Solid State Technology Branch of NASA Lewis Research Center
Fifth Annual Digest
Preface

This year, 1993, was the year of "changing the paradigm," "empowering the staff," "satisfying the customer," "considering the stakeholders," and "transferring the technology," for "times are changing." However, customers are never satisfied with a substandard product. Salesmanship (transfer mechanisms) does not substitute for a good product. In fact, if one has trouble "transferring technology," there's a fair chance that the problem lies with the quality of the technology, since invariably the ease of technology transfer is proportional to its quality. These parts of the paradigm have not changed and will not change. What has changed, particularly for industrial research, is that the link to applications must be extremely short. As a result, most industrial labs have, in fact, become development labs or even product improvement labs. It falls, therefore, to the government laboratories to fill the void and supply the more long-range, high-risk research that feeds those development labs. Such research then is the "product" of the government laboratory. And the industrial development lab is its "customer," albeit a nonpaying one, to whom the technology must be transferred. This is not a new philosophy for the Solid State Technology Branch and the list of coauthors on the papers here illustrates that clearly.

The 49 papers in this volume include coauthors from Texas Instruments, Spire Corporation, Hughes Research Laboratories, IBM R&D Labs, TRW, Ball Aerospace, and Johnson Space Center—all "customers" for our technology and our expertise—all papers in which our in-house team has made a genuine contribution. In addition they include collaborators from 14 major universities, such as the University of Michigan, University of Texas, UCLA, Ohio State University, and the University of Nebraska—strong evidence that our work provides, quite properly in my opinion, a bridge between the truly basic research of the university and the focused shorter term development programs of industry.

The technical content of the papers presented here represents much the same mix as in previous years. In spite of the erosion of budgets, however, the number of papers presented or published in the year ending June 30, 1993 has increased dramatically. The digest which appeared in June 1991 contained reprints of just 25 papers; the June 1992 edition comprised 35; this year's volume contains a record high 49 papers which have been either published in journals or presented at conferences. Most of these latter are also available in the proceedings of those conferences.

Principal thrusts for this year include, in the circuits area, development of new transmission media, including analytical models, and techniques for coupling them to antennas; work on the use of silicon as a microwave substrate; methods to remove active devices or circuits from the substrate on which they were fabricated; and the development of pseudomorphic devices based on indium phosphide with an active layer of high indium content InGaAs.

Materials characterization work focused heavily on MODFET structures, such as InGaAs/InP, as well as on the evaluation of SiGe/Si materials from a multitude of sources. This last activity, as well as the work on transmission lines on silicon, is related to an attempt to evaluate the SiGe/Si structure for use in either FET or HBT-based microwave circuits, and possibly hybrid microwave/digital circuits.
Finally, work in superconductivity is still focused primarily on part 2 of the Naval Research Laboratory’s (NRL) High Temperature Superconducting Space Experiment (HTSSE-II). During the year, a prototype superconducting X-band receiver, developed in collaboration with the Jet Propulsion Laboratory, was delivered to NRL. Work was also undertaken this year on the deposition of BKBO superconducting films, primarily for use in mixers at THz frequencies.

Facilities augmentations this year were relatively modest, but included an automated noise figure measurement set up which permits us to measure device noise figures both at room temperature and at cryogenic temperatures.

Finally, we would like to acknowledge the contributions of Dr. Richard Q. Lee of the Antenna and RF Systems Technology branch. The collaboration between Dr. Lee and personnel of the Solid State Branch has been exceptionally fruitful.

Regis F. Leonard  
Chief, Solid State Technology Branch  
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SECTION ONE

MICROWAVE CIRCUIT AND ANTENNA DEVELOPMENT
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A 10-GHz Amplifier Using an Epitaxial Lift-Off Pseudomorphic HEMT Device

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Abstract—A process to integrate epitaxial lift-off devices and microstrip circuits has been demonstrated using a pseudomorphic HEMT on an alumina substrate. The circuit was a 10 GHz amplifier with the interconnection between the device and the microstrip circuit being made with photolithographically patterned metal. The measured and modeled response correlated extremely well with a maximum gain of 6.8 dB and a return loss of –14 dB at 10.4 GHz.

I. INTRODUCTION

In 1978, Konagai et al. [1] demonstrated that a thin film of GaAs based material could be removed from its growth substrate using a preferential etch of a buried AlAs layer. It is well known [2] that AlAs etches in HF:DI (1:10) at a rate $10^7$ times faster than Al$_x$Ga$_{1-x}$As when $x$ is less than 0.4. Also, because of the unique relationship between the lattice constant of AlAs–GaAs based materials, a structure can be made on GaAs that has a thin layer of AlAs grown between the substrate and the active device layer. The active layer is then later easily removed from the substrate via a HF etch of the AlAs sacrificial layer and the thin active layer can be attached to a limitless number of host substrates.

Work on epitaxial lift-off (ELO) techniques has progressed from optoelectronical devices [3], [4], to active circuits [5] and to microwave applications [6]–[8]. Shah et al. [6] demonstrated a MESFET device that had been fabricated after ELO which resulted in a $f_{\text{max}}$ of 14 GHz. Van Hoof [7] demonstrated a MESFET that had been fabricated before ELO. They compared device properties to see the effects of the ELO step on HEMT device characteristics [9], [10]. We found no degradation in the performance of the devices, but rather an enhancement of $f_T$ and the low-frequency gain. It was shown by Mena et al. [11] that an enhancement in the 2-D carrier confinement was detected after ELO, which would, in turn, explains the improvement in the gain of the HEMT device.

The purpose of making ELO devices is to independently optimize device and substrate properties in microwave circuit design. Here, for the first time, we present the integration of an ELO pseudomorphic HEMT (P-HEMT) device on a microwave substrate to fabricate a 10-GHz amplifier. The design will use a discrete ELO transistor attached to an alumina substrate. A classical, narrow band amplifier was designed using open circuit stub match and the typical scattering parameters of an ELO PHEMT device. Contact between the circuit and the PHEMT ELO device was made via photolithographically patterned metal lines. These interconnect lines step from the alumina substrate to the device, without the need of bondwires.

II. FABRICATION

The P-HEMT structure was MBE grown material, provided by QED Corporation, consisting of a Al$_{0.23}$Ga$_{0.77}$As–In$_{0.2}$Ga$_{0.8}$As–GaAs quantum-well structure with silicon pulse doping in the wide-band Al$_{0.23}$Ga$_{0.77}$As region. A 500-Å AlAs release layer was grown between the GaAs substrate and the superlattice to enable the ELO step. Varied thicknesses of the AlAs sacrificial layer from 50 to 1000 Å were evaluated and no significant difference in the ELO capability was detected.

Device fabrication started with a mesa isolation process that etched approximately 1500 Å of material to insure isolation while avoiding the AlAs layer. Ohmic contacts were formed using Au–Ge–Au–Ni–Au alloyed for 15 seconds at 400°C. Contact composition and alloying parameters are critical in maintaining good contact resistivities after ELO. Because of the extreme flexing of the thin film after ELO, the contacts must be able to withstand large angles of flexing without damage. Ti–Au gates were used to form 0.8-, 1.0-, and 1.2-µm gate lengths. The structure uses a dual 100-µm gate finger design to form a 200-µm gate width with a source to drain separation of 4 µm.

The ELO step was done using an apiezon wax coating of approximately 30-µm thick on the front side of the sample and cured at 150°C for 30 minutes. This gives the wax a compressive force to help facilitate the ELO step and protects the active device. The sample edges were cleaned and subjected to a preferential etch of hydrogen peroxide/ammonia hydroxide to remove the exposed active edge layer, leaving the AlAs release layer exposed [12]. The samples were then allowed to etch in a diluted HF solution overnight at room temperature to release the active layer from the GaAs substrate. Samples were attached to the alumina substrates and adhesion...
of the device was achieved via Van der Waals forces. To improve adhesion for further circuit processing and to allow for more stable device measurements, the devices were coated with a spin-on glass (SOG) and cured at 250°C for 4 hours. The SOG also improves the metal step coverage over the 8000-Å step generated by the ELO film and the alumina substrate [10]. A classical narrow-band, high-gain amplifier was designed using EESOF\textsuperscript{TM} with a center frequency of 10 GHz and optimized for a 10 mil alumina substrate. The microstrip circuit consists of one quarter wavelength coupled line dc blocks, series/shunt microstrip matching networks and bias networks that use a 1/4 wavelength high-impedance line cascaded with a 1/4 wavelength radial stub to provide RF isolation. The amplifier transmission lines were formed with a metal lift-off process after the ELO device was attached using 1.6 µm of gold. Contact between the transmission lines and the finished amplifier were made by opening contacts through the SOG. The amplifier design and finished active device are shown in Fig. 1(a) and (b), respectively.

III. RESULTS AND DISCUSSION

The circuit was mounted into a custom designed package utilizing coaxial connectors. Measurement of the device was done on a HP8510B based automatic network analyzer and the bias of the circuit was adjusted for optimum output performance.

The gain and return loss are shown in Fig. 2 for the finished circuit. A small signal gain maximum of 6.8 dB was measured at 10.4 GHz at a gate bias of −1.8 volts and drain bias of 3 volts. This compares with the modeled gain maximum of 9.2 dB with a design bandwidth of 1 GHz. However, the modeled response did not take into account such parameters as connector loss, radiation losses or an imperfect ground plane. The grounding used for this design was a front side ground plane created via a tapered 1/2 wavelength line to physical ground. Experimentally it was shown that the ground plane was sensitive to the slight variations in shape and imperfections that tended to degrade the amplifier gain. The return loss for the amplifier is a much narrower bandwidth than the gain response with a minimum of −14 dB at 10.4 GHz.

\textsuperscript{TM} EESOF is a registered trademark of EESOF, 5601 Lindero Canyon Road, Westlake Village, CA 91362.
GHz and a –2 dB out of band response. The data was taken at a –10 dBm input rf power level.

There was a strong correlation between the shape and frequency tracking of the modeled and measured data. In a circuit that utilizes standard discrete HEMT devices, it is difficult to predict the effect of bondwire length at the input, output and ground plane of the device. With ELO devices, the effect of bondwires are eliminated and the interconnecting lines between the circuit and the discrete device can be modeled accurately. The SOG was also investigated to determine its effect on RF device performance and it was determined to be negligible.

IV. CONCLUSION

An ELO P-HEMT discrete device was used in a narrow band amplifier design on an alumina substrate. The interconnection between the discrete device and the transmission lines of the alumina substrate were photolithographically defined eliminating the need for bondwires. The gain of the circuit was 6.8 dB and the return loss minimum was –14 dB at 10.4 GHz. This is the first reported use of a ELO P-HEMT device in a microwave circuit and demonstrates the feasibility of such a process for microwave applications.

Some of the advantages of using ELO devices and optimized substrates in microwave circuit design are: reduced substrate losses of the transmission lines; smaller transmission lines by using substrates with a smaller effective wavelength (λ_eff), i.e., 20% reduction in λ_eff when the substrate ε_r is increased from 13.1 to 20 at 10 GHz; better substrate power dissipation; lower engineering cost associated with circuit tuning and redesigns; and the integration of devices with dissimilar profiles such as diodes, FET’s, optoelectronic, and passive components.

ACKNOWLEDGMENT

The authors wish to thank N. Varaljay for his technical assistance throughout this research.

REFERENCES

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AN X-BAND "PEELED" HEMT AMPLIFIER

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ABSTRACT

A discrete peeled high electron mobility transistor (HEMT) device was integrated into a 10 GHz amplifier. The discrete HEMT device interconnects were made using photo patterned metal, stepping from the 10 mil alumina host substrate onto the 1.3 um thick peeled GaAs HEMT layer, eliminating the need for bond wires and creating a fully integrated circuit. Testing of devices indicate that the peeled device is not degraded by the peel off step but rather there is an improvement in the quantum well carrier confinement. Circuit testing resulted in a maximum gain of 8.5 dB and a return loss minimum of -12 dB.

INTRODUCTION

Epitaxial lift off of GaAs based layers allows for the removal of the active layer from the growth substrate and reattachment of the thin film discrete device to various host substrates. The thin film layers are of the order of microns thick and allow for the integration of a thin film active GaAs layer into normally incompatible device technologies such as indium phosphide, silicon or sapphire.

Various discrete devices have been peeled off and attached to host substrates. As examples, solar cell [1][2] and laser structures [3] were first demonstrated using the peel off technology. FET [4] devices were also peeled and tested on host substrates with a reported Fmax of 14 GHz for a 1.3 um GaAs MESFET.

To determine the effects of the peel off step on HEMT devices, data was presented by this author [5],[6] and the devices showed a quantum well electron carrier confinement improvement of the order of 10% after peel off. When designing a HEMT based circuit the effects of the peel off step are required to predictably design and fabricate a microwave circuit.

To date, there has been no reported integration of a peeled HEMT device into a microwave circuit due to processing problems and the lack of

device characterization. This paper will demonstrate an integrated X-band amplifier on alumina utilizing a peeled HEMT discrete device. The microwave circuit uses microstrip lines optimized for the alumina substrate and the peeled device is connected to the microstrip lines via photo patterned metal stepping over the thin film active device, thus eliminating the need for bond wires.

FABRICATION

The HEMT structure was MBE grown material, provided by QED Corporation, consisting of a Al$_{0.3}$Ga$_{0.7}$As/GaAs/Al$_{0.3}$Ga$_{0.7}$As square quantum well structure with silicon pulse doping in the wideband Al$_{0.3}$Ga$_{0.7}$As region. A 500A AlAs release layer was grown between the GaAs substrate and the superlattice to facilitate the "peel off" (See figure 1.)

Devices were fabricated using a mesa etch procedure for device isolation. Ohmic contacts were formed using a standard metal liftoff process and sequentially e-beam evaporated Au/Ge/Au/Ni/Au contacts. Alloying of the contacts was done in a RTA system for 15 seconds at 400°C. Gate photo patterning was followed by gate recessing to reduce exposure of the undoped wide bandgap AlGaAs material. Ti/Au was used to form 1.0, 1.2, and 1.4 μm gate lengths. The structure uses a dual 100 μm gate finger design to form a 200 μm gate width with a source to drain separation of 4 μm.

The peel off process was done using an apiezon wax coating of approximately 30 μm thickness. The wax was cured at 150°C for 30 minutes to give a compressive force to the wax to help facilitate the peel off step. The sample edges were cleaned and subjected to a hydrogen peroxide:ammonia hydroxide etch to remove the exposed active edge layer, leaving to AlAs release layer exposed. The samples were then allowed to etch in a diluted HF solution overnight at room temperature to release the active layer from the GaAs substrate.

Samples were attached to the alumina substrates and adhesion of the device was achieved via Van der Waals forces. To improve adhesion for further circuit processing and to allow for more stable device measurements, the devices are coated with a spin on glass and cured at 250°C for 4 hours (see figure 2(a)). Contacts were then opened using standard photo processing and metal patterning was complete as shown in figure 2(b).

A classical narrowband, high gain amplifier was designed with a center frequency of 10 GHz and optimized on a 10 mil thick alumina substrate. The microstrip circuit consists of quarter-wavelength coupled line DC blocks, series/shunt microstrip matching networks and bias networks which use a 1/4 wavelength high impedance line cascaded with a 1/4 wavelength radial stub to provide rf isolation. The finished amplifier is shown in figure 3.
RESULTS AND DISCUSSION

To do the circuit design, an analysis of the discrete device performance is required to evaluate the rf response after peel off. Figure 4 illustrates the measured gain response before and after peel off for a discrete HEMT device. As can be seen, the device experiences an improvement in the low frequency gain of approximately 2 dB but $F_{\text{max}}$ doesn't appear to be improved in this devices structure. An analysis of $H_{21}$ before and after peel off indicate $F_T$ values of 26 and 30 GHz, respectively, with $H_{21}$ showing a positive shift of 2 dB for the peeled sample.

Analysis of the S-parameters before and after peel off show a 5 dB decrease in $S_{12}$ and an increase of .5 dB for $S_{21}$ after peel off. Based on a lumped element equivalent circuit model of the peeled and unpeeled device, it was concluded that the intrinsic transconductance increased from the before peeled value of 194 mS/mm to 204 mS/mm. The most significant parametric change was a decrease in the drain-source resistance from 725 to 557 ohms before and after peel off.

Hall measurements were also conducted on peeled and non peeled Hall bars and the increase in the device performance for the peeled device is attributed to an improvement of the quantum well electron carrier confinement [5] resulting in an increased intrinsic transconductance. While there was an improvement in the transconductance, it's effect on $F_{\text{max}}$ was offset by the decrease in the source-drain resistance. Consequently, $F_{\text{max}}$ remained the same while $F_T$ experienced a 4 GHz enhancement after peel off.

DC characteristics of the amplifier circuit is shown in figure 5 for a device using one of the two 100 um gate fingers. As is illustrated by the DC performance, metal step coverage was achieved from the alumina substrate onto the 1.5 um thick GaAs HEMT device resulting in a fully integrated circuit.

Circuit performance of the X-band circuit was measured and is compared to modeled results (see figure 6). The design indicates a gain maximum response of 12 dB at 9.2 GHz while the measured gain was found be 8.5 dB at 9.3 GHz for the peeled HEMT amplifier. Further deviations from the designed response are seen in the measured circuit at frequencies greater than 9.3 GHz. Best return loss for the peeled circuit at 10.3 GHz was -12 dB as compared to the modeled value return loss at 10.3 GHz of -18 dB.

Based on the circuit model, the origin of the gain curve spike is attributed to source to ground inductance. Additionally, losses of the circuit can also be traced to connector losses and a imperfect rf ground scheme. The grounding used in this design utilizes low impedance, 1/2 wavelength stubs to ground rather than industry standard via holes to ground.
CONCLUSION

This paper presents the first reported use of a peeled HEMT device in a microwave integrated circuit. A X-band amplifier was modeled and fabricated using a discrete HEMT device on an alumina substrate. A fully integrated circuit was achieved eliminating the need for bond wires.

The discrete device performance was evaluated for a GaAs square channel structure and the discrete device response did experience a parametric change. An increase in the intrinsic transconductance and decrease of source-drain resistance after peel off was seen.

Amplifier performance was evaluated and the maximum gain was 8.5 dB at 9.3 GHz. Amplifier performance did follow the modeled trend but there was circuit loss which decreased the overall amplifier gain.

ACKNOWLEDGMENTS

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REFERENCES

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<tr>
<td>n+ GaAs capping layer</td>
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<tr>
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<tr>
<td>undoped GaAs channel (300Å)</td>
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<td>AlAs release layer (500Å)</td>
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<tr>
<td>undoped GaAs substrate</td>
<td></td>
</tr>
</tbody>
</table>

delta doping of Si 3.5e12/cm²

Figure 1. Square well, GaAs channel peel HEMT structure.

Figure 2. a.) Finished device structure with spin-on glass, b.) Discrete device structure showing metal contact method.
Figure 3. Finished X-band amplifier.

Figure 4. Measured $G_{\text{max}}$ before and after peel off for a discrete square well HEMT device.
Figure 5. Measured DC characteristics of Amplifier for one of the two 100 um gate fingers.

Figure 6. Measured and modeled gain response for the X-Band amplifier.
Characteristics of 0.8- and 0.2-μm Gate Length 
InₙGa₁₋ₓAs/In₀.₅₂Al₀.₄₈As/InP (0.53 ≤ x ≤ 0.70) Modulation-Doped Field-Effect Transistors at Cryogenic Temperatures

Richard Lai, Pallab K. Bhattacharya, Fellow, IEEE, David Yang, Timothy L. Brock, Samuel A. Alterovitz, and Alan N. Downey

Abstract—We have investigated analytically and experimentally the performance characteristics of InP-based InₓGa₁₋ₓAs/In₀.₅₂Al₀.₄₈As (0.53 ≤ x ≤ 0.70) pseudomorphic modulation-doped field-effect transistors (MODFET's) as a function of strain in the channel, gate, length, and temperature. The strain in the channel was varied by varying the In composition x. The temperature was varied in the range of 40–300 K and the devices have gate lengths L₉ of 0.8 and 0.2 μm. Analysis of the device was done using a one-dimensional self-consistent solution of the Poisson and Schrödinger equations in the channel, a two-dimensional Poisson solver to obtain the channel electric field, and a Monte Carlo simulation to estimate the carrier transit times in the channel. An increase in the value of the cutoff frequency is predicted for an increase in In composition, a decrease in temperature, and a decrease in gate length. The improvements seen with decreasing temperature, decreasing gate length, and increased In composition were smaller than those predicted by analysis. The experimental results on pseudomorphic InGaAs/InAlAs MODFET's have shown that there is a 15–30% improvement in cutoff frequency in both the 0.8- and 0.2-μm gate length devices when the temperature is lowered from 300 to 40 K.

I. INTRODUCTION

INDIUM PHOSPHATE-based pseudomorphic modulation-doped field-effect transistors (MODFET's) have demonstrated high-frequency and low-noise performance superior to that of any other field-effect transistors [1], [2]. In exploring the properties of high-performance pseudomorphic MODFET's, there are several important and critical issues. The transport properties of the channel and ultimately the device performance depend on the nature of the heterointerface across which electron transfer takes place. This, in turn, depends on the amount of strain in the channel, the growth parameters, and the growth modes. The question is, how much strain should be accommodated in the channel before the advantages listed above are outweighed by growth-related factors which ultimately degrade the transistor performance? Another important issue is the improvement in the performance of pseudomorphic MODFET's as the gate length is reduced.

In other words, it is important to determine if the performance of submicrometer-gate pseudomorphic MODFET's is significantly better than that of lattice-matched submicrometer devices. Finally, cryogenic operation of MODFET receivers and amplifiers has shown improved gain characteristics and lower noise figures compared to operation at room temperature [3], [4]. Other potential benefits such as greater reliability, lower metal resistance, and integration with high-temperature superconductors have further increased the interest in MODFET operation at cryogenic temperatures [5].

In the work reported here, we have investigated some of these issues in the context of understanding the performance characteristics of 0.8- and 0.2-μm gate length InₓGa₁₋ₓAs/In₀.₅₂Al₀.₄₈As heterostructure (x = 0.53, 0.60, and 0.70) pseudomorphic MODFET's at cryogenic temperatures.

II. NUMERICAL ANALYSIS OF DEVICE PERFORMANCE

We have analyzed the microwave performance of both the 0.8- and 0.2-μm devices in order to understand the characteristics of pseudomorphic InGaAs/InAlAs MODFET's. The schematic of a typical structure is shown in Fig. 1. The source-to-drain spacing is 3.5 and 2.0 μm for the 0.8- and 0.2-μm gate-length devices, respectively. The unintentional background doping for the InGaAs and InAlAs layers is assumed to be 2.0 × 10¹⁵ cm⁻³. The simulation was carried out as follows: first, the charge distribution in the growth direction (z direction) was obtained by self-consistently solving one-dimensional Poisson's equation and Schrödinger equation; next the two-dimensional Poisson's equation was solved for the device by a finite difference technique and the electric field along
A typical calculated band profile is shown in Fig. 2. The electric field profiles for a 0.2-µm device with In composition $x = 0.70$ are shown in Fig. 3(a) and (b). The gate is located in the middle of the plot, i.e., from 0.9 to 1.1 µm in position.

Self-consistent solutions of Poisson and Schrödinger equations show that as the In content in the pseudomorphic channel increases, the sheet charge carrier density $n_s$ also increases. This is expected and has been also observed experimentally. It arises mainly due to the increase in the band offset at the heterointerface $\Delta E_L$ with increasing indium in the channel. Note that in order to improve the quality of the active heterojunction, a 400-Å smoothing layer of lattice-matched InGaAs is incorporated below the channel layer. The electron wave function actually extends into this buffer layer, which can lead to inferior charge control with gate bias. Higher indium composition in the channel layer can lead to better charge confinement so that most of the conduction electrons will have smaller effective mass.

The electric field obtained from the solution of two-dimensional Poisson equation shows that most of the channel, except the region below the gate, is under low electric field. At the drain side of the gate, the electric field increases due to a pinch-off effect. As the gate length decreases from 0.8 to 0.2 µm, the electric field under the gate changes abruptly (Figs. 3(a) and (b)) due to the small dimension of the Schottky gate.

The Monte Carlo analysis gives insight to the electron transport properties in the channel. For both 0.8- and 0.2-µm gate-length devices, a small fraction of the electrons traveling in the high-field region of the channel are scattered into the $L$ valley. They gradually relax back into the $T$ valley as they travel through the gate–drain section. This is shown, as an example, in Fig. 4 for a 0.2-µm gate-
length device with the In composition in the channel \( x = 0.53 \). As \( x \) increases, the transfer to the \( L \) valleys decreases due to the larger \( \Gamma - L \) separation.

For the 0.8-\( \mu \text{m} \) gate-length device, the electron velocity in the channel increases with increasing In composition and decreasing temperature. For the 0.2-\( \mu \text{m} \) gate-length device, the abrupt change of the electric field under the gate leads to nonstationary transport [8]. Electron transport under the gate in these devices is dominated by velocity overshoot effects. Calculated 300 K velocities and electric fields in the channel for a 0.2-\( \mu \text{m} \) gate-length device with \( x = 0.7 \) are shown in Fig. 3(a). As the temperature is reduced to 40 K, phonon scattering is greatly reduced and the overshoot increases as seen in Fig. 3(b).

The average channel velocities for the different samples at 300 and 40 K are listed in Table I.

The time required for electrons to transit the channel under the gate is obtained from a transient Monte Carlo analysis. The intrinsic cutoff frequency without considering the gate-drain transit time is then obtained from

\[
fr_{\text{int}} = \frac{1}{2\pi \tau}
\]  

(1)

where \( \tau \) is the gate delay time. The calculated delay times for 0.8- and 0.2-\( \mu \text{m} \) gate-length device with channels of different composition and at temperatures of 40 and 300 K are shown in Fig. 5(a) and (b). The values of \( fr_{\text{int}} \) obtained from (1) are listed in Table II.

