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TABLES AND GRAPHS OF NORMAL-SHOCK PARAMETERS
AT HYPERSONIC MACH NUMBERS AND
SELECTED ALTITUDES

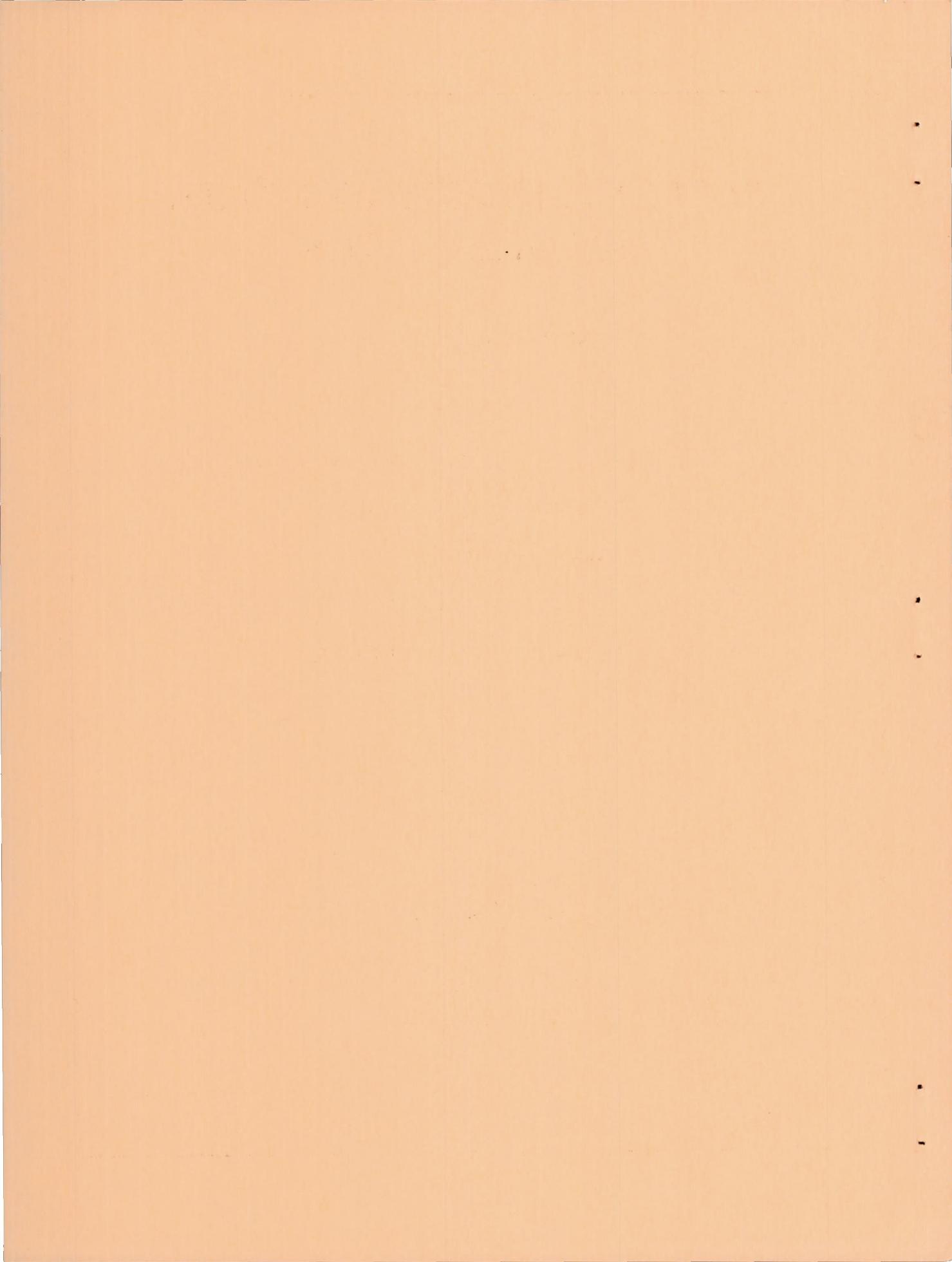
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SUMMARY

Tables and graphs of normal-shock parameters are presented for real air in thermal and chemical equilibrium at conditions ahead of the shock corresponding to six selected altitudes, and for temperatures behind the shock from $2,000^{\circ}$ K to $11,000^{\circ}$ K. The altitudes used are those representing the boundaries of the isothermal layers in that part of the earth's atmosphere considered applicable to aerodynamic flight; that is, below an altitude of 300,000 feet. The altitude data and the real-air thermodynamic data used are reliable for application to this range of altitudes. Tabulated values at each altitude as a function of the temperature behind the shock are presented of the normal-shock Mach numbers, flight velocity, enthalpy behind the shock, and ratios of real to ideal values of pressure, density, temperature, and velocity of sound. Graphs are presented to show the variation of the normal-shock parameters with flight Mach number and altitude, and some discussion of the dependence of the parameters on the initial pressure and temperature is given. A method for adapting the data to the case of oblique shocks is included.

INTRODUCTION

It can be shown from the tabulated thermodynamic properties for real air (for example, ref. 1) and the Rankine-Hugoniot shock relations that the hypersonic shock parameters are strongly dependent upon both temperature and pressure as well as on Mach number. This concept is in contrast to that for ideal air in which no temperature or pressure dependency is indicated because of the assumed constancy of the specific heats, constancy of the molecular weight, and perfectness of the gas. (See, for example, ref. 2.) Until the relatively recent advent of hypersonic flight in the atmosphere, the assumption of near ideal air has been adequate for flight, since the temperatures encountered were moderate and hence the thermal properties of the air were near to the ideal values. At high temperatures, however, the thermal properties of

air become greatly different from those of ideal air, and, in fact, the air changes composition due to dissociation and ionization of the constituent particles.

A number of real-air hypersonic shock computations have been published in recent years (refs. 3 to 8) in which the latest accepted thermodynamic air data (9.758 electron volts for the dissociation energy of nitrogen molecules) are used. In general, however, either outdated altitude information was used, or the conditions ahead of the shock were specified in terms of independent values of temperature and pressure. The latter is very useful for general application to hypersonic tunnel work, but since the atmosphere involves a rather definite combination of pressure and temperature at each altitude, interpolation of the data to conditions corresponding to a given altitude is often cumbersome. This inconvenience arises from the double interpolation required to correct for initial temperature and pressure, whereas certain of the functions are strongly, but not linearly, dependent on temperature or pressure (or both) in the hypersonic atmospheric regime.

In order to provide values of the normal-shock parameters which are directly applicable to the selected altitudes, the computations presented are based upon reliable thermodynamic information for high-temperature argon-free air (ref. 1) and atmospheric conditions at altitudes up to 300,000 feet (refs. 9 and 10). This range of altitudes encompasses that part of the earth's atmosphere in which flight where aerodynamic forces are used to advantage is generally considered. It may be noted that more recent higher altitude atmosphere data from earth satellites have superseded the model atmosphere of reference 10 for altitudes above 450,000 feet, but in the range of altitudes used herein there has been no significant change. Reference 10 should, therefore, still represent the best available data. The computations are based on complete thermal and chemical equilibrium, and it is to be remembered that thermal relaxation and reaction rate phenomena in hypersonic flow will, in some cases, restrict the usefulness of such computations. References 11 and 12 contain discussions of possible effects attributable to these nonequilibrium phenomena.

SYMBOLS

| | |
|---|---|
| H | geopotential altitude, ft (defined in refs. 9 and 10) |
| u | fluid velocity, ft/sec |
| h | specific enthalpy, $\frac{\text{ft}^2}{\text{sec}^2}$ |

| | |
|-------------|--|
| p | absolute pressure, lb/sq ft abs |
| V | molal volume based on undissociated mole, $\frac{m_0}{m} \frac{RT}{p}$, $\frac{\text{ft}^3}{\text{slug-mole}}$ |
| T | absolute temperature, °K or °R, as required |
| a | velocity of sound, ft/sec |
| M | Mach number, u/a |
| K | ratio of real-gas parameter to ideal-gas parameter for same value of M_1 , where the particular parameter is indicated by a subscript (for example, $K_{\rho 2} = \frac{\rho_2}{\rho_{2,i}}$) |
| m | molecular weight, $\frac{\text{slugs}}{\text{slug-mole}}$ |
| R | universal gas constant, $\frac{\text{ft-lb}}{\text{slug-mole-}^\circ\text{K}}$ |
| δ | flow-deflection angle |
| ρ | mass density, m_0/V , slugs/cu ft |
| θ | oblique-shock angle |
| γ | ratio of specific heats |
| Subscripts: | |
| 0 | at standard sea-level pressure (2,116 lb/sq ft abs); at temperature of 273.16° K |
| 1 | at altitude conditions and ahead of normal shock |
| 2 | behind normal shock |
| i | ideal air ($\gamma = 1.40$; $m = m_0$; $\frac{pV}{RT} = 1.0$) |
| θ | at altitude conditions and ahead of oblique shock |
| δ | deflected flow behind oblique shock |

METHOD OF COMPUTATION

The equations denoting conservation of mass, momentum, and energy are written for the case of a normal shock wave in the following equations:

$$\rho_1 u_1 = \rho_2 u_2 \quad (1)$$

$$p_1 + \rho_1 u_1^2 = p_2 + \rho_2 u_2^2 \quad (2)$$

$$h_1 + \frac{1}{2} u_1^2 = h_2 + \frac{1}{2} u_2^2 \quad (3)$$

The ideal-gas relations for the equation of state at the reference conditions and the velocity of sound on the low-pressure side (ahead of the shock) are:

$$\left. \begin{aligned} \frac{p_0}{\rho_0} &= \frac{R}{m_0} T_0 \\ a_1^2 &= \gamma_1 \frac{p_1}{\rho_1} \end{aligned} \right\} \quad (4)$$

since the gas is very nearly ideal at these conditions.

If equations (1), (2), (3), and (4) are combined, the following relations are obtained:

$$\left(\frac{p_2}{p_0} - \frac{p_1}{p_0} \right) \left(\frac{1}{\rho_1} + \frac{1}{\rho_2} \right) = 2 \left(\frac{h_2}{\frac{R}{m_0} T_0} - \frac{h_1}{\frac{R}{m_0} T_0} \right) \quad (5)$$

$$M_1^2 = \frac{1}{\gamma_1} \frac{\rho_2}{\rho_1} \frac{\frac{p_2}{p_1} - 1}{\frac{\rho_2}{\rho_1} - 1} = \left(\frac{u_1}{a_1} \right)^2 \quad (6)$$

Equation (5) is in a form suitable for insertion of tabulated values of the thermodynamic properties for real air and of the ambient-air properties at selected altitudes. Solution of equation (5) is obtained by

specifying values of T_2 , $\frac{p_1}{p_0}$, $\frac{\rho_1}{\rho_0}$, and $\frac{h_1}{\frac{R}{m_0} T_0}$ and iterating by using

interpolated values of the tabulated thermodynamic properties - $\frac{p_2}{p_0}$, $\frac{\rho_2}{\rho_0}$, and $\frac{h_2}{\frac{R}{m_0} T_0}$ at the specified value of T_2 until the equation is

satisfied. Interpolation of these tabulated air properties is accurately accomplished by linear interpolation of the logarithms of the values. Iteration of equation (5) is made rapidly convergent by first choosing two sets of the tabulated properties and plotting values of the left and right sides of the equation as a function of $\frac{p_2}{p_0}$ for these two cases and

finding a straight-line intersection. This intersection is generally very close to the final solution for $\frac{p_2}{p_0}$. Values of M_1 and u_1 are then found directly from equation (6) by using values of γ_1 and a_1 for argon-free air. In order to present the Mach number and velocity of sound behind the normal shock, values of $\frac{a_2}{a_0}$ pertinent to each solu-

tion $\left(\frac{h_2}{\frac{R}{m_0} T_0} \text{ and } T_2 \right)$ were read from a large chart available in refer-

ence 6. This chart is based on computations of a_2 from reference 13 and represents the case of complete thermal and chemical equilibrium.

The ratios M_2 and $\frac{a_2}{a_1}$ were then computed by using $\frac{u_2}{u_1}$ from equation (1) and $\frac{a_2}{a_0}$ along with values of $\frac{a_1}{a_0}$ for each altitude.

