NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

REPORT No. 701

MECHANICAL PROPERTIES OF FLUSH-RIVETED JOINTS

By W. C. BRUEGGEMAN and FREDERICK C. ROOP

1940
### AERONAUTIC SYMBOLS

#### 1. FUNDAMENTAL AND DERIVED UNITS

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Metric Unit</th>
<th>English Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>( l )</td>
<td>meter</td>
<td>foot (or mile)</td>
</tr>
<tr>
<td>( t )</td>
<td>second</td>
<td>second (or hour)</td>
</tr>
<tr>
<td>( F )</td>
<td>weight of 1 kilogram</td>
<td>weight of 1 pound</td>
</tr>
<tr>
<td>( P )</td>
<td>horsepower (metric)</td>
<td>horsepower</td>
</tr>
</tbody>
</table>

#### 2. GENERAL SYMBOLS

\[ W, \quad W = mg \]
\[ g, \quad \text{Standard acceleration of gravity} = 9.80665 \text{ m/s}^2 \text{ or } 32.1740 \text{ ft./sec.}^2 \]
\[ m, \quad \text{Mass} = \frac{g}{g} \]
\[ I, \quad \text{Moment of inertia} = mk^2 \] (Indicate axis of radius of gyration \( k \) by proper subscript.)
\[ \mu, \quad \text{Coefficient of viscosity} \]

#### 3. AERODYNAMIC SYMBOLS

\( S, \quad \text{Area} \)
\( S_w \), Area of wing
\( G, \quad \text{Gap} \)
\( b, \quad \text{Span} \)
\( c, \quad \text{Chord} \)
\( b^2 \), Aspect ratio
\( V, \quad \text{True air speed} \)
\( q, \quad \text{Dynamic pressure} = \frac{1}{2} \rho V^2 \)
\( L, \quad \text{Lift, absolute coefficient} = \frac{L}{qS} \)
\( D, \quad \text{Drag, absolute coefficient} = \frac{D}{qS} \)
\( D_b, \quad \text{Profile drag, absolute coefficient} = \frac{D_b}{qS} \)
\( D_i, \quad \text{Induced drag, absolute coefficient} = \frac{D_i}{qS} \)
\( D_p, \quad \text{Parasite drag, absolute coefficient} = \frac{D_p}{qS} \)
\( C, \quad \text{Cross-wind force, absolute coefficient} = \frac{C}{qS} \)
\( R, \quad \text{Resultant force} \)

\( \rho, \quad \text{Kinematic viscosity} \)
\( \rho, \quad \text{Density (mass per unit volume)} \)
\[ \text{Standard density of dry air, } 0.12497 \text{ kg-m}^{-1}\text{s}^{-2} \text{ at } 15^\circ \text{C. and } 760 \text{ mm}; \text{ or } 0.002378 \text{ lb.-ft}^{-1}\text{sec}^{-2} \]
\[ \text{Specific weight of "standard" air, } 1.2255 \text{ kg/m}^3 \text{ or } 0.07651 \text{ lb./cu. ft.} \]

\( \mu, \quad \text{Reynolds Number, where } l \text{ is a linear dimension} \)
\( \alpha, \quad \text{Angle of attack} \)
\( \epsilon, \quad \text{Angle of downwash} \)
\( \alpha_0, \quad \text{Angle of attack, infinite aspect ratio} \)
\( \alpha_n, \quad \text{Angle of attack, induced} \)
\( \alpha_{s2}, \quad \text{Angle of attack, absolute (measured from zero-lift position)} \)
\( \gamma, \quad \text{Flight-path angle} \)
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National Bureau of Standards
NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

HEADQUARTERS, NAVY BUILDING, WASHINGTON, D. C.

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SUMMARY

The strength of representative types of flush-riveted joints has been determined by testing 835 single-shear, double-shearing, and tensile specimens representing 7 types of rivet and 18 types of joint. The results, presented in graphic form, show the stress at failure, type of failure, and d/t ratio. In general, dimpled joints were appreciably stronger than countersunk or protruding-head joints, but their strength was greatly influenced by constructional details. The optimum d/t ratios have been determined for the several kinds of joints. Photomicrographs of each type show constructional details and, in several instances, cracks in the sheet.

INTRODUCTION

Aluminum-alloy sheet metal fastened by rivets is widely used as an exterior “skin” or plating on modern aircraft. The performance of aircraft depends to some extent on the smoothness of this skin because protruberances and irregularities cause frictional resistance. Protruding rivet heads are known to be an important source of skin friction both in air (references 1, 2, and 3) and in water (references 4 and 5). This consideration has caused manufacturers to use various “flush” rivets, that is, rivets the manufactured head of which is virtually continuous with the adjacent sheet.

Many highly ingenious designs and techniques for flush riveting have been developed. Generally a recess is formed in the sheet by either countersinking or dimpling to fit the manufactured head of the rivet. By countersinking is meant the removal of metal at one end of the rivet hole to form a circular bevel. Dimpling consists in forming an indentation in the sheet by means of suitable dies applied by pressure or impact. Dimpling is used to a greater extent than countersinking in thin sheets but, where sheets are joined to a relatively thick structural member, the sheet is often dimpled and the member countersunk. Details of flush-riveted joints used in German aircraft are given in reference 6. Reference 7 describes an American manufacturer’s production methods of flush riveting. Tools for drilling, dimpling, countersinking, and heading in flush riveting are described in reference 8.

The procedure and the assumptions used in the design of protruding-head or countersunk-head riveted joints for aircraft are substantially the same as those used for decades in the design of other riveted engineering structures. An adequate concept of the strength of dimpled joints cannot be obtained on this familiar basis, however, because a considerable portion of the load on a dimpled joint may be transmitted through the bearing surfaces of the dimple without acting on the rivet. Dimpled rivets are of great importance in modern flush riveting; a wide variety of constructional details and fabrication techniques are used. Consequently, a large amount of systematic test data would be required to put the design of dimpled joints on a basis as rational as the regular procedure for designing protruding-head and countersunk-head riveted joints. Although most manufacturers have made tests of the type of flush rivet used in their particular aircraft, technical literature contains little information useful in designing flush-riveted joints. It is the object of this investigation to obtain and to make available such information. The work was carried out by the National Bureau of Standards at the request of the National Advisory Committee for Aeronautics.

