RESEARCH MEMORANDUM

ANALYTICAL AND EXPERIMENTAL INVESTIGATION OF THRUST AUGMENTATION OF AXIAL- AND CENTRIFUGAL-COMPRESSOR TURBOJET ENGINES BY INJECTION OF WATER AND ALCOHOL IN COMBUSTION CHAMBERS

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NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

WASHINGTON
April 13, 1950
Declassified November 8, 1957
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SUMMARY

An investigation of thrust augmentation by injection of water and water-alcohol mixtures in the combustion chambers has been conducted at sea-level zero-ram flight conditions on 4000-pound-thrust axial-flow and centrifugal-flow turbojet engines. The engines were equipped with variable-area exhaust nozzles that were used to maintain constant turbine-outlet temperatures during injection. The thrust augmentation, compressor characteristics, fuel flow, and turbine-outlet-temperature distributions are presented for various injection rates and water-alcohol mixtures. The thrust augmentation obtained by combustion-chamber injection is compared with results of both inlet injection and interstage injection from other investigations for the axial-flow-type engine. A method of computing the thrust augmentation by injection into the combustion chambers is also presented and is compared with the results of the experimental investigation of the axial-flow engine.

A maximum ratio of augmented to normal thrust of 1.18 was obtained for the axial-flow-compressor engine by the injection of 0.78 pound per second of alcohol and 4.6 pounds per second of water into the combustion chamber. The computed augmented-thrust ratios were within 1 percent of the experimental results. No appreciable thrust augmentation was obtained with the centrifugal-flow-type engine by injection of water into the combustion chamber. This result is explained by the shape of the compressor-characteristic curves for this engine.
INTRODUCTION

As a part of a general research program of thrust augmentation of turbojet engines, several investigations of injection of water and water-alcohol mixtures have been conducted at the NACA Lewis laboratory. Results of investigations of injection of water and alcohol into the compressor inlets of both axial- and centrifugal-flow engines are presented in references 1 to 3. Interstage injection into the compressor of an axial-flow engine was also investigated (reference 4).

An investigation of water and water-alcohol injection into the combustion chambers of 4000-pound-thrust axial- and centrifugal-flow engines at sea-level, zero-ram conditions is reported herein. Similar injection systems were used on both the axial- and centrifugal-flow engines; four different arrangements of injection nozzles were investigated on the axial-flow engine. Both engines were equipped with variable-area exhaust nozzles to provide control of the exhaust-gas temperature independent of injection rate and engine speed. The investigation with the axial-flow engine was conducted at limiting conditions of speed and exhaust-gas temperature and covered a range of injection rates from 0 to 4.6 pounds per second of water with 0.8 pound per second of alcohol and a somewhat smaller range of injection rates with water alone. The investigation with the centrifugal-flow engine was conducted over a range of engine speeds and was confined to the injection of 1 and 2 pounds per second of water alone.

The thrust-augmentation and fuel-flow data, compressor characteristics, and turbine-outlet temperature distributions are given for the various injection-nozzle arrangements used in the axial-flow engine. For the centrifugal-flow engine, thrust data and compressor characteristics are presented. The thrust augmentation of the axial-flow engine is compared to that obtained with inlet injection and interstage injection. A method of computing the thrust augmentation by combustion-chamber injection is also presented and is compared with the experimental results for the axial-flow engine.

APPARATUS

Engines. - The investigation was conducted on J35 and J33 engines. The J35 engine has an 11-stage axial-flow compressor, eight cylindrical combustion chambers, and a single-stage turbine. The nominal military rating of the engine is 4000-pounds thrust at a rotor speed of 7700 rpm and zero-ram, sea-level conditions.
The J33 engine has a double-entry centrifugal-flow compressor, 14 cylindrical combustion chambers, and a single-stage turbine. The nominal military rating of the engine is 4000-pounds thrust at 11,500 rpm and zero-ram, sea-level conditions.

Engine installation and component parts. - The general arrangement of the installation of the J35 engine in the test chamber is shown in figure 1. The J33 setup was similar in most details. The engine was mounted on a swinging framework suspended from the ceiling of the test chamber; the engine thrust was balanced and measured with an air-pressure diaphragm. Engine air entered the nearly airtight chamber through two 18-inch-diameter A.S.M.E. nozzles that were used to measure the air flow. The engine speed and the fuel flow were measured with standard instrumentation.

A spherical clamshell-type variable-area exhaust nozzle was installed at the end of a tail pipe 30 inches in length, which provided for discharge of the exhaust gas outside the test chamber. A cowling was installed at the engine inlet to facilitate measurement of the engine inlet-air temperature.

Liquids. - For this investigation AN-F-32 (Amendment-3) fuel was used. The alcohol used was a mixture of 50-percent methyl and 50-percent ethyl alcohol by volume. The water was obtained from Cleveland city mains.

Water-alcohol injection systems. - For the investigation in the J35 engine four modifications of the water- and alcohol-injection nozzles, designated nozzle arrangements A, B, C, and D, were used. The locations and the details of installation of the nozzles are shown in figure 2. The number, size, type, and location of injection nozzles used are listed in the following table:
On the basis of preliminary investigations conducted on a
single combustion chamber (reference 5), the liquids were introduced
at approximately the midpoint of the combustion chamber into the
primary combustion zone near the liner walls. The injected liquids
entered the nozzles tangentially; the swirl thereby induced
a fine hollow cone spray for all of the injection systems except D.
System D utilized nozzles with straight through flow to obtain a
solid jet. In all configurations the water was introduced upstream
of the alcohol.

