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ABSTRACT

Nonintrusive measurements of density, temperature, and their turbulent fluctuation levels have been obtained in the boundary layer of an unseeded, Mach 2 wind tunnel flow. The spectroscopic technique that was used to make the measurements is based on the combination of laser-induced oxygen fluorescence and Raman scattering by oxygen and nitrogen from the same laser pulse. Results from this demonstration experiment are compared with previous measurements obtained in the same facility using conventional probes and an earlier spectroscopic technique. Densities and temperatures measured with the current technique agree with the previous surveys to within 3% and 2%, respectively. The fluctuation amplitudes for both variables agree with the measurements obtained using the earlier spectroscopic technique and show evidence of an unsteady, weak shock wave that perturbs the boundary layer.

INTRODUCTION

The development of spectroscopic techniques for the investigation of turbulent, compressible flow phenomena is directed towards the simultaneous measurement of mean values and fluctuation levels for multiple gasdynamic variables [1]. One such technique has been developed for measuring density, temperature, and their turbulent fluctuations in high-speed, compressible flows using laser-induced fluorescence (LIF) of oxygen in combination with Raman scattering from oxygen and nitrogen [2,3]. The principal advantage of this approach is that flow seeding is unnecessary and measurement uncertainties due to temporal or spatial seed nonuniformity are thereby avoided. In this report we present measurements obtained with this LIF/Raman (LIF/R) technique in a turbulent, supersonic air flow. Following a description of the LIF/R technique and a discussion of the instrumentation, profiles of density, temperature, and their fluctuation amplitudes are presented for the flow boundary layer. These profiles are compared with previous results which were obtained from conventional probe and nitric-oxide (NO)-LIF measurements in the same facility [4,5]. The favorable agreement between the present and previous surveys demonstrates the ability of the LIF/R technique to accurately characterize the thermodynamic variables in unseeded, turbulent, supersonic flows.

LIF/R TECHNIQUE

Experimental investigations into the spectroscopy of both the LIF and Raman processes that guided the development of the LIF/R technique are detailed in previous publications [2,3]. The following discussion is a brief outline of the important aspects of LIF/R spectroscopy relevant to its implementation as a flow diagnostic technique.

The temperature measurement capability of the LIF/R technique is based on the use of a narrow-band, ArF-excitation laser to induce fluorescence from a single ro-vibrational transition of the oxygen Schumann-Runge system. A notable feature of this system is that the upper electronic state of the transition is perturbed by an unbound state that provides a predissociative deexcitation path for resonant oxygen molecules. For the vibrational bands accessible to the ArF laser, the predissociative depopulation rate of the upper state is at least $10^5$ times faster than either collisional quenching or fluorescence decay. Since only one in $10^8$ molecules fluoresce, predissociation results in a reduced signal level; but its rapidity effectively precludes collisional quenching. Another manifestation of the strong predissociation is that natural lifetime broadening dominates the transition lineshape [6] and greatly reduces the sensitivity to collisional (and Doppler) broadening and shift. With negligible influence from collisional processes, the collected fluorescence is more easily interpreted since it is linearly dependent on density through the initial state population. If the oxygen mole fraction is constant and the laser fluence not excessive, the expression for the fluorescence signal, $S_F$, can be written as

$$S_F = K_F \rho f_i(T)$$

(1)

for narrow-band excitation of a single transition, following the derivation in [2]. In the above expression, $K_F$ is an optical and spectroscopic constant, $\rho$ is density, and $f_i(T)$ is the temperature dependent Boltzmann population of resonant $O_2$ molecules in the ground state. For temperatures below 350 K, the temperature dependence of the fluorescence signal arises mainly from the thermal change of the rotational energy distribution and only the lowest vibrational level ($v'' = 0$) has significant population. The expression for $f_i(T)$ for this temperature range is

$$f_i(T) = (2K'' + 1) \frac{2\theta_i}{T} \exp\left[-K''(K'' + 1)(\theta_i/T)\right]$$

(2)

where $K''$ is the ground state rotational quantum number, $\theta_i$ is the characteristic rotational temperature (2.1 K), and $T$ is temperature.

