AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG AND A COMPARISON WITH JET EFFECTS AT TRANSONIC SPEEDS

By Maurice S. Cahn

SUMMARY

Results are presented of an investigation of sting-support interference on afterbody drag at transonic speeds. Stings with varying diameter, cone angle, and cylindrical length were tested at the rear of a model with various afterbody shapes. The data were obtained at an angle of attack of 0° and at Mach numbers from 0.80 to 1.10. In general, the addition of a sting was found to cause a drag reduction. A method is presented whereby approximate sting-interference corrections may be made to models with afterbodies and sting supports of size and scale similar to those of this investigation, provided the boundary layer is turbulent at the model base and the Reynolds numbers are of the same order of magnitude. Reynolds number of the tests presented varied from $15.0 \times 10^6$ to $17.4 \times 10^6$ based on body length.

Sting effects are compared with data of jet effects on the same afterbodies. The results of this comparison indicate that, for the more gradually contoured afterbodies, a sting shape can be found which will duplicate the jet effects, but that for blunt afterbodies no solid sting shape will duplicate the jet effects.

INTRODUCTION

A large part of wind-tunnel testing involves the use of rear sting-supported models. Experimental data for sting-support effects on model characteristics are needed in order to estimate more exactly free-flight conditions. A recent summary of information on sting-support interference (ref. 1) presents a comprehensive study of sting effects at supersonic speeds; however, as noted in reference 1, the acute problem at transonic speeds requires more experimental data. An investigation has been conducted in the Langley 8-foot transonic tunnel to evaluate some of the effects of sting-support configuration on the drag characteristics of a systematic series of afterbodies. The tests were conducted at an angle of attack of 0° through the Mach number range from 0.80 to 1.10 for stings with varying cone-angle, length, and diameter. The sting effects determined are compared with data of jet effects on the same afterbodies.

SYMBOLS

- $A$ cross-sectional area
- $C_1, C_2, C_3$ representative constant values of $D_s/l$
- $C_D$ pressure drag coefficient, $\sum \frac{p_b A_t}{A_{max}}$
- $\Delta C_D$ increment between total afterbody pressure drag coefficient at any given $D_s/l$ and at $D_s/l=0$
- $\Delta C_{D, max}$ increment between total afterbody pressure drag coefficient at $D_s/l=\infty$ and at $D_s/l=0$
- $C_p$ pressure coefficient, $\frac{p_t-p_s}{\frac{1}{2} \rho v^2}$
- $D$ diameter
- $L$ body length
- $l$ sting length between model base and sting cone
- $M$ free-stream Mach number
- $p$ static pressure
- $p_t/p_s$ ratio of jet total pressure to free-stream static pressure
- $q$ dynamic pressure
- $R$ Reynolds number based on body length
- $T_j$ jet total temperature, °F
- $x$ station along longitudinal axis
- $\beta$ afterbody boattail angle, deg
- $\theta$ sting cone half-angle, deg

SUBSCRIPTS:

- $A$ afterbody
- $b$ base
- $s$ sting
- $\infty$ free stream
- $\beta$ boattail
- $l$ local
- $max$ model maximum

APPARATUS AND METHODS

WIND TUNNEL

This investigation was conducted in the Langley 8-foot transonic tunnel, which has a dodecagonal slotted test section. Continuous testing up to a Mach number of 1.10 was possible for these models. Details of the test section are presented in reference 2. Characteristics of the airstream are given in reference 3, wherein the maximum deviation from the indicated free-stream Mach number is shown to be ±0.008.
The models used in the investigation were bodies of revolution that consisted of a single forebody with interchangeable afterbodies. These bodies had fineness ratios of 10 or 10.6, depending on the choice of afterbody. They were supported in the tunnel as shown in figure 1 by two 45° swept struts. These struts had chords of 11.25 inches and NACA 65-010 airfoil sections measured parallel to the airstream. Their leading edges intersected the bodies 21.7 inches from the nose.