ACKNOWLEDGMENTS

Credit is due the United States Army Air Corps for assistance in obtaining test specimens, the Boeing Aircraft Co., the Curtiss-Wright Corporation, the Douglas Aircraft Co., Inc., the Glenn L. Martin Co., the Naval Aircraft Factory, the North American Aviation, Inc., the Seversky Aircraft Corporation, and the Sikorsky Aircraft Division of United Aircraft Corporation for submitting test specimens of flush-riveted joints; to the Aluminum Co. of America for donating the sheet and the rivets used in the joints fabricated at the National Bureau of Standards; and the Metallurgical Division of the National Bureau of Standards for making photomicrographs of the joints.

SPECIMENS

GENERAL

Seven airplane manufacturers and the Naval Aircraft Factory cooperated by furnishing specimens representative of commercial production. Each manufacturer fabricated specimens according to his own production methods. In addition two groups of specimens were fabricated at the National Bureau of Standards, using special-oval-countersunk and brazier-head...
rivets. Although these specimens are not strictly flush-riveted joints they were included because they represent alternative types that are sometimes used; the brazier-head specimens also permit a comparison with a conventional protruding-head type.

**DESIGN**

A standardized series of single-shearing, double-shearing, and tensile (load parallel to the rivet axis) specimens was used. A schematic load diagram for each kind is given in figure 1; drawings of the specimens are given in figures 2 and 3. The specimens were made

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**Figure 1.** Schematic diagram of specimens showing loads.

**Figure 2.** Shearing specimens.

**Figure 4.** Machine and fixture for testing shearing specimens.
as elementary as possible to permit an easy comparison between the different types of rivet.

Tensile specimens were included because it is obvious that some resistance to pulling the rivet heads out of the sheet is required, notwithstanding the assumption by many designers that the strength of a rivet under tensile load is negligible. Severe conditions of tensile loading would probably more often result from accident than from design. Portions of the plating of aircraft have been known to tear off when through accident the interior surface of the plating became exposed to the dynamic pressure of the air; the loading of a single-shearing joint (fig. 1) to failure is generally accompanied by bending of the offset members and resultant tensile loading of the rivet; local buckling of sheet often exerts prying forces on the rivets.

The shearing specimens (fig. 2) consisted of overlapping strips of sheet fastened by single rivets. The expression for the width W shown in figure 2 gives a constant ratio of net cross-sectional area of the sheet at the rivet to the area of the rivet. The double-shearing specimen was left optional. The specimens were held in the testing machine by pin connections as shown in figure 4. In the type of single-shearing specimen used the deformation before failure of the sheets is believed to be greater and the conditions of loading more severe than if two or more rivets had been used in tandem or two abutting sheets had been riveted to a third sheet.

The tensile specimen (fig. 3) consisted of two square sheets riveted together at the center. Each sheet was bolted to a flange (fig. 5) which was connected to the testing machine. Specimens having different rivet diameters were geometrically similar in the plane of the sheets; therefore the results are directly comparable if the d/t ratio is the same. The results of all tensile tests of riveted joints necessarily depend on the design of the specimen and the fixture; the results obtained in this investigation are therefore not directly comparable with results obtained by other methods. Tensile tests of protruding-head riveted joints are reported in reference 9. The specimen used in the present investigation was of the same design.
DESCRIPTION AND MACROSTRUCTURE

All manufacturers submitted single-shearing and tensile specimens; some manufacturers also submitted double-shearing specimens. Each manufacturer is designated by a letter: A, B, C, D, E, F, or G. The Naval Aircraft Factory is designated by NAF and the National Bureau of Standards by NBS. Cross-sectional drawings of the joints are shown in figure 6.

Cracks, shown in figure 10 (b), were found in only one specimen, type 21.

The following description of the specimens contains a summary of each manufacturer’s statement regarding his specimens followed by other information obtained from an examination of the specimens.

TABLE I.—MEANING OF SECOND DIGIT IN JOINT NUMBERS

<table>
<thead>
<tr>
<th>Single Shearing</th>
<th>Double Shearing</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>5</td>
<td>All sheets dimpled</td>
</tr>
<tr>
<td>2</td>
<td>6</td>
<td>Machine countersunk</td>
</tr>
<tr>
<td>3</td>
<td>7</td>
<td>Protruding Brazier head</td>
</tr>
<tr>
<td>4</td>
<td>8</td>
<td>1 sheet dimpled, 1 sheet machine countersunk</td>
</tr>
</tbody>
</table>
Manufacturer A—rivet 6; joints 62 and 66; figures 6 and 7.—An included angle of 100°, a slight crown and a cylindrical edge were shown in a drawing of type-6 rivets submitted by manufacturer A. He stated that the rivets were driven by hand in machine-countersunk sheets and finished with a rivet peen.

Figure 7 shows a slight crevice between the manufactured head and the sheet. Such a crevice is said to facilitate corrosion by retaining moisture.

Manufacturer B—rivet 1, joint 11; rivet 5, joint 51; figures 6 and 8.—Manufacturer B stated that 78° countersunk-head rivets conforming to Air Corps specification 25526-A, Standard Sheet AN425 type AD were used for most of the specimens (joint 11) and a few brazier-head rivets, type AN455AD, were used (joint 51). All sheets were dimpled. Rivets 1/2 to 7/2 inch in diameter were driven by a pneumatic gun; rivets of diameters 1/4 and 1/8 inch were driven by hand.