The trends in the calculated cutoff frequency values show the general improvement in values when increasing the In composition in the channel, decreasing the temperature, and decreasing the gate length. Indeed, we have observed experimentally the improvement in the average velocity for In\(_{0.53}\)Ga\(_{0.47}\)As/In\(_{0.52}\)Al\(_{0.48}\)As (0.53 \( \leq x \leq 0.65 \)) MODFET structures both with increasing In composition and decreasing temperature [9]. The improvement with increasing In composition can be attributed mainly to a smaller effective mass, a larger \( \Delta E_r \), and a decrease in alloy scattering. The improvement with decreasing temperature can be mainly attributed to a decrease in phonon scattering as well as other scattering rates. At the lower temperatures, polar optical phonon emission, ionized im-

![Fig. 4](image-url) Calculated \( \Gamma \)- and \( L \)-valley occupancy versus position in the source-drain region of an In\(_{0.53}\)Ga\(_{0.47}\)As/In\(_{0.52}\)Al\(_{0.48}\)As MODFET with 0.2-\( \mu \text{m} \) gate-length and 2.0-\( \mu \text{m} \) source-drain spacing. \( V_g = 0.2 \text{ V} \) and \( V_{dd} = 1.5 \text{ V} \) for this calculation.

![Fig. 5](image-url) Calculated gate delay times versus In composition at 300 and 40 K in pseudomorphic In\(_{x}\)Ga\(_{1-x}\)As/In\(_{0.52}\)Al\(_{0.48}\)As \((x = 0.53, 0.60, \text{ and } 0.70)\) channel MODFET's with (a) a 0.2-\( \mu \text{m} \) gate-length device and (b) a 0.8-\( \mu \text{m} \) gate-length device with \( V_g = 0.2 \text{ V} \) and \( V_{dd} = 1.5 \text{ V} \).

### TABLE I

<table>
<thead>
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<th>( x )</th>
<th>( V_g = 300 \text{ K} )</th>
<th>( V_g = 40 \text{ K} )</th>
<th>( V_g = 300 \text{ K} )</th>
<th>( V_g = 40 \text{ K} )</th>
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</table>

### TABLE II

<table>
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<tr>
<th>( x/L_g )</th>
<th>( fr_{\text{int}} )</th>
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<th>( fr_{\text{int}} )</th>
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<td>189.2</td>
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<td>52.7</td>
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purity scattering, piezoelectric scattering, and alloy scattering become the dominant scattering mechanisms. With decreasing gate length from 0.8 to 0.2 μm, velocity overshoot of the electrons increases the average velocity in the channel which leads to higher values of cutoff frequency. When combining the improvements seen with two or more of the variables (In composition, temperature, and gate length) interesting trends can be seen. The improvement seen with decreasing temperature is smaller as the In composition is increased in the channel. Also, the improvement seen with decreasing temperature is smaller with decreasing gate length. It should be noted that the data obtained from the analysis represent the theoretical uppermost limit in cutoff frequency obtainable for these devices. Due to nonideal device characteristics, such as interface roughness and interface traps in the layers, it is expected that any experimental data would show lower values for cutoff frequency compared to the theoretical ones, as will be evident in Section VI.

III. MOLECULAR BEAM EPITAXIAL GROWTH AND TRANSPORT PROPERTIES

The next step was to attempt to verify experimentally some of the results and their trends derived from the theoretical analysis. Schematic of the typical MODFET structure grown by MBE is shown in Fig. 1. Hall measurements were first made on van der Pauw samples to determine the transport properties. The Hall samples were recessed so that the InGaAs cap layers were removed to reduce parallel conduction. The sheet electron density in all the samples varied in the range of 2.0-3.2 \times 10^{12} cm^{-2}. In Fig. 6, we show a plot of the 300 and 77 K mobilities versus In content in the channel. It may be noted that as excess In is added, initially the mobility increases as expected. However, upon further increase of In, the mobility starts to saturate and even decrease. We have recently analyzed this transport behavior in detail and have found that the turnaround in mobility occurs at large misfits (> 1.5%) due to the onset of a three-dimensional island growth mode [10]. In other words, the minimum free energy for a strained system for misfits > 1.5% favors a three-dimensional surface. It is interesting and important to note that the dc and microwave characteristics of the MODFET's made with channels of increasing In content also exhibit the same behavior. In other words, the performance peaks at about x = 0.70 beyond which there is an observed degradation. The measured microwave characteristics of 0.8- and 0.2-μm gate pseudomorphic MODFET's at room temperature are listed in Table III.

IV. DEVICE FABRICATION

The heterostructures, shown in Fig. 1, were used to fabricate both 0.8- and 0.2-μm gate-length pseudomorphic In_{0.52}Ga_{0.48}As/In_{0.52}Al_{0.48}As (x = 0.53, 0.60, and 0.70) MODFET's. Standard lithography was used to fabricate the devices. The source-to-drain separation for the 0.8- and 0.2-μm gate length devices were 3.5 and 2.0 μm, respectively. For the 0.8-μm gate devices, optical lithography was used while for the 0.2-μm gate devices, electron-beam lithography using a P(MMA-MAA)/PMMA bilayer resist system was used. With the bilayer resist, T-shaped gates consisting of Ti/Pt/Au were realized and the gate length was measured using Scanning Electron Microscopy (SEM) to be 0.15-0.2 μm. The gate widths on the devices ranged between 50 and 150 μm.

V. DC CHARACTERISTICS

The 0.8-μm gate device showed a peak transconductance of 510 mS/mm at 300 K with a channel current of
200 mA/mm while the 0.2-µm gate device showed a peak transconductance of 705 mS/mm with a channel current of 300 mA/mm. Both devices were biased at a drain voltage of 1.5 V. The devices also showed low gate leakage (110 µA at $V_g = -0.5$ V for a $0.2 \times 45$ µm $^2$ device) and good pinchoff characteristics although in the submicrometer devices, output conductance increased dramatically. This increase in the output conductance may be attributed to an increase in leakage in the buffer layer, an increase in the background impurities (we observed a significant increase in the background impurities in our system when the wafers used for 0.2-µm gate devices were grown), and short-channel effects. 77 K dc measurements on the 0.8-µm gate device showed an increase in peak transconductance to 680 mS/mm, a decrease in output conductance from 40 to 20 mS/mm, and a decrease in gate leakage from 9 to less than 1.0 µA measured at a drain bias of 1.5 V and a gate bias of 0 V.

VI. MICROWAVE CHARACTERISTICS AT ROOM AND CRYOGENIC TEMPERATURES

Room-temperature microwave characteristics were measured for both 0.8- and 0.2-µm gate devices and for each In channel composition. The scattering parameters were measured using an HP8510 automatic network analyzer and a CASCADE wafer probe station from 0.5 to 26.5 GHz at various gate and drain bias voltages. Table III shows some of the results of the pseudomorphic $\text{In}_x\text{Ga}_{1-x}\text{As}/\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ MODFET's ($0.53 \leq x \leq 0.85$) that have been fabricated in our laboratory. Estimation of the maximum available gain cutoff frequency $f_{max}$ for the submicrometer devices were not made because the stability factor $k$ was smaller than 1.0 over the entire measured frequency range. The current-gain cutoff frequency $f_T$ was extrapolated from the measured current gain ($H_{21}$) versus frequency dependence with a $-6$-dB/octave slope. The best result achieved was an extrapolated $f_T$ value of 180 GHz for an $\text{In}_{0.70}\text{Ga}_{0.30}\text{As}/\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ MODFET with a gate dimension of $0.15 \times 150$ µm$^2$ with a maximum stable gain (MSG) of 17.3 dB at 26.5 GHz.

For cryogenic microwave characterization, the devices were diced, mounted, and bonded to coplanar chip carriers. The devices were measured in a coplanar waveguide test fixture (DESIGN TECHNIQUES). A spring loading capability was added to the test fixture to ensure repeatable contacts between the device carrier and the coaxial connectors especially during cooling. The cryogenic system included a helium closed-cycle refrigerator, a temperature controller, a silicon diode thermometer, and the test fixture attached to the refrigerator cold finger in a vacuum environment. The cryogenic system is capable of achieving and stabilizing temperature down to 40 K. The microwave measurements were again done using an HP8510 automatic network analyzer. Prior to cooling the device, the measurement setup was calibrated at room temperature using a set of open, short, and through standards. Then, a short-circuit standard was cooled to the desired temperatures to account for any shifts in the reference plane caused by the contraction of the cables, connectors, and the coplanar lines due to the lowering of temperature. This calibration method was found to be valid up to a frequency of 10–11 GHz. The problems at higher frequencies seem to be due to the fact that accounting for shifts in the reference plane is not sufficient to correct for the differences between room temperature and cryogenic temperatures. For example, the return loss for a through line measured at cryogenic temperatures after using the calibration routine becomes significantly degraded at higher frequencies.

The microwave characteristics of each device were measured at 300, 200, 120, 77, and 40 K from 0.5 to 11.0 GHz. The devices were measured over a range of $V_{ds}$ from 1.2 to 1.8 V and at various values of $V_g$ near the peak $g_m$ point. For both the 0.8- and the 0.2-µm gate devices, there was an observed increase in the measured magnitude of $S_{21}$ of up to 3 dB and commensurate increase in the current gain $H_{21}$ with decreasing temperature (shown in Fig. 7(a), (b) for the 0.8- and 0.2-µm gate devices with an $\text{In}_{0.70}\text{Ga}_{0.30}\text{As}$ channel) with decreasing temperature. The
TABLE IV

<p>| Extrapolated Values for Cutoff Frequency ( f_T ) (GHz) from Cryogenic Microwave Characteristics of 0.2- and 0.8-µm Gate MODFET's with Pseudomorphic In(<em>{x})Ga(</em>{1-x})As/In(<em>{0.52})Al(</em>{0.48})As Quantum Wells ((V_d = 1.5 \text{ V})) |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|</p>
<table>
<thead>
<tr>
<th>( f_T ) (x/L_s)</th>
<th>300 K 0.8 µm</th>
<th>40 K 0.8 µm</th>
<th>300 K 0.2 µm</th>
<th>40 K 0.2 µm</th>
<th>300 K 0.2 µm</th>
<th>40 K 0.2 µm</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.53</td>
<td>22</td>
<td>29</td>
<td>92</td>
<td>105</td>
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<td>29</td>
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<tr>
<td>0.60</td>
<td>38</td>
<td>51</td>
<td>121</td>
<td>145</td>
<td>0.70</td>
<td>38</td>
</tr>
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</table>

The measured microwave data were modeled to a standard equivalent circuit model for a MODFET (Fig. 8). The fitting of the microwave data had a maximum error of 5–10% over the frequency range of 0.5 to 11.0 GHz primarily due to noise in the measured data. Table V shows the equivalent circuit parameters that were extracted for the pseudomorphic In\(_{0.70}\)Ga\(_{0.30}\)As/In\(_{0.52}\)Al\(_{0.48}\)As MODFETs at 40 and 300 K. The parasitic gate-to-source capacitance \( C_{gs} \) is decreased as the gate length decreased from 0.8 to 0.2 µm, which will lead to an increase in cutoff frequency and hence the maximum oscillation frequency. The intrinsic \( f_T \) values showed approximately the same improvement in performance with lowering of temperature as the extrinsic \( f_T \). The improvement in microwave performance for both the 0.8- and 0.2-µm gate-length devices is approximately 15–30% when the temperature is lowered from 300 to 40 K and the relative improvement is found to be approximately the same as In composition in the channel is increased. The experimental results indicate a smaller improvement of cutoff frequency as In composition is increased and temperature is decreased than the values predicted in the analysis. More experiments need to be done to further investigate this point. However, the improvement with decreasing temperature was found to be slightly higher in the 0.8-µm device (25–30%) compared to the 0.2-µm (15–20%) device. This is consistent with the trend predicted by the analysis. Also, the values for cutoff frequency measured experimentally are significantly less than those predicted in the analysis section. Part of the reason may be due to the fact that effective gate length of a MODFET is larger than the metallurgical gate length [11]. The extra effective gate length can add up to an increase of 0.08 µm to the gate length of the device and can explain part of the difference between the calculated and measured data. Note that the transconductance delay time \( \tau_r \), which is obtained from a fit of the measured microwave data with the equivalent circuit, is different from \( \tau \) in (1).

| TABLE V | Equivalent Circuit Parameters of 0.8-µm \((V_d = 1.5 \text{ V}, V_g = 0.0 \text{ V})\) and 0.2-µm \((V_d = 1.4 \text{ V}, V_g = 0.15 \text{ V})\) Gate-Length MODFET's with Pseudomorphic In\(_{0.70}\)Ga\(_{0.30}\)As/In\(_{0.52}\)Al\(_{0.48}\)As Quantum Wells |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| \( L_s \) (nH) | 0.63            | 0.64            | 0.28            | 0.30            | 0.60            | 0.65            |
| \( L_g \) (nH) | 0.05            | 0.05            | 0.07            | 0.10            | 0.05            | 0.05            |
| \( R_s \) (Ω)  | 5.61            | 4.27            | 8.14            | 7.78            | 5.63            | 4.27            |
| \( R_g \) (Ω)  | 3.79            | 3.46            | 3.33            | 2.50            | 3.78            | 3.46            |
| \( C_{ds} \) (pF) | 0.065           | 0.288           | 0.075           | 0.17            | 0.065           | 0.288           |
| \( G_{ds} \) (mS) | 4.08            | 3.65            | 18.8            | 19.0            | 4.08            | 3.65            |

FIG. 8. Standard equivalent circuit model for a MODFET.
measured output conductance. The main reason for this is the improved confinement of the carriers in the 2DEG channel at lower temperatures. A slight increase in the extracted gate to source capacitance $C_{gs}$ was also observed (10%). This has been previously observed and modeled in GaAs/AlGaAs MODFET's [12]. It should be noted that the trends in $G_{ds}$ and $C_{gs}$ with temperature were observed for both the 0.2- and 0.8-µm gate-length devices.

Another observation that was made during these measurements was the absence of significant effects due to deep-level traps such as the collapse of $C_{gs}$ at low temperatures [13]. It should be noted that since the chamber was completely enclosed, the measurements were carried out in the dark. A small threshold shift of up to +0.21 V was observed in the dc characteristics for both the 0.2- and 0.8-µm gate-length devices. This value is smaller compared to the threshold shifts observed in AlGaAs/GaAs MODFET devices which typically range from +0.2 to +0.4 V [13]. The threshold shift in AlGaAs/GaAs MODFET's were mainly due to DX centers in the AlGaAs layers. Meanwhile, the threshold voltage shift in InAlAs/InGaAs MODFET's were due to interface traps in the InAlAs/InGaAs interface.

VIII. CONCLUSION

In conclusion, we have investigated the performance characteristics of InP-based pseudomorphic MODFET's with varying the In composition (0.53 ≤ x ≤ 0.70) which changes the strain in the channel. The temperature is varied in the range of 40–300 K and the devices have gate lengths $L_g$ of 0.8 and 0.2 µm. The analytical analysis predicts an increase in the intrinsic cutoff frequency with increasing In composition and decreasing temperature and gate length. Also, the analysis predicts that the increase in cutoff frequency with decreasing temperature is less significant with increasing In composition and decreasing gate length. Preliminary experimental results show that as In composition increase from 0.53 to 0.70, $f_T$ increase by 30–40%, and as the temperature decrease from 300 to 40 K, $f_T$ improves by 15–30%, both for 0.8- to 0.2-µm devices. These are among the first reported microwave measured data of pseudomorphic In$_{0.53}$Ga$_{0.47}$As/In$_{0.52}$Al$_{0.48}$As MODFET's at cryogenic temperatures.

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He joined NASA Lewis Research Center, Cleveland, OH, in 1977 and joined the Space Communications Division in 1979. From 1979 to 1985 he was engaged in microwave measurement and solid-state technology research, followed by a three-year hiatus in the Communications Projects Branch, acting as Experiments Manager for the Applications Technology Satellites Program. He returned to the Solid State Technology Branch in July of 1989, and his current research interests include the RF characterization of novel HEMT structures at cryogenic temperatures, MMIC applications, and micromachined passive electronic components for submillimeter wave radiometry.
PERFORMANCE OF A WIDEBAND GaAs LOW-NOISE AMPLIFIER AT CRYOGENIC TEMPERATURES

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KEY TERMS
GaAs low-noise amplifier, cryogenic temperatures, microwave measurements

ABSTRACT
The gain, noise figure, and 1-dB compression point of a commercially available GaAs amplifier were measured at cryogenic temperatures. The gain and noise figure characteristics were improved by decreasing temperature, while the 1-dB compression point remained unchanged. Repeated temperature cycling had no adverse effect on amplifier performance. © 1992 John Wiley & Sons, Inc.

I. INTRODUCTION
It is well known that semiconductor devices and circuits exhibit lower noise figures and higher gains at cryogenic temperatures [1-3]. The lower noise figure is due to reduced lattice vibrations in the device and the fact that external, additive noise varies directly with the absolute temperature. Gallium arsenide (GaAs) devices have better low-temperature characteristics than silicon devices, since they do not suffer from carrier freeze out when the doping is insufficient to form impurity bands. As a result, GaAs conductivity remains high even at very low temperatures, where Si conductivity is decreasing. The higher conductivity of GaAs makes it the key semiconductor in microwave devices and circuits. GaAs and heterostructure FETs have been extensively investigated at cryogenic temperatures [1-3]; however, GaAs monolithic microwave integrated circuits (MMIC) only recently have been evaluated. It was found that cryogenic operation would result in an increase in gain and a reduction in noise figure of MMICs, as is observed for discrete GaAs FET amplifiers [4, 5].

While important parameters for determining the cryogenic gain of an FET circuit, such as the transconductance at cryogenic temperatures, can sometimes be inferred from room-temperature data, this is not uniformly true. The same holds for cryogenic temperature values of minimum noise temperature. The spread in values is smaller for FETs from the same lot than for FETs from different lots. This means that before any amplifier design with stringent specifications can be carried out, extensive testing of the devices to be used will have to be performed. For devices such as distributed amplifiers, an additional problem is one of maintaining the integrity of bonds, traces, and/or solder joints. This is especially true if the device is repeatedly cycled over temperature.

II. EXPERIMENTAL DESIGN
For our experiment we used an AVANTEK low-noise amplifier (LNA), the PGM 11421. The amplifier is specified with a frequency response from 4 to 11 GHz, a minimum gain of 8.0 dB, a typical noise figure of 2.5 dB, and a minimum power output for 1-dB gain compression of +5 dBm. The dc bias for the package was 8 V at 60 mA (max.) The amplifier was mounted in a brass test fixture between 50-Ω input/output microstrip lines which were fabricated on a 10-mil Duroid (εr = 2.9) substrate, designed to be 14 long at 8 GHz. This length as chosen so as to minimize the interaction between the launcher pins and the amplifier. The coax to microstrip connection was accomplished by using SMA female flange connectors. A small amount of silver paint was used to improve the contact between the center conductor of the launcher and the microstrip line, and 0.010-in. diameter gold bond wire was used to connect the microstrip line to the amplifier package.

To measure the performance of amplifiers at low temperatures, a cryogenic system was used. It consists of a test chamber which can be evacuated by a vacuum pump, a cold finger on which the sample is mounted, an electrical feedline which supplies dc bias to the amplifier, and two electrical temperature sensors. With no thermal load, the cold finger is capable of achieving a temperature of 10 K. The sensors were connected to a temperature controller which could maintain a desired temperature by controlling a heater element wrapped around the cold finger via a feedback system. Two semirigid copper coaxial cables which extend beyond the cryocooler are used as input and output lines for the RF signals. Each semirigid cable is 12 in. long to minimize the thermal load on the circuit in the cryostat as well as the thermal gradient between the inside and outside environments. A piece of indium foil was put between the cold finger and the test fixture to help increase the thermal conductivity.

One of the temperature sensors was mounted on the cold finger; the other one was alternately mounted on the top surface of the test fixture, or on the side of the fixture as close as possible to the amplifier. There is a temperature difference between the two locations of the sensor on the test fixture of nearly 4 K. This temperature difference would vary with different types of amplifiers that had different dc bias levels. This is due to the fact that the amplifier is dissipating heat into the test fixture. While the sensor near the amplifier may indicate a temperature of 77 K, clearly the amplifier package is at a higher internal temperature. This is not considered a problem since the purpose of the experiment is to see whether or not commercially packaged devices could function in the cryogenic environment which is required to exploit the advantages of high-temperature superconducting passive (HTS) devices that must operate at cryogenic temperatures. Whatever advantages may be obtained by cooling the package amplifier to its actual internal temperature is an added bonus to the primary advantage of using these packaged devices in the same cryogenic environment along with HTS passive devices.

The S parameters were measured on a HP 8510B automatic network analyzer. A full two-port calibration was performed at the ends of the semirigid coax inside the cryostat so as to establish the reference planes at the terminals of the amplifier test fixture. The calibration performed at 300 K was used to make the measurements at 77 K, since no practical method exists at the present to perform this calibration at 77 K inside the cryostat. A two-port calibration was chosen over a TRL calibration since the amplifier test fixture was one piece, so that separate TRL fixtures would be required to perform the calibration. Using separate test fixtures would introduce errors due to physical differences in the test fixtures used to perform the TRL. As is the case for two port calibration, no
technique exists at present to perform a TRL calibration at low temperature that does not involve repeated temperature cycling. Since the purpose of this experiment was to determine whether or not commercial amplifier packages can operate reliably at cryogenic temperatures, it was determined that a two-port calibration would suffice for this experiment. Future work will focus on optimum measurements and characterization of these devices, at which time a fixture suitable for accurate TRL calibration will be used.

III. RESULTS

Figure 1 displays the measured $S_{21}$ values for the PGM 11421 GaAs FET amplifier at room temperature and 77 K. The useful frequency range of this amplifier is specified as 4-11 GHz. These figures show that the gain increased about 2 dB with decreasing temperature from 300 to 77 K. As expected, the bandwidth increased at low temperature since the transconductance increases and output capacitance decreases with decreasing temperature, and these parameters determine the high-frequency cutoff for an FET [7].

Noise-figure measurements were made on a HP 8970A noise figure meter. Figure 2 shows the values for the noise figure at 300 and at 77 K. These results show that the noise figure was about 2.5 dB at room temperature, and dropped to about 1 dB at 77 K.

To obtain accurate noise figure measurements, the LNA was replaced by a 50-$\Omega$ thru line supplied by Avantek, and the insertion loss for the test fixture, along with the two semirigid cables of the cryostat were measured on the ANA at 300 and at 77 K. This loss was measured to be nearly 2 dB at 300 K, and 1 dB at 77 K, over the frequency range of 4.0-11.0 GHz. One half of this loss, representing the loss of the test setup up to the input to the LNA, was subtracted away from the noise figure values obtained for the LNA. The other half of this insertion loss acts as a second stage contribution to the measured noise figure, and this was entered into the 8970A as a correction factor to the calibration that was performed. The effects of the bond wires are included in this measurement. The total insertion loss of the test fixture alone can be used to determine the actual gain of the LNA as well.

Table 1 shows the result obtained for the input 1-dB compression point at 300 and at 77 K. As may be seen from this table, the change in compression point with temperature is negligible. In order to perform this measurement, the loss in the cables used was measured in the HP 8510B at 300 and at 77 K. This information was used to accurately determine the input 1-dB compression point ($P_{i-1}$) for the amplifier.

To obtain these measurements, the LNA was cycled down to 77 K five times. It was used in other experiments as well, and has been cycled down to 35 K 30 times to date, and there has been no loss of performance noticed so far. The only low-temperature failures noticed in this experiment involved broken bond wires between the amplifier and the input/output microstrip lines. For reliable performance, it was found that the amplifier bonding pads should be located at the same height as the microstrip lines, and that there should be some slack introduced into the bond wire to allow for vibration from the compressor pump in the cold head assembly and thermal contraction in the Duroid substrate. The Duroid substrate had to be firmly bonded to the test fixture near the amplifier to ensure against warping in the substrate as the fixture is cycled over temperature.

IV. CONCLUSION

This article has presented gain and noise figure performance of the commercial packaged GaAs amplifier at different temperatures. As expected, a lower noise figure and a higher gain were induced by decreasing the temperature. No significant change in the input 1-dB compression point was observed.

The results obtained in this experiment would indicate that commercially packaged devices can be used at cryogenic temperatures. This would be a significant help in developing cryogenic microwave systems where packaged devices can be used in conjunction with high-temperature superconducting (HTS)
passive components [8], all at the same temperature. While this experiment does not establish the long-term reliability of commercial MMIC packages that are repeatedly cycled over temperature, it shows that there is potential for reliable operation in circumstances where the MMIC package is cooled only once, and kept at cryogenic temperatures for an extended length of time.

ACKNOWLEDGMENT
The authors wish to thank Mr. Ed Rylander, Sr., Test Engineer at Avantek Inc., Folsom, CA, for his generous advice on noise figure measurements and for supplying Avantek thru lines for calibration purposes.

REFERENCES

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FULL WAVE CHARACTERIZATION OF MICROSTRIP OPEN END DISCONTINUITIES PATTERNED ON ANISOTROPIC SUBSTRATES USING POTENTIAL THEORY

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Abstract

A technique for the full wave characterization of microstrip open end discontinuities fabricated on uniaxial anisotropic substrates using potential theory is presented. The substrate to be analyzed is enclosed in a cut-off waveguide, with the anisotropic axis aligned perpendicular to the air-dielectric interface. A full description of the sources on the microstrip line is included with edge conditions built in. Extension to other discontinuities is discussed.