ACCURACY

In the iteration of equation (5) it was arbitrarily decided that the accepted solution would require at least 0.2 percent agreement between the values for the left and right sides of the equation. Inspection of equations (5) and (6) and of the thermodynamic data shows that this requirement establishes a similar accuracy for p_2 and ρ_2 , with the value of M_1 from equation (6) being within 0.1 percent of the correct value. Justification for this seeming crudeness lies mainly in the strong dependence of the results on the altitude data, which are certainly

not available for application to a given flight case to any greater accuracy. Some justification also may be found as a result of the use of argon-free-air data, which may be of the order of 1 percent different from atmospheric air in the enthalpy-temperature relation, although the errors resulting in the relations of the nondimensional aerodynamic parameters (for example, $\frac{p_2}{p_1} = f(M_1)$) should be less than 1 percent.

DATA INPUT

Values of the parameters $\frac{p_2}{p_0}$, $\frac{\rho_2}{\rho_0}$, $\frac{h_2}{\frac{R}{m_0} T_0}$, and T_2 were taken from

reference 1 and represent equilibrium values of the properties including effects of dissociation and ionization for an assumed argon-free real air. A somewhat more complete tabulation of the real-air thermodynamic properties may be found in reference 13 with the values being essentially in agreement with those of reference 1. Tabulated air properties may also be found in reference 14. Values of the parameters T_1 , $\frac{p_1}{p_0}$, and $\frac{\rho_1}{\rho_0}$ as functions of H were taken from data given in references 9 and 10 and represent a reliable model of the upper atmospheric conditions for the range of altitudes applicable to aerodynamic flight.

Values of $\frac{h_1}{\frac{R}{m_0} T_0}$ and $\frac{a_1}{a_0}$ were taken from reference 15 for conditions corresponding to each altitude.

Computations of the shock parameters are included for the range of temperatures T_2 from 2,000° K to 11,000° K at the intervals found in reference 1, for each altitude chosen. The altitudes chosen were those below 300,000 feet which represent boundaries of the isothermal layers within this region of the earth's atmosphere as taken from references 9 and 10. These altitudes and a few others are listed in table I and pertinent information for use in the computations is also shown in table I and plotted in figures 1 and 2.

Only these six altitudes were selected because it was desirable to limit the computations to a minimum number of cases. Since the temperature variation with altitude in the atmosphere is so peculiarly non-monotonic (see fig. 1), selection of the discontinuous points with the rather linear variation between these points allows for possible interpolation of such functions as may exhibit relationships that are largely

temperature dependent. The data of figure 2 indicate that solely pressure-dependent functions may be logarithmically interpolated to other altitudes to a reasonable degree.

RESULTS

The results of the computations are given in table II for each altitude as a function of the temperature T_2 behind the normal shock. The tabulated values include the parameters $\frac{p_2}{p_1}$, $\frac{\rho_2}{\rho_1}$, M_1 , u_1 , $\frac{T_2}{T_1}$,

$\frac{h_2}{\frac{R}{m_0} T_0}$, $\frac{a_2}{a_1}$, and M_2 . Also tabulated are the ratios of these real-air

parameters to the corresponding ideal-air parameters, K_{p2} , $K_{\rho 2}$, K_{T2} , K_{a2} , and K_{M2} , for the same value of M_1 (ideal parameters are independent of p_1 and T_1 and therefore of H). The ideal-air normal-shock parameters are computed from the relations found in reference 2 by use of $\gamma_1 = 1.400$. Plotted in figures 3 to 7 are the ratios K_{p2} , $K_{\rho 2}$, K_{T2} , K_{a2} , and K_{M2} as functions of M_1 for each altitude. The values of a_2 and consequently of M_2 given in the tables and figures are listed only within the range of data contained in the chart of reference 6.

Marked departures of the real-air normal-shock parameters from the ideal-air values are shown to occur in these figures with K being as low as 0.17 and as high as 3.5. In general, the nonideality of the results increases with flight Mach number and altitude - this being physically a result of the large increase of the heat capacity of the gas with temperature (Mach number) and the large increase of degree of dissociation with the inverse of pressure (altitude) at these temperatures. The peculiar nonlinearity of the results when plotted as a function of Mach number is largely due to the dissociation at different energy levels of oxygen and nitrogen and when plotted as a function of altitude is due also to the peculiar variation of temperature in the atmosphere (fig. 1). It is obvious that interpolation or extrapolation, even of altitude results such as these, should be attempted with extreme caution.

For purposes of interpolation to other altitudes, however, it can be shown from table II (and from examination of the shock equations) that certain parameters will exhibit less sensitivity to the real-air effects than others. For example, the shock pressure ratio p_2/p_1 as a

function of Mach number M_1 has a relatively slight dependence on initial pressure and temperature, whereas this parameter as a function of u_1 shows a strong dependence on the initial temperature T_1 but again little or no dependence on initial pressure p_1 . The shock density ratio ρ_2/ρ_1 shows only a slight dependence on initial temperature when plotted as a function of flight velocity u_1 but has a definite dependence on initial pressure; however, when plotted as a function of M_1 , the shock density ratio shows appreciable dependence on both temperature and pressure. For another example, use of the shock temperature ratio T_2/T_1 as a parameter introduces a strong dependence on the initial temperature T_1 , whether it be plotted as a function of flight velocity or Mach number, whereas if shock temperature rise $T_2 - T_1$ or T_2 is used, this temperature dependency is greatly reduced, particularly when plotted against u_1 . A pressure dependency, however, is seen in all cases. In general, by judicious use of the shock parameters, altitude interpolation is possible to a reasonable degree of accuracy for many engineering applications.

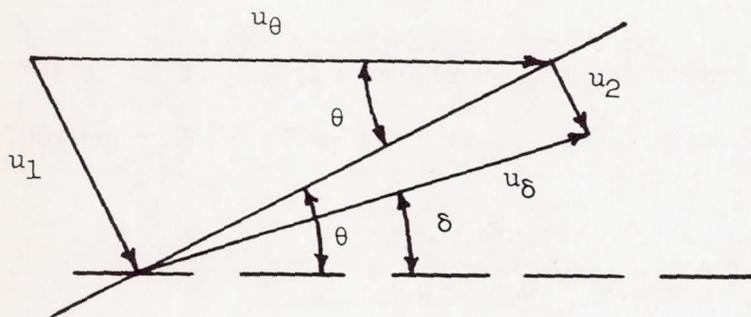
As an aid in interpolation of these results to other altitudes, therefore, the parameters $K_{\rho 2}$ and T_2 are plotted as a function of flight velocity u_1 in figures 8 and 9, respectively. For use with these figures the atmospheric velocity of sound a_1 , calculated by using equation (4), is shown as a function of altitude H in figure 10 for readily finding the value of $u_1 = M_1 a_1$ at any desired altitude and Mach number.

It is seen in figures 1 and 2 that the altitude data from reference 10, which are considered to be the most applicable data to aerodynamic flight in the atmosphere, are significantly different from the older data (ref. 16) at altitudes above 82,000 feet and are much closer to the data of reference 17. This comparison indicates that normal-shock computations based on the older data (for example, ref. 6) would also be different above this altitude. Differences of as high as 25 percent may be noted in values of p_2/p_1 or T_2/T_1 plotted against u_1 .

One exception is noted to the differences that may occur above 82,000 feet and that is that the altitude data at 120,000 feet used for the computations of reference 6 are very close to the later altitude data (see figs. 1 and 2). In order, therefore, to provide an additional altitude on figures 3 to 7, the curves for an altitude of 120,000 feet from reference 6 have been read and replotted to these coordinates.

A word may be said about the stagnation-point values in the flow behind the shock wave. Computations of these values have not been included in the report for two reasons; first, the change in flow values from behind the normal shock to the stagnation point is relatively small, and second, where such values may be required, the computation is readily made by using table II along with a large Mollier type chart such as is obtained from reference 6. With regard to the first reason, it can be shown from inspection of the energy equation applied to this case, together with a few sample computations in the hypersonic range, that the temperature rise at stagnation behind the normal shock is of the order of 1 percent and that the density and pressure rise are of the order of 5 percent.

Values of the oblique-shock parameters, although not included in the present analysis, may be readily computed from the normal-shock parameters found in table II along with the oblique-shock relations illustrated in the following sketch:



These parameters are:

$$\sin \theta = \frac{u_1}{u_\theta} = \frac{M_1}{M_\theta} \quad (7)$$

$$\frac{\tan(\theta - \delta)}{\tan \theta} = \frac{u_2}{u_1} = \frac{1}{\rho_2/\rho_1} \quad (8)$$

$$\sin(\theta - \delta) = \frac{u_2}{u_\delta} = \frac{M_2}{M_\delta} \quad (9)$$

For each desired altitude and flight velocity u_0 (or M_0):

(1) Assume values of u_1 (or M_1) as listed in table II, and read corresponding values of ρ_2/ρ_1 , p_2/p_1 , and so on.

(2) Find θ from equation (7), δ from equation (8), and u_8 from equation (9).

CONCLUDING REMARKS

Normal-shock parameters for real air in thermal and chemical equilibrium have been presented in both tabular and graphical form for six selected altitudes for the range of temperatures behind the shock from $2,000^\circ\text{K}$ to $11,000^\circ\text{K}$. Reliable altitude and thermodynamic air data for application to aerodynamic flight in the atmosphere have been used. The graphs serve to illustrate the variation of the normal-shock parameters with Mach number and altitude. The dependence of the parameters on initial temperature and pressure is indicated so that interpolation of the parameters to other altitudes may be readily carried out. Included is a method for adapting the data to the case of oblique shocks.

Langley Aeronautical Laboratory,
National Advisory Committee for Aeronautics,
Langley Field, Va., June 9, 1958.

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TABLE I.- ATMOSPHERIC ALTITUDE CONDITIONS AS TAKEN
FROM REFERENCES 9 AND 10

| H, ft | T ₁ , °K | $\frac{p_1}{p_0}$ | $\frac{\rho_1}{\rho_0}$ | $\frac{a_1}{a_0}$ | $\frac{h_1}{\frac{R}{m_0} T_0}$ |
|----------|------------------------|------------------------|-------------------------|-------------------|---------------------------------|
| 0 | 288 | 1.00 | 0.9474 | 1.0272 | 3.68 |
| 36,000 | 217 | .2243 | .2824 | .8905 | 2.77 |
| 82,020 | 217 | $.2456 \times 10^{-1}$ | $.3095 \times 10^{-1}$ | .8905 | 2.77 |
| 120,000 | 251 | $.4518 \times 10^{-2}$ | $.4910 \times 10^{-2}$ | .9591 | 3.21 |
| 154,200 | 283 | $.1189 \times 10^{-2}$ | $.1148 \times 10^{-2}$ | 1.0174 | 3.61 |
| 173,885 | 283 | $.5756 \times 10^{-3}$ | $.5559 \times 10^{-3}$ | 1.0174 | 3.61 |
| 246,060 | 197 | $.2420 \times 10^{-4}$ | $.3356 \times 10^{-4}$ | .8484 | 2.51 |
| 295,280 | 197 | $.1792 \times 10^{-5}$ | $.2485 \times 10^{-5}$ | .8484 | 2.51 |

Constants for argon-free air are (ref. 1):

| | |
|--|---|
| $p_0 = 2,116 \text{ lb/sq ft}$ $T_0 = 273.16^\circ \text{ K}$ $\rho_0 = 0.002499 \text{ slug/cu ft}$ $a_0 = 1,089 \text{ ft/sec}$ | $m_0 = 28.86 \frac{\text{slugs}}{\text{slug-mole}}$ $\gamma_1 = 1.400$ $\frac{R}{m_0} T_0 = 847,100 \frac{\text{ft}^2}{\text{sec}^2}$ |
|--|---|

