tr>
<td>Refractive index</td>
<td>universal</td>
<td>(10^{-7})</td>
<td>(10^4)</td>
</tr>
<tr>
<td>Fluorometric</td>
<td>selective</td>
<td>(10^{-11})</td>
<td>(10^5)</td>
</tr>
<tr>
<td>Amperometric</td>
<td>selective</td>
<td>(10^{-12})</td>
<td>(10^5)</td>
</tr>
<tr>
<td>Conductometric</td>
<td>selective</td>
<td>(10^{-8})</td>
<td>(10^3)</td>
</tr>
</tbody>
</table>

Table 1.1 HPLC Detectors

UV-visible absorption detectors are based on the absorption of ultraviolet or visible radiation by components as they pass out of the column. Three types of UV-visible detectors are available: fixed-wavelength, variable-wavelength, and photodiode-array. Fixed-wavelength detectors use discrete light sources which emit light at several wavelengths. Each wavelength can be selected by use of narrow bandpass filters. A fixed-wavelength detector with a mercury lamp as the source has useful emission lines at 254, 280, 313, 334, and 365 nm. These detectors are simple, stable, sensitive, and inexpensive. However, only the solutes that absorb at the given wavelengths will be detected. Variable wavelength detectors use continuous light sources in combination with a monochromator. These detectors offer unlimited selection of UV and visible wavelengths. Photodiode array detectors consist of a continuous light source, a monochromator, and silicon diode array detector. These detectors simultaneously monitor all
wavelengths. An entire spectrum can be collected and stored as each separated species passes out of the column. Photodiode array detectors are especially useful during the development of a new LC method because they help the analyst identify the optimal detector wavelength. UV visible detectors are selective in that they respond only to species that absorb ultraviolet or visible radiation. Detectable species include the unsaturated hydrocarbons, including aromatics, and compounds that contain atoms such as nitrogen, oxygen, sulfur, and halogen.

Refractive index (RI) detectors are based on difference in refractive index between the mobile phase (reference) and the column eluent. Because most substances differ in refractive index, the refractive index detector is universal in response. However, this detector is not very sensitive and is seldom useful for trace-level components. Its universal response usually precludes its use in gradient elution procedures where the changing mobile phase composition results in drifting baselines. Refractive index detectors are extremely sensitive to temperature changes and flow rate fluctuations.

Fluorometric detectors respond to the fluorescent emission of molecules that have been electronically excited by a suitable source. Fluorometric detectors are more selective and more sensitive than UV-visible absorption detectors. The detector's selectivity is due to the fact that not all molecule fluoresce. Compounds that can be detected include pollutants such as the polynuclear aromatics and biologically significant species such as vitamins, alkaloids, and catecholamines. The extreme sensitivity of fluorometric detectors results from a low background level of fluorescence. This detector can be used with gradient elution.

Amperometric detectors are based on the measurement of current flow as analytes in the eluent undergo oxidation or reduction at an electrode. Typical amperometric detector cells have a three-electrode arrangement consisting of a working electrode (which detects the analyte), an inert reference electrode, and an auxiliary electrode. A potential is applied between the working and reference electrodes, while current flows between the working and auxiliary electrodes. The working electrode composition is important because it determines the range of potentials that can be applied and, therefore, the species that can be detected. Dual electrode detector cells have two working electrodes which can be placed in series or in parallel with the flowing eluent. In the series configuration, the upstream electrode produces an electrochemically active product that can be detected at the downstream electrode. This approach enhances the selectivity of the detector, and also enhances sensitivity by reducing background noise due to mobile phase electrolysis. In the parallel configuration, the two working electrodes are held at different potentials. The ratio of currents measured at the two electrodes provides an indication of the peaks purity and identity. Amperometric detectors are more sensitive and more selective than UV-visible and RI detectors. Amperometric detection is widely applicable. However, amperometric detectors are not widely used due to several disadvantages. Amperometric detectors adversely respond to fluctuations in eluent flow rate. Many compounds adsorb onto the electrodes, requiring frequent and time-consuming cleaning and recalibration. Operation in the reductive mode may require exclusion of oxygen from the system and the use of mercury electrodes.

Conductivity detectors measure the ability of the eluent to carry an electric current under the influence of a potential gradient. These detectors respond to species that form ions in solution
(electrolytes). Conductivity detectors are used with ion chromatography.

The mobile phases used in ion chromatography are ionic solutions which produce a high background conductivity. To detect analytes, the eluent conductivity must be suppressed. Membrane suppressors are used for anion (and cation) exchange separations. The eluent is passed over one side of a cation (or anion) exchange membrane. The membrane is continuously regenerated by flowing an acidic (or basic) solution over the other side of the membrane.

Mass spectrometer detectors provide both structural and quantitative information. Interfacing liquid chromatography with mass spectrometry has been difficult because of the mismatch between the large mass flow rates used in liquid chromatography and the vacuum requirements of mass spectrometry. Several interfaces have been developed. In the moving-belt interface, the column effluent is deposited on a continuous moving belt. The belt moves through a heated chamber, where the solvent is evaporated, and into the ion source of the spectrometer. In the thermospray interface, the column effluent is passed through a heated capillary tube to produce an aerosol of solvent vapor and analyte molecules. When polar mobile phases containing a salt (such as ammonium acetate) are used, the analyte can be ionized through charge exchange with the salt. When nonpolar or weakly ionizable mobile phases are used, an electron beam is used to achieve ionization.
1.2. Spectroscopy and Spectrometry

This section introduces the fundamental principles of spectroscopy, and describes specific instrumental methods based on these principles. Absorption, emission, or scattering of electromagnetic radiation alters the energy state of the interacting atom or molecule. Because each chemical species has characteristic energy states, a species interacts only with a particular region or energy range of the electromagnetic spectrum. The energy at which interaction occurs can be used to identify the interacting species, and the intensity of the interaction can be used to quantify its concentration.

Spectroscopic methods are based on absorption, emission, or scattering of electromagnetic radiation by matter. Electromagnetic radiation is a form of energy that is transmitted through space at the speed of light \( (3 \times 10^8 \text{ m/s}) \). Electromagnetic radiation can be described in terms of a wave model. An electromagnetic wave consists of electrical and magnetic field components which oscillate in planes perpendicular to each other and to the direction of wave propagation. The electrical field component of electromagnetic radiation is responsible for most of its interactions with matter. Figure 1.7 depicts the electrical field component and illustrates several parameters used to characterize electromagnetic radiation.

![Electromagnetic Wave](image)

**Figure 1.7. Electromagnetic Wave**

The wavelength, \( \lambda \), is the distance between successive maxima or minima of either the electrical or magnetic component. The frequency, \( \nu \), is the number of waves that pass a fixed point in a unit of time, usually a second. Frequency is determined by the source of the radiation and remains unchanged by propagation of the wave through matter. The velocity of propagation, \( v \), is the rate at which the wave passes through a medium. The velocity of electromagnetic radiation in a vacuum, \( c \), is \( 3 \times 10^8 \text{ m/s} \). Due to interactions between the electric field component and matter, electromagnetic radiation is propagated or transmitted through matter at velocities less than \( c \). The ratio of the speed of light in a vacuum to the speed of light in a medium is the refractive index \( n \) of the medium. Because the frequency is invariant, the wavelength must also decrease as radiation...
passes from a vacuum to another medium. The wavenumber, \( \bar{\nu} \), in units of cm\(^{-1}\) is the number of wave crests that occur per centimeter. Wavenumbers are often used instead of frequency, and can be calculated as:

\[
\bar{\nu} = \frac{1}{\lambda} \quad \text{or} \quad \bar{\nu} = \frac{v}{c}
\]

The radiant power, \( P \), is the amount of energy transmitted per second and is proportional to the square of the wave amplitude, \( A \).

Refraction, diffraction, and interference are phenomena that can readily be explained by the wave model. However, absorption and emission of electromagnetic radiation by matter can be described only by treating radiation as a stream of discrete particles or quanta of energy known as photons. The energy of a photon depends upon the frequency of the radiation, and is given by:

\[
E = h\nu
\]

where \( E \) is in joules, and \( h \) is Plank's constant \((6.62 \times 10^{-34} \text{ J sec})\).

The quantum model is needed to describe photoionization, the emission of electrons from the surface of a solid when a sufficiently energetic radiation impinges on the surface. The energy of the emitted electrons is related to the frequency of incident radiation:

\[
E = h\nu - w
\]

where the work function, \( w \), of the solid is the work required to remove an electron. The number of emitted electrons is dependent on the number of impinging quanta of radiation having a certain minimum energy.

Figure 1.8 on the next page depicts the electromagnetic spectrum, the broad range of radiations that extend from gamma rays to radio waves. The various types of electromagnetic radiation differ in frequency, wavelength, and nature of interaction with chemical species.
Low-energy radio waves cause reorientation of nuclear spin states in materials placed in a magnetic field. Photons in the microwave region cause changes in rotational energy states of molecules. Absorption of infrared radiation results in changes in both vibrational and rotational energy states of molecules and complex ions. Absorption of visible or ultraviolet radiation changes the energy states of outer shell (valence) electrons. X-ray absorption results in ejection of inner shell (core) electrons (the photoelectron effect). These interactions of electromagnetic radiation with chemical species will be described in more detail in the following pages.

When electromagnetic radiation passes through a sample of matter, select frequencies may be transferred to the sample's atoms and molecules by the process of absorption. As a result, the absorbing species are promoted from a low energy state to a higher energy state, or excited state. Most chemical species at room temperature are in the lowest energy state, a ground state. Absorption, then, usually involves a transition from the ground state to an excited state. An atom or molecule in an excited state may return to the ground state by emission, the release of energy as radiation.

According to quantum theory, atoms and molecules exist only in a limited number of discrete potential energy levels. The energy of the impinging photon must match the energy difference between the ground state and an excited state of the absorbing particle for absorption to occur. Similarly, energy lost by emission of radiation must match the energy difference between an excited state and the ground state, or between two excited states. Because these energy differences are unique for each atom or molecule, the energies (frequencies) at which a species absorbs or emits radiation can be used to identify the species.

Absorption or emission of radiation is accompanied by transition of electrons between fixed energy levels. Ultraviolet and visible radiation are sufficiently energetic to cause transitions of outer shell or valence electrons. Absorption or emission of x-rays leads to transition of inner shell, or core, electrons.

Molecular spectra are more complex than atomic spectra due to an increased
number of energy states available. The potential energy of a molecule is the sum of the electronic, vibrational, and rotational energies. Normally, several rotational energy states exist for each vibrational energy state, and several vibrational states exist for each electronic state. The schematic energy level diagram in Figure 1.9 shows some of the electronic and vibrational states of a molecule. Lines labelled $E_n$ represent electronic energy states. $E_0$ refers to the electronic ground state, $E_1$ and $E_2$ refer to first and second electronic excited states. Several vibrational energy levels (labelled $v_0$ to $v_3$) are pictured for each electronic state. The energy differences between adjacent electronic states is $10$ to $100$ times greater than the energy differences between adjacent vibrational states. The figure also illustrates two analytically useful processes, absorption and fluorescence.

![Figure 1.9. Molecular Energy Levels](image)

1.2.1 Atomic Spectroscopy

Atomic spectroscopy is used to determine the concentration of a particular element in a sample, regardless of the chemical environment and oxidation state of the element. Atomic spectroscopic methods are listed in Table 1.2. In each method, the molecular components of the sample are converted to free atoms by the process of atomization. In atomic emission spectroscopy (AES), absorption of additional thermal energy from the atomization device transforms the free atoms to excited electronic states. As the excited atoms return to the ground state, they emit ultraviolet or visible
radiation at wavelengths characteristic of the atoms present in the sample. The intensity of the emitted radiation is measured, and is the basis of the analytical determination. In atomic absorption spectroscopy (AAS), the atoms are transformed to excited states by absorption of radiant energy from an external ultraviolet/visible light source. The analytical determination is based on the amount of radiant energy absorbed. In atomic fluorescence spectroscopy (AFS), the atoms are excited by a radiation source placed at 90° to the optical axis of the spectrometer. Quantitation is based on the intensity of radiation emitted as fluorescence. The basic components of instruments used for AES, AAS, and AFS are compared in Figure 1.10. All instruments used for atomic spectroscopy include an atomization device, a monochromator to resolve the emitted or transmitted light into its component wavelengths, and a detector for ultraviolet/visible radiation. Atomic spectroscopic instruments differ primarily in atomizer type, the absence or presence of an external light source, and orientation of the components.

![Diagram of atomic spectroscopy instruments](image)

Figure 1.10. Instruments for Atomic Spectroscopy
Atomic spectroscopic methods are frequently classified according to atomizer type. The most commonly used atomizers are the combustion flame, the electrothermal analyzer, and the plasma. Flame atomizers are used for AES, AAS, and AFS. Electrothermal atomizers are primarily used for AAS and AFS, whereas plasma sources are used for AES and AFS.

<table>
<thead>
<tr>
<th>Technique (Abbreviation)</th>
<th>Atomization Source (Temperature)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Flame atomic absorption spectroscopy (FAAS)</td>
<td>Flame (1700-3200°C)</td>
</tr>
<tr>
<td>Electrothermal atomic absorption spectroscopy</td>
<td>Furnace (1200-3000°C)</td>
</tr>
<tr>
<td>Flame emission spectroscopy (FES)</td>
<td>Flame (1700-3200°C)</td>
</tr>
<tr>
<td>Inductively coupled plasma atomic emission spectroscopy (ICP/AES)</td>
<td>Argon plasma (6000-8000°C)</td>
</tr>
<tr>
<td>Direct current argon plasma spectroscopy (DCP)</td>
<td>Argon plasma (6000-10000°C)</td>
</tr>
<tr>
<td>Arc-source emission spectroscopy</td>
<td>Arc plasma (4000-6000°C)</td>
</tr>
<tr>
<td>Spark-source emission spectroscopy</td>
<td>Spark plasma</td>
</tr>
<tr>
<td>Atomic fluorescence spectroscopy (AFS)</td>
<td>Flame (1700-3200°C)</td>
</tr>
<tr>
<td>Electrothermal atomic fluorescence spectroscopy</td>
<td>Furnace (1200-3000°C)</td>
</tr>
<tr>
<td>Inductively coupled plasma atomic fluorescence spectroscopy (ICP/AFS)</td>
<td>Plasma (6000-8000°C)</td>
</tr>
</tbody>
</table>

Table 1.2 Atomic Spectroscopy Methods

In the following section, the atomic spectroscopic techniques most commonly used will be discussed. These techniques are: flame atomic absorption spectroscopy, electrothermal atomic absorption spectroscopy, and inductively coupled plasma/atomic emission spectroscopy.

1.2.2 Flame and Electrothermal Atomic Absorption Spectroscopy

Atomic absorption spectroscopy is a sensitive technique for the quantitative determination of approximately seventy metallic or metalloid elements in solution matrices. The basic instrumental components were shown above in Figure 1.10.
Electrothermal and flame atomizers are used in atomic absorption instruments. Flame atomizers consist of a nebulizer and a burner. The nebulizer transforms the liquid sample into an aerosol which is introduced into the burner. Figure 1.11 illustrates the two main types of burners: the total consumption (turbulent flow) and laminar flow burners.

![Diagram of atomizers for Atomic Absorption Spectroscopy](image)

Figure 1.11. Atomizers for Atomic Absorption Spectroscopy

In the total consumption burner, the nebulizer and burner are combined into a single unit. The oxidant flow around the sample capillary tip draws the sample up the capillary and into the burner. Fuel gas mixes with the oxidant and the sample, and helps to break up the sample. The flame forms at the top of the burner. Total consumption burners offer several advantages over laminar flow burners: (1) the entire sample is aspirated into the flame, eliminating error due to loss of nonvolatile components, (2) no possibility of flashback or explosion exists (see discussion of laminar flow burner, below), and (3) the burner is inexpensive and easy to maintain. Disadvantages include: (1) vaporization and atomization efficiency are low, (2) operators must take special precautions to prevent clogging of the tip, (3) short flame path length results in decreased signal in AAS, and (4) total consumption burners are very noisy, both electronically and aurally due to turbulence.

In the laminar flow burner, the sample is drawn into a mixing chamber and nebulized by the flow of oxidant across the capillary tip. A series of baffles in the mixing chamber remove larger droplets from the sample stream. The remaining aerosol mixes with additional oxidant and fuel, and passes into the burner head and the flame. Laminar flow burners offer several advantages: (1) sensitivity is greater due to relatively long path length (5-10 cm), (2) burner is quiet, and (3) because larger drops are eliminated in the premix chamber, laminar flow burners seldom clog. Disadvantages are: (1) in samples containing more than one solvent, the more volatile components
may be preferentially vaporized in the mixing chamber, while less volatile components may drain off and not reach the flame (2) the mixing chamber contains an explosive mixture which can be ignited by a flashback, and (3) most of the sample goes down the drain.

Conversion of the sample to free atoms in the flame involves a sequence of events. The sample enters the flame as a solution aerosol. The solvent evaporates or, in the case of an organic solvent, burns, leaving behind a solid aerosol. The solid particles undergo volatilization, and then dissociation to form free atoms. These atoms are then excited by radiant energy from a uv-visible light source. Atomization efficiency is the efficiency with which the flame produces atoms by this sequence of events. Several processes can decrease atomization efficiency and, therefore, the analytical response. If the sample drops are too large, they may pass through the flame without completely evaporating. Droplet size can change significantly with a change in solvent due to viscosity differences. The rate at which the sample is introduced into the flame also effects atomization efficiency because solvent evaporation requires energy and lowers flame temperature.

Flame atomization surpasses other atomization methods in terms of reproducibility. However, sampling efficiency of the flame is low because much of the sample is discarded (in case of the laminar flow burner) or incompletely atomized (in the case of the total consumption burner), and the residence time of the analyte atoms in the optical path of the flame is short. The sampling efficiency and, therefore, sensitivity of other atomization methods is better.

Electrothermal atomizers provide high sensitivity because the entire sample is atomized quickly and the residence time in the optical path is on the order of seconds. Compared to flame atomization, electrothermal atomization enhances sensitivity by factor of 100 to 4000. Electrothermal atomizers can accommodate very small sample volumes (0.5 - 100 \text{L}) and solid samples. Electrothermal atomizers are electronically less noisy than flames. However, the precision of electrothermal methods, typically 5 to 10\%, compares unfavorably with the 1 to 2\% precision obtained with the flame methods.

An excitation source that emits light having an energy equal to the difference in energies between the ground state and excited state of the element being analyzed is used. Hollow cathode lamps are the most common excitation sources for AAS. Hollow cathode lamps consist of a cylindrical cathode constructed of the element being analyzed, and a tungsten anode, both sealed in a glass tube filled with an inert gas. When a sufficiently large potential is applied across the electrodes, the inert gas ionizes, forming highly energetic cations. As these cations strike the cathode's surface, atoms on the surface are dislodged. Some of the metal atoms are in excited electronic states and emit lines of radiation characteristic of the cathode element as they return to the ground state. Usually, a different lamp must be used for each element, although some multielement lamps are available. The source emission is directed through the atomized sample in the flame or furnace. The light not absorbed by the sample passes through to
the monochromator and the detector. The absorbance is calculated from the intensities of light detected with \( I \) and without \( I_0 \) the analyte in the flame:

\[
A = \log \left( \frac{I_0}{I} \right)
\]

To absorb the source radiation, an atom in the flame must be of the same element used in the source lamp. Therefore, the absorbance is element-specific. The absorbance is also directly proportional to the analyte's concentration.

1.2.3 Inductively Coupled Plasma/Atomic Emission Spectroscopy

Inductively coupled plasma/atomic emission spectroscopy is used for the qualitative and quantitative analysis for over seventy elements in solution. ICP/AES is capable of multi-element analysis, performed in either a simultaneous or rapid sequential mode. This technique is used for determination of major, minor and trace level elements.

In ICP/AES the sample is atomized by an argon plasma sustained by inductive coupling to an \( rF \) (radio frequency) field. An ICP torch consists of three concentric quartz tubes as shown in Figure 1.12. An induction coil, powered by an \( rF \) generator, circles the top of the tube assembly. Argon flowing between the two inner tubes is initially ionized by a spark form a Tesla coil. An annular plasma forms when the resulting ions and electrons interact with the oscillating magnetic field generated by the induction coils. The analyte is introduced as an aerosol through the central tube. A gas (usually argon) flows tangentially between the two outer tubes to contain the plasma and to cool the quartz cylinder walls.
Samples are usually introduced into the plasma as a solution aerosol generated by a pneumatic nebulizer. The most commonly used pneumatic nebulizers are the concentric (or Meinhard) nebulizer and the crossflow nebulizer. In both types, the sample is drawn through a capillary into a low pressure region generated by the flow of a gas past the capillary tip. The aerosol produced in the nebulizer passes through a spray chamber, which removes or breaks up the larger droplets, and into the ICP torch.

When the sample is introduced into the plasma it is atomized and elevated to an excited state as a result of collisions with the argon ions. The excited analyte atoms relax to their ground state by emitting photons. The emitted radiation is dispersed by either a polychromator, for simultaneous multi-element analysis, or by a scanning monochromator, for sequential multi-element analysis.

In the polychromator, the emitted light is focused onto a concave grating where it is dispersed into its component wavelengths. Selected spectral lines are isolated by a series of exit slits. Each line is focused onto a detection device, a photomultiplier tube. The polychromator permits the simultaneous detection of up to 60 spectral lines (corresponding to 60 elements). Simultaneous multi-element analysis is especially useful in applications involving routine analyses of large numbers of samples having similar elemental composition. In the scanning monochromator, a lens focuses the emitted light onto a concave mirror, which collimates the light onto a planar grating.
mounted on a computer-controlled stepper motor. The grating disperses the light, and a final mirror focuses the light onto an exit slit before the detector. The wavelength is selected by rotating the grating. Only one wavelength can be detected at a given time. For multi-element analysis, the grating must be driven in a sequential manner to a position corresponding to the appropriate analytical wavelength for each element to be measured. The scanning monochromator is more flexible than the polychromator because it offers a greater choice of analytical wavelengths. This is an advantage in the development of new methods, or in laboratories where samples vary widely in elemental composition.

1.2.4 X-ray Fluorescence Spectroscopy

X-ray fluorescence (XRF) spectroscopy is used for qualitative and quantitative multi-element analysis. XRF can qualitatively identify all elements of atomic number greater than eleven, and quantitatively measure all elements of atomic number greater than fourteen present within a sample at the parts-per-million (ppm) or greater level. This technique is extremely useful because it is readily applicable to most solid and liquid samples with minimal sample preparation.

XRF is based on the emission of characteristic x-ray lines by atoms following excitation by high energy photons from an x-ray source. The most commonly used x-ray source is the x-ray tube which consists of a tungsten filament cathode and a target anode, both sealed within a highly evacuated tube. Electrons are thermally emitted from the cathode when the filament is heated. These electrons are then accelerated across a high potential gradient to the target anode. Target materials include copper, molybdenum, iron, chromium, nickel, silver, and tungsten. X-rays are produced by bombardment of the target material. X-rays emitted by the source are then directed onto the sample. Upon absorption of the x-radiation, atoms within the sample become electronically excited. The excited atoms relax to their ground states by fluorescent emission of x-rays of characteristic energy. Sample fluorescence is collimated, and then dispersed by a crystal mounted on a goniometer. The goniometer permits control of the angle ϑ between the incident collimated radiation and the crystal face. The collimated x-rays are diffracted from lattice planes within the crystal. The value at which a given wavelength λ is diffracted is given by Bragg's law, nλ = 2d sin ϑ, where d is the lattice spacing of the crystal. X-rays diffracted by the analyzing crystal are detected by gas-filled detectors or by scintillation counters.