Figure 8 shows that the dimple of type-11 joints was curved to an unusually large radius, probably to avoid cracks. The gradual curvature at the dimple introduces a crevice between the manufactured head and the sheet, and also a certain amount of waviness in the surface of the joint caused by the large diameter of the dimple. According to reference 6, tests of airfoils containing a pattern of annular grooves 0.007 inch deep simulating the crevice between the head of a 3/16-inch dimpled rivet and the surrounding sheet show that such grooves appreciably increase the drag, even though no part of the rivet projects above the sheet.

The brazier head of the type-5 rivets is flattened during driving and becomes approximately flush with the sheet, as shown in figure 8. Severe shearing deformation of the sheets at the rim of the manufactured head is evident in the type-51 joint. The top sheet has cracked at this location. This deformation probably resulted either from poorly fitting dimpling tools or from excessive pressure.

Manufacturer C—rivet 3; joints 31 and 35; figures 6 and 9.—Manufacturer C stated that his rivets had an included angle of 100° and a cylindrical edge. They were driven by a process termed "punch countersinking" in which the manufactured head forms its own dimple. A special "one-shot" gun was used. This rivet and process were adopted after considerable experimenting. The tools used to drive the rivet were not described, but it is probable that dimpling of the sheets and heading of the rivet were accomplished with the same tools and at the same time. An included angle of 100° was said to be best for self-dimpling heads. Heads having a smaller angle are extruded into the hole to some extent and the remaining material is severely cold-worked to a final shape which may be too shallow in spite of the greater initial depth. Heads having included angles greater than 100° are initially too shallow to have adequate strength and rigidity.
The purpose of the cylindrical edge on the manufactured head is to prevent fatigue failure, which had been found to occur in sharp edges and also to prevent damage in handling and shipping. The usual type of pneumatic drive rivets in two or three blows was developed by manufacturer C. Punch countersinking was said to be most satisfactory for sheet thicknesses between 0.014 and 0.064 inch.

Cross sections of joints 31 and 35 are shown in figure 9 (a). When self-dimpling rivets are driven, if the \( d/t \) ratio is very low, the compressive stress in the manufactured head corresponding to the load required to dimple the sheet becomes so great that a very shallow-manufactured head results. (See fig. 9 (a).)
The top joint in figure 9 (a) apparently has a crack in the rivet shank, which is shown enlarged in (b). Manufacturer D—rivet 1; joint 11; figures 6 and 8.

Manufacturer D stated that his 78° countersunk-head type AN425D rivets were driven by a one-shot gun in machine-dimpled sheets.

FIGURE 8.—Cross section of joints, manufacturers B, D, F, G, and NAF.

When the shank was again sectioned, as shown in (c), at 90° to the plane exposed in (a) and (b) no crack was visible. The deformed and undeformed grains of this
Figure 8 shows that the radius of the dimple was comparatively short. Practically the full depth of the manufactured head is in contact with the dimple. The rivet holes appear to have been redrilled after dimpling. The driven head in the lower joint is folded around the edge of the lower sheet.

Manufacturer E—rivet 2; joints 21, 22, 24, 25, and 28; figures 6 and 10.—A drawing of type-2 rivets submitted by manufacturer E showed a 78° manufactured head smaller in diameter and depth than type 1. All rivets were 3/8 inch in diameter. It was stated that all sheets in the joint were simultaneously dimpled.
with a special tool in a pneumatic vibrator except in the case of 0.051- and 0.064-inch sheets which were machine countersunk. Where sheets of these thicknesses were joined to thinner sheets the latter were dimpled by

“vibrating” them into the countersunk recess (types 24 and 28). The sheets in most of the tensile specimens were unequal in thickness. The thinner sheet was adjacent to the manufactured head in every case. The rivets were driven with a squeezer.

Cross sections of four joints submitted by manufacturer E are shown in figure 10 (a). No cracks are visible, but when tensile tests were made it became evident that the sheets of some of the joints were cracked at the rim of the dimple. Other specimens (figure 10 (c) and (e)) were subsequently examined and circumferential cracks were found. [See also figure 10 (d) and (f).] The two cracks shown are probably the result of dimpling the sheet around too short a radius in an effort to obtain a smooth flush surface at the rivet head.
Figure 10 (b) shows radial cracks found in the 0.040-inch sheet of a type-21 joint when sectioned at a plane normal to the rivet axis and intersecting the dimple on the convex side. The sheet sectioned was adjacent to the driven head.

Manufacturer F—rivet 1; joints 11 and 12; figures 6 and 8.—Manufacturer F used 78° countersunk rivets (AN425-D, Air Corps Specification 25526-A). Sheets less than 0.102 inch thick were dimpled with punches having a 78° included angle for the sheet adjacent to the manufactured head and a 90° angle for the other. The 0.102- and 0.125-inch sheets were machine countersunk. The rivets were driven by a pneumatic hammer.

Manufacturer G—rivet 1; joint 11; figures 6 and 8.—Manufacturer G used 78° rivets (AN425AD and AN425DD, Air Corps Specification 25526-A). It was stated that the rivets were driven (not squeezed), presumably by a pneumatic hammer. The dimples shown in figure 8 are formed to a comparatively long radius.
NAF—rivet 4; joints 41 and 45; figures 6 and 8.—The Naval Aircraft Factory furnished a drawing of their self-dimpling rivet. It is similar to the brazier-head but has a larger fillet between the head and the shank. The rivet hole is drilled with a radius-counterbore drill, which forms the edge of the hole to fit this fillet. A recessed rivet set (fig. 12) is used at the driven head and a flat set at the manufactured head. Under the impacts of a one-shot hammer the shank is upset, the convex surface of the head is hammered flush with the sheet, and the sheets are dimpled with the same tools and at the same time. Three blows are required for \( \frac{3}{16} \)-inch rivets and five blows for \( \frac{5}{32} \)-inch rivets.

Objectionable "dishing" of the sheet surrounding the rivet was evident in these joints.

NBS—rivets 5 and 7; joints 53, 57, 72, and 76; figures 6 and 11.—Special-oval-countersunk-head rivets, type 7, and brazier-head rivets, type 5, were used in joints fabricated at the National Bureau of Standards. Specifications for these rivets are included in Navy Department Specification 43R5c (designated types 1 and 2, respectively, in that specification). The crown of the type 7 rivet has a \( \frac{3}{16} \)-inch depth for all sizes and the included angle of the head is decreased with increasing diameter. The sheet was machine countersunk.