TABLE II. - HYPERSONIC NORMAL-SHOCK PARAMETERS AT SIX SELECTED ALTITUDES

| T_2 , °K | $\frac{p_2}{p_1}$ | $\frac{\rho_2}{\rho_1}$ | M_1 | u_1 , ft | $\frac{T_2}{T_1}$ | $\frac{h_2}{\frac{R}{m_0} T_0}$ | $\frac{a_2}{a_1}$ | M_2 | K_{p2} | $K_{\rho 2}$ | K_{T2} | K_{a2} | K_{M2} |
|--|-------------------|-------------------------|--------|-------------------------|-------------------|---------------------------------|-------------------|--------|----------|--------------|----------|----------|----------|
| H = 36,000 ft; $T_1 = 217^\circ$ K; $p_1 = 0.2243$ atm. | | | | | | | | | | | | | |
| 2,000 | 58.29 | 6.315 | 6.971 | 6.760 × 10 ³ | 9.217 | 29.15 | ----- | ----- | 1.0314 | 1.1608 | 0.8871 | ----- | ----- |
| 2,200 | 66.01 | 6.507 | 7.404 | 7.180 | 10.138 | 32.60 | ----- | ----- | 1.0346 | 1.1833 | .8738 | ----- | ----- |
| 2,400 | 74.01 | 6.686 | 7.828 | 7.591 | 11.060 | 36.17 | ----- | ----- | 1.0376 | 1.2052 | .8602 | ----- | ----- |
| 2,600 | 82.52 | 6.876 | 8.252 | 8.002 | 11.982 | 39.91 | ----- | ----- | 1.0410 | 1.2302 | .8448 | ----- | ----- |
| 2,800 | 91.62 | 7.079 | 8.679 | 8.416 | 12.903 | 43.88 | ----- | ----- | 1.0446 | 1.2581 | .8277 | ----- | ----- |
| 3,000 | 101.29 | 7.286 | 9.109 | 8.833 | 13.825 | 48.12 | 3.481 | 0.3591 | 1.0482 | 1.2876 | .8096 | 0.8424 | 0.9220 |
| 3,200 | 111.90 | 7.518 | 9.555 | 9.266 | 14.747 | 52.72 | 3.594 | .3537 | 1.0521 | 1.3215 | .7887 | .8311 | .9104 |
| 3,400 | 123.45 | 7.761 | 10.017 | 9.714 | 15.668 | 57.73 | 3.695 | .3493 | 1.0562 | 1.3580 | .7661 | .8170 | .9012 |
| 3,600 | 136.20 | 8.027 | 10.500 | 10.182 | 16.590 | 63.19 | 3.818 | .3426 | 1.0604 | 1.3984 | .7413 | .8071 | .8860 |
| 3,800 | 150.02 | 8.293 | 10.998 | 10.665 | 17.512 | 69.22 | 3.931 | .3374 | 1.0644 | 1.4393 | .7159 | .7947 | .8743 |
| 4,000 | 164.51 | 8.547 | 11.497 | 11.149 | 18.433 | 75.36 | 4.054 | .3318 | 1.0680 | 1.4784 | .6918 | .7854 | .8614 |
| 4,200 | 179.89 | 8.791 | 12.003 | 11.640 | 19.355 | 81.94 | 4.189 | .3260 | 1.0713 | 1.5160 | .6684 | .7784 | .8474 |
| 4,400 | 195.50 | 8.998 | 12.447 | 12.070 | 20.277 | 88.71 | 4.312 | .3208 | 1.0739 | 1.5477 | .6475 | .7706 | .8352 |
| 4,600 | 211.32 | 9.178 | 12.980 | 12.587 | 21.198 | 95.55 | 4.464 | .3168 | 1.0760 | 1.5750 | .6290 | .7689 | .8256 |
| 4,800 | 227.15 | 9.330 | 13.446 | 13.039 | 22.120 | 102.31 | 4.607 | .3128 | 1.0777 | 1.5981 | .6128 | .7667 | .8161 |
| 5,000 | 242.53 | 9.445 | 13.886 | 13.466 | 23.042 | 108.93 | 4.745 | .3099 | 1.0790 | 1.6149 | .5995 | .7653 | .8091 |
| 5,500 | 279.31 | 9.627 | 14.889 | 14.438 | 25.346 | 124.74 | 5.070 | .3050 | 1.0807 | 1.6407 | .5754 | .7640 | .7976 |
| 6,000 | 315.43 | 9.746 | 15.814 | 15.335 | 27.650 | 140.49 | 5.343 | .3037 | 1.0817 | 1.6658 | .5578 | .7588 | .7954 |
| 6,500 | 354.44 | 9.893 | 16.752 | 16.245 | 29.954 | 157.46 | 5.576 | .3037 | 1.0831 | 1.6782 | .5396 | .7483 | .7963 |
| 7,000 | 401.69 | 10.158 | 17.811 | 17.272 | 32.258 | 177.54 | 5.826 | .3010 | 1.0858 | 1.7197 | .5151 | .7362 | .7898 |
| 7,500 | 459.21 | 10.517 | 19.011 | 18.435 | 34.562 | 201.81 | 6.098 | .2964 | 1.0895 | 1.7771 | .4853 | .7226 | .7786 |
| 8,000 | 528.31 | 10.937 | 20.353 | 19.737 | 36.866 | 231.02 | 6.406 | .2907 | 1.0935 | 1.8448 | .4524 | .7096 | .7644 |
| 8,500 | 609.90 | 11.390 | 21.828 | 21.167 | 39.171 | 265.49 | 6.744 | .2842 | 1.0976 | 1.9183 | .4185 | .6971 | .7479 |
| 9,000 | 703.30 | 11.817 | 23.402 | 22.693 | 41.475 | 304.90 | 7.120 | .2782 | 1.1011 | 1.9874 | .3861 | .6869 | .7327 |
| 9,500 | 805.62 | 12.229 | 25.009 | 24.252 | 43.779 | 347.96 | 7.519 | .2720 | 1.1043 | 2.0544 | .3572 | .6791 | .7167 |
| 10,000 | 913.96 | 12.548 | 26.610 | 25.804 | 46.083 | 393.65 | 7.925 | .2676 | 1.1066 | 2.1060 | .3324 | .6860 | .7050 |
| 11,000 | 1129.29 | 12.904 | 29.547 | 28.652 | 50.691 | 485.05 | ----- | ----- | 1.1090 | 2.1629 | .2970 | ----- | ----- |
| H = 82,020 ft; $T_1 = 217^\circ$ K; $p_1 = 0.2456 \times 10^{-1}$ atm. | | | | | | | | | | | | | |
| 2,000 | 58.39 | 6.330 | 6.975 | 6.764 × 10 ³ | 9.217 | 29.16 | ----- | ----- | 1.0319 | 1.1634 | 0.8862 | ----- | ----- |
| 2,200 | 66.33 | 6.535 | 7.420 | 7.195 | 10.138 | 32.65 | ----- | ----- | 1.0354 | 1.1881 | .8705 | ----- | ----- |
| 2,400 | 74.63 | 6.734 | 7.856 | 7.618 | 11.060 | 36.38 | ----- | ----- | 1.0388 | 1.2133 | .8544 | ----- | ----- |
| 2,600 | 84.00 | 6.981 | 8.314 | 8.062 | 11.982 | 40.46 | ----- | ----- | 1.0437 | 1.2477 | .8330 | ----- | ----- |
| 2,800 | 94.54 | 7.267 | 8.799 | 8.533 | 12.903 | 45.01 | ----- | ----- | 1.0485 | 1.2893 | .8065 | ----- | ----- |
| 3,000 | 106.72 | 7.603 | 9.321 | 9.039 | 13.825 | 50.23 | 3.453 | 0.3550 | 1.0545 | 1.3401 | .7750 | 0.8176 | 0.9126 |
| 3,200 | 120.77 | 7.983 | 9.886 | 9.587 | 14.747 | 56.26 | 3.567 | .3468 | 1.0607 | 1.3985 | .7393 | .7986 | .8943 |
| 3,400 | 136.93 | 8.402 | 10.494 | 10.176 | 15.668 | 63.16 | 3.700 | .3377 | 1.0671 | 1.4639 | .7008 | .7826 | .8733 |
| 3,600 | 154.97 | 8.845 | 11.131 | 10.794 | 16.590 | 70.80 | 3.842 | .3276 | 1.0732 | 1.5336 | .6626 | .7678 | .8494 |
| 3,800 | 174.80 | 9.249 | 11.794 | 11.437 | 17.512 | 79.16 | 3.998 | .3190 | 1.0783 | 1.5968 | .6257 | .7557 | .8288 |
| 4,000 | 193.32 | 9.536 | 12.384 | 12.009 | 18.433 | 87.20 | 4.150 | .3130 | 1.0815 | 1.6412 | .5992 | .7481 | .8145 |
| 4,200 | 211.93 | 9.776 | 12.950 | 12.558 | 19.355 | 95.22 | 4.310 | .3074 | 1.0840 | 1.6778 | .5768 | .7441 | .8011 |
| 4,400 | 229.64 | 9.949 | 13.470 | 13.062 | 20.277 | 102.72 | 4.481 | .3021 | 1.0857 | 1.7039 | .5598 | .7445 | .7882 |
| 4,600 | 245.81 | 10.049 | 13.930 | 13.508 | 21.198 | 109.66 | 4.637 | .2989 | 1.0866 | 1.7181 | .5481 | .7456 | .7806 |
| 4,800 | 261.03 | 10.114 | 14.353 | 13.917 | 22.120 | 116.12 | 4.784 | .2966 | 1.0870 | 1.7266 | .5396 | .7472 | .7750 |
| 5,000 | 275.45 | 10.149 | 14.741 | 14.294 | 23.042 | 122.31 | 4.899 | .2965 | 1.0872 | 1.7304 | .5334 | .7453 | .7754 |
| 5,500 | 311.69 | 10.227 | 15.678 | 15.203 | 25.346 | 138.21 | 5.143 | .2980 | 1.0876 | 1.7392 | .5201 | .7367 | .7803 |
| 6,000 | 356.88 | 10.491 | 16.757 | 16.250 | 27.650 | 157.67 | 5.380 | .2969 | 1.0900 | 1.7797 | .4978 | .7219 | .7784 |
| 6,500 | 418.16 | 10.970 | 18.100 | 17.552 | 29.954 | 183.51 | 5.654 | .2918 | 1.0945 | 1.8563 | .4633 | .7032 | .7661 |
| 7,000 | 499.39 | 11.632 | 19.728 | 19.131 | 32.258 | 217.61 | 5.987 | .2833 | 1.1002 | 1.9636 | .4210 | .6839 | .7445 |
| 7,500 | 601.18 | 12.361 | 21.589 | 20.935 | 34.562 | 260.39 | 6.376 | .2739 | 1.1055 | 2.0823 | .3773 | .6662 | .7208 |
| 8,000 | 721.70 | 13.059 | 23.603 | 22.888 | 36.866 | 310.92 | 6.827 | .2648 | 1.1107 | 2.1960 | .3374 | .6531 | .6974 |
| 8,500 | 855.66 | 13.656 | 25.656 | 24.879 | 39.171 | 366.57 | 7.300 | .2574 | 1.1145 | 2.2933 | .3038 | .6429 | .6784 |
| 9,000 | 989.01 | 14.031 | 27.556 | 26.722 | 41.475 | 423.09 | 7.784 | .2523 | 1.1166 | 2.3539 | .2791 | .6385 | .6653 |
| 9,500 | 1114.41 | 14.179 | 29.241 | 28.356 | 43.779 | 475.87 | 8.260 | .2497 | 1.1174 | 2.3771 | .2618 | .6390 | .6590 |
| 10,000 | 1222.52 | 14.255 | 30.621 | 29.694 | 46.083 | 521.67 | ----- | ----- | 1.1177 | 2.3884 | .2514 | ----- | ----- |
| 11,000 | 1389.66 | 14.018 | 32.670 | 31.681 | 50.691 | 592.92 | ----- | ----- | 1.1160 | 2.3472 | .2431 | ----- | ----- |