Compared to ICP/AES and AA, XRF is more rapid and more readily applicable to various samples. However, ICP/AES and AA are more sensitive than XRF.

1.2.5 Infrared Spectroscopy

Infrared spectroscopy (IR) is used to identify organic and inorganic materials, to elucidate molecular structures, and to quantitatively determine nontrace components of mixtures. This technique can be applied to solid, liquid, or gaseous samples.
The infrared region of the electromagnetic spectrum includes radiation with wavenumbers between 12,800 and 10 cm\(^{-1}\) (wavelengths between 0.78 and 1000 \(\mu\)m). Most analytical applications make use of the mid-infrared region which encompasses wavenumbers from 4400 to 200 cm\(^{-1}\).

Absorption of infrared radiation by a molecule results in vibration of the molecule's component atoms relative to each other. Two types of vibrations occur: stretching and bending. Stretching involves a change in the distance between two atoms, with movement along the bond axis. Bending can occur in any molecule having three or more atoms and involves a change in the angle(s) between bonds.

A molecule will absorb infrared radiation only when the molecule undergoes a net change in dipole moment as a result of its vibrational motion. For example, the hydrogen chloride molecule possesses a significant dipole moment due to non-symmetric charge distribution between the hydrogen and chlorine atoms. Stretching of the hydrogen-chlorine bond causes a change in dipole moment, and absorption of infrared radiation can occur provided the frequency of the radiation matches the vibrational frequency. It is not necessary for a molecule to possess a permanent dipole moment to absorb infrared radiation. For example, due to its symmetry, the carbon dioxide molecule has no permanent dipole moment. However, two of its three vibrations produce a change in dipole moment. These vibrations absorb infrared radiation. Vibration of homonuclear diatomic molecules, such as \(\text{N}_2\) and \(\text{O}_2\), does not cause a net change in dipole moment. Vibrations of such molecules are not accompanied by absorption of infrared radiation.

Infrared spectra of diatomic and triatomic molecules are simple. Polyatomic molecules containing a number of different types of atoms exhibit complex spectra. The number of possible vibrations within a molecule containing \(N\) atoms is \(3N-6\) (or \(3N-5\) for a linear molecule). Each of these vibrations is called a normal mode of vibration, and its frequency is referred to as a fundamental frequency. The number of peaks observed in the infrared spectrum does not necessarily equal the number of normal modes. Some normal modes do not give rise to an infrared absorption peak because no net dipole moment occurs, or the vibrational frequency is beyond the range of the instrument. If two or more vibrations occur at the same or nearly the same frequency, only one peak may appear. Additional peaks may be observed in the spectrum due to interaction or coupling of two normal modes. Overtone lines appear at approximately two and three times the fundamental frequency. The occurrence of multiple vibrations in a molecule gives rise to a complex spectrum that is uniquely characteristic of the molecule.

The frequency at which an organic functional group (such as C-H, C=O, C=C) vibrates is determined by the masses of the atoms involved and the force constant of the bond between them. This frequency, called a group frequency, is often unchanged, or only slightly changed, by other atoms attached to the functional group. Over the years, group frequencies have been determined empirically for a large number of functional groups and are commonly summarized in correlation charts, as shown in Figure 1.28 and 1.29. Group frequencies are used to establish the presence or absence of a
functional group in a molecule. Fingerprint frequencies are due to vibrations of the molecule as a whole and are characteristic of the specific molecule.

Several types of infrared instruments are commercially available. Most widely used are the dispersive instruments, which use a grating for wavelength selection, and the popular nondispersive Fourier Transform Infrared (FTIR) spectrometer, which uses an interferometer. Whether dispersive or nondispersive, each infrared instrument contains three essential elements: a radiation source, an optical system for wavelength selection, and a detector. The components of an FTIR instrument are shown in Figure 1.13.

Figure 1.13. Schematic of an Infrared Spectrometer

Mid-infrared sources include the incandescent wire, the Nernst glower, and the Globar. The incandescent wire source consists of a tightly wound coil of nichrome wire electrically heated to about 1100° C. The Globar is a silicon carbide rod electrically heated to about 1300° C. The Nernst glower is composed of zirconium, yttrium, and erbium oxides electrically heated to about 1500° C. Globar and Nernst glower sources are hotter and, therefore, more intense than the incandescent wire source. However, the incandescent wire is more rugged and requires less maintenance.

Two types of detectors are used in the mid-infrared region: thermal and photon. In a thermal detector the infrared radiation is absorbed by a detector element. The resultant rise in temperature produces a measurable change in a physical property of the detector. A thermal detector may consist of several thermocouples, each fabricated from two dissimilar metals. When a thermocouple absorbs infrared energy, a measurable potential difference develops at the junction of the two metals. Another type of thermal detector is the pyroelectric detector. In this device, the sensing element is a thin crystal of a pyroelectric material, such as deuterated triglycine sulfate (DTGS), between two electrodes. Heating of the crystal by absorption of infrared radiation alters the polarization of charge within the crystal, and a measurable change in capacitance is produced. In a photon detector, infrared photons striking a semiconductor surface excite
electrons on the surface from a nonconducting energy state, or valence band, into a conducting state. The photovoltaic detector is a type of photon detector in which a small voltage is produced in response to infrared radiation exposure. Two examples of the photovoltaic detector are the lead tin telluride detector and the mercury cadmium telluride detector. Photon detectors respond more rapidly than the thermal detectors, but the two types have similar sensitivities.

Infrared spectra can be obtained for gaseous, liquid, and solid samples. Most widely used as cell windows are the alkali halides, especially sodium chloride and potassium bromide. Unfortunately, these materials are fogged by exposure to moisture. Silver chloride can be used for aqueous solutions or most samples. However, silver chloride darkens with continued exposure to light.

Solid and liquid samples can be analyzed in solution. No single solvent is transparent over the entire infrared region. To obtain the entire spectrum of a sample, two or more solvents must be used. Carbon tetrachloride and carbon disulfide are useful for many organic compounds. Carbon tetrachloride is transparent at wavenumbers above 1333 cm\(^{-1}\), whereas carbon disulfide is transparent below 1333 cm\(^{-1}\). Acetone, acetonitrile, chloroform, and methylene chloride are used for polar materials that are insoluble in carbon tetrachloride and carbon disulfide. Because alkali halide cell windows are attacked by moisture, solvents must be dried before use. Water absorbs strongly in the infrared and is seldom used as a solvent for infrared analysis. Infrared cells for solution samples are commonly constructed with sodium chloride windows separated by Teflon spacers or gaskets. Because solvents absorb infrared radiation, path lengths are short (0.005 to 5 mm). Both variable path length and fixed path length cells are available.

When a suitable solvent is not available, spectra of liquids can be obtained from capillary films. A drop of liquid is placed between two windows, which are squeezed together to give a thin (0.001 to 0.05 mm) film. This technique does not give a reproducible path length and is limited to qualitative investigations.

Spectra of solids not soluble in a suitable solvent are often obtained from a dispersion of the solid sample in a solid or liquid matrix called a mull. To prevent signal loss due to scattering or refraction of the infrared radiation, the sample must be thoroughly ground to a particle size smaller than the analytical wavelength (less than 2\(\mu\)m) and dispersed in a mulling agent whose refractive index is close to that of the sample. For best results, a very small amount (less than 10-20 mg) of sample is ground in an agate mortar until the powder forms a glossy cake on the sides of the mortar. The resulting powder is then mixed with the mulling agent.

Mineral oil (Nujol) is frequently used as a liquid mulling agent. If hydrocarbon bands interfere, a chlorofluorocarbon grease (Fluorolube) or hexachlorobutadiene may be used. To obtain a complete spectrum free of interfering bands, the halogenated agents are used for the 4000 to 1340 cm\(^{-1}\) region, and mineral oil is used below 1340 cm\(^{-1}\). One or two drops of mulling oil are added to the powder in the mortar, and the grinding action continued until the solid is uniformly dispersed in the oil. The resulting
paste is then analyzed as a thin film.

Potassium bromide and other alkali halides are used as solid mulling agents. In the KBr mull or pellet technique, the finely ground sample (up to 1 mg) is intimately mixed with approximately 100 mg powdered KBr. The mixture is then pressed in a die, under a pressure of 10,000-15,000 psi, to form a transparent or translucent disc. Better results are often achieved when the die is evacuated to eliminate occluded air. Adequate KBr pellets can be obtained without evacuation in a stainless steel Mini-Press. This device consists of two highly polished bolts within a cylindrical nut. The KBr mixture is placed between the bolts, and the bolts are tightened against each other to produce a pellet.

The KBr pellet method has several advantages: (1) KBr has no interfering bands, (2) quantitative analysis is readily possible with an internal standard, and (3) the formed pellets can often be stored. However, the method also has disadvantages: (1) Some materials decompose or change form under the pressure and heat encountered during pellet formation, (2) inorganic salts may exchange ions with the KBr, and (3) KBr may absorb water which absorbs near 3450 and 1640 cm\(^{-1}\).

Polyurethane and polyisocyanurate foams, cork, and epoxy resins are examples of materials that cannot be reduced to a powder by grinding in a mortar. A mechanical grinder or ball mill can be used for such materials. Grinding efficiency may be enhanced by first freezing the sample with liquid nitrogen.

Polymers can be analyzed as unsupported films. A polymer solution is poured onto a glass or metal casting plate. The solvent is evaporated in a vacuum oven or under an infrared lamp, and the sample film is stripped from the plate. Samples run as unsupported films frequently exhibit interference fringes which interfere with the spectrum. In these cases, the attenuated total reflectance (ATR) technique, described below, is extremely useful.

Attenuated total reflectance ATR (also called internal reflectance) greatly enhances the sampling capability of infrared spectroscopy. With this technique, infrared spectra can be obtained from solid materials that cannot be readily dissolved, dispersed in mulls, or cast as films. ATR is widely used to sample polymers, rubbers, cured resins, fibers, textiles, and papers. Figure 1.14 shows an internal reflection element (IRE), composed of a transparent material of high refractive index, surrounded by a sample. When radiation passes from a more dense medium into a less dense medium, part of the radiation is transmitted through the interface and part is reflected. The fraction of the radiation that is reflected increases as the angle of incidence at the interface between the two media becomes larger. Beyond a certain critical angle, all of the radiation is reflected. During the reflection process, the radiation penetrates a very small distance into the sample, and a portion of the radiation is absorbed by the sample. The loss in intensity due to sample absorption is sensed by the detector.
1.2.6 Raman Spectroscopy

Raman spectroscopy is used primarily for the identification of functional groups and the determination of molecular structure in organic and inorganic compounds. Similar to infrared spectroscopy, Raman spectroscopy is based on vibrational changes within molecules. However, vibrations that are observed in the Raman spectrum may not be seen in the infrared spectrum, and vice versa. Therefore, complimentary information can be obtained from using both techniques.

Raman spectroscopy is based on a light scattering phenomenon. When light passes through a transparent material, a very small fraction of the light is scattered due to collisions with molecules present within the material. Two types of collisions occur: elastic and inelastic. In an elastic collision, the scattered light is of the same energy as the incident light. However, in an inelastic collision, energy is exchanged between the molecule and the incident radiation so that the energy of the scattered light is different from that of the incident light. This is known as the Raman effect. When this type of collision occurs, the energy of the scattered light is $h(n_0 - n_n)$ where $h$ is Plank's constant, $n_0$ is the frequency of the incident radiation, and $n_n$ is a frequency in the infrared region of the electromagnetic spectrum. The Raman effect is inherently very weak. The intensity of the Raman scattered light is, at most, only 0.001% the intensity of the source radiation.

Inelastic collisions give rise to two types of scattered radiation: Stokes radiation and anti-Stokes radiation. Stokes radiation, observed at a lower energy that the incident radiation, occurs when a molecule initially in the ground vibrational level is raised to an excited vibrational level as a result of interaction with the incident light. The energy of the Stokes radiation is $h(n_0 - n_n)$ where $h(n_n)$ is the difference in energy between the ground vibrational level and the excited vibrational level. Anti-Stokes radiation occurs when molecules already in an excited vibrational level decay to the ground vibrational level during the interaction with the incident light. Anti-Stokes radiation is observed at a higher energy than the incident radiation. The energy of the anti-Stokes scattered radiation is $h(n_0 + n_n)$. Because most molecules are initially in the ground vibrational level, anti-Stokes radiation is much less intense than Stokes radiation. Except for very specialized applications, the Stokes lines are predominantly used in analytical Raman spectroscopy.
In the previous section, it was stated that for a vibration to be observed in the infrared spectrum, the vibration must cause a change in the molecule's dipole moment. The dipole moment is the product of the distance between two centers of charge in a molecule and the magnitude of the charge difference. Polar function groups such as hydroxyl (O-H) and carbonyl (C=O) give strong peaks in the infrared. For a vibration to be observed in the Raman spectrum, the polarizability of the molecule must change as a result of the vibration. Polarizability is the measure of the ease with which the electron distribution within the molecule is distorted in an electromagnetic field. Nonpolar functional groups with symmetrical charge distribution, such as C=C, N=N, S-S, and C≡C, give strong Raman peaks. Some vibrational modes can be observed in both the Raman and infrared spectra. Other vibrations can be observed only by infrared spectroscopy, or only by Raman spectroscopy. Therefore, although each technique provides considerable information about the functional groups present in a molecule, more information is obtained by using both techniques to characterize a material.

Raman spectroscopy is especially useful for detecting the C=C group in olefins. The C=C stretching mode is usually very weak in the infrared spectrum. When the C=C group is symmetrically substituted, as in ethylene (H₂C=CH₂), no band appears in the infrared spectrum because there is no change in dipole moment during the vibration. On the other hand, this group gives an intense peak in the Raman. Similarly, Raman surpasses infrared in detecting disubstituted acetylenes (R-C≡C-R) and disulfides (R-S-S-R). Even in cases where the two R groups are not identical, but only similar in size, the intensity of the Raman peak will be stronger than that of the infrared peak. Raman spectroscopy can also be used to detect and analyze homonuclear diatomic molecules, such as H₂ or N₂, which are not infrared active. Another area in which Raman spectroscopy is useful is the study of materials in aqueous solution. Water is a weak Raman scatterer and therefore does not cause interference. In contrast, it is difficult to obtain infrared spectra from aqueous solutions because water absorbs strongly in the infrared.

A typical Raman spectrometer is shown schematically in Figure 1.15. Because of the inherent weakness of the Raman effect, lasers are used almost exclusively as sources in Raman spectroscopy. The most commonly used lasers are continuous-wave gas lasers. The helium/neon laser produces an intense line at 632.8 nm. The argon laser produces useful lines at 488.0 and 514.5 nm. The laser beam is focused on the sample by a series of lenses and mirrors. Because both the incident and scattered radiations are in the visible region of the electromagnetic spectrum, glass can be used for cell windows, lenses, and other optical components. The scattered light is collected at 90° relative to the laser beam and is focused on the entrance slit of a double monochromator. The scattered light is dispersed into its component frequencies by gratings within the monochromator, and the dispersed light passes through the monochromator exit slit into the detector. The most commonly used detector for Raman spectroscopy is the photomultiplier tube (PMT). PMT's give low background signals and high sensitivity in the visible region of the spectrum. Because PMT response is a function of wavelength, the type of PMT used depends on which laser line is used for excitation.
Raman spectroscopy can be performed on solids, liquids, and gases. Liquids are usually contained in a glass capillary tube. Solids are sampled in several ways: as pure powders in a glass capillary tube, as pressed pellets (either pure or mixed with an inert solid), and as single crystals. A visible light microscope can be coupled to the optical system and can be used to obtain spectra from microscopic particles. A major limitation to Raman spectroscopy is interference by fluorescence originating either in the analyte itself, or in other species present in the sample. Because fluorescence is inherently more intense than Raman scattering, it is difficult if not impossible to detect Raman scattering in the presence of fluorescence. If the fluorescence is due to other species present, it may be possible to remove the fluorescent component by extraction, distillation, or another purification procedure. If the fluorescence is due to the analyte itself, selection of a different laser line for excitation may be helpful. Another problem is the decomposition of the sample in the laser beam. This occurs frequently when the sample is highly absorbing (colored). This problem can sometimes be overcome by rotating the sample or by reducing the power of the laser source.

1.2.7 Nuclear Magnetic Resonance Spectroscopy

Nuclear magnetic resonance (NMR) spectroscopy is used primarily to elucidate the structure of organic and inorganic compounds containing atoms which possess a magnetic moment, such as $^1$H, $^{13}$C, $^{19}$F, $^{29}$Si, and $^{31}$P.

When the nuclei of certain atoms spin, a magnetic moment is generated. If these nuclei are placed in a strong magnetic field, the magnetic moments will assume different orientations with respect to the external field. Each orientation corresponds to a discrete energy state. Absorption of radio-frequency radiation causes a nucleus to undergo a transition from one orientation to another. The required energy of the radio-frequency radiation depends, in part, on the identity of the nucleus and chemical environment of the nucleus. Therefore, this technique is extremely useful in the determination of molecular structure.

The components of a Fourier transform NMR spectrometer are shown in Figure
1.16. In this instrument, all of the nuclei are excited simultaneously by a pulsed, high intensity radio-frequency source. This generates a time-domain spectrum that is converted to frequency-domain by Fourier transformation. A computer controls the pulses and performs the Fourier transformation.

![Diagram of a Nuclear Magnetic Resonance Spectrometer](image)

Figure 1.16 Schematic of a Nuclear Magnetic Resonance Spectrometer

Two effects are important in structural analysis: chemical shift and spin-spin splitting. Not all nuclei of the same type (e.g., $^1$H or $^{13}$C) absorb at the same frequency. The frequency at which absorption occurs is strongly affected by the chemical environment of the nucleus. This effect, called the chemical shift, is due to the circulation of electrons around the atom being probed. Electron circulation generates a small magnetic field which is usually in opposition to the external field. The field actually sensed by the nucleus depends on the electron density and, therefore, the chemical environment around the nucleus. NMR peaks are usually reported relative to the peak obtained for a reference compound that is measured at the same time. Neighboring nuclei which have nonzero magnetic moments generate magnetic fields. This effect causes splitting of the NMR peaks and is called spin-spin splitting. Structural analysis is based on an analysis of the chemical shifts and spin-spin splitting observed in the NMR spectrum.

1.2.8 Mass Spectrometry

Mass spectrometry provides qualitative and quantitative information about the atomic and molecular composition of organic and inorganic materials. This technique is used to elucidate the molecular structure of unknown compounds, and to confirm the presence of known compounds. Combined with a separation technique, such as gas or liquid chromatography, mass spectrometry can also be used to identify and quantitatively measure the components of a complex mixture.

In mass spectrometry, molecules within a sample are converted into highly ener-
getic, gaseous ions. During the ionization process, the molecule may be fragmented to produce smaller ions. These ions are then separated on the basis of their mass-to-charge (m/z) ratios. A mass spectrum is a plot of the relative abundance of ions measured at each value of m/z. Every compound has a unique fragmentation pattern, and therefore a unique mass spectrum.

The major components of a mass spectrometer are pictured in Figure 1.17. The sample introduction system must permit introduction of the sample into the ion source, which is maintained at $10^{-5}$ to $10^{-6}$ Torr. Sample introduction systems include batch inlets, direct insertion probes, and gas and liquid chromatographic inlets. Gases and volatile liquids can be introduced through a batch inlet system in which the sample is first volatilized (by applying vacuum and, sometimes, heat) and then allowed to leak into the ionization chamber through a pinhole in a glass or metal diaphragm. Solids and nonvolatile liquids can be introduced with a direct insertion probe. The sample is placed on the probe which is then introduced directly into the ionization chamber. The chromatographic inlets are described in Section 1.1.

Figure 1.17. Schematic of a Mass Spectrometer

The ion source ionizes and fragments the molecules within the sample. Commonly used ionization sources include the electron impact (EI), chemical ionization (CI), and fast atom bombardment (FAB) sources. The electron impact source is the most commonly used. Electrons emitted from a heated filament are accelerated by applying a potential between the filament and an anode. When these high energy electrons collide with the sample molecules, positive ions are produced. Some of these ions have the same mass as the original analyte molecule, and are referred to as the molecular or parent ions. Because of the high energy of the electron impact source, many of the molecules are extensively fragmented. The fragmentation pattern is characteristic of the molecule and is useful for identification. However, in some cases fragmentation is so extensive that the molecular ion is not observed. In these cases, it is more difficult to determine the molecular weight and, therefore, the structure of the compound. In chemical ionization, the gaseous sample is ionized by collisions with ions generated by electron bombardment of a reagent gas, usually methane. Chemical ionization produces less fragmentation than electron impact ionization. In fast atom bombardment, the sample is ionized by collisions with high energy argon or xenon atoms. Fast atom bombardment produces relatively large amounts of the parent ion, and is especially useful for the characterization of high-molecular-weight materials.
After leaving the ion source, the ions are accelerated and focused onto the entrance of the mass analyzer. The mass analyzer separates the ions according to their mass-to-charge ratios. The magnetic sector and the quadrupole mass analyzers are the most commonly used. Magnetic sector mass analyzers utilize an electromagnet to bend the paths of the ions. Ions of different mass are alternately focused on the exit slit by varying the strength of the magnetic fields. In quadrupole mass analyzers, four electrically conducting rods are positioned parallel to and symmetrically around the ion path. Opposite pairs of rods are electrically connected, and one pair is held at a positive dc potential, while the other pair is at a negative dc potential. In addition, radio-frequency ac potentials, $180^\circ$ out of phase with each other, are applied to the two pairs. The combined electromagnetic fields cause the ions to oscillate as they pass along the axis of the quadrupole. When the oscillations are sufficiently large, the ions collide with the rods and are neutralized. By varying the dc potential and/or the frequency of the ac field, ions of different mass-to-charge ratio are allowed to pass through the analyzer.

Most mass spectrometers use electron multipliers for ion detection. Ions leaving the mass analyzer are accelerated and focused onto a metal plate, or dynode. The dynode emits several electrons as a result of each ion bombardment. These electron are accelerated toward a second dynode, where more electrons are emitted. As the electrons strike successive dynodes, the amplification process continues. Current amplification of $10^5$ to $10^7$ is attained.

1.3 Microanalytical Techniques

The advent of high technology has brought about the need to interrogate smaller and smaller samples of materials to solve complex materials problems. From the concerns of particulate contamination in high performance aerospace engines to the performance of magnetic storage media there is a great demand for the capability to analyze very small quantities of materials. And with this demand for analysis comes the necessity to successfully collect and test the material of interest. When the sample comes from an almost endless source such as in the production of commodity materials, the problem is not too little sample, but in contamination or failure investigations the samples are usually limited and hard to recover. This section will describe sampling and detection methods for microscopic analysis. Sampling techniques will be discussed in detail since this topic is seldom covered in instrumental analysis text books.

1.3.1. Microsampling Techniques

Microsampling techniques are usually applied to materials with limited quantity and can either be solids or liquids. The solid samples can include particles, fibers, films, laminates, inclusions, suspensions or residues. Each of these materials requires a different approach to their collection. Another confounding aspect to the sampling is the accessibility of the material. If the material of interest is under a film as an inclusion or in a solid mixture as a discrete particle the analyst must be creative, and sure-handed to retrieve the materials.
Some of the tools that can be used for microsampling include tweezers with sharpened tips, Exacto knives and single-edged razor blades, tungsten probes that have been formed into fine points, glass slides, capillary brushes, Roller Knife and maybe the most important is a prep microscope. The prep microscope is used to see samples when they are being transferred or prepared for analysis. The prep microscope can have magnification from 10x to 50x and should have the capability for transmission and reflectance imaging. It should have a substantial fixed stage that will support some force in forming samples. Any variation from the Bausch and Lomb StereoZoom series or equivalent would be a good choice. Pamphlets 1, 2 supplied with the microscope give some instruction as to the use of the microscope but experience from others or with time will better develop knowledge needed in specific applications. Publications such as "The Microscope"3 is also a good source of information for microscopic sample collection.