Dynamic Source Reversal Technique

The anisotropic axis of the substrate is aligned perpendicular to the air-dielectric interface as shown in Fig. 1. The anisotropic dielectric may be represented as a tensor quantity given by

$$\kappa(y) = \kappa(y)I + \kappa_y(y)\mathbf{a_ya_y}$$

where I is the unit dyad and $\kappa(y) = \kappa_y(y) = 1$ for $y > h$. The microstrip line is assumed to be infinitely thin and located at a height $y = h$. In terms of the sources on the microstrip line, the scalar and vector potentials, $\Phi$ and $A$ respectively, for the dielectric loaded waveguide may be determined from

$$\nabla^2 A_x + \kappa_0^2 A_x = -\mu_0 J_x$$

$$\nabla^2 A_y + \kappa_0^2 A_y = -\mu_0 J_y$$

$$\nabla^2 \phi + \kappa_0^2 \phi = j\omega \mu \epsilon_0 (\kappa - 1) \phi (y - h) \delta (y - h) + j\omega \mu \epsilon_0 (\kappa_y - \kappa) \delta \phi \delta y$$

The potentials appearing in Eqs. (2) to (5) are obtained from the appropriate Green’s functions and the corresponding sources using

$$A_{x,y}(x,h,z) = \mu_0 \int \int G_{x,y}(x,h,z;x',h,z') A_{x,y}(x',h,z') dx'dz'$$

Introduction

While there is extensive data available on the microwave characterization of a variety of microstrip discontinuities using both quasi-static [1-3] and full wave techniques [4-6], the characterization has been restricted to isotropic substrates. To date, there is no published data regarding microstrip discontinuities patterned on anisotropic substrates. Some very useful microwave substrates however, like sapphire, are anisotropic and so any discontinuity structures fabricated on them cannot be properly characterized by the techniques that have been developed for isotropic dielectric substrates.

A technique for the full wave characterization of microstrip open ends fabricated on lossless uniaxial anisotropic substrates has been developed and is presented here. It is based on a dynamic source reversal technique that uses potential theory [7], which is a generalization of the charge reversal technique introduced several years ago [1]. The discontinuity is enclosed in a waveguide of infinite extent whose dimensions are such that the guide is cut-off for the propagating frequency on the microstrip. All sources on the microstrip are represented, and the technique does not require a model for the source exitation.

*National Research Council—NASA Research Associate at Lewis Research Center.
\[ \varepsilon_0 \Phi(x,h,z) = \int \int C_\Phi(x,h,x';x',h,z') \rho(x',h,z') \, dx' \, dz' \]  
(7)

From these potentials the electric field components are found using
\[ \begin{align*}
E_x &= -j \omega A_y - \partial \Phi / \partial x \\
E_y &= -j \omega A_y - \partial \Phi / \partial y \\
E_z &= -j \omega A_z - \partial \Phi / \partial z
\end{align*} \]  
(8)

where it is required that for this particular geometry \( E_x \) and \( E_z \) vanish on the microstrip. The anisotropic effect appears only in the LSM mode terms, which are present in \( A_y \) and \( \Phi \). The LSE modes are unchanged from those obtained for the isotropic case.

A complete set of dominant mode sources on the microstrip are represented; the longitudinal and transverse currents, as well as the charge on the microstrip line, with appropriate edge conditions built in. For a wide range of practical open end discontinuities, a valid approximation is that \( J_x = 0 \), so only the boundary condition \( E_z = 0 \) is required for this problem.

A line terminated at \( z = 0 \), thus forming an open end, would create reflected dominant mode sources on the line, along with perturbed sources localized near the discontinuity. The total source distribution on an open end may be written as
\[ J_s(x',h,x') = J_0 s(x')(e^{-j \beta x'} - Re^{-j \beta x'}) + J_1 s(x',x') \]  
(9)

\[ \rho(x',h,z') = \rho_0(x')(e^{-j \beta z'} + Re^{+j \beta z'}) + \rho_1(x',z') \]  
(10)

for \( z' \leq 0 \), where \( J_0 s, \rho_0 \) and \( \beta \) are the yet to be determined amplitudes and propagation constant, respectively, of the dominant microstrip mode, \( R \) is an unknown reflection coefficient, and \( J_1 s \) and \( \rho_1 \) represent the perturbed source amplitudes near the open end. Weighted Chebychev polynomials are used to represent the sources in \( x \) for both dominant and perturbed sources, while triangle and pulse functions are used to represent the perturbed sources in \( z \).

Equations (9) and (10) may be written as
\[ \begin{align*}
J_s(x',h,x') &= [(1 + R)J_0 s(x')(B_{in} \cos(\beta z') - \sin(\beta z')) + J_1 s(x',x')] \cdot [1 - U(z')] \\
\rho(x',h,z') &= [(1 + R)\rho_0(x')(B_{in} \sin(\beta z') + \cos(\beta z')) + \rho_1(x',z')] \cdot [1 - U(z')]
\end{align*} \]  
(11) and (12)

and the dominant mode sources are assumed to exist for \( -\infty \leq z' \leq \infty \). Then dominant mode sources for \( z' > 0 \) are subtracted away to create the terms that multiply the \((1 + R)\) coefficient in (11) and (12). Since the amplitudes of \( J_1 s \) and \( \rho_1 \) are arbitrary at this point, they may be defined so as to include the \((1 + R)\) term. Now the \((1 + R)\) term is common to all of the source terms, so it may be normalized to 1.0.

Using Eqs. (11) and (12) in Eqs. (6) and (7) and substituting into Eq. (8) gives the electric field in terms of the sources on the open end microstrip line. When the requirement that \( E_x = 0 \) on the microstrip is enforced, the terms corresponding to the dominant mode on the infinite line already satisfy the boundary condition on the strip, so they drop out. The sources existing for \( z' > 0 \) may be considered "source reversed" terms which produce an impressed field in the region \( z \leq 0 \) but localized near the discontinuity. The factor \((1 + R)\) can be included into the arbitrary amplitude of the dominant mode sources. Thus, apart from the unknown parameter \( B_{in} \), the dominant mode sources in \( z' > 0 \) produce a known forcing function in the strip for \( z' < 0 \). The electric field produced by the perturbed sources \( J_1 s \) and \( \rho_1 \), must cancel the tangential component of the applied field for \( z \leq 0 \). A modified perturbation technique [8] is used to determine the unknown dominant mode amplitudes and propagation constant for an infinite line.

The method of moments is then used to reduce the resulting integral equation to a matrix equation which can be solved for the unknown input admittance \( B_{in} \), as well as for \( J_1 s \) and \( \rho_1 \). Only one matrix inversion is required to find \( B_{in} \).

Results

The pulse width, \( \Delta \), of the expansion functions was chosen to be 0.32 mm at \( f = 2.0 \) GHz (or \( \Delta \approx 0.0053\lambda_g \) for sapphire). This pulse width guaranteed a converged value for \( B_{in} \) [7] for all of the examples presented. To verify the accuracy of the theory as well as the resulting program, the program was checked for the isotropic case, and was able to duplicate data obtained in [1] and [7].

Table I shows the results obtained using this technique for several different anisotropic substrates as a function of microstrip line width. The open circuit capacitance, \( C_{oc} \), is found using \( C_{oc} = B_{in} / Z_0 \), where the characteristic impedance \( Z_0 \) is obtained from a computer program developed on the basis of the theory presented in [8] for the characterization of infinite microstrip lines with sidewalls, but no top cover. To justify using values of \( Z_0 \) thus obtained, calculations performed for a microstrip line with an air dielectric showed less than 2% difference in \( Z_0 \) values obtained with and without a top cover. Table II shows the variation of \( C_{oc} \) as a function of line width for sapphire, and compares the results obtained for a substrate with an isotropic dielectric constant of 9.4, as well as for an isotropic dielectric constant of 11.6. Table III shows the effects of fixed waveguide dimensions on \( B_{in} \) and \( C_{oc} \) as a function of frequency of the propagating microstrip mode. For low frequencies, \( B_{in} \) varies linearly with frequency, starting to deviate as the frequency increases, this effect becomes more pronounced until the cut off frequency of the \( E_{11} \) waveguide mode is reached. This effect may be overcome by either frequency scaling the input parameters or by adjusting the waveguide dimensions accordingly.
The BASIC computer program developed to implement this technique can be executed on a personal computer with as little as 640K of RAM. Other discontinuity structures can be characterized in a similar manner. The technique is computationally efficient, there is no need to model the source excitation, and the admittance can be solved for directly in the case of a one port network. All integrals involving the expansion and testing functions are performed analytically so no numerical integrations are necessary, and the dominant portions of slowly converging series can be extracted and summed into closed form.

This technique can be extended to rapidly and accurately characterize a number of other commonly used discontinuity structures, especially "coaxial" two port structures such as asymmetrical gaps and steps in width. To characterize a two port structure in terms of an equivalent "Tee" or "Pi" network, the Tangent Plane method [9] can be used to extract parameter values.

References


TABLE I.—OPEN CIRCUIT CAPACITANCE, $C_{oc}$, FOR SEVERAL ANISOTROPIC DIELECTRIC MATERIALS. FREQUENCY = 2.0 GHz, $h = 1.0$ mm, $b = 11$ mm, $2a = 20$ mm FOR $W/h < 4.0$ ELSE $2a = 10(W/h)$. $Z_0$ VALUES OBTAINED FROM REF. 8. UNITS ARE pF/METER FOR $C_{oc}$.

<table>
<thead>
<tr>
<th>W/h</th>
<th>0.25</th>
<th>0.5</th>
<th>1.0</th>
<th>2.0</th>
<th>4.0</th>
<th>6.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>PTFE/Woven glass</td>
<td>$\kappa$</td>
<td>1.914</td>
<td>1.941</td>
<td>1.981</td>
<td>2.042</td>
<td>2.129</td>
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<tr>
<td>$\kappa = 2.84$</td>
<td>$Z_0$</td>
<td>150.5</td>
<td>119.9</td>
<td>90.02</td>
<td>62.46</td>
<td>39.82</td>
</tr>
<tr>
<td>$\kappa = 2.45$</td>
<td>$C_{oc}/W$</td>
<td>29.85</td>
<td>23.71</td>
<td>19.90</td>
<td>17.66</td>
<td>16.29</td>
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<tr>
<td>Boron nitride</td>
<td>$\kappa$</td>
<td>2.676</td>
<td>2.699</td>
<td>2.738</td>
<td>2.808</td>
<td>2.922</td>
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<tr>
<td>$\kappa = 5.12$</td>
<td>$Z_0$</td>
<td>127.4</td>
<td>101.7</td>
<td>76.68</td>
<td>53.38</td>
<td>34.09</td>
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<tr>
<td>$\kappa = 3.4$</td>
<td>$C_{oc}/W$</td>
<td>43.04</td>
<td>33.95</td>
<td>28.27</td>
<td>24.84</td>
<td>22.72</td>
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<tr>
<td>Sapphire</td>
<td>$\kappa$</td>
<td>6.724</td>
<td>7.012</td>
<td>7.647</td>
<td>8.145</td>
<td>9.007</td>
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<td>$\kappa = 9.4$</td>
<td>$Z_0$</td>
<td>80.90</td>
<td>63.65</td>
<td>46.94</td>
<td>31.82</td>
<td>19.80</td>
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<tr>
<td>$\kappa = 11.6$</td>
<td>$C_{oc}/W$</td>
<td>80.36</td>
<td>65.56</td>
<td>56.38</td>
<td>50.95</td>
<td>47.43</td>
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<tr>
<td>$\kappa = 13$</td>
<td>$Z_0$</td>
<td>79.90</td>
<td>63.44</td>
<td>47.39</td>
<td>32.61</td>
<td>20.55</td>
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<tr>
<td>$\kappa = 10.3$</td>
<td>$C_{oc}/W$</td>
<td>95.28</td>
<td>76.26</td>
<td>64.44</td>
<td>57.35</td>
<td>52.93</td>
</tr>
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TABLE II.—VARIATION OF $C_{oc}$ AS A FUNCTION OF LINE WIDTH FOR SAPPHIRE, $\kappa = 9.4, \kappa_y = 11.6$ COMPARED TO THAT OF AN ISOTROPIC DIELECTRIC. FREQUENCY = 2.0 GHz, $h = 1.0$ mm, $b = 11$ mm, $2a = 20$ mm FOR $W/h < 4.0$, ELSE $2a = 10(W/h)$. UNITS ARE pF/METER FOR $C_{oc}$.

<table>
<thead>
<tr>
<th>W/h</th>
<th>0.25</th>
<th>0.5</th>
<th>1.0</th>
<th>2.0</th>
<th>4.0</th>
<th>6.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sapphire</td>
<td>$\kappa = 9.4$</td>
<td>$C_{oc}/W$</td>
<td>80.36</td>
<td>65.56</td>
<td>56.38</td>
<td>50.95</td>
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<td>$\kappa_y = 11.6$</td>
<td>$C_{oc}/W$</td>
<td>75.56</td>
<td>61.06</td>
<td>52.10</td>
<td>46.80</td>
<td>43.42</td>
</tr>
<tr>
<td>Sapphire</td>
<td>$\kappa = 9.4$</td>
<td>$C_{oc}/W$</td>
<td>90.18</td>
<td>73.27</td>
<td>62.58</td>
<td>56.21</td>
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<tr>
<td>$\kappa_y = 11.6$</td>
<td>$C_{oc}/W$</td>
<td>75.56</td>
<td>61.06</td>
<td>52.10</td>
<td>46.80</td>
<td>43.42</td>
</tr>
</tbody>
</table>

TABLE III.—VARIATION OF THE NORMALIZED INPUT SUSCEPTANCE, $B_{in}$, AND OPEN CIRCUIT CAPACITANCE, $C_{oc}$, WITH FREQUENCY. WAVEGUIDE DIMENSIONS ARE $2a = 20$ mm, $b = 11$ mm AND $h = 1$ mm.

<table>
<thead>
<tr>
<th>Frequency, GHz</th>
<th>$B_{in}$</th>
<th>$C_{oc}$ (pF/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>0.008388</td>
<td>56.26</td>
</tr>
<tr>
<td>1.0</td>
<td>0.016776</td>
<td>56.26</td>
</tr>
<tr>
<td>2.0</td>
<td>0.033256</td>
<td>56.38</td>
</tr>
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<td>4.0</td>
<td>0.068373</td>
<td>56.85</td>
</tr>
<tr>
<td>6.0</td>
<td>0.167738</td>
<td>90.81</td>
</tr>
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</table>
A comprehensive theoretical and experimental study of coplanar waveguide shunt stubs

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ABSTRACT

A comprehensive theoretical and experimental study of straight and bent CPW shunt stubs is presented. In the theoretical analysis, the CPW is assumed to be inside a cavity, while, the experiments are performed on open structures. A hybrid technique has been developed to analyze the CPW discontinuities which has been proven to be accurate since the theoretical and experimental results agree very well. Throughout this study, the effect of the cavity resonances on the behavior of the stubs with and without air-bridges is investigated. In addition, the encountered radiation loss due to the discontinuities is evaluated experimentally.

INTRODUCTION

Recently, with the push to high frequencies and monolithic technology, coplanar waveguides (CPWs) have experienced a growing interest due to their appealing properties. While there is no need for via holes in CPW circuits, air-bridges are fundamental components required to connect the ground planes for suppression of the coupled slotline mode. In the past few years, there has been several attempts to characterize, theoretically and/or experimentally, CPW discontinuities with air-bridges or bond wires [1-5]. The Finite Difference Frequency Domain method was used in [6] to treat two common types of CPW air-bridges where it was found that the reflection coefficient (or $S_{11}$) varies linearly with frequency. This fact suggests that a typical air-bridge can be modeled as a frequency dependent lumped element [1, 2]. With this fact in mind, a hybrid technique has been developed by the authors [2] to analyze CPW discontinuities with air-bridges. In this technique, at first, the frequency dependent equivalent circuit of the discontinuity, with the air-bridges removed, is derived using the Space Domain Integral Equation (SDIE) method [7]. Then, this equivalent circuit is modified by incorporating the parasitic reactances introduced by the air-bridges. These reactances, a series inductance and a shunt capacitance, are evaluated by modeling the air-bridges as sections of an air filled microstrip line or parallel plate waveguide. The SDIE method will not be discussed here since it has been presented in detail in [7]. However, a slight modification on the equivalent circuit presented in [2] is needed as discussed below.

After applying the method of moments, the electric field in the slot apertures, which forms standing waves of the fundamental coplanar waveguide mode away from the discontinuity, is obtained. Notice that the slotline mode will not be excited in the CPW feed lines since the discontinuities considered here (Fig.2) are symmetric with respect to the center axis of the feeding lines. Consequently, an ideal transmission line method can be used to determine the scattering parameters and evaluate the elements of the equivalent circuit shown in Fig.3a. It should be noticed that in the case of straight stubs, the two reactances $X_1$ and $X_2$ are equal due to the symmetry of the circuit. Fig.3b shows the new equivalent circuit after taking the air-bridges into consideration. The air-bridges can be modeled as sections of an air-filled microstrip line [1], and simple design formulas can be used to evaluate the parasitic capacitance $C_a$ and inductance $L_a$. Alternatively, a parallel plate waveguide model can be employed to evaluate the same parasitic effects. It is found that the difference in the values of the parasitic reactances as predicted by the two models has a


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negligible effect on the performance of the circuit. Finally, new scattering parameters are evaluated from the modified equivalent circuit.

RESULTS AND DISCUSSION

In the numerical results shown here, the considered CPW discontinuities are suspended inside a rectangular cavity, as shown in Fig.1, with \( h = 400 \mu m, \varepsilon_{11} = 13, \varepsilon_{22} = 1, S = 75 \mu m, W = 50 \mu m, \) and \( h_1 = h_2 = 1.2 \text{ mm}. \) On the other hand, the slots and center conductor of the CPW stubs have equal widths of 25 \( \mu m. \) In addition, in the case of the open-end stubs, the width of the open-end is 25 \( \mu m. \) In all examples presented here, the stubs are placed symmetrically at the center of the cavity.

The experiments were performed in an open environment with the CPW circuits fabricated on 400 \( \mu m \) thick GaAs using lift-off processing. The CPW center strip and ground planes consist of 200 \( A \) of Cr and 1.5 \( \mu m \) of Au. The air-bridges have 10 \( \mu m \) square posts and are 14 \( \mu m \) wide. The air-bridge thickness and height are 1.0 \( \mu m \) and 3.0 \( \mu m \) respectively. The GaAs circuit was placed on a piece of 3.175 \( mm \) 5880 RF/duroid which has a dielectric constant of 2.2.

The circuits were tested with HP 8510 network analyzer and a Cascade probe station. The calibration standards for a TRL calibration were fabricated on the wafer to allow calibration to the reference planes of the CPW stubs. To cover the 5-40 GHz bandwidth, three delay lines were used. The probe positioning on the wafer was determined to be repeatable to within 3 \( \mu m \) which creates a maximum error in the phase of \( S_{21} \) of 0.76° at 40 GHz.

Fig.4 shows the S-parameters of the straight open-end stub (Fig.2a) of length \( L = 1100 \mu m \) and with the air-bridges removed as a function of frequency. It is noticed that the theoretical and experimental results agree very well up to the first resonance, after which, discrepancy in noticeable. This is attributed to the radiation loss encountered in the measurements which is mainly due to the excitation of the slotline mode in the CPW stubs in the absence of the air-bridges. It is found that the anomalous behavior seen between 41 and 45 GHz is due to a cavity resonance at 43 GHz which corresponds to the \( LSM_{121} \) mode excited in the partially filled lower cavity (the cavity width was chosen to be 3.425 \( mm \)). It is interesting to note that the \( LSM_{211} \) and \( LSM_{131} \) modes which have resonant frequencies of 38 and 48 GHz, respectively, do not show any effect on the stub. This may be attributed to the fact that the longitudinal electric field component of the \( LSM_{111} \) and \( LSM_{131} \) is an odd function with respect to a symmetry plane placed at the center of the cavity, as opposed to the \( LSM_{211} \) mode whose longitudinal component is an even function around the same plane. Thus, cavity modes, which have an even variation with respect to this plane, interact with the slotline mode in the stubs, which in turn affects the value of the series reactance in the equivalent circuit. It is expected that if the CPW structure is placed asymmetrically inside the cavity, other cavity resonances will also have an effect on the circuit performance.

Fig.5 shows the S-parameters of the same straight open-end stub with air-bridges. As it can be seen, the stub resonates at nearly 24.5 GHz where the length of the stub is approximately quarter of a coplanar mode wavelength. It can be noticed that the agreement between the theoretical and experimental data in Fig.5 is much better than the one seen in Fig.4. This can be attributed to the fact that the air-bridges tend to prevent the slotline mode from being excited in the CPW stubs which effectively reduces radiation losses. In addition, it can be seen that the resonance effect noticed in Fig.4 has disappeared since \( X_L \) is shorted by the relatively small air-bridge inductance \( L_a. \) Alternatively, the air-bridges short out the slotline mode, thus, eliminating interaction with the cavity resonances. As a result, with the presence of air-bridges, cavity resonances have no effect on the characteristics of a straight stub as long as it is placed symmetrically inside the cavity. One can also notice an anomalous effect at 40 GHz existing in Fig.5. A similar effect has been found in [4] for the case of a bent open-end stub. This effect may be due to a resonating slotline mode excited in the stubs beyond the air-bridge.

Fig.6 shows \( Mag(S_{12}) \) for the bent open-end CPW stub (Fig.2b) of mean length 1100 \( \mu m \) with and without air-bridges. In this case, the width of the cavity is taken to be 2 \( mm. \) It can be seen that for the bent stub without air-bridges, the agreement between theory and experiment is better than that seen in Fig.4 for the straight stub without air-bridges. The same behavior, observed in the straight open-end stubs with air-bridges at 40 GHz, can be seen more clearly in Fig.6 for the bent stubs with air-bridges. Moreover, the resonant frequency of this bent stub with air-bridges is approximately the same as the one for the straight stub of the same mean length.

From the measured scattering parameters, the loss factor due to the stubs can be calculated. This loss factor includes radiation, conductor, and dielectric losses. Since the stubs are all the same length, a comparison of the loss factor can provide a measure of the radiation loss. Fig.7a shows the loss factor of the open-end stubs without air-bridges. It is noticed that loss is maximum at the resonant frequency of the stubs, which is similar to what has been found in microstrip stubs [8]. Furthermore, the loss factor for the straight stub is larger than that for the bent stub. Lower loss is due to the fact that in the case of bent stubs, the fields radiated by the slotline modes in the two opposing stubs partially cancel. This explains why the agreement between the theoretical and experimental results for the bent stubs without air-bridges (Fig.6) is better than that for the straight stubs without air-bridges (Fig.4). The loss factor for the open-end stubs with air-bridges is shown in Fig.7b. The air-bridges reduce radiation loss by shorting out the coupled slotline mode, but it is still noted that the straight stub have increasing radiation loss after the first resonant frequency.

Numerical and experimental results for the short-end stubs (Figures 2c and 2d) will be presented in the symposium.
CONCLUSIONS

A comprehensive theoretical and experimental study of CPW shunt stubs has been presented. In the theoretical analysis, the CPW was assumed to be inside a cavity, while, the experiments were performed in an open environment. A hybrid technique has been developed to analyze the CPW discontinuities which proved valid since the results obtained theoretically and experimentally agreed very well. In addition, the effect of the cavity resonances on the behavior of the stubs has been studied. It was found that air-bridges suppress the slotline mode and cancel the effect of the cavity resonances on the characteristics of the stub. Moreover, it has been shown through experiments that bent CPW stubs should be used whenever the circuit layout permits to reduce the radiation loss caused by the parasitic coupled slotline mode.

ACKNOWLEDGMENT

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REFERENCES


Figure 1: A cross section of a CPW inside a cavity.

Figure 2: Different CPW shunt stubs. (a) Straight open-end CPW stub. (b) Bent open-end CPW stub. (c) Straight short-end CPW stub. (d) Bent short-end CPW stub.

Figure 3: (a) Equivalent circuit of the CPW discontinuities shown in Fig. 2 without the air-bridges. (b) The modified equivalent circuit after taking the air-bridges into consideration. (The reference planes are taken at the end of the uniform feeding lines)
Figure 4: Scattering parameters of the straight open-end stub without air-bridges with $L = 1100\mu m$.

Figure 5: Scattering parameters of the straight open-end stub with air-bridges with $L = 1100\mu m$.

Figure 6: $\text{Mag}(S_{12})$ of the bent open-end stub with and without air-bridges with mean length of $1100\mu m$ ($L_1 = 100\mu m$, $L_2 = 1025\mu m$).

Figure 7: The measured loss factor of the open-end CPW stubs (a) without air-bridges. (b) with air-bridges.
A Comparative Study between Shielded and Open Coplanar Waveguide Discontinuities

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ABSTRACT

A comparative study between open and shielded coplanar waveguide (CPW) discontinuities is presented. In this study, the space domain integral equation method is used to characterize several discontinuities such as the open-end CPW and CPW series stubs. Two different geometries of CPW series stubs (straight and bent stubs) are compared with respect to resonant frequency and radiation loss. In addition, the encountered radiation loss due to different CPW shunt stubs is evaluated experimentally. The notion of \textit{forced radiation} simulation is presented, and the results of such a simulation are compared to the \textit{actual} radiation loss obtained rigorously. It is shown that such a simulation cannot give reliable results concerning radiation loss from printed circuits. © 1992 John Wiley & Sons, Inc.