TABLE II.- HYPERSONIC NORMAL-SHOCK PARAMETERS AT SIX SELECTED ALTITUDES - Continued

| T_2 , °K | $\frac{P_2}{P_1}$ | $\frac{\rho_2}{\rho_1}$ | M_1 | u_1 , ft | $\frac{T_2}{T_1}$ | $\frac{h_2}{R M_0^2 T_0}$ | $\frac{a_2}{a_1}$ | M_2 | K_{P2} | $K_{\rho 2}$ | K_{T2} | K_{a2} | K_{M2} |
|---|-------------------|-------------------------|--------|---------------------|-------------------|---------------------------|-------------------|--------|----------|--------------|----------|----------|----------|
| H = 154,200 ft; $T_1 = 283^\circ$ K; $p_1 = 0.1189 \times 10^{-2}$ atm. | | | | | | | | | | | | | |
| 2,000 | 43.72 | 6.178 | 6.032 | 6.683×10^3 | 7.067 | 29.29 | ----- | ----- | 1.0341 | 1.1713 | 0.8818 | ----- | ----- |
| 2,200 | 50.31 | 6.454 | 6.454 | 7.151 | 7.774 | 33.11 | ----- | ----- | 1.0389 | 1.2048 | .8600 | ----- | ----- |
| 2,400 | 58.43 | 6.836 | 6.929 | 7.677 | 8.481 | 37.69 | ----- | ----- | 1.0462 | 1.2580 | .8252 | ----- | ----- |
| 2,600 | 68.97 | 7.374 | 7.492 | 8.301 | 9.187 | 43.55 | ----- | ----- | 1.0560 | 1.3384 | .7750 | ----- | ----- |
| 2,800 | 82.69 | 8.070 | 8.158 | 9.038 | 9.894 | 51.09 | ----- | ----- | 1.0672 | 1.4460 | .7126 | ----- | ----- |
| 3,000 | 99.66 | 8.856 | 8.910 | 9.872 | 10.601 | 60.45 | 3.047 | 0.3302 | 1.0780 | 1.5690 | .6472 | 0.7528 | 0.8467 |
| 3,200 | 119.34 | 9.652 | 9.708 | 10.756 | 11.307 | 71.16 | 3.196 | .3147 | 1.0872 | 1.6939 | .5869 | .7282 | .8107 |
| 3,400 | 138.98 | 10.271 | 10.446 | 11.573 | 12.014 | 82.01 | 3.362 | .3025 | 1.0932 | 1.7903 | .5422 | .7141 | .7821 |
| 3,600 | 156.18 | 10.637 | 11.057 | 12.250 | 12.721 | 91.50 | 3.529 | .2946 | 1.0963 | 1.8453 | .5147 | .7098 | .7636 |
| 3,800 | 170.65 | 10.816 | 11.551 | 12.798 | 13.428 | 99.48 | 3.706 | .2882 | 1.0974 | 1.8702 | .4994 | .7146 | .7482 |
| 4,000 | 181.92 | 10.834 | 11.928 | 13.215 | 14.134 | 105.80 | 3.858 | .2854 | 1.0971 | 1.8691 | .4941 | .7213 | .7419 |
| 4,200 | 191.88 | 10.798 | 12.213 | 13.531 | 14.841 | 111.49 | 3.981 | .2841 | 1.0964 | 1.8596 | .4924 | .7251 | .7391 |
| 4,400 | 201.68 | 10.763 | 12.566 | 13.922 | 15.548 | 117.10 | 4.059 | .2876 | 1.0957 | 1.8507 | .4913 | .7216 | .7488 |
| 4,600 | 212.28 | 10.766 | 12.894 | 14.286 | 16.254 | 123.18 | 4.128 | .2901 | 1.0954 | 1.8483 | .4886 | .7157 | .7559 |
| 4,800 | 225.06 | 10.833 | 13.273 | 14.706 | 16.961 | 130.23 | 4.197 | .2914 | 1.0960 | 1.8602 | .4819 | .7074 | .7600 |
| 5,000 | 240.24 | 11.010 | 13.705 | 15.184 | 17.668 | 138.65 | 4.281 | .2908 | 1.0972 | 1.8839 | .4716 | .6993 | .7591 |
| 5,500 | 294.36 | 11.785 | 15.127 | 16.760 | 19.435 | 168.48 | 4.526 | .2836 | 1.1034 | 2.0070 | .4277 | .6715 | .7420 |
| 6,000 | 379.31 | 13.045 | 17.101 | 18.947 | 21.201 | 214.57 | 4.875 | .2689 | 1.1123 | 2.2114 | .3668 | .6412 | .7052 |
| 6,500 | 496.72 | 14.460 | 19.497 | 21.601 | 22.968 | 277.87 | 5.313 | .2538 | 1.1205 | 2.4418 | .3068 | .6140 | .6670 |
| 7,000 | 634.15 | 15.611 | 21.974 | 24.346 | 24.735 | 352.49 | 5.819 | .2419 | 1.1260 | 2.6288 | .2608 | .5975 | .6366 |
| 7,500 | 767.45 | 16.260 | 24.144 | 26.750 | 26.502 | 424.83 | 6.315 | .2351 | 1.1287 | 2.7332 | .2319 | .5907 | .6193 |
| 8,000 | 873.84 | 16.405 | 25.758 | 28.538 | 28.269 | 482.75 | 6.782 | .2315 | 1.1292 | 2.7548 | .2175 | .5949 | .6102 |
| 8,500 | 947.86 | 16.200 | 26.839 | 29.736 | 30.035 | 524.31 | ----- | ----- | 1.1281 | 2.7191 | .2130 | ----- | ----- |
| 9,000 | 1003.36 | 15.891 | 27.632 | 30.614 | 31.802 | 555.15 | ----- | ----- | 1.1266 | 2.6658 | .2129 | ----- | ----- |
| 9,500 | 1051.30 | 15.572 | 28.304 | 31.359 | 33.569 | 581.93 | ----- | ----- | 1.1250 | 2.6116 | .2142 | ----- | ----- |
| 10,000 | 1097.98 | 15.274 | 28.946 | 32.070 | 35.336 | 609.11 | ----- | ----- | 1.1235 | 2.5609 | .2156 | ----- | ----- |
| 11,000 | 1216.15 | 14.950 | 30.488 | 33.778 | 38.869 | 674.53 | ----- | ----- | 1.1216 | 2.5051 | .2139 | ----- | ----- |
| H = 173,885 ft; $T_1 = 283^\circ$ K; $p_1 = 0.5756 \times 10^{-3}$ atm. | | | | | | | | | | | | | |
| 2,000 | 43.78 | 6.185 | 6.035 | 6.686×10^3 | 7.067 | 29.35 | ----- | ----- | 1.0343 | 1.1724 | 0.8808 | ----- | ----- |
| 2,200 | 50.82 | 6.510 | 6.482 | 7.182 | 7.774 | 33.35 | ----- | ----- | 1.0403 | 1.2140 | .8533 | ----- | ----- |
| 2,400 | 59.68 | 6.961 | 6.993 | 7.748 | 8.481 | 38.35 | ----- | ----- | 1.0489 | 1.2787 | .8114 | ----- | ----- |
| 2,600 | 71.72 | 7.617 | 7.623 | 8.446 | 9.187 | 45.01 | ----- | ----- | 1.0606 | 1.3788 | .7506 | ----- | ----- |
| 2,800 | 87.70 | 8.456 | 8.378 | 9.282 | 9.894 | 53.85 | ----- | ----- | 1.0732 | 1.5098 | .6782 | ----- | ----- |
| 3,000 | 107.35 | 9.374 | 9.218 | 10.213 | 10.676 | 64.56 | 3.055 | 0.3215 | 1.0847 | 1.6542 | .6113 | 0.7320 | 0.8260 |
| 3,200 | 128.39 | 10.171 | 10.042 | 11.126 | 11.307 | 76.09 | 3.224 | .3062 | 1.0928 | 1.7792 | .5502 | .7112 | .7902 |
| 3,400 | 148.59 | 10.704 | 10.780 | 11.943 | 12.014 | 86.78 | 3.406 | .2953 | 1.0974 | 1.8607 | .5104 | .7020 | .7646 |
| 3,600 | 163.48 | 10.954 | 11.297 | 12.516 | 12.721 | 95.46 | 3.588 | .2875 | 1.0992 | 1.8972 | .4938 | .7069 | .7458 |
| 3,800 | 175.73 | 11.009 | 11.712 | 12.976 | 13.428 | 102.32 | 3.760 | .2830 | 1.0992 | 1.9017 | .4862 | .7154 | .7351 |
| 4,000 | 185.55 | 10.956 | 12.040 | 13.339 | 14.134 | 107.94 | 3.883 | .2831 | 1.0982 | 1.8890 | .4847 | .7194 | .7361 |
| 4,200 | 195.05 | 10.902 | 12.349 | 13.682 | 14.841 | 113.33 | 3.981 | .2845 | 1.0974 | 1.8766 | .4846 | .7197 | .7403 |
| 4,400 | 205.32 | 10.889 | 12.672 | 14.040 | 15.548 | 119.15 | 4.050 | .2874 | 1.0969 | 1.8713 | .4833 | .7140 | .7484 |
| 4,600 | 217.25 | 10.917 | 13.035 | 14.442 | 16.254 | 125.88 | 4.114 | .2899 | 1.0968 | 1.8730 | .4783 | .7056 | .7557 |
| 4,800 | 232.02 | 11.092 | 13.462 | 14.915 | 16.961 | 134.04 | 4.187 | .2899 | 1.0982 | 1.8996 | .4687 | .6961 | .7567 |
| 5,000 | 250.35 | 11.342 | 13.971 | 15.479 | 17.668 | 144.16 | 4.270 | .2885 | 1.1002 | 1.9387 | .4542 | .6846 | .7537 |
| 5,500 | 318.45 | 12.457 | 15.696 | 17.390 | 19.435 | 181.13 | 4.553 | .2767 | 1.1086 | 2.1183 | .3979 | .6514 | .7247 |
| 6,000 | 423.47 | 14.003 | 18.021 | 19.966 | 21.201 | 238.16 | 4.964 | .2593 | 1.1182 | 2.3697 | .3308 | .6200 | .6808 |
| 6,500 | 561.50 | 15.521 | 20.679 | 22.911 | 22.968 | 312.58 | 5.456 | .2442 | 1.1259 | 2.6170 | .2731 | .5950 | .6423 |
| 7,000 | 709.17 | 16.544 | 23.195 | 25.698 | 24.735 | 392.30 | 5.986 | .2342 | 1.1302 | 2.7830 | .2343 | .5826 | .6168 |
| 7,500 | 832.52 | 16.888 | 25.117 | 27.828 | 26.502 | 459.94 | 6.487 | .2293 | 1.1314 | 2.8369 | .2144 | .5835 | .6042 |
| 8,000 | 918.87 | 16.771 | 26.395 | 29.244 | 28.249 | 507.15 | ----- | ----- | 1.1307 | 2.8152 | .2071 | ----- | ----- |
| 8,500 | 977.24 | 16.424 | 27.240 | 30.180 | 30.035 | 539.84 | ----- | ----- | 1.1291 | 2.7558 | .2068 | ----- | ----- |
| 9,000 | 1023.63 | 16.034 | 27.901 | 30.912 | 31.802 | 566.59 | ----- | ----- | 1.1273 | 2.6903 | .2088 | ----- | ----- |
| 9,500 | 1071.93 | 15.727 | 28.571 | 31.655 | 33.569 | 593.26 | ----- | ----- | 1.1257 | 2.6372 | .2102 | ----- | ----- |
| 10,000 | 1126.13 | 15.496 | 29.300 | 32.462 | 35.336 | 623.39 | ----- | ----- | 1.1245 | 2.5976 | .2105 | ----- | ----- |
| 11,000 | 1266.51 | 15.273 | 31.090 | 34.445 | 38.869 | 702.48 | ----- | ----- | 1.1233 | 2.5587 | .2058 | ----- | ----- |