Collecting samples in the field requires many specialized tools to effectively isolate and collect the sample. Along with the techniques and tools to be described later there are several items that are useful and should be included in a Microscopists tool kit. The most important of these items is a magnifier. This is almost a necessity since to sample it is necessary to see the object. The magnifier can be used with a flashlight or can be equipped with an appropriate illuminator as an integral part of the magnifier. Sample transfer from the point of sampling is also important since the effort expended in sampling can be negated if the sample is lost or contaminated with unrelated foreign matter. Foresight in selecting sample containers that have been previously inspected for microcontamination will benefit the analyst in the long run. Plastic petrie dishes and self-sealing bags are convenient but require prior inspection to assure that particles are not present as a result of static attraction or contamination during production.

1.3.1.1. Particulate Sampling

Particulate sampling is probably one of the easier sampling problems but by no means simple. Particulates that are loosely adhered to a surface can be easily removed using tweezers with very sharp, straight points. This fact needs to be emphasized; don't share the sampling tools that you accumulate with anyone that is not familiar with their use. It might seem trivial that anyone can use tweezers but to care for a finely sharpened pair and then have them used as a pry to remove a stuck septa or ferrule can be very disconcerting. Particles that are brittle, very flat or adhere strongly to the substrate may require the use of a sharp blade such as a single-edge razor, or an Exacto knife. Cleanliness is paramount when using any sampling device and should be of special concern with blades. A small foreign particle on the blade prior to collection of the sample can become a point of contention when the sample is analyzed because this foreign particle can be misconstrued as part or a major portion of the suspect. The use of lens paper or lint-free laboratory wipes to clean the sampling tools prior to use followed by subsequent inspection using a microscope to observe cleanliness is a minimum.
In dry atmospheres charges tend to accumulate on sampling tools and particles. With loose samples this can manifest itself in the "Calivaris County Frog Syndrome" where the precious sample that is setting so pristinely on the substrate leaps uncontrollably out of sight. This charge concentration phenomena can be eliminated by using a static discharge gun such as a Zerostat gun (Ernest F. Fullam, Latham, N.Y). Two conditions should be observed when using this static discharge gun. First, never use the gun in an explosive environment and second, the gun discharges both positive and negative charges with each stroke; a positive discharge with the squeeze of the trigger and negative discharge with the release of the trigger. It is important to discharge both the sample and the sampling tools prior to sampling. This is a trial and error effort to select the proper discharge combination that hopefully doesn't end in errors too frequently. Of course since opposites attract, static charges can also be a benefit since they can aid sample collection by causing particles to cling to the sampling tool, a very fortuitous event.

In addition to the tweezers and blade, a tungsten probe is very useful to push or hold a particle while using another tool to retrieve it, or if static charges are helpful, to pick up the sample. A capillary brush (whose construction will be detailed later) is also a useful tool to collect large numbers of particles. The application of the capillary brush is limited in particulate collection since separation of the particles from the brush fibers might be problematic. An alternative to the capillary brush is the vacuum tip, a device constructed to provide a vacuum to pick up small particles and a filter medium to capture the particle for analysis. This apparatus can be constructed of a capillary and filter holder attached to an appropriate vacuum source. The use of adhesive tapes are quite useful in collecting and transporting particulates, but removing the sample from the adhesive can be cumbersome. An alternative is to dissolve the adhesive from the backing using filtered toluene and evaporating it onto the KBr window prior to analysis. The particle is surrounded in a matrix that can hold it securely and can be removed digitally from the collected spectrum by spectral subtraction.

Particles are found not only on the surface, but can also be imbedded in objects as inclusions. Included particles are complex sampling problems. If the material in which they are contained is soft and pliable it is possible to excise them from the material using blades, probes, dental picks and tweezers. The best approach is to observe the particle under a prep microscope. A large diameter tungsten probe would be beneficial since it could be used to penetrate the substrate and pry the sample to the surface where it can be picked up with tweezers or a blade. The adherence of the surrounding material is of some concern, but it is of benefit and can be used in the analysis of the particle as a reference in spectral subtraction (the application of spectral subtraction will be covered elsewhere). This sampling technique is of course destructive in nature but can probably be limited to small areas. Substrates of an intractable nature are more problematic since the substrate can prevent penetration because of their hardness and strength. If probes and blades are not successful it might be necessary to cut the substrate and the particle using a diamond or jeweler's saw. The cut will have to be made first to remove a larger piece from the substrate to include the particle and then through the particle to expose it to the surface. A microtome can also be useful here to
take a small, thin slice of the sample. The microtome is an expensive item, so unless this type of sampling is a routine occurrence the effort expended in sawing is more cost-effective.

Particles suspended in liquids can be handled very easily by using filtration media of the proper construction and observe cleanliness in sample handling. A typical apparatus that would be used to separate suspended particles would include a gas tight syringe of 5 ml or less supplied with a Luer-Lok connector. A syringe filter holder and filter medium constructed of materials compatible with the suspension solvent should be used. Filter media such as Nuclepore filters and equipment (Costar Corp. Cambridge, MA.) is a good selection since the filter media has uniform pore size and is constructed of nonfibrous, solvent resistant materials. It is important to use a filter medium free of fibers to avoid confusion of sample with medium. To aid in locating transparent samples more easily, the filter media can be sputter-coated with gold/palladium from a sputter coating apparatus used in Scanning Electron Microscopy if available. An aliquot of the suspension is passed through the filter and then flushed with an aliquot of the same solvent as the suspension to rinse the filter of any dissolved material that might crystallize after the solvent has evaporated. The flushing solvent should have been passed through a filter medium of at least the same pore size as that used for the sampling to avoid contamination of the sample with foreign particles. Once rinsed the filter media containing the particles of interest can be examined under a prep microscope and the particles can be removed from the filter by any appropriate method previously mentioned.

1.3.1.2. Fibers

The problems that arise in fiber collection are far fewer than those experienced in particulate sampling. Fibers are an easier material to handle since they are flexible and usually have one large dimension. They can exhibit charging as do particles, that can be neutralized with static discharge guns. Tweezers are the most appropriate tool to use in fiber collection, but things as diverse as adhesive tape or vacuum filters can also be used. An easy vacuum method utilizes the filter support and media used to filter solutions and a vacuum source. These techniques are appropriate for isolated fibers or those that are loose and non-woven. For woven fabric or bundled fibers the sampling methods become more complex. In fabric the sampling of individual fibers can be performed by using a tungsten probe to lift the fiber from the weave, tweezers to pull out an appropriate length and a pair of sharp, small scissors to cut the selected fiber. With this method any number of individual fibers can be removed from the fabric for analysis. Fiber bundles can be treated in the same manner as fabric except for a need to immobilize the bundle. Immobilizing the bundles can be done with adhesive tape as a support or by holding the bundle between two glass slides so that their ends extend past the edge of the slide. It should be noted that some glass slides are lubricated with formate salts and should be removed by scraping one slide edge over the surface of another. This will eliminate the possibility of sample contamination. The individual fibers can then be selected using tweezers. If the fiber is coated or multilayered and a cross-section is desired so that each layer can be observed, the fiber can be mounted into
epoxy contained in the end of a Pasteur pipet. The mounted sample can then be sliced or microtomed before analysis.

Fibers are usually extruded and for that reason have a uniform cylindrical shape. This shape acts as a lens when exposed to the spectrometer and distorts the beam causing aberrations in the baseline and changes in relative absorbivities of some peaks. To avoid this problem it is best to flatten the fiber in the area of interest. This can be performed using either a rigid spatula or a Roller Blade (Spectra Tech, Stamford CT). The Roller Blade can be used with the smallest fibers to roll a portion of the sample flat. This flattened area is then ideal for analysis.

1.3.1.3. Films and Laminates

The sampling of films and laminates can be divided into two classes that are dependent on the choice of analytical method. For thin films, transmission measurements would be the most appropriate if the film is transparent and thin enough to allow light to pass through. In this case the film should be treated as particulate material. If the film is too thick for transmission or opaque or a laminate, a thin cut can be taken from the edge of the sample using the following procedure. The film is placed between two glass slides (which have been cleaned as mentioned earlier) in such a way as to leave a portion of the film overlapping the edge. The exposed film edge is then cut flush with the glass slides. The sample is then repositioned so that a thin section overlaps the edge of the slide and a very thin cut is made from the edge of the sample. The use of a prep microscope is of benefit here. The thin section that was formed in the second cut should be almost translucent and can be handled as a particle. If the sample is a laminate each of the layers can be analyzed individually. The laminates can also be sampled by cutting obliquely through the sample thickness to expose wide surfaces of each laminate. As an alternative to sectioning, thick films of an adequate size can be sampled using organic-free abrasive paper such as is supplied with the Si-Carb Sampling Kit (Spectra Tech, Stamford, CT). The abrasive paper is used to remove a portion of the surface of the film and then analyzed by reflectance techniques directly on the pad. This sampling is limited to surfaces and would be ineffective in laminated structures.

1.3.1.4. Micro-pyrolysis

Solid samples are at times intractable even to crushing. This requires harsh treatment of the sample in order to transform it into a more easily manipulated configuration. This can be done using micro-pyrolysis. Micro-pyrolysis is a technique that is used to convert insoluble, hard samples to a soluble liquid or solid. The method involves placing the sample particle or film into a capillary about 3 mm from the end. The sample end of the capillary is heat-sealed and the particle is then heated with a microburner until pyrolysate droplets are formed. The sealed end of the tube containing the ash, if any, is broken off and solvent is allowed to flush the sample onto an appropriate surface for analysis. As was previously noted cleanliness of the solvent is
critical to the analysis to avoid contamination.

1.3.1.5. Liquid Micro-Sampling

Liquids are probably the easiest samples to collect since they are not usually subject to static charges and infrequently do they adhere to the substrate. However, the small quantities that usually occur when collected for micro-analysis are easily lost in the collecting tools normally used for liquid collection, such as pipets or syringes. Certainly microsyringes are appropriate for this task since they hold very small volumes. When samples are not confined to small volumes, but spread out over a large area or in small droplets, it is difficult to collect samples. A solution to this is the use of the capillary brush. The capillary brush is a glass capillary fitted with glass fibers welded to the end. The process of making these brushes is tedious but worthwhile. Small groups of silica fibers such as those used in gas chromatography are placed in the end of the capillary. A microtorch is then used to melt the capillary slightly, enough to hold the fibers but not so much as to close the capillary. The fibers are allowed to extend out of the capillary and are trimmed to form an even tip. This brush can be used to collect samples from enclosed areas or broad surfaces by immersing the fibers into the liquid and allowing it to "capillary" into the fibers and capillary tube. Once the sample is isolated in the capillary it can be transported to the analytical station and removed from the capillary by flushing the capillary with a solvent by "capillary action" onto an appropriate surface for analysis.

1.3.2. Micro-Spectroscopy Using Fourier Transform Infrared and Raman Spectroscopies

Molecular vibrational spectroscopy is an important means of identifying the structure of chemical compounds. Each bond in a molecule has a specific response to incident light energy and will affect the energy contained in the incident light in a specific way. All wavelengths of the incident energy are not absorbed, but rather only those energies that interact with bonds in the sample will be affected. This absorption occurs at specific frequencies and is related to the bonds in the structure with which it has interacted. The interactions are not random but abide by specific rules described by quantum mechanics and are, therefore, reproducible and predictable. When these absorptions are detected and plotted as a function of incident energy frequency it represents an absorption spectrum. Each peak of this absorption plot can be assigned a specific structure with which the incident light has interacted. These interactions cause the atoms and bonds to distort by stretching or bending.

1.3.2.1. Infrared Micro-spectroscopy

The application of microscopic sampling to infrared spectroscopy has had a long history dating back to the 1940s when Burch applied a microscopic accessory equipped with Casagranian lenses to collect microspectra using a dispersive infrared instrument. The first application of microspectroscopy to Fourier transform instruments was in
1983 when BioRad Instruments introduced the FT-IR microscope.

Figure 1.18 is a schematic of the beam path of a typical infrared microscope. It is similar to a sophisticated light microscope in that it contains both a substage condenser and an objective lens. These lenses are, however, reflective rather than transmissive lenses to accommodate the infrared beam. Standard glass lenses would be opaque through most of the mid-infrared region and therefore are not used. Another difference between the light microscope and the infrared microscope is that the latter includes a movable beamsplitter that allows viewing the sample during positioning and focusing, and variable apertures, in some cases, both before and after the sample. The apertures are used to mask both the incident beam and the transmitted beam. This "redundant aperturing" is used to assure that an undistorted baseline is collected by removing stray light (light which has passed around the sample). The aperture after the sample in the transmitted beam can be used to spectrally isolate the unwanted portions of complex sample from contributing to the collected spectrum. The spectral isolation permits analysis of small inclusions in larger matrices that would contribute to the sample's spectrum. The aperture before the sample limits the light scattered by the substage condenser from reaching the detector. The microscope accessory can be used to collect spectra in both the transmission (through the sample) and reflection (from the surface) mode. Reflectance is more troublesome in the interpretation of the resulting spectrum since they are usually distorted by refractive index effects. These refractive index effects are manifested in the reflectance spectra by "derivative-shaped" peaks. The position of the peak is also shifted by several wavenumbers from typical positions found in transmission spectra.

Figure 1.18. Schematic of the Beampath of an Infrared Microscope
The operation of the infrared microscope is straight-forward and is very similar to a light microscope. Unlike light microscopy, however, the infrared radiation wavelength imparts problems to the collection of spectra from samples whose particle size is less than about 50 \( \mu \)m. Particles in this range will be of the same size or smaller than the infrared wavelength. Shape and thickness of the sample are critical since irregularly shaped samples are capable of greater diffraction of the incident beam. The diffracted beam then forms nodes that divide the incident energy and reduce the total throughput of the sample. The use of apertures again play a significant role here but this time to the detriment of total signal since they effectively eliminate some of the diffracted nodes. Some improvement in the spectrum is gained because the apertures eliminate the diffracted nodes from other areas of the sample, which is the spectral isolation function mentioned earlier.

Most samples to be analyzed by infrared microspectroscopy are introduced into the accessory by placing the sample on an infrared-transparent material such as a KBr or NaCl window. The first step of the collection process is focusing the microscope on the sample. Focusing is important since it minimizes spectral distortions caused by irregular samples. It is good practice to focus deep into the sample if the sample has a rough surface. That is to say, rather than use the top surface of the sample use a focal plane that appears to be inside the sample. Flat samples are easily analyzed since they have a uniform surface and focusing on the top surface is adequate for data collection.

The second step in the collection process is to select the area of interest in the sample by using the apertures to outline this area. This aperturing performs two practical functions. The first is to define the portion of the sample to be analyzed and the second is to block radiation not passing through the sample or the area of interest. The radiation not passing through the sample will cause a shift or distortion of the baseline leading to spectral irregularities such as incorrect peak ratios within the sample and sloping baseline. The sloping baseline manifests itself in the display of the spectrum and in spectral subtraction (to be covered later).

Once the sample is in place the third step is data collection. The FT-IR instrument is a single-beam spectrometer and it is necessary to collect a background spectrum to which the sample spectrum is ratioed. The sample in the microscope has been masked by an aperture and it is necessary to collect the background using the same aperture size as the sample. Since it is impossible to know the sample aperture size before-hand it is common to collect the background spectrum after the sample spectrum but before ratioing the sample to a background. The background spectrum is collected by moving the image field from the sample to an area of the supporting window that has no sample present.

The collection of a good spectrum using microspectroscopy is best served by analyzing flat samples, but, in practice few samples are flat. Particles that are too thick to produce a spectrum of less than 2AUFS (absorbance units full scale) should be crushed to reduce the thickness. Spectral absorbance above 2AUFS will distort the relative ratios of the absorbing peaks, especially the peaks of greatest intensity.
Crushing can be done by placing the particle between two clean glass microscope slides and squeezing it until the sample is translucent. The crushed sample can then be transferred to a KBr window for analysis. Two KBr windows can also be used to crush softer samples. When crushing between KBr windows, additional KBr powder should be placed between the windows to provide a location for collecting a background. If no KBr were present an interference fringe would be formed by the gap between the two windows when the background was collected. The interference in the background would unnecessarily distort the sample spectrum during ratioing. In the case of elastomeric materials the difficulty in collecting a spectrum is not in flattening a thick sample, but maintaining the thickness after crushing. Because of their resilience the elastomers tend to return to their original shape. The solution to this problem is to compress the sample between two KBr windows and while holding them securely place fast-curing glue (Crazy Glue, for example) on the edge of the windows to hold them in place. Allow the glue to cure and then collect the spectrum. Samples that are difficult to secure on the slide can be immobilized on the KBr window by embedding them in rubber cement diluted 1:1 with cyclohexane. The spectrum can then be collected and the embedding media contribution to the spectrum can be removed by spectral subtraction.

Single fibers are a difficult sample for classical transmission spectroscopy because of their dimensions. In conventional spectroscopy the single fiber was difficult to mount reproducibly into the infrared beam and to observe without spectral distortion. Microspectroscopy has opened the field to capabilities that were non-existent in the past. The infrared microspectroscopic accessory enables the analyst to collect high quality spectrum from single fibers as small as 5 μm in diameter. The fiber sample can be synthetic or natural of any dimension. The only restriction on the sample is that it should be capable of compression to form a flat area for analysis. This flat area can be formed using a hard probe to roll the fiber or a diamond anvil cell to crush the area of interest. In either case the fiber is flattened so that the it does not act as a cylindrical lens in the infrared beam. It should be noted here that modifying the fiber in such a manner will possibly alter any orientation information that can be obtained from the spectrum.

Samples that are in the form of fine powders can pose a problem in conventional spectroscopy since the formation of a pellet will so dilute the sample that a complete spectrum is impossible to collect. The preparation of the sample as a salt dispersion or micropellet can be of benefit only when the sample can be observed. A salt dispersion can be made on a glass slide by mixing the sample with salt and then crushing the particles to reduce their size. The micropellet provides an easier means of handling the sample and can be made using a microgrinder (such as a Wiggle-Bug) and dies that produce 3 mm pellets when compressed. The microscope provides the method of condensing and focusing the beam to collect the spectrum.

The infrared microscope is not only useful for solid materials, but is also useful for limited amounts of liquids. The deposition of the liquid sample onto a window by an appropriate technique such as a microbrush or microsyringe can form a spot that is dependent on sample size but can be focused on be the accessory. With careful concen-
tration on the window a small spot can be formed whose spectrum can then be collected as with any other transparent sample. Microspectroscopy is applicable as a tandem technique for gas chromatography since the spectrum of the liquid can be collected and then have the sample transferred to the GC for further investigation. It can also be applied to HPLC eluents where evaporation of the mobile phase and resultant analysis can yield spectral information about the solute.

1.3.2.2. Raman Microspectroscopy

The first application of microspectroscopy was reported in 1979. The advent of laser applied to Raman spectroscopy has enabled standard metallurgical microscopes to be coupled with the Raman spectrometer for the collection of spectra from small samples. Optical glass does not have a Raman interaction and is therefore readily adapted to Raman spectroscopy with little modification to the microscope optics. The Raman microscope has the same limitations as does Raman spectroscopy in that only samples with little color and low fluorescence can be analyzed. The spatial resolution of the microscope is excellent with sample sizes only limited by the focal size of the incident laser onto the sample. In practical terms this resolution is 5-10 μm.

The operation of the Raman microscope is relatively straightforward for sample analysis. The sample is placed onto the sample stage with the microscope in the reflectance mode, the area of interest is located, and focus is obtained for the sample and the laser spot on the sample. For samples that are thermally stable the spectrum can be collected using high laser energy input. The greater the incident energy the greater the emitted signal. Thermally labile samples are significantly more complex in the analytical approach used. Because the high incident created in the microscope field by the laser generates significant amounts of heat, thermally sensitive samples must be handled with more conservative methods.

The thermal deterioration is significant since repeated occurrences lead to the deterioration of the microscope objective through deposition of the evolved materials onto the objective. The first and most obvious means of reducing thermal destruction is to reduce the incident energy. This approach will reduce the thermal load on the sample but with proportional reductions in Raman effect emitted light. The compromise here is to increase the data collection time with either increased sampling rate or increased number of coadded scans. Both of these options increase data collection times but provide less aggressive environments. An alternative to incident energy reduction is to provide a means for heat to dissipate from the sample during analysis. The easiest and most straightforward methods are to embed the sample in water glass, a concentrated solution of sodium silicate that is transparent to the Raman effect and forms a hard, transparent mount for the sample. The water glass also protects the sample and objectives from thermal decomposition by providing a mode for the excess heat energy to be dissipated. Samples can also be diluted in a pellet made of materials that have no Raman effect such as alkali halides to minimize heating. Defocusing the incident beam is also an effective technique for mediation of localized heating but signal reduction may result in poor quality spectra.
Liquid samples of limited volumes can also be analyzed by Raman microspectroscopy. The application does not require complex sampling method but merely placing the sample in a glass capillary. Care should be taken in focusing the laser beam on the sample. It is necessary to first focus the visual image of the capillary surface and then while observing the laser image raise the stage to move the beam into the capillary. A distinct change in the laser image will occur when the beam has passed into the capillary contents. Data collection is identical to any other sample.

Fiber samples can also be evaluated as with infrared microspectroscopy except that the fiber need not be crushed to reduce thickness but can be collected without modification. Samples can be immobilized on a glass slide using adhesive tape. In addition, surface particles on the fibers can be evaluated using appropriate pinhole masks to spatially separate the area from the matrix. Characteristics of the area of interest can also be accentuated in the final spectrum by spectral subtraction.

1.3.3. Scanning Electron Microscopy

Scanning electron microscopy (SEM) is used to produce high resolution and depth of field images of sample and to provide chemical analysis of micron sized areas on or near the surface. Products obtained from interactions between bombarding electrons and the atomic species in the specimen are ejected from an excitation volume in the sample and monitored during a typical SEM scan. Any partially conducting material or non-conducting materials coated with a thin layer of gold or gold alloy, which has a low vapor pressure can be analyzed with the SEM.

In SEM analysis, the specimen is bombarded with high energy electrons (5 to 30 kilovolts) which produces several different types of signals to provide information about the specimen. Both elastic and inelastic collisions result from the interactions of the electrons with the atoms in the sample. The elastic collisions between the bombarding electrons and the atomic nuclei of the specimen produce backscattered electrons (BSE), as shown in Figure 1.19, which provides both topographical and compositional information about the sample. Imaging with the BSE signals provides a means of distinguishing zones of different atomic number within a specimen due to the greater probability of elastic collisions with higher atomic number. The penetration depth of the bombarding electrons depends upon the accelerating voltage and the atomic number of the sample. Typically the BSE images provide useful information down to about 0.5 microns.

Inelastic collisions between the bombarding electrons and the atomic electrons of the specimen produce secondary electron imaging signals, x-rays and Auger electrons from interactions with inner shell electrons and light in the form of cathodoluminescence from lower energy processes. The secondary electrons are collected to produce the micrograph images which are normally associated with SEM. The depth of penetration for these signals are usually 2 to 10 nm for metals and 5 to 50 nm for poor conductors. The x-ray information typically arises from a volume around 1 micron in
depth, while cathodo-luminescence is observed almost totally from the surface. Auger electrons arise from interactions in the first 0.5 to 2 nanometer layer of the specimen.