INTRODUCTION

Coplanar waveguide (CPW) is rapidly becoming the transmission line of choice in high-frequency applications and is successfully competing against the microstrip which has been the primary structure for hybrid and monolithic circuits. Due to many years of microstrip use, a large body of published data and CAD software pertaining to low- and high-frequency microstrip circuit and antenna design has been widely available. In contrast, models for shielded or open coplanar waveguide circuit design are still under development [1–21]. In addition, there is little data available concerning the radiation loss from CPW discontinuities [7,12,19]; therefore, there are no guidelines for low-loss, high-frequency CPW design. Nevertheless, despite this scarcity of reliable circuit models, CPW has provided an attractive alternative to conventional microstrip lines at high frequencies due to many appealing properties [22–27]. These include the ability to wafer probe, and the ease in connecting shunt lumped elements or devices without using via holes. Such advantages arise because both conducting surfaces (the center conductor and the ground plane) are on the same side of the dielectric substrate.

Another important characteristic of coplanar waveguides is that the line impedance and phase velocity are less dependent on the substrate height than on the aspect ratio (slot width/center conductor width). Since the conducting surfaces of a CPW structure are all printed on the same interface, careful design could efficiently confine the fields to this interface. This characteristic benefits both shielded and open CPW lines as it provides control over leakage and unwanted parasitic coupling. Printed lines which are not enclosed in a metallic package, such as the feed network of a monolithic array, tend to radiate power in the...
form of space and surface waves. In conventional monolithic lines, the level of parasitic radiation is strongly affected by the electric thickness of the substrate, which complicates high-frequency design due to little flexibility in choosing appropriate substrate structures. Since mechanical considerations put a lower limit on the physical thickness of integrated circuit substrates, it is difficult to avoid excessive loss when operating above 100 GHz in lines such as the microstrip where the field penetrates the whole substrate. In contrast, in coplanar waveguides the substrate thickness plays a lesser role; the fields are concentrated in the slots and are better confined on narrow apertures. Since the dimensions of the slots are limited only by photolithographic techniques, coplanar waveguides have more flexibility in design and, therefore, greater potential for low radiation loss and low dispersion.

However, even if coplanar waveguides radiate much less than a microstrip operating at the same frequency, as this frequency enters the submillimeter-wave region, the radiation loss increases and complicates the design. As a result, further reduction of parasitic radiation is required. A way to achieve this and be able to extend the operation of a coplanar waveguide into the submillimeter-wave region is to generate a surface-wave–free environment. This is possible with the use of a matched dielectric lens which has been exploited effectively to excite aperture-type radiating elements [28,29]. In such a structure, as in almost all CPW circuits, air-bridges (or bond wires) are used to connect the ground planes in order to suppress the coupled slotline mode. These air-bridges can be characterized by either using a rigorous full wave analysis [10,16,17,20] or a hybrid technique [11,14].

In this article, shielded and open CPW discontinuities will be analyzed using the space domain integral equation (SDIE) technique [8,9,12,30]. This method has shown excellent versatility in the study of a wide range of planar elements, and its accuracy has been demonstrated by comparison to measurements performed on a variety of open and shielded structures. The integral equation is formulated in terms of equivalent magnetic currents flowing on the slot apertures, as opposed to the full-wave technique presented in refs. [1,6,19], where an integral equation in terms of the electric current on the conducting surfaces is formed. The former technique is more appropriate for CPW problems where the ground planes approach the boundary surfaces, while the latter better fits problems having finite size conductors. The SDIE technique, as presented here, accurately takes into account all loss mechanisms by employing the appropriate Green's functions. Specifically, in the case of open coplanar waveguide discontinuities, the open space Green's function is expressed in terms of Sommerfeld integrals so that radiation in the form of space and surface waves is accurately evaluated. This is in contrast to techniques used elsewhere [31,32], which simulate open space by setting the cover resistance to 377 Ω (forced radiation). Resonant properties and radiation losses for a number of shielded and open CPW stub discontinuities will be presented and guidelines for design will be given.

2. THEORY

A generic geometry for a conventional coplanar waveguide structure is shown in Figure 1. The dielectric layers supporting the coplanar structure are considered lossless and the conducting surfaces have zero ohmic loss. The two-slot apertures have width $W$ and are separated by a distance $S$. With the application of the equivalence principle, the two slots can be replaced by equivalent magnetic currents $(\bar{M}_x^s, \bar{M}_y^s)$ flowing on a perfectly conducting surface which covers the slot apertures (see Fig. 2). These magnetic currents radiate electric fields, which are continuous across the surface...
of the slot apertures, as shown by the following equations:

\[
\begin{align*}
\vec{M}_s^+ &= -\vec{M}_s^- = \vec{M}_s \\
\vec{M}_s^+ &= \vec{E}_s \times \hat{\alpha}_z, \quad z \geq 0 \\
\vec{M}_s^- &= \vec{E}_s \times (-\hat{\alpha}_z), \quad z \leq 0
\end{align*}
\]  

with

\[
\vec{E}_s = \sin[\xi(x' - x_{n-1})] \\
\times \frac{\sin(\xi \delta)}{\sin(\xi \delta)}
\]

\[
\vec{H}_s = \vec{E}_s \times \hat{\alpha}_z
\]

where \(\vec{E}_s\) is the electric field in the slot apertures. Furthermore, continuity of the magnetic fields on the slot apertures results in the expression

\[
\hat{\alpha}_z \times [\vec{H}^+ (\vec{M}_s^+ - \vec{H}^- (\vec{M}_s^-)] = \hat{\alpha}_z \times \vec{H}_s
\]

where \(\vec{H}^+ (\vec{M}_s^+)\) and \(\vec{H}^- (\vec{M}_s^-)\) are the magnetic fields radiated above and below the slots, respectively, and \(\vec{H}_s\) is the incident magnetic field exciting the CPW line. The magnetic fields may be expressed in terms of the unknown equivalent magnetic currents through a first-order Fredholm integral equation:

\[
\vec{H}_s = \int \int_{S_{CPW}} [k_2^2 \vec{I} + \vec{V} \vec{\nabla}] \\
\times \vec{F}_m(\vec{r} / \vec{r}') \cdot \vec{M}_s(\vec{r}') \, ds'
\]

In eq. (5), \(S_{CPW}\) is the surface of the slot apertures and \(k_2^2\) and \(\vec{F}_m\) are the wavenumbers and magnetic field dyadic Green's functions in the regions above and below the CPW slots, respectively. The space domain integral eq. (4) is solved numerically using the Method of Moments [33]. In this solution scheme, the equivalent magnetic currents flowing on the slot apertures are expanded into a summation of piecewise sinusoidal basis functions, as shown:

\[
\vec{M}(x', y') = \sum_{i=1}^{N+1} \sum_{n_{i-1} = 0}^{M_{i+1} - 1} [V_{n,m_i}]^T [\phi_{n,m_i}(x', y')] \]

where \(V_{n,m_i}\) is the transposition of the vector of unknown current coefficients, and \(\phi_{n,m_i}(x', y')\) is the vector of the known basis functions. These functions are considered to be separable with respect to \(x'\) and \(y'\) parameters and have the following form:

\[
\phi_{n,m_i}(x', y') = f_{n}(x') g_{m_i}(y')
\]

with

\[
\begin{align*}
f_{n}(x') = \begin{cases} 
\frac{\sin(\xi(0 - x_{n-1})]}{\sin(\xi \delta)} & x_{n-1} \leq x' \leq x_n \\
\frac{\sin[\xi(x_{n-1} - x')]}{\sin(\xi \delta)} & x_n \leq x' \leq x_{n+1} \\
0 & \text{elsewhere}
\end{cases}
\end{align*}
\]

where \(\xi\) is the subsection length and \(\xi\) the wave number in the dielectric. The functions \(f_{n}(y')\) and \(g_{m_i}(y')\) are given by eqs. (9) and (10) with \(x\), \(x'\), \(y\), and \(y'\) replaced by \(x\), \(x'\), \(y\), and \(y'\), respectively.

In view of eqs. (6) and (7), and with the application of Galerkin's method, equation (4) takes the matrix form:

\[
[Y_{m\nu}] [V_{m\nu}] = [I_{nu}]
\]

with \(Y_{m\nu}\) the elements of the admittance matrix, \(I_{nu}\) the elements of the excitation vector, and \(V_{m\nu}\) the amplitude coefficients for the magnetic current expansion functions. The excitation of the CPW structures is provided by ideal current sources appropriately placed on the slot apertures [8,9]. The solution of the matrix eq. (11) results in the evaluation of the equivalent magnetic currents and, consequently, the electric fields in the slots. From the field distribution, the network parameters may be computed by transmission line theory assuming that a single mode (the coplanar mode) is excited along the feeding lines [8,9]. For example, the input impedance of a one port CPW discontinuity can be evaluated from the positions of the minima and maxima of the electric field standing wave in the feeding lines. These minima and maxima positions may be obtained accurately by applying cubic spline fit on the field distribution derived through the method of moments. Such a technique has been successfully used previously, and has shown very good accuracy in characterizing multiport planar discontinuities [8,9,30,34].
evaluation. Issues associated with the accurate evaluation of the Green's function and the complexities introduced by its form in the open and shielded CPW structures will be discussed in detail in following sections. The Green's function included in the integral eq. (5) is the electric vector potential produced by a unit magnetic current source and, as such, satisfies all the appropriate conditions on the boundary surfaces surrounding the volume of interest. Specifically, in open CPW problems, the magnetic field satisfies the radiation condition:

$$\lim_{r \to \infty} \left( \frac{\partial \vec{H}}{\partial r} - jk \vec{H} \right) = 0$$  (12)

while, in the case of shielded CPW, the spatial spectral components of the magnetic field given by eq. (5) satisfy the following equation on the cavity walls:

$$\hat{n}_w \times (\nabla \times \vec{H}_k) = \mathbf{Z}_{sw}^k \cdot \vec{H}_k$$  (13)

where k indicates the order of the spatial spectral field components, $\hat{n}_w$ is the vector normal to the walls toward the interior of the cavity, and $\mathbf{Z}_{sw}^k$ is the surface impedance dyad [35] for the kth spatial spectral component. In the case of perfectly conducting walls this dyad becomes identical to zero, while for resistive walls it becomes complex. The surface impedance spectral dyad is uniquely specified by the boundary conditions of the problem under study, and for this reason is restricted in form. This implies a very limited choice of values which could simulate physically realizable boundaries. Furthermore, there are no values for these spectral dyads, which could accurately simulate free space. Attempts to force radiation in shielded problems by arbitrarily choosing the spectral dyads can lead to quite inaccurate and inconclusive results, specifically with respect to radiation loss for circuit elements and radiation resistance for antenna elements. In the following sections, we discuss issues associated with the Green's function in shielded and open CPW and will also address the approach of forced radiation.

### 2.1. Shielded Coplanar Waveguides

When the CPW structure under study is shielded by a cavity (see Fig. 3), the excited electromagnetic field can be decomposed into a discrete infinite set of spectral solutions, each one satisfying the appropriate boundary conditions on the cavity walls. Similarly, the modified Green's function pertinent to the corresponding boundary value problem is a dyad

$$\mathbf{G}_m = G_x^* \hat{x} \hat{x} + G_{yy}^* \hat{y} \hat{y} + G_{xy}^* \hat{x} \hat{y}$$  (14)

which is defined as

$$\mathbf{G}_m^* = [k_x^2 I + \nabla \nabla] \cdot \mathbf{F}_m^* (\vec{r}/\vec{r}')$$  (15)

Each component of $G_m^*$ is a superposition of infinitely many discrete solutions and, consequently, can be written into the form of a double infinite sum of PG (Pincherle-Goursat) type, as shown below [8,9]

$$G_{xx}^*(\vec{r}/\vec{r}') = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \frac{2e_n}{aL} \frac{1}{k_x^2 + k_y^2} [P_+ + k_x^2 Q_+] \sin(k_x x') \cos(k_y y') \sin(k_x x) \cos(k_y y)$$  (16)

$$G_{yy}^*(\vec{r}/\vec{r}') = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \frac{4}{aL} \frac{k_x k_y}{k_x^2 - k_y^2} \cdot [P_+ - Q_+] \sin(k_x x') \cos(k_y y') \cos(k_x x) \sin(k_y y)$$  (17)

$$G_{xy}^*(\vec{r}/\vec{r}') = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \frac{4}{aL} \frac{k_x k_y}{k_x^2 - k_y^2} \cdot [P_+ - Q_+] \cos(k_x x') \sin(k_y y') \sin(k_x x) \cos(k_y y)$$  (18)
\[ G_{\pm}^m(\hat{r}/\hat{r}') = \sum_{m=0}^{\infty} \sum_{n=0}^{\infty} 2e^{\alpha L} \frac{1}{k_{+}^2 - k_{+}^2} \left[ k_{+}^2 P_{+} + k_{+}^2 Q_{+} \right] \cos(k_{+} x') \sin(k_{+} y') \cos(k_{+} x) \sin(k_{+} y) \] (19)

where

\[ P_{+} = \left( \frac{k_{+}^2 + j \omega \epsilon_{+}}{\omega \mu_{+}} \right) \frac{Z_{SE}^{+} \tan(k_{+} z, d_{+})}{k_{+}^2 - k_{+}^2} \] (20)

\[ Q_{+} = \left( \frac{k_{+}^2 + j \omega \epsilon_{+}}{\omega \mu_{+}} \right) \frac{Z_{SM}^{+} \tan(k_{+} z, d_{+})}{k_{+}^2 - k_{+}^2} \] (21)

The components of \( G_{\pm}^m \) are given by equations similar to eqs. (16)–(27) [8,9].

In the expressions for the modified Green’s function, as given by (16)–(27), the summations over \( m \) and \( n \) are theoretically infinite. For the numerical solution of the integral equation, these summations are truncated, and the number of terms kept depends on the convergence behavior of the admittance matrix. Due to the nature of the problem solved here, the above summations have a convergence behavior similar to summations described elsewhere [34]. In the present work, the number of terms in the summations and the number of basis functions are chosen so that convergence of the scattering parameters of the coplanar waveguide discontinuity is achieved [8,9].

### 2.2. Open Coplanar Waveguides

When the cavity of a shielded CPW is moved to infinite, the environment surrounding the structure becomes open permitting real power to leak to free-space in the form of radiation modes (space waves) or guided modes (surface and leaky waves). From these two types of generated electromagnetic waves, the former have a continuous spectrum, while the latter a discrete one. As a result, the infinite summations in the shielded CPW case, which are characteristic of the Green’s functions and the corresponding excited fields, turn into infinite integrals of Sommerfeld type. In the simplest case of an open CPW printed on a dielectric substrate of thickness \( h \) and with a dielectric constant, \( \epsilon_r \), (see Fig. 1), the components of the magnetic-field dyadic Green’s function, \( \vec{F}_m \), are in the form [36]:

\[
F_{ix} = \frac{1}{j \omega 2 \pi \mu_0} \int_0^{\infty} J_1(\lambda \rho) \frac{\lambda}{u} \sin\left[u(h + z)] + \epsilon \mu_0 \sinh[u(h + z)]\right] f_1(\lambda, \epsilon, h) \, d\lambda
\] (28)

\[
F_{ix} = \text{cot} (\phi) \frac{1}{j \omega 2 \pi \mu_0} \cos(\phi) \int_0^{\infty} J_1(\lambda \rho) \frac{\sinh(uz)}{\lambda^2 f_1(\lambda, \epsilon, h) f_2(\lambda, \epsilon, h)} \, d\lambda.
\] (29)

The functions, \( f_1(\lambda, \epsilon, h) \) and \( f_2(\lambda, \epsilon, h) \), are the characteristic equations for the surface waves, TE
and TM, to the dielectric interface, and are given by:

\[ f_1(\lambda, \epsilon_r, h) = \epsilon_r u_0 \cosh(uh) + u \sinh(uh) \]  
\[ f_2(\lambda, \epsilon_r, h) = u_0 \sinh(uh) + u \cosh(uh) \]  
\[ u_1^2 = \lambda^2 - \omega^2 \mu_0 \epsilon_0 \]  
\[ u^2 = \lambda^2 - \omega^2 \mu_0 \epsilon_0 \epsilon_r. \]  

This formulation allows for a dielectric substrate or half space of any dielectric constant, thus, the components of \( k_n \) can also be obtained from the same equations.

For the solution of eq. (11), most of the computation effort is spent on the evaluation of the elements of the admittance matrix. The complexity in these computations comes from the Sommerfeld integration as it is combined with multiple space integrals. As a result, these integrals are computed using a special treatment, which consists of numerical and analytical techniques as described elsewhere \[36,37\].

2.3. Forced Radiation

There has been an attempt to model radiation loss from printed circuits by setting the resistance of the top wall of the shielding box to 377 \( \Omega \) \[31,32\]. As noted above, such an attempt can lead to quite inaccurate and inconclusive results. In fact, forced radiation simulations may predict a loss factor much larger than the "actual" one, which can only be obtained through a rigorous analysis of the open structure \[32\]. This is due to the fact that there are no values for the surface impedance dyad in eq. (13) which could accurately simulate free-space environment. In the next section, a CPW series stub inside a box with the resistance of the lower and bottom walls set to 377 \( \Omega \) will be analyzed. Radiation loss predicted from such a simulation will be compared to the "actual" radiation loss. In addition, it will be shown that the distance at which these walls are positioned is a critical parameter that affects the derived results considerably.

3. NUMERICAL EXAMPLES

Figure 4 shows the normalized capacitive reactance for an open-end CPW discontinuity of shielded and open type. The results for the two cases are in good agreement, differing only by the amount of power radiated into the substrate and free space. The radiation loss from this one-port discontinuity (Fig. 5) increases with the gap width and the center conductor width. Two series stub geometries are shown in Figure 6, and the magnitude of \( S_{12} \) of both stubs with a mean length of 1.35 mm is given in Figure 7. This
plot indicates that the stub geometry may affect the resonant frequency by as much as 7%. Specifically, the straight stub has a resonance at about 22 GHz, while for the bent geometry the resonance is 1.5 GHz higher. The sharper resonance of the nonshielded bent stub indicates lower radiation loss than the straight stub. As shown in Figure 8, the straight stub experiences severe loss which exceeds 25% of the input power. The parasitic radiation is high in this example because the electric fields in the two-stub slots are in phase, and thus they radiate constructively. In contrast, the electric fields in the bent geometry are 180° out of phase.

Four different CPW shunt stubs are shown in Figure 9, where air-bridges are used to connect the ground planes of the CPW stub in order to prevent the excitation of the coupled slotline mode. A comprehensive theoretical and experimental study of these stubs has been performed [11,38]; however, for illustration purposes, only the measured radiation loss of the open-end stubs will be presented here. Figure 10 shows the measured loss factor of these stubs, which includes radiation, conductor, and dielectric losses. Since the stubs are all of the same length, a comparison of the loss factor can provide a measure of the radiation loss. It can be noticed that loss is maximum at the resonant frequency for all stubs, which agrees with the radiation behavior of microstrip stubs above resonance [30]. Furthermore, the loss factor for straight stubs is larger than that for bent stubs. This is due to the fact that, in the case of bent stubs, the fields radiated by the coupled slotline modes in the two opposing stubs partially cancel. It can be seen also that the air-bridges reduce radiation loss by shorting out the coupled slotline model in the CPW stubs. But, it is still noted that the straight stubs have increasing radiation loss after the first resonant frequency.
Figure 9. Different CPW shunt stubs. (a) Straight open-end CPW stub. (b) Bent open-end CPW stub. (c) Straight short-end CPW stub. (d) Bent short-end CPW stub.

Figure 11 compares the radiation loss of a straight series stub, as predicted by setting the resistance of the top and bottom walls of the rectangular box to 377 $\Omega$, to the “actual” radiation loss. The top and bottom walls are at a distance $D$ from the slot aperture and the lower interface of the dielectric substrate, respectively. In addition, the parameter “$a$” indicates the cavity width. It can be noticed that the parameter $D$ undoubtedly affects the final result. Furthermore, there is no specific $D$ at which one can be sure that the predicted radiation loss is the closest to the actual one. Thus, such a simulation cannot provide any consistent results with respect to the radiation loss in printed circuits or radiation resistance in printed antennas. Nonetheless, such a simulation can still predict the resonant frequency of the circuit or antenna element.

Figure 10. The measured loss factor $(1 - |S_{11}|^2 - |S_{21}|^2)$ of the open-end shunt stubs (a) without air-bridges and (b) with air-bridges. $S = 75 \mu m$, $W = 50 \mu m$, $h = 400 \mu m$, $\varepsilon_r = 13$, mean stub length = 1100 $\mu m$; the slots and center conductor of the stubs have equal widths of 25 $\mu m$.

4. CONCLUSIONS

A comparative study between open and shielded CPW discontinuities has been presented. In this study, the space domain integral equation method was used to characterize several discontinuities such as the open-end CPW and CPW series stubs. It has been found that bent CPW stubs tend to radiate less than straight ones, which makes them more appropriate for use in microwave circuits. The notion of “forced radiation” simulation has been presented in which an open structure is simulated by setting the resistances of the top and bottom walls of the shielding box to 377 $\Omega$. The results of such a simulation have been compared.
to the “actual” radiation loss obtained rigorously. It has been found that these results are not reliable since they are considerably affected by the size of the cavity.

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BIOGRAPHY

Nihad Dib received the BSc and MSc degrees in Electrical Engineering from Kuwait University in 1985 and 1987, respectively. He worked as a Laboratory Engineer in the ECE Department at Kuwait University for two years. He has been with the Radiation Laboratory, University of Michigan, since September of 1988, where he is currently working toward his PhD degree. He is a recipient of a predoctoral Rackham Fellowship, University of Michigan, during the 1991–92 academic year. His research deals mainly with the construction of CAD programs for the analysis of coplanar waveguide structures.

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A Theoretical and Experimental Study of Coplanar Waveguide Shunt Stubs

Nihad I. Dib, Member, IEEE, George E. Ponchak, Member, IEEE, and Linda P. B. Katehi, Senior Member, IEEE

Abstract—A comprehensive theoretical and experimental study of straight and bent coplanar waveguide (CPW) shunt stubs is presented. In the theoretical analysis, the CPW is assumed to be inside a cavity, while, the experiments are performed on open structures. For the analysis of CPW discontinuities with air-bridges, a hybrid technique has been developed which has been validated through extensive theoretical and experimental comparisons. Throughout this study, the effect of the cavity resonances on the behavior of the stubs with and without air-bridges is investigated. In addition, the encountered radiation loss due to the discontinuities is evaluated experimentally.

I. INTRODUCTION

COPLANAR WAVEGUIDE (CPW) is rapidly becoming the transmission line of choice in high frequency applications and is successfully competing against the microstrip which has been the primary structure for hybrid and monolithic circuits. Due to many years of microstrip use, a large body of published data and CAD software pertaining to low- and high-frequency microstrip circuit and antenna design has been widely available. On the contrary, models for shielded or open coplanar waveguide circuit design are still under development [1]–[22]. Nevertheless, despite this scarcity of reliable circuit models, CPW has provided an attractive alternative to conventional microstrip lines at high frequencies due to many appealing properties [23]–[31].

While there is no need for via holes in CPW circuits, air-bridges are fundamental components required to connect the ground planes for suppression of the coupled slotline mode. In the past few years, there has been several attempts to characterize, theoretically and/or experimentally, CPW discontinuities with air-bridges or bond wires [16]–[22]. The full wave computationally intensive Finite Difference Time Domain technique was used in [17], [21] to analyze a CPW shunt stub with bond wires and a modified CPW air-bridge T-junction. On the other hand, the Finite Difference Frequency Domain method was used in [22] to treat two common types of CPW air-bridges where it was found that the reflection coefficient (or \( S_{11} \)) varies linearly with frequency. This fact suggests that a typical air-bridge can be modeled as a frequency dependent lumped element [16], [18], [19], [28], [32]. With this in mind, a hybrid technique has been developed to analyze CPW discontinuities with air-bridges. In this technique, the frequency dependent equivalent circuit of the discontinuity, with the air-bridges removed, is derived using the Space Domain Integral Equation (SDIE) method [8], [9]. Then, this equivalent circuit is modified by incorporating the air-bridge parasitic inductance and capacitance which are evaluated using a quasistatic model.

In this paper, the above mentioned hybrid technique is used to study a variety of CPW shunt stub geometries (Fig. 2) and the validity of the model is verified by performing extensive measurements. The scattering parameters of the stubs with and without air-bridges are presented and a very good agreement is found between theoretical and experimental data. In addition, since a shielded structure is assumed in the formulation of the theory, the effect of cavity resonances on the behavior of these stubs is shown. Moreover, the encountered radiation loss in open discontinuities is investigated experimentally.

II. THEORY

In the theoretical analysis, the CPW under consideration is assumed to be shielded by a rectangular cavity with perfectly conducting walls as shown in Fig. 1. As pointed out in the introduction, a hybrid technique is used to analyze coplanar waveguide discontinuities with air-bridges. First, the frequency dependent equivalent circuit of the discontinuity, with the air-bridges removed, is derived using the Space Domain Integral Equation (SDIE) method [8], [9]. Then, this equivalent circuit is modified by incorporating the parasitic reactances introduced by the air-bridges. Only the main steps of the SDIE method are given here, since the details can be found in [8], [9].

The integral equation which is formulated here in terms of equivalent magnetic currents flowing on the slot apertures is different from the fullwave technique presented in [1], [5], [14], where an integral equation in terms of the electric current on the conducting surfaces is formed. The former technique is more appropriate for CPW problems where the ground planes approach the boundary surfaces (open or shielded), while the latter better fits problems with finite size ground conductors.

The integral equation (1) is solved using the Method of Moments [33] where the unknown magnetic current is expanded in terms of rooftop basis functions. Then, Galerkin’s method is applied to reduce the above equation to a linear system of equations

\[
\begin{pmatrix}
Y_{yy} & Y_{yz} \\
Y_{zy} & Y_{zz}
\end{pmatrix}
\begin{pmatrix}
V_y \\
V_z
\end{pmatrix} = \begin{pmatrix}
I_x \\
I_y
\end{pmatrix}.
\]

In the above, \(Y_{ij}\) represent blocks of the admittance matrix, \(V_i\) is the vector of unknown \(y\) and \(z\) magnetic current amplitudes, and \(I_j\) is the excitation vector which is identically zero everywhere except at the position of the sources. The solution of the matrix equation (2) results in the evaluation of the equivalent magnetic currents and consequently the electric fields on the slots.