Eight afterbody configurations (identified herein as afterbodies A to H) were designed, with the exception of afterbody E, on the basis of the following equation (see fig. 2):

$$r = r_{\text{max}} - (r_{\text{max}} - r_b) \left( \frac{x_b - x_0}{x_1 - x_0} \right) \tan \beta$$  \hspace{1cm} (1)

where:
- \(r\) is the radius at any station.
- \(r_{\text{max}}\) is the maximum radius.
- \(r_b\) is the radius at base.
- \(x_b\) is the distance from afterbody origin to any station.
- \(x_0\) is the distance from afterbody origin to the end of the cylindrical section.
- \(x_1\) is the distance from afterbody origin to the body base.
- \(\beta\) is the boattail angle.

The design values of the afterbody variables are given in table I. Drawings of the afterbody shapes are shown in figure 3. Afterbody E, while not of this afterbody family, is included since it provides a low boattail angle otherwise not available for the bodies having a fineness ratio of 10.0. Tabulated in table II are the ordinates from which the body shapes were constructed. A sketch of the body shapes appears as figure 4.

The models were instrumented with 26 static-pressure orifices in each of three rows located 0°, 45°, and 72° from the plane of symmetry. Orifice distribution was the same in each row. Also, two diametrically opposite base-pressure orifices were located a short distance inside the model base annulus.

The sting was constructed of wood and was attached to the rear of the models by means of an adapter contained within the sting and the afterbody. The models were tested with no sting and with the stings shown in figure 5. These stings included configurations having conical half-angles from 0° to 10° and no cylindrical sections ahead of the cone, stings with conical half-angles of 5° and cylindrical sections ahead of the cone varying from 0 to 13.40 inches, and cylindrical stings having cylindrical sections ahead of the cone.

### TABLE I.—AFT'ERBODY DESIGN

<table>
<thead>
<tr>
<th>Afterbody</th>
<th>(r_{\text{max}}), in.</th>
<th>(x_b), in.</th>
<th>(\beta), deg</th>
<th>(r_b), in.</th>
<th>(x_1), in.</th>
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Figure 2.—Afterbody shape.
AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG

TABLE II.—BODY ORDNATES

(a) Forebody Ordinates

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<thead>
<tr>
<th>Station x, in.</th>
<th>Radius, r, in.</th>
<th>Station x, in.</th>
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(b) Afterbody Ordinates

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<th>Afterbody C</th>
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![Figure 4.—Body shapes.](image)

The pressure coefficients of these tests were numerically integrated to obtain values of afterbody pressure drag efficient which are based on body frontal area. The stings used in this investigation had no effect on the forebody pressure drag as will be shown in the section entitled “Results and Discussion.” Base drags were obtained by assuming that measured base pressures acted over the entire model base.

PRECISION

Total-drag-coefficient errors due to possible inaccuracies in measurement and to tunnel-empty stream nonuniformities are estimated generally to be less than 0.005 at subsonic speeds and not more than 0.010 at supersonic speeds.

The magnitude of the sting effects may be somewhat affected by tunnel-wall disturbances above $M=1.0$. A detailed analysis of shock reflections of this type may be found in reference 3.

RESULTS AND DISCUSSION

DESCRIPTION OF FLOW PHENOMENA

Prior to presentation of these results, a brief discussion of the flow mechanism occurring at the model base is considered to be desirable. Inasmuch as the flow separates from the body at the model base, a region of low-energy air is created immediately behind the base. As a consequence, the streamline adjacent to the wake has essentially a constant pressure. The way in which the pressure at the base arrives at its steady value can be illustrated by considering a cylindrical afterbody. If in some way an external stream is immediately imposed on this afterbody, the base pressure...
Boattailing, if not so great as to cause separation ahead of the base, will cause an increase in base pressure. (See fig. 7 (c).) This increase in base pressure results from an increase in compression over the body as well as from the fact that less wake region is exposed to the aspiration effects of the external stream. Placing a sting in the rear of a model, in addition to causing less wake exposure, requires the external stream to be turned outward more rapidly. (See fig. 7 (d).) These effects result in a base-pressure increase. Increasing the sting cone angle or moving the sting cone closer to the base thus causes a further increase in the turning rate of the external stream near the base and results in a further base-pressure increase.

