NATIONAL ADVISORY COMMITTEE
FOR AERONAUTICS

REPORT No. 455

PENETRATION AND DURATION OF FUEL SPRAYS
FROM A PUMP INJECTION SYSTEM

By A. M. ROTHROCK and E. T. MARSH

1933
1. FUNDAMENTAL AND DERIVED UNITS

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<td>Speed</td>
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2. GENERAL SYMBOLS, ETC.

- $W$, Weight = $mg$
- $g$, Standard acceleration of gravity = $9.80665 \text{ m/s}^2 = 32.1740 \text{ ft./sec.}^2$
- $m$, Mass = $\frac{W}{g}$
- $\rho$, Density (mass per unit volume)
- Standard density of dry air, $0.12497 \text{ (kg-m}^{-4} \text{s}^2)$ at $15^\circ \text{ C. and 760 mm} = 0.002378 \text{ (lb.-ft.}^{-4} \text{ sec.}^2)$
- Specific weight of “standard” air, $1.2255 \text{ kg/m}^3 = 0.07651 \text{ lb./ft.}^3$

3. AERODYNAMICAL SYMBOLS

- $V$, True air speed
- $q$, Dynamic (or impact) pressure = $\frac{1}{2} \rho V^2$
- $L$, Lift, absolute coefficient $C_L = \frac{L}{qS}$
- $D$, Drag, absolute coefficient $C_D = \frac{D}{qS}$
- $D_p$, Profile drag, absolute coefficient $C_{D_p} = \frac{D_p}{qS}$
- $D_i$, Induced drag, absolute coefficient $C_{D_i} = \frac{D_i}{qS}$
- $D_p$, Parasite drag, absolute coefficient $C_{D_p} = \frac{D_p}{qS}$
- $C$, Cross-wind force, absolute coefficient $C_C = \frac{C}{qS}$
- $Q$, Resultant moment
- $\Omega$, Resultant angular velocity
- $V_l$, Reynolds Number, where $l$ is a linear dimension
- $\mu$, Coefficient of viscosity
- $\alpha$, Angle of attack
- $\epsilon$, Angle of downwash
- $\alpha_s$, Angle of attack, infinite aspect ratio
- $\alpha_i$, Angle of attack, induced
- $\alpha_a$, Angle of attack, absolute
- $\gamma$, Flight path angle
REPORT No. 455

PENETRATION AND DURATION OF FUEL SPRAYS
FROM A PUMP INJECTION SYSTEM

By A. M. ROTHROCK and E. T. MARSH
Langley Memorial Aeronautical Laboratory
NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

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PENETRATION AND DURATION OF FUEL SPRAYS FROM A PUMP INJECTION SYSTEM

By A. M. Rothrock and E. T. Marsh

SUMMARY

High-speed motion pictures were taken of individual fuel sprays from a pump injection system. The changes in the spray-tip penetration with changes in the pump speed, injection-valve opening and closing pressures, discharge-orifice area, injection-tube length and diameter, and pump throttle setting were measured. The pump was used with and without a check valve. The results show that the penetration of the spray tip can be controlled by the dimensions of the injection tube, the area of the discharge orifice, and the injection-valve opening and closing pressures.

INTRODUCTION

In order to determine the suitability of a given type of injection system for high-speed compression-ignition engines, it is necessary to know the operating characteristics of the system. One of the most important characteristics to be investigated is the formation and the development of the fuel spray. During the last five years the National Advisory Committee for Aeronautics has published considerable information on the effects of the various factors which control the formation and the development of the fuel spray. Investigations have been conducted with a mechanically operated injection valve and with automatic injection valves. In these investigations it was necessary to operate the injection system from a constant source of pressure because the purpose of the tests was to investigate the effects of such variables as the injection pressure, the spray-chamber density, and the discharge-orifice design.

With pump injection systems, however, the injection pressure varies with pump speed and in some cases with the fuel quantity delivered. Tests already conducted (reference 1) have shown that the injection pressures affect the penetration of the fuel spray during the first few thousandths of a second. As this is the time available for injection in a high-speed compression-ignition engine, it is important to know how the pressure variations in a pump injection system will affect the fuel-spray penetration and dispersion. It is also advantageous to know the effects of such variables as the injection-tube length, the injection-tube diameter, the discharge-orifice diameter, and the injection-valve opening and closing pressures on the penetration and dispersion of the fuel spray.