Depending on the anticipated range of temperatures, the laser is tuned to resonance with a rotational transition that has been selected for suitable temperature sensitivity and signal level. Figure 1 illustrates the fluorescence signal temperature dependence at constant density given by equation (2) for two different rotational transitions of the $(4 \rightarrow 0)$ vibrational band. Signals for each transition are normalized by their respective values at 300 K. The transition with the higher rotational quantum number, $R19$, has greater temperature sensitivity over the whole range as
shown by the steeper slope of the solid line. Signal strength for the R19 transition is sufficient for temperature measurements above 100 K. However, the signal is very weak below 100 K due to relatively low population, and the greater population of the P15 transition makes it a better choice for measurements at lower temperatures.

There have been several demonstrations of temperature measurement using LIF of oxygen at constant pressure [2,3,7-11]. Most of these experiments were directed toward high-temperature applications, such as flame diagnostics, where the higher vibrational levels of the ground electronic state are significantly populated. Another technique for measuring temperatures at varying density or pressure relies on a two-transition approach [12]. However, if density is measured independently during the same laser pulse, the density dependence of the LIF signal can be accounted for and temperature can then be derived from the fluorescence variation of a single transition [13].

Spontaneous Raman scattering by oxygen and nitrogen molecules provides a convenient, independent measurement of density that is also used to account for the density dependence of the fluorescence. Any temperature sensitivity of the Raman signals is removed by spectrally integrating the total Q-branch scattering. Since the spontaneous Raman cross-section varies as frequency to the fourth power, Raman scattering is more efficient at ultraviolet wavelengths. In addition, the oxygen Raman cross-section is considerably enhanced by near-resonant contributions within the Schumann-Runge band that increase the scattered light level by a factor of 22 over the expected level near 193 nm [14].

The Raman signal, $S_R$, for constant air composition can be simply written as

$$S_R = K_R \rho$$

(3)

where $K_R$ is an optical and spectroscopic constant. Density measurements are obtained directly from equation (3) and temperature measurements are derived from the variation of the fluorescence signal (equ. (1)) divided by the Raman signal (equ. (3)),

$$S_F/S_R = (K_F/K_R) f_0(T)$$

(4)

Equations (3) and (4) are the basic relations used in this work. In practice however, the ArF laser induces fluorescence from additional transitions due to spectral overlap with both narrow-band and unlocked, broad-band radiation. (Not all of the amplified laser emission is narrow-band when the laser is operated in the multipass amplifier configuration.) For this reason a numerical model of the $O_2$-LIF process [2] is used to evaluate equation (4).

**EXPERIMENTAL CONSIDERATIONS FOR THE LIF/R TECHNIQUE**

The optical configuration for implementation of the LIF/R technique is shown in Fig. 2. Pulses from a tunable, ArF-excimer laser are delivered to the wind tunnel at a rate of 10 Hz and are focussed to a 0.5 mm by 1 mm spot at the measurement location. Portions of the beam are split off before and after the wind tunnel and directed to photodiodes to account for laser-pulse energy fluctuations and varying attenuation. The LIF and Raman signals emanating from the laser probe volume are collected with a twolens telescope (magnification = 3.3) and dispersed by a 0.32 m spectrometer fitted with a 1200 line/mm holographic grating. An entrance slit width of 0.5 mm limits the observed length of the probe volume to 0.15 mm for the pointwise measurements. The dispersed spectrum is recorded by an optical multichannel analyzer (OMA) and stored in a personal computer along with the photodiode signals from the same laser pulse. Both the OMA and the gated integrator are controlled by a single personal computer using PC-DOS and multitasking software. Exposure of the OMA to the 15 usec laser pulse is controlled through gating of the intensifier on the photodiode array. As shown on the figure, the OMA is triggered at twice the laser repetition rate to clear the array of accumulated signal from previous laser pulses. These signal remnants are caused by slow radiative decay of the intensifier phosphor (P-20 for this OMA) and they generate a persistent image that can compromise single-pulse spectral measurements [15].