A sting also has effects on the body pressures ahead of the model base that are similar to the sting effects on base pressure. These effects, which are transmitted through the body boundary layer, become smaller with increasing distance upstream of the base, as is shown in figure 8. In figure 8 are typical pressure distributions over the body with and without a sting. The pressure coefficients for the orifice row along the plane of symmetry are shown for afterbodies B and D at four Mach numbers. The two afterbodies represent a blunt and a gradually contoured rear end configuration, and the sting is the one which had the largest effect. These results indicate that the sting did not affect the body pressures forward of the 60-percent station.

**EFFECT OF STING CONFIGURATION ON BASE PRESSURE**

In figure 9, base pressure coefficients are presented as a function of sting half-angle, length, and cross-sectional-area parameters. As previously stated, the presence of a sting
AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG

Figure 7.—Sketch of flow mechanism at base.

results in changes in base pressure as well as similar changes in body pressures upstream of the base. Consequently, as would be expected, the variations in afterbody drag, which will be discussed in the following sections, are similar to changes in base pressure.

EFFECT OF STING CONFIGURATION ON DRAG

Sting cone-angle effect.—Figure 10 shows the effect of sting half-angle on afterbody pressure drag. Presented at Mach numbers from 0.80 to 1.10 are curves of base, boattail, and total afterbody pressure drag coefficients as a function of sting half-angle for each body tested. The length l of the cylindrical section ahead of the sting cone is zero. These data show that in spite of the large differences in absolute drag values, the curves are similar for all afterbodies in that the drag became lower with increasing sting cone angle. This trend occurred primarily because of the more rapid rate of turning of the external stream with increasing sting cone angle. It should be pointed out that the downstream end of the sting cones was limited to a diameter of 3.75 inches.

Since the curves of figure 10 tended to be linear, slopes of the total afterbody drag curves were taken. These slopes are plotted in figure 11 and can be used to summarize the sting cone angle effect. For the cases where the variation of drag with sting cone angle was not linear, the slopes were taken so as to favor the low-angle portion of the curves. For afterbodies B, C, and D, the curves indicate that the sting cone angle effect near the speed of sound can be double the effect noted at higher and lower speeds. The subsonic and supersonic levels of the angle effect, \(\frac{\partial C_D}{\partial \theta}\), for all bodies were of the order of \(-0.006\) with the exception of afterbody H. Afterbody H was effectively the most blunt afterbody tested.

It can be seen that increasing boattail angle in general caused an increase in sting-angle effect. This result was attributed to the increased turning rate required by the external stream at the model base.

Sting-cone-position effect.—Figure 12 shows the effect of varying sting-cone position along the sting on base, boattail, and afterbody pressure drag coefficients. These data were obtained with cones of 5° half-angle behind varying lengths of constant-diameter cylindrical sting sections. A drag reduction always occurred as the sting cone was moved toward the base (increasing \(D/\ell\)) and caused an increased rate of turning of the external flow. Similar trends, although of different magnitude, were noted in reference 4 for a somewhat different configuration. It should again be pointed out that the downstream end of the sting cones was limited to a diameter of 3.75 inches.

The effect of sting-cone position has been determined only for stings with a 5° cone half-angle. However, it is believed that reasonable approximations of the effect of varying cone position for stings with other cone angles can be obtained by proper interpolation of the results presented herein. A simple method of achieving this can be illustrated by use of a typical plot of drag coefficient against sting angle. (See fig. 13.) The entire range of angles and lengths is bounded by the two linear curves for \(D/\ell=0\) and \(D/\ell=\infty\). The curves for the intermediate values of \(D/\ell\) cannot cross over each other since the variation of drag with sting length is a monotonic function. Therefore, it would appear that the drag for intermediate values of \(D/\ell\) could be reasonably approximated with linear curves. Having the drag values for the intermediate \(D/\ell\) values for \(\theta=5^\circ\) will allow these approximation lines to be determined.