This report presents the results obtained from an investigation made at the Langley Memorial Aeronautical Laboratory, Langley Field, Va., to determine the effect of pump speed, the dimensions of the injection tube, the pump throttle setting, the discharge-orifice diameter, and the adjustment of the injection valve on the penetration and dispersion of the fuel spray. As far as was practicable the test conditions were the same as those used by Rothrock in his investigation of the hydraulics of fuel-pump injection systems. (See reference 2.) The injection valve and the fuel pump were the same as those described in reference 2. The pump was tested with and without a check valve.

APPARATUS AND METHODS

A diagrammatic arrangement of the apparatus used in this investigation is shown in Figure 1. This apparatus is a modification of the N. A. C. A. spray photographic equipment (reference 3) used in taking high-speed motion pictures of a single spray discharge from a common-rail system. Two modifications have been made: a change from the common-rail system to the pump system of injection, and a change in the

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spray chamber so that continuous injections from a fuel pump into the compressed air would not fog the chamber and prevent photographs from being taken of a single spray.

In the modified spray chamber (fig. 2) a funnel was arranged in front of the nozzle to deflect the sprays into a reservoir. Releasing the funnel catch allowed the funnel to drop below the nozzle and permitted the spray to enter the spray chamber. With the proper timing the funnel uncovered the valve nozzle between pump discharges so that there was no interference between the spray and the funnel.

The pump tested was a 6-cylinder commercial fuel pump. A cross section through one of the cylinders of the pump (fig. 3) shows its construction. The outlets from five of the pump plungers were by-passed to the oil reservoir and the sixth was connected to the injection valve with a seamless steel tube having an outside diameter approximately twice the inside diameter.

The injection pump was rotated by a variable-speed electric motor and was connected to the camshaft through a jaw clutch. The camshaft remained stationary until engaged by this clutch. It then made one revolution with the pump shaft. During this revolution of the camshaft, the funnel catch was released; the rotary switch completed the electric circuit between the condensers and the spark gap. The rotary switch and the pump were timed with the serrated coupling so that the spray was synchronized with the discharges of the condensers. The injection-valve closing pressure instead of opening pressure was measured because of the greater accuracy of this measurement. (See reference 2.) The injection-valve opening pressure was approximately 1.4 times the closing pressure.

The fuel oil used had a specific gravity of 0.83 and an absolute viscosity of 0.022 poise at 100°F.

Unless otherwise stated, all tests were made with a 0.020-inch diameter orifice and a 34-inch injection tube. The discharge orifice length/diameter ratio was 6:1 in all tests.

The procedure for taking a spray photograph was the same for all tests. The pump was brought up to the desired speed and the throttle opened for a few revolutions to expel all air from the injection tube. Air was then blown through the spray chamber to clear the glass walls and to remove suspended oil particles. The air pressure, unless otherwise stated, was raised to 200 pounds per square inch, a density of 1.1 pounds per cubic foot, which is equivalent to the density in the combustion chamber of an engine operating at a compression ratio of 14, and the funnel was raised and latched in position. When the desired film-drum speed was reached, the pump throttle was again opened, and after several revolutions of the pump the clutch was engaged. A progressive series of photographs was thus recorded of the spray development. From these records the spray-tip penetration curves were obtained.
Stem-lift records of the injection-valve stem were also taken in a few cases to determine the movement of the valve stem under the pressure conditions in the injection valve. The method was the same as described in reference 2.

**TEST RESULTS AND DISCUSSION**

**SPRAY-TIP PENETRATION**

The results of the tests are shown by graphs on which the penetration of the fuel spray-tip in the spray chamber is plotted against time. Tangents to these curves indicate the rate of penetration of the spray tip. A separate curve is plotted for each variable and the effect of the variable on spray-tip penetration is noted. Each curve is plotted from two or three tests under the same conditions. Additional checks were made when large variations appeared. Zero time on the graphs refers to the start of the spray from the orifice.

**Effect of pump speed.**—In reference 2 it was shown that varying the pump speed added to the initial pressure (approximately the valve-closing pressure) in the injection tube instantaneous values of pressure proportional to the velocity of the pump plunger. As the initial pressure was increased the ratio of the pressures created by the motion of the pump plunger to the total pressure at any instant decreased. It has also been shown in references 1 and 4 that both the maximum injection pressures and the injection-valve opening pressure affect the spray-tip velocity. However, as the rate-of-pressure rise, after the injection valve opens, decreases or as the ratio of the maximum pressure to the injection-valve opening pressure decreases it can be expected that the effect of the injection-valve opening pressure on the spray-tip penetration will increase and the effect of the maximum pressure will decrease. We can therefore expect that, in general, as the injection-valve opening pressure is increased the effect of pump speed on spray-tip penetration will decrease.