Only one injection system was used on the J33 engine. One
solid jet and three hollow-cone water-injection nozzles (similar
to those used on the J35 engine) were attached to each burner at
the locations shown in figure 3. The nozzles were located as near as possible to the midpoint of each combustion chamber. The number, size, type, and location of nozzles used in the J33 engine are summarized in the following table:

<table>
<thead>
<tr>
<th>Type Spray</th>
<th>Nozzles per Chamber</th>
<th>Throat Diameter (in.)</th>
<th>Distance from upstream flange of chamber, (in.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hollow Cone</td>
<td>3</td>
<td>3/16</td>
<td>12</td>
</tr>
<tr>
<td>Solid Jet</td>
<td>1</td>
<td>3/16</td>
<td>12</td>
</tr>
</tbody>
</table>

The single solid-jet-type nozzle (used in each combustion chamber) was installed on the outer periphery of the engine in an effort to eliminate a high-temperature region at the root of the turbine blades.

**Temperature and pressure instrumentation.** - The locations of temperature and pressure instruments on both engines are shown in figure 1. The number, type, and location of thermocouples in the J35 engine were as follows:

(a) Total temperature at engine inlet (station 0) \( T_0 \): Average of 20 thermocouples, five in each of four rakes 90° apart, at entrance to inlet cowlung

(b) Total temperature at compressor outlet (station 2) \( T_2 \): Average of 20 thermocouples, five in each of four rakes located upstream of combustion chambers 2, 4, 6, and 8

(c) Turbine-outlet-temperature survey downstream of the combustion chambers (station 5) \( T_5 \): four rakes of four thermocouples each located at four radii downstream of center lines of combustion chambers 2, 4, 6, and 8. The four thermocouple readings at each radius were averaged to obtain an average radial temperature distribution.
(d) Turbine-outlet-temperature survey between combustion chambers (station 5) $T_{5'}$: four rakes of four thermocouples located at four radii downstream of midpoints between burners 2 and 3, 4 and 5, 6 and 7, and 8 and 1. The four thermocouple readings at each radius were averaged to obtain an average radial temperature distribution.

(e) Temperature at tail-pipe inlet (station 7) $T_{7}$: Average of eight strut-type thermocouples equally spaced circumferentially and 4 inches from tail-pipe wall.

The number, type, and location of pressure tubes in the J35 engine were as follows:

(a) Total pressure at engine inlet (station 0) $P_{0}$: one open-end tube in quiescent zone of test chamber

(b) Total pressure at compressor outlet (station 2) $P_{2}$: Average of 12 total-pressure tubes, three in each of four rakes upstream of combustion chambers 1, 3, 5, and 7

Similar instrumentation was used for the J33 engine.

PROCEDURE

The investigation of engine performance with water and alcohol injection in the combustion chambers of the J35 engine was conducted for the following injection flows:

<table>
<thead>
<tr>
<th>Nozzle arrangement</th>
<th>Water flow (lb/sec)</th>
<th>Alcohol flow (lb/sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A,B,C,D</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>A,B,C,D</td>
<td>0.8</td>
<td>0,0.8</td>
</tr>
<tr>
<td>A,B,C,D</td>
<td>1.6</td>
<td>0,0.8</td>
</tr>
<tr>
<td>A,B,C,D</td>
<td>2.4</td>
<td>0,0.8</td>
</tr>
<tr>
<td>A,B,C,D</td>
<td>3.2</td>
<td>0.8</td>
</tr>
<tr>
<td>A,B,D</td>
<td>3.2</td>
<td>0</td>
</tr>
<tr>
<td>C,D</td>
<td>4.0</td>
<td>0.8</td>
</tr>
<tr>
<td>C</td>
<td>4.25</td>
<td>0.8</td>
</tr>
<tr>
<td>D</td>
<td>4.6</td>
<td>0.8</td>
</tr>
</tbody>
</table>
All runs were made at an indicated engine speed of 7700 rpm with an indicated tail-pipe temperature of 1660° R (maintained by exhaust-nozzle adjustment). The runs with zero water and alcohol injection were conducted periodically during the course of the investigation in order to provide normal performance data upon which to base the thrust augmentation.

Injection into the combustion chambers of the J33 engine was investigated over an engine-speed range from 10,500 to 11,500 rpm. Two series of runs were conducted, one with an exhaust-nozzle size providing an indicated tail-pipe temperature of 1685° R at 11,500 rpm and the other with an exhaust-nozzle size providing an indicated tail-pipe temperature of 1660° R at 11,500 rpm (both maintained by exhaust-nozzle adjustment) with water-injection flows of 1.0 and 2.0 pounds per second, respectively. The reason for operating at two tail-pipe temperatures will be subsequently discussed. Normal performance data were also obtained over a range of engine speeds with the exhaust-nozzle size providing an indicated tail-pipe temperature of 1685° R at 11,500 rpm upon which to base the augmentation.