Let \(\Delta C_D\) be defined as the difference between total afterbody drag coefficient at any given \(D/\ell\) and at \(D/\ell=0\), and let \(\Delta C_D,\text{max}\) be the difference between total afterbody drag coefficient at \(D/\ell=\infty\) and \(D/\ell=0\). Then, on the basis of the foregoing discussion \(\Delta C_D/\Delta C_D,\text{max}\) for any \(D/\ell\) may be considered to be approximately a constant for all values of \(\theta\).
Figure 8.—Typical pressure distributions for orifice row along the plane of symmetry. Afterbodies B and D.
AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG

Figure 9.—Variation of base pressure coefficient with sting parameters.

(a) Afterbody A. $\beta=8^\circ; \frac{D_b}{D_{max}}=0.334$.

(b) Afterbody B. $\beta=16^\circ; \frac{D_b}{D_{max}}=0.334$. 
(e) Afterbody C. $\beta = 24^\circ$, $D_b / D_{max} = 0.334$.

(d) Afterbody D. $\beta = 45^\circ$, $D_b / D_{max} = 0.334$.

Figure 9.—Continued.
AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG

Figure 9.—Continued.

(e) Afterbody E. \( \beta = 7.7^\circ; \frac{D_b}{D_{max}} = 0.503. \)

(f) Afterbody F. \( \beta = 16^\circ; \frac{D_b}{D_{max}} = 0.473. \)
(g) Afterbody G. $\beta=24^\circ$; $\frac{D_b}{D_{\text{max}}}=0.473$.

(h) Afterbody H. $\beta=45^\circ$; $\frac{D_b}{D_{\text{max}}}=0.473$.

Figure 9.—Concluded.
Figure 10.—Variation of base, boattail, and total afterbody pressure-drag coefficient with sting half-angle with $\frac{D}{t} = \infty$.

(a) Afterbody A. $\beta = 8^\circ; \frac{A_s}{A_b} = 0.559; \frac{D_{tb}}{D_{max}} = 0.334.$

(b) Afterbody B. $\beta = 10^\circ; \frac{A_s}{A_b} = 0.559; \frac{D_{tb}}{D_{max}} = 0.334.$
(c) Afterbody C. \( \beta = 24^\circ; \frac{A_1}{A_b} = 0.559; \frac{D_{b1}}{D_{max}} = 0.334 \).

(d) Afterbody D. \( \beta = 24^\circ; \frac{A_1}{A_b} = 0.559; \frac{D_{b2}}{D_{max}} = 0.334 \).

Figure 10.—Continued.
AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG

(e) Afterbody E. $\beta=7.7^\circ; \frac{A_s}{A_b}=0.247; \frac{D_b}{D_{ms=0}}=0.503$.

(f) Afterbody F. $\beta=10^\circ; \frac{A_s}{A_b}=0.280; \frac{D_b}{D_{ms=0}}=0.473$.

Figure 10.—Continued.
Figure 10.—Concluded.
AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG

Figure 11.—Variation of sting-half-angle effect with Mach number.

\[ \frac{D_\beta}{l} = 0. \]
Figure 12.— Variation of base, boattail, and total afterbody pressure-drag coefficient with ratio of base diameter to sting length with \( \theta = 5^\circ \).
AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG

**FIGURE 12.**—Continued.

(c) Afterbody C. $\beta = 24^\circ; \frac{A_t}{A_b} = 0.559; \frac{D_b}{D_{max}} = 0.334.$

(d) Afterbody D. $\beta = 45^\circ; \frac{A_t}{A_b} = 0.559; \frac{D_b}{D_{max}} = 0.334.$
(e) Afterbody E. \( \beta = 7.7^\circ; A_L \frac{A_A}{A_L} = 0.247; \frac{D_s}{D_{max}} = 0.503. \)