In reference 2 it has also been shown that as the pump speed is decreased a speed is reached below which the pressure waves originating at the fuel pump are not sufficient to hold the injection-valve stem from the seat. This value of speed depends on the injection-pump plunger diameter, the pump-cam contour, the injection-tube diameter, the initial pressure in the injection tube, the injection-valve opening and closing pressures, and the pressure into which the discharge takes place. It is, within practical limits, independent of the injection-tube length. For speeds below this valve the injection-valve stem will tend to oscillate, thereby opening and closing the injection valve. The phenomenon is sometimes accompanied by a chattering of the injection-valve stem against its seat during the injection period. When this phenomenon occurs the fuel discharge instead of consisting of a single spray will consist of two or more individual sprays following each other, generally in quick succession. Under certain circumstances the stem may not lift sufficiently to expose a flow area greater than the discharge-orifice area. In this case the stem and seat together act as a variable-area orifice. Owing to restriction to flow the spray will not have the penetrating ability possible were the stem fully lifted.

The effect of pump speed on the spray-tip penetration at an injection-valve closing pressure of 2,000 pounds per square inch is shown in Figure 4. In no case was there evidence of primary sprays before the main spray at pump speeds above 760 r. p. m. The variation in maximum pressures and in the rate-of-pressure rise was sufficient to cause the spray-tip penetration to increase with pump speed.

Figure 5 shows the effect of low pump speeds on the spray-tip penetration at an injection-valve closing pressure of 2,500 pounds per square inch. The figure
shows that at the two lower speeds primary sprays appeared before the main spray. These primary sprays were caused by the seating of the injection-valve stem after the initial opening. After the second lifting of the stem the pressure was sufficient to keep the injection-valve stem off its seat. If the main sprays at the two lower speeds are compared with those at the higher speeds (fig. 5(b)) it is seen that the penetration of the main spray is not appreciably affected by the pump speed. It may be concluded that in this case the injection-valve closing pressure was sufficiently high so that the effect of the rate-of-pressure rise and maximum pressures had no appreciable effect on the spray-tip penetration of the main sprays.

At low pump speeds and with an injection-valve closing pressure of 500 pounds per square inch, the rate-of-pressure rise and the maximum pressures materially influenced the penetration. (Fig. 6.) At the two lower speeds primary sprays occurred.

Figure 7 shows a spray photograph and stem-lift record taken at a pump speed of 190 r. p. m. with atmospheric pressure in the spray chamber. The small lines at the top of the stem-lift record were caused by a spark gap placed in series with the main gap for taking the photographs. Consequently, each line corresponds to a spray photograph. Because the stem record extended for more than a single revolution of the film drum, the spray photographs and the stem record are not synchronized. The injection-valve stem oscillated, thus opening and closing the injection valve and causing a series of sprays. The bouncing of the stem was eliminated when the chamber pressure was increased to 200 pounds per square inch, because of the additional force on the stem. However, when the pump speed was decreased to 108 r. p. m. (fig. 8) the bouncing of the stem during the whole injection period again occurred though the chamber pressure was 200 pounds per square inch. Comparison of Figures 7 and 8 shows that in the former the stem lift and consequently the pressures were higher than in the latter.

Effect of injection-valve closing pressure.—Figure 9 shows the effect of the injection-valve closing pressure on the penetration of the tip of the main spray for a pump speed of 470 r. p. m. The records showed that there were primary sprays with injection-valve closing pressures of 1,500 pounds per square inch or greater. The figure shows that the penetration of the main spray increases as the injection-valve closing pressure was increased until a value of 1,500 pounds per square inch is reached. For this pressure the spray-tip penetration decreased. As the injection-valve closing pressure was further increased the penetration again increased. The decrease in the penetration at the injection-valve closing pressure of 1,500 pounds per square inch was probably caused by the injection-valve stem throttling the flow of fuel past the valve seat. Above this injection-valve closing pressure, although throttling still occurred as has been shown in reference 2, the pressure at the start of injection was sufficient to give the spray the increased penetration.

The penetration of both the primary and main sprays for the injection-valve closing pressures of 1,500 and 2,000 pounds per square inch is shown in Figure 10. It is seen that the primary spray as well as the main spray penetrated at a faster rate as the injection-valve closing pressure was increased.

Figure 11 shows the effect of the injection-valve closing pressure on the spray-tip penetration for a pump speed of 760 r. p. m. No primary sprays were observed at this speed. However, as was the case with 470 r. p. m. a minimum penetration occurred at a particular injection-valve closing pressure, 2,000 pounds per square inch.