CORRECTION AND ADJUSTMENT OF DATA

All performance data presented were corrected to standard sea-level conditions by use of the conventional generalization parameters in order to adjust for small variations in inlet conditions that occurred during the investigation. These factors, although unverified by experiment for application to combustion-chamber injection data, are believed accurate for the small ranges of inlet conditions encountered in this investigation; they should not be used, however, to extrapolate the present data to altitude conditions without further experimental verification.

The corrected engine-performance parameters are:

\[
\begin{align*}
F/\delta & \quad \text{thrust} \\
N/\sqrt{\theta} & \quad \text{engine speed} \\
F/\delta & \quad \text{pressure} \\
T/\theta & \quad \text{temperature} \\
\frac{W_{\text{air}}/\sqrt{\theta}}{\delta} & \quad \text{air flow}
\end{align*}
\]
injected-water flow

\[
\frac{W_w \sqrt{\theta}}{\delta}
\]

injected-alcohol flow

\[
\frac{W_\text{al} \sqrt{\theta}}{\delta}
\]

combined fuel flow

\[
\frac{W_f K}{\delta \sqrt{\theta}}
\]

where

\[
\delta = \frac{\text{compressor-inlet total pressure}}{\text{NACA standard sea-level pressure}}
\]

\[
\theta = \frac{\text{compressor-inlet total temperature}}{\text{NACA standard sea-level temperature}}
\]

All the symbols used in this report are defined in appendix A.

The correction factors applied to the injected-water and injected-alcohol flows are the same as those applied to the air flow in order to maintain the same water-air and alcohol-air ratios before and after data correction. The factor \( K \) included in the correction to engine-fuel flow serves to maintain a heat balance from uncorrected to corrected conditions. The factor \( K \) is defined as follows:

\[
K = 1 + \left( \frac{1200}{\eta_f h_f} \frac{W_\text{f}}{W_f} - 0.35 \frac{W_\text{al}}{W_f} \right) (\theta - 1)
\]

where \( h_f \) is the heating value of the fuel and \( \eta_f \) is the combustion efficiency. The value of 0.35 in the equation is the effective ratio of the net heating value of the alcohol to the net heating value of the fuel and was obtained from analysis of the data reported herein. The value of 1200 accounts for the enthalpy rise of the water during vaporization.

Because the investigation of the axial-flow engine was conducted at various ambient conditions, the data were not obtained at exactly the same corrected engine speeds and tail-pipe temperatures. Additional adjustment of the data was therefore made to reduce the results to a constant corrected engine speed of 7550 rpm.
and a tail-pipe temperature of 1580° R. These adjustments were made by using the slopes of curves of the corrected engine-performance parameters plotted against engine speed for nonaugmented operation. Although this procedure may not be exact, the resultant error for the small range of engine speeds involved (7400 to 7700 rpm) is believed to be negligible.

**ANALYSIS**

The effect on engine operation of injection of liquids into the combustion chamber may be illustrated by reference to the compressor-characteristics curves of figure 4, which were obtained on the axial-flow engine. Because the flow through the turbine-nozzle throat is sonic and the area is fixed, the ratio of total gas flow to turbine-inlet (or compressor-outlet) pressure is constant for a given turbine-inlet temperature if the change in physical properties of the working fluid with injection of water is neglected. The injection of water and alcohol therefore tends to produce a decrease in compressor air flow. This air-flow decrease, however, is accompanied by a simultaneous increase in compressor-pressure ratio, as shown by the compressor-characteristic curves for a given engine speed. A new equilibrium operating point of the engine, having a lower compressor air flow, a higher compressor-pressure ratio, and hence a higher total gas flow through the turbine, is thus obtained. The thrust augmentation produced therefore depends on the operating characteristics of the compressor and is a result of both the increased mass flow and the higher jet velocity provided by the increased pressure ratio. In addition to these effects, the increased gas constant and specific heat of the water-alcohol-air mixture contribute, to a smaller degree, to an increase in the turbine-outlet pressure and consequently in the jet velocity.

The foregoing discussion of the fundamental effects of combustion-chamber injection on the engine cycle indicates that the thrust augmentation may be calculated from a knowledge of the compressor characteristics. Calculation of augmented-thrust ratios (ratio of augmented to normal thrust) was therefore made based on the experimental compressor-characteristic curve (fig. 4) for the engine. For this analysis, the new equilibrium running point between the compressor and the turbine was determined for various injection rates by graphically superimposing the compressor- and turbine-flow characteristics. (See appendix B.) Using the compressor-pressure ratio and air flow thus determined, the performance of the complete cycle was computed from values of
compressor efficiency computed from unaugmented test data, an assumed value of turbine efficiency, and conventional thermodynamic methods of analysis. The analysis was made for a range of water-injection rates from 1 to 5 pounds per second and for alcohol-injection rates of 0 and 0.78 pound per second. Calculations of thrust augmentation were made using values of thermodynamic properties of the working fluid (γ and R) taking into account the changes in these properties caused by the injected water and alcohol, and additional calculations were made neglecting these changes in gas properties. Further details of the method of analysis and the equations used are given in appendix B.

RESULTS AND DISCUSSION

The results of the investigations with the axial- and centrifugal-flow engines are presented separately and a comparison of combustion-chamber injection with other injection methods is given for the axial-flow engine.