![Figure 12. Tools for driving NAF rivets.](image-url)

![Figure 13. Fixture used to drive NBS rivets by compressive loading in a testing machine.](image-url)
The rivets were sawed to a length equal to the grip plus a head allowance of 1½ diameters. Two methods of driving were used, pressing and hammering. The load was applied to the press-driven rivets in a hydraulic testing machine (fig. 13). The diameter of the driven head was made 1½ times the shank diameter. The driving stresses used were 150,000 pounds per square inch for A17ST and 175,000 pounds per square inch for 17T rivets. The drop hammer (fig. 14) was used for the hammer-driven rivets. Five equal blows were used for each rivet. The height of drop, given in table III, was experimentally determined in advance to produce a diameter of driven head 1½ times the shank diameter. This method of hammering was adopted because it gives controllable and reproducible conditions of driving.

### TABLE III.—WEIGHT AND FALL OF DROP HAMMER

<table>
<thead>
<tr>
<th>Rivet diameter (in.)</th>
<th>Hammer weight (lb)</th>
<th>Fall (ft)</th>
</tr>
</thead>
<tbody>
<tr>
<td>¼</td>
<td>5</td>
<td>1.0</td>
</tr>
<tr>
<td>5/32</td>
<td>5</td>
<td>1.6</td>
</tr>
<tr>
<td>½</td>
<td>5</td>
<td>3.1</td>
</tr>
<tr>
<td>¼</td>
<td>20</td>
<td>1.1</td>
</tr>
</tbody>
</table>

Special-oval-countersunk-head rivets are also used in dimpled sheets, as specified in Naval Aircraft Factory Process Specification FR–1a for Sunken Rivet Construction in Bottom Plating of Main Floats. In this case the dimple is of such a depth that the top of the manufactured head is flush with the surface of the sheet outside the dimple. Joints of this type were not tested in this investigation. According to tests reported in reference 4 this construction offers no hydrodynamic advantage over a dimpled or a countersunk joint in which the crown of the head projects beyond the adjacent sheet.

### MECHANICAL PROPERTIES OF SHEET AND RIVET WIRE

Samples of the sheet used in the joints were submitted by most of the manufacturers. Tensile specimens conforming to Type 5, Federal Specification QQ–M–151a for Metals—General Specification for the Inspection of—were machined from these samples and tested with the results given in table IV. The yield strength was determined by the offset method from the stress-strain diagram using a 0.2 percent set. The tensile properties of all the 24ST sheets for which samples were available complied with the requirements of United States Army Specification 57–152–6 Type II and Navy Department Specification 47A10a, Condition T; the tensile properties of the alclad 24ST sheets complied with the requirements of United States Army
Air Corps Specification 11067, Type II and Navy Department Specification 47A8a, Condition T. In several instances where samples were not provided in tests having a 1-inch gage length and a reduced section 9/16-inch wide. These were machined from shearing specimens of joints that had been tested. These results are also given in table IV.

Bend specimens conforming to Federal Specification QQ-M-151a par. 18b were machined from samples of all the sheet used. The bend properties of all the sheets complied with the requirements of these specifications under tensile properties.

### TABLE IV. TENSILE PROPERTIES OF ALUMINUM-ALLOY SHEET

<table>
<thead>
<tr>
<th>Manufacturer</th>
<th>Material</th>
<th>YIELD STRENGTH (ksi)</th>
<th>Tensile Strength (ksi)</th>
<th>Elongation in 2 in. (%), Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>A. Alclad</td>
<td>.032</td>
<td>39,500</td>
<td>63,200</td>
<td>18% Submitted with shearing specimens.</td>
</tr>
<tr>
<td>A. Alclad</td>
<td>.036</td>
<td>41,000</td>
<td>65,800</td>
<td>18% Submitted with shearing specimens.</td>
</tr>
<tr>
<td>A. Alclad</td>
<td>.051</td>
<td>41,500</td>
<td>66,800</td>
<td>18% Submitted with shearing specimens.</td>
</tr>
<tr>
<td>A. Alclad</td>
<td>.072</td>
<td>42,000</td>
<td>66,800</td>
<td>21% Submitted with shearing specimens.</td>
</tr>
<tr>
<td>A. Alclad</td>
<td>.126</td>
<td>42,000</td>
<td>64,600</td>
<td>21% Submitted with shearing specimens.</td>
</tr>
</tbody>
</table>

**Remarks:**

1. The length of the specimen was transverse to the direction of rolling (transversal) unless the specimen is denoted "longitudinal." The orientation was determined by inspection.
Tensile and bend specimens of the aluminum-alloy wire from which the types 5 and 7 NBS rivets were made were tested. The results for the tensile specimens, given in table 5, complied with the requirements of Navy Department Specification 43R5c. The bend specimens also complied.

Samples of wire representing the rivets used by the manufacturers were not available.

### Diameters of Driven Heads

The diameter of the driven head was measured on each of the joints submitted by the manufacturers to determine what diameter was considered adequate by manufacturers and to aid in interpreting the results of the tensile test. The minimum, the average, and the maximum diameter, expressed as a multiple of the nominal Shank diameter, is given in table VI for each size of rivet used by each manufacturer.

### TESTING

The shearing and the tensile specimens were loaded to fracture as shown in figures 4 and 5, respectively, and the maximum load was determined. For each combination of sheet thickness and rivet diameter in the joints submitted by the manufacturers, 3 or 4 like specimens were tested. For each such combination in NBS joints, 15 specimens were tested: namely, 1 using each of 3 sheet materials (24ST, 24SRT, al clad 24ST) in each of the following 5 groups: 17ST rivets, type 7, press driven; A17ST rivets, type 7, press driven and hammer driven; A17ST rivets, type 5, press driven and hammer driven.