At low injection-valve closing pressures and a pump speed of 760 r. p. m., it was shown in reference 2 that the pressure-wave phenomenon caused secondary discharge after cut-off occurred at the fuel pump. Secondary discharges did not occur with the higher injection-valve closing pressures. The photographs showed these secondary discharges with the low valve closing pressures, but because of the fogging of the chamber the photographs were not clear enough to reproduce on a half-tone photo-engraving.

Effect of injection-tube diameter.—As shown in reference 2, it is advisable to use an injection-tube diameter equal to or slightly greater than the critical tube diameter so that the flow through the injection tube will be laminar with a resultant small pressure loss caused by friction. Figure 12 (a) shows that the penetration at a pump speed of 760 r. p. m. was nearly the same for all injection-tube diameters even when diameters considerably less than the critical diameter (0.098 inch) were employed. For the conditions shown in Figure 12 (a) it may be concluded that the
Figure 7.—Spray photograph and stem-lift record at low pump speed. Pump speed, 190 r. p. m. Injection-valve closing pressure, 500 lb./sq. in. Injection tube inside diameter, 0.125 in. Tube length, 34 in. Spray chamber density, 0.0765 lb./cu. ft.

Figure 8.—Spray photograph and stem-lift record at low pump speed. Pump speed, 108 r. p. m. Injection-valve closing pressure, 500 lb./sq. in. Injection tube inside diameter, 0.125 in. Tube length, 34 in. Spray chamber density, 1.11 lb./cu. ft.
injection-valve opening and closing pressure controlled the spray-tip penetration.

For the pump speed of 470 r. p. m. (fig. 12 (b)) the smaller tube gave the lower spray-tip penetration. As the test conditions caused primary starts at the beginning of the spray (fig. 10) the drop in rate of penetration was probably due to their formation.

In order to illustrate the influence of these primary sprays in this instance, a comparison of Figure 10 with Figure 12 (b) shows that the primary spray penetration for the 0.076-inch tube falls below the curve for the primaries of the 0.041 and 0.059 inch diameter tubes, indicating lower penetration for the 0.076-inch tube.

However, the main spray for the 0.076-inch tube shows greater penetration. The spray photographs for the 0.041 and 0.059 inch diameter tubes show primaries but the main sprays are not clear enough to be measured directly. Measurement of the clearest main spray (0.059-inch tube) shows the main spray penetration to be the same as that for the 0.076-inch tube.

The increase in penetration for the 0.125-inch tube (470 r. p. m.) is due to laminar flow which exists in the tube. As shown in reference 2, turbulent flow in a tube results in friction and pressure losses which give a low initial stem lift and a slow rise in pressure at the injection valve. Both conditions aid the formation of primary sprays. With laminar flow these conditions are lacking and a faster rate-of-pressure rise results which increases the penetration.

**Effect of injection-tube length.**—Figure 13 shows the effect of the injection-tube length on the spray-tip penetration. The results show that there was little variation in the spray-tip penetration for tube lengths between 34 and 70 inches. Because of the limitations of the apparatus it was not possible to test injection-tube lengths of less than 34 inches. However, it was shown in reference 2 that the instantaneous pressures showed little variation with injection-tube lengths of from 4 to 34 inches. Consequently, it may be assumed that the injection-tube length does not have an appreciable effect on the penetration of the fuel spray.

**Effect of pump-throttle setting.**—Increase in the pump-throttle setting (fig. 14) gave decreased penetration. The injection periods for low throttle settings...
were short, but the spray reached the maximum penetration that could be measured before cut-off occurred. The effect of the initial pressure rise with early cut-off should have a determining effect on the action of the spray. From stem-lift records (reference 2, fig. 17) the pressure rise as the valve stem is first lifting is more rapid at the lower throttle setting. The higher initial velocity of the spray gives, therefore, an increased rate of penetration for the lower throttle settings.

Effect of check valve in pump.—With no check valve in the pump there was a slight increase in the rate of penetration over that obtained by using a check valve, as is shown by Figure 15. The results without the check valve were erratic. In reference 2, Figure 19, the stem-lift curve obtained without a check valve in the pump shows a faster rate of stem lift than with a check valve, indicating a greater pressure rise and greater initial spray-tip velocity than that obtained with a check valve in the pump, but the injection period was materially decreased. How-

ever, later results have shown that removing the check valve also decreases the total fuel quantity discharged.

With no check valve between the pump and the injection tube, the tube often became air locked causing a pulsating flow in the injection tube, but no injection. The air lock was probably caused by air leakage from the spray chamber past the injection-valve seat. This air lock persisted even after the injection-valve closing pressure had been raised to 4,500 pounds per square inch. The other five plungers would discharge regularly into the oil reservoir. With the check valve in the pump, any air in the tube was forced out during the first few revolutions.