Performance of Axial-Flow Engine

Compressor operating characteristics. - The shift in the engine operating point with combustion-chamber injection (previously discussed) is illustrated in figures 5 and 6. The air flow and compressor-pressure ratio for nozzle-arrangement C are plotted against the total liquid flow for constant corrected engine speed and tail-pipe gas temperature. Figure 5 shows that the air flow decreases slightly with increased liquid-injection rates. Although the scatter in the data is relatively large, the trend was confirmed by data from other nozzle arrangements. The small change in air flow is accompanied by a relatively large change in compressor-pressure ratio, as shown by the data in figure 6. The curve of pressure ratio predicted from the measured air flow and the compressor-characteristic curves of figure 4 is shown by the dashed line in figure 6. The departure of the dashed curve from the experimental points is attributed to discrepancies in the air-flow data.

Experimental thrust augmentation. - The augmented-thrust ratios experimentally obtained for the four injection-nozzle arrangements are plotted in figure 7 as a function of corrected total liquid flow for 0 and 0.78 pound per second of corrected injected-alcohol flows and for a corrected engine speed of 7550 rpm and a corrected tail-pipe temperature of 1580° R. All the data correlate, indicating that within the accuracy of the data the amount
of augmentation available for a given total liquid flow was independent of both the nozzle arrangement and the mixture of water and alcohol injected. The maximum injection rate of water alone was limited by the capacity of the engine fuel system to a flow of 3.2 pounds per second. For this condition, the augmented-thrust ratio was 1.12 with a total liquid flow of 4.6 pounds per second. For the water-alcohol mixture, the maximum injected flow rate was 4.6 pounds per second of water plus 0.78 pound per second of alcohol as limited by hot streaks and overheating of the engine tail pipe. The maximum augmented-thrust ratio obtained at this point was 1.18 with a total liquid flow of 6.63 pounds per second. The augmented-thrust ratio showed no tendency to drop off with increased injected flow rate. This result indicates that higher augmentations might have been obtained with an improved injection system that would permit operation with higher flows. Operation of the engine became increasingly impaired, however, as the injected flows were increased, as will be subsequently discussed.

Fuel flow. - The corrected fuel flow obtained with nozzle-arrangement C is plotted against corrected injected-water flow for 0 and 0.78 pound per second of injected-alcohol flow in figure 8. The fuel flow increases rapidly as the injected-water flow increases and decreases with injected-alcohol flow. With an alcohol flow of 0.78 pound per second and a water flow of 2.67 pounds per second, the fuel flow is equal to the fuel flow without injection. The mixture of water and alcohol for constant engine fuel flow is therefore 23-percent alcohol by weight. The data are insufficient to determine whether the engine could be operated at this constant fuel flow for other injected flows with this mixture.

An increase in the injected-alcohol flow from 0 to 0.78 pound per second decreased the fuel flow required by approximately 0.27 pound per second. Calculations based on these flow rates and on heating values of 18,700 and 10,900 Btu per pound for fuel and alcohol, respectively, and for a fuel combustion efficiency of 95 percent indicate that 56 percent of the heating value of the alcohol is released in the combustion chambers.

Turbine-outlet temperature surveys. - Temperature surveys at the turbine outlet for various rates of water and alcohol injection with nozzle-arrangement D are shown in figure 9. The temperature distributions for nozzle-arrangements A, B, and C were similar to those for arrangement D, and no significant differences were obtained by the changes made in the nozzle arrangement. Curves are shown for the average radial distribution between burners and directly downstream of the burners. (See section entitled "Temperature and Pressure Instrumentation" for location of thermocouple rakes.)
All the data are for the same over-all average tail-pipe gas temperature (1660° R). The radial temperature gradient is about the same for all injection rates; increasing the injected-water and alcohol flow decreased the temperatures between the combustion chambers (fig. 9(a)) by about the same amount as it increased the temperatures directly downstream of the burner (fig. 9(b)). The change in temperature was approximately 300° R for an injection of 4.6 pounds per second of water and 0.78 pound per second of alcohol. Inasmuch as the gas temperature for unaugmented operation was higher directly downstream of the combustion chambers, injection had the effect of increasing the highest temperatures and decreasing the lowest temperatures.

Operating characteristics. - Visual observations of the engine during this investigation showed that water-injection rates above 3 pounds per second caused hot streaks to appear on the tail cone. In general, the hot streaks became brighter with increases in injected-water flow. The addition of alcohol to the injected mixture also caused the streaks to become more pronounced, possibly due to afterburning of the alcohol through the turbine. No significant difference was observed for any of the nozzle arrangements investigated, and because of these hot streaks the maximum injected flow was limited to 5.4 pounds per second.

Immediately after operation with injection of 4.6 pounds per second of water and 0.80 pound per second of alcohol during the investigation of nozzle-arrangement D, a turbine blade was found to be broken off at a point about one-third of the blade length from the tip. The warped condition of a number of the blades in the turbine-nozzle diaphragm after this failure is shown in figure 10.

The exact cause of these failures was not determined, but it is probable that the failures were caused by prolonged operation at maximum turbine-inlet temperature and engine speed with frequent changes in temperature distribution caused by variable rates of injection encountered while setting test conditions.