(f) Afterbody F. \( \beta = 16^\circ; A_L \frac{A_A}{A_L} = 0.280; \frac{D_s}{D_{max}} = 0.473. \)

**Figure 12.—Continued.**
(g) Afterbody G. $\beta=24^\circ$; $\frac{A_1}{A_b}=0.280$; $\frac{D_b}{D_{max}}=0.473$.

(h) Afterbody H. $\beta=45^\circ$; $\frac{A_1}{A_b}=0.280$; $\frac{D_b}{D_{max}}=0.473$.

FIGURE 12.—Concluded.
The parameter \( \Delta C_D / \Delta C_{D, \text{max}} \) represents the ratio of sting-cone effect on drag for a given sting length \( (D_s/l) \) to the maximum sting-cone effect on drag. The maximum effect is obtained when the sting length is zero \( (D_s/l = \infty) \). Values of \( \Delta C_D / \Delta C_{D, \text{max}} \) obtained from the data of figure 12 are presented in figure 14(a). Their variation with \( D_s/l \) is shown for each afterbody configuration through the Mach number range. Values of \( \Delta C_D / \Delta C_{D, \text{max}} \) for configurations having larger values of \( D_s/l \) than those shown in figure 14(a) may be obtained in figure 14(b). These values are plotted against the reciprocal of \( D_s/l \) for each afterbody configuration through the Mach number range. Figure 15 presents the slopes of the linear portion of the curves shown in figure 14(a). The magnitude of these slopes is about 1.0 for all configurations tested.

### Sting-size effect

The effect on the base, boattail, and afterbody pressure drag coefficients of varying the cross-sectional area of a cylindrical sting is presented in figure 16 for each afterbody. No sting cone was present on the sting for these data and the effect of limiting the sting length to 26 inches is believed to be negligible. In general, the effect of increasing the sting size was to decrease the drag. Average slopes of total afterbody pressure drag with the sting size parameter are plotted against Mach number in figure 17. The slopes are seen to vary from approximately zero to \(-0.05\).

### STING-INTERFERENCE CORRECTIONS

Inasmuch as a large number of afterbodies and stings were tested in combination, a general equation has been derived from the results to provide corrections to wind-tunnel drag measurements for sting-interference effects. Although the scope of the present investigation was rather large, it was necessarily limited. Therefore, any corrections obtained empirically from these results should be restricted to stings and afterbodies similar in scale and shape to those investigated. It is also recommended that the results be used only for models having Reynolds number and boundary-layer conditions that comply with those of the present tests. (See ref. 1.) The boundary layer was turbulent ahead of the model base for the present tests.

Provided the previously mentioned limitations apply, it is suggested that the derived general equation be used for obtaining sting interference corrections in the following manner. An afterbody shape should be selected from this report similar to the one for which corrections are desired. The correction due to the presence of the sting cone is

\[
\Delta C_D = \left( \frac{\Delta C_D}{\Delta C_{D, \text{max}}} \right) \Delta C_{D, \text{max}}
\]

where \( \Delta C_D / \Delta C_{D, \text{max}} \) can be read from figure 14 for the proper values of \( D_s/l \) and \( M \); or for \( D_s/l \) less than 0.5, \( \Delta C_D / \Delta C_{D, \text{max}} \) can be approximated by using figure 15.

Inasmuch as the variation of \( C_D \) with sting angle is linear,

\[
\Delta C_{D, \text{max}} = \frac{\partial C_D}{\partial \theta}
\]

where \( \partial C_D / \partial \theta \) can be read from figure 11 for the correct value of \( M \).

Substitution from equation (3) into equation (2) gives the drag correction

\[
\Delta C_D = \theta \left( \frac{\Delta C_D}{\Delta C_{D, \text{max}}} \right) \left( \frac{\partial C_D}{\partial \theta} \right)
\]

This relation will correct data for a sting with a conical section to data for a sting with only a cylindrical section.