### RESULTS

#### General

The strength of the single-shearing, double-shearing, and tensile specimens is plotted (upper series of points) against the d/d ratio in figures 15 to 38, inclusive.

The shearing stress at failure $S_s$ was computed by dividing the maximum load $P$ by the nominal cross-sectional area of the rivet for the single-shearing specimens and by twice the nominal area for the double-shearing specimens:

$$S_s = \frac{4P}{\pi d^2} \text{ for single-shearing specimens}$$

$$S_s = \frac{2P}{\pi d} \text{ for double-shearing specimens}$$

The tensile stress at failure $S_t$ was computed by dividing the maximum load by the nominal cross-sectional area of the rivet. In the computation of the d/d ratio the average of the measured thicknesses of both sheets was used for the single-shearing and the tensile joints except where the two sheets were not of the same nominal thickness (types 21, 22, and 24). In this case the lesser thickness was used. Either the average thickness of the outer sheets of the double-shearing joints or half the thickness of the inner sheet, whichever was the lesser ($t_{\text{min}}$) was used.

The bearing stress at failure may be estimated from the curves shown in the plots of shearing strength. These curves are drawn for constant values of bearing stress

$$S_b = \frac{P}{d t} \text{ for single-shearing specimens}$$

$$S_b = \frac{P}{2d t_{\text{min}}} \text{ for double-shearing specimens}$$

#### Table V—Tensile Properties of Wire From Which NBS Rivets Were Made

<table>
<thead>
<tr>
<th>Rivet diameter (in.)</th>
<th>Tensile Strength (lb/sq in.)</th>
<th>Elongation in 4% (percent)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A17ST</td>
<td></td>
<td></td>
</tr>
<tr>
<td>&amp;1</td>
<td>25,500</td>
<td>46,200</td>
</tr>
<tr>
<td>&amp;2</td>
<td>25,500</td>
<td>44,200</td>
</tr>
<tr>
<td>&amp;3</td>
<td>26,500</td>
<td>45,800</td>
</tr>
<tr>
<td>&amp;4</td>
<td>25,700</td>
<td>46,600</td>
</tr>
<tr>
<td>17ST</td>
<td></td>
<td></td>
</tr>
<tr>
<td>&amp;1</td>
<td>34,500</td>
<td>58,700</td>
</tr>
<tr>
<td>&amp;2</td>
<td>33,800</td>
<td>57,500</td>
</tr>
<tr>
<td>&amp;3</td>
<td>36,500</td>
<td>63,300</td>
</tr>
<tr>
<td>&amp;4</td>
<td>37,300</td>
<td>62,500</td>
</tr>
</tbody>
</table>

#### Table VI—Ratio of Driven-Head Diameter to Nominal Shank Diameter

<table>
<thead>
<tr>
<th>Manufacturer</th>
<th>Minimum Shank diameter (in.)</th>
<th>Average Shank diameter (in.)</th>
<th>Maximum Shank diameter (in.)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Minimum</td>
<td>Average</td>
<td>Maximum</td>
</tr>
<tr>
<td>A</td>
<td>1.52</td>
<td>1.56</td>
<td>1.73</td>
</tr>
<tr>
<td>B</td>
<td>1.53</td>
<td>1.56</td>
<td>2.03</td>
</tr>
<tr>
<td>C</td>
<td>1.61</td>
<td>1.64</td>
<td>1.91</td>
</tr>
<tr>
<td>D</td>
<td>1.62</td>
<td>1.65</td>
<td>2.05</td>
</tr>
<tr>
<td>E</td>
<td>1.58</td>
<td>1.61</td>
<td>2.00</td>
</tr>
<tr>
<td>F</td>
<td>1.65</td>
<td>1.68</td>
<td>2.09</td>
</tr>
<tr>
<td>G</td>
<td>1.50</td>
<td>1.53</td>
<td>1.79</td>
</tr>
<tr>
<td>NAF</td>
<td>1.50</td>
<td>1.53</td>
<td>1.79</td>
</tr>
<tr>
<td>NBS</td>
<td>1.50</td>
<td>1.53</td>
<td>1.79</td>
</tr>
</tbody>
</table>
They were calculated by eliminating $P$ from (1) and (2) so that

$$S_b = \frac{\pi d}{4 t} S_s$$ for single-shearing specimens

$$S_b = \frac{\pi d}{4 t_{min}} S_s$$ for double-shearing specimens

The lower series of points in figures 15 to 38 indicates the rivet diameter (number=diameter in thirty-seconds of an inch) and the type of failure. (For meaning of symbols see table VII). Each point in the lower series corresponds to a point in the upper series plotted directly above it. Corresponding points in the two series can be identified by the similarity of their position with respect to other points. For example, in figure 15 the single-shearing specimen having the greatest strength is one of a group of three whose $d/t$ ratio (abscissa) is 1.5. The ordinate of this point is $S_s=47,500$ pounds per square inch. Interpolation between the curves $S_s=40,000$ and 60,000 pounds per square inch shows the bearing stress at failure to be
about 55,000 pounds per square inch. The highest point in the lower series shows that the rivet diameter for this specimen was \( \frac{5}{32} \) or \( \frac{3}{16} \) inch and the specimen failed by type \( j \) which is shearing of the rivet shank (from table VII).

The Vickers number was determined on the manufactured head of some of the rivets used by manufacturer F to determine whether the six rivets in the type-12 joints that had low strengths \( (d/t=1.5, \text{ three single shearing and three tensile, fig. 24}) \) also had low Vickers number. The Vickers number of these six rivets was found to be appreciably lower than the Vickers number of the other rivets used by manufacturer F. This result may be indicative of a rivet alloy other than 17ST or of improper heat treatment of these rivets.