An investigation of the magnitude of the image persistence effect for the OMA used in this work and its reduction for different array cleaning schemes is summarized in Fig. 3. The figure shows the image persistence, which is defined as the percentage of the original image read off of the array following a trigger pulse, as a function of time. With the block at $t = 0$, the OMA has been exposed to light signals induced by laser pulses at a rate of 10 Hz (0.1 sec between pulses). At $t = 0$, the laser light is blocked, but the OMA array is still read at each trigger pulse. Signals read from the array after the light is blocked represent the sum of decaying signal remnants from previous exposures that remain as an image on the long-lived intensifier phosphor. The circular symbols represent the basic image persistence level of the OMA for an array temperature of 20°C with no cleaning between laser pulses. Signals are only read from the OMA each time the laser fires. At the time of the first laser pulse following the block, 20% of the initial signal remains. After five pulses, the remaining signal has decayed to about 3% of the original level. The solid line through the circles is a power law fit to the data ($x^{-n}$). If a single cleaning pulse is supplied to the OMA between laser shots, the image persistence is substantially reduced, as shown by the square symbol distribution. With the additional read between laser shots, 4% of the original signal level remains on the array at the time of the second laser pulse and about 1% is left.

![Experimental arrangement for the application of the LIF/R technique to the investigation of a turbulent, supersonic boundary layer flow.](image)
The wind tunnel used for the demonstration measurements is a Mach 2, blow-down facility that has a rectangular cross section for providing two-dimensional flow. A schematic representation of the tunnel is shown in Fig. 4. Clean, dry air at high pressure and room temperature is expanded through a Laval nozzle into a long, slightly-divergent flow channel which was designed to provide fully turbulent flow and to accommodate boundary layer growth on the top and bottom walls. At the measurement location, 0.76 m downstream of the throat, the test section is 32.5 mm high by 63 mm wide, the free stream Mach number is 2.06, and the boundary layer is 12.1 mm thick. Laser beam access is provided through two ultraviolet-grade fused silica windows and light signals are collected through an identical window in the top wall. For the current setup, the long dimension of the rectangular laser spot is oriented perpendicular to the bottom wall of the tunnel and this limits the spatial resolution of the present boundary layer survey to 1 mm. A pressure tap is located on the bottom wall at the measurement location directly opposite the collection window and is used to record the static pressure during the run and calibration measurements. Since the blow-down is a constant-volume expansion process, both the stagnation pressure and stagnation temperature decrease during the run. A thermocouple upstream of the Laval nozzle and a pressure tap in the storage vessel are used to monitor the changing reservoir conditions. The time-averaged stagnation conditions and important boundary layer properties for the flow facility are summarized in Table 1. Flow centerline pressure and temperature at Mach 2.06 are nominally 32 kPa and 157 K for the given stagnation conditions. The total run duration is 15 sec and the useful steady-flow measurement time is about 13 sec. For a laser repetition rate of 10 Hz, at least 90 signal records can be acquired during a typical wind tunnel run. Previous surveys of the boundary layer by pitot...
LIF/R MEASUREMENT RESULTS