Effect of open nozzle.—The open nozzle used in these tests was fitted with a ball-check valve close to the nozzle to prevent leakage of air into the injection line, as recommended in reference 5. With the check valve in the pump a marked increase in the rate of penetration was noted at 760 r. p. m. (fig. 16) over that obtained without the check valve. The increase at 470 r. p. m. was not so noticeable. The increase in rate of penetration was due to the fact that the closing of the check valve trapped an initial pressure in the

![Figure 13](image1.png)

**Figure 13.**—Effect of injection-tube length on spray-tip penetration. Injection-valve closing pressure, 2,500 lb./sq. in. Injection-tube inside diameter, 0.125 in. Orifice diameter, 0.020 in.

![Figure 14](image2.png)

**Figure 14.**—Effect of pump throttle setting on spray-tip penetration. Pump speed, 760 r. p. m. Injection-valve closing pressure, 2,900 lb./sq. in. Injection-tube inside diameter, 0.076 in. Tube length, 34 in. Orifice diameter, 0.020 in.

![Figure 15](image3.png)

**Figure 15.**—Effect of check valve on spray-tip penetration. Injection-valve closing pressure, 3,500 lb./sq. in. Injection-tube inside diameter, 0.125 in. Tube length, 34 in. Orifice diameter, 0.020 in.

![Figure 16](image4.png)

**Figure 16.**—Effect of check valve and open nozzle on spray-tip penetration. Open nozzle. Injection-tube inside diameter, 0.125 in. Tube length, 34 in. Orifice diameter, 0.020 in.
injection tube equal to the spray-chamber pressure. This initial pressure aided in building up higher pressures in the injection tube. Furthermore, the check valve lessened the probability of the formation of an air pocket in the injection tube.

The penetration obtained with the open nozzle with and without the check valve at the pump was less than that obtained with the closed nozzle under the same conditions.

**Effect of orifice diameter.**—Figure 17 shows the results obtained with an 0.030-inch diameter orifice at pump speeds of 470 and 760 r. p. m. These curves show a lower rate of penetration than the corresponding series for the 0.020-inch orifice (fig. 15(b)) and the 0.030-inch orifice. These higher pressures resulted in a higher rate of penetration for the smaller orifice.

**CONCLUSIONS**

1. The test results presented show that fuel-injection pumps designed for high-speed compression-ignition engines have satisfactory operating characteristics over the speed range which is encountered under load in ordinary practice. At low speeds, such as are used for starting and idling, the fuel injection takes place as a series of sprays, because the fuel pressures originating at the pump are not sufficient to maintain high injection pressures at the discharge orifice of the injection valve. The results also show that the fuel-spray characteristics are affected by the injection-tube diameter, the discharge-orifice area, the pump throttle setting, and check valves placed in the system.

2. Increasing the injection-valve opening and closing pressure increases the spray-tip penetration, decreases the duration of the injection, and increases the tendency for primary sprays to appear before the start of injection.

3. Increasing the pump speed increases the spray-tip penetration with low injection-valve opening and closing pressures, but has little effect on the penetration for high injection-valve opening and closing pressures; decreases the injection lag; increases the duration of the injection in pump degrees; and decreases the tendency for primary discharge to occur.

**REFERENCES**

Positive directions of axes and angles (forces and moments) are shown by arrows.

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Absolute coefficients of moment:

\[ C_L = \frac{L}{q_b S} \]
\[ C_M = \frac{M}{q_b S} \]
\[ C_N = \frac{N}{q_b S} \]

Angle of set of control surface (relative to neutral position), \( \delta \). (Indicate surface by proper subscript.)

4. PROPELLER SYMBOLS

- \( D \), Diameter.
- \( p \), Geometric pitch.
- \( p/D \), Pitch ratio.
- \( V' \), Inflow velocity.
- \( V_s \), Slipstream velocity.
- \( T \), Thrust, absolute coefficient \( C_T = \frac{T}{\rho n^2 D^4} \).
- \( Q \), Torque, absolute coefficient \( C_Q = \frac{Q}{\rho n^2 D^4} \).
- \( P \), Power, absolute coefficient \( C_P = \frac{P}{\rho n^2 D^5} \).
- \( C_s \), Speed power coefficient = \( \sqrt{\frac{s \rho V^3}{P n^3}} \).
- \( \eta \), Efficiency.
- \( n \), Revolutions per second, r. p. s.
- \( \Phi \), Effective helix angle = \( \tan^{-1} \left( \frac{V}{g \pi n} \right) \).

5. NUMERICAL RELATIONS

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