**TABLE VII.—DESIGNATION OF TYPES OF FAILURE**

<table>
<thead>
<tr>
<th>Letter</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>Rivet canted appreciably in direction of loading.</td>
</tr>
<tr>
<td>b</td>
<td>Manufactured head pulled through sheet.</td>
</tr>
<tr>
<td>c</td>
<td>Driven head pulled through sheet.</td>
</tr>
<tr>
<td>d</td>
<td>Sheet tore at driven head.</td>
</tr>
<tr>
<td>e</td>
<td>Sheet tore at manufactured head.</td>
</tr>
<tr>
<td>f</td>
<td>Inner sheet tore (double-shearing joints).</td>
</tr>
<tr>
<td>g</td>
<td>One sheet ruptured at circumference of dimple.</td>
</tr>
<tr>
<td>h</td>
<td>Part or all of manufactured head sheared from shank.</td>
</tr>
<tr>
<td>i</td>
<td>Part or all of driven head sheared from shank.</td>
</tr>
<tr>
<td>j</td>
<td>Rivet shank sheared.</td>
</tr>
<tr>
<td>k</td>
<td>Rivet shank crumpled, ultimately failed by shearing.</td>
</tr>
<tr>
<td>l</td>
<td>Rivet hole in outer sheet elongated, shank canted and failed with jagged bearing fracture under combined shearing, tensile, bending, and bearing stresses.</td>
</tr>
<tr>
<td>m</td>
<td>Rivet shank failed with tensile fracture.</td>
</tr>
</tbody>
</table>

Typical failures of shearing and tensile joints are shown in figure 39. When the strengths of different types of joints are compared, it should be remembered that

(a) The same alloys were not used in all joints.
(b) The range of \( d/t \) is not the same for all groups, although in most cases the ranges overlap each other.
(c) The plotted results exhibit considerable scatter in some cases.
(d) The trend of curves representing the strength of different types of joints may be different.

**SINGLE SHEARING**

Figure 40 is a diagram summarizing the test results for all single-shearing specimens. Average strengths for like specimens were used in plotting this diagram. The lines indicate, for a given \( d/t \) ratio, the upper and the lower limits of the shearing and bearing stresses at ultimate load for each class of joint. For simplicity, all types of dimpled joints are grouped together in one class.

The lines designated by numbers in figure 40 may be interpreted as follows:

1. Designates scattered points that appear anomalous for no obvious reason. The range of \( d/t \) was generally too limited to establish the trend of a line representing these points.
(2) A horizontal line indicates that the shearing stress is critical and shows the range of $d/t$ for maximum ultimate shearing stress.

(3) A vertical line indicates that the bearing stress is critical and shows the range of $d/t$ for maximum ultimate bearing stress.

(4) A line showing decreasing ultimate shearing stress with increasing ultimate bearing stress indicates that both shearing and bearing stresses are critical. In this transitional range of $d/t$, neither the ultimate shearing stress in the rivet nor the ultimate bearing stress in the sheet attains its maximum possible value.

(5) A line showing decreasing ultimate bearing stress with increasing $d/t$ ratio at the greater values of $d/t$ probably reflects buckling of the sheet before tearing failure occurs.

(6) A line showing decreasing ultimate bearing stress with decreasing $d/t$ ratio for dimpled specimens probably reflects the decreasing "keying effect" of the dimple for joints employing self-dimpling rivets (types 31 and 51) as $d/t$ is decreased below a critical value. The dimple tends to become shallower as $d/t$ is decreased.

The lines described under (5) and (6) are rather doubtfully defined by the data, because they stand at the
FIGURE 20.—Test results for single-shearing specimens, manufacturer D.

FIGURE 21.—Test results for single-shearing and tensile specimens, manufacturer E. Points in the upper series indicate the stress at failure. Directly below each of these corresponding points is shown to indicate by number and letter symbols the rivet diameter in units of 1/8 inch and the type of failure (table VIII), respectively.

FIGURE 22.—Test results for single-shearing specimens, manufacturer G.
MECHANICAL PROPERTIES OF FLUSH-RIVETED JOINTS

Figure 23.—Test results for double-shearing specimens, manufacturer E.

Figure 21.—Test results for tensile specimens, manufacturer D.

Figure 24.—Test results for single-shearing and tensile specimens, manufacturer F. Points in the upper series indicate the stress at failure. Directly below each of these a corresponding point is shown to indicate by number and letter symbols the rivet diameter in units of 1/64 inch and the type of failure (table VII), respectively.
extremes of the available range of \( d/t \) ratios. It is possible that an extension of the range of \( d/t \) ratios investigated would alter the picture in this respect, but such extreme values of \( d/t \) are of little practical importance.

A trend of variation with respect to \( d/t \) is evident in the type of failure as well as the strength of the dimpled joints, as follows:

<table>
<thead>
<tr>
<th>( d/t ) ratio</th>
<th>Nature of failures (see table VII)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Less than 2.8.</td>
<td>Rivet failure (type j) exclusively.</td>
</tr>
<tr>
<td>2.8–4.9 (about 60 percent of the dimpled joints tested fall in this range).</td>
<td>Transitional between rivet and sheet failure: Type j (with a, d, or e in some cases), particularly in lower part of range. Type h, and a few type i (manufacturer B only), together with a and d, e or g. Type b or e with d, e, or both and generally a, particularly in the upper part of the range. A few type g with a and d or e (manufacturer G only).</td>
</tr>
<tr>
<td>Greater than 4.9.</td>
<td>Sheet failure: Nearly all type b or e, with d, e, or both and generally a. A few type e and type g with a and d or e (manufacturer G only). One rivet failure, type aeh, ( d/t = 6.0 ), manufacturer F.</td>
</tr>
</tbody>
</table>

---

**Figure 26.**—Test results for tensile specimens, manufacturer G.

**Figure 27.**—Test results for single-shearing and tensile specimens, manufacturer NAF. Points in the upper series indicate the stress at failure. Directly below each of these a corresponding point is shown to indicate by number and letter symbols the rivet diameter in units of \( \frac{1}{40} \) inch and the type of failure (table VII), respectively.
MECHANICAL PROPERTIES OF FLUSH-RIVETED JOINTS

Figure 28.—Test results for double-shearing specimens, manufacturer NAF.