TABLE II.- HYPERSONIC NORMAL-SHOCK PARAMETERS AT SIX SELECTED ALTITUDES - Concluded

| T_2 , °K | $\frac{p_2}{p_1}$ | $\frac{\rho_2}{\rho_1}$ | M_1 | u_1 , ft | $\frac{T_2}{T_1}$ | $\frac{h_2}{\frac{R}{m_0} T_0}$ | $\frac{a_2}{a_1}$ | M_2 | K_{p2} | $K_{\rho 2}$ | K_{T2} | K_{a2} | K_{M2} |
|---|-------------------|-------------------------|--------|---------------------|-------------------|---------------------------------|-------------------|--------|----------|--------------|----------|----------|----------|
| H = 246,060 ft; $T_1 = 197^\circ$ K; $p_1 = 0.2420 \times 10^{-4}$ atm. | | | | | | | | | | | | | |
| 2,000 | 67.23 | 6.593 | 7.465 | 6.897×10^3 | 10.152 | 29.97 | ----- | ----- | 1.0368 | 1.1974 | 0.8620 | ----- | ----- |
| 2,200 | 81.53 | 7.183 | 8.172 | 7.550 | 11.168 | 35.55 | ----- | ----- | 1.0487 | 1.2868 | .8019 | ----- | ----- |
| 2,400 | 103.82 | 8.208 | 9.142 | 8.446 | 12.183 | 44.07 | ----- | ----- | 1.0666 | 1.4499 | .7086 | ----- | ----- |
| 2,600 | 135.95 | 9.581 | 10.371 | 9.581 | 13.198 | 56.24 | ----- | ----- | 1.0849 | 1.6711 | .6039 | ----- | ----- |
| 2,800 | 173.55 | 10.869 | 11.647 | 10.760 | 14.213 | 70.46 | ----- | ----- | 1.0978 | 1.8783 | .5203 | ----- | ----- |
| 3,000 | 206.74 | 11.650 | 12.674 | 11.709 | 15.228 | 83.14 | 3.850 | 0.2825 | 1.1041 | 2.0021 | .4732 | 0.6790 | 0.7360 |
| 3,200 | 229.96 | 11.910 | 13.357 | 12.340 | 16.244 | 91.89 | 4.096 | .2738 | 1.1057 | 2.0406 | .4559 | .6862 | .7141 |
| 3,400 | 244.88 | 11.810 | 13.790 | 12.740 | 17.259 | 97.83 | 4.314 | .2707 | 1.1045 | 2.0201 | .4551 | .7006 | .7068 |
| 3,600 | 257.03 | 11.648 | 14.139 | 13.062 | 18.274 | 102.73 | 4.468 | .2717 | 1.1028 | 1.9898 | .4590 | .7080 | .7098 |
| 3,800 | 269.55 | 11.523 | 14.488 | 13.385 | 19.289 | 107.74 | 4.550 | .2763 | 1.1015 | 1.9662 | .4619 | .7041 | .7222 |
| 4,000 | 284.46 | 11.489 | 14.887 | 13.753 | 20.305 | 113.70 | 4.621 | .2804 | 1.1009 | 1.9581 | .4611 | .6963 | .7335 |
| 4,200 | 304.54 | 11.614 | 15.397 | 14.225 | 21.320 | 121.37 | 4.686 | .2829 | 1.1017 | 1.9765 | .4532 | .6832 | .7406 |
| 4,400 | 331.61 | 11.913 | 16.050 | 14.828 | 22.335 | 131.71 | 4.774 | .2822 | 1.1040 | 2.0257 | .4376 | .6683 | .7393 |
| 4,600 | 369.09 | 12.433 | 16.903 | 15.616 | 23.350 | 145.78 | 4.904 | .2773 | 1.1078 | 2.1084 | .4133 | .6524 | .7274 |
| 4,800 | 418.60 | 13.145 | 17.962 | 16.594 | 24.366 | 164.49 | 5.057 | .2702 | 1.1127 | 2.2248 | .3827 | .6337 | .7092 |
| 5,000 | 482.44 | 14.032 | 19.236 | 17.771 | 25.381 | 188.47 | 5.246 | .2613 | 1.1180 | 2.3703 | .3482 | .6144 | .6865 |
| 5,500 | 703.72 | 16.518 | 23.106 | 21.347 | 27.919 | 271.48 | 5.864 | .2385 | 1.1301 | 2.7787 | .2665 | .5730 | .6280 |
| 6,000 | 973.55 | 18.426 | 27.093 | 25.030 | 30.457 | 371.79 | 6.589 | .2232 | 1.1371 | 3.0919 | .2120 | .5497 | .5885 |
| 6,500 | 1185.12 | 18.969 | 29.870 | 27.595 | 32.995 | 451.81 | 7.214 | .2183 | 1.1387 | 3.1792 | .1892 | .5462 | .5758 |
| 7,000 | 1301.24 | 18.605 | 31.318 | 28.933 | 35.533 | 496.59 | ----- | ----- | 1.1374 | 3.1166 | .1854 | ----- | ----- |
| 7,500 | 1370.66 | 18.006 | 32.173 | 29.723 | 38.071 | 523.71 | ----- | ----- | 1.1351 | 3.0154 | .1883 | ----- | ----- |
| 8,000 | 1434.92 | 17.486 | 32.948 | 30.439 | 40.609 | 548.29 | ----- | ----- | 1.1331 | 2.9278 | .1915 | ----- | ----- |
| 8,500 | 1505.79 | 17.049 | 33.779 | 31.207 | 43.147 | 577.86 | ----- | ----- | 1.1313 | 2.8539 | .1937 | ----- | ----- |
| 9,000 | 1611.57 | 16.915 | 34.955 | 32.293 | 45.685 | 616.69 | ----- | ----- | 1.1307 | 2.8307 | .1915 | ----- | ----- |
| 9,500 | 1747.11 | 16.911 | 36.396 | 33.625 | 48.223 | 668.79 | ----- | ----- | 1.1306 | 2.8292 | .1865 | ----- | ----- |
| 10,000 | 1928.51 | 17.101 | 38.227 | 35.316 | 50.761 | 736.97 | ----- | ----- | 1.1313 | 2.8610 | .1781 | ----- | ----- |
| 11,000 | 2433.88 | 17.740 | 42.898 | 39.631 | 55.838 | 928.96 | ----- | ----- | 1.1337 | 2.9648 | .1556 | ----- | ----- |
| H = 295,280 ft; $T_1 = 197^\circ$ K; $p_1 = 0.1792 \times 10^{-5}$ atm. | | | | | | | | | | | | | |
| 2,000 | 72.88 | 7.082 | 7.729 | 7.140×10^3 | 10.152 | 32.04 | ----- | ----- | 1.0481 | 1.2791 | 0.8084 | ----- | ----- |
| 2,200 | 98.83 | 8.488 | 8.897 | 8.220 | 11.168 | 41.94 | ----- | ----- | 1.0721 | 1.5041 | .6837 | ----- | ----- |
| 2,400 | 139.56 | 10.459 | 10.458 | 9.662 | 12.183 | 57.16 | ----- | ----- | 1.0953 | 1.8228 | .5486 | ----- | ----- |
| 2,600 | 183.48 | 12.041 | 11.918 | 11.010 | 13.198 | 73.80 | ----- | ----- | 1.1083 | 2.0775 | .4621 | ----- | ----- |
| 2,800 | 213.73 | 12.628 | 12.841 | 11.863 | 14.213 | 85.18 | ----- | ----- | 1.1119 | 2.1684 | .4306 | ----- | ----- |
| 3,000 | 229.52 | 12.501 | 13.315 | 12.301 | 15.228 | 91.46 | 4.067 | 0.2619 | 1.1105 | 2.1422 | .4299 | 0.6833 | 0.6833 |
| 3,200 | 241.13 | 12.273 | 13.660 | 12.620 | 16.244 | 96.05 | 4.249 | .2623 | 1.1085 | 2.1004 | .4363 | .6965 | .6847 |
| 3,400 | 252.29 | 12.050 | 13.986 | 12.921 | 17.259 | 100.57 | 4.320 | .2687 | 1.1064 | 2.0596 | .4434 | .6925 | .7017 |
| 3,600 | 266.18 | 11.953 | 14.372 | 13.278 | 18.274 | 106.12 | 4.373 | .2750 | 1.1053 | 2.0403 | .4445 | .6821 | .7188 |
| 3,800 | 286.50 | 12.086 | 14.905 | 13.770 | 19.289 | 113.78 | 4.435 | .2781 | 1.1060 | 2.0596 | .4370 | .6674 | .7274 |
| 4,000 | 316.41 | 12.489 | 15.644 | 14.453 | 20.305 | 125.12 | 4.526 | .2767 | 1.1089 | 2.1241 | .4184 | .6498 | .7245 |
| 4,200 | 360.27 | 13.212 | 16.656 | 15.388 | 21.320 | 141.88 | 4.662 | .2704 | 1.1136 | 2.2416 | .3884 | .6293 | .7088 |
| 4,400 | 424.16 | 14.315 | 18.020 | 16.648 | 22.335 | 165.69 | 4.845 | .2598 | 1.1201 | 2.4226 | .3486 | .6052 | .6821 |
| 4,600 | 510.38 | 15.691 | 19.706 | 18.205 | 23.350 | 197.66 | 5.081 | .2472 | 1.1269 | 2.6488 | .3054 | .5810 | .6497 |
| 4,800 | 619.70 | 17.194 | 21.654 | 20.005 | 24.366 | 238.23 | 5.352 | .2353 | 1.1332 | 2.8962 | .2645 | .5576 | .6192 |
| 5,000 | 745.54 | 18.584 | 23.699 | 21.894 | 25.381 | 285.58 | 5.664 | .2251 | 1.1381 | 3.1249 | .2304 | .5397 | .5928 |
| 5,500 | 1059.71 | 20.759 | 28.177 | 26.031 | 27.919 | 402.58 | ----- | ----- | 1.1443 | 3.4817 | .1798 | ----- | ----- |
| 6,000 | 1234.65 | 20.708 | 30.416 | 28.100 | 30.457 | 468.91 | ----- | ----- | 1.1441 | 3.4700 | .1684 | ----- | ----- |
| 6,500 | 1309.71 | 19.696 | 31.370 | 28.981 | 32.995 | 497.64 | ----- | ----- | 1.1409 | 3.2993 | .1716 | ----- | ----- |
| 7,000 | 1366.07 | 19.070 | 32.067 | 29.625 | 35.533 | 520.62 | ----- | ----- | 1.1389 | 3.1937 | .1769 | ----- | ----- |
| 7,500 | 1439.73 | 18.519 | 32.948 | 30.439 | 38.071 | 549.65 | ----- | ----- | 1.1370 | 3.1008 | .1796 | ----- | ----- |
| 8,000 | 1555.53 | 18.345 | 34.257 | 31.648 | 40.609 | 592.86 | ----- | ----- | 1.1363 | 3.0705 | .1772 | ----- | ----- |
| 8,500 | 1728.80 | 18.510 | 36.107 | 33.358 | 43.147 | 657.88 | ----- | ----- | 1.1368 | 3.0968 | .1696 | ----- | ----- |
| 9,000 | 1973.21 | 18.966 | 38.550 | 35.615 | 45.685 | 751.10 | ----- | ----- | 1.1382 | 3.1715 | .1576 | ----- | ----- |
| 9,500 | 2306.36 | 19.576 | 41.642 | 38.471 | 48.223 | 876.46 | ----- | ----- | 1.1401 | 3.2722 | .1426 | ----- | ----- |
| 10,000 | 2725.45 | 20.275 | 45.228 | 41.784 | 50.761 | 1033.05 | ----- | ----- | 1.1421 | 3.3873 | .1273 | ----- | ----- |
| 11,000 | 3716.52 | 21.215 | 52.757 | 48.740 | 55.838 | 1405.64 | ----- | ----- | 1.1446 | 3.5422 | .1030 | ----- | ----- |

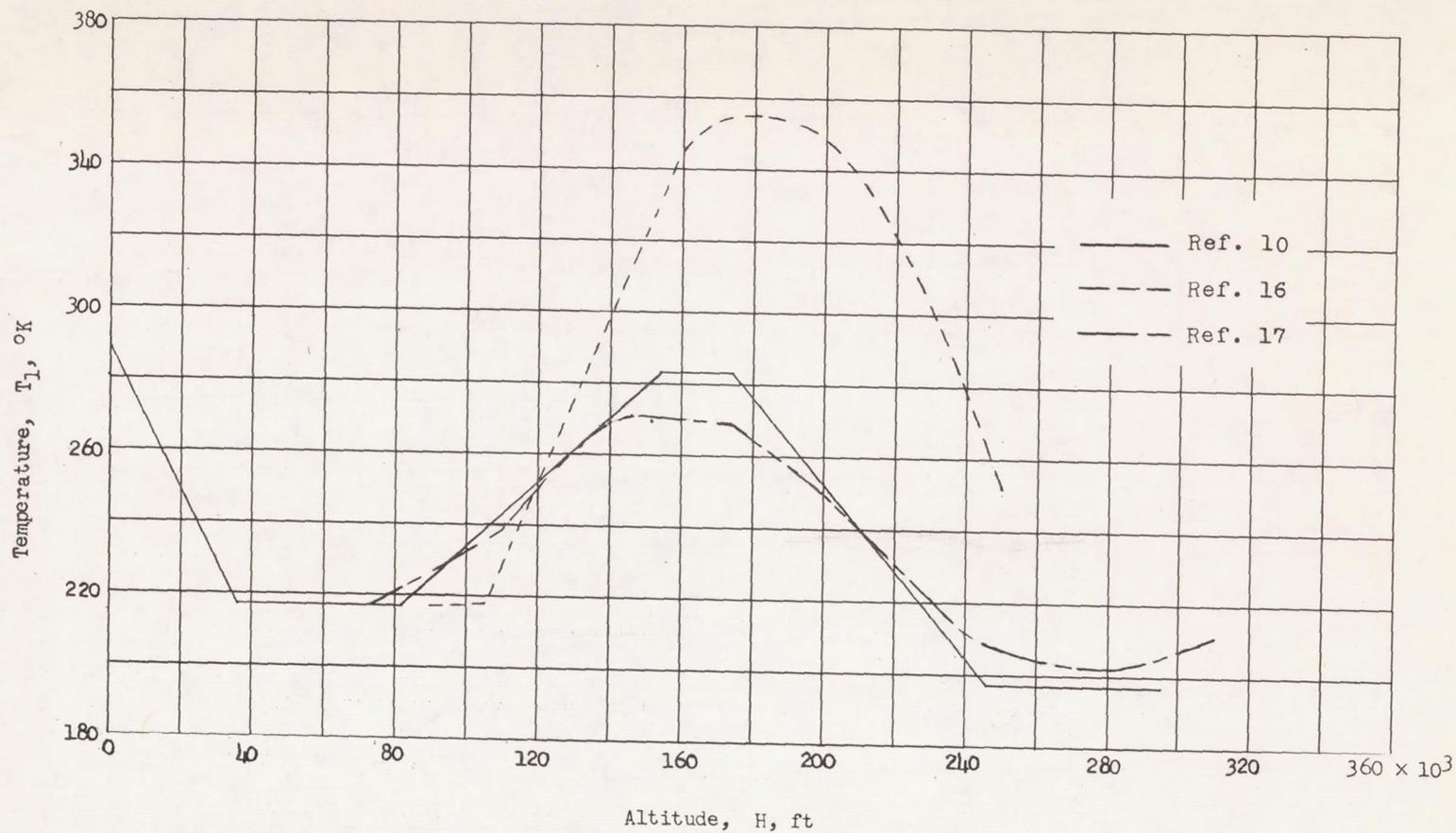


Figure 1.- Variation of atmospheric temperature with altitude.