The great depth of field of the SEM (up to 500 times that of an optical microscope) allows it to produce completely in-focus images of rough surfaces at high magnification. However, SEM is generally inferior to the optical microscope for routine examination of samples prepared using standard metallographic techniques at low magnification (300 X - 400X). Some of the current SEM instruments allow for samples as large as 15 to 20 cm to be analyzed. An excellent reference for using SEM in a variety of analytical applications is given in the monograph by Gabriel.

![Schematic showing the principal mechanisms occurring in SEM.](image)

**Figure 1.19** Schematic showing the principal mechanisms occurring in SEM.

### 1.3.4. Optical Microscopy

Conventional optical microscopy is a relatively inexpensive analytical tool for the examination of particulates and microstructures. Typically resolutions of 500 nanometers are possible, which allows for observation of surface faceting and dislocations. Catalogs of particulates, fibers, and morphological species of many materials are available for use to identify a particular material. Many applications using polarized light and the new confocal microscopes enable optical microscopy to continue to provide analytical information which is not available from the other methods.

A major disadvantage of current uses of optical microscopy is that experienced microscopists can identify many species; however, computerized databases with efficient pattern recognition capabilities are not readily available for the industrial laboratory. Such data can be included in chemical fingerprinting databases and will make the technique even more useful.
1.3.5. Transmission Electron Microscopy

Transmission electron microscopy is extremely useful for characterizing materials with high resolution imaging from small (submicron) regions of the sample. The information obtained from TEM analysis includes microstructural analysis of metallic, ceramic and polymeric materials as well as chemical and crystallographic information. Certain crystallographic details such as crystal orientation and matrix-precipitate orientation relationships are also possible. The advent of scanning transmission electron microscopes (STEM) has expanded the role of this analytical tool from primarily new chemical structures and failure analysis to activities such as fingerprinting.

TEM and STEM normally use an electron beam (varying from 60 to 300 kilovolts for TEM and 2-50 kilovolts for STEM) to pass through a thin specimen and the resulting intensity distribution is imaged by a photographic imaging system or electron energy loss spectrometer. The interactions between the electron beam and the sample provide several types of information. Chemical and density effects result in intensity variations much like an optical microscope, except that the resolution of the electron microscope is much higher than the wavelength of the electron beam. In addition, diffraction effects from the crystal lattices present in the specimen can also be used to identify or characterize the material.

The capability to attach an energy dispersive x-ray spectrometer on the side of the instrument column allows collection of x-rays generated by interactions between the focused electron beam and the specimen; enabling characterization or identification of the chemical or elemental composition of submicron volumes possible. The limitations of current energy dispersive spectrometer systems is for the atomic number must be 6 or higher.

1.3.6. X-ray Diffraction

X-ray diffraction is extremely useful for identifying and characterizing a large variety of materials. In general, x-ray analysis is restricted to crystalline materials, although some information may be obtained from amorphous and powdered samples. Most x-ray diffraction techniques are rapid and nondestructive and are capable of identifying the phases, grain size, texture, and crystal imperfection. Samples are acceptable in many different forms, depending upon the availability of the material and the type of analysis to be performed.

The X-ray diffraction technique is based upon diffraction effects of x-rays traveling through a sample. This phenomenon is characterized by the Bragg equation:

\[ \sin \theta = \frac{n\lambda}{d} \]
where $\lambda$ is the wavelength of the x-rays and $d$ is the characteristic interatomic distance of the material. A number of spots or fringes are observed at various angles represented by the $\sin \theta$. These spots or fringes result from constructive interference of the diffracted beams and are specific for the crystal lattices of each material. Hence the ability to identify or characterize a material is quite good.

Current x-ray diffraction instrumentation can be portable. Also, there is a substantial amount of software available today supporting the interpretation of x-ray diffraction data as well as databases associated with compilations from different laboratories.

1.3.7. Low Energy Electron Diffraction

Low energy electron diffraction is a technique for characterizing surfaces and overlayers absorbed on surfaces. It can be considered the surface analog of x-ray diffraction. Low energy electrons (30 - 200 electron volts) have limited penetration into materials and consequently provides high sensitivity for periodic atomic structure at the surface. The periodic atomic structures at the surface diffracts a monoenergetic electron beam like a diffraction grating. The diffraction pattern and its intensity distribution can provide information about the atomic positions and the crystallographic features of the surface.

The diffraction pattern obtained during a LEED analysis consists of a small number of spots displayed as a CRT image as whose symmetry of arrangement is that of the surface grid of atoms. Any surface contamination on the surface of the material will significantly affect the diffraction pattern observed and provides a useful capability for discriminating against undesired surface features. Catalogued LEED patterns are available for many single-crystalline materials.
The diffraction pattern obtained during a LEED analysis consists of a small number of spots displayed as a CRT image as whose symmetry of arrangement is that of the surface grid of atoms. Any surface contamination on the surface of the material will significantly affect the diffraction pattern observed and provides a useful capability for discriminating against undesired surface features. Catalogued LEED patterns are available for many single-crystalline materials.

1.4. Surface Science

Surface Science has evolved over the past 25 years to become widely accepted for the evaluation and characterization of solid vacuum compatible materials used in the aerospace industry. Although there are many techniques available, the most practical are:

- ESCA or XPS - Electron Spectroscopy for Chemical Analysis or X-ray Photoelectron Spectroscopy
- AES - Auger Electron Spectroscopy
- SAM - Scanning Auger Microscopy
- SIMS - Secondary Ion Mass Spectroscopy
- ISS - Ion Scattering Spectroscopy

Each of these techniques exhibits certain advantages when used alone, but when two or more techniques are combined they exhibit a synergism that constitutes a better understanding of the process or material being studied.

Except for OM or CM, the primary excitation sources used by these techniques include photons, electrons or ions. The primary particles interact with the surface and emit secondary particles (i.e., photoelectrons, Auger electrons, secondary ions or scattered ions). The emitted secondary particles are analyzed using either an energy or mass analyzer.

The information gained from surface analysis includes the elemental and chemical composition of typically the top $2.0 - 5.0$ nanometers (top few atom layers) of the sample surface. The surface sensitivity of surface analysis is due to the inelastic mean free path of low energy electrons in solids. The energy of the emitted electrons is typically between 30 and 2000 eV. Such low energy particles allow only those originating from the very near surface of the material to escape and be detected. Particles originating deeper within the solid will interact with neighboring atoms loose their energy and be absorbed by the solid or contribute to the background signal. Generally, the elemental sensitivity of surface analysis is of the order of 0.5 % of an atom layer which further makes surface science very sensitive to surface contamination.

Surface science can be used on a wide variety of failure and special materials investigations or characterizations. Some of the materials investigations where surface science has proven most valuable include:

- Chemical Staining of Processed 2219 T87 Aluminum
- Epoxy Primer Pinhole Investigations
The following is a brief discussion of each of the surface science techniques mentioned above, their advantages, disadvantages, types of samples analyzed, method for technique selection and examples.

1.4.1 Electron Spectroscopy for Chemical Analysis and X-ray Photoelectron Spectroscopy

ESCA is a technique which uses an X-ray source of known energy for the primary source of sample excitation (Figure 1.20).

\[
E_{K.E.} = h\nu - E_{B.E.} - \phi
\]

Figure 1.20. Diagram of the ESCA Process.
where $E_{K,E.}$ = Kinetic Energy of the Ejected Photoelectron
$h\nu$ = Incident X-ray Photon Energy
$E_{B,E.}$ = Binding Energy of the Ejected Photoelectron
$\Phi$ = Work Function of the Electron Energy Analyzer

By knowing the analyzer work function, incident photon energy and measuring the kinetic energy of the ejected photoelectron one is able to determine the binding energy of the photoelectron to within typically 0.1 eV. ESCA not only provides the elemental identification of the elements present but also offers the ability to determine the chemical state of the atoms on a solid surface via small shifts in binding energy.

The ESCA technique is such that it can be performed easily on any solid vacuum compatible material. Consequently, another key advantage of ESCA is its ability to analyze both electrically conductive (i.e. metals, metal oxides, etc.) as well as insulating materials (i.e. powders, polymers, catalysts, etc.). ESCA is not limited by the electrical properties of the sample being analyzed.

As an example, an ESCA survey scan of a chemically processed 2219 T87 aluminum surface was analyzed (Figure 1.21). ESCA identified the presence of carbon, oxygen, fluorine and aluminum on its surface. The survey scan was acquired with the x-ray source powered at 250 watts each Mg/Zr and the spectrum normalized to zirconium at 2042.4 eV. Consequently, the kinetic energy at the 0 eV binding energy is the zirconium fermi edge.

![ESCA Survey Scan](image-url)

Figure 1.21. Typical ESCA survey scan of a clean chemically processed 2219 T87 aluminum surface normalized to Zr at 2042.4 eV.
Another key advantage of ESCA is the ease of quantitation with the use of developed peak area sensitivity factors. If the sample is assumed homogeneous within the analysis volume, the intensity of the photoelectron peak is given by the equation:

\[ I = n f \sigma \theta y \lambda AT \]

where

- \( I \) = The intensity of the photoelectron peak
- \( n \) = Number of atoms of an element/cm\(^3\)
- \( f \) = Incident x-ray flux in photons/cm\(^2\)-sec
- \( \sigma \) = Photoionization cross-section
- \( \theta \) = Instrumental angular efficiency factor
- \( y \) = Efficiency of the photoelectron process
- \( \lambda \) = Mean free path of a photoelectron in a solid
- \( A \) = Area of sample analyzed
- \( T \) = Detection efficiency

Thus, solving for the number density of atoms yields:

\[ n = I/(f \sigma \theta y \lambda AT) \]

Defining the denominator as the Atomic Sensitivity factor (\( S \)) reduces the equation to:

\[ n = I/S \]

If we consider the ratio of two elements in a homogeneous matrix we have the expression:

\[ n_1/n_2 = (I_1/S_1)/(I_2/S_2) \]

The generalized expression for determining the atomic fraction of any element in a sample is than represented by the equation:

\[ C_x = (n_x/S n_i) = (I_x/S_x)/S (I_i/S_i) \]

This expression, although far from absolute, offers the ability to perform semiquantitative ESCA analysis to within 10 - 20% on homogeneous samples. When more accurate quantitative analysis is desired, standards of known concentrations which accurately represent the samples of interest must be analyzed. In this way, escape depths, chemical effects, matrix effects, etc. are similar and thus cancel each other.

Quite often the main disadvantage of ESCA is its large analysis area. Conventional ESCA instruments have a very large analysis area. For example, some instruments have a fixed analysis area of about 12 mm\(^2\). Although most samples are sufficiently large and unaffected by this constraint, some samples are far too small for accurate ESCA measurements. One such example is pinholes in epoxy primer. The majority of these anomalies are typically about 1 mm in diameter (< 1 mm\(^2\)) which is 1/12 the analysis area of the instrument. Newer instruments have been developed which render such analyses routine. These small area ESCA instruments,
have variable analysis areas and are able to analyze surface features as small as 75 •m. The minimum effective analysis area of a small area ESCA unit is 0.004 mm\(^2\) which is far below that required for the analysis of pinholes. Small area ESCA was performed on the pinhole anomaly and found to be extremely effective.

1.4.2 Auger Electron Spectroscopy & Scanning Auger Microscopy

Auger Electron Spectroscopy differs from ESCA in that AES uses an electron beam for sample excitation and occurs as a result of a relaxation process (Figure 1.22).

![Diagram of the Auger Process](image)

Figure 1.22. Diagram of the Auger Process. Note that AES is a Three Electron Process.

Whereas ESCA uses an X-ray source to eject photoelectrons for analysis, AES uses a finely focused electron beam to eject core level electrons thus placing the surface atoms in an excited state. The excited surface atoms relax to the ground state via radiation or the Auger process. The energy of the primary electron is typically between 3 and 10 kV. Most AES analyses are performed using 5 kV. The Auger process involves three electrons. The first electron (\(E_1\)) is ejected by the primary electron (\(E_p\)). A second electron (\(E_2\)) from a higher energy level fills the core hole created by the ejection of \(E_1\). The excess energy between \(E_1\) and \(E_2\) is translated to a third electron (\(E_3\)). The third electron is the Auger electron. The Auger process places the atom in a doubly ionized state. The Auger process is independent of excitation source and each element beginning with lithium has its own set of characteristic Auger transitions. AES is also sensitive to 0.5 % of an atom layer or 0.1 atomic %. The Auger electrons are also passed through an electron energy analyzer and detected. The result is an elemental identification of the elements present on the sample surface.

As an example, a typical AES survey scan of the same aluminum surface discussed above identified the presence of carbon, oxygen, sulfur, chlorine, nitrogen, fluorine, copper and aluminum (Figure 1.23). The AES spectrum was acquired using a 5 kV and 1 mA electron
beam. The spectra is displayed as the derivative of the signal \( \frac{d(N/E)}{dE} \) as a function of energy.

![Figure 1.23. Typical AES survey scan of a clean chemically processed 2219 T87 aluminum surface acquired using a 5 kV, 1mA electron beam.](image)

Quantitation of AES spectra is another advantage of performing AES analysis. The method employed is somewhat similar to that of ESCA, however, the derivative spectra or the peak-to-peak is used as a measure of intensity. This method for quantitation is less accurate than the peak area measurement used by ESCA.

One of the key advantages of AES over ESCA is its small analysis area. AES has a high spatial resolution due to the use of a finely focused electron beam for excitation. Older instrument models have a minimum AES analysis area of \( 8 \times 10^{-7} \text{ mm}^2 \) (~ 1 mm diameter), the newer commercially available instruments have analysis areas of the order of \( 5 \times 10^{-10} \text{ mm}^2 \). Regardless of the instrument, AES is orders of magnitude better suited than ESCA to the elemental identification of small surface features.

Still another advantage of AES is its ability to scan the electron beam over an area of the sample and obtain maps showing the elemental distribution of differing elements. This is the SAM feature of the surface analysis instrument. Instruments can operate effectively at magnifications of 1000X. As an example, SAM was found very useful in the investigation of a
weld defect. Here samples were machined from scrapped flight hardware where defects were known from x-ray inspection to exist. The samples were then mounted, introduced into the ultrahigh vacuum analysis chamber (5 X 10^{-10} torr) and fractured in-situ. In-situ fracture exposed the weld defects under UHV which were then analyzed by both AES point analysis and SAM. This approach allowed the identification of the contamination causing this anomalous condition.

Another example of the SAM capability was the analysis of a contaminated aluminum surface. AES point analysis found the composition of the surface to vary from point to point. Additionally, a 250X SEM image contained bright spots randomly dispersed on its surface. The elements present were aluminum, oxygen and carbon. Thus, 250X SAM elemental maps were acquired for these elements (Figure 1.24).

Figure 1.24. 250X SEM (bottom-left) and SAM elemental maps for aluminum (top-left), oxygen (top-right) and carbon (bottom-right).
The SAM maps revealed aluminum and oxygen surface voids which were found to be rich in carbon. The carbon was found to be dispersed islands on the surface of the sample. These analyses were performed at a magnification of 250X.

Although AES is a very powerful analytical tool, it does have disadvantages. A major disadvantage of AES is the types of samples which can be analyzed. Unlike ESCA, AES is not capable of analyzing electrically insulating materials. Due to the use of an electron gun for excitation, samples must be electrically conductive and have a conductive path to ground. Thus, AES and SAM analysis is limited to semiconductive and conductive materials. Furthermore, AES does not offer the same level of chemical state information gained by ESCA. However, AES is typically a quicker technique to perform. AES was not employed in the epoxy primer pinhole investigation due to the fact both the contamination and primer materials are non-conductive.

1.4.3 Secondary Ion Mass Spectroscopy

SIMS is the most sensitive of the surface science techniques to surface contamination. SIMS is typically several orders of magnitude more sensitive than either AES or ESCA. The lower detection limit for many elements by SIMS is of the order of 1 ppm. Furthermore, SIMS is the only surface science technique capable of detecting hydrogen and is sensitive to the entire periodic table of elements.

Secondary Ion Mass Spectroscopy is performed using an Argon inert gas ion gun for excitation and a quadrupole mass analyzer (QMA) for detection. The SIMS process involves the Argon being ionized and accelerated onto the sample surface with typically 0.5 to 4 kV. The incident Argon ions interact with the surface species of the sample through exchange of energy and momentum. The surface species are ejected from typically the top two atom layers of the sample (~ 5 Å) as positive ions, negative ions and molecular fragments (Figure 1.25).

![Figure 1.25 Illustration of the SIMS Process.](image)

The emitted secondary ions and ionic fragments are then focused into an energy filter, passed through a mass analyzer and detected. The SIMS spectra are displayed as the intensity (log or linear scale) vs atomic mass unit (AMU). Similar to ESCA, SIMS analysis can be performed on both electrically conductive and non-conductive materials. One major
disadvantage of SIMS over ESCA and AES is that it is a destructive technique. Once SIMS is performed on a sample surface whether static or dynamic the original as received surface has been destroyed. Consequently, SIMS is usually the only or last technique to be performed on a sample surface.

As an example of the utility of SIMS, analysis was performed on a chemically processed 2219 T87 aluminum surface. Both positive and negative SIMS spectra were acquired (Figure 1.26).

Figure 1.26. Positive (top) and negative (bottom) SIMS spectra of a chemically processed 2219 T87 aluminum surface.
The spatial resolution of SIMS is governed by the spot size or raster area of the incident ion gun. A minimum spot size of 800 \( \mu \text{m} \) translates into an analysis area of 0.5 \( \text{mm}^2 \). Typically, however, a 2 mm X 2 mm raster area is analyzed (4 \( \text{mm}^2 \)).

Another major disadvantage of SIMS is the difficulty in the quantitation of SIMS data. This is due to the fact that the elemental sensitivities for SIMS cover a very wide range (i.e. \( 10^4 \)). SIMS is an excellent complimentary technique to both ESCA and AES. Furthermore, good sample to sample or good to bad comparisons can be made of similar sample materials.

Compared to the AES and ESCA spectra discussed earlier, SIMS is far more sensitive to certain surface species. SIMS identified the presence of sodium, magnesium, potassium, calcium, silicon, titanium, vanadium, chromium, copper, iron, zirconium, and hydroxide on a similar surface analyzed by both ESCA and AES.

1.4.4 Ion Scattering Spectroscopy

Ion Scattering Spectroscopy is similar to SIMS in that it uses an inert gas incident ion beam for sample excitation. ISS uses a monoenergetic low energy (0.1 to 3 kV) helium, neon or argon ion beam as its excitation source. A fraction of the incident ions interact with the sample surface and are scattered from the surface atoms by binary elastic collisions (similar to the scattering of billiard balls of different masses). The ISS process (see Figure 1.27 on the next page) is governed by the equation:

\[
E_1 = \frac{E_0}{(1+\mu)} \left[ \cos \theta + (\mu^2 - \sin^2 \theta) \right]^{1.2} \]

where

- \( E_1 \) = Energy of the Scattered Ions
- \( E_0 \) = Energy of the Incident Ions
- \( M_1 \) = Mass of the Incident Ions
- \( M_2 \) = Mass of the Surface Atoms
- \( \mu \) = \( M_2/M_1 \)
- \( \theta \) = Scattering Angle

An ISS spectrum is a measure of the energy distribution of scattered incident ions leaving the sample. ISS peaks occur at specific values of \( E_1 \). Furthermore, the scattered ion signal is proportional to the number of surface atoms for a given element, probability that the incident ions will remain ionized and differential scattering cross-section. The differential scattering cross-section increases with atomic number such that ISS is most sensitive to higher mass elements. The probability that an incident ion will remain ionized following scattering is \( 10^3 \) and decreases dramatically with subsurface atoms which gives ISS its unique ability to analyze the very top atom layer of a material. Thus, the primary advantage of ISS is its unique surface sensitivity.
As an example, ISS was performed in the characterization of staining of chemically processed 2219 T87 aluminum. Both AES and ESCA identified the presence of copper in the area of the stain. These techniques, however, were unable to identify the elements at the very top of the sample surface. ISS clearly identified the presence of an elevated amount of copper in the stained area compared to an unstained area (Figure 1.28).
Figure 1.28. He\textsubscript{3} ISS survey spectra of a stained (top) and unstained (bottom) chemically processed aluminum surface.

Some of the disadvantages of ISS are similar to SIMS. Quantitation is difficult and the surface of the sample may be changed due to minor sputtering of the surface species during analysis. Still another common problem encountered with ISS is its limitation in mass range and resolution with any given incident ion species. Helium is able to detect the lighter elements beginning with lithium and offers the greatest range of sensitivity. Neon is sensitive to elements greater than magnesium while argon is sensitive to elements greater than titanium.

1.4.5. Technique Selection Considerations for these Techniques

The above discussions explained in some detail the four surface science techniques. It is important to keep in mind that no one technique is considered "THE" most appropriate technique for a given sample. AES and ESCA are by far the two most popular. However, the best approach to be used in a given analysis is to perform multiple techniques on a given sample. Thus, when possible, both ESCA and AES should be performed followed by either ISS and/or SIMS. To assist with the appropriate selection of techniques to be used, refer to the attached Table 1.3 on the next page.
## Table 1.3 Selecting the Appropriate Surface Analysis Technique

<table>
<thead>
<tr>
<th>CHARACTERISTIC</th>
<th>AES/SAM</th>
<th>ESCA or XPS</th>
<th>ISS</th>
<th>SIMS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Excitation Source</td>
<td>Focussed Electron Beam</td>
<td>Mg and/or Zr X-ray source</td>
<td>He, Ne, or Ar ion beams</td>
<td>Primary - Ar ion beam</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Secondary - He &amp; Ne ion beams</td>
</tr>
<tr>
<td>Spatial Resolution</td>
<td>1-5 Micronmeters</td>
<td>4 millimeters</td>
<td>2 x 2 millimeters</td>
<td>800 micrometers</td>
</tr>
<tr>
<td>Depth Resolution</td>
<td>1 - 5 nanometers</td>
<td>1 - 5 nanometers</td>
<td>First atomic layer</td>
<td>Beginning with first atomic layer</td>
</tr>
<tr>
<td>Sensitivity</td>
<td>Good sensitivity throughout the atomic number range. Spectra become more complicated with atomic number.</td>
<td>Similar to AES/SAM</td>
<td>Higher sensitivity for larger atomic number elements</td>
<td>Excellent sensitivity for low atomic number elements. Also sensitive to molecular fragments and isotopes.</td>
</tr>
<tr>
<td>Detection Limit</td>
<td>0.1 Atomic Percent</td>
<td>0.1 Atomic Percent</td>
<td>1 atomic Percent</td>
<td>~1 ppm for many elements. Most sensitive technique.</td>
</tr>
<tr>
<td>Materials</td>
<td>Excellent for metals and thin metal oxide films. Materials must be somewhat conductive.</td>
<td>Excellent for all solid vacuum compatible materials. Least destructive of the four techniques</td>
<td>Best suited for metals and metal oxides. Somewhat surface destructive.</td>
<td>Best suited for metals and metal oxides. Applicable to both conductive and non-conductive materials. Technique is surface destructive by its nature.</td>
</tr>
<tr>
<td>Elemental Identification</td>
<td>Lithium through Uranium</td>
<td>Lithium through Uranium</td>
<td>Lithium through Uranium</td>
<td>Hydrogen through Uranium</td>
</tr>
<tr>
<td>Chemical Bonding</td>
<td>Very limited, e.g. Al vs Al₂O₃</td>
<td>Excellent for differentiating between chemical states of materials</td>
<td>Not applicable</td>
<td>Not applicable</td>
</tr>
<tr>
<td>Ion Etching</td>
<td>Excellent due to small analysis area @ .5 - 50 nm/Min.</td>
<td>Only fair due large analysis area @ .5 - 5 nm/min.</td>
<td>Poor due to low energy ions used.</td>
<td>Good due to small analysis area required by the very nature of the technique. 0.5 - 25 nm/min.</td>
</tr>
<tr>
<td>Depth Profiling</td>
<td>Excellent for elemental composition analysis as a function of depth</td>
<td>Poor for elemental composition as function of depth. Excellent for chemical composition as a function of depth.</td>
<td>Poor</td>
<td>Good for elemental composition as function of depth. Excellent for molecular fragment composition as a function of depth.</td>
</tr>
</tbody>
</table>
A number of thermal and mechanical methods of analysis of materials can be very useful for chemical fingerprinting purposes. Several instruments for frequently used for determining materials' thermal and mechanical properties using temperature programmed analysis include high temperature differential thermal analysis (DTA), thermogravimetric analysis (TGA), thermomechanical analysis (TMA) and differential scanning calorimetry (DSC). Included in this category of instrumentation is also the very useful technique described as rheometric dynamic spectrometry (RDS). These methods have primarily been used to characterize polymers and their precursors; however, numerous laboratories use them to characterize metals and ceramics as well. A general discussion of these methods follows.