In case of isolated CPW structures which are symmetric with respect to the center line, the coupled slotline mode is not excited, and hence, the aperture fields in the feeding lines form standing waves of the fundamental coplanar waveguide mode. Consequently, using the derived electric field, transmission line theory can be utilized to determine the scattering parameters and derive a lumped element equivalent circuit for the discontinuity. In case of asymmetric CPW discontinuities, the derived field in the feeding lines is the sum of the fundamental coplanar and slotline modes each one having its own spatial parameters, and consequently, a special treatment is needed to separate the two modes and derive the scattering parameters of the discontinuity [35].

B. Modeling the Air-Bridges

Fig. 3(a) shows the equivalent circuit (\(\pi\)-model) for the CPW discontinuities shown in Fig. 2 with the air-bridges removed. \(X_1\) and \(X_2\) represent the reactances due to the coplanar waveguide mode excited in the CPW stub, while \(X_3\) is due to the coupled slotline mode [34]. The reference planes at which these reactances are evaluated are at the ends of the uniform feeding lines. It should be noted that in the case of straight stubs, the two reactances \(X_1\) and \(X_2\) are equal due to the symmetry of the circuit. Thus, only two independent excitations are needed to evaluate the elements of the equivalent circuit, as opposed to three required in the case of the bent stubs \((X_1 \neq X_2)\) [9].

Fig. 3(b) shows the new equivalent circuit after taking the air-bridges into consideration. The air-bridges can be modeled as sections of an air-filled microstrip line [16], [28], and simple formulas can be used to evaluate the parasitic capacitance of the air-bridges.
$C_A$ and inductance $L_a$ [34]. Alternatively, a parallel plate waveguide model can be employed to evaluate the same parasitic effects. It has been found that the difference in the values of the parasitic reactances as predicted by the two models has a negligible effect on the performance of the circuit. Finally, new scattering parameters are evaluated from the modified equivalent circuit. It should be emphasized that such a hybrid technique assumes that the air-bridges are positioned as close to the cross junction as possible, which is always the case in practice. Moreover, it is worth mentioning that the CPU time required for the evaluation of the scattering parameters (taking into account all the existing physical symmetries) ranges from one to three minutes for each frequency on Apollo Domain 10000.

III. RESULTS AND DISCUSSION

In the numerical results shown here, the considered CPW discontinuities are suspended inside a rectangular cavity, as shown in Fig. 1, with $h = 400 \mu m$, $\epsilon_{r1} = 13$, $\epsilon_{r2} = 1$, $S = 75 \mu m$, $W = 50 \mu m$, and $h_1 = h_2 = 1.2 \ mm$. The characteristic impedance of such a line is approximately $50 \Omega$. On the other hand, the slots and center conductor of the CPW stubs have equal widths of $25 \mu m$. In addition, in the case of the open-end stubs, the width of the open-end is $25 \mu m$. In all examples presented here, the stubs are placed symmetrically at the center of the cavity with length approximately equal to $3\lambda_0$.

The experiments were performed in an open environment with the CPW circuits fabricated on $400 \mu m$ thick GaAs using lift-off processing. The CPW center strip and ground planes consist of 200 $\mu$m of Cr and 1.5 $\mu$m of Au. The air-bridges have $10 \mu m$ square posts and are $14 \mu m$ wide. The air-bridge thickness and height are $1.0 \mu m$ and $3.0 \mu m$, respectively. The GaAs circuit rests on a piece of 3.175 mm 5880 RT/duroid which has a dielectric constant of 2.2.

It will be shown that the theoretical and experimental data agree despite the difference in $\epsilon_{r2}$ of the substrate ($\epsilon_{r2} = 1$ versus 2.2). This is due to the relatively large thickness of the GaAs substrate layer as compared to $S + 2W$. The choice of $\epsilon_{r2} = 1$ in the theoretical calculations is intended in order to avoid some of the unwanted cavity resonances.

The circuits were tested with an HP 8510 network analyzer and a Cascade probe station. The calibration standards for a TRL calibration were fabricated on the wafer to allow calibration to the reference planes of the CPW stubs. To cover the 5–40 GHz bandwidth, three delay lines were used. The probe positioning on the wafer was determined to be repeatable to within $3 \mu m$ which creates a maximum error in the phase of $S_{21}$ of 0.76° at 40 GHz.

A. Open-End Shunt Stubs

Fig. 4 shows the magnitude of the scattering parameters of the straight open-end stub (Fig. 2(a)) of length $L = 1100 \mu m$ with the air-bridges removed as a function of frequency. It is noticed that the theoretical and experimental results agree very well up to the first resonance, after which, discrepancy is noticeable. This is attributed to the fact that no loss is assumed in the theoretical formulation, while, experiments were performed on CPW structures in an open environment. The loss encountered in the measurements is mainly due to radiation by the slotline mode excited in the CPW stubs in the absence of the air-bridges. To understand the unexpected behavior seen between 41 and 45 GHz, the reactances $X_1$ and $X_3$ of the equivalent circuit are plotted in Fig. 5. It can be seen that $X_1$, which corresponds to the coplanar mode in the CPW stub, behaves as a real open-end shunt stub. On the other hand, $X_3$, which is due to the slotline mode in the CPW stubs, behaves somewhat anomalously between 41
and 45 GHz. It is found that this behavior is due to a cavity resonance at 43 GHz which corresponds to the \( L S M_{121} \) mode excited in the partially filled lower cavity (the cavity width was chosen to be 3.425 mm). It is interesting to note that the \( L S M_{111} \) cavity mode, which has a resonant frequency of 38 GHz, does not show an observable effect on the stub under consideration. Also, the shunt reactances seem to be unaffected by the \( L S M_{121} \) cavity mode.

Fig. 6 shows the scattering parameters (magnitude and phase) of the same straight open-end stub with air-bridges. The good agreement between the theoretical and experimental results validates the developed hybrid technique. As it can be seen, the stub resonates at nearly 24.5 GHz where the length of the stub is approximately quarter of a coplanar mode wavelength. It can be noticed that the agreement between the theoretical and experimental data in Fig. 6(a) is much better than the one seen in Fig. 4. This is due to the fact that the air-bridges tend to prevent the slotline mode from being excited in the CPW stubs which effectively reduces radiation losses encountered in the measurements. In addition, it can be seen that the resonance effect noticed in Fig. 4 has disappeared since \( X_3 \) is shorted by the relatively small air-bridge inductance \( L_a \).

As a result, with the presence of air-bridges, cavity resonances have no effect on the characteristics of a straight stub as long as it is placed symmetrically inside the cavity. One can also notice an anomalous effect at 40 GHz existing in Fig. 6. A similar effect has been found in [17] for the case of a bent open-end stub. This effect may be due to a resonating slotline mode excited in the stubs beyond the air-bridge.

Fig. 7 shows the magnitude of the scattering parameters for the bent open-end CPW stub (Fig. 2(b)) of mean length \( L = 1100 \mu m \) without air-bridges. In this case, the width of the cavity is taken to be 2 mm. It can be seen that the agreement between theory and experiment is better than that seen in Fig. 4 for the straight stub without air-bridges. Moreover, it has been found that the parallel combination of \( X_1 \) and \( X_2 \) behaves as expected for a real shunt open-end stub (i.e. similar to the variation of \( X_1 \) in Fig. 5). Fig. 8 shows the magnitude of the scattering parameters of the same bent open-end stub with air-bridges. It can be seen that the anomalous effect at 40 GHz is more pronounced in this case than that in Fig. 6. In addition, the resonant frequency of this bent stub with air-bridges is approximately the same as the one for the straight stub of the same mean length.

**B. Short-End Shunt Stubs**

Figs. 9 and 10 show \( Mag(S_{11}) \) for the straight and bent short-end CPW stubs, respectively, of mean length \( L = 1100 \mu m \) with and without air-bridges. It can be noticed that both stubs resonate at approximately 25.5 GHz. The same arguments presented above for the open-end stub hold here too.
It is interesting to note that for all structures containing air-bridges, the measured resonant frequency is larger than the theoretically predicted one. This systematic deviation may be due to the effect of finite metallization thickness (1.5 µm) which is neglected in the theoretical analysis. The finite metallization thickness reduces the phase constant [36] and thus increases the stub resonant frequency. EESof Touchstone has predicted an increase of approximately 1.2% in the resonant frequency of a section of CPW of length 1100 µm due to the finite conductor thickness.

Since the experiments were performed on open CPW discontinuities, the measured scattering parameters can provide the loss factor. This loss factor includes radiation, conductor and dielectric losses. However, since the stubs are all of the same length and printed on the same substrate, a comparison of the loss factor can provide a measure of the radiation loss. Figs. 11(a) and 12(a) show the loss factor of the short-end and open-end stubs without air-bridges, respectively. It is noticed that loss is maximum at the resonant frequency for all stubs, which is similar to what has been found in microstrip stubs [37]. Furthermore, the loss factor for straight stubs is larger than that for bent stubs especially after resonance. This behavior is due to the fact that in the case of bent stubs, the fields radiated by the coupled slotline mode in the two opposing stubs...
Fig. 11. The measured loss factor \((1 - |S_{11}|^2 - |S_{12}|^2)\) of the short-end CPW stubs. (a) Without air-bridges. (b) With air-bridges.

Fig. 12. The measured loss factor of the open-end CPW stubs. (a) Without air-bridges. (b) With air-bridges.

partially cancel. This explains why the agreement between the theoretical and experimental results for the bent stubs without air-bridges (Fig. 7 and Fig. 10) is better than that for the straight stubs without air-bridges (Figs. 4 and 9). The loss factor for the stubs with air-bridges is shown in Figs. 11(b) and 12(b). It can be seen that the presence of air-bridges reduces the loss factor appreciably since they short out the radiating coupled slotline mode. However, it is still noted that the straight stubs have increasing radiation loss after the first resonant frequency. Finally, it can be noticed that the difference between the loss factor of the straight and bent stubs (with or without air-bridges) below the resonant frequency is within the experimental error. Thus, no concluding remarks can be made concerning the loss from the two stubs in this region.

IV. CONCLUSIONS

A comprehensive theoretical and experimental study of CPW shunt stubs has been presented. In the theoretical analysis, the CPW was assumed to be inside a cavity, while the experiments were performed in an open environment. A hybrid technique has been developed to analyze the CPW discontinuities which proved valid since the results obtained theoretically and experimentally agreed very well. It was found that bent stubs without air-bridges tend to radiate less than straight stubs of the same length. In addition, the effect of the cavity resonances on the behavior of the stubs has been studied. It has been shown through experiments that bent CPW stubs should be used whenever the circuit layout permits.

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A coplanar waveguide radial line stub resonator is experimentally characterized with respect to stub radius, sectoral angle, substrate thickness and relative dielectric constant. A simple closed-form design equation, which predicts the resonance radius of the stub, is presented.

Introduction: Coplanar waveguide (CPW) technology is emerging as a viable alternative to stripline and microstrip for monolithic microwave integrated circuits [1]. There are several applications in which a CPW radial line stub resonator is necessary; these include: bias line filters requiring a point of virtual RF ground, mixer and frequency multiplier circuits that require a reactance to terminate the diodes and the harmonics, respectively. In addition, a grounded CPW radial line stub resonator is experimentally characterised with respect to stub radius, sectoral angle, substrate thickness and relative dielectric constant. A simple closed-form design equation, which predicts the resonance radius of the stub, is presented.

Experimental results and closed-form equation: The measured return loss and insertion loss of a CPW radial line stub are compared with those of a straight CPW stub in Fig. 2. In this experiment θ and R2 for the radial stub are arbitrarily chosen as 60° and 5.08 mm, respectively. The length L of the straight stub is 7 mm. The measurements show that for identical εr and resonance frequency f0, the radius R2 is 37% smaller than the length L. Further, the radial line stub has a wider bandwidth. The bandwidth of the two structures as a function of the attenuation is compared in Table 1. The excess loss defined as 1 - |S11|^2 - |S21|^2, and determined from the measured S parameters, is small. It is of the order of 0.09 and 0.05 for the radial line stub and straight stub, respectively.

A GCPW radial line stub with εr = 2.2, D = 0.254 mm and θ and R2 the same as for the CPW radial line stub, has a much wider bandwidth. The characteristics for the GCPW radial line stub are also included in Table 1. The excess loss is of the order of 0.04.

Table 1 PERCENTAGE BANDWIDTH OF STRAIGHT AND RADIAL LINE STUB

<table>
<thead>
<tr>
<th>Attenuation (dB)</th>
<th>Straight</th>
<th>CPW radial</th>
<th>GCPW radial</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>18.3</td>
<td>25.7</td>
<td>58.1</td>
</tr>
<tr>
<td>20</td>
<td>5.6</td>
<td>8.0</td>
<td>15.8</td>
</tr>
<tr>
<td>30</td>
<td>1.6</td>
<td>2.5</td>
<td>3.5</td>
</tr>
</tbody>
</table>

For a CPW radial line stub, the measured f0, as a function of θ for a fixed R2 is shown in Fig. 3. The f0 decreases by 20% as θ increases from 30 to 90°. It is also worth noting that R1 does not remain constant but increases with θ. The excess loss is small and decreases from 0.12 to 0.06 as θ increases from 30 to 90°.
Fig. 4 Measured resonance frequency against outer radius of radial stub for θ = 60°

(i) GCPW:
- (a) S = 0.518 mm, W = 0.127 mm, D = 0.254 mm, εr = 2.2, R1 = 0.3 mm
- (b) S = 0.33 mm, W = 0.234 mm, D = 0.635 mm, εr = 10.5, R1 = 0.191 mm
- (c) S = 0.33 mm, W = 0.185 mm, D = 0.254 mm, εr = 10.5

(ii) CPW:
- (d) S = 0.33 mm, W = 0.234 mm, D = 0.635 mm, εr = 6, R1 = 0.3 mm
- (e) S = 0.152 mm, W = 0.114 mm, D = 0.381 mm, εr = 11.7, R1 = 0.092 mm

Fig. 4 shows the product of √(εr) and measured f0 as a function of R2 for CPW and GCPW radial line stubs. By curve fitting the measured data, the coefficients of a simple closed-form equation to predict R2 are determined using a sigma plot. The equations for CPW and GCPW are as follows:

\[
\log(R_2) = C_1 \log[\sqrt{\varepsilon_r} f_0] \\
+ C_2 \log(D) + C_3 \log(R_1) + C_4 \\
\log(R_2) = C_5 \log[\sqrt{\varepsilon_r} f_0] \\
+ C_6[\log(D) + \log(R_1)]
\]

where f0 is in gigahertz, R1, R2, and D are in metres. The coefficients were determined to be: C1 = -1.0496, C2 = 0.098375, C3 = -0.1401, C4 = -1.297, C5 = -0.82462 and C6 = 0.21201, respectively. These equations are valid for the geometry and the range of parameters given in Fig. 4. The range of parameters considered are those typically used in microwave circuit design. The standard error of the equation is at most 0.18 and 0.01% for the CPW and GCPW, respectively.

Conclusions: A CPW radial line stub resonator is experimentally characterised in terms of its radius, sectoral angle, substrate thickness and relative dielectric constant. A simple closed-form design equation which predicts the resonance radius of the stub for a given set of parameters is also presented. The radial line stub, when compared to a straight stub, has a wider bandwidth and shorter length.

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ATTENUATION AND $\varepsilon_{\text{eff}}$ OF COPLANAR WAVEGUIDE TRANSMISSION LINES ON SILICON SUBSTRATES

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Abstract

Attenuation and $\varepsilon_{\text{eff}}$ of Coplanar Waveguide (CPW) transmission lines have been measured on Silicon substrates with resistivities ranging from 400 to greater than 30,000 ohm-cm, that have a 1000 angstrom coating of SiO$_2$. Both attenuation and $\varepsilon_{\text{eff}}$ are given over the frequency range 5 to 40 GHz for various strip and slot widths. These measured values are also compared to the theoretical values.

Introduction

Historically, Silicon has not been the material of choice for microwave applications because of its extremely high loss and its lack of high frequency active devices. Recently, however, high frequency Silicon devices have become available. In addition, Silicon Germanium (SiGe) shows great promise for high frequency Silicon based devices [1].

Theoretical work has been done in calculating the attenuation of microstrip lines on Silicon as a function of resistivity and frequency [2]. There has also been some work on Coplanar Waveguide (CPW) lines on Silicon on Insulator (SOI) [3] as a function of resistivity. This paper presents both measured and theoretical attenuation and $\varepsilon_{\text{eff}}$ data of CPW lines on Silicon as a function of resistivity, strip and slot width and frequency.

Results

Groups of CPW lines were fabricated on five different Silicon wafers. The wafers were 8 mils thick and had resistivities of 400-720 ohm-cm, 2500-3300 ohm-cm, 5000-10,000 ohm-cm, and greater than 30,000 ohm-cm. A 1000 angstrom layer of SiO$_2$ was deposited on the wafers, followed by a 2.5µm thick Au layer. The CPW lines were fabricated using etch back. Each group of CPW lines consisted of on open, thru, and four delay lines with a different strip width ($s$) and slot width ($w$) for each group. The $s$ and $w$ of each of the groups were: $s=2 \ w=1$, $s=4 \ w=2$, and $s=6 \ w=3$. The impedance of these lines was approximately 50 ohms. The CPW lines were on wafer probed using PicoProbes and an HP8510 Automatic Network Analyzer. The data from each group was analyzed using NIST's DEEMBED software to obtain values for the attenuation and $\varepsilon_{\text{eff}}$.

Figure 1 shows the measured attenuation of a CPW line with $s=4 \ w=2$ on Silicon substrates of varying resistivities. As the resistivity of the material increases, the attenuation decreases. This is attributed to the reduction of dielectric loss. Loss also increases with frequency, due to an increase in the effective length of the line. Note that for substrates of medium resistivity (400-720 ohm-cm), the loss is twice that of those with resistivities greater than 2,500 ohm-cm. However, the improvement in attenuation for substrates with resistivities greater than 2,500 ohm-cm is small.

Figure 2 shows the attenuation of CPW lines on a Silicon wafer with resistivity of 2,500-3,300 ohm-cm as a function of $s$ and $w$. Measured and theoretical curves are shown.

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The theoretical curves were given by Gupta [4]. As was predicted by the theory, the loss of the CPW lines decrease with increasing s and w; however, the measured values of attenuation are slightly lower than the theory predicts.

$\varepsilon_{\text{eff}}$ is not a function of resistivity but of s and w. Figure 3 shows theoretical and measured values for $\varepsilon_{\text{eff}}$ of CPW lines with $s=6$ $w=3$. The theoretical values were again given by Gupta [4]. The value of $\varepsilon_{\text{eff}}$ is virtually independent of resistivity and closely matches the theoretical value.

Conclusions

Both measured and theoretical values for attenuation and $\varepsilon_{\text{eff}}$ for CPW lines on Silicon wafers were shown as a function of resistivity, strip and slot width and frequency. Losses for CPW lines on Silicon can be minimized if the resistivity of the wafer is kept above 2,500 ohm-cm. Thus making Silicon a viable microwave material.

Acknowledgment

The authors would like to thank Dr. Roger Marks of NIST for his help with the software and Dr. Rainee Simons for his support during this project.

References

Figure 1: Measured attenuation of CPW lines on Silicon substrates with resistivities: a) 400-720 ohm-cm  b) 2500-3300 ohm-cm  c) 5000 ohm-cm  d) >30,000 ohm-cm

Figure 2: Measured and theoretical attenuation of CPW lines on a Silicon substrate, resistivity= 2500-3300 ohm-cm: a) s=2, w=1  b) s=4, w=2  c) s=6, w=3
Figure 3: $\varepsilon_{\text{eff}}$ of CPW lines on Silicon substrates, $s=6$ $w=3$, with resistivities: a) 400-720 ohm-cm  b) 2500-3300 ohm-cm  c) 5000 ohm-cm  d) $>30,000$ ohm-cm  e) theory
NOVEL COPLANAR WAVEGUIDE TO SLOTLINE TRANSITION ON HIGH RESISTIVITY SILICON

R. N. Simons, S. R. Taub and P. G. Young

Indexing terms: Coplanar waveguide, High resistivity silicon

Two novel coplanar waveguide (CPW) to slotline transitions have been fabricated and tested on high resistivity silicon. The first transition uses an air bridge to couple RF power from the CPW line to the slotline and has the entire circuit on the top side of the wafer. In the second transition, the grounded CPW (GCPW) line and the slotline are on opposite sides of the wafer and are coupled electromagnetically. The measured average insertion loss and return loss per transition are better than 1.5 and 10 dB, respectively, with a bandwidth greater than 30% at C-band frequencies.

Introduction: Recently, Si$_x$Ge$_{1-x}$-on-silicon devices have emerged as a viable alternative to GaAs- and InP-based heterostructure devices [1]. It appears that this material technology will be suitable for monolithic microwave integrated circuits (MMICs) for a number of reasons, some of which are the following: The technology is compatible with existing silicon technology which is extensively used for digital circuits and the low cost of silicon wafers. The active devices such as transistors and diodes are fabricated on the heterostructure substrate. By choosing a silicon substrate with sufficiently high resistivity it is possible to make the dielectric attenuation constant of the interconnecting microwave transmission lines approach those of GaAs [2]. For this to be possible, the transmission line interconnects must be characterised on silicon.

This Letter presents two new CPW to slotline transitions fabricated on high resistivity silicon substrates. A transition between a coplanar waveguide (CPW) and a slotline on a high resistivity silicon substrate has several applications. These include: facilitating fast and inexpensive testing of CPW and slotline MMICs using on-wafer RF probes, functioning as a balun in mixer circuits, and providing interconnection between CPW MMIC phase shifters or amplifiers and linearly tapered slot antennas in phased arrays. In the past, several investigators have worked on conventional CPW to slotline transitions on alumina and GaAs substrates [3, 4]. In these transitions the CPW line and the slotlines are orthogonal to each other.

Transition design and fabrication: The first transition presented in this Letter uses an air bridge to couple RF power from the CPW line to the slotline and has the entire circuit on the same side of the wafer. In the second transition, the grounded CPW (GCPW) line and the slotline are on opposite sides of the wafer and are coupled electromagnetically. In both cases these circuits, the CPW line and the slotline are collinear. Both transitions are fabricated on a single 5000-10 000 cm² resistivity silicon wafer. The thickness of the wafer is 0.381 mm with $\varepsilon_r = 11.7$. The thickness $T$ of the gold metallisation is about three times the skin depth at the centre frequency $f_0$ of 6 GHz.

(a) Air-bridge coupled CPW to slotline transition: An air-bridge coupled CPW to slotline transition is illustrated in Fig. 1. At the input port the characteristic impedance $Z_0$, is 50 $\Omega$ for compatibility with on-wafer RF testing. The line transforms to a 60 $\Omega$ line that terminates in an open circuit. The $Z_0$ of the slotline is 60 $\Omega$. The circular bend at the feed end of the slotline provides a smooth transition. A 1 mil diameter bond wire between the open end of the CPW centre strip conductor and the opposite edge of the slotline functions as an air bridge and couples RF energy. The length $L_m$ is $\approx \frac{\lambda_{microstrip}}{4}$ at $f_0$.

(b) Electromagnetically coupled GCPW to slotline transition: Fig. 2 shows a transition with electromagnetic coupling between a GCPW and a slotline which are on opposite sides of a wafer. At the input port $Z_0$ is 50 $\Omega$, and in the centre region $Z_0$ is 60 $\Omega$. This is realised by gradually flaring the GCPW slots. At the open end the top ground planes are terminated in two open circuited stubs of length $L_s$. Owing to the lack of CPW discontinuity models, these stubs are modelled as microstrip lines of very low $Z_0$ ($\approx 10 \Omega$) and length about $\frac{\lambda_{microstrip}}{4}$. They provide a virtual short circuit between the top ground planes of the GCPW and the slotline. In addition, the GCPW has a finite ground plane of width $G$ to suppress the parallel plate waveguide mode [5]. The $Z_0$ of the slotline is 60 $\Omega$. Once again, owing to a lack of CPW discontinuity models, the centre strip conductor of the GCPW which extends beyond the terminated ground planes of the GCPW to form the transition is modelled as a microstrip line. The distances $L_m$ and $L_s$ are $\approx \frac{\lambda_{slotline}}{4}$ and $\frac{\lambda_{microstrip}}{4}$, respectively, at $f_0$.

Transition performance and discussions: During testing, the circuits were suspended 10 mm above the probe station stage. The insertion loss and return loss were measured using Cascade Microtech on-wafer probes. For two back-to-back air-bridge coupled CPW to slotline transitions, with a short length of slotline in between, the measured characteristics are shown in Fig. 3. The insertion loss and return loss per transition are $\approx 1.5$ dB, and better than 10 dB, respectively, over greater than 30% bandwidth centred at $f_0$. The above insertion loss includes the insertion loss of the two air bridges and the following which were not practical to calibrate out: the 19.8 mm length of slotline between the transitions, and two
5.08 mm long CPW lines located at the input and output ports. Fig. 4 shows the measured insertion loss and return loss, respectively, for the electromagnetically coupled GCPW to slotline transitions with a short length of slotline in between. The insertion loss and return loss per transition are ~1.5 dB, and better than 10 dB, respectively, over greater than 40% bandwidth centred at 4.55 GHz. The above insertion loss includes the insertion loss of the two junctions and the following which were not practical to calibrate out: the

18.7 mm length of slotline between the transitions, and two 5.08 mm long GCPW lines at the input and output ports. The return loss of this transition is observed to be better than the previous design because of better impedance match between the strip and the slot. However, the shift in the centre frequency from 6 to 4.55 GHz is caused by discontinuity effects which were not fully accounted for in the design.