Comparison with other injection methods. - A comparison of thrust augmentation by water injection at the compressor inlet and by interstage injection with that obtained by combustion-chamber injection is shown in figure 11. The data for inlet injection (reference 2) and for interstage injection (reference 4) are compared with combustion-chamber-injection results on an uncorrected basis because of the uncertainty of the correction methods for inlet injection in an axial-flow-compressor engine. The comparison shows that injection at the compressor inlet
produces greater thrust augmentation than combustion-chamber injection throughout almost the entire range of flows investigated. The use of compressor-inlet injection at total liquid flows above 3.5 or 4.0 pounds per second, however, has been found to result in sufficient centrifugal separation of the liquid and air and attendant uneven temperature distributions in the compressor to produce rubbing of the compressor blades on the casing (reference 2). In view of this limitation to the applicability of compressor-inlet injection, it appears that for augmented-thrust ratios above about 1.14 the combustion-chamber injection system is superior to that of inlet injection. Interstage injection produces a greater thrust augmentation over the entire range of liquid flows than combustion-chamber injection. The maximum difference is about 5 percent of the normal thrust at a total liquid flow of 5.5 pounds per second.

Calculated augmented-thrust ratio. - The augmented-thrust ratio calculated by the method discussed in the section entitled "Analysis" and outlined in appendix B is shown in figure 12 and is compared with the curve of experimental augmented-thrust ratio taken from figure 7. Calculated curves are shown for two cases: (1) neglecting and (2) accounting for the effect of the presence of water and alcohol on the gas properties (γ and R). As previously discussed, the analysis was made for a range of injected-water flows from 1 to 5 pounds per second and for injected-alcohol flows of 0 and 0.78 pound per second; for simplicity, it was assumed that all the injected alcohol and fuel burned. On this basis, the augmented-thrust ratio as a function of total liquid flow was independent of the water-alcohol mixture for the range investigated and therefore the results for the various water-alcohol mixtures are not distinguished in figure 12. If a 50-percent combustion efficiency for the alcohol had been assumed (as indicated by the experimental results), an increase in total liquid flow of about 3 percent at the same augmented-thrust ratios would have been obtained for the conditions with alcohol injection. The curve of augmented-thrust ratio calculated by accounting for changes in gas properties with injection is about 1 percent higher than the experimental curve. The curve for calculated augmentation neglecting the changes in gas properties is considerably lower than the experimental curve, particularly at the higher total liquid flows. Results of the analysis further show that about one-fourth of the augmentation produced is due to changes in thermodynamic properties of the working fluid and of the remaining three-fourths, half is due to increased mass flow and half to increased jet velocity resulting from the higher compressor-pressure ratio. The thrust augmentation obtained by combustion-chamber injection may thus be calculated with good accuracy if the changes in gas properties are considered.
Performance of Centrifugal-Compressor Engine

The results of the investigations conducted with the centrifugal-flow engine are summarized in figure 13, in which the corrected thrust is plotted against the corrected engine speed for two tail-pipe-temperature settings at maximum engine speed. The maximum injected-water flow with the variable-area nozzle set for a tail-pipe temperature of 1685° R was limited to a flow between 1.5 and 2.0 pounds per second by compressor surge. Inasmuch as the thrust increase shown by the line for an injection rate of 1.0 pound per second was small, very little further increase could be expected up to surge. As an alternative method of operation, the tail-pipe gas temperature was reduced to 1660° R at maximum speed by increasing the exhaust-nozzle area to permit a higher total mass flow and an attendant higher injection rate, which was accompanied by a favorable change in gas properties before surge was encountered. The injected-water flow at this tail-pipe-temperature setting was limited to a flow between 2.0 and 2.5 pounds per second by compressor surge. The augmented thrust for a tail-pipe temperature of 1660° R and an injected-water rate of 2.0 pounds per second was, however, about the same as the normal thrust at a tail-pipe temperature of 1685° R. Thus for both conditions investigated, the thrust augmentation was very small.

The small increase in thrust with water injection is explained by the compressor-characteristic curves for a similar centrifugal-flow-type engine, which are replotted from an unavailable publication in figure 14. Also shown in this figure are the operating points for two rates of water injection. It is apparent that the shift in the compressor operating point with increased injection rate produces very little increase in compressor-pressure ratio due to the very flat compressor characteristic and, consequently, the compressor-outlet pressure is nearly constant for all injection rates from normal operation to surge. Because the compressor-outlet pressure is nearly constant (fig. 14), the mass flow through the engine was also nearly constant; hence the thrust produced is approximately constant.

SUMMARY OF RESULTS

The following results were obtained in the sea-level, zero-ram investigation of thrust augmentation of 4000-pound-thrust axial- and centrifugal-compressor turbojet engines by injection of water and water-alcohol mixtures in the combustion chambers:
1. The injection of liquids into the combustion chamber caused a shift in the equilibrium running point of the engine to a lower air flow, a higher pressure ratio, and a higher total mass flow rate. This shift in running conditions of the engine was a result of the flow limitations imposed by the turbine nozzles and depended in magnitude upon the compressor characteristics of the engine. From a knowledge of the compressor characteristics, the thrust augmentation produced could be calculated with a good degree of accuracy provided that changes in thermodynamic properties of the working fluid were properly accounted for. In a sample calculation, the computed augmented-thrust ratio was within 1 percent of the experimental results.

2. A maximum augmented-thrust ratio of 1.18 was obtained for the axial-flow-compressor engine for a maximum injection rate of 0.78 pound per second of alcohol and 4.6 pounds per second of water; the total liquid flow including fuel at this condition was 6.63 pounds per second.