High temperature differential thermal analysis consists of instrumentation that measures the temperature of a milligram sized specimen as heat is applied at a controlled rate. The upper limit of these systems is generally around 1500 °C. The heat capacity of the material is easily obtained, as well as latent heat effects such as phase changes or transformations and autoignition. The normal display of the temperature changes during the programmed heating provides indication of contaminants or out-of-specification material. The critical glass temperature, which is a measure of the purity of the material, can also be a useful characteristic for the material.

Thermogravimetric analysis is performed by placing a milligram-sized sample onto a temperature programmed microbalance. The upper limit of most systems is around 1000 °C. Fingerprinting can be performed by determining whether a material's thermal weight loss is characteristic of the normal material. This technique can also be used to evaluate wiring covers, crystallinity, stabilizer addition and the thermal stability of many types of polymeric and ceramic materials.

Thermal mechanical analysis is performed by placing a sample between a vitreous silica platform and a movable silica rod and subjecting the sample to a variable load. In dilatory, the sample is wetted with a liquid and the swelling behavior followed by the measurement of the movement of the silica rod. TMA is performed at various controlled temperatures, where characteristic properties such as thermal relaxation phenomena and tensile compliance in polymers, fibers, and powders can be obtained.

Differential scanning calorimetry is similar to differential thermal analysis, except that the temperature of the sample is monitored for a controlled heat input. The upper limit of most systems is around 500 °C when using aluminum pans to contain the samples. Fusion between the aluminum pans normally occurs when measurements are made above that temperature. Materials properties which are obtained in this technique include glass transition temperature, crystalline transition temperatures, latent heat transformations, and specific heat measurements.

Rheometrics dynamics spectrometry determines the viscous and elastic properties of a material by imposing a cyclical load on the material at programmed temperatures and measuring the resultant torques and body forces. Dynamic viscosity, dynamic modulus and
loss angle can be calculated from this data. Sample temperatures can be programmed from -150 to 400 °C.

1.7. Strategy for Instrument Hierarchy

Analytical instrumentation and instrumental techniques frequently used for chemical analysis and materials characterization were described in the previous section. The theoretical basis, application areas, sample requirements, and limitations of each technique were discussed. The tables and flow charts in this section were developed to serve as guides in the selection and application of instrumental techniques to solve a given analytical problem.

Before selecting specific techniques to be used, the analytical problem should be defined by asking the following types of questions:

What is the nature of the sample?
- Is it a solid, liquid, or gas?
- Is it organic or inorganic?
- Is it a mixture, or a pure substance?
- What is already known about its composition?
- Is it permissible to destroy the sample during testing?
- How much sample is available for analysis
- What is the material's history, and its future?

What kind of information about the sample is desired?
- Is an elemental or molecular analysis desired?
- Is complete identification of all species present required?
- Or, is it sufficient to identify the major and minor components?
- Which specific species or components are to be analyzed?
- What is the required precision and accuracy of the data?

A few of the questions will be immediately answered by visual observation of the sample. Others can be answered readily through discussions or correspondence with the person requesting the analysis. More information may be provided by persons experienced in the testing or processing of the material, or by the material's supplier. The remaining questions will require a physical or chemical measurement to be performed.
An analytical problem can be attacked in three ways:

- Consult with leading experts in the field
- Search the literature for a solution
- Experiment based on theoretical predictions

The first two points should not be overlooked. Do not risk reinventing the wheel by failing to consult others who may have had experience with the same type of problem. These people may be within your company, may be even in your own lab. The companies from whom you have purchased analytical instrumentation may have applications chemists available to help you. Some instrument manufacturers publish newsletters and product bulletins that may provide valuable information. A literature search may turn up the perfect solution to your problem. On the other hand, if the problem involves a proprietary material, literature searches may be of little help. When these sources of information have been exhausted, it is time to experiment.

One source of information about most materials that are used in industrial and laboratory processes that may contain chemical information is the Materials Safety Data Sheet (or MSDS). These information packages are readily available to the user to ensure that personnel safety is always maintained and necessarily do have to identify any toxic precursors which exist in the product.

Unfortunately, no single procedure exists for the selection of the most effective instrumental approach to a given analytical problem. Factors to consider include the capabilities and limitations of the available instrumentation, and the quality of the analytical results versus the cost in time and materials required to obtain them. Table 1.4 surveys the more common instrumental techniques and summarizes each technique's application areas, limitations and sample requirements. This table can be used to identify the techniques that could be applied to the problem at hand. The remaining tables and charts contain additional information that will help the analyst to "narrow the field" and arrive at specific instrumental methods that can be applied to the problem.
<table>
<thead>
<tr>
<th>Method</th>
<th>Applications</th>
<th>Advantages</th>
<th>Method Limitations</th>
<th>Sample Limitations</th>
<th>Sample Size</th>
</tr>
</thead>
<tbody>
<tr>
<td>Atomic Absorption Spectrometry (AAS)</td>
<td>Quantitative and/or trace analysis of a single element for each measurement</td>
<td>Fast, reliable, high sensitivity for some 70 elements, relatively inexpensive</td>
<td>Not applicable to most non-metallic materials or simultaneous multi-element analysis, Small linear response range</td>
<td>Requires time-consuming dissolution of sample or graphite furnace for atomizing solids.</td>
<td>mg to g</td>
</tr>
<tr>
<td>Inductively Coupled Plasma-Atomic Emission Spectrometry (ICP-AES)</td>
<td>Quantitative multi-elemental analysis Determination of trace, minor and major elements</td>
<td>Simultaneous determination of up to 60 elements. Good for refractory materials. Large dynamic range</td>
<td>Limited sensitivity for nonmetals. Expensive</td>
<td>Requires time-consuming dissolution of sample or graphite buffer for atomizing solids.</td>
<td>mg to g</td>
</tr>
<tr>
<td>X-ray Fluorescence Spectrometry (XRF)</td>
<td>Quantitative analysis of all elements of atomic no. &gt; 14. Qualitative determination of all elements with atomic no. &gt;11.</td>
<td>Minimal sample preparation. Inexpensive</td>
<td>Detection limits not as good as AA or ICP/AES</td>
<td>Solid or nonvolatile liquid</td>
<td>mg</td>
</tr>
<tr>
<td>Infrared Spectrometry (IR or FTIR)</td>
<td>Identification and structural determination of materials, including surface adsorbants</td>
<td>Applicable to most materials. Extensive libraries of reference spectra available.</td>
<td>Composition limited to molecular species identified. Medium sensitivity. Trace and minor components can be masked by major components.</td>
<td>Material must contain bonds which undergo dipole moment change during vibration</td>
<td>μg</td>
</tr>
<tr>
<td>Raman Spectroscopy</td>
<td>Identification and structural determination of materials, including surface adsorbants</td>
<td>Identification of non-polar functional groups. Minimal sample preparation.</td>
<td>Low sensitivity. Fluorescence can interfere with Raman signals. Limited libraries of reference spectra. Expensive.</td>
<td>Material must contain bonds which undergo polarizability change during vibration</td>
<td>1 to 100 mg</td>
</tr>
<tr>
<td>Nuclear Magnetic Resonance Spectroscopy (NMR)</td>
<td>Structural determination and identification of both organic and inorganic materials</td>
<td>Determination of molecular configuration and conformation</td>
<td>Applicable only to samples containing magnetic moment. Low sensitivity. Expensive.</td>
<td>Sample must be liquid or soluble solid</td>
<td>1 - 100 mg</td>
</tr>
<tr>
<td>Energy Dispersive X-ray Spectroscopy (EDS)</td>
<td>Elemental inorganic identification of elements</td>
<td>Low level detection</td>
<td>Elements ≥ Na</td>
<td>Sample must be liquid or soluble solid</td>
<td>~ 3 cm diameter</td>
</tr>
<tr>
<td>Method</td>
<td>Applications</td>
<td>Advantages</td>
<td>Method Limitations</td>
<td>Sample Limitations</td>
<td>Sample Size</td>
</tr>
<tr>
<td>---------------------------------------</td>
<td>------------------------------------------------------------------------------</td>
<td>----------------------------------------------------------------------------</td>
<td>----------------------------------------</td>
<td>--------------------</td>
<td>-------------</td>
</tr>
<tr>
<td>Mass Spectrometry</td>
<td>Structural determination and identification of organic and some inorganic materials.</td>
<td>Widely applicable to most materials. Extensive on-line reference libraries available.</td>
<td>Slow Expensive</td>
<td>Sample must be volatized.</td>
<td>0.01 g</td>
</tr>
<tr>
<td>Gas Chromatography (GC)</td>
<td>Separation of multicomponent mixtures of volatile materials.</td>
<td>Selectivity ranges from general to specific</td>
<td>Not applicable to nonvolatile and thermally unstable materials</td>
<td>Material must be volatile and thermally stable</td>
<td>µg to mg</td>
</tr>
<tr>
<td>Liquid Chromatography (LC or HPLC)</td>
<td>Separation of multicomponent mixtures of liquids and soluble solids</td>
<td>Widely applicable to nonvolatile organics. Applicable to thermally unstable materials. Separated materials can be identified by other methods.</td>
<td>No sensitive universal detector. Subsequent analysis by IR or MS necessary to identify components. Moderately expensive.</td>
<td>Must be soluble in one of many suitable solvents.</td>
<td>µg to mg</td>
</tr>
<tr>
<td>Ion Chromatography (IC)</td>
<td>Separation of complex mixtures of ionic species for quantitative analysis. Elemental analysis of organics after decomposition.</td>
<td>Applicable to a wide range of organic and inorganic anions and to many cations.</td>
<td>Analysis of trace species in presence of high concentration species is difficult. Method development is time consuming. Moderately expensive.</td>
<td>Must ionize in solution. Nonaqueous applications limited. Decomposition of organics time consuming.</td>
<td>1 to 5 mg</td>
</tr>
<tr>
<td>Size Exclusion Chromatography (SEC)</td>
<td>Separation of complex mixtures based on molecular size. Determination of polymer molecular weight distribution.</td>
<td>Applicable to polymers. Determines molecular weight distribution.</td>
<td>Calibration time consuming. Moderately expensive.</td>
<td>Must be soluble in limited number of suitable solvents. GPC performed in water.</td>
<td>µg to mg</td>
</tr>
<tr>
<td>Gel Permeation Chromatography (GPC)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Combined Gas or Liquid Chromatography with Mass Spectrometry (GC/MS or LC/MS)</td>
<td>Separation, identification and quantitative analysis of complex mixtures.</td>
<td>Combines separation capability of GC or LC with identification and sensitivity of MS</td>
<td>Slow Method development is time consuming Expensive</td>
<td>Same as GC, LC and MS</td>
<td>20 - 200 ng</td>
</tr>
<tr>
<td>Method</td>
<td>Applications</td>
<td>Advantages</td>
<td>Method Limitations</td>
<td>Sample Limitations</td>
<td>Sample Size</td>
</tr>
<tr>
<td>--------------------------------</td>
<td>--------------------------------------------------</td>
<td>-------------------------------------------------</td>
<td>-------------------------------------------------------------</td>
<td>----------------------------------------------------------</td>
<td>-------------</td>
</tr>
<tr>
<td>Differential Thermal Analysis</td>
<td>Quantitative characterization of materials &amp; contaminants Dilatometry, autoignition</td>
<td>Separates materials by differences in thermal properties in inert or oxidizing atmosphere</td>
<td>Very few; can handle a large variety of solids and liquids, such as foams, films, powders, or fibers.</td>
<td>Small sections that fit in sample crucibles Sample containment can be expensive</td>
<td>mg</td>
</tr>
<tr>
<td>(DTA)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Thermal Gravimetric Analysis</td>
<td>Quantitative characterization of materials, wire coatings</td>
<td>Measures resistance to thermal degradation. Inert or oxidizing atmosphere.</td>
<td>Very few; can handle a large variety of solids and liquids, such as foams, films, powders, or fibers.</td>
<td>Small sections; determined by size of sample pan and autobalance range.</td>
<td>mg</td>
</tr>
<tr>
<td>(TGA)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Differential Scanning</td>
<td>Quantitative characterization of polymers &amp; inorganics by heat absorption, $T_a$</td>
<td>Differences in thermal properties easily measured. Inert or oxidizing atmosphere.</td>
<td>Very few; can handle a large variety of solids and liquids, such as foams, films, powders, or fibers.</td>
<td>Small sections determined by sample pan size.</td>
<td>mg</td>
</tr>
<tr>
<td>Calorimetry (DSC)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Thermal Mechanical Analysis</td>
<td>Semi-quantitative characterization of polymers &amp; organics</td>
<td>Distinguishes materials by differences in thermo-mechanical properties.</td>
<td>Very few; can handle a large variety of solids and liquids, such as foams, films, powders, or fibers.</td>
<td>Small sections determined by sample pan size.</td>
<td>mg</td>
</tr>
<tr>
<td>(TMA)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Rheometric Dynamic Spectrometer</td>
<td>Quantitative characterization of viscous and elastic properties</td>
<td>Measures properties with many geometries</td>
<td>Can handle both solid and liquid samples.</td>
<td>Small sections that fit into test cells.</td>
<td>mg</td>
</tr>
<tr>
<td>(RDS)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Dynamic Mechanical Analysis</td>
<td>Quantitative characterization of viscous and elastic properties $T_e$ and $T_m$</td>
<td>Separates materials by differences in mechanical properties</td>
<td>solid samples</td>
<td>small sections that fit into test cell.</td>
<td>mg</td>
</tr>
<tr>
<td>(DMA)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Optical Microscopy</td>
<td>Qualitative analysis of Particulates</td>
<td>Fast Relatively inexpensive Knowledge and experience of personnel very important</td>
<td>Sample Limitations</td>
<td>Small samples</td>
<td>ng</td>
</tr>
<tr>
<td>X-ray Diffraction (XDS)</td>
<td>compound identification of crystalline materials</td>
<td>Identify crystalline compounds Slow process</td>
<td>Sample Limitations</td>
<td>Small sections of single crystal or powder</td>
<td>$1 \times 10^{-3}$ mm$^3$</td>
</tr>
<tr>
<td>Transmission Electron Microscope</td>
<td>Microstructural analysis of metals, ceramics and polymers.</td>
<td>Very high magnification Slow &amp; expensive</td>
<td>Sample Limitations</td>
<td>small sections of solids Sample preparation can be difficult</td>
<td>$\mu$</td>
</tr>
<tr>
<td>(TEM)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Scanning Electron Microscope</td>
<td>Surface Morphology and high spatial resolution of small samples.</td>
<td>Greater depth of field and resolution than optical microscopy.</td>
<td>Samples must withstand High vacuum</td>
<td>small sections of solids Sample preparation can be time consuming</td>
<td>$\mu$</td>
</tr>
<tr>
<td>(SEM)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Method</td>
<td>Applications</td>
<td>Advantages</td>
<td>Method Limitations</td>
<td>Sample Limitations</td>
<td>Sample Size</td>
</tr>
<tr>
<td>---------------------------------------------</td>
<td>---------------------------------------------------</td>
<td>-------------------------------------------------</td>
<td>-----------------------------------</td>
<td>------------------------</td>
<td>-----------------</td>
</tr>
<tr>
<td>Auger Electron Spectroscopy (AES)</td>
<td>Compositional analysis of conducting surfaces</td>
<td>High Spatial resolution.</td>
<td>Insensitive to He and H</td>
<td>Solids, must be conductive, vacuum compatible</td>
<td>microns down to nm.</td>
</tr>
<tr>
<td>X-ray Photoelectron Spectroscopy (XPS)</td>
<td>Elemental analysis of surfaces and coatings</td>
<td>Nondestructive</td>
<td>Interrogates only top 10 nm.</td>
<td>Solids, vacuum compatible</td>
<td>cm</td>
</tr>
<tr>
<td>Ion Scattering Spectroscopy (ISS)</td>
<td>Identification of elements on surfaces</td>
<td>Depth profiling can analyze for elements through several thousand Angstroms.</td>
<td>Can be time consuming to depth profile several thousand Angstroms</td>
<td>Solid, vacuum compatible</td>
<td>down to 0.05 cm</td>
</tr>
<tr>
<td>Secondary Ion Mass Spectroscopy (SIMS)</td>
<td>Surface compositional analysis Trace element analysis of surfaces and thin films</td>
<td>Good resolution from 1 to 5 nm in depth</td>
<td>Analysis is destructive and can be time consuming</td>
<td>Solid, vacuum compatible Flat surfaces desired</td>
<td>cm</td>
</tr>
<tr>
<td>Low Energy Electron Diffraction (LEED)</td>
<td>Surface analysis of conducting materials</td>
<td>High resolution</td>
<td>Surface preparation can be expensive and difficult</td>
<td>Small sections of solids</td>
<td></td>
</tr>
</tbody>
</table>
Infrared spectroscopy is usually a good place to start. Due to the variety of sampling accessories available, this technique can accommodate most types of samples. Infrared provides information about the organic and inorganic functional groups present, and an estimate of the sample's purity.

Functional groups present in a material can be identified by infrared spectroscopy with the aid of correlation charts, such as the ones pictured in Figures 1.29 and 1.30. These charts summarize the characteristic frequencies of the major functional groups. Frequencies associated with carbon-carbon and carbon-hydrogen bonds are pictured at the top of each chart. Functional groups containing oxygen and silicon atoms are featured in the middle of each chart. Characteristic frequencies of groups containing nitrogen, sulfur, phosphorus, and the halogens are shown at the bottom.
Figure 1.28. Correlation Chart of Infrared Group Frequencies, 1500-3700 cm$^{-1}$
Figure 1.30. Correlation Chart of Infrared Group Frequencies, 600-2000 cm\(^{-1}\)

When cautiously used, correlation charts can be valuable tools in the interpretation of infrared spectra. However, correlation charts alone can seldom unambiguously establish the molecular structure or identify an unknown material. Group frequency ranges are determined empirically from a large number of samples and are
often broad. Group frequency ranges may overlap each other considerably. Because the physical state of the sample (i.e., the sampling technique) can cause band frequency shifts or broadening, the sample should be run under conditions similar to those used during compilation of the correlation chart. Throughout the interpretation process, always keep in mind all of the information known about the sample, such as its physical state, results of other analyses, and elements known to be present or absent.

If the sample is a complex mixture, it may be possible only to identify the major functional groups present. If the material is a pure compound, it can be unambiguously identified if its spectrum exactly matches the reference library spectrum of a known compound. When infrared spectral libraries are not available or no match can be found, the compound's molecular structure can sometimes be deduced by interpretation of the infrared spectrum with the aid of the correlation charts. The following general procedure may be successful:

I. Look at the group frequency region (4000 to 1350 cm\(^{-1}\)) first, concentrating in turn, on the strong bands, then on the medium intensity bands.

II. Look at the 2800 to 3300 cm\(^{-1}\) region to determine the presence and types of carbon-hydrogen vibrations.
   A. No bands at 2800-3300 indicates no C-H bonds. Consider totally halogenated organics, or inorganics.
   B. Bands at 3000 to 3300 cm\(^{-1}\) indicates presence of unsaturated carbon atoms or a halogenated compound.
   C. Bands at 2800 to 3000 cm\(^{-1}\) indicate presence of saturated carbon atoms.

III. Now look at the rest of the group frequency region.
   A. Bands at 1450-1465 cm\(^{-1}\) indicate presence of methyl (-CH\(_3\)) or methylene (-CH\(_2\)-) groups
      1. A band at 1375 to 1380 cm\(^{-1}\) indicates C-CH\(_3\)
      2. A band at 718 to 720 cm\(^{-1}\) indicates a string of 7 or more methylene groups
   B. Bands at 1470 to 1525 cm\(^{-1}\) and 1565 to 1620 cm\(^{-1}\) indicate presence of aromatics. Use Figure 1.29 to determine substitution pattern.
   C. Continue to interpret the strong (and then the medium) intensity bands in the group frequency region. Follow-up on each interpretation by examining other regions of the spectrum. As examples:
1. A band observed at 1715 cm\(^{-1}\) indicates the presence of a carbonyl (C=O) group. Is the compound a carboxylic acid, an ester, a ketone, or an amide? The presence of two bands near 3400 and 3520 cm\(^{-1}\) along with a strong band near 1600 cm\(^{-1}\), would identify the compound as a primary amide.

2. A strong band is observed at 1060 cm\(^{-1}\). Is the compound an ether, a siloxane, or an alcohol? A strong band at 3600 cm\(^{-1}\) would identify the compound as an alcohol.

IV. The following generalizations should be kept in mind:

A. Not all of the bands can be interpreted as group frequencies. Some bands are due to vibration of the molecule as a whole. Other bands are due to combinations of fundamental group frequencies.

B. Aromatic compounds tend to give sharp bands.

C. Spurious bands may appear (i.e., bands not attributable to the sample). For example, bands at 3300-3700 cm\(^{-1}\) and 1600-1800 cm\(^{-1}\) may be due to water in the sample or in the atmosphere within the sample compartment. Similarly, bands near 2325-2350 cm\(^{-1}\) and 670 cm\(^{-1}\) may be caused by the presence of carbon dioxide.

D. The infrared spectrum alone may not provide enough information to identify the compound. Never ignore information from other analyses.

Figure 1.32 is a guide for the selection of a chromatographic method. Selection is based on three sample properties: volatility, complexity, and polarity. Speed, resolution, and the quantity of sample should also be considered. In general, gas chromatography surpasses liquid chromatography in resolution and speed. Capillary columns (or open tubular columns) give the best resolution, but packed columns can accommodate larger samples.
Figure 1.31. Characteristic Infrared Frequencies for Benzene Derivatives
Figure 1.32. Selection of a Chromatographic Method

The sample's volatility, complexity, and polarity are often known or can be surmised based on information provided by the customer. If necessary, a microdistillation can be run to determine volatility. An infrared spectrum will identify functional groups and provide information about the sample's polarity and complexity.

If it is determined that the sample is volatile enough to be run by gas chromatography, Table 1.7 and Figure 1.33 can be used as guides for stationary phase and detector selection. If the sample is nonvolatile or thermally unstable, an LC separation mode can be selected based on the sample's solubility, polarity, and molecular weight according to Figure 1.34. If the sample is believed to be composed of a wide
molecular weight range of species, or if it is thought to contain species with molecular weights over 2000, size exclusion chromatography should be considered.