Figure 30.—Test results for NBS AISI press-driven special-oval-countersunk-head riveted double-shearing specimens.

Figure 29.—Test results for NBS AISI press-driven special-oval-countersunk-head riveted single-shearing and tensile specimens. Points in the upper series indicate the stress at failure. Directly below each of these a corresponding point is shown to indicate by number and letter symbols the rivet diameter in units of \( \frac{1}{32} \) inch and the type of failure (table VII), respectively.
FIGURE 31.—Test results for NBS 17ST hammer-driven special-oval-countersunk-head riveted single-shearing and tensile specimen. Points in the upper series indicate the stress at failure. Directly below each of these a corresponding point is shown to indicate by number and letter symbols the rivet diameter in units of \( \frac{1}{32} \) inch and the type of failure (table VII), respectively.

FIGURE 32.—Test results for NBS 17ST hammer-driven special-oval-countersunk-head riveted double-shearing specimens.

FIGURE 33.—Test results for NBS 17ST press-driven special-oval-countersunk-head riveted double-shearing specimens.
It is to be noted that the values bounding the three ranges of \( d/t \) ratio closely correspond to the values at which the lines (2), (3), and (4) for dimpled joints join each other in figure 40. The relationship of strength to failure type may easily be seen by considering together the dependence of strength on \( d/t \) ratio according to figure 40 and of failure type on \( d/t \) ratio according to the preceding tabulation and regarding this latter quantity as a parameter.

Figure 41 shows, on a diagram similar to figure 40, the detailed comparison among dimpled rivets between the various manufacturing techniques and rivet types. Each line on figure 41 is to be interpreted in a similar manner to those on figure 40.

An examination of the results for the single-shearing specimens discloses the following significant points:

The critical shearing stress for protruding-head rivets is the same as for machine-countersunk rivets of the same alloy but, for protruding-head rivets, the critical bearing stress and the \( d/t \) ratio at which bearing stress becomes critical are higher. The scatter of the results on these joints is partly due to differences in sheet material; when shearing stresses are critical, joints in alclad material are slightly stronger than joints in 24ST and 24SRT, and vice versa when bearing stresses are critical. No significant difference can be found in the data between press-driven and hammer-driven rivets.

In some cases dimpled rivets had nearly twice the shearing and bearing strength of brazier and countersunk rivets. Figure 41 shows that, in general, the joints of manufacturer G (type 11) had the greatest strength,
Figures 35-38: Test results for NBS AI7ST press-driven brazier-head riveted single-shearing and tensile specimens. Points in the upper series indicate the stress at failure. Directly below each of these corresponding point is shown to indicate by number and letter symbols the rivet diameter in units of 1/32 inch and the type of failure (table VII), respectively.
clusion that details of design and technique of fabrication predominate in determining the strength of a dimpled joint.

Over a limited range of \(d/t\) the type-41 joints were approximately equal to the best type-11 joints in strength; the results for the type-41 joints were unusually consistent.

**Tensile**

A general classification with respect to principal types of failure, similar to that made for single-shearing joints, may also be made for the tensile joints as follows:

<table>
<thead>
<tr>
<th>(d/t) ratio</th>
<th>Nature of failures (see table VII)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Less than 2.1</td>
<td>Rivet failure exclusively; A few type m at the least values of (d/t) ratio (NBS only). Type h.</td>
</tr>
<tr>
<td>2.1–4.0</td>
<td>Transitional between rivet and sheet failures: Type h or dh (one type i, mfr. B). Type b or bd with or without g or h. Some type e, or ce with or without g or h. A few type g.</td>
</tr>
<tr>
<td>Greater than 4.0</td>
<td>Sheet failure exclusively: Type bd or ce with or without g. Type g with or without d or e.</td>
</tr>
</tbody>
</table>

For tensile joints, these three classes do not correspond to any well-marked trends of the plotted data. No quantitative criteria are known, analogous to shearing stress (for rivet failure) and bearing stress (for sheet failure) in the case of shearing joints, to which critical values defining the tensile strength of a joint may be assigned.

The stress, which is actually critical for rivet failure (except type m, tensile shank failure), is a combined bending and shearing stress on a cylindrical surface; the cylindrical surface is the projection into the head of the lateral surface of the shank.

For sheet failure, the stress that is actually critical is either a hoop stress around the edge of the hole or, for some dimpled joints, a combined shearing and bending stress at the most sharply curved section of the dimple.

Up to a \(d/t\) ratio of about 4, type-41 joints had the greatest tensile strength; for \(d/t\) ratios above 4, type-31 joints were stronger. Type-21 and type-24 joints had the least tensile strength.

The low tensile strength of some of type-21 and type-24 joints was definitely identified with the cracks in the sheet at the rim of the dimple, shown in figure 10 (d) and (f). In type-g failures the fractures occurred at the location where cracks were found in some of the
FIGURE 39.—Typical failures of test specimens. The symbols designate the manufacturer, the joint number (fig. 6), the rivet diameter in units of \( \frac{1}{32} \)-inch, and the type of failure (table VII).
Figure 40.—Summary of test results for all single-shearing specimens. The numbers in parentheses are explained in the text.
joints. However, it is improbable that all of the joints failing by type g had cracks. Type-g failure was not confined to type-21 and type-24 joints.

At the higher values of $d/t$ many of the joints failed by pulling the driven head through the sheet, but it is not believed that in many cases the tensile strength would be appreciably increased by increasing the driven-head diameter (given in table VI) because tearing of the sheet commenced underneath the head at the edge of the hole.

**Double Shearing**

Fewer types of double-shearing specimens were submitted than types of single-shearing and tensile specimens, and the range of $d/t$ covered by each type was generally less. Consequently a classification of failure-
types, like those made in the preceding sections, is more
difficult. Rivet failure (type j) exclusively occurred when
d/t was less than 3.6 and transitional failures (types k and l, mingled with type j and with type b) occurred when 
d/t = 3.6-6.8. No specimens having a
d/t ratio greater than 6.8 were tested.