3. Within the range of conditions investigated, the thrust augmentation of the axial-flow engine for a given total liquid flow was unaffected by the injection-nozzle arrangement used or by the mixture of water and alcohol injected.

4. For the four nozzle arrangements used on the axial-flow engine, the intensity of hot streaks in the tail pipe during operation with high total liquid flows was considered sufficiently severe to limit the amount of injected flow to values less than about $5\frac{1}{2}$ pounds per second.

5. The increase in compressor-pressure ratio with injection rate for the centrifugal-flow engine was small due to the flat compressor characteristic at the operating point. As a result, the total mass flow through the engine was nearly constant and the thrust increase was small. The injected-water flow for this engine was limited to small quantities by compressor surge.

6. Because combustion-chamber injection permitted operation at higher liquid flows than the operational limit with compressor-inlet injection, it is considered superior to inlet injection for the axial-flow engine for total liquid flows above 3.5 to 4.0 pounds per second. Compressor-interstage injection produced higher thrust augmentation than combustion-chamber injection over the entire range of liquid flows investigated.
7. Injection into the axial-flow engine had little effect on the radial turbine-outlet-temperature profile. The normally present circumferential temperature gradients, however, became more severe with increased injection rate, with the temperatures directly downstream of the combustion chambers increasing as much as 300°F and the temperatures between combustion chambers decreasing as much as 300°F as the injection rate was increased up to 5.4 pounds per second. Inasmuch as the temperature without injection was higher downstream of the combustion chamber, injection had the effect of increasing the highest temperatures and decreasing the lowest temperatures. Changes in the injection-nozzle arrangement had little effect on the temperature distributions.

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APPENDIX A

SYMBOLS

\( A_t \) effective turbine-nozzle-throat area, sq ft
\( C \) constant
\( C_v \) exhaust-nozzle velocity coefficient
\( c_p \) specific heat at constant pressure, Btu/(lb)(\(^{\circ}\)R)
\( F \) normal jet thrust (without injection), lb
\( F_A \) augmented jet thrust (with injection), lb
\( g \) mass conversion factor, ft/sec\(^2\)
\( h_f \) lower heating value of fuel, Btu/lb
\( J \) mechanical equivalent of heat, ft-lb/Btu
\( N \) engine speed, rpm
\( P \) total pressure, lb/sq in. abs.
\( p \) static pressure, lb/sq in. abs.
\( R \) gas constant, ft-lb/(lb)(\(^{\circ}\)R)
\( T \) total temperature, \(^{\circ}\)R
\( V \) velocity, ft/sec
\( W_a \) air flow, lb/sec
\( W_{al} \) injected-alcohol flow, lb/sec
\( W_f \) engine fuel flow, lb/sec
\( W_m \) flow of gas mixture passing through turbine, lb/sec
\( W_w \) injected-water flow, lb/sec
\( \beta \) function of properties of water-air mixture

\( \gamma \) ratio of specific heat

\( \delta \) compressor-inlet total pressure
NACA standard sea-level pressure

\( \eta_c \) compressor adiabatic efficiency

\( \eta_f \) combustion efficiency

\( \eta_t \) turbine adiabatic efficiency

\( \Theta \) compressor-inlet total temperature
NACA standard sea-level temperature

Subscripts:

A augmented

A' augmented neglecting changes in gas properties

A'' augmented accounting for changes in gas properties

a air

g gas

j jet

m mixture passing through turbine

S standard

w water

0 cowling or compressor inlet

2 compressor outlet

4 turbine inlet

5 turbine outlet
APPENDIX B

METHOD OF CALCULATING AUGMENTED-THRUST RATIO FOR COMBUSTION-CHAMBER INJECTION OF WATER AND ALCOHOL

The following values were assumed constant throughout the calculation:

\[ \begin{align*}
  c_{p,a} & \quad 0.24 \text{ Btu/(lb)(}^{\circ}\text{R)} \\
  (c_{p,m})_S & \quad 0.273 \text{ Btu/(lb)(}^{\circ}\text{R)} \\
  R_w & \quad 85.8 \text{ ft-lb/(lb)(}^{\circ}\text{R)} \\
  \eta_t & \quad 0.81 \\
  \gamma_a & \quad 1.4 \\
  \gamma_{m,S} & \quad 1.336
\end{align*} \]

For the engine speed considered, calculations of compressor efficiency \( \eta_c \) from the unaugmented test data (the data from which the compressor-characteristic curve was determined) showed that the efficiency was nearly constant at a value of 0.84. This value was accordingly used in the analysis.

The equilibrium running point of the engine for various rates of injection into the combustion chamber is determined by superimposing the compressor and turbine operating characteristics.

For supercritical-pressure ratio across the turbine nozzles, the mass flow of mixture through the turbine is given by

\[
W_m = \eta_t \frac{\gamma_m g}{R_m T_4} \left( \frac{2}{\gamma_m - 1} \right) \left( \frac{\gamma_{m+1}}{\gamma_{m+1}} \right)
\]

(1)
From zero-ram sea-level conditions

\[ P_0 = 2116 \text{ lb/sq ft} \] (2)

When pressure losses in the combustion chamber are neglected,

\[ P_2 = P_4 \] (3)

By use of equations (2) and (3), equation (1) may be written

\[ W_m = 2116 A_t \frac{P_2 P_0}{R_m T_4 (\gamma_m + 1) (\gamma_m^{-1})} \] (4)

A factor \( \beta \) is defined as

\[ \beta = \frac{\gamma_m + 1}{\gamma_m^{-1}} \] (5)

For these computations, the fuel flow and the injected-alcohol flow are neglected in evaluating \( \beta \). For a constant gas temperature, \( \beta \) is therefore a function of only the water-air mixture passing through the turbine.