<table>
<thead>
<tr>
<th>Required Response Selectivity</th>
<th>Required Detection Limit</th>
<th>Appropriate Detector</th>
</tr>
</thead>
<tbody>
<tr>
<td>universal detection (general survey)</td>
<td>10 ppm</td>
<td>TCD, thermal conductivity</td>
</tr>
<tr>
<td>nearly universal (most organics)</td>
<td>0.1 ppm</td>
<td>FID, flame ionization</td>
</tr>
<tr>
<td>compounds containing nitrogen or phosphorus</td>
<td>1 ppb</td>
<td>TED, thermionic emission or NPD, nitrogen-phosphorus</td>
</tr>
<tr>
<td>compounds containing electronegative atoms, halogenated and sulfur containing compounds, anhydrides, nitrates, nitriles, peroxides</td>
<td>1 ppb</td>
<td>ECD, electron capture</td>
</tr>
<tr>
<td>highly selective for many classes of compounds, compound identification possible</td>
<td>1 ppm</td>
<td>MS, mass spectrometer</td>
</tr>
<tr>
<td></td>
<td>1 ppb</td>
<td>SIM, mass spectrometer with selective monitoring</td>
</tr>
</tbody>
</table>

Figure 1.33. Detector Selection for Gas Chromatography.

<table>
<thead>
<tr>
<th>Types of Separations</th>
<th>Required Polarity</th>
<th>Stationary Phase Composition</th>
</tr>
</thead>
<tbody>
<tr>
<td>hydrocarbons, gases</td>
<td>nonpolar</td>
<td>hexamethylenehexacosane</td>
</tr>
<tr>
<td>general purpose (boiling point separation)</td>
<td>nonpolar</td>
<td>poly(dimethylsiloxane)</td>
</tr>
<tr>
<td>aromatics, olefins</td>
<td>nonpolar</td>
<td>poly(dimethyl(diphenyl)iloxane) (80% methyl, 20% ophenyl)</td>
</tr>
<tr>
<td>aromatics, phenols glycols</td>
<td>semipolar</td>
<td>poly(dimethyl(diphenyl)iloxane) (50% methyl, 50% phenyl)</td>
</tr>
<tr>
<td>alcohols, esters, ketones carboxylic acids</td>
<td>polar</td>
<td>polyethylene glycol</td>
</tr>
</tbody>
</table>

Table 1.7. Stationary Phase Selection for Gas Chromatography
Figure 1.34. Selection of a Liquid Chromatographic Mode

Real samples cannot always be classified as totally volatile or nonvolatile. Consider, for example, a polyurethane foam formulation containing extremely volatile components, such as CFC or HCFC blowing agents, along with nonvolatile, polymeric alcohols and siloxanes. In this type of situation, it is necessary to use both gas and liquid chromatographic procedures to isolate each ingredient.

Once a chromatographic separation has been obtained, the separated components can be collected and identified by IR, MS, or NMR. Coupled, or hybrid, instrumental techniques such as GC/MS, GC/IR, or LC/MS permit both separation and identification of unknown components in a single instrumental procedure.

If the elemental composition of the sample is of interest, a qualitative survey analysis can be obtained by XRF provided the sample is nonvolatile. For quantitative elemental analyses, or for volatile samples, an atomic spectroscopic technique can be selected based on the elemental detection limits shown in Figure 1.35. In selection of an
atomic spectroscopic method, the advantages and limitations of each method (given in Table 1.4) should be kept in mind. For example, the lower detection limits provided by furnace (electrothermal) atomic absorption are accompanied by decreased precision and increased analysis time. Both ICP/AES and ICP/MS are capable of multi-element analysis, while only one or two elements can be determined simultaneously by AA.

As stated before, no single procedure exists for the selection of the best instrumental method combination to solve an analytical problem. As an example, consider a polyurethane foam material received as two components, one of which is a mixture of polyols, flame retardants, catalysts, surfactants, and blowing agent. Some of these ingredients are mixtures themselves, and some contain solvents. The ingredients differ significantly in concentration, molecular and elemental composition, and physical and chemical properties. Because of the material's complexity, a combination of instrumental methods is required. FTIR can be used to identify the functional groups present, and to monitor the composition of the polyols which are present at a high concentration level. GC can be used to monitor the more volatile constituents. Because of the wide range of volatilities and concentrations, more than one GC procedure is required. ICP/AES or other atomic spectroscopic methods can be used to measure levels of specific elements, such as phosphorus, silicon, potassium, or tin to monitor the flame retardants, surfactants, and catalysts present in the material.
Figure 1.35. Atomic Spectroscopic Detection Limits (ng/mL).
2.0 CHEMOMETRICS

Chemometrics is a discipline within analytical chemistry concerned with the selection and optimization of instrumental methods as well as the interpretation of data from these chemical analyses. Chemometrics makes extensive use of mathematical and statistical methods with the intent of producing a maximum of concise chemical information. Given these mathematical underpinnings, this section presents a description of a number of the most useful methods together with a discussion of their application to the resolution of problems solved by chemical fingerprinting.

Chemometrics has undergone rapid evolution and proliferation due, in a large part, to the availability of computer hardware and software capable of complex calculations performed on large quantities of data. Although excellent statistical software packages (programs) running on a variety of computer platforms exist, little or no guidance is usually given for the appropriate application of the individual procedure(s). The practitioner, therefore, must employ his combined knowledge of chemistry, statistics, and the nature and source of the data to ensure that the correct computations are performed. It is the purpose of this section to offer some useful advice in these matters.

2.1 Basic Statistics

The purpose of any quantitative chemical analysis is to obtain a valid estimate of the true value of the chemical characteristic being measured. Variation is ever present and inevitably produces a certain amount of uncertainty in the outcome. This uncertainty is called error. All variation and the associated errors can be categorized into four main groups:

- **Common causes** - the collection of factors which produce relatively small and random changes in results and are sometimes referred to as system errors. While these errors can be minimized, they generally cannot be eliminated.

- **Special causes** - factors which sporadically introduce variation over and above inherent system variation. Sometimes called assignable causes because the source can usually be discovered and corrected.

- **Structural causes** - regular systematic changes due to cyclic factors such as day/night, morning/afternoon, and seasonal changes.

- **Tampering** - variation induced by unnecessary adjustments usually made in a vain attempt to compensate for inherent (common cause) fluctuations.

It is imperative that the analyst be able to distinguish between these causes as the appropriate remedial measures for each are quite different. When viewed as a process,
most analytical procedures can benefit substantially from the application of modern statistical process control (SPC) methods.

When an analytical chemist performs replicate analyses on the same sample using the same procedure(s), instrument(s), and reagent(s), the individual results will be found to vary from one to another due to common causes (system error). While these results do differ, they also exhibit a strong tendency to cluster around a certain value. This value is the mean or arithmetic mean, or simply the sample average. Mathematically it is sum of the individual results divided by the number of these results and is denoted by "x". This sample mean is a statistic and therefore an estimate of the parameter known as the population mean which is denoted by "µ". Note that there is a very important distinction between the statistic derived from sampled data and a population parameter. It is seldom if ever that we have available the complete set of observations for the entire population which would allow us to compute the population parameters (µ, s², and s). It is, therefore, necessary to calculate estimates (statistics) of these parameters based on measurements performed on samples drawn from the population (x, s², and s).

\[
\mu = \frac{\sum(x_i)}{N} \\
\bar{x} = \frac{\sum(x_i)}{n}
\]

Where: 
\(x_i=\) individual observations  
\(n=\) number of observations  
\(N=\) total population

The mean is the most useful statistic. Other statistics include the mode, the median, and the midrange.

The mode is defined as that observation which occurs most frequently in the data set.

The median is defined as that observation which, when the data are arranged in order of magnitude, is the middle value.

The midrange (MR) is defined as that observation which is halfway between the largest and the smallest observation.

\[
\text{Midrange} = \frac{(x_{\text{max}} - x_{\text{min}})}{2}
\]

These statistics all provide information about the location of the center of the data and are also known as measures of location. This information, while useful, is less than complete. An adequate description should also include a measure of how much the individual observations differ from the chosen measure of location. Collectively these quantities are known as measures of dispersion or measures of variation and include the range, the mean absolute deviation, the variance, and the standard deviation.
The range is the simplest measure of dispersion and is numerically equal to the difference between the largest observation and the smallest.

\[ \text{Range} = (x_{\text{max}} - x_{\text{min}})/2 \]

The mean absolute deviation is defined as the mean (average) of the absolute values obtained by the subtraction of the arithmetic mean from each observation. It is therefore a measure of how much, on average, each observation differs from the mean.

\[ \text{Mean Absolute Deviation} = \frac{\sum |x_i - \bar{x}|}{n} \]

The variance is a measure of dispersion calculated by summing the squares of the differences of the individual observations from the mean, and then computing the mean of this sum. It must be pointed out that there are two forms of this measure: the population variance which is a parameter and denoted by "\( \sigma^2 \)" and the sample variance which is a statistic and denoted by "\( s^2 \)". As with the two means above, this is an important distinction.

\[ \sigma^2 = \frac{\sum (x_i - \mu)^2}{N} \]
\[ s^2 = \frac{\sum (x_i - \bar{x})^2}{(n - 1)} \]

The standard deviation is defined as the positive square root of the variance and also has two forms: the population standard deviation denoted by "\( \sigma \)" and the sample standard deviation denoted by "\( s \).

\[ \sigma = \left[ \frac{\sum (x_i - \mu)^2}{N} \right]^{1/2} \]
\[ s = \left[ \frac{\sum (x_i - \bar{x})^2}{(n - 1)} \right]^{1/2} \]

Another term frequently encountered is the coefficient of variation (C.O.V.) or relative standard deviation and is defined as the standard deviation expressed as a percentage of the mean.

- (population) relative standard deviation = 100 \( (\sigma/\mu) \) %
- (sample) relative standard deviation = 100 \( (\sigma/\bar{x}) \) %

Note that measure of relative dispersion cannot be used in cases where the individual observations take on both positive and negative values as, for example, after a data transformation which has placed the mean at a value of zero.

A word of explanation about the denominator "\( (n-1) \)" in the above equations. This quantity (the number of observations minus one) is the degrees of freedom (DF) for the
statistic and is, in general, equal to the number of observations minus the number of constants calculated from them. Since the mean (x) must first be calculated before the variance (s^2) can be computed, this "uses up" one degree of freedom and therefore DF = (n-1). If "n" rather than "n-1" were used, it can be shown that the variance would be biased (underestimated) by a factor of (n-1)/n. It is intuitively obvious that as the number of samples increase so does our confidence in the calculated estimates. There is, however, a point beyond which additional samples produce a very small increase in confidence and this value is approximately 30 samples.

When one looks closely at the data, there appears to be a pattern of the dispersion of observations about the central location. This pattern is called a distribution. A distribution can be also be depicted graphically by an "X - Y" plot of the frequencies at which given observations occur ("Y" axis) versus the observation values ("X" axis). A number of distributions exist and include the normal, the binomial, the Poisson, the chi-square, the t, Weibull, and the F. By far the distribution used most often in analytical chemistry is the normal or Gaussian.

The graphical representation of a normal distribution of a large number of observations can be accomplished by grouping the observations into classes, each a small and consistent range of values, and then counting the number of observations belonging to each class. If one next constructs a series of rectangles whose width is the class interval and whose height is proportional to the number of observations in that class, then a histogram is created by placing the rectangles, in ascending order of class magnitude along the "X" axis (left to right) in a contiguous fashion (see Figure 2.1). Note that the individual areas of these rectangles are proportional to the density (number) of observations in those classes. To make additional observations from the population, the probability of obtaining a given value is then determined by the ratio of the area of the class rectangle (to which it belongs) to the total area of all the rectangles. Successive observations occur most frequently at values within the class intervals of those rectangles having the greatest area.

More observations can be made and placed in smaller and smaller class intervals as shown in Figure 2.1(b) - 2.1(c). In the limit, the smooth and continuous bell shaped curve of Figure 2.1 (d) is formed. This is the well known shape of the normal distribution and is a continuous probability density function symmetrical about a central value which is the mean "μ". In fact, the curve (function) is described by the following equation:

\[ y = \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}} \]

Where: \( \pi = 3.14159 \ldots \)
\( e = 2.71828 \ldots \)
The above equation contains two constants, "μ" and "σ", the values of which uniquely determine the location of ("X" axis) and the shape (peaked or broad) of the distribution. A common chemical example of this distribution is the shape of the chromatographic peak. The mathematical term for the shape of this curve is kurtosis; broad curves (large values of "σ") are platykurtic while narrow curves (small values of "σ") are leptokurtic. Note that the curve approaches the "X" axis asymptotically (never reaches zero probability) when moving away from the mean "μ" in either direction.

Figure 2.1 Histograms of Decreasing Cell Size

A standardized form of the normal distribution, used in many statistical tables, is created when the value of "μ" is set to zero and the value of "σ" is made equal to one. This standard normal distribution has been extensively studied and is well documented in numerous tables. Normality is a remarkably valid assumption for many distributions found in both analytical chemistry and science in general.

If the standard normal distribution equation is integrated for values of "X" over the range of minus infinity to plus infinity, the total area under the curve is equal to one, the "X" axis is in units of +/- σ (usually denoted by "z" or "z score"), and the maximum is located at zero. Any real distribution with a known "μ" and "σ" can be transformed into this standard normal format by this equation:

\[ z = \frac{(X-\mu)}{\sigma} \]
This transformation is extremely useful. The area under the curve between any two values of \( z \) is the percentage of the population included within these values. For instance, the area under the curve between \( \mu \) and either \( +1\sigma \) or \( -1\sigma \) is 0.3413 representing 34.13\% of the population. The area between \( -2\sigma \) and \( +2\sigma \) is 0.6826 representing 68.26\% of the total population. Almost all (99.73\%) of the population is bounded by the interval \( -3\sigma \) to \( +3\sigma \). Since these areas also represent probabilities, questions like: "What is the probability of obtaining an observation with a value equal to or less than \( \mu \) minus \( \sigma \)? can easily be answered. The answer is easily calculated to be 15.87\%." This also means that in a sample containing 25 observations we would expect that four will have values less than or equal to \( \mu \) minus \( \sigma \).

The ability to transform sets of observations into their equivalent \( z \) values provides us with a method to scale sets of very different types and numerical ranges for easy comparison. This normalizing technique is also useful in the analysis of multivariate data.

Although the mean \( \bar{x} \) of a set of observations provides an estimate of the population mean \( \mu \), it is very unlikely that \( \bar{x} \) is exactly equal to \( \mu \). There are two reasons for this: (1) the random error in the measurement and (2), the number of observations used to calculate \( \bar{x} \). If another equal number of observations are performed on a sample from the same population, the \( \bar{x} \) from this set will probably not equal the \( \bar{x} \) from the first set. Repeating this process would yield a series of \( \bar{x}'s \) which would, in turn, have a normal distribution about a central value - \( \mu \). This is the Central Limit Theorem and is true even if the population from which the \( \bar{x}'s \) came is not a normal distribution! This distribution is known as the sampling distribution of the mean and has a mean of \( \mu \) and a standard deviation equal to \( \sigma/(n)^{1/2} \). The term \( \sigma/(n)^{1/2} \) is called the standard error of the mean and gives a measure of the uncertainty associated with estimating \( \mu \) from \( \bar{x} \). Since, in practice we seldom know the value of \( s \) and must use the estimate \( \bar{s} \); \( s/(n)^{1/2} \) is usually not identical to \( \sigma/(n)^{1/2} \).

A statistic, \( t \) has been introduced to compensate for both \( s \) and the confidence limit we place on our estimate of \( \mu \). The value of \( t \) depends on both the confidence interval (usually 95\%) and the degrees of freedom (DF) for computing \( s \). We can now state the range of values within which we are confident \( \mu \) exists as follows:

\[
\mu = \bar{x} \cdot ts/(n)^{1/2}
\]

This \( t \) is itself a distribution having the normal or Gaussian shape. The \( t \) tables are rows and columns for confidence interval and degrees of freedom respectively. As the degrees of freedom increase, the kurtosis of the \( t \) distribution approaches that of the normal curve.
The "t" statistic affords a means to perform tests on certain conjectures or hypotheses. For example: does a method have a systematic error when analyzing a sample of known value? In comparing two different analytical methods, do they give results (means) which differ significantly or are the differences due to chance alone? The test procedure will compare the derived 't' statistic to the table of 't critical' values or as usually called, the 't table'. If the calculated 't' for the sample set is higher than the critical 't', then the two methods do differ significantly.

Example. The values from the determination of the percentage of a known analyte(38.9%) are:

38.9% 37.4% 37.1%

Is there any evidence of systematic error?

Calculations using the various software or calculators gives the values for the mean = 37.8% and for the Std. Dev. = 0.964%. Therefore the calculation for t is given by:

\[ t = \frac{(38.9 - 37.8)(3/0.964)^{1/2}}{1.98} \]

From the "t" Table for DF = 2 and 95% confidence level, the critical value for "t" is 4.3. Since the calculated "t" (1.98) is less than the critical "t" value (4.3) there is no reason to suspect a systematic error.

There are also instances when, instead of comparing means, we wish to assess the precision of two different methods which amounts to a comparison of the variances (\( s_1^2 \) vs. \( s_2^2 \)). Another statistical test known as the "F" test permits this kind of comparison by considering the ratio of two variances. By convention the larger of the two variances is always the numerator so that the value of "F" is always equal to or greater than one. If the differences between variances are small, the value of "F" is close to one and the differences are probably due to chance alone. Larger values of "F" imply differences too great to be attributed to random causes. The degrees of freedom for the two variances need not be equal, but both have an influence on the value of "F" and the decisions based upon it. The tables of critical values for "F" are constructed in rows and columns of DF of the numerator and denominator respectively and provide for a selection of confidence intervals as well. Performing the "F" test involves computing the "F" from the variances and for a given confidence interval and DFs, finding the critical value from the "F" tables. Once again, if the computed "F" is greater than the critical value, real (statistically significant) differences in the variances exist.
Example. A proposed method is to be compared to an existing method for the
determination of chemical oxygen demand in a standard sample. Eight
determinations by each method produced the following results:

<table>
<thead>
<tr>
<th>Method</th>
<th>Mean (mg/l.)</th>
<th>Std. Dev. (mg/l.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Existing Method</td>
<td>72</td>
<td>3.31 (s₁)</td>
</tr>
<tr>
<td>Proposed Method</td>
<td>72</td>
<td>1.51 (s₂)</td>
</tr>
</tbody>
</table>

\[ F_{7,7} = (s_1)^2/(s_2)^2 = (3.31)^2/(1.51)^2 = 4.8 \]

From the "F" Table for DF₁ = DF₂ = 7 and 95% confidence level, the critical
value for "F" is 3.787. Since the calculated "F" value (4.8) is larger than the
critical "F" value (3.787), the proposed method is more precise.

The "F" statistic is also a distribution but, unlike the "t", it is a quadratic function and is
skewed ("tails out") to the right.

There arise, from time to time, situations in which one or more of a set of observations
appear(s) to be quite different from others in the set. The term for this observation is
outlier. The outlier, upon examination, may be found to be the result of human error
such as the transposition of numbers or the misplacement of a decimal point. Even after
the correction of these errors, observations which appear to be outliers may still be
present. The analyst is now faced with a difficult decision: should these observations
be retained or rejected? The values of the statistics ("x", "s²", and "s") computed from
the observations will depend on whether or not the outlier(s) are included in the
statistical calculations. One possible reason for the presence of outliers is that our
assumption of a normal distribution is not valid. In this event, a test for distribution or
frequency is appropriate.

Note that in the Central Limit Theorem that multiple determinations of the sample mean
"x" from samples of a population has a normal distribution about the population mean
"μ" with a standard deviation of "σ/√n" which can be estimated by "ts/(n)½." What
about the distributions of the sample variance "s²" and the sample standard deviation
"s"? Like the "F" statistic, the sample variance is a quadratic function and it follows
what is called the "chi-square" distribution. This distribution is the basis for the "chi-
-square" test which is used to determine if an observed distribution of observations is
drawn from a population having a certain theoretical distribution (goodness of fit). The
test is performed by sorting the observations into classes of observed frequencies;
calculating the "chi-square" statistic by taking the sum of the squared difference
between the observed and expected frequencies divided by the expected frequency for
each class. The degrees of freedom (DF) for this calculation is equal to the number of
classes minus one. The calculated "chi-square" value is then compared with the "critical value" found in a table at the desired confidence interval and DF. If the calculated "chi-square" value is less than the critical value, the theoretical distribution is considered to be valid.

If, however, the assumption of a normal distribution is valid, then there is a test called the "Q" test or "Dixon's Q" which can provide some guidance for the accept/reject decision. Like the other test statistics, the critical values for "Q" are given in a table. The test is performed by computing the "Q" ratio and then from the table finding the critical value of "Q" for the desired confidence interval and number of observations. If the computed value of "Q" is greater than the critical value, the suspect observation is rejected. The "Q" ratio is calculated by dividing the absolute value of the difference between the suspect observation and the observation nearest to it by the range of the observations (including the suspect value). Note that the rejection of an outlier can have a dramatic effect on the values of both the variance and standard deviation. The confidence interval implies that there is a small but finite chance of making the wrong decision, hence caution is advised in working with these concepts. If more than one observation in the set is suspect, the situation is more complex and the observations should be repeated or the problem referred to a statistician.

Most modern analytical chemical instruments can usually make accurate observations over a considerable range of values (several orders of magnitude) requiring that the data be treated in a manner that is different from the methods employed in the analysis of repeated single measurements. The usual procedure involves performing observations on samples from populations whose values are known (standards), including a blank (no analyte) sample, and span the range expected for the "unknown" samples. From these data, a "calibration curve" is prepared and, by interpolation, is used to determine the value(s) of the unknown sample(s). Most analytical instruments are designed such that the signal is a linear first order function of the sample value (Figure 2.2). Ideally, this straight line function should pass through the origin (no analyte, no signal) and have a steep slope \((dy/dx)\) as this is a direct measure of the instrument's sensitivity. This ideal relationship can be expressed in this form:

\[
y = a + bx
\]

Where:

- \(a\) = the "Y" intercept (ideally = 0)
- \(b\) = the slope (ideally > 1)
A detailed consideration of this approach raises a number of important statistical issues:

1. Since this line must be "fitted" to the experimental data, which always contains error, what is the "best line" through these data?

2. What are the error estimates for the constants "a" and "b"?

3. What are the error estimates for values predicted by the "best line"?

4. What is the least analyte value that can reasonably be determined (limit of detection)?

5. How valid is the implicit assumption that all errors are in the "Y" values and the "X" values are error-free?

6. If each of the "Y" calibration values is the mean of several observations, are the variances of these values equal?

7. Can a quantitative "figure of merit" be computed to describe how well the "Y" calibration values match the values predicted by the equation of the "best line"?

The most universally accepted answer to Issue #1 is the method of least squares. Using the assumption that all error is in the "Y" values (Issue #5), the "best line" is the one which minimizes the differences between the observed and predicted "Y". Since these
differences (known as residuals) can have both positive and negative values, it is customary to attempt to minimize the "sum" of the "squares" of these residuals. Most statistical software and many inexpensive pocket calculators can perform this task easily and will output values for the constants "a" and "b" as well as a value for the "correlation coefficient" (Issue #7).

It is also possible to calculate a statistic, analogous to the sample variance, for both the "a" ("Y" intercept) and the "b" (slope) constants (Issue #2). These statistics are often provided by the statistical software also.