For machine-countersunk joints (manufacturers A
and NBS) the ultimate shearing and bearing stresses had about the same relation to d/t ratio as for the
single-shearing joints of these manufacturers. For self-dimpling rivets (manufacturers C and NAF) the
ultimate shearing stress was lower than for comparable
single-shearing joints. This effect may probably be
ascribed to the longer grip in double-shearing joints as
compared with single-shearing joints of the same d/t ratio, which results in a shallower dimple. No double-
shearing joints were submitted that would show whether
the great superiority of some dimpled single-shearing
joints over machine-countersunk joints could be
reproduced for double-shearing joints.

The type-45 joints and the type-66 joints having
24ST rivets had the greatest strength of all double-
shearing joints submitted.

CONCLUSION

The mechanical properties of a joint, its surface
smoothness, the occurrence of cracks and the cost of
production are all determining factors in selecting a
flush-riveted joint. The importance of each of these
interrelated factors must be decided by the manufac-
turer for each particular application. For this
reason it seems impracticable to rate individual types
or to make a general statement regarding their merits.

Concerning the strength of flush-riveted joints in
aluminum-alloy, the following conclusions may be
drawn from data obtained in this investigation:

The optimum value of d/t ratio was the highest
value for which shearing stress alone is critical, unless
a high tensile strength is important, in which case a
somewhat lower d/t ratio may be indicated. Approxim-
ate average values for the optimum d/t ratio, neglecting tensile strength, were as follow:

<table>
<thead>
<tr>
<th>Class of joint</th>
<th>d/t</th>
</tr>
</thead>
<tbody>
<tr>
<td>Single-shearing machine countersunk</td>
<td>2.1</td>
</tr>
<tr>
<td>Single-shearing dimpled</td>
<td>2.8</td>
</tr>
<tr>
<td>Single-shearing protruding (brazier) head</td>
<td>3.7</td>
</tr>
<tr>
<td>Double-shearing</td>
<td>3.6</td>
</tr>
</tbody>
</table>

At d/t ratios below 2.1, machine-countersunk joints
had approximately the same shearing strength as bra-
zier-head riveted joints. This strength was slightly
higher for joints in alclad sheet than for joints in other
sheets of the same alloy. Although dimpled joints of dif-
ferent designs from different manufacturers showed wide

variations in strength, almost all of the dimpled single-
shearing joints having a d/t ratio above 2.1 showed an
important advantage in strength over machine-counter-
sunk joints. This value of d/t is probably the lower
limit at which satisfactory dimpling can be performed.

A detailed comparison of the strength of the various
types of single-shearing joints submitted by manu-
facters for this investigation is shown in figures 40
and 41.

The number of cracks found in randomly selected
dimpled joints emphasizes the need for avoiding severe
bends when flanging the sheet to form the dimple.
Unfortunately, it does not seem practicable to use a
bend of long radius at the dimple without introducing
bulging of the sheets and a crevice between the manu-
factured head and the sheet. The recent trend toward
a larger included angle of the manufactured head
(100°-120°) seems to offer a partial solution to this
difficulty in that the smaller bend angle at the dimple
permits a sharper bend without danger of rupture;
some reduction in the shearing strength would be ex-
pected to accompany this increase in the included
angle. The tensile test of joints was found to be
effective in detecting circumferential cracks in the sheet at the edge of the dimple.

NATIONAL BUREAU OF STANDARDS,
WASHINGTON, D. C. November, 1939.

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Characteristics of a 6- by 36-foot Clark Y Metal Airfoil.
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tional Resistance Caused by Various Types of Rivet Heads
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Heads on the Water Performance of a Seaplane Float.
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815.
Considerations for Quantity Production. S. A. E. Jour.,
9. Brueggeman, W. C.: Mechanical Properties of Aluminum-
Positive directions of axes and angles (forces and moments) are shown by arrows.

<table>
<thead>
<tr>
<th>Axis</th>
<th>Positive direction</th>
<th>Angle Velocities</th>
<th>Moment about axis</th>
<th>Force (parallel to axis) symbol</th>
</tr>
</thead>
<tbody>
<tr>
<td>Designation</td>
<td>Symbol</td>
<td>Designation</td>
<td>Symbol</td>
<td>Designation</td>
</tr>
<tr>
<td>Longitudinal</td>
<td>X</td>
<td>Rolling</td>
<td>L</td>
<td>( Y \rightarrow Z )</td>
</tr>
<tr>
<td>Lateral</td>
<td>Y</td>
<td>Pitching</td>
<td>M</td>
<td>( Z \rightarrow X )</td>
</tr>
<tr>
<td>Normal</td>
<td>Z</td>
<td>Yawing</td>
<td>N</td>
<td>( X \rightarrow Y )</td>
</tr>
</tbody>
</table>

Absolute coefficients of moment

\[ C_l = \frac{L}{q\beta S} \]  
\[ C_m = \frac{M}{q\epsilon S} \]  
\[ C_n = \frac{N}{q\beta S} \]

4. PROPELLER SYMBOLS

- **\( P \)**, Power, absolute coefficient \( C_P = \frac{P}{\rho n^2 D^4} \)
- **\( C_T \)**, Speed-power coefficient \( = \sqrt{\frac{P V^3}{\rho n^2}} \)
- **\( \eta \)**, Efficiency
- **\( n \)**, Revolutions per second, r.p.s.
- **\( \Phi \)**, Effective helix angle \( = \tan^{-1} \left( \frac{V}{2\pi n} \right) \)

5. NUMERICAL RELATIONS

- 1 hp. = 76.04 kg-m/s = 550 ft-lb./sec.
- 1 metric horsepower = 1.0132 hp.
- 1 m.p.h. = 0.4470 m.p.s.
- 1 m.p.s. = 2.2369 m.p.h.
- 1 lb. = 0.4536 kg.
- 1 kg = 2.2046 lb.
- 1 mi. = 1,609.35 m = 5,280 ft.
- 1 m = 3.2808 ft.