The implementation of the LIF/R technique in the wind tunnel requires that spectra collected during the tunnel run be compared with an emission spectrum acquired at known density and temperature for calibration of the signal levels. This aspect of the technique is illustrated in Fig. 5, which compares an averaged spectrum from the wind tunnel boundary layer with a calibration spectrum acquired at the same location in still air after the tunnel run. The laser is resonant with the R19 (4 → 0) transition and each spectrum represents the average of 95 spectra that are normalized by laser-pulse energy measurements. The mean flow and mean calibration conditions for the spectra are given in the figure legend. Signal levels for the emission features are plotted versus wavelength. The O2 and N2 Raman transitions are located on the left and the O2-LIF emission features on the right are identified by the difference in their final and initial ground state vibrational quantum numbers. The fluorescence transitions used for the temperature measurements are \( \Delta v = 4, 5, 6, \) and 7. A lower density during the wind tunnel run is directly measured by the reduction in Raman signal levels. The lower level of the mean LIF signal for the wind tunnel run is due to both the decreased density and a lower temperature. The Raman and LIF signals for each laser pulse are obtained by integrating the selected features over their respective wavelengths for each individual spectrum. Density and temperature values for each pulse during the wind tunnel run are then derived by comparing the signal levels with the mean calibration values at the known reference conditions. An additional result of the calibration spectrum acquisition for quiescent air is the simultaneous determination of the instrumental noise level in the absence of turbulent fluctuations. Single-pulse departures from the mean of the measured property values during the wind tunnel run are due to a combination of turbulent fluctuations and instrumental noise, and each contribution is statistically independent of the other. Therefore, the square of the calibration deviations can be subtracted from the square of the tunnel run deviations to remove the instrumental noise from the total fluctuation level and determine the turbulent fluctuation amplitude. Typical values of the instrumental noise level for these experiments were 4% for density and 3% for temperature.

Mean flow property measurements from the LIF/R boundary layer survey are compared in Fig. 6 with results from the previous experiments [4]. All measured flow properties are normalized by their respective values in the free stream at the flow centerline and the measurement locations are shown as the distance from the bottom wall normalized by the boundary layer thickness, \( \delta \). The upper dashed line is the temperature distribution that was derived from pitot-probe and thermocouple-probe surveys. The flow temperature shows a monotonic decrease from the adiabatic wall value to the free stream value. In the absence of an external pressure gradient, the probe-measured static pressure is constant through the boundary layer, as shown by the solid line. The density variation was obtained from the temperature and pressure distributions using the ideal gas equation of state and is shown by the lower dashed line. (Although previous measurements of the mean flow properties were obtained with the NO-LIF technique [4], the results are not shown because they did not differ from the probe-measured distributions.) Open symbols represent measurements of mean flow density and temperature using the LIF/R technique. The mean values obtained thus far agree with the previous measurements to within 3% for density and 2% for temperature. Through the ideal gas equation of state, the LIF/R-measured densities and temperatures are used to derive the static pressure distribution, which is denoted on the figure by the solid squares. As expected, static pressure is constant to within 2% through the boundary layer.

The uncertainty levels for these LIF/R measurements are relatively high due to a strong instrumental noise contribution from the image intensifier that is used to gate the OMA. This intensifier noise was larger than the photon-statistical noise contribution for the measured signal levels. Consequently, the total instrumental noise was effectively constant for a large range of signals and the uncertainty for both variables can be calculated using the following relations,

\[
\frac{\Delta \rho}{\rho} = \left[ \left( \frac{\Delta \rho}{\rho} \right)^2 + 2 \left( \frac{\Delta S_{\text{I}}}{S_{\text{I}}} \right)^2 \right]^{1/2}
\]
\[
(DT/T) = \left[ (B - 1) \frac{\Delta T}{T} \right] + 2 \left( \frac{\Delta S_{F}}{S_{F}} \right) + 2 \left( \frac{\Delta S_{R}}{S_{R}} \right) \right]^{1/2}
\]

In the above expressions, \( \Delta \rho / \rho \) is the density uncertainty and \( \Delta T/T \) is the temperature uncertainty. \( \Delta S_{F}/S_{F} \) and \( \Delta S_{R}/S_{R} \) are the LIF and Raman signal uncertainties and both are given by the measured instrumental noise levels discussed earlier (0.03 and 0.04, respectively). The subscript \( r \) refers to the value measured during the tunnel run and the subscript \( c \) refers to the calibration value. 

The uncertainties in the reference values of density and temperature were about 1%. Using these values and the above relations, the uncertainties for the LIF/R boundary layer survey were 5.5% for density and 2.5% for temperature. Agreement between the LIF/R measurements and previous results is within the uncertainty for both variables.