For simplicity, the turbine-inlet temperature \( T_4 \) is considered constant for that part of the analysis concerned with establishing the operating point of the engine. For the rest of the analysis, the turbine-outlet temperature is assumed to be constant, and the turbine-inlet temperature variable. Check calculations reveal that this simplifying assumption produces negligible error.

Because \( T_4 \) is considered constant, a constant \( C \) may be defined as

\[ C = 2116 A_t \frac{\sqrt{\gamma}}{T_4} \] (6)

where \( A_t \) is evaluated from analysis of normal engine performance data.
By substituting equations (5) and (6) into equation (4)

\[ W_m = C\beta \frac{P_2}{P_0} \quad (7) \]

From conservation of mass for standard conditions

\[ (W_m)_S = (W_a)_S + (W_f)_S \quad (8) \]

and for augmented conditions

\[ (W_m)_A = (W_a)_A + (W_f)_A + W_w + W_{al} \quad (9) \]

For augmented conditions, substitution of equation (9) in equation (7) therefore gives

\[ (W_a)_A + (W_f)_A + W_{al} + W_w = C\beta \frac{P_2}{P_0} \quad (10) \]

Rearrangement of equation (10) gives

\[ (W_a)_A = C\beta \frac{P_2}{P_0} - [ (W_f)_A + W_w + W_{al} ] \quad (11) \]

This equation expresses the turbine-flow characteristics in terms of conventional compressor characteristics, that is, \( W_a \) and \( P_2/P_0 \).

Assumed values of \( W_a \) and \( W_w \) permit determination of corresponding values of \( \beta \). Assuming the temperature rise in the combustion chamber to be constant for all operating conditions and a combustion efficiency of 100 percent serves as a basis for evaluating the fuel flow \( W_f \) from the charts of reference 6, which includes the heating value of the alcohol. With all factors of equation (11) except \( P_2/P_0 \) thus determined or assumed, \( P_2/P_0 \) is calculated for several values of \( W_a \), and the points thus obtained are plotted on the same coordinates as the compressor-characteristic curve; the intersection of the two curves thus establishes the equilibrium running point of the engine. The final operating curves are shown in figure 15, where the compressor-characteristic curve for a corrected engine speed of 7550 rpm and the turbine-flow characteristics for a range of water- and alcohol-injection rates are illustrated.
When the running points of the engine for various injection rates and mixtures have been established by the foregoing procedure, the augmented-thrust ratios may be calculated by means of the following equations.

The temperature rise through the compressor is determined from the pressure ratio established by this procedure from

\[
T_2 - T_0 = \frac{T_0}{\eta_c} \left[ \frac{\gamma_a - 1}{\gamma_a} \right] (12)
\]

Because the compressor and turbine work are equal

\[
W_a c_p,a (T_2 - T_0) = W_m c_p,m (T_4 - T_5)
\]

Solving for the turbine-temperature ratio gives

\[
\frac{T_4}{T_5} = 1 + \frac{W_a c_p,a (T_2 - T_0)}{W_m c_p,m T_5} (13)
\]

Expressing the turbine pressure ratio in terms of the temperature ratio and substituting from equation (3) gives

\[
\frac{P_4}{P_5} = \frac{P_2}{P_5} = \left[ 1 + \frac{1}{\eta_t} \left( \frac{T_4}{T_5} - 1 \right) \right]^{\frac{\gamma_m}{\gamma_m - 1}} (14)
\]

The exhaust-nozzle pressure ratio may be determined from the compressor and turbine pressure ratios as follows:

\[
\frac{P_0}{P_5} = \left( \frac{P_0}{P_2} \right) \left( \frac{P_2}{P_5} \right) (15)
\]

Inasmuch as \( P_0 = P_0 \) at zero-ram sea-level conditions, equation (15) reduces to

\[
\frac{P_0}{P_5} = \left( \frac{P_0}{P_2} \right) \left( \frac{P_2}{P_5} \right) (15a)
\]
The expression for the jet thrust for zero-ram sea-level conditions is

\[ F = \frac{W_m}{g} V_j \]  (16)

Where

\[ V_j = C_v \sqrt{\frac{2 \gamma_m}{\gamma_m - 1}} g R_m T_5 \left[ \frac{\gamma_m - 1}{\gamma_m} \right] \]  (17)

Expressing the engine performance in terms of the augmented thrust ratio and canceling like terms gives

\[ \frac{F_{A'''}}{F_s} = \frac{\frac{W_{m,A'''}}{W_{m,S}}}{\frac{\gamma_m}{\gamma_m - 1} A_m, A} \left[ \frac{R_{m,A}}{R_{m,S}} \right] \left[ 1 - \frac{P_0}{P_5 A'''} \right] \]  (18)