In order to correct for the cylindrical-section diameter

\[
\Delta C_D = \left( \frac{A_s}{A_b} \right) \left[ \frac{\partial C_D}{\partial \left( A_s/A_b \right)} \right]
\]

where \( \partial C_D / \partial (A_s/A_b) \) can be read from figure 17. The complete sting correction then becomes

\[
\Delta C_D = \theta \left( \frac{\Delta C_D}{\Delta C_{D, \text{max}}} \right) \left( \frac{\partial C_D}{\partial \theta} \right) + \left( \frac{A_s}{A_b} \right) \left[ \frac{\partial C_D}{\partial \left( A_s/A_b \right)} \right]
\]
AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG

(a) Variation of $\Delta C_D / \Delta C_{D_{\text{max}}}$ with ratio of base diameter to sting length.

(b) Variation of $\Delta C_D / \Delta C_{D_{\text{max}}}$ with ratio of sting length to base diameter.

Figure 14.—Sting-length effect with $\theta = 5^\circ$. 
Figure 15.—Variation of sting-length effect with Mach number. $\theta=5^\circ$. 

The diagram shows the variation of sting-length effect with Mach number for different angles of attack ($\beta$, deg) ranging from 8 to 45 degrees. The data is plotted on a graph with Mach number on the x-axis and the effect on the y-axis. The afterbody effect is also plotted to show the impact on the overall aerodynamic performance.
AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG

Figure 16.—Variation of base, boattail, and total afterbody pressure-drag coefficient with ratio of sting to base area with $\frac{D_b}{l}$ = 0.

(a) Afterbody A. $\beta = 8^\circ; \frac{D_b}{D_{maa}} = 0.334$.

(b) Afterbody B. $\beta = 10^\circ; \frac{D_b}{D_{maa}} = 0.334$. 

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This figure illustrates the variation of base, boattail, and total afterbody pressure-drag coefficient with the ratio of sting to base area for two different afterbody designs. The data points are represented for different Mach numbers ($M$) and include the effects of sting-to-base area ratios ($\frac{D_b}{l}$) on drag coefficients ($C_{D, A}$, $C_{D, B}$, $C_{D, T}$). The figure highlights the significant impact of these ratios on the overall drag profile, which is crucial for understanding aerodynamic performance in sting-supported configurations.
(c) Afterbody C. $\beta=24^\circ$; $\frac{D_h}{D_{max}}=0.334$.

(d) Afterbody D. $\beta=45^\circ$; $\frac{D_h}{D_{max}}=0.334$.

Figure 16.—Continued.
(e) Afterbody E. $\beta=7.7^\circ$; $\frac{D_b}{D_{max}}=0.503$.

(f) Afterbody F. $\beta=16^\circ$; $\frac{D_b}{D_{max}}=0.473$.

Figure 16.—Continued.
(g) Afterbody G. \( \beta = 24^\circ; \frac{D_b}{D_{max}} = 0.473 \).

(h) Afterbody H. \( \beta = 45^\circ; \frac{D_b}{D_{max}} = 0.473 \).

Figure 16.—Concluded.
AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG

353

The correction thus obtained must be subtracted from the total-drag coefficient based on model frontal area. It should be noted that the value of $\Delta C_D$ will in all cases be negative and will result in a drag increase when data are corrected to the sting-off condition. It is estimated that the above method of obtaining sting corrections will give drag-coefficient increments generally within 0.03 of the values obtained by using the actual data points.

Corrections determined from the present results have been calculated for a model discussed in reference 5. In figure 18, the resulting corrections are compared with the corrections determined by the method described in reference 5. The model of reference 5 had $\beta=5.6^\circ$, $D_s/D_{max}=0.416$, $\theta=4.2^\circ$, $D_s/l=\infty$, and $A_s/A_2=0.85$. Afterbody E was chosen as most closely approximating the model. The model was tested in a closed-throat tunnel. The sting corrections in reference 5 were determined by using decreasing sting sizes and extrapolating the zero sting size. Figure 18 indicates good agreement between the present results and reference 5 for all configurations below a Mach number of 0.9. Above this speed, indications are that sting corrections are more sensitive to changes in tail configurations.