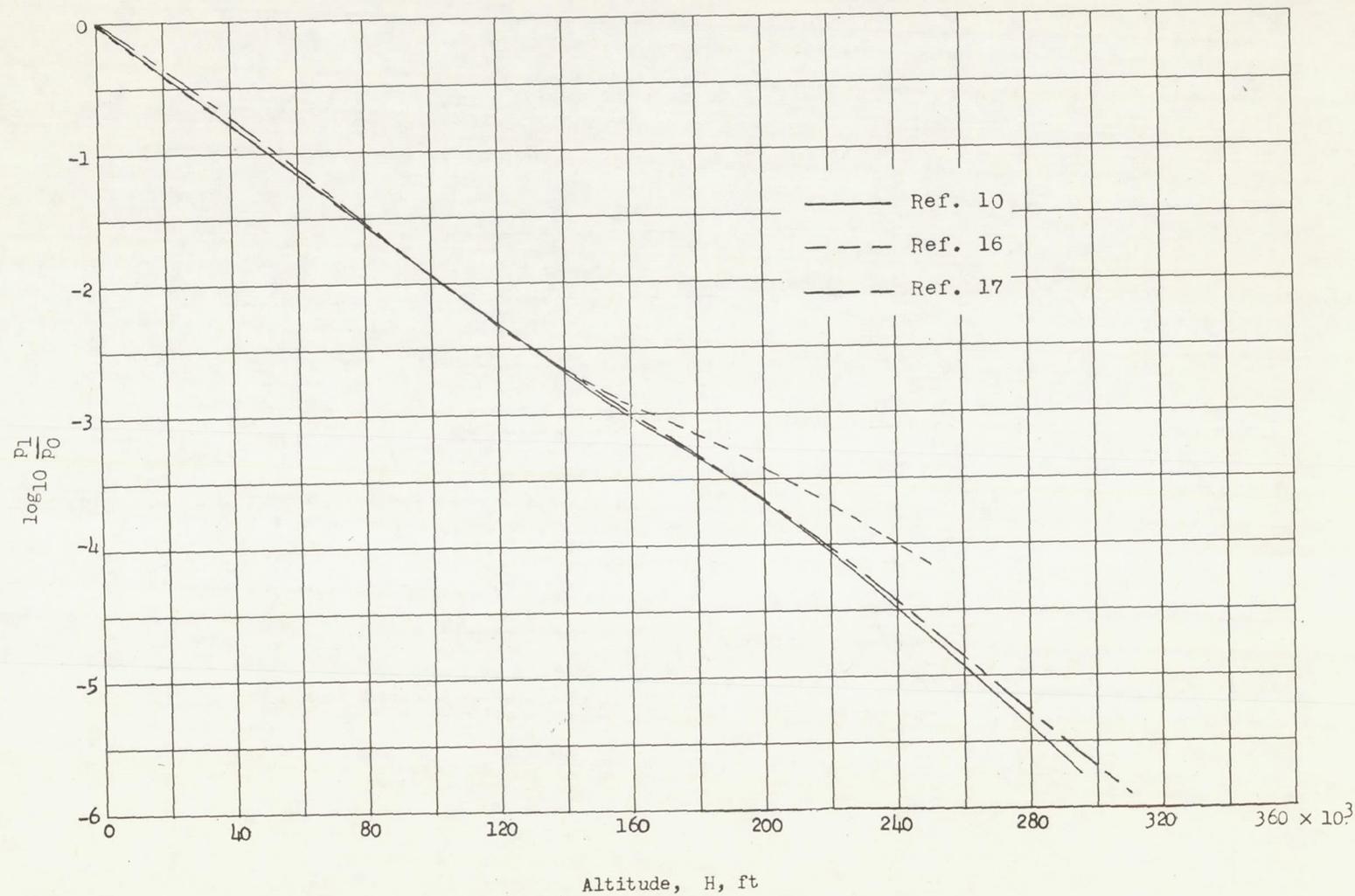


Figure 2.- Variation of atmospheric pressure with altitude.

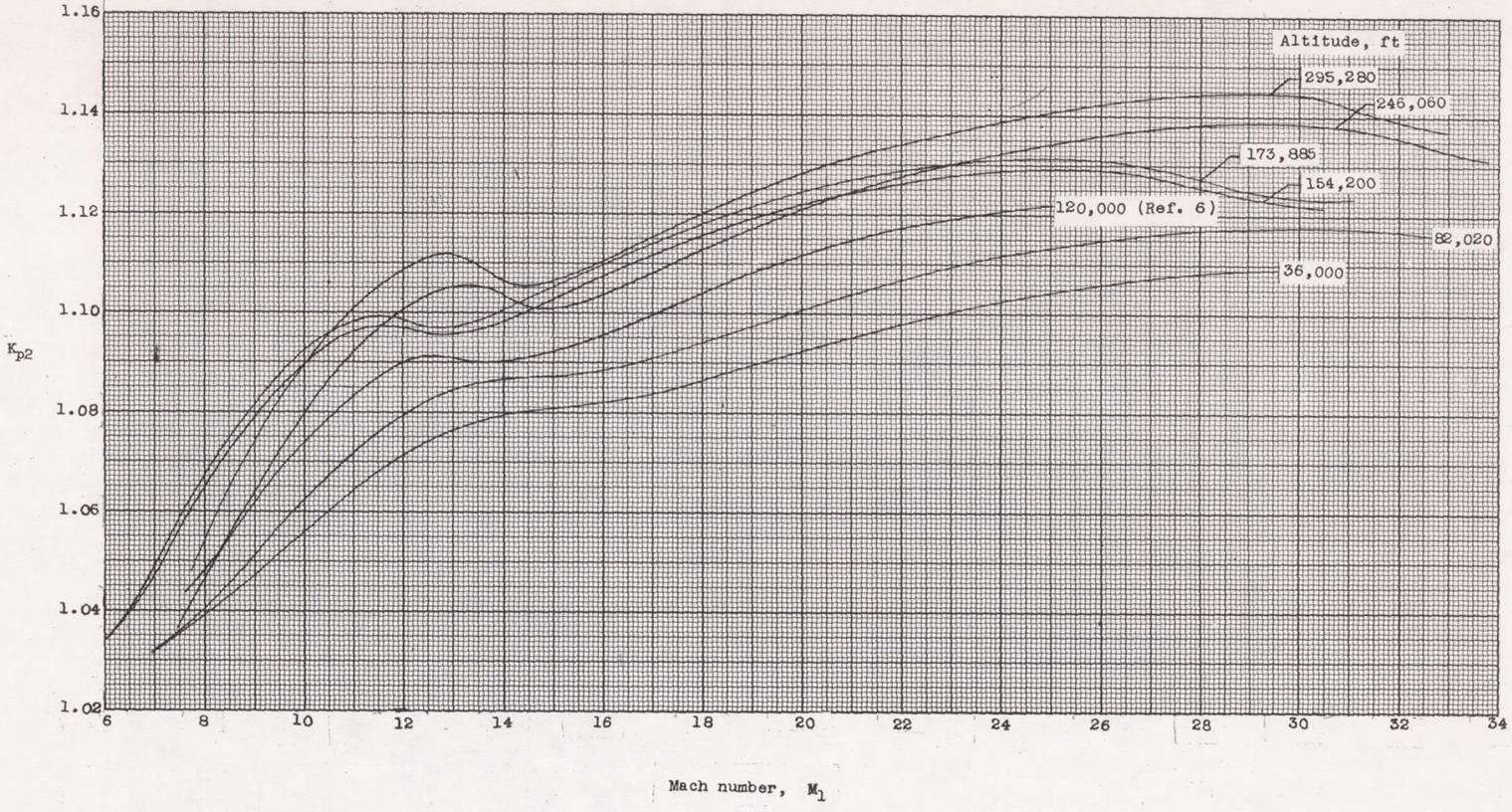


Figure 3.- Variation with Mach number and altitude of the ratio of real to ideal values of normal-shock pressure ratio.

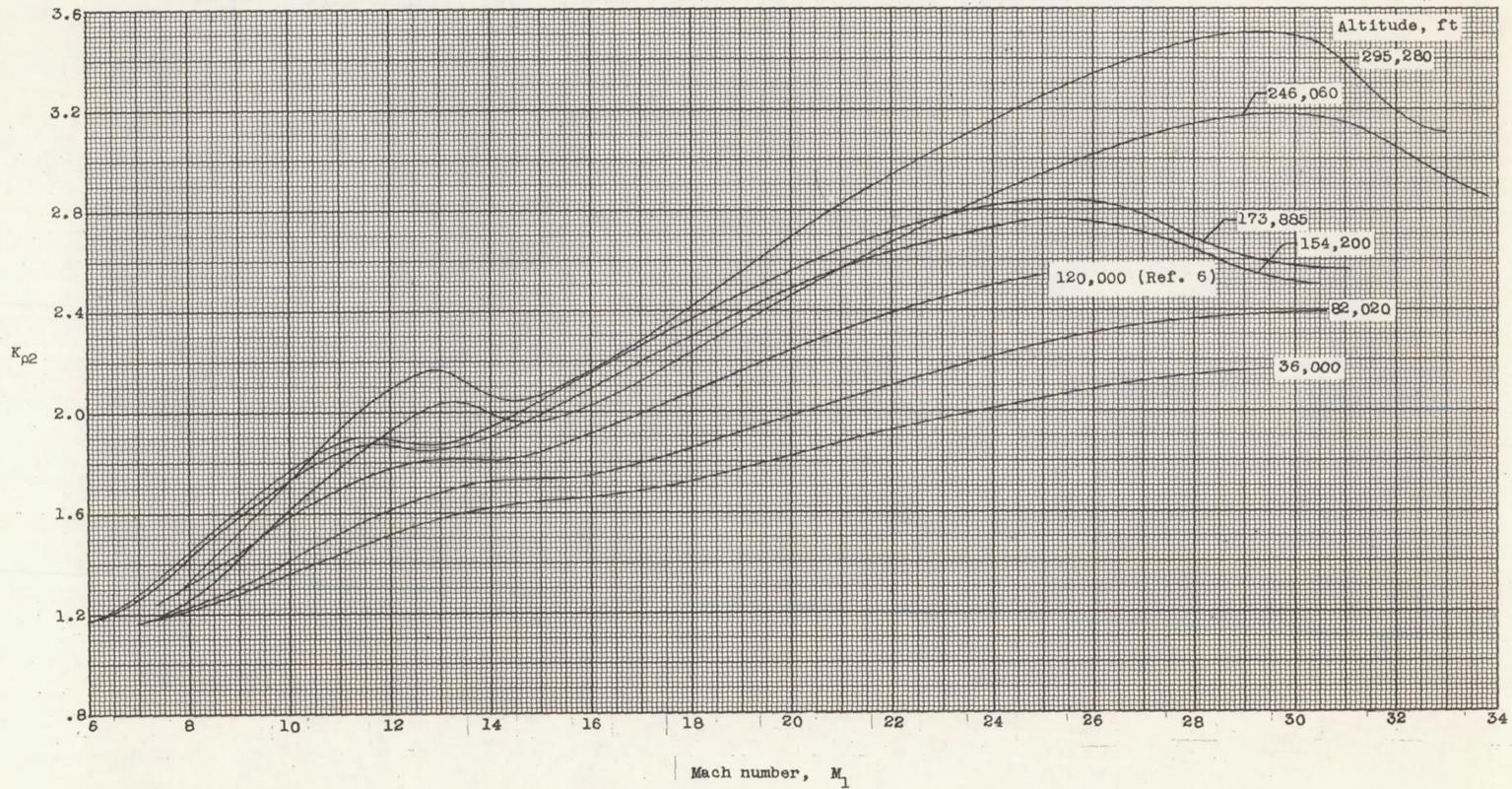


Figure 4.- Variation with Mach number and altitude of the ratio of real to ideal values of normal-shock density ratio.