Conclusions: Two novel CPW to slotline transitions on high resistivity silicon substrates have been experimentally demonstrated. The transitions are fabricated either on the same side or on opposite sides of a wafer and use an air bridge or electromagnetic coupling, respectively, to couple power. The measurements show that the transitions have good insertion loss, return loss and bandwidth characteristics.

2nd October 1992

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References
MICROWAVE CHARACTERIZATION OF SLOTLINE ON HIGH RESISTIVITY SILICON FOR ANTENNA FEED NETWORK

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ABSTRACT

This paper presents the effective dielectric constant ($\varepsilon_{\text{eff}}$) and attenuation constant ($\alpha$) of a unshielded slotline on a high resistivity (5000 to 10,000 $\Omega$-cm) silicon wafer. The $\varepsilon_{\text{eff}}$ (DC to 40 GHz) and $\alpha$ (DC to 26.5 GHz) are determined from the measured resonant frequencies and the corresponding insertion loss of a slotline ring resonator. The measurements are carried out at room temperature and without the application of a DC bias. The attenuation for slotline on silicon are compared with microstrip line and coplanar waveguide on other semiconductor substrate materials. Finally, applications of the slotline to antenna feed network are addressed.

I. INTRODUCTION

There are several reasons why silicon is now a viable microwave material. One reason is that silicon MOSFET's with cutoff frequencies as high as 89 GHz have been reported (ref.1). Another, is that silicon MMIC amplifiers, mixers and IMPATT diodes are now commercially available (refs. 2 thru 4). The final reason is that transmission lines, such as, microstrip line (refs. 5 thru 9) and Coplanar Waveguide (CPW) (ref. 10) with low loss have been demonstrated on high resistivity silicon. Silicon has several advantages over GaAs and InP technologies, such as: better thermal conductivity, higher reliability, higher circuit complexity, availability of wafers of very large diameters, better mechanical properties, and lower cost (ref. 9). Furthermore, integration of MMIC's with digital control circuits and radiating elements on a single silicon wafer is possible. This can enhance the reliability, efficiency and lower the cost of phased array antenna systems. However, silicon substrates do have slightly higher dielectric loss than traditional microwave substrates. DC bias and high operating temperatures can increase this loss. Additional loss can be introduced, if during processing, the wafers are exposed to temperatures high enough to significantly lower their resistivity (ref. 9).

Conventional silicon wafers have low resistivity and consequently an unacceptably high value of dielectric attenuation. Therefore, microwave circuits for phased array antenna systems fabricated on these wafers have low efficiency. By choosing a silicon substrate with sufficiently high resistivity it is possible to make the dielectric attenuation of the interconnecting microwave transmission lines approach those of GaAs or InP (refs. 6 and 7).
In order to fabricate microwave circuits on silicon, the transmission lines on this material must be characterized. Recently, the attenuation of microstrip transmission lines on high resistivity, bare and passivated silicon as a function of frequency, temperature and DC bias have been measured (ref. 9). Also, attenuation and $\varepsilon_{\text{eff}}$ of CPW lines as a function of resistivity, frequency and geometry on silicon substrates has been examined experimentally and theoretically (ref. 10). This paper presents the effective dielectric constant ($\varepsilon_{\text{eff}}$) and attenuation constant ($\alpha$) of an unshielded slotline on a high resistivity (5000 to 10,000 $\Omega$-cm) silicon wafer over the frequency ranges DC to 40 GHz and DC to 26.5 GHz respectively. The measurements are carried out at room temperature and without the application of a DC bias.

II. THEORY

An experimental slotline ring resonator is shown in figure 1. The advantage of a ring resonator over a series gap coupled linear resonator is that the ring resonator is free of end effects. The loaded Q-factor, $Q_L$, of the resonator is determined from the following equation relating the measured resonance frequency, $f_0$, and the frequency range, $\Delta f$, between the 3-dB points on either side of the resonance:

$$Q_L = \frac{f_0}{\Delta f}.$$  

The unloaded Q-factor, $Q_u$, of the resonator is determined from the following equation relating the measured peak insertion loss, $L$, at resonance and $Q_L$:

$$L \text{ (dB)} = 20 \log \left(1 - \frac{Q_L}{Q_u}\right).$$  

The $\varepsilon_{\text{eff}}$ is determined from the following equation:

$$\varepsilon_{\text{eff}} = \left(30 \frac{n}{f_0} \frac{1}{l}\right)^2$$  

Where $n$ is an integer and denotes the order of resonance. Therefore for $n$ resonances of a particular resonator, $n$ values of $\varepsilon_{\text{eff}}$ can be obtained. $l$ is the mean circumference of the ring in cm. $f_0$ is in GHz.

The phase velocity, $v_{\text{ph}}$, of the electromagnetic wave on the slotline is equal to

$$v_{\text{ph}} = 3 \times 10^8 \sqrt{\varepsilon_{\text{eff}}} \text{ (mt/sec).}$$  

Finally, the attenuation constant $\alpha$ of the slotline is determined from the relation:

$$\alpha = \pi \frac{f_0}{Q_u} v_{\text{ph}} \text{ (Np/mt).}$$  

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III. RESONATOR FABRICATION AND EXPERIMENTAL RESULTS

The slotline ring resonator is fabricated on a silicon wafer which is coated sequentially with 700 Å of silicon dioxide, 200 Å of chromium and 2.5 μm of gold. The thickness, T, of the gold metalization is greater than three times the skin depth at 8.5 GHz and above. The measured resistivity of the silicon dioxide layer is $10^{14}$ Ω·cm. The $\varepsilon_{\text{eff}}$ and $\alpha$ are determined by substituting the measured resonant frequencies and the corresponding insertion loss in equations 1 thru 5. Figure 2 presents the $\varepsilon_{\text{eff}}$ as a function of the frequency. In this figure the slot width W, wafer thickness D, and relative dielectric constant $\varepsilon_r$, are equal to 0.1 mm, 0.381 mm and 11.7, respectively. Also shown in Fig.2 is the computed $\varepsilon_{\text{eff}}$ which is obtained as described in ref.11. The measured and computed $\varepsilon_{\text{eff}}$ are in good agreement.

The intrinsic peak insertion loss $L$ of the resonator is corrected for the insertion loss due to the microstrip feed lines and the coaxial connectors of the fixture. This is done by subtracting the feed and connector loss from the overall measured insertion loss. These excess losses are determined from a separate set of measurements using a thru line of length equal to the sum of the feed line lengths in the test fixture. Figure 3 presents the measured attenuation $\alpha$ as a function of the frequency. The W, D and $\varepsilon_r$ of the slotline are the same as those in Fig. 2. The attenuation of slotline is compared in Table 1 with the measured results from the open literature for microstrip line and coplanar waveguide on various other semiconductor substrate materials. It is worth mentioning here that the attenuation values quoted in Table 1 depend on the substrate thickness, metalization thickness and also the strip conductor width and/or slot width which are not the same in all cases.

IV. CONCLUSIONS AND DISCUSSIONS

The $\varepsilon_{\text{eff}}$ and $\alpha$ for a slotline on a high resistivity silicon substrate have been experimentally obtained. The attenuation constant for slotline has been compared with that of microstrip line and coplanar waveguide on other semiconductor substrate materials. The value of attenuation for slotline was found to be comparable to other transmission lines. This, however, can only be a rough comparison because attenuation depends upon the substrate thickness, metalization thickness and strip conductor width and/or slot width which are not the same in all the cases. However our experiments demonstrate the viability of high resistivity silicon for low loss antenna feed network. Application of this information to the feed network will be presented at the symposium.
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TABLE 1
Comparision of Attenuation Constant of Microwave Transmission
Lines on Semiconductor Substrates

<table>
<thead>
<tr>
<th>TRANSMISSION LINE</th>
<th>SUBSTRATE MATERIAL</th>
<th>DIMENSIONS (Inch)</th>
<th>ATTENUATION @ 10 GHz (dB/cm)</th>
<th>REFERENCE</th>
</tr>
</thead>
</table>
| Microstrip (Z₀ = 50 Ω) | SI GaAs | D = 0.025
W = 0.025
T = 3 μm* | 0.105 | 12 |
| Coplanar Waveguide (CPW) (Z₀ ≈ 50 Ω) | SI GaAs | D = 0.025
S = 0.025
W = 0.0125
T = 3 μm* | 0.16 | 12 |
| Coplanar Waveguide (CPW)¹ (Z₀ ≈ 35 Ω) | SI InP | D = 0.5 mm
S = 0.025
W = 16 μm
T = 0.25 μm* | 4.5 | 14 |
| Coplanar Waveguide (CPW) (Z₀ = 50 Ω) | SI GaAs | D = 0.5 mm
S = 75 μm
W = 56 μm
T = 3 μm* | 0.45 | 13 |
| Microstrip (Z₀ = 50 Ω) | High Res. silicon (1.5 k Ω·cm) | D = 0.01
W = 0.006$ | 0.5 | 5 |
| Microstrip (Z₀ ≈ 50 Ω) | High Res. Silicon (8 k Ω·cm) | D = 0.021
W = 0.016
T = 3 μm | 0.16 | 9 |
| Coplanar Waveguide (CPW)² (Z₀ ≈ 50 Ω) | High Res. Silicon (2.5 - 3.3 k Ω·cm) | D = 0.008
S = 0.004
W = 0.002
T = 2.5 μm* | 0.62 | 10 |
| Coplanar Waveguide (CPW)² (Z₀ = 60 Ω) | High Res. Silicon (4 k Ω·cm) | D = 400 μm
S = 30 μm
W = 35 μm
T = 1 μm* | 3 | 8 |
| Slotline² (Z₀ = 60 Ω) | High Res. Silicon (5 - 10 k Ω·cm) | D = 0.015
W = 0.004
T = 2.5 μm* | 0.25 | This work |

D is substrate thickness and T is metalization thickness
**Microstrip:** W is strip width
**Coplanar Waveguide:** S is center strip width and W is slot width
¹Metal thickness less than one skin depth
²A SiO₂ interfacial layer is present
*Gold conductors, $Aluminium conductors
Figure 1.—Slotline ring resonator electromagnetically coupled to microstrip feed lines.

\[ R = 1.00584 \text{ cm} \]
\[ W_m = 0.01016 \text{ cm} \]
\[ L_s = 0.09271 \text{ cm} \]
\[ T = 2.5 \mu\text{m} \]
\[ \varepsilon_r = 11.7 \]

\[ \varepsilon_0 \varepsilon_r \]

Figure 2.—Effective dielectric constant.

Figure 3.—Attenuation constant.
NEW COPLANAR WAVEGUIDE FEED NETWORK FOR 2 × 2 LINEARLY TAPERED SLOT ANTENNA SUBARRAY

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KEY TERMS
Coplanar waveguide, linearly tapered slot antenna, slot line, array antenna

ABSTRACT
A new technique for exciting a 2 × 2 subarray of linearly tapered slot antennas (LTSA) with coplanar waveguide (CPW) is presented. rf power is coupled to each element through a CPW-to-slotline transition by a coax-to-CPW in-phase four-way radial power divider. The transition and the power divider are coupled by a novel nonplanar CPW right-angle bend. Measured results at 18 GHz show excellent radiation patterns and return-loss characteristics. © 1992 John Wiley & Sons, Inc.

I. INTRODUCTION
Linear tapered slot antennas (LTSA) are useful in applications which require high gain, narrow beamwidth and wide bandwidth [1]. The most common approach of exciting a single-element LTSA is with a microstrip/slotline transition. Recently, the use of coplanar waveguide feeding a single-element LTSA has been demonstrated [2]. For LTSA arrays, finite-to-waveguide [1] and slotline-to-microstrip [3] feed structures have been reported. The former feeding approach is bulky in size, while the latter could produce spurious radiation.

This article proposes a new technique for exciting a 2 × 2 LTSA subarray using a CPW-to-slotline transition in conjunction with a coax-to-CPW in-phase four-way radial power divider. The transition and the power divider are coupled by a novel nonplanar CPW right-angle bend. This compact feed design is easy to integrate, and using CPW as the transmission medium produces less spurious radiation.

II. CPW FEED NETWORK AND SUBARRAY DESIGN
Figure 1 illustrates the construction of the 2 × 2 LTSA subarray. The feed network for this subarray consists of a CPW-to-slotline transition and a coax-to-CPW in-phase four-way, radial power divider [4] on separate dielectric substrates coupled by a novel nonplanar CPW right-angle bend.

a. LTSA and CPW-to-Slotline Transition. The LTSA and the CPW feed are etched on opposite sides of the circuit board and electromagnetically coupled, as shown in Figure 1. The LTSA is formed by gradually flaring the width of the slotline by an angle 2α. In general, a symmetric beam is required to illuminate a reflector for maximum aperture efficiency, this is achieved by choosing 2α equal to 10.6 degrees [1]. Similarly, to optimize the radiation efficiency of the LTSA, H is chosen to be 0.75 λo, where λo is the free-space wavelength at the center frequency f0 of 18 GHz. The length L of the antenna as determined by α and H is 4.1 λo.

To couple power to the antenna, the center strip conductor of the CPW is extended to form a CPW-to-slotline transition with the LTSA. The distances from the short-circuit termination of the slotline and the open termination of the extended center strip conductor, to the CPW-to-slotline junction is approximately a quarter of a wavelength at f0. To provide a smooth transition, the slotline at the feed end of the LTSA has a circular bend instead of a right-angle bend. The radius of curvature of the bend is approximately R = λo/6. The finite ground planes of the CPW lines are connected to the antenna ground plane via holes to ensure odd-mode excitation. Further, the CPW ground planes are tapered to provide good impedance match.

The coax-to-CPW in-phase four-way radial power divider circuit board is also shown in Figure 1. Design details for the radial power divider are given in [4].

b. Nonplanar CPW Right-Angle Bend. The nonplanar CPW right-angle bend is illustrated in Figure 2. In this bend, the center strip conductor of the CPW line is enlarged, forming a circular island that facilitates drilling a hole for a pin con-

Figure 1 Schematic diagram illustrating the construction of 2 × 2 LTSA subarray
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Further, the CPW line beyond the island is terminated in a short-circuited stub for impedance matching. The radius of the island $R_1$, the surrounding slot region $R_2$, the diameter of the pin $D$, and the length of the CPW short-circuited stub $L$, were experimentally optimized to obtain the best insertion loss and return loss characteristics. $R_1$, $R_2$, $D$, and $L$ are approximately $0.043 \lambda_r$, $0.063 \lambda_r$, $0.024$ cm, and $0.2 \lambda_r$, respectively, where $\lambda_r$ is the CPW guide wavelength at $f_0$. The power divider network as well as the subarray are fabricated on $0.0508$-cm-thick RT/Duroid 5880 ($\varepsilon_r = 2.2$) circuit board.

III. CPW RIGHT ANGLE BEND AND SUBARRAY PERFORMANCE

The measured insertion loss ($S_{11}$) of the nonplanar CPW right-angle bend is shown in Figure 3. The measured insertion loss includes the losses occurring in the bend, the attenuation of the $2.54$-cm length of CPW line on either side of the bend, and that of the two coaxial connectors used at the measurement ports. Also superimposed on Figure 3 is the return loss ($S_{11}$), which is better than $-10$ dB and has a bandwidth of $1.45$ GHz centered at $f_0$.

The measured E- and H-plane radiation patterns of the $2 \times 2$ LISA subarray at $f_0$ are shown in Figure 4. The $3$-dB beamwidth is approximately $23$ degrees in the principal planes, and the measured cross-polarization is less than $-16$ dB. The measured gain of the single-element LISA is approximately $11$ dB, and hence the gain of the $2 \times 2$ LISA subarray is estimated to be $17$ dB. Last, as shown in Figure 5, the measured return loss at the coaxial input port of the subarray is better than $-10$ dB, and the $2:1$ VSWR bandwidth is the same as the CPW right-angle bend.

IV. CONCLUSIONS AND DISCUSSIONS

A new feeding technique for a $2 \times 2$ LISA subarray using a CPW-to-slotline transition and a coax-to-CPW in-phase four-way radial power divider have been demonstrated. The characteristics of a novel nonplanar CPW right-angle bend have also been presented. The subarray has excellent radiation patterns and symmetric beamwidth. Because of its compactness, this subarray module is suitable as a feed for a reflector antenna or as building blocks for large arrays.

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LINEARLY TAPERED SLOT ANTENNA WITH DIELECTRIC SUPERSTRATE

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ABSTRACT

The effect of dielectric superstrate on a linearly tapered slot antenna (LTSA) was investigated experimentally. It was observed that the dielectric superstrate improves the directivity but generally at the expense of higher sidelobe level. The dielectric superstrate could be used to reduce the physical length and to improve the radiation characteristics of the LTSA.

INTRODUCTION

In recent years, research on linearly tapered slot antennas (LTSA) have been extensive [1],[2]. Most of these studies concerns with the performance characteristics and feeding techniques of the LTSA, and there is disproportionately little effort devoted to the study of superstrate effects on linearly tapered slot antennas. These effects are important in a stacked array antenna in which a dielectric spacer between two arrays inadvertently serves as a superstrate. The superstrate alters the guide wavelength of the LTSA and thus impacts the overall antenna design. In this paper, the effects of dielectric superstrate on the directivity and radiation patterns of a full length and reduced length LTSA will be presented and discussed.

ANTENNA CONFIGURATION

The LTSA used in the experiment is shown in Fig. 1. The LTSA having an aperture width L of 1.27 cms, a taper angle, 2α, of 11.2° and an aperture width H of 1.27 cms is etched on a 0.0508 cm RT/Duroid 5880 substrate (εr = 2.2). The LTSA is electromagnetically coupled to a coplanar waveguide (CPW) with the center strip conductor of the CPW extented to form a CPW-to-slotline transition with the LTSA. The distances Ls from the short circuit termination of the slotline and Lw from the open termination of the extented center strip conductor to the CPW-to-slotline junction are about a quarter of a wavelength at 20 GHz. The ground

plane of the CPW is connected to the antenna ground plane through via holes to ensure good impedance match and odd mode operation.

RESULTS AND DISCUSSIONS

In our experiment, the effect of superstrate was examined for LTSA with various lengths. Fig. 2 shows the measured H- and E- patterns of the regular length (L = 6.6 cm) LTSA without superstrate at 11.67, 20.15 and 22.8 GHz. Results indicate that the patterns are generally symmetrical, and the directivity increases faster in the H-plane than in the E-plane with frequency. The measured gain of the LTSA is about 11 dB.

The superstrate increases the electrical length as well as the effective aperture of the antenna, and thus enhances the antenna directivity. The increase in directivity is evident from the measured antenna pattern which shows a narrower main lobe. Fig. 3(a)-(b) displays the measured H- and E-plane patterns with and without a superstrate. As indicated, the effect of the superstrate is more pronounced in the H-plane than in the E-plane. The beamwidths of the the LTSA with and without superstrate have been recorded for frequencies ranging from 10 to 20 GHz. The results are plotted in Fig. 4. With superstrate, the beamwidth is generally narrower; however, the sidelobe level is also higher.

By reducing the length ,L, of the LTSA, the radiation patterns become broader indicating a reduction in antenna gain. The superstrate increases the electrical length of the LTSA and enhances its directivity. The improvement in directivity results in narrower beamwidth for the LTSA with superstrate as indicated in Fig. 5. Fig. 6 shows the measured patterns of the reduced length LTSA with and without superstrate at 11 GHz. The patterns appear symmetrical with the superstrate.

CONCLUSION

The effect of superstrate on a LTSA has been studied. Results indicate that the superstrate improves the patterns and directivity of the antenna by increasing the electrical length and effective aperture of the antenna. A superstrate can also be used to reduce the physical length of the antenna without compromising the pattern quality.

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Fig. 1. Schematic for the LTSA and the CPW feed circuit
S=0.762 mm, W=0.254 mm, G=5.08 mm, L_w=2.951 mm,
 r_1=2.171 mm, r_2=2.425 mm, L_s=3.43 mm.
(a) Top metalization is the feed structure.
(b) Bottom metallization is the antenna.

Fig. 2. Measured radiation patterns of the LTSA without a superstrate: (a) H-plane and (b) E-plane.
Fig. 3. Measured radiation patterns of the LTSA with and without a superstrate at 11 GHz: (a) H-plane and (b) E-plane.

Fig. 4. Measured beamwidth vs. frequency for the LTSA with and without superstrate at 11 GHz.

Fig. 5. Measured beamwidth vs. reduced lengths of the LTSA with and without superstrate at 11 GHz.

Fig. 6. Measured radiation patterns of the reduced length LTSA with and without superstrate at 11 GHz: (a) H-plane and (b) E-plane.
EFFECT OF A DIELECTRIC OVERLAY ON A LINEARLY TAPERED SLOT ANTENNA EXCITED BY A COPLANAR WAVEGUIDE

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KEY TERMS
Slot antenna, coplanar waveguide, antenna feed

ABSTRACT
A linearly tapered slot antenna (LTSA) with a dielectric overlay was experimentally investigated. The presence of dielectric overlay alters the guide wavelength of the LTSA, and thus the radiation characteristics of the antenna. Results indicate that dielectric overlay could be used to reduce the physical length and to improve the radiation characteristics of the LTSA. © 1993 John Wiley & Sons, Inc.

I. INTRODUCTION
The linearly tapered slot antenna (LTSA) has been developed for potential millimeter-wave applications, e.g., as a radiating element for reflector or lens antennas. Compared to other types of printed circuit antennas, these end-fire antennas have higher directivity, broader bandwidth, and less spatial constraint for solid-state device integration [1]. The LTSA has been studied extensively in the past decade. Most of these studies concern the performance characteristics and feeding techniques of the LTSA [2, 3]. Recently, a LTSA of nonplanar geometry fed with a balanced microstrip line has also been reported to have excellent radiation and bandwidth characteristics [4]. Despite all these efforts, little information is available on the effects of dielectric overlays on linearly tapered slot antennas. These effects are important in a stacked array antenna in which a dielectric spacer between two arrays inadvertently serves as an overlay. In addition, the dielectric overlay changes the guide wavelength of the LTSA and thus impacts the overall antenna design. In this article we report our experimental findings of the effects of dielectric overlay and also the effects of reduction in physical length of the LTSA on the radiation patterns.

II. DESIGN AND FABRICATION
Figure 1 shows the layout of the LTSA which has a physical length \( L \) of 6.6 cm, a taper angle, \( 2\alpha \), of 11.2 degrees, and an aperture width \( H \) of 1.27 cm. The LTSA is electromagnetically coupled to a coplanar waveguide (CPW) feed etched on the opposite side of a 0.0508-cm RT/Duroid 5880 substrate (\( \varepsilon_r = 2.2 \)). The finite ground plane of the CPW is connected to the antenna ground plane via holes to ensure good impedance match and odd-mode operation. For efficient power coupling, the center strip conductor of the CPW is extended to form a CPW-to-slot-line transition with the LTSA. The distance \( L_w \), from the short-circuit termination of the slot line, the \( L_w \) from open termination of the extended center strip conductor, to the CPW-to-slot-line junction are about a quarter of a wavelength at the center frequency of 20 GHz. To provide a smooth transition, the slot line at the feed end has a circular bend instead of a right-angle bend.

III. RESULTS AND DISCUSSIONS
In our experiments, the effect of dielectric overlay was examined for LTSA with regular and reduced lengths. These results were compared to those of identical LTSA without dielectric overlay. The experimental findings are summarized below.

A. Regular-Length LTSA Performance. The measured return loss is displayed in Figure 2, which shows a 2:1 VSWR bandwidth of 20 GHz over a frequency range of 10–30 GHz. These results indicate that the regular-length \( L = 6.6 \) cm \( \text{LTSA} \) without overlay has ultrawideband characteristics and good impedance match. Typical measured H- and E-plane radiation patterns are shown in Figures 3(a) and 3(b), respectively. The patterns are generally symmetrical over a wide range of frequencies. Results also indicate that the directivity increases faster in the \( H \) plane than in the \( E \) plane with increasing frequency. The measured gain of the LTSA is about 11 dB.

B. Overlay Effect. The effect of the overlay was found to have a significant effect on the regular-length LTSA at the lower end of the frequency band. At these frequencies, the
Figure 2 Measured return loss ($S_11$) as a function of frequency.

Figure 3 Measured radiation patterns of the regular-length LTSA without a dielectric overlay at 10.67, 20.15, and 22.8 GHz. (a) $H$ plane. (b) $E$ plane.

Figure 4 Measured radiation patterns of the regular-length LTSA without and with a dielectric overlay at 11 GHz. (a) $H$ plane. (b) $E$ plane.

Figure 5 Measured radiation patterns of the reduced-length LTSA without and with a dielectric overlay at 11 GHz. (a) $H$ plane. (b) $E$ plane.

C. Reduced-Length LTSA Performance. By reducing the length $L$ from 6.6 to 4.4 cm the radiation pattern broadens due to reduction in gain. By providing a dielectric overlay the electrical length and the effective aperture are small; hence the directivity is low and the beamwidth is broad. By introducing an overlay, the electrical length as well as the effective aperture are increased, thus enhancing the directivity. The increase in directivity is evident from the measured antenna pattern which now has a narrower main lobe. Figures 4(a) and 4(b) illustrate the measured $H$- and $E$-plane radiation patterns without and with an overlay. These patterns further indicate that the effect of overlay is more pronounced in the $H$ plane than in the $E$ plane. This is due to the fact that in the $E$ plane, the incident wave is perpendicular to the plane of the substrate.