The estimation of the error in obtaining an "X" value from an experimental "Y" value (Issue #3) is a mathematically complex undertaking and, if required, should include the assistance of an experienced statistician. Formulae for an approximation of this error do, however, exist and suggest that the error will be the least when the "Y" values are nearest to the "centroid" of the "best line."

"Limits of Detection" (Issue #4) considerations arise during trace analysis or when the "blank" standard produces a measurable instrumental response ("Y" value). There are at least two reasons, one chemical and one statistical, for this "blank" response. The chemical reason may be due to "interferences" or "matrix effects" and may be ameliorated by "spiking" of the samples using the "method of standard additions." The statistical reason, however, is more complex and is a subject of much controversy. A reasonable working definition is very method and sample specific and should, therefore, be documented in the reported results.

Our confidence in the assumption of an error free "X" axis (Issue #5) is inexorably tied to our confidence in the accuracy of the calibration standards we use. The need for this assumption is fundamental to the method and consequently the great care and attention given to the preparation, storage, and use of these calibration standards cannot be overemphasized.

If the "Y" values (signals) are the mean of several observations (Issue #6), it is not unusual to find that the variances associated with these means increase with increasing values of the means. Clearly, the values having the smallest variances should exert a greater influence in the determination of the "best line" than those with larger variation. It is possible to assign "weights" to the "Y" values which are inversely proportional to their variances and use these "weighted values" to compute the "best line." Note that the centroid, and along with it, the zone of least error will be moved down the "best line" closer to the origin, thereby improving the accuracy of the smaller sample observations (Figure 2.3).
The "correlation coefficient" (Issue #7) is usually provided along with the values for "a" and "b" in the "best line" equation by the statistical software and is denoted by "r". The values for this statistic range from -1 to +1 with "r = +1" indicating a perfect point-by-point correlation along a "best line" having a positive slope (b > 0). For "r = -1" a perfect negative correlation (b < 0) exists. For "r = 0" there is no correlation ("X" and "Y" are independent). The square of the "correlation coefficient" (r²) is known as the "coefficient of determination" and is a measure of the proportion of the variation of the "Y" values accounted for by the "X" values.

2.2 Design of Experiments

The process of formulating an accurate, reliable, and efficient plan for the investigation of the effects of certain "factors" on the performance of a "system" is the focus of Design of Experiments. An analytical chemist involved in "fingerprinting" is faced with a task broader than just the measurement of a chemical or physical property of a material. The proposed measurements, in many cases, must be evaluated in the context of their ability to provide some or all of the information necessary to successfully fingerprint the product or material under investigation. Design of Experiments methodology is especially valuable for systems with multivariate relationships. Design
Design of Experiments is the planning activity which precedes and interacts with the phases of method development, data acquisition, data treatment/processing, and data interpretation. Design of Experiments can, and has been, successfully applied to a broad spectrum of scientific and engineering investigations.

The approach to a scientific investigation is composed of answering a number of well-phased concise questions. These questions define the analytical problem and are formulated on the prior development of a model of the system under investigation. A complex system may require more than one model, each of which may constitute an independent investigation. The models most commonly used are polynomials of the first or second degree which have been demonstrated to be adequate descriptions for the vast majority of systems. The model will, in turn, define the requirements for obtaining the necessary information including the data and its quality (accuracy, precision, repeatability, etc.).

The Design of Experiments strategy is generally a sequence of plans created to identify, analyze, and optimize the effects of factors on a system or analytical method under investigation. The first phase is a screening design and will identify those factors (and any interactions between them) which have a statistically significant effect on the performance of the system. The screening experiments segregate the "vital few" from the "insignificant many." The next phase will separate and elucidate the "main effects" from the "interactions." The third phase will provide a mathematical model (see above) of the "response surface" for the system and thereby guidance for system optimization. Figure 2.4 illustrates the methodology one might perform is carrying out such a design.
Although all experimentation requires careful planning, some simple investigations need no special considerations (as in the case where only one factor has an effect on the system's performance). Design of Experiments, however, offers considerable advantages in both the economy of experimental resources and maximum production of information especially where there are a number of factors to be investigated. The "classical" approach in which the system's response is explored for each factor in turn while all other factors are maintained at some constant level is not as efficient nor as informative as the "factorial" method of Design of Experiments. The factorial method measures the system's response at all or some fraction of the possible combinations of the chosen (usually two or three) levels of the factors. There are two convincing reasons for the choice of the factorial over the classical method:

1) The factorial detects and estimates any interaction between factors while the classical method cannot.

2) The factorial requires fewer experiments than the classical method for the same precision.

It can be demonstrated that for "k" factors, a classical approach involves "k" times as many experiments as the factorial approach for the same precision. The factorial design approach involves measures for "k" factors with "p" levels for a total of "p^k" experiments. For example, for three factors at two levels each, the factorial method requires 8 experiments, while the classical method requires 24 experiments (see Figure 2.6).

In order to understand the factorial design concept, it is necessary to introduce the idea of "measurement space." Each of the factors is assigned an axis orthogonal to the rest resulting in a "space filling" model encompassing the "experimental volume" of the system. For example, a system involving three factors would be represented as a three
dimensional cube (Figure 2.5). It is not possible to visualize a cube in more than three dimensions (a hypercube), however, the mathematics generalized from three dimensions are valid. An additional benefit of factorial designs is the "hidden replication" inherent in the geometry of the design. For obvious reasons, it is desirable to maximize the "experimental volume" by choosing large ranges (tempered by good judgment) for the factors. This is known as "bold" experimentation.

Factorial experiments are generally performed at either two or three levels of each factor. The two level designs are represented as $2^k$ factorials where "k" is the number of factors. These two level designs will not detect any "curvature" in the data and are limited to linear first order applications. In many cases a "fractional factorial" design is adequate; it

![Factorial Design](image)

Figure 2.5 Factorial Design

is not necessary to perform the full factorial number of experiments. The fractional designs require 1/2 to 1/8 the number of experiments of the full factorial design and are well suited to the "screening" of potential factors to identify those which are critical to the selection and development of an analytical method.

The three level designs are represented as $3^k$ factorials where "k" is the number of factors. These designs will detect "curvature" in the data and are sometimes called
"limited response surface" models. The principle of fractional factorials can be extended to the three level designs and require 1/3 to 1/27 the number of experiments of the full factorial design.

A special form of two level fractional factorial design known as "Plackett-Burman" is a very economical screening design frequently useful when the number of factors are one less than multiples of four (3, 7, 11, 15, 19, 23, 27, 31, etc.).

The design strategy uses some of the experiments from the screening phase as elements of the limited response surface design (by inclusion) and further reduces the number of required experiments. This process of "overlaying" the designs is carried on to the response surface designs with similar economy.

The preparation of any of these factorial designs is not a trivial undertaking and is usually a task for the statistician. The individual experiments are dictated by the geometry of the design and must be performed exactly as specified (even though the analyst may think the specified conditions are unrealistic). Clear written instructions and close supervision should be provided. The data analysis and interpretation are a form of "Analysis of Variance" (ANOVA) and should be performed by, or under the supervision of, a statistician. Experience has shown that success with design of experiment is only achieved by close cooperation between the analytical chemist and the statistician. Figure 2.6 presents a convenient guide for designs involving up to eighteen independent variables.

Figure 2.6 Selection Guide to Experimental Designs

It is the intent of design of experiment to provide information for the selection of factor values which will maximize the response of the dependent variable. Performing this
task is known as "optimization." If no significant interaction between factors exists, this task is relatively simple. In the presence of interactions, however, the task can be quite complex. As stated earlier, the description of the response surface takes the form of a first or second degree polynomial equation in the "k" factors. Visualizing the surface when "k" >2 is not possible and solving the polynomial equation for maximum response in "k" factors is computationally intense. In those situations where the objective is to reach the optimum response and a "model" of the response surface is not required, a procedure known as the "Simplex Method" is an excellent and economical approach. This "Simplex Method" should not be confused with the "Simplex Technique" of linear programming or the "Simplex Mixture" design of formulation problems. A "simplex" is a regular geometric figure whose corners (vertices) are all equidistant. For the optimization of "k" factors, a simplex of "k + 1" vertices is required. Thus for one factor, the simplex is a line segment; for two factors, it is an equilateral triangle; and for three factors, it is a tetrahedron.

A useful concept for determining where to start in a Design of Experiments approach to improving quality in manufacturing operations has evolved through the Taugchi approach. This methodology has become popular in today's quality engineering strategies for achieving target values in production and identifying variables which can be controlled so as to reduce performance variations. A more extended analysis usually requires the use of the approaches shown in Figure 2.6 to optimally determine the responses of factors in an analytical program.
Page intentionally left blank
Page intentionally left blank
2.3 Multivariate Methods

As the title implies, multivariate methods deal with bodies of data representing observations of several (usually more than three) variables on each sample. These data may be composed of measurements of very different kinds including both continuous and discrete variables and may be expressed by a variety of units encompassing a wide range of values. These observations are usually summarized in a data matrix of "p" variables (columns) measured on "n" samples (rows). Thus the data can be considered to describe "n" points (objects) in "p" dimensions (space). Obviously, if "p" is greater than three, visual display of the data becomes a challenge.

"p" variables

\[
\begin{array}{cccc}
  x_{11} & x_{12} & x_{13} & x_{14} \\
  x_{21} & x_{22} & x_{23} & x_{24} \\
  x_{31} & x_{32} & x_{33} & x_{34} \\
  \vdots & \vdots & \vdots & \vdots \\
  x_{n1} & x_{n2} & x_{n3} & x_{np}
\end{array}
\]

"n" objects

"Chemical fingerprinting" is a methodology designed to provide a detailed description of complex chemical formulations for which no single measurement provides adequate information. It is, therefore, a multivariate approach based on measurements developed in designed experiments and addresses four important issues:

- reduction of dimensionality
- multivariate correlations
- multivariate classification
- data summarization.

It is important to keep in mind that the multivariate methods applied to these issues are not always exclusive in that, for example, a method for the reduction of dimensionality may also provide useful information on possible classifications. Graphical presentation of the results of an analysis is a vital and common feature in all of these methods and can often provide the analyst with important new insights.

It is the aim of all multivariate analyses to gain some insight into the structure and information content of these data. The efforts to achieve this aim are generally directed to a few broad issues:

1. Reduction of "dimensionality" - can fewer than "p" dimensions (variables) describe (graph) the data without significant loss of information?
2. Multivariate correlations - are there significant correlations between some of the "p" variates?

3. Multivariate classification/discrimination - are there "natural" groupings in the data and can individual samples be "assigned" to one of these groups?

4. Summarization and presentation of results - what are the "best" methods for conveying the information content of the data?

Prior to actually performing multivariate analysis on experimental data sets, one should consider the following issues:

1. In the beginning, it is not always known exactly which direction the analysis should take and a good deal of data exploration may be required.

2. Given data of many different types and value ranges, should the data be "normalized" prior to analysis and, if so, by which means?

3. If some of the "p" variables are more important than others, a scheme for "weighing" the variables must be selected and applied.

4. In most cases the selection of the "p" variables is based on scientific intuition and imposes a limit on how much analysis can be performed.

5. The nature of the problem and available experimental resources determine the ratio of "n" to "p" (ideally 10:1). This places constraints on the extent of the analysis.

6. Quite often, the human inability to visualize graphically more than three orthogonal axes prevents the analyst from obtaining a necessary "feel" for the data and, hence, a notion of what to do next.

7. Multivariate methods are computationally intense and the "number crunching" capacity of most available computers sets an upper limit on "p", "n", or both.

8. Unlike univariate points on a line, points in "p" space do not have a unique linear ordering and the human desire to impose this condition may result in a misleading view.

Close cooperation between the analytical chemist and the statistician can overcome most, if not all, of the above difficulties and produce insights and understandings of complex multidimensional objects (samples) which would, in the absence of these methods, be obscured.

In the section 2.2 Design of Experiments, the idea of "measurement space" was
introduced and this concept is a fundamental component of the multivariate approach. The individual objects (samples) can be seen as "points" in a space of "p" dimensions. The location of the points (in "p" space) is specified by a set of coordinates which are the values of the "p" variables for that object (sample). An equivalent description is that the "points" are the terminations of "vectors" whose components are the same "p" variables. Now it is possible to understand that "points" which are close to each other in this "p" space are also "close" in their measured variables; the "distance" between them being a measure of their "similarity." If all of the "p" variables are of the same kind (concentration, absorbance, mass abundance, wavelength, etc.) there is no difficulty with this simple model. If, however, the variables are of a mixture of kinds with quite different "values," the simple model may be distorted by the larger "values" and consideration should be given to "scaling" the variables by some "normalizing" technique. By far the most common normalizing technique is the "z score" method whereby the variables are each transformed to have a mean of zero and a variance of one. The effect of this transformation is to place all of the variables on an equal basis and if this is not the case (all variables equally important), the variables must then be individually assigned "weights" by the analytical chemist (here, the statistician can only provide advice). These decisions concerning "normalization" and "weighing" of the variables are important data "pre-treatment" considerations, but, given the preservation of the original "raw data," are not irrevocable.

For those conditions where "p" is greater than three, visual examination of the vector terminations (or points) is not possible. However, the principles of Euclidean Geometry are also equally valid for vectors in "p" dimensions. The true length of the vector is equal to the square root of the sum of the squares of its coordinates. The Euclidean distance "d" between the terminations of any two vectors is simply the square root of the sum of the squares of the difference between their respective "p" coordinates. These relationships are summarized for 2, 3, and "p" dimensional space in Figures 2.7, 2.8, and
Figure 2.7  Two Dimensional Case (Plane Geometry)

Three points (origin and the terminations of \( R_1 \) & \( R_2 \)) define a plane (two dimensions).

Figure 2.8. Three Dimensional Case (Solid Geometry)

\[
R_1 = [(x_1)^2 + (y_1)^2]^{1/2}
\]

\[
R_2 = [(x_2)^2 + (y_2)^2]^{1/2}
\]

\[
d = [(x_2 - x_1)^2 + (y_2 - y_1)^2]^{1/2}
\]
2.9. Note that the two vectors ("R₁" and "R₂") and the distance line "d" in each case form a triangle and only requires two dimensions to display the graphical features. This holds for the comparison of any two objects (points) in "p" dimensional space. Given a set of "n" objects (samples) defined by "p" variables, it is possible to calculate all of the \(n(n-1)/2\) pairs of "d" distances between the objects.

\[
\begin{align*}
R₁ &= [(x₁)² + (y₁)² + (z₁)² + \ldots + (p₁)²]^{1/2} \\
R₂ &= [(x₂)² + (y₂)² + (z₂)² + \ldots + (p₂)²]^{1/2} \\
d &= [(x₂ - x₁)² + (y₂ - y₁)² + (z₂ - z₁)² + \ldots + (p₂ - p₁)²]^{1/2}
\end{align*}
\]

Figure 2.9  Multi (p) - Dimensional Case (Hyperspace)

A distance between variables can also be calculated by means of a transformation of the correlation matrix. The correlation matrix is a square symmetrical matrix providing for each pair of variables, a correlation coefficient "r". The diagonal of the matrix is unity for all self-correlations. The most direct transformation is made by subtracting the absolute value of the individual correlation coefficients from one (1). If negative correlation coefficients are to be considered an indication of dissimilarity, then one should use the signed values in place of the absolute values. Having done this we now have a pseudo distance table for the variables.

The Euclidean distance measure discussed above is only one of many possible metrics or measuring systems. If each of the "p" variables are normally distributed (which is most often the case), then the points in "p" space have a characteristic form or pattern. This pattern is dependent upon both the individual variances and the correlations between the variables. If, for instance, "p" = 2, "r" (correlation coefficient) = 0 (no correlation) and the variances are equal, the locus of points equidistant from the centroid of the pattern is a circle. Given some degree of correlation between variables and/or unequal variances, the locus becomes an ellipse. With "p" > 2, the locus of points equidistant from the centroid is the surface of an ellipsoid ("p" = 3) or hyperellipsoid ("p" > 3). Note that the major diameter of the ellipse (or ellipsoid) is in the direction of greatest variance. The Euclidean metric defines the locus of points equidistant from the centroid to be a circle ("p" = 2), the surface of a sphere ("p" = 3), or a hypersphere ("p"
3) and distances (to the centroid) based on this metric can, in a statistical sense, be misleading. A metric which does take into account these statistical considerations (unequal variances and correlations) is the Mahalanobis distance. Although this metric is often superior to the Euclidean, its computation is more complex and involves matrix algebra to find the matrix inverse of the covariance matrix: a job best left to a statistician and computer.

A closer look at the multivariate ideas and techniques having the most relevance to the search for chemical "fingerprints" and signatures is now in order.

Issue #1. Reduction of dimensionality

Two techniques, Multi-Dimensional Scaling (MDS), and Principal Component Analysis (PCA), have direct applications to the "fingerprinting" problem in that both provide a picture in two or three dimensions of the similarities (or differences) between the signatures of the samples. These methods not only facilitate interpretation, but simplify the mathematics (fewer dimensions or variables to handle). Additional benefits include the elimination of redundancies (correlations) in the original data and the possibility that the abstract "new" dimensions (variables) may have some "real" physical significance (reification).

The technique of MDS is designed to produce a "map" depicting the relationships between the objects (samples) based on a table (see above) of distances between all pairs of objects. As noted above, these distances are usually expressed in the Euclidean metric, but not exclusively so. The MDS procedure first finds from the table the two objects which are maximally distant. These objects are then plotted on the map's central horizontal axis at maximum separation. Next, the object at maximum distance from the first two is identified and, by an arbitrary convention, is plotted either above or below the central horizontal axis to form a triangle whose sides are the distances between the three objects. The remaining objects are then in turn "fitted" into this triangular configuration. An initial "goodness of fit" between these configuration distances and the distance table is then calculated and used iteratively to change each object's map coordinates until no further improvement in "fit" can be made. At this point the final map is drawn. Most MDS software give the user some control of:

1. Map dimensionality (usually 1, 2, or 3)
2. Assignment of "weights" for the variables
3. Choice of "normalizations" for the variables
4. Choice of the distance metric
5. The maximum number of allowed iterations
6. Map "convergence" parameters
7. Map editing - size, position, and rotation

The method of Principal Component Analysis (PCA) is a transformation of the original variables into a completely new set with reduced dimensionality, the principal components. While there exist the same number of new principal components as original variables, there is also the expectation that the first few principal components (2 or 3) will account for most or possibly all of the information content in the original data set. PCA is general in its scope, makes no assumptions about the nature of the original variables, and uses no mathematical model. The principal components (PCs) generated by the procedure have the following properties:

1. Each PC is a linear combination of the original variables. That is, each is equal to a sum of the original variables each having unique coefficients.

2. For each PC the sum of the squares of the coefficients is unity.

3. The first PC is that linear combination having the greatest variance.

4. The succeeding PCs are uncorrelated with previous PCs and contain the greatest amount of the remaining variance.

A consequence of 3 and 4 above is a set of variables (PCs) which are uncorrelated with one another and, therefore, mutually orthogonal and are arranged in decreasing order by the percentage of the total variance they contain.

The PCA procedure can be explained in geometric terms. If the original "p" variables are all normally distributed, the collection of the "n" points (samples) in "p" space will be a hyperellipsoid having a definite centroid located at the coordinates of the common mean. Finding the PCs corresponds exactly to finding the principal diameters of the hyperellipsoid and placing them in decreasing order of length. The locations of the projections of the "n" points onto these diameters as measured from the centroid are the individual PCs.

One should understand that the PCA method is not independent of the scale of the original variables and the application of "weightings" to some of these variables can have a profound effect on the results. If the original variables are of quite different types, of different units, or of different scales, consideration should be given to normalizing or standardizing these data prior to PCA. If a correlation analysis reveals that the original variables are all uncorrelated, or nearly so, there is little to be gained from a PCA as the probable result would be a computationally expensive coordinate transformation.

In practice, the entry point for the PCA is the matrix of correlations between the original variables (or a variance/covariance matrix). The matrix is a square ("p" x "p") symmetrical about the diagonal. Mathematical operations are performed on this matrix.
and result in "p" eigenvalues together with "p" eigenvectors whose "p" components are the coefficients described in 1 and 2 above. The percentage each eigenvalue has of the sum of all the eigenvalues is the percentage of the total variance it contains.

**Issue #2 - Multivariate Correlations**

In the section *Basic Statistics* we discussed briefly the calibration of an analytical instrument using the *method of least squares*. That is we developed the equation:

\[ y = a + bx \]

where: \( a \) = the "y" intercept, \( b \) = the slope

This is an example of a *univariate linear regression*. We also calculated a "figure of merit" for this equation called the *correlation coefficient* "\( r \)" with values ranging from -1 through 0 to +1. Recall that large absolute values of "\( r \)" indicate a close relationship (correlation) between "\( x \)" and "\( y \)."

In the section *Design of Experiments* an extension of this idea was presented when the "fitting" of a "model" was used to define the response surface. In fact, using a first degree polynomial equation in the "\( k \)" factors to predict the value of the dependent variable (response) is an example of a *Multiple Regression Analysis*. Multiple regression analysis is a very useful and general statistical procedure for the study of the relationship (correlation) of a single variable (response) to a linear combination of two or more other variables (predictors), including a constant term and a random error term.

\[ y_1 = b_0 + b_1 x_1 + b_2 x_2 + b_3 x_3 + b_4 x_4 + \ldots + b_p x_p + e_p \]

Where: \( y_1 \) = response variable  
\( b_0 \) = constant term  
\( x_1 \ldots x_p \) = predictor variables  
\( b_1 \ldots b_p \) = regression coefficients  
\( e_p \) = random error term (residual)

An example of a chemometric application of this method is the study of possible relationship of a measured physical property of a material (tensile strength, viscosity, hardness, etc.), to a group of chemical measurements made on the same sample of the material.

As with the univariate regression above, a "figure of merit" can be computed for the result of a multiple regression analysis and it is known as the *coefficient of determination* ("\( r^2 \)") and its values range from 0 to 1. The exploration of these correlations is complicated by the large number of possible linear combinations of the predictor variables and many statistical software programs provide a means to automate the search for an optimum combination. There are usually three approaches to the problem and all are based on a user supplied criterion (rule) for the determination of the
optimum combination:

1. A forward selection of predictors.
3. A stepwise regression (a mixture of #1 and #2).

Having completed these searches, it is left to the user to make the important decision on which linear combination of predictors and coefficients will become the model. The software can provide some assistance in the form of "F" statistic values and sometimes graphical plots of the predicted values versus the measured values for each combination can be examined.

Example: Determination of the component ratio for polyurethane foam insulation for an aerospace system.

An important requirement in the preparation of a cured thermal protection polyurethane foam material is the control of the two part component ratio A and B. A study to determine the true relative amounts of the 'A' Component (isocyanate) and the 'B' Component (polyol) was conducted using instrumental analytical methods (FTIR, ICP, and TGA) to determine the true ratio of these components after cure has been completed. The application of these analytical methods together with the use of multivariate linear regression techniques permit the determination of the true 'A':'B' ratio with an error of less than ten percent (10%).

Fingerprinting work performed on this foam material has demonstrated that FTIR, ICP, and TGA are the instrumental methods best suited to the ratio determination.