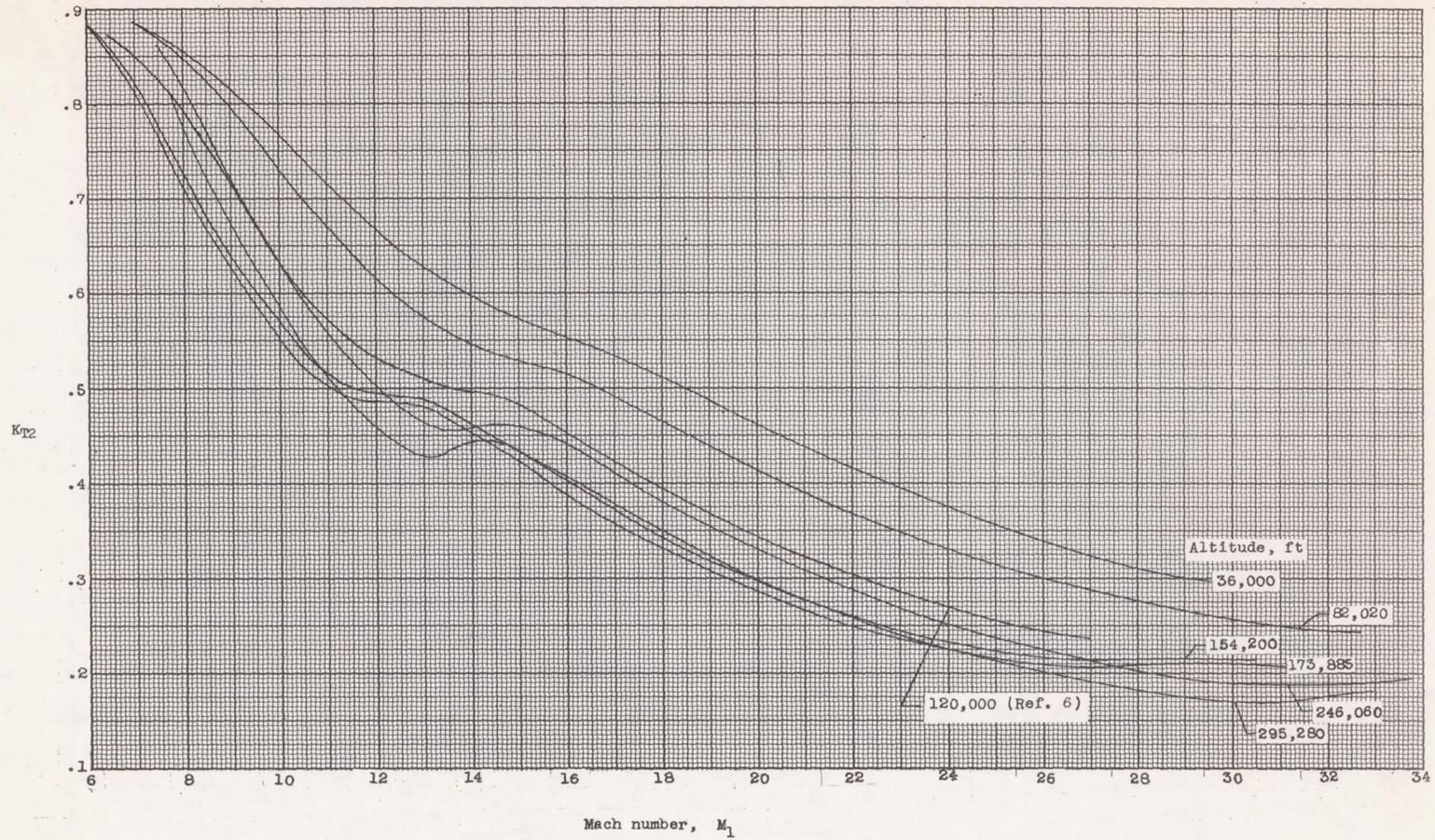


Figure 5.- Variation with Mach number and altitude of the ratio of real to ideal values of normal-shock temperature ratio.

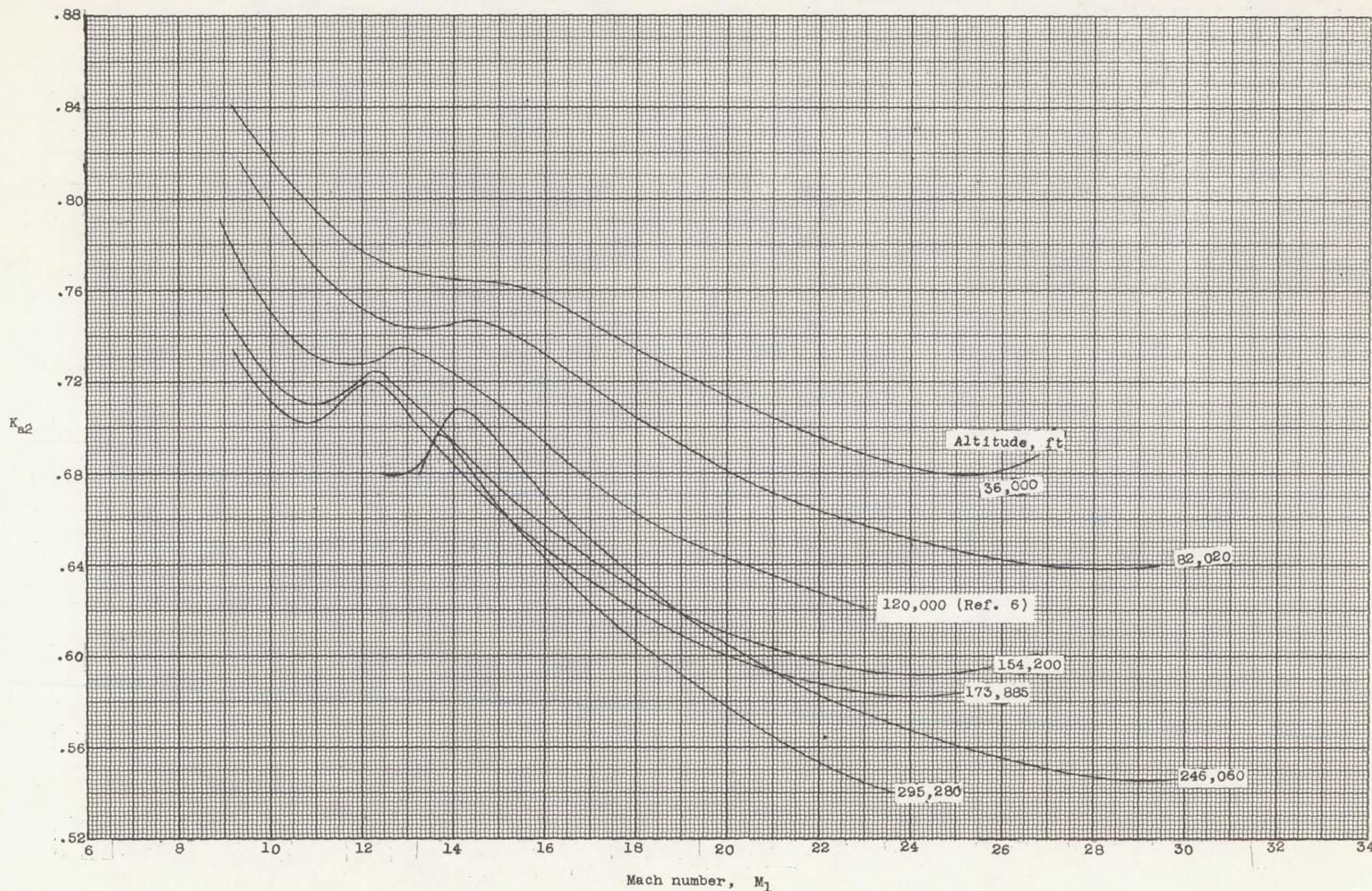


Figure 6.- Variation with Mach number and altitude of the ratio of real to ideal values of normal-shock velocity-of-sound ratio.

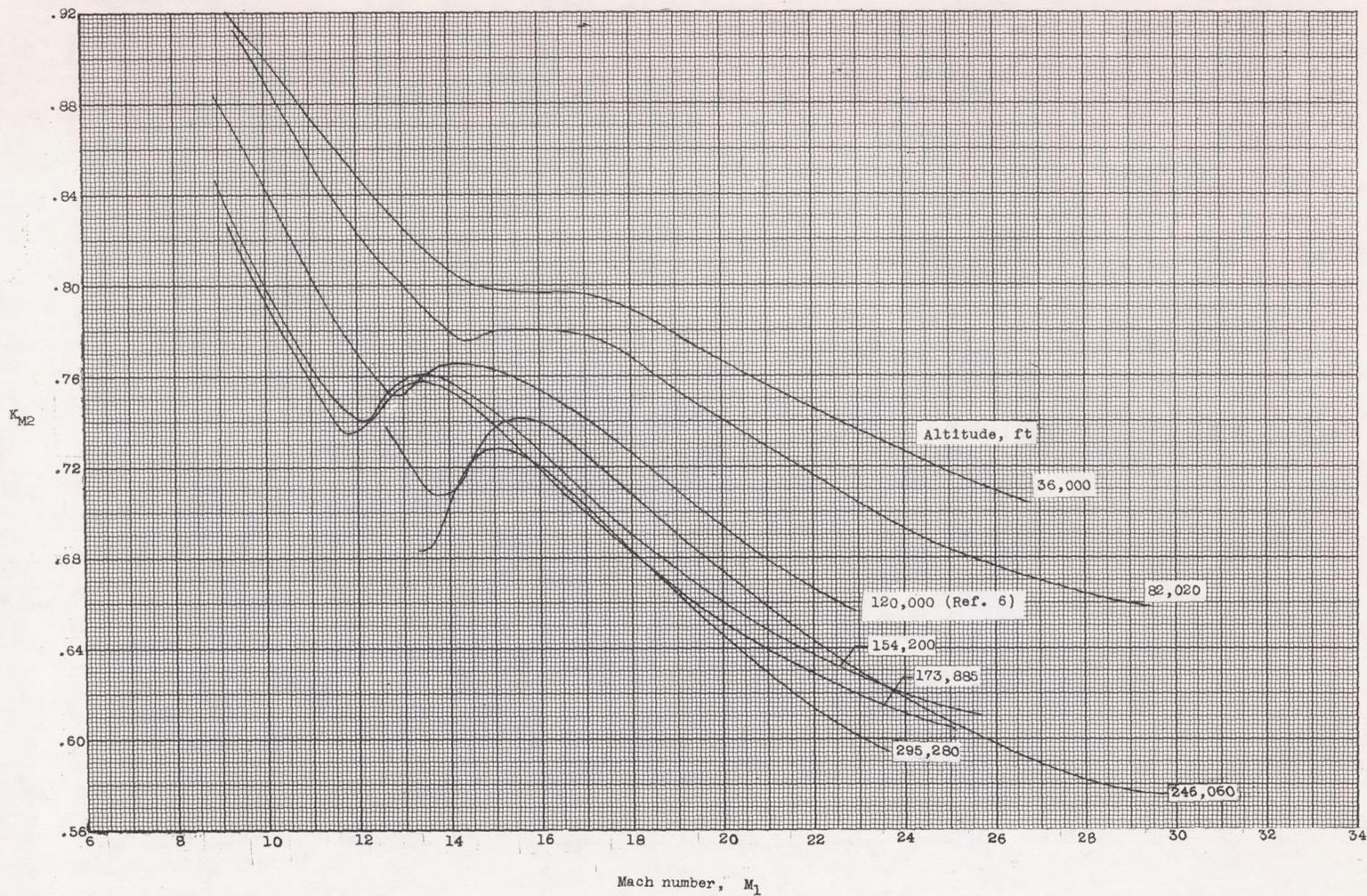


Figure 7.- Variation with Mach number and altitude of the ratio of real to ideal values of Mach number behind normal shock.