A direct comparison with the sting effects of references 4 and 6 could not be made since none of the afterbodies of this report approximately the configurations of references 4 and 6. However, it is worthy of note that the sting effects in references 4 and 6 are considerably larger than any of this test. This difference is a result of the configurations of references 4 and 6 having larger values of $D_s/D_{max}$ (0.737 and 1.00, respectively).

SIMULATION OF JET EFFECTS WITH A STING

Jet effects studies were made on each afterbody including tests on a sting which had the shape of a free sonic jet expanding from the rear of the bodies. The sting shape was determined by measurements of a schlieren photograph of a jet at a total-pressure ratio of 5 and a temperature of 1,200° F. This sting having the same size and shape as the free jet always produced higher afterbody pressures than the jet. This result was as might be expected, since the sting could produce the solid-body effect but not the aspirating effect of the jet.

There is, however, a possibility of simulating jet effects with a sting of a different shape than that of the free jet. In figure 19 is shown the variation of afterbody pressure drag coefficient with the sting parameters of this investigation and with jet total-pressure ratio for a sonic free jet exhausting at 1,200° F.

Figure 19 indicates that for the gradually contoured afterbodies a practical sting shape can be made which will produce the same drag as the jet at a given pressure ratio. As the afterbody shape becomes more blunt, the aspiration effect of the jet becomes increasingly predominant on the larger wake behind the blunt rear end, and it becomes increasingly more difficult to simulate the jet effect with solid sting shapes. This simulation is impossible for afterbody G. Afterbodies F and E would probably show agreement between sting and jet data at pressure ratios above those presented since for the higher jet-pressure ratios, the free jet size would increase and cause higher pressures rearward of the base.
Figure 19.—Comparison of sting and jet effects.
(a) Afterbody C. \( \beta = 24^\circ; \frac{D_b}{D_{max}} = 0.334; \frac{D_l}{D_b} = 0.742. \)

(d) Afterbody D. \( \beta = 45^\circ; \frac{D_b}{D_{max}} = 0.334; \frac{D_l}{D_b} = 0.742. \)

Figure 19.—Continued.
(e) Afterbody E. \( \beta = 7.7^\circ; \frac{D_b}{D_{max}} = 0.503; \frac{D_l}{D_b} = 0.898. \)

(f) Afterbody F. \( \beta = 16^\circ; \frac{D_b}{D_{max}} = 0.473; \frac{D_l}{D_b} = 0.742. \)

Figure 19.—Continued.
AN EXPERIMENTAL INVESTIGATION OF STING-SUPPORT EFFECTS ON DRAG

Figure 19.—Concluded.

(g) Afterbody G. \( \beta = 24°; \frac{D_l}{D_{ess}} = 0.473; \frac{D_l}{D_b} = 0.742. \)

(h) Afterbody H. \( \beta = 45°; \frac{D_l}{D_{ess}} = 0.473; \frac{D_l}{D_b} = 0.742. \)
From an investigation to determine the effects of sting-support on several body shapes, the following conclusions have been drawn:

1. The presence of a sting in general causes a drag reduction.
2. Increasing sting cone angle, decreasing sting cylindrical length ahead of the sting cone, and in general increasing sting diameter causes a drag reduction.
3. Sting-cone-angle effect increases with increasing boattail angle.
4. Approximate sting interference corrections can be made on models with afterbodies and sting supports similar in scale and geometry to those reported, provided the Reynolds number is of the same order of magnitude and the boundary layer ahead of the model base is turbulent.
5. For gradually contoured afterbodies, a sting can be made which will duplicate jet effects, but for blunt afterbodies no solid sting shape will produce the same effect as the jet.

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REFERENCES