IV. CONCLUSION

The effect of dielectric overlay on a LTSA has been studied. The LTSA under study exhibits very wide bandwidth and excellent radiation patterns. A dielectric overlay improved the patterns and directivity of the antenna by increasing the electrical length and effective aperture of the antenna. A
Figure 2 Measured return loss \( S_{11} \) as a function of frequency.

Figure 3 Measured radiation patterns of the regular-length LTSA without a dielectric overlay at 10.67, 20.15, and 22.8 GHz. (a) \( H \) plane, (b) \( E \) plane.

Figure 4 Measured radiation patterns of the regular-length LTSA without and with a dielectric overlay at 11 GHz. (a) \( H \) plane, (b) \( E \) plane.

Figure 5 Measured radiation patterns of the reduced-length LTSA without and with a dielectric overlay at 11 GHz. (a) \( H \) plane, (b) \( E \) plane.

Electrical length and the effective aperture are small; hence the directivity is low and the beamwidth is broad. By introducing an overlay, the electrical length as well as the effective aperture are increased, thus enhancing the directivity. The increase in directivity is evident from the measured antenna pattern which now has a narrower main lobe. Figures 4(a) and 4(b) illustrate the measured \( H \)- and \( E \)-plane radiation patterns without and with an overlay. These patterns further indicate that the effect of overlay is more pronounced in the \( H \) plane than in the \( E \) plane. This is due to the fact that in the \( E \) plane, the incident wave is perpendicular to the plane of the substrate.

C. Reduced-Length LTSA Performance. By reducing the length \( L \) from 6.6 to 4.4 cm, the radiation pattern broadens due to reduction in gain. By providing a dielectric overlay the electrical length of the LTSA increases and the directivity improves. The improvement in directivity is evident from the patterns shown in Figures 5(a) and 5(b).

IV. CONCLUSION

The effect of dielectric overlay on a LTSA has been studied. The LTSA under study exhibits very wide bandwidth and excellent radiation patterns. A dielectric overlay improved the patterns and directivity of the antenna by increasing the electrical length and effective aperture of the antenna.
dielectric overlay can also be used to reduce the physical length of the antenna without compromising the pattern quality.

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CHARACTERISTICS OF LINEARLY TAPERED SLOT ANTENNA WITH CPW FEED ON HIGH RESISTIVITY SILICON

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SUMMARY

A linearly tapered slot antenna (LTSA) has been fabricated on a high resistivity silicon substrate and tested at C-Band frequencies. The LTSA is electromagnetically coupled to a coplanar waveguide (CPW) feed. In this paper, the measured radiation patterns, gain and return loss are presented and discussed.

INTRODUCTION

Linearly tapered slot antennas (LTSA's) have many exceptional features such as narrow beamwidth, high element gain, wide bandwidth and small transverse spacing between elements in an array. These features make them attractive in satellite communication antennas (ref. 1). Previously reported LTSA antennas are fabricated on low dielectric constant RT-5880 Duroid substrate (refs. 2 to 4). This paper describes the design and performance of a LTSA constructed on a high resistivity silicon substrate. By choosing a silicon substrate with sufficiently high resistivity it is possible to make the dielectric attenuation constant of the microwave transmission line for the feed network approach that of GaAs (ref. 5). Compared to designs presented earlier, the new design has smaller dimensions because of the higher dielectric constant of silicon. In addition, the use of silicon provides for the potential of integration with silicon MMIC's and digital control circuits. Lastly, when compared with GaAs, silicon wafers are available in much larger diameters and at lower cost thus facilitating integration of active devices, antenna and control circuits on a single wafer.

ANTENNA DESIGN AND FABRICATION

The antenna and the feed network are fabricated on a single 5000 to 10,000 Ω-cm silicon wafer. The thickness of the wafer is 0.381 mm with \( \varepsilon_r = 11.7 \). The thickness of the gold metalization is about 2.5 μm which is about three times the skin depth at the center frequency \( f_0 \) of 6 GHz. This substrate has an effective thickness ratio (ref. 1) of 0.02 which is within the optimum range for high gain and low side lobes. Figure 1 shows a feed with electromagnetic coupling between a grounded CPW (GCPW) and slotline which are on opposite sides of a silicon wafer (ref. 6). At the GCPW input port, \( Z_0 \) is 50 Ω while close to the transition to the slotline \( Z_0 \) is 60 Ω. The \( Z_0 \) of the slotline is 70 Ω. The distances \( L_s \) and \( L_m \) are \( \lambda_g(\text{slotline})/4 \) and \( \lambda_g(\text{microstrip})/4 \), respectively at \( f_0 \). The LTSA is formed by gradually flaring the width of the slotline by an angle \( 2\alpha \). When \( 2\alpha \) is close to 11 degrees a symmetric beam width is achieved for an antenna on Duroid (ref. 1). A symmetric beam results in high aperture efficiency if used for illuminating a reflector. The width \( H \) of the antenna is
arbitrarily chosen as 0.3 $\frac{\lambda}{g(\text{slotline})}$. The length $L$ of the antenna as determined by $\alpha$ and $H$ which is 1.5 $\frac{\lambda}{g(\text{slotline})}$. Figure 2 shows a picture of the fabricated antenna.

ANTENNA PERFORMANCE AND DISCUSSIONS

The measured return loss ($S_{11}$) at the coaxial input port of the feed network is shown in figure 3. The return loss is observed to be better than $-10$ dB (2:1 VSWR) over a frequency range extending from 6 to 8 GHz. Although, the antenna has been designed at 6 GHz, the best return loss occurs at about 7 GHz. This could be due to double side processing of the wafer which might have inadvertently offset the feed resulting in a shorter stub length. Typical measured E- and H-plane radiation patterns are shown in figure 4. The patterns are found to have good characteristics. The measured gain of the antenna is 5, 7, and 9 dB at 5, 7, and 9.4 GHz, respectively. Lastly, optimization of the LTSA on silicon has not been carried out and better performance might be expected with improvements.

CONCLUSIONS

The design and performance characteristics of a LTSA fabricated on high resistivity silicon wafer is presented. The LTSA exhibits good impedance match and radiation patterns.

ACKNOWLEDGMENT

The authors would like to thank Paul G. Young for the fabrication of the antenna.

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Figure 1.—Schematic of the linearly tapered slot antenna. \( W_a = 0.16 \text{ mm}, \ W_m = 0.15 \text{ mm}. \)

(a) Front side metalization.

(b) Back side metalization.

Figure 2.—Photograph of the antenna.

(a) Linearly Tapered Slot Antenna (LTSA) on silicon.

(b) Coplanar Waveguide Feed (CPW) for Linearly Tapered Slot Antenna on silicon.

Figure 2.—Photograph of the antenna.
Figure 3.—Measured return loss (S$_{11}$) at the coaxial input port.

Figure 4.—Measured radiation pattern of the LTSA at 7 GHz.
NONPLANAR LINEARLY TAPERED SLOT ANTENNA WITH BALANCED MICROSTRIP FEED

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ABSTRACT

A nonplanar linearly tapered slot antenna (LTSA) has been fabricated and tested at frequencies from 8 to 32 GHz. The LTSA is excited by a broadband balanced microstrip transformer. The measured results include the input return loss as well as the radiation pattern of the antenna.

INTRODUCTION

Linearly tapered slot antennas (LTSA) have many salient features such as narrow beam width, high element gain, wide bandwidth and small transverse spacing between elements in an array. These features make them attractive in satellite communication antennas involving beam shaping and switching (ref. 1). Previously reported LTSA antennas are excited either by a fin line (ref. 2), coplanar waveguide (CPW) (ref. 3), or by a microstrip to slot line transition (ref. 3). The latter makes use of quarter wavelength stubs for impedance matching and hence the 2:1 VSWR bandwidth of the circuit is very small (ref. 3).

This paper describes the design and performance of a LTSA excited by a balanced microstrip (fig. 1). Compared to the fin line feed, the new design is smaller, less complex, and is not limited to a waveguide band. In addition, when compared to CPW or microstrip/slot line feed, the new design eliminates the necessity of quarter wavelength stubs and hence has a much wider bandwidth.
BALANCED MICROSTRIP FEED DESIGN

The feed system, as shown in figure 1, consists of a conventional microstrip on a dielectric substrate of thickness $D$ with the ground plane tapered to a width equal to the strip width $W$ (0.071 cm) to form a balanced microstrip. The radius $R_2$ of the arc is arbitrarily chosen as half free space wavelength ($\lambda_0/2$) at the design frequency ($f_0$) of 18 GHz. The taper helps to match the characteristic impedance of the conventional microstrip (50 $\Omega$) to the balanced microstrip. The characteristic impedance of the balanced microstrip is chosen as $\approx 160 \Omega$ which is equal to the input impedance of the LTSA. This input impedance is twice the input impedance of a regular half LTSA above a ground plane ($\approx 80 \Omega$) (ref. 2). The electric field lines at various cross sections along the feed and the antenna are shown in figure 2. The electric field lines which are spread out in the conventional microstrip concentrate between the metal strips of the balanced microstrip and finally rotate while travelling along the axis of the antenna.

NONPLANAR LTSA DESIGN

The nonplanar LTSA is formed by gradually flaring the strip conductors of the balanced microstrip on opposite sides of the dielectric substrate by an angle $\alpha$ with respect to the antenna axis. A symmetric beam width is necessary while illuminating a reflector for maximum aperture efficiency; this is achieved is $2\alpha$ is close to 11° (ref. 1). Hence $\alpha$ is chosen as 5.3° in our design. The radius $R_1$ of the arc is arbitrarily chosen as 0.9 $\lambda_0$. In order for the LTSA to operate as a travelling wave antenna, the width $H$ must be greater than $\lambda_0/2$ (ref. 1); hence, $H$ is chosen as 0.75 $\lambda_0$. The length $L$ of the antenna as determined by $\alpha$ and $H$ is 4.3 $\lambda_0$. The entire circuit is fabricated on 0.0508 cm thick RT/Duroid 5880 ($\varepsilon_r = 2.2$) substrate. This substrate has an effective thickness ratio of 0.03 which is within the optimum range for high gain and low side lobes (ref. 1).

ANTENNA PERFORMANCE AND DISCUSSIONS

The measured return loss ($S_{11}$) at the coaxial input port of the feed network is shown in figure 3. The return loss is observed to be better than -10 dB (2:1 VSWR) over a frequency range extending from 8 to 32 GHz. This is a significant improvement over the LTSA reported in the literature (ref. 3).

The measured E- and H-plane radiation patterns at three different frequencies are shown in figures 4(a) and (b) respectively. The measured patterns are found to be excellent.

The measured H-Plane cross-polarized radiation is -16 dB below the copolarized radiation at $f_0$. Further improvement could be achieved by varying the substrate thickness.

CONCLUSIONS

The design and performance characteristics of a LTSA with a balanced microstrip feed network has been presented. A LTSA fed with this feed network exhibits very broad bandwidth extending from X-band to Ka-band with good impedance match and excellent radiation patterns.
REFERENCES


Figure 2.—The electric field distribution at various cross sections.

Figure 3.—Measured return loss ($S_{11}$) at the coaxial input port.

Figure 4.—Measured radiation pattern of the non-planar LTSA.
SLOT-COUPLED PATCH ANTENNA WITH COPLANAR WAVEGUIDE FEED

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ABSTRACT

Two slot-coupled feeding techniques for exciting a patch antenna with a coplanar waveguide (CPW) were experimentally investigated. In the first technique, a CPW with two notches on both sides of the slot lines is used to couple power to the antenna through a narrow rectangular slot. In the second technique, a grounded CPW with a series gap in the center strip conductor is used to couple power to the antenna through a 'dumbbell' slot. Results indicated that both techniques are feasible and yield high coupling efficiency.

INTRODUCTION

Previous work on slot-coupled patch antennas concerns mainly with feed structure of microstrip type. Only recently, slot-coupled feeding technique with coplanar waveguide (CPW) feed has been demonstrated [1]. Compared to direct probe feeding approach, slot-coupled feeding requires no physical contact with the antenna, has wider bandwidth, and allows independent optimization of antennas and feed networks by using substrates of different thickness and permittivity. Further, the use of CPW as transmission media can reduce circuit radiation losses, and facilitates monolithic microwave integrated circuit (MMIC) device integration.

In this paper, we report two feeding techniques where the patch antenna is excited by coupling power electromagnetically through a slot from a CPW feed. The two techniques differ from each other in the CPW feed structure and slot designs. The first technique uses a grounded CPW with notches on both sides of the slot lines and a narrow rectangular slot, while the second technique uses a CPW with a series gap in the center strip conductor and a 'dumbbell' slot. The latter permits insertion of solid state devices in the series gap of the CPW and thus, is suitable for use in active antenna or quasi-optical combiner/mixer designs. To optimize the coupling efficiency, three different slot/gap designs have been tested.

DESIGN DESCRIPTION

Figure 1 (a) shows the slot-coupled patch antenna excited by a CPW with notches on both sides of the slot lines. The patch and the CPW feed structure are fabricated on separate substrates with the rectangular slot located in the common ground plane directly above the notches. The slot width and length are initially chosen to be 0.254 mm and \( \lambda_g / 2 \) respectively, where \( \lambda_g \) is the wavelength of an uniform slot line [2]. The slot length is then

slightly reduced to account for the slot end effects. The notch has a width of 0.762 mm and an end-to-end distance approximately equal to the slot length. To ensure good coupling and odd mode operation, the CPW is terminated in a short circuit at a distance of approximately $\lambda_{g(\text{cpw})}/2$ from the center of the notch, and a pair of bond wires is inserted on both sides of the notches.

Figure 1 (b) shows the slot-coupled patch antenna excited by a CPW with a series gap in the center strip conductor. The inset in Figure 3 shows the three different slot/gap designs tested. In the first design, the dimensions of the series gap and the rectangular slot are $(L_1, S)$ and $(L_2, W_2)$ respectively. In the second design, the width of the series gap is enlarged from $S$ to $S'$ by flaring the center strip conductor of the CPW near the gap location. In the third design, the rectangular slot is replaced by a 'dumbbell' slot of identical length and width. The design parameters are given in the figure caption.

RESULTS AND DISCUSSIONS

Measured input impedance on Smith chart for the patch antenna with CPW/notch feed structure is shown in Figure 2. At the best impedance match frequency of 14 GHz, the return loss is greater than 20 dB and the 2:1 VSWR bandwidth is 4.2 %. Figure 3 shows the measured return losses for the three different feed configurations. As indicated, the return losses are improved from -8.2 dB for (a) to -13.2 dB for (b) to -16.9 dB for (c). Results indicate that the coupling efficiency was improved by more than 3 dB each by using an enlarged series gap or a 'dumbbell' slot. However, the geometrical change in the series gap and slot of the feed structure produced a slight change in the resonance frequency. Measured H- and E-plane patterns for the patch antenna excited by a CPW through notch/slot and gap/slot coupling are displayed in Figure 4 (a) and (b) respectively. The patterns appear symmetrical. The measured front-to-back ratio is about 14 dB which is typical for slot-coupled antenna configurations.

CONCLUSION

Two slot-coupled techniques for exciting patch antennas with CPW feeds have been demonstrated. Techniques for improving coupling efficiency are also described and discussed. Measured results indicate excellent patterns and coupling efficiency.

REFERENCES:

Fig. 1  Schematic of the CPW fed patch antenna with: (a) notch/slot coupling and (b) gap/slot coupling
L₁=0.025 cm, L=0.711 cm, L₂=0.025 cm, W₂=0.69 cm,
a=0.76 cm, b=1.14 cm, T₁=0.051 cm, T₂=0.025 cm,
S=0.076 cm, W=0.025 cm, ε₁=2.2, ε₂=2.2

Fig. 2  Measured input impedance of the CPW fed patch antenna with notch/slot coupling.
Fig. 3  Measured return losses vs. frequency for feed structures with: (a) a series gap and a rectangular slot, (b) an enlarged series gap and a rectangular slot, and (c) an enlarged series gap and a 'dumbbell' slot. 
\((S_1=0.355 \text{ cm}, L_t=0.711\text{ cm}, \text{ and } R=0.0843 \text{ cm})\)

Fig. 4  Measured radiation patterns for the CPW fed patch antennas with (—) notch/slot and (---) gap/slot coupling: (a) H-plane and (b) E-plane.
BANDWIDTH ENHANCEMENT OF DIELECTRIC RESONATOR ANTENNAS

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ABSTRACT

This paper reports an experimental investigation of bandwidth enhancement of dielectric resonator antennas (DRA) using parasitic elements. Substantial bandwidth enhancement for the HE136 mode of the stacked geometry and for the HE136 mode of the coplanar collinear geometry have been demonstrated. Excellent radiation patterns for the HE116 mode were also recorded.

INTRODUCTION

A dielectric resonator placed over a ground plane can serve as an effective radiator [1-2]. Compared to printed antennas, the DRA has lower ohmic losses and higher radiation efficiency particularly at high frequencies. However, because of high Q factor, the DRA has very narrow bandwidth which severely limits its usefulness as an antenna. It has been demonstrated that significant bandwidth enhancement can be achieved for microstrip antennas by placing closely spaced parasitic elements on both sides of or directly above a driven patch [3]. It appears that parasitic elements can also be used to enhance the bandwidth of a DRA. This paper is concerned with an experimental investigation of the effects of parasitic elements on dielectric resonator antennas.

THE EXPERIMENT

The single DRA as shown in Fig. 1(a) is placed on a ground plane and aperture coupled to a notched coplanar waveguide (CPW) through a slot. The slot is positioned along the y-axis (\(\phi=90^\circ\)) so the HE116 and the HE136 modes can be excited [4]. Bond wires are used to keep the CPW ground planes at equal potential and suppress the slotline even mode. The DRA of diameter D and height H of 6.223 mm and 2.489 mm respectively is constructed from ZrSnTiO4 material of relative permittivity \(\varepsilon_{r2}=36.0\), and the CPW feed is fabricated from 20 mil (0.508 mm) RT-5880 Duroid substrate of \(\varepsilon_{r1}=2.2\). In the experiment, identical dielectric resonators were placed directly above and on both sides of the driven DRA.

RESULTS AND DISCUSSIONS

The measured return losses for the single DRA is shown in Fig. 2(a). Results indicate that with proper aperture lengths, either the HE_{116} or the HE_{136} mode can be strongly excited. The aperture length was found to have a strong impact on the bandwidth of the DRA. The HE_{116} mode excited with an aperture L_1 = 0.40 cm has a 2:1 VSWR bandwidth of 8.8 %, while the HE_{136} excited with an aperture L_1 = 0.68 cm has a bandwidth of only 2.5 %. The return losses are less than -10 dB for both modes indicating strong coupling. Figure 3(a) shows the measured patterns for the HE_{116} which has a broader main lobe in the \( \phi=90^\circ \) plane than in the \( \phi=0^\circ \) plane. The pattern is asymmetrical along the \( \phi=0^\circ \) plane due to interference from the test fixture.

Figure 1(b) shows the collinear geometry where two identical dielectric resonators are proximity coupled to a driven DRA along the \( \phi=0^\circ \) plane with one on each side of the DRA. The separation between resonators is 1 mm. It was observed that placing the parasitic dielectric along the \( \phi=0^\circ \) plane produces strong coupling with the HE_{136} mode, while along the \( \phi=90^\circ \) plane produces strong coupling with the HE_{116} mode. The strong coupling is caused by high field concentrations of the HE_{136} and HE_{116} in the \( \phi=0^\circ \) and \( \phi=90^\circ \) plane respectively. Figure 2(b) shows the measured return losses which are less than -18 dB for the HE_{136} mode with \( \phi=0^\circ \) orientation and about -50 dB for the HE_{116} with \( \phi=90^\circ \) orientation. The parasitic elements has increased the 2:1 VSWR bandwidth of the HE_{136} from 2.5 % to 3.7 %. The measured patterns for the HE_{116} mode as shown in Fig. 3(b) exhibits excellent broadside characteristics.

Figure 1(c) shows the stacked geometry. The overlaying parasitic resonator was found to couple strongly to the HE_{116} mode where the electric field is maximum near the top surface of the driven DRA [6]. As indicated in Fig. 2(c), the measured return loss is less than -20 dB for the HE_{116} mode with the higher order mode suppressed. The parasitic resonator increases the 2:1 VSWR bandwidth of the HE_{116} mode to over 5.3 %. As with the previous case, excellent radiation patterns have been obtained for the HE_{116} mode. These patterns are displayed in Fig. 3(c).

CONCLUSIONS

Substantial enhancement in bandwidth has been demonstrated for the HE_{11} and the HE_{13} modes with the parasitic resonators placed directly above and on both sides of the DRA respectively. Because of excellent
return loss and radiation characteristics, the DRA should be excited in $HE_{11}$ mode when used as radiating elements in an array.

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Fig. 1 Schematic Illustrating a Grounded Dielectric Resonator Aperture Coupled to a Notched CPW feed: (a) Single , (b) multiple and (c) Stacked Dielectric Resonator Antenna.
Fig. 2  Measured Return Losses for: (a) Single, (b) Multiple and (c) Stacked Dielectric Resonator Antenna.

Fig. 3  Measured Radiation Patterns for the HE_{11f} Mode for: (a) Single, (b) Multiple and (c) Stacked Dielectric resonator Antenna (f = 8.2 GHz).
A space power amplifier composed of active linearly tapered slot antennas (LTSAs) has been demonstrated and shown to have a gain of 30 dB at 20 GHz. In each of the antenna elements, a GaAs monolithic microwave integrated circuit (MMIC) three-stage power amplifier is integrated with two LTSAs. The LTSA and the MMIC power amplifier have a gain of 11 dB and power added efficiency of 14 percent respectively. The design is suitable for constructing a large array using monolithic integration techniques.

This paper presents for the first time a spatial amplifier with GaAs monolithic microwave integrated circuit (MMIC) multi-stage power amplifiers. In this approach an array of active antenna modules constructed from nonplanar LTSAs and GaAs MMIC amplifiers receives signals at lower power, and after amplification re-radiates signals into free space. The two advantages of the spatial amplifier over the spatial oscillator are that only a single stable lower power source is required (thus greatly simplifying the combiner construction) and that the amplifiers can be individually optimized. Figure 1 schematically illustrates a possible arrangement for space power amplification.

Active Antenna Module Characteristics

The experimental three-element array module is shown schematically in Figure 2. The array elements are constructed by integrating a GaAs MMIC multi-stage power amplifier between two nonplanar LTSAs.

The feed system of the nonplanar LTSA consists of a conventional microstrip with the ground plane tapered to form a balanced microstrip. The strip conductors of the balanced microstrip are gradually flared with respect to the antenna axis to form an active antenna array which combines power radiatively in free space. The advantages of quasi-optical power combiners over conventional power combiners are higher combining efficiency because of lower conductor losses and larger dimensional tolerances with the absence of resonance modes. In addition both antennas and devices can be integrated on a single semiconductor wafer thus simplifying the array construction. The disadvantage of oscillator based quasi-optical combiners is that the individual oscillators have to be phase locked to a reference source or the active array has to be placed in a Fabry-Perot resonator to produce coherent radiation.

Another way to obtain high power is to construct a spatial amplifier. One such scheme is the grid amplifier. Each unit cell of the grid amplifier consists of a pair of packaged GaAs MESFETs with the sources connected together to form a differential amplifier and with the gate and drain terminals extending radially to form a pair of orthogonal strip antennas. Radiation to and from a planar array of identical unit cells is quasi-optically coupled by a vertically or a horizontally polarized beam respectively.

GaAs MMIC Multi-Stage Power Amplifier

The GaAs MMIC three-stage power amplifier was designed and fabricated by Texas Instruments for NASA Lewis Research Center. A photograph of the amplifier chip is shown in Figure 3. The amplifier is constructed on a GaAs substrate with an active layer doping level of 2.5x10^{17} cm^{-3}. The gate widths of the three stages are 1.2, 2.4, and 6.0 mm, respectively, and the gate length is 0.5 µm in all the stages. The chip size is about 4.0 by 3.0 by 0.1 mm. The bias network is incorporated on the chip. The drain voltage V_d and current I_d is 6.3 V and 1.9 A, respectively. The gate voltage

97
Vg is -0.6 V. The measured gain (S_{21}) on a HP 8510B ANA with a 40 dB coaxial attenuator on the drain side of a typical amplifier is shown in Figure 4. The gain is greater than 10 dB over the frequency range of 18 to 21 GHz. The saturated output power measured on a Pacific Instruments scalar network analyzer at 20 GHz is about 1.8 W with a gain of 10 dB and power added efficiency of 14 percent.9

Experimental Results and Discussions

A simple measurement procedure has been developed to estimate the gain of the space amplifier. This procedure involves the LTSSAs at the input terminals are space fed from a single horn antenna while those at the output terminals radiate into free space. The free space radiation is picked up by a second horn antenna which is placed at a far field distance from the array. The ratio of the measured received power with and without bias to the MMIC amplifiers provides an estimate of the gain of the space amplifier. In the setup, the two horn antennas are orthogonally polarized but the LTSSAs are oriented to have the same polarization as their respective horn antennas, thus good isolation between the transmitting and the receiving horn antennas is established. Also, for comparison purposes, a single LTSA was tested as a receive antenna. The H-plane pattern is shown in Figure 5 which exhibits a power gain of 6.7 dB with the MMIC amplifier turned ON.

Three-Element Array Module

In this experiment, the LTSSAs at the amplifier input and output are oriented with the H and E vectors of the receiving horn, respectively as shown in Figure 6(a). This arrangement allows the horn to excite the three LTSSAs with equal amplitude. The measured radiation pattern is shown in Figure 7(a) with the amplifiers turned ON and OFF, respectively. The gain increases by as much as 30 dB when the amplifiers are turned ON which is in good agreement with the measured gain of the amplifiers.