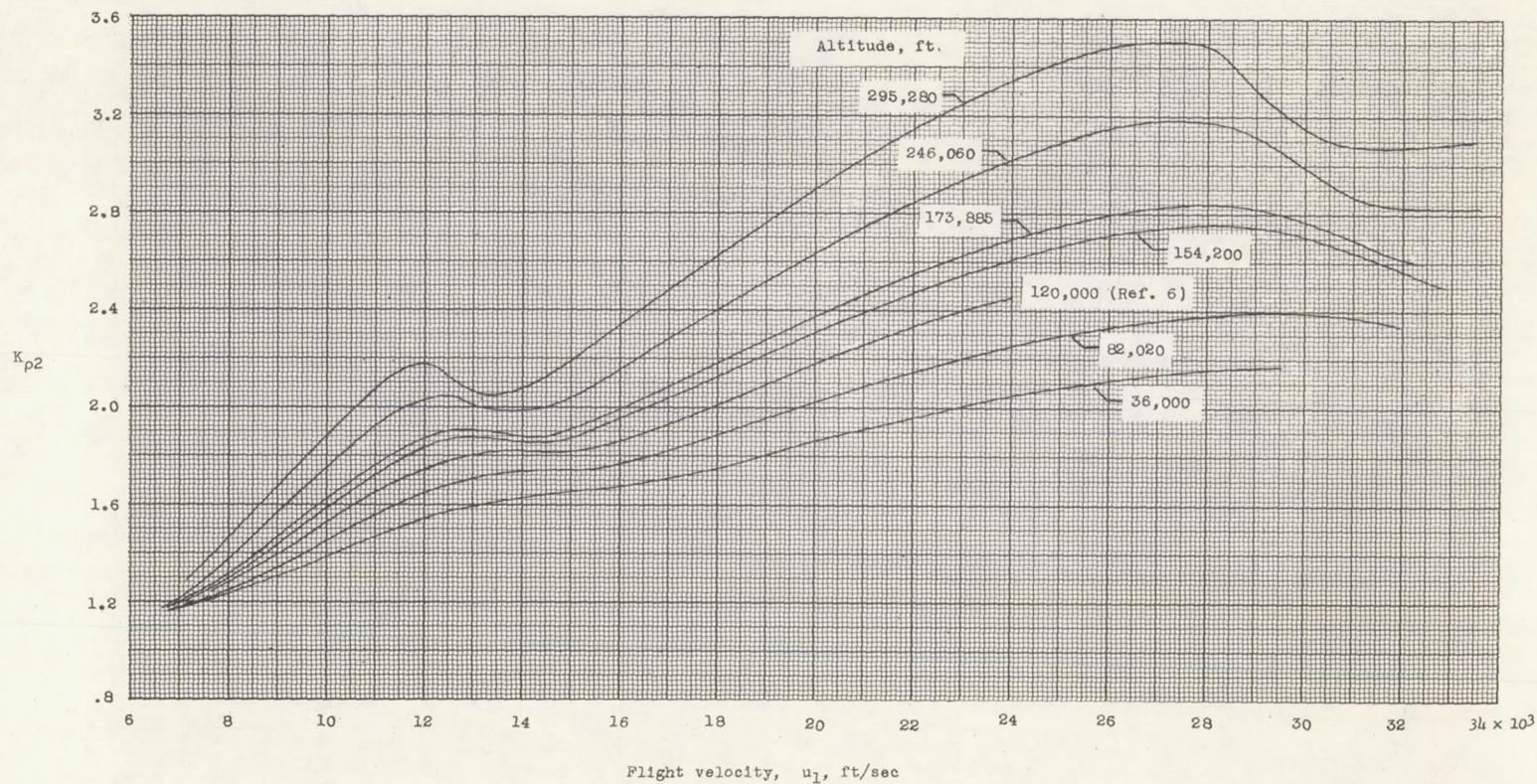


Figure 8.- Variation with flight velocity and altitude of the ratio of real to ideal values of normal shock density ratio.

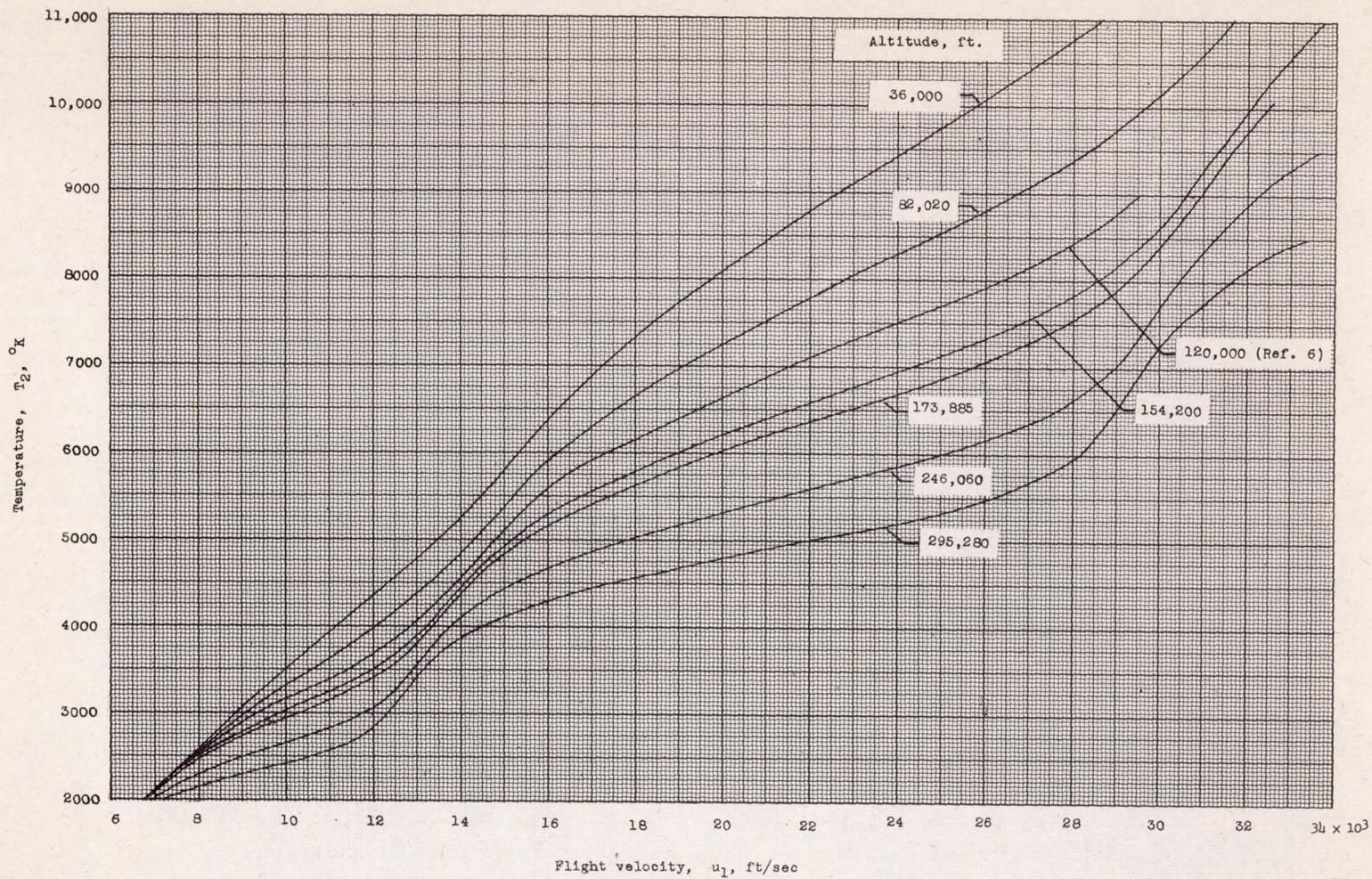


Figure 9.- Variation with flight velocity and altitude of the temperature behind a normal shock.

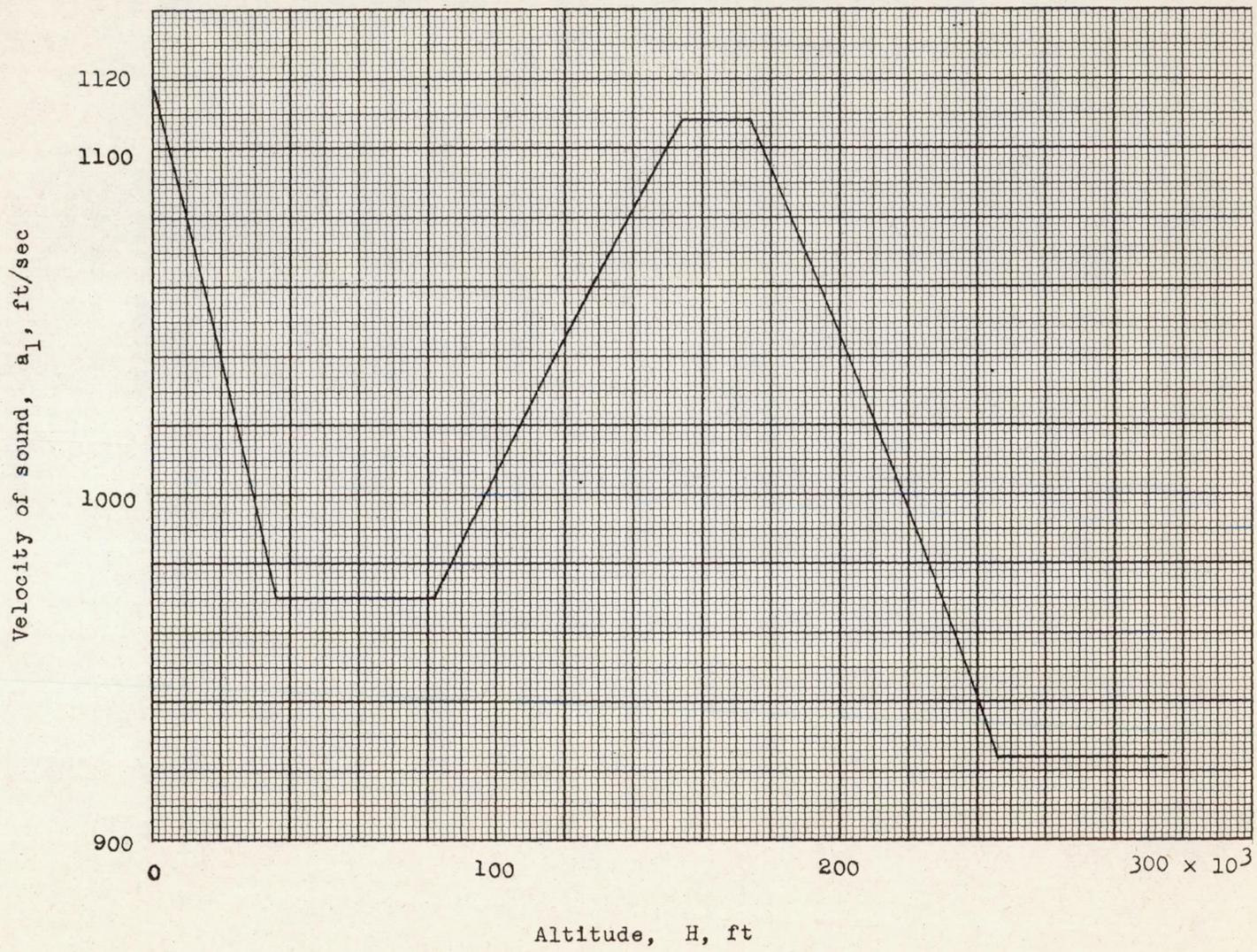


Figure 10.- Variation of velocity of sound with altitude for an argon-free model atmosphere.