Comparisons of the fluctuation amplitude distributions measured by the LIF/R technique with those from the previous measurements are shown in Fig. 7a for temperature and in Fig. 7b for density. The root-mean-square (RMS) fluctuation amplitude is the average deviation level divided by the local mean property value. Both variables are again plotted as a function of the nondimensional distance from the bottom wall. The solid line in each figure is a cubic spline interpolation of the hot-wire anemometer measurements of Logan et al. [5].

In Fig. 7a, the RMS temperature fluctuation amplitudes measured with the LIF/R technique are denoted by the open circles and the NO-LIF values from [4,5] are represented by the solid circles. Each of the independently measured temperature fluctuation distributions shows the same basic trend throughout the boundary layer. The maximum temperature fluctuation amplitude of about 4.5% occurs near \( Y/\delta = 0.6 \), and in that region the optically-measured amplitudes are slightly greater than the hot-wire measurements.

For the RMS density fluctuations in Fig. 7b, the LIF/R measurements are the open triangles and the NO-LIF results from [4,5] are shown by the solid triangles. In the figure, there is some disagreement between the measured distributions that is quite pronounced near \( Y/\delta = 0.6 \). Both of the optically-measured profiles show a substantially higher value for density fluctuations in this region than indicated by the hot-wire measurements. In the previous studies, this increase in density fluctuation level was attributed to an unsteady, weak shock wave that moves intermittently through the measurement location. Histograms of more than 300 single-pulse density measurements from the NO-LIF technique [16] show a bimodal distribution in this region, which supports the hypothesis that an unsteady wave is present. While the preliminary LIF/R density record also indicates a bimodal distribution near \( Y/\delta = 0.6 \), there are not yet a sufficient number of measurements to be conclusive. As described in [6], the relative change in flow properties caused by the unsteady wave movement can be evaluated using the weak shock relations [17].

\[
\frac{\Delta \rho}{\rho} = \frac{1}{\gamma - 1} \frac{\Delta T}{T}, \quad \frac{\Delta P}{P} = \gamma \frac{\Delta \rho}{\rho}
\]

where \( P \) is the static pressure and \( \gamma \) is the ratio of specific heats. The symbol \( \Delta \) here represents the change in properties from the upstream side of the weak shock to the downstream side. For a diatomic gas with \( \gamma = 7/5 \), the density change across a weak shock wave is 2.5 times greater than the change in temperature. Therefore, the effect of the weak wave movement is more readily apparent in the density fluctuation distribution than in the temperature fluctuations. Pressure variation for the same weak shock process is even stronger (14 times greater than the density variation for \( \gamma = 7/5 \)). However, to obtain density fluctuation amplitudes from hot-wire measurements, pressure fluctuations are assumed to be negligible. This assumption is inappropriate for this flow and the weak shock driven increase in the density fluctuation level to 6.5% near \( Y/\delta = 0.6 \) could not be measured with the hot-wire anemometer.

**CONCLUSIONS**

The measurements of density, temperature, and their fluctuations in the Mach 2 boundary layer represent the first application of the LIF/R technique to the investigation of an unseeded, turbulent, supersonic flow. For each of the measured variables, the agreement between the present and previous results demonstrates the ability of the LIF/R technique to accurately characterize the mean and fluctuating components in a typical wind tunnel.

With a single cleaning pulse and an array temperature of 20°C, the OMA image persistence has a negligible effect on all flow property measurements. The instrumental noise level for the present experiment is dominated by a strong contribution from the OMA intensifier that is larger than the photon-statistical noise contribution. This noise level is relatively high and it limits the uncertainty of the measurements to 5.5% for density and 2.5%
for temperature. The LIF/R technique does not require an OMA and efforts are underway to repeat the boundary layer survey with reflective filters and photomultiplier tubes in place of the OMA and spectrometer. The results of the repeated surveys will guide further development of instrumentation for applications to hypersonic flows.

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