A single lot of foam material for which the results from the full complement of acceptance tests were available was used to prepare accurately weighed "cup" samples (in triplicate) of 0.60:1.00, 0.80:2.00, 1.00:1.00, 1.20:1.00 and 1.40:1.00 'A':'B' ratios. A complement of "production sprayed" samples were also prepared for correlation analysis. The ability to produce these samples (cured foam material) from such extreme ratios is a testimonial to the robust nature of this formulation. The individual samples were then each subjected to FTIR, ICP, and TGA analyses. Both a forward and backward stepwise multiple linear regression analysis was performed on the results from each method and on a composite of all of the results. The resulting predicting equation are of the form:

\[ Z = a + b_1 x_1 + b_2 x_2 \ldots + b_i x_i \]

where:
- \( Z = 'A':'B' \) ratio
- \( a = \) intercept (forced to zero)
- \( b = \) regression coefficient
- \( x = \) predictor variable
From the analysis of fourteen wavelengths in the infra-red spectrum, 1510 cm\(^{-1}\) and 1067 cm\(^{-1}\) were identified as the critical predictor variables. These two intensities remained the critical predictors in the composite regression analysis. Partial "f" tests and "t" tests confirmed the significance of these two predictors at the 95% confidence level.

The final prediction equation defines a three dimensional plane (See Figure 1.):

\[
Z = 0.02349x_1 - 0.02494x_2
\]

where: \(x_1 = 1510\) cm\(^{-1}\)
\(x_2 = 1067\) cm\(^{-1}\)

![Response surface for two wavelengths used in this study.](image)

This equation produces an adjusted coefficient of determination \(r^2 = 0.999\) and an interval error estimate of \(-0.071\) meaning that 99.9\% of the 'A':'B' ratio is explained over the entire ratio interval with a probable error no greater than 7\%. The ICP and TGA regressions each had a coefficient of determination of approximately 0.95 and interval error estimates of 0.10 (10\%). A graphical representation of the response surface is shown below.

Conclusions and Recommendations
An on-going study to determine if foam aging has a significant effect on the analytical results is being completed. Consideration will also be given to the expansion of this effort to include the correlation of the foam's physical and mechanical properties to both the 'A':'B' ratio and its analytical predictors. Alternatively, the knowledge gained in this study could be applied to the adjustment of some or all of the major material or process factors to produce the desired 'A':'B' ratio. It is now possible to accurately determine whether, in the foam application process, the desired 'A':'B' ratio has, in fact, been achieved. FTIR analysis, in particular, revealed that the ratio of infra-red light absorption be a pulverized sample of foam at 1410 cm\(^{-1}\) and 1067 cm\(^{-1}\) is a direct measure of the relative amounts of the 'A' and 'B' components reacted to form the cured foam.

Example. Using factor analysis to determine the reliability of a spectroscopic analysis by determining the number of significant factors

Consider the case where a spectroscopic analysis is performed in the presence of other potential absorbants and system noise. The analyst records measurements for two peaks in the absorption spectrum of the desired compound at different concentrations. This approach can be used to answer the following questions:

(a) How many compounds are in the mixture?
(b) What are the intensities at these wavelengths for these compounds?
(c) What is the concentration of each compound in each experiment?

The theoretical absorption for peak 2 should be twice that of peak 1; however, the data is recorded as:

<table>
<thead>
<tr>
<th>Wavelength 1</th>
<th>Wavelength 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.8404</td>
<td>2.0296</td>
</tr>
<tr>
<td>1.8982</td>
<td>4.1676</td>
</tr>
<tr>
<td>3.1831</td>
<td>5.8166</td>
</tr>
<tr>
<td>4.1665</td>
<td>7.9562</td>
</tr>
<tr>
<td>5.3620</td>
<td>9.8650</td>
</tr>
<tr>
<td>5.9200</td>
<td>11.6624</td>
</tr>
<tr>
<td>7.0987</td>
<td>13.8794</td>
</tr>
<tr>
<td>8.1588</td>
<td>16.3139</td>
</tr>
<tr>
<td>8.9828</td>
<td>18.0685</td>
</tr>
<tr>
<td>10.3643</td>
<td>20.3791</td>
</tr>
</tbody>
</table>

The data can be graphed according to the figure below. Note that the linear fit is not very good. Variations from the linear relationship may be due to system noise or the effects of unknown absorbants.

Ordinarily the analyst would determine the best linear fit to the data by performing a
linear regression on this data. One would then obtain the equation:

\[ I_1 = 0.5063I_2 + 0.02125. \]

This equation is represented by the line drawn through the data points in the graph. In most cases this approach is satisfactory; however, there is always a lingering question about if this one fit is sufficient.

Another useful approach is to reduce the dimensionality of the data using principal components and see how many factors are needed to accurately model the data. A regression and principal component analysis using a commercial software package provides the following information:

<table>
<thead>
<tr>
<th>Source</th>
<th>DF</th>
<th>Sum of Squares</th>
<th>Mean Square</th>
<th>F Ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model</td>
<td>1</td>
<td>87.016642</td>
<td>87.0166</td>
<td>2101.656</td>
</tr>
<tr>
<td>Error</td>
<td>8</td>
<td>0.331231</td>
<td>0.0414</td>
<td></td>
</tr>
<tr>
<td>C Total</td>
<td>9</td>
<td>87.347873</td>
<td>0.0000</td>
<td></td>
</tr>
</tbody>
</table>

Note that the sum of squares for the one degree of freedom model is much larger than the error variance., hence the F ratio is very high. Obviously the analyst is able to apply the least squares fit to the data with confidence.

Further results from the analysis gives:

**Response: Wavelength 1**

<table>
<thead>
<tr>
<th>Summary of Fit</th>
<th>Rsquare</th>
<th>0.996208</th>
</tr>
</thead>
<tbody>
<tr>
<td>Root Mean Square Error</td>
<td>0.203479</td>
<td></td>
</tr>
<tr>
<td>Mean of Response</td>
<td>5.59748</td>
<td></td>
</tr>
<tr>
<td>Observations (or Sum Wgts)</td>
<td>10</td>
<td></td>
</tr>
</tbody>
</table>

The response parameters show an \( r^2 = 0.996 \) for the 10 data points. Hence the linear fit is good. The response curve for this data set also shows a good fit in the plot:
For the principal components portion of the analysis, one then decomposes the original data into principal components of the form:

\[ X_1 = x_1 \cos f + x_2 \sin f \]
\[ X_2 = -x_1 \sin f + x_2 \cos f. \]

This analysis reveals the following information:

| Eigenvalue | 1.9981 |
| Percent:   | 99.9051 |

which indicates that the principal component at wavelength 1 accounts for 99.9% of the information, thereby confirming the earlier observations.

**Issue #3 - Classification and Discrimination**

The method of *Cluster Analysis* is directed to the task of identifying groups of similar objects based on the observational data. This analysis is usually performed to search for the existence of some *natural* grouping in the data. The method is relatively simple, straightforward, and produces an easily understood *dendrogram* or hierarchical *tree*. Cluster analysis, like MDS, is based on *distances* and can be applied to the study of the relationships between individuals (samples) as well as variables.

There are two basic approaches to the clustering problem:
1. The *divisive* approach which begins with all of the objects in a single cluster and proceeds to subdivide this cluster into separate clusters based on dissimilarities.

2. The *agglomerative* approach which begins with each object in its own cluster and proceeds to form other clusters based on similarities.

By far, the agglomerative approach is the most popular and, therefore, the one we will examine. The method requires measures of similarity between all objects being studied and this is usually a distance matrix. Any data which can be used to create such a matrix is, therefore, suitable and the previous comments on the distance metric apply. The four general steps in the clustering procedure are:

1. Assign each object to its own unique cluster.
2. Locate the *shortest* distance in the matrix and merge these two clusters.
3. Update the distance matrix for this cluster's distance to the remaining clusters.
4. Repeat steps #2 and #3 until there is only one cluster.

During this procedure a *linked list* is generated which contains, in order, the mergings (fusions) and the distance at which they occurred. This list is then used to draw the dendrogram or tree. The rules by which the distance matrix is updated in step #3 above are known as the *clustering algorithm* and there are five popular ones:

1. The single linkage algorithm
2. The complete linkage algorithm
3. The average linkage algorithm
4. The centroid algorithm
5. Ward's method

Implementation of these algorithms on a single data set will generally produce five distinct dendrograms and this raises the question "Which is best?" The best will usually be the dendrogram with the most faithful reproduction of the original distance matrix. The distance between any two clusters (objects or groups) is the distance level at which they both first appear in the same cluster (fusion level). With this understanding, a distance matrix can be constructed from the dendrogram and then compare the corresponding entries to the ones in the original distance matrix and even calculate a goodness of fit in much the same (RMS Error) way as for the MDS map. In fact both cluster analysis and MDS constitute summaries (in different visual forms) of the information contained in a distance matrix.

The analyst must make many of the same basic decisions prior to a cluster analysis as
was necessary for MDS, namely:

1. Should the variables be normalized?
2. Should "weights" be assigned to the variables?
3. Should principal components be used and if so, how many?
4. Which algorithm should be used?
5. If variables instead of samples are being studied, how should the distance matrix be calculated?
6. Which "goodness of fit" calculation should be used and what is the decision value?

A major criticism of cluster analysis is that it will by its very design always find clusters even when "homogeneous" or "clusterless" data are analyzed. Any clusters identified by this method should be confirmed by MDS and scatter plots. The analyst should be aware that the results of cluster analysis depend a great deal on the distance matrix and the particular algorithm used.

The method of Discriminant Analysis deals with the problem of developing an optimal separation rule to distinguish between two or more known (a priori) groups of objects (samples) based on the measurements of several variables on all of the objects. The method could be used, for example, to investigate how well samples of acceptable and unacceptable materials can be separated using a number of chemical measurements applied to both. The intent is to develop a rule which would, on the basis of the chemical measurements, correctly allocate a subsequent sample to one or the other group (acceptable or unacceptable). While the advantages of such a rule are great, there is a certain probability of misallocation and the rule must be chosen to minimize this risk.

There are a number of ways to view this task. First, it can be seen as an extension to multivariate observations of the method of analysis of variance wherein the "between group" variances are maximized while at the same time the "within group" variances are minimized. Like multiple regression analysis, discriminant analysis is concerned with finding an optimal linear combination of the original variables (or a subset thereof) which satisfies these variance objectives. That is to say, the optimal linear combination (an equation having a constant term and coefficients for all included variables) would, when applied to all objects in both groups, yield means for the groups which have the greatest possible numerical difference and variances for each group that are as small as possible. Application of this rule would then create a condition where the centers (means) of the groups are far apart and there is minimal overlap between their distribution curves (minimum variances). The calculated numerical result for any individual object (sample) is known as a discriminant score and the equation's individual
coefficients can be viewed as weights for their respective variables.

$$DF = b_0 + b_1x_1 + b_2x_2 + b_3x_3 + b_4x_4 + \ldots + b_px_p$$

Where: $DF =$ discriminant function  
$b_0 =$ constant term  
$x_1 \ldots x_p =$ variables  
$b_1 \ldots b_p =$ discriminant coefficients

An equivalent geometrical interpretation is to find the centroids of the hyperellipsoids of the groups in "p" (or less) space which are maximally distant from one another. It is preferred that the distance be the Mahalonobis distance based on the normalized (z-scored) variables. Then the degree to which the hyperellipsoids interpenetrate each other sets the limit on the method's ability to properly allocate an object to a given group. Having located the group centroids and objects in "p" (or less) space, the simple method of "k" nearest neighbors can be used to assign a new object to the proper group. The method assigns the new object to the group having the largest percentage of the "k" neighbors closest to it. The value of "k" is usually taken to be a small odd number in order to prevent "tie" votes. Given a rather large number of assigned objects in the groups, this method is rapid, straight forward, and makes good statistical sense. The other methods of making assignments require the calculation of discriminant score value known as the cutting score and this can be a complicated matter if the population size of the groups differ significantly.

Since the mechanics of discriminant analysis and multiple regression analysis have mathematically much in common, the statistical software programs usually provide the same types of options for exploring the data: "forward" selection, "backward" elimination, and "stepwise" operations on the original variables. Here too, it is sometimes possible to examine a graphical plot of the separation results.

**Issue #4 - Presentation of Results**

While it cannot be denied that tables and listings of calculations and results efficiently present the essential hard facts, graphical displays or other visual representations of multivariate data are extremely useful tools for their examination and presentation. Contour maps (response surfaces), similarity maps (multidimensional scaling and principal components analysis), dendrograms/trees (cluster analysis), and scatter plots (regression analysis) are all intuitive and easily understood by everyone. A deep understanding of the mechanics behind the generation of these visualizations is not a prerequisite to reading the information they contain and this should be a major consideration when presenting results to the non-statistician. Frequently a picture is not only the best, but the only way to convey the complex relationships between multivariate objects. Beyond their value in data presentation, the graphical techniques are indispensable in the exploring and formulating stages of analysis. A great deal of good and practical advice on the design and preparation of a variety of charts and graphs is contained in the book by W. S. Cleveland and the two books by E. R. Tufte (see
Final Comments and Advice

With most multivariate data sets there are almost always a variety of alternative analytical approaches. The choice of which method is most appropriate depends on the data type(s) and the objective(s) of the analysis. Unfortunately, no one method or technique is necessarily the best choice and it is often wise to use several methods to explore different facets of the data. There are two ways to view the data set: as the relationships between the individuals (samples) as defined by the variables and their values, and as the relationships between variables defined either by their pairwise correlations or their variance/covariance structure. In the first case we examine the "n" individuals in the "p" variables space while in the second we see the "p" variables in "n" space.

Before undertaking any multivariate analysis, the univariate summary statistics for each variable should be thoroughly studied. The mean, variance, standard deviation, range, the skew, the kurtosis, and the z-scores can all be easily calculated using available software. This variable by variable "quick look" should be supplemented by histograms to verify distribution assumptions and to screen for "outliers." Next, the correlation matrix should be created and examined, followed by a scrutinizing of the scatter plots of all pairs of variables. The correlation matrix contains only the simple linear correlations and if the relationships are more complex, the scatter plots together with "eye-brain" device may uncover them. Recall that if the variables are all relatively uncorrelated, a principal components analysis is probably pointless. The degree to which some of the variables are correlated will give some guidance in the investigation of possible linear combinations. At this point it is advisable to consider the question of normalization of the variables and whether some of the variables should be assigned weights.

A statistical computer software program will obligingly perform any of its analyses on a data set whether or not the method is appropriate. Consider the problem to be solved and your objectives, then use common sense (the computer has none).

Just as in the univariate case, multivariate outliers can exist and if scanning the data by eye fails to detect them, consider using the Mahalanobis distances from the common centroid as a discriminator.

Finally, recognize that multivariate analyses do not always give "text book" answers, even after a great deal of exploration. It is also very difficult to know when one has exhausted all of the many possible approaches. One of the best ways to develop skills and gain experience in these methods is to use available software to analyze the classical (known) data sets (many of the data sets are included in the books listed in the Reference Materials).
3.0 REFERENCES


Other Reference Materials

This section contains recommended books that we have found beneficial. They are listed according to topic.

Chemometrics


Computers


Design of Experiments


Graphical Methods


Instrumental Analysis


**Microspectroscopy**


**Multivariate Analysis**


**Spectral Interpretation**


**Spectral Interpretation - ESCA/Auger**


**Spectral Interpretation - Infrared and Raman**


**Spectral Interpretation - Mass Spectra**

118


**Spectral Interpretation - NMR**


**Statistics**


**Surface Science**


**Quality Assurance - Quality Control**

### List of Acronyms

<table>
<thead>
<tr>
<th>Acronym</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>AAS</td>
<td>Atomic absorption spectroscopy</td>
</tr>
<tr>
<td>AES</td>
<td>(1) Atomic emission spectroscopy, (2) Auger electron spectroscopy</td>
</tr>
<tr>
<td>AFS</td>
<td>Atomic fluorescence spectroscopy</td>
</tr>
<tr>
<td>AA</td>
<td>Atomic absorption</td>
</tr>
<tr>
<td>AI</td>
<td>Artificial Intelligence</td>
</tr>
<tr>
<td>AMU</td>
<td>Atomic mass unit</td>
</tr>
<tr>
<td>ANOVA</td>
<td>Analysis of variance</td>
</tr>
<tr>
<td>ASCII</td>
<td>American Standard Code for Information Interchange</td>
</tr>
<tr>
<td>ESCA</td>
<td>Electron spectroscopy for chemical analysis</td>
</tr>
<tr>
<td>ATR</td>
<td>Attenuated total reflectance</td>
</tr>
<tr>
<td>AUFS</td>
<td>Absorbance units full scale</td>
</tr>
<tr>
<td>CC</td>
<td>Capillary column</td>
</tr>
<tr>
<td>CFC</td>
<td>Chlorofluorocarbons</td>
</tr>
<tr>
<td>CI</td>
<td>Chemical ionization</td>
</tr>
<tr>
<td>CILO</td>
<td>Computer Integrated Laboratory Operations</td>
</tr>
<tr>
<td>COV</td>
<td>Coefficient of variation</td>
</tr>
<tr>
<td>CPU</td>
<td>Central processing unit</td>
</tr>
<tr>
<td>CRT</td>
<td>Cathode ray tube</td>
</tr>
<tr>
<td>DF</td>
<td>Degrees of freedom</td>
</tr>
<tr>
<td>DOE</td>
<td>Design of experiments</td>
</tr>
<tr>
<td>DSC</td>
<td>Differential scanning calorimetry</td>
</tr>
<tr>
<td>DTGS</td>
<td>Deuterated triglycerine sulfate</td>
</tr>
<tr>
<td>ECD</td>
<td>Electron capture detectors</td>
</tr>
<tr>
<td>EDS</td>
<td>Energy dispersive X-ray Spectroscopy</td>
</tr>
<tr>
<td>EI</td>
<td>Electron impact</td>
</tr>
<tr>
<td>ES</td>
<td>Expert Systems</td>
</tr>
<tr>
<td>ET</td>
<td>External Tank</td>
</tr>
<tr>
<td>FAAS</td>
<td>Flame atomic absorption spectroscopy</td>
</tr>
<tr>
<td>FAB</td>
<td>Fast atom bombardment</td>
</tr>
<tr>
<td>FES</td>
<td>Flame emission spectroscopy</td>
</tr>
<tr>
<td>FID</td>
<td>Flame ionization detector</td>
</tr>
<tr>
<td>FTIR</td>
<td>Fourier transform infrared spectroscopy</td>
</tr>
<tr>
<td>GC</td>
<td>Gas chromatograph</td>
</tr>
<tr>
<td>GC/FID</td>
<td>Gas chromatographic with a flame ionization detector</td>
</tr>
<tr>
<td>GC/MS</td>
<td>Gas chromatography/mass spectrometry</td>
</tr>
<tr>
<td>GLC</td>
<td>Gas-liquid chromatography</td>
</tr>
<tr>
<td>GSC</td>
<td>Gas-solid chromatography</td>
</tr>
<tr>
<td>HCFC</td>
<td>Hydrochlorofluorocarbons</td>
</tr>
<tr>
<td>Abbr.</td>
<td>Description</td>
</tr>
<tr>
<td>-------</td>
<td>-------------</td>
</tr>
<tr>
<td>HPLC</td>
<td>High performance liquid chromatography</td>
</tr>
<tr>
<td>IC</td>
<td>Ion chromatography</td>
</tr>
<tr>
<td>ICP</td>
<td>Inductively coupled plasma</td>
</tr>
<tr>
<td>ICP/AES</td>
<td>Inductively coupled plasma/atomic emission spectroscopy</td>
</tr>
<tr>
<td>IEC</td>
<td>Ion-exchange chromatography</td>
</tr>
<tr>
<td>IR</td>
<td>Infrared spectroscopy</td>
</tr>
<tr>
<td>IRE</td>
<td>Internal reflection element</td>
</tr>
<tr>
<td>ISS</td>
<td>Ion scattering spectroscopy</td>
</tr>
<tr>
<td>LAN</td>
<td>Local area network</td>
</tr>
<tr>
<td>LC</td>
<td>Liquid chromatography</td>
</tr>
<tr>
<td>LLC</td>
<td>Liquid area network</td>
</tr>
<tr>
<td>LIMS</td>
<td>Laboratory Information Management System</td>
</tr>
<tr>
<td>LHDS</td>
<td>Laboratory Host Data System</td>
</tr>
<tr>
<td>LNTB</td>
<td>Laboratory Network Test Bed</td>
</tr>
<tr>
<td>LSC</td>
<td>Liquid-solid chromatography</td>
</tr>
<tr>
<td>MAD</td>
<td>Mean absolute deviation</td>
</tr>
<tr>
<td>MAPTIS</td>
<td>Materials and Processes Technical Information System</td>
</tr>
<tr>
<td>MCT</td>
<td>Mercury cadmium telluride</td>
</tr>
<tr>
<td>MR</td>
<td>Midrange</td>
</tr>
<tr>
<td>MS</td>
<td>Mass spectrometer</td>
</tr>
<tr>
<td>NMR</td>
<td>Nuclear magnetic resonance</td>
</tr>
<tr>
<td>NPD</td>
<td>Nitrogen-phosphorus detector</td>
</tr>
<tr>
<td>NP</td>
<td>Normal phase (LC term)</td>
</tr>
<tr>
<td>NS</td>
<td>Nonpolar stationary phase (GC term)</td>
</tr>
<tr>
<td>P</td>
<td>Polar stationary phase (GC term)</td>
</tr>
<tr>
<td>PC</td>
<td>(1) Personal computers; (2) Packed column (GC term)</td>
</tr>
<tr>
<td>PMT</td>
<td>Photo multiplier tube</td>
</tr>
<tr>
<td>QC</td>
<td>Quality control</td>
</tr>
<tr>
<td>QEL</td>
<td>Quality Evaluation Laboratories</td>
</tr>
<tr>
<td>QLI</td>
<td>Quality Laboratory Instructions</td>
</tr>
<tr>
<td>QMA</td>
<td>Quadrupole mass analyzer</td>
</tr>
<tr>
<td>RDS</td>
<td>Rheometrics dynamic spectrometry</td>
</tr>
<tr>
<td>RI</td>
<td>Refractive index</td>
</tr>
<tr>
<td>RP</td>
<td>Reverse phase (LC term)</td>
</tr>
<tr>
<td>SA</td>
<td>Solid adsorbent (GC term)</td>
</tr>
<tr>
<td>SAM</td>
<td>Scanning Auger microscopy</td>
</tr>
<tr>
<td>SEC</td>
<td>Size exclusion chromatography</td>
</tr>
<tr>
<td>SEM</td>
<td>Scanning electron microscopy</td>
</tr>
<tr>
<td>SFC</td>
<td>Supercritical fluid chromatography</td>
</tr>
<tr>
<td>SIMS</td>
<td>Secondary ion mass spectroscopy</td>
</tr>
<tr>
<td>SIM</td>
<td>Selective ion monitoring</td>
</tr>
<tr>
<td>SOP</td>
<td>Standard operating procedures</td>
</tr>
<tr>
<td>SPC</td>
<td>Statistical process control</td>
</tr>
<tr>
<td>SRM</td>
<td>Standard Reference Materials</td>
</tr>
<tr>
<td>TCD</td>
<td>Thermal conductivity detector</td>
</tr>
<tr>
<td>Acronym</td>
<td>Description</td>
</tr>
<tr>
<td>---------</td>
<td>------------------------------</td>
</tr>
<tr>
<td>TED</td>
<td>Thermionic emission detector</td>
</tr>
<tr>
<td>TGA</td>
<td>Thermo-gravimetric analysis</td>
</tr>
<tr>
<td>TMA</td>
<td>Thermal Mechanical analysis</td>
</tr>
<tr>
<td>UV</td>
<td>Ultra-violet</td>
</tr>
<tr>
<td>XPS</td>
<td>X-ray photoelectron spectroscopy</td>
</tr>
<tr>
<td>XRF</td>
<td>X-ray fluorescence spectroscopy</td>
</tr>
</tbody>
</table>