For the case where the change in thermodynamic properties due to injection are neglected, equation (18) reduces to

\[ \frac{F_{A'\prime}}{F_s} = \frac{\frac{W_{m,A'\prime}}{W_{m,S}}}{\frac{\gamma_m}{\gamma_m - 1} A_s, S} \left[ \frac{R_{m,S}}{R_{m,S}} \right] \left[ 1 - \frac{P_0}{P_5 S} \right] \]  (19)
The specific heat of the air, water, fuel, and alcohol mixture is determined from the law of mixtures, as follows:

\[
c_{p,m} = c_{p,g} \left( \frac{W_m - W_w}{W_m} \right) + c_{p,w} \frac{W_w}{W_m}
\]  

(20)

where \( c_{p,g} \) as well as \( R_g \) to be used later, are determined from curves of specific heat of gases for various fuel-air ratios and temperatures prepared from the data of reference 7. The injected alcohol was considered as fuel in the fuel-air ratio used in these charts. The specific heat of the water vapor \( c_{p,w} \) is obtained from the following empirical equation of reference 8:

\[
c_{p,w} = 19.86 - \frac{597}{\sqrt{T}} + \frac{7500}{T}
\]  

(21)

Similarly, the value of the gas constant \( R_m \) is determined from

\[
R_m = R_g \left( \frac{W_m - W_w}{W_m} \right) + R_w \frac{W_w}{W_m}
\]  

(22)

The value of the specific heat function is determined from

\[
\frac{\gamma_m}{\gamma_{m-1}} = \frac{J c_{p,m}}{R_m}
\]

REFERENCES


Figure 1. - Typical installation of turbojet engine.
Figure 2. - Installation of water-alcohol injection nozzles in combustion chambers of axial-flow engine.
Figure 3. - Installation of water-injection nozzles in combustion chambers of centrifugal-flow engine.
Figure 4. - Compressor-characteristic curves for various exhaust-nozzle sizes on axial-flow engine.
Corrected injected-alcohol flow, \( W_a \sqrt{\delta/\delta} \) (lb/sec)

Corrected total liquid flow, \( W_w \sqrt{\delta/\delta} + W_a \sqrt{\delta/\delta} + W_{fK/\delta} \sqrt{\delta}, \) lb/sec

Figure 5. - Variation of corrected air flow with corrected total liquid consumption for 0 and 0.78 pound per second of injected alcohol flow for nozzle-arrangement C on axial-flow engine. Corrected engine speed, 7550 rpm; corrected tail-pipe temperature, 1580° R.
Corrected injected-alcohol flow, 
\( W_{al} / \delta \) 
(lb/sec)

- 0
- 0.78

Corrected total liquid flow, 
\( W_{w} \sqrt{\delta/\delta} + W_{al} \sqrt{\delta/\delta} + W_{fK/\delta} \sqrt{\delta}, \) 
lb/sec

Figure 6. - Variation of compressor-pressure ratio with corrected total liquid consumption for 0 and 0.78 pound per second of injected alcohol flow for nozzle-arrangement C on axial-flow engine. Corrected engine speed, 7550 rpm; corrected tail-pipe temperature, 1580° R.
Figure 7. - Augmented-thrust ratio for four nozzle arrangements on axial-flow engine. Corrected engine speed, 7550 rpm; corrected tail-pipe temperature, 1580° R.
Corrected injected-alcohol flow, 
\( W_{al} \sqrt{\delta/\delta} \) (lb/sec)

Corrected injected-water flow, \( W_{w} \sqrt{\delta/\delta} \), lb/sec

Figure 8. Variation of corrected fuel flow with corrected injected-water flow for nozzle-arrangement C on axial-flow engine. Corrected engine speed, 7550 rpm; corrected tail-pipe temperature, 1580° R.
Corrected injected flow
\[
\frac{W_w}{\sqrt{\theta/8}} \quad \frac{W_{al}}{\sqrt{\theta/8}}
\]
(\text{lb/sec}) \quad (\text{lb/sec})

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Radial distance across turbine-outlet annulus (measured from outside wall), in.

(a) Radial distribution between burners.

Figure 9. - Temperature surveys at turbine outlet of axial-flow engine for nozzle-arrangement D.
Figure 9. - Concluded. Temperature surveys at turbine outlet of axial-flow engine for nozzle arrangement D.
Figure 10. - Turbine-nozzle diaphragm for axial-flow engine after turbine-blade failure.
Figure 11. - Comparison of augmented-thrust ratio for water-alcohol injection in the combustion chamber with that for water injection at the compressor inlet and for water-alcohol injection interstage on axial-flow engine. Uncorrected engine speed, 7835 rpm; uncorrected tail-pipe temperature, 1665° R; engine-inlet temperature, 548° R.
Figure 12. - Comparison of calculated and experimental augmented-thrust ratio for axial-flow engine.

Corrected total liquid flow, $W_l \sqrt{\theta/\delta} + W_{al} \sqrt{\theta/\delta} + W_{rK/\delta} \sqrt{\theta}$, lb/sec
Figure 13. - Variation of corrected thrust for centrifugal-flow engine with corrected engine speed with and without injection.
Figure 14. - Runs with and without injection superimposed on compressor-characteristic curves for similar centrifugal-flow engine.
Figure 15. - Axial-flow-compressor characteristic curve for corrected engine speed of 7550 rpm showing operating points for several injection rates at zero-ram sea-level conditions.