A second experiment, as shown in Figure 6(b), is carried out with the LTSSAs at the input and output oriented with the H and E vectors of the receiving horn, respectively. The measured radiation pattern is shown in Figure 7(b). In this arrangement the gain increases by 25 dB when the amplifiers are turned ON. The gain is lower in this case because the LTSSAs on either side of the center element are excited with a lower amplitude due to the amplitude taper of the electric field distribution of the transmitting horn. The experimental three element LTSA MMIC array module is shown in Figure 8.

Conclusions

A space power amplifier composed of active LTSA antennas has been demonstrated and shown to have a gain of 30 dB at 20 GHz. In each of the antenna elements, a MMIC three-stage power amplifier is integrated with two LTSSAs. The GaAs MMIC power amplifier and the LTSA have a power added efficiency of 14 percent and a gain of 11 dB, respectively. The design is suitable for constructing a large array using monolithic integration techniques.

References


MMIC Amplifiers

Figure 1.—Schematic illustrating a possible arrangement for space amplification.

Figure 2.—Schematic illustrating the three-element array module. ($\lambda_0$: free space wavelength.)

Figure 4.—Typical measured gain of MMIC amplifier.

Figure 5.—The measured H-plane radiation pattern of a single LTSA with and without the amplifier.
Figure 6.—LTSA orientation in the three-element array module for gain measurement.

Figure 7.—The measured radiation pattern of the horn antenna showing space power amplification.

Figure 8.—The experimental three element LTSA MMIC array module.
AN ANALYSIS OF THE FREQUENCY LIMITATIONS OF AN Al,Ga_{1-x},As/GaAs OPTICAL MODULATOR

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KEY TERMS
Optical modulators, heterojunction devices, interferometers

ABSTRACT
Frequency response of an optical modulator, operating at \( \lambda = 0.83 \) \( \mu \)m and utilizing the linear electro-optic (Pockels) effect in a Mach-Zehnder configuration using an Al,Ga_{1-x},As/Al,Ga_{1-x},As double heterostructure, is analyzed. We show that in semiconductor modulators, electroabsorption should be taken into account in optimizing the frequency response of the device. © 1993 John Wiley & Sons, Inc.

I. INTRODUCTION
Light modulators, integrated with optoelectronics, have attracted intense research activities in recent years. Speed and inherent parallelism of all-optical signal processing usually justify overall larger size of the optical components, and much activity is devoted to establishing fabrication sequences that result in reliable integrated devices and waveguides [1, 2]. Electro-optic modulators based on the linear electro-optic effect are expected to have very fast response, limited only by the transit times and RCs (R is the resistance and C is the capacitance) of the geometry and, in the case of traveling-wave modulators, walk off between the light and the microwave. They are also relatively insensitive to the frequency of the light and their RCs and characteristic impedances do not change under illumination. On the other hand, the performance of electroabsorption modulators is very sensitive to the wavelength of the light and their time constants and characteristic impedances are affected by absorption. However, they can be made in much smaller sizes than the electro-optical modulators.

In most cases where one wishes to construct an electro-optic modulator from semiconductor materials, some electroabsorption cannot be avoided. This leads to slower response speeds, because the capacitance of the structure increases as electron-hole pairs (EHPs) are optically excited, as well as higher than expected attenuation. Particularly, the presence of impurity levels in the band gap can considerably contribute to the electroabsorption. In this article we analyze the performance of a Al,Ga_{1-x},As/GaAs optical modulator based on the above considerations.

II. THEORETICAL CONSIDERATIONS
A typical semiconductor-based Mach-Zehnder electro-optic modulator is depicted in Figure 1(a) [2]. In this device, the integrated optical waveguide separates into two parallel branches which form the arms of the interferometer. Electrodes situated in a push-pull configuration produce the electric fields which rotate the polarization vector of the light and change its phase (the electro-optic effect) in the two arms. When the light that is traveling through these two arms is recombined, due to mode conversion, its intensity is modulated.

A cross-sectional schematic through the parallel branches [Figure 1(b)] shows the epitaxial structure that constitutes the waveguide. It consists of three layers of Al,Ga_{1-x},As grown on a semi-insulating GaAs substrate. The middle AlGaAs layer acts as the guiding channel for the light and the upper and lower layers of the AlGaAs act as cladding. The refractive indices of different AlGaAs layers are tailored by adjusting the molar ratio of the Al to Ga. The higher concentration of aluminum results in lower index of refraction. To minimize

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addition, the lower layer also isolates the optical field from the free-carrier absorption. All these layers are undoped. In short, at photon energies near the band-gap energy of the GaAs substrate which has a higher refractive index than the optical channel, two-dimensional waveguides are formed by etching ridges in the upper cladding layer, which increases the effective index of refraction in the region beneath it. The epitaxial layer thickness and ridge dimensions, shown in Figure 1(b) were chosen to produce single mode guides [3]. Figure 2(a) schematically shows ideal electro-optic modulator.

The induced phase shift in the electro-optic effect is linearly proportional to the electric field \( E \) and the interaction length \( (Z) \) [5]: \( \Theta \propto n_f r_1 E Z \) (where \( n_f \) is the refractive index; \( r_1 \), the electro-optic coefficient, for GaAs is \( 1.1 \times 10^{-12} \text{ m/V} \)). Therefore, at photon energies near the band-gap energy of the waveguide, the electro-optic effects are quite small compared to the electroabsorption which manifests itself through the exponential dependence on the absorption coefficient \( \alpha \): \( I(z) = I_0 e^{-\alpha z} \) [where \( I(z) \) is the transmitted light power at position \( z \); \( I_0 \) is the input power]. Depending on the photon energies, \( \alpha \) depends on the band structure (band gap), and the applied electric field (this dependence has a form of \( E_{\text{abs}} - E \)) as discussed earlier). The electroabsorption, then, with the exponential dependence on the electric field, can overwhelm the electro-optic effect. When electroabsorption occurs, the absorbed light generates electron-hole pairs (EHP).

Therefore, the capacitance and the resistance of the structure changes under illumination. The change is intensity and frequency dependent.

Figure 2(b) shows the band diagram of an \( n \)-type semiconductor used in metal-insulator-semiconductor electroabsorptive modulator and Figure 2(c) after the interface. The analysis directly applies to \( p \)-type semiconductors as well. The modulating electric field, when it is positive, results in accumulation at the surface, and when it is negative, it results in depletion at the surface. The band bending is exponential in accumulation and it has square-root dependence in depletion. This yields different probabilities of light absorption, through the Franz-Keldysh effect [4], under accumulating and depleting electric fields. Also, high carrier concentration reduces the refractive index, which results in a shift in the confinement of the light. The shift is away from the interface under accumulation and it is toward the interface under depletion.

When an insulator is not used between the semiconductor and the metal electrode, accumulating electric fields result in large current conduction and cannot be used. Thus, in Schottky diode structures only depleting electric fields are used. This is a serious drawback since a depleting dc bias voltage should be applied to prevent forward conduction by a microwave. Under reverse bias, dark current flows through the diode, and depending on the heterostructure quality and the magnitude of the reverse bias, the dark current changes as a function of time, deteriorating the modulator performance.

The second problem is generation of photocurrent, which increases the power consumption of the device. The photocurrent is generated due to EHP generation and clearly it is light-intensity and frequency dependent. Any impurity levels in the band gap will contribute to the current in two ways: (i) they increase the dark current, and (ii) they modify the carrier lifetime modifying the photocurrent. The most important factor determining the response time, however, is the capacitance associated with the depletion width in the waveguide and the series resistance. The capacitance is voltage, light-intensity, and frequency dependent. As light is absorbed, the width of the depletion region becomes smaller, increasing the capacitance.

Using the above considerations, we proceed to determine the frequency characteristics of depletion capacitance of a Schottky diode when the optical generation rate and trap density are nonzero. The electric field dependence of \( g_{\text{op}} \) can be estimated as follows. First, it is easily shown that for unity quantum efficiency (i.e., one electron-hole pair per absorbed photon) the average number of EHPs generated per unit volume per second is given by \( g_{\text{op}} = \frac{1}{y} \frac{1}{L h \nu} \int \frac{I_0 \text{d}x}{V} \), where \( V \) is the volume, \( L \) is the interaction length, \( h \nu \) is the photon energy, and \( I_0 \)'s are as defined before). Assuming a unit area and small \( \alpha \) (for below band-gap illumination), it is easy to show that \( g_{\text{op}} \) is proportional to \( \alpha \) (\( g_{\text{op}} = \alpha n/2 \)), where \( n \) is the average number of electron-hole pairs generated per unit area per second). According to the Franz-Keldysh effect, the electric field dependence of the absorption coefficient is given by \( \alpha = (KE/\Delta E) \exp(-C(\Delta E)^{1/2}/E) \) (where \( K \) and \( C \) are...
material constants and $\Delta E = E_e - h\nu$). Using the numerical values of the constants in GaAs, and for large fields ($E/4.74 \times 10^4 > 1$), we get $g_{op} = 1.24 \times 10^{-2} nE$.

Next, using the semiconductor constitutive equations in one dimension $(x)$ in $n$-type materials, and using the above $g_{op}$, we arrive at the following well-known linearized fourth-order partial differential equation for the potential $V$ inside the semiconductor:

$$
\frac{d^4V}{dx^4} - \frac{1}{\tau D} + i\omega D \frac{d^2V}{dx^2} - q\alpha/2\varepsilon D \frac{dV}{dx} = 0. \quad (1)
$$

where $\rho$ is the charge density, $\varepsilon_s$ is the dielectric constant of the semiconductor, $n$ is the free carrier density, and $\Delta n$ is the excess carrier density. Moreover, $\tau$ is the carrier recombination lifetime, $J_s$ is the current density, $E_s$ is the electric field, and $N_D$ is the doping concentration (all ionized: $N_D = N_D^0$). The direction $x$ is shown in Figure 1(b). In deriving the above equation, it is also assumed that the potential carrier density has a $e^{i\omega t}$ time dependence ($\omega$ is the radial frequency of the modulating microwave). Assuming that the position dependence of the potential is of the form $e^{i\omega t}$. $\gamma$'s are given by the roots of the following algebraic equation:

$$
\gamma^3 - \frac{1}{\tau D} + i\omega D + q\mu N_D/\varepsilon_s D \gamma - q\alpha/2\varepsilon, D = 0. \quad (2)
$$

In general the potential $V$ is given by

$$
V(x) = \sum_{i=1}^{3} V_i e^{i\gamma x} \quad (3)
$$

where $V_i$'s are determined from the boundary conditions.

The following values, which are typical in GaAs at room temperature $[4]$, are used in solving for $\gamma$'s: $\tau = 1 \times 10^{-9}$ sec, $D = 100$ cm$^2$/sec, $\varepsilon_s = 13 \times 8.854 \times 10^{-14}$ F/cm, $N_D = 10^{15}$ cm$^{-3}$, $\Delta E = 20$ meV, $q = 1.6e - .19$ coulomb, $k_B T/q = 0.0259$ eV ($k_B$ is the Boltzmann constant, and $T$ is temperature in degrees Kelvin), and $D/\mu = k_B T/q$. The values in AlGaAs, with low concentration of Al, are close to the above values, which are more exactly known in GaAs. For these values, one of the roots ($\gamma_1$) has a positive real part. Therefore, $V_i = 0$ for $V$ to stay bounded as $x$ becomes large.

The ability of a modulator to properly modulate the light is closely related to the ability of an externally applied signal to modulate the potential $V(x)$ inside the semiconductor. In Figure 3, $\gamma_2$ and $\gamma_3$ as a function of frequency and $n$ (photons/sec cm$^2$). (b) $\gamma_2$ and $\gamma_3$ as a function of frequency and carrier lifetime $\tau$ (sec) in GaAs shorter $\tau$ results in wider bandwidths but smaller $\gamma_2$ with $\gamma_3$ being nearly zero. Smaller $\gamma_2$ results in a potential that decays much faster inside the semiconductor. This in turn results in narrower space charge region where the gradient of the potential is not negligible.

The capacitance of the structure is approximately proportional to the inverse of the space charge width. As $\tau$ decreases or as $n$ increases, the capacitance increases. If the response of the modulator is limited by the RC of the structure, larger capacitance results in larger RCs and, hence, smaller bandwidths.

III. EXPERIMENTAL RESULTS

The design and fabrication of traveling-wave Mach-Zehnder configuration electro-optic modulator, shown in Figure 1(a), has been reported elsewhere $[1, 2]$. Fiber optics were used to couple light in and out of the modulator. Optical coupling was accomplished by butt coupling from a single mode fiber pigtailed to a laser diode (Ortel LD-620s, peak wavelength of $10^6 (1000 \times 1000) \mu$m$^2$. With $n = 10^{22}$ photons/sec cm$^2$, and the rest of the parameters as given above. $\gamma$ versus $\log(f)$ plots are generated with $\tau$ as a variable as shown in Figure 4. It is interesting to note that
of 826.6 mm ~ 1.5 eV). The end facets of the modulator were prepared by cleaving; no antireflection coatings were applied. The output was monitored by an IR-sensitive camera and/or an optical power meter during alignment.

Measurements with zero applied voltage showed that the insertion loss was approximately 24 dB; this includes losses from: (1) Fresnel reflection, (2) mode mismatching between the fiber and the waveguide, and (3) absorption and scattering within the waveguide which includes losses at bends and the Y branch. The modulator 3-dB bandwidth was experimentally measured to be 0.5 GHz [2]. The modulator was designed to have an 11-GHz bandwidth.

The observed transmitted optical intensity and the calculated \( \cos^2 \phi \) intensity, expected for electro-optic modulation, as a function of applied voltage is shown in Figure 5. The observed intensity versus voltage behavior does not match the \( \cos^2 \phi \) behavior, but more closely resembles a continuous exponential decrease. Observations on straight sections of waveguide (i.e., without an interferometer configuration) showed a similar decrease in intensity with applied voltage.

Spectroscopy was performed on the waveguides, and Figure 6 shows the observed transmission through the waveguide as a function of wavelength for applied voltages of 0, 10, and 20 V. The application of a voltage shifts the absorption edge from 814 nm (1.523 eV) at 0 V to 821 nm (1.510 eV) at 20 V, a shift of 0.013 eV. The transmission drops off at higher wavelengths partly due to waveguide cutoff and partly due to somewhat lower output of the monochromator and lower detection efficiency of the detector at larger wavelengths.

### IV. DISCUSSION

According to Figure 6, the absorption edge at \( V = 0 \) is around 814 nm (1.52 eV). The relationship between the \( E_x \) and the composition index \( y \) when \( 0 < y < 0.35 \) is \[ E_x = 1.424 + 1.247y \] (eV). The 1.52-eV absorption edge means that the effective \( y \) is around 0.08 (8% Al) instead of the expected value of 0.1 (10% Al). This discrepancy can also be caused by a nonzero internal electric field when \( V = 0 \). From the position of the laser diode at 826 nm (1.501 eV) it is obvious that the applied voltage significantly increases the absorption. From Figures 5 and 6 it is clear that the observed intensity modulation with applied voltage is due to electroabsorption.
Any change related to the electro-optic effect is rendered unobservable by the much larger absorption effect.

To determine the bandwidth of the modulator, we note that as the light is absorbed in the Al,Ga,As layer, EHPs are generated. In the presence of an electric field, EHPs are spatially separated. Since this layer has lower Al concentration than the adjacent layers, its band gap is lower. Thus, it can contain the EHPs forming a two-dimensional low-resistivity layer. This sheet of charge provides a relatively good conducting layer. Therefore, the effective distance between the metallic electrodes is shortened and the capacitance between them is increased. Assuming that the top Al,Ga,As layer is semi-insulating, the characteristic impedance of the electrodes and the modified structure is calculated, using standard microwave programs to be 2.31 Ω. With such a large mismatch between the line impedance (50 Ω) and the modulator. With such a large mismatch between the line impedance (50 Ω) and the modulator impedance, most of the microwave power is reflected. Only at relatively low frequencies is the transmitted microwave able to modulate the potential inside the waveguide to any appreciable width. This is discussed in the previous section.

In terms of lumped parameters, the capacitance per unit area is 1.15 nF/cm² ( = ε0/2ε0, d = 0.5 µm, and ε0 = 13 x 8.854 x 10⁻¹²), which results in an RC of 1.15 x 10⁻¹⁹ sec (f = 0.87 GHz). This is in good agreement with the experimentally observed bandwidth of our modulator.

V. CONCLUSION

In semiconductors the Franz-Keldysh effect, which results in an increase in optical generation rate, can increase the capacitance of the structure, lowering the bandwidth of the modulator. The effects that are discussed here can also be incorporated to increase the figure of merit, for example, by including the effect of optical generation rate, and hence the excess carrier generation on the refractive index change. This also suggests the possibility of using a second light beam to modulate light with an applied electric field as an adjustable variable that determines the coupling between the two light beams through the band bending. It can also be concluded that by incorporating an insulator (a semiconductor with a large band gap) between the metallic electrode and the channel [5, 6], the capacitance of the electroabsorptive modulator can be kept low at a reasonable value under the worst conditions.

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SECTION TWO

SEMICONDUCTOR MATERIAL CHARACTERIZATION
Ellipsometric characterization of $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ and of modulation doped field effect transistor structures on InP substrates

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The dielectric function of a thick layer of $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ lattice matched to InP was measured by variable angle spectroscopic ellipsometry in the range 1.9–4.1 eV. The $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ was protected from oxidation using a thin $\text{In}_{0.53}\text{Ga}_{0.47}\text{As}$ cap that was mathematically removed for the dielectric function estimate. The $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ dielectric function was then verified by ellipsometric measurements of other $\text{In}_{0.53}\text{Ga}_{0.47}\text{As}/\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ structures, including modulation doped field effect transistors (MODFET), and is shown to provide accurate structure layer thicknesses.

In this letter, we present a measurement of the dielectric function of $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ and apply it to the ellipsometric characterization of $\text{In}_{0.53}\text{Ga}_{0.47}\text{As}/\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ heterostructures. The main application of $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ is as a high band gap semiconductor in $\text{In}_{0.53}\text{Ga}_{0.47}\text{As}/\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ heterostructures lattice matched to InP, which are used in a variety of microwave and optical applications. An important property of $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ is the fact that, unlike InP, it can be grown in thin film form by solid molecular beam epitaxy (MBE), as opposed to phosphorus containing III-V semiconductors which require gas sources. Important parameters for any applications that can be measured by ellipsometry are the thicknesses of the layers, interface quality, and surface contaminations, roughness and oxidation. In addition, the dielectric function of $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ in the visible may be useful in applications involving waveguides in this spectral range.

Ellipsometry, particularly variable-angle spectroscopic ellipsometry (VASE) in the visible and near UV, has been used to characterize, nondestructively, a variety of modulation doped field effect transistors (MODFETs) and optoelectronic structures grown on GaAs substrates. Dielectric functions of the constituents necessary for the ellipsometric analysis were taken from the literature. However, at this time no reliable experimental dielectric function of $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ has been published. Ellipsometry has been used twice in the past to obtain the dielectric function of $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ in the visible. In Ref. 5, only results for the refractive index were published, while in Ref. 6, the dielectric function of $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ was estimated by scaling the InP values and using an effective medium model with a 3% negative voids fraction. Clearly, a direct experimental dielectric function for $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ is preferable.

In most aluminum containing III-V semiconductor ternaries, the top layer of the material will oxidize in air in a time scale of hours. As ellipsometry is very sensitive to the surface conditions, we protected the top layer with $\text{In}_{0.53}\text{Ga}_{0.47}\text{As}$. We kept the thickness of this cap layer to a minimum in order to get reliable results for the $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ dielectric function in the near UV, where the light penetration depth is very small. As a check of the accuracy of our result, we used our experimental $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ dielectric function to fit two other $\text{In}_{0.53}\text{Ga}_{0.47}\text{As}/\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ structures using two parameter fits only. Finally, we used our result to analyze five MBE grown $\text{In}_{0.53}\text{Ga}_{0.47}\text{As}/\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ complete MODFET structures. The MODFETs were grown at two laboratories to make sure that no systematic error in the analysis was carried over from a systematic error in the growth parameters of one group.

All samples, except three MODFETs, were grown at the University of Michigan. The $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ growth temperature used was the optimum value of 520°C that was found to result in smooth films with the least amount of clustering. Some of the MODFET structures were grown at 500°C. The growth rate was in the range 0.6–1.2 µm per hour. The ellipsometric measurements were taken at 3–7 angles of incidence in the range 300–750 nm (i.e., spectral range with reasonable experimental reflectivity) with 10 nm increments. The calibration sample was measured in 5 nm increments for better resolution. Marquardt least square fits were used to estimate the desired parameters.

The calibration sample was a 1-µm-thick $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ on top of a 30 period 3 nm/3 nm $\text{In}_{0.53}\text{Ga}_{0.47}\text{As}/\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ buffer. For ellipsometry purposes, the $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ was treated as the substrate, assuming it to be optically thick. The free parameters of the model were the oxide and cap layer thicknesses and the values of the $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ dielectric function at all experimental wavelengths. The calibration functions for the oxide were taken from the literature. The resulting $\text{In}_{0.52}\text{Al}_{0.48}\text{As}$ dielectric function $\varepsilon$ is shown in Fig. 1. The values of the dielectric function for energies below 1.9 eV ($\lambda > 650$ nm) are not as accurate as those above that energy due to the light penetrating into the superlattice region. Conventionally, a layer is considered optically thick if its thickness is greater than 2$\delta$, where $\delta$ is the light

obtained a mean square error (MSE) for the tan α and oxide thickness and a nominal 2 nm In0.52Al0.48As cap layer and use a 36° cutoff criterion. The ellipsometric result also provided best fit values of 2.2 nm of oxide and 1.3 nm of In0.53Ga0.47As cap. We obtained a mean square error (MSE) for the tan α and the penetration depth. We choose to be more conservative and E2 are the real and imaginary parts of the dielectric function, respectively.

The values of the MSE for these two parameter fits, especially for sample A, are extremely good. In both cases, the ln

FIG. 1. Dielectric function ε of In0.52Al0.48As in the range 1.9-4.1 eV. ε1 and ε2 are the real and imaginary parts of the dielectric function, respectively.

and 2) and by a commercial vendor\textsuperscript{13} (sample Nos. 3, 4, and 5). All structures had complex buffer layers. For example, the University of Michigan samples had the following layers: starting from the semi-insulating InP substrate, a 30 period 3 nm/3 nm In0.53Ga0.47As/In0.52Al0.48As buffer layer and a 400 nm undoped In0.52Al0.48As as the lower part of the conduction channel quantum well. The other samples (Nos. 3, 4, and 5) had additional layers below the 30 period lattice, but they had the same buffer structure just below the conduction channel. As the ellipsometric analysis was limited to the device active layers, the 400 nm In0.52Al0.48As layer was regarded as substrate. Thus, we limited our analyses to wavelengths below 540 nm. The layer thicknesses, as estimated by RHEED, are given in Table II. In all samples, the active layers included an undoped In0.53Ga0.47As channel, an In0.52Al0.48As donor layer, and an In0.53Ga0.47As cap layer. The In0.52Al0.48As donor layer had a doped (5×10\textsuperscript{18} cm\textsuperscript{-3}, Si) 15 nm layer on top of a 5 nm undoped spacer. The cap layer was also n doped, at 3×10\textsuperscript{18} cm\textsuperscript{-3}, Si. In the ellipsometric model, doping effects on the dielectric function were neglected.\textsuperscript{2,3} The nominal ellipsometric models, including all layer thicknesses for the five samples, are given in Table II under the heading “Nominal.” A summary of the ellipsometric results is given in Table II under the heading “VASE.” The errors shown are the 90% confidence limits obtained from the least squares fitting.\textsuperscript{14} Representative tan α and cos Δ fit\textsuperscript{2} of 1.0×10\textsuperscript{-5}, where Δ is the ellipsometric experimental results. This exceedingly low value of MSE is due to the large number of parameters.

Next, two samples of thick In0.52Al0.48As layers were measured, both grown on InP without a superlattice buffer. Sample A had a nominal 2-µm-thick In0.52Al0.48As while sample B had a little over a 1-µm-thick layer. Both had a thicker In0.53Ga0.47As cap layer than the calibration sample. The ellipsometric model used for these samples included two parameters only, the thicknesses of the oxide and the In0.53Ga0.47As cap layer. The In0.52Al0.48As dielectric function used was the result obtained here in the first stage of the work. The results for samples A and B are summarized in Table I. The values of the MSE for these two parameter fits, especially for sample A, are extremely good. In both cases, the In0.53Ga0.47As layer thickness estimated by ellipsometry is smaller than the nominal value. We believe some of the material was oxidized and some error may be due to the growth calibration. However, we did not encounter this discrepancy in MODFET samples made at another laboratory, as will be shown below.

The MODFET structures shown in Table II were made at both the University of Michigan (sample Nos. 1

TABLE I. Best fits for layer thicknesses in nm for samples made of a thick In0.52Al0.48As layer, considered as substrate. Analysis range 300-620 nm.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Oxide</th>
<th>In0.53Ga0.47As</th>
<th>In0.52Al0.48As</th>
<th>In0.53Ga0.47As</th>
<th>MSE\times10\textsuperscript{-4}</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>Nominal VASE</td>
<td>Nominal VASE</td>
<td>Nominal VASE</td>
<td>Nominal VASE</td>
<td>MSE\times10\textsuperscript{-4}</td>
</tr>
<tr>
<td>B</td>
<td>Nominal VASE</td>
<td>Nominal VASE</td>
<td>Nominal VASE</td>
<td>Nominal VASE</td>
<td>MSE\times10\textsuperscript{-4}</td>
</tr>
</tbody>
</table>

TABLE II. Best fits for In0.53Ga0.47As/In0.52Al0.48As MODFET layer thicknesses (in nm). Analysis wavelength range 300-405 nm. 400 nm In0.52Al0.48As layer used as substrate.

<table>
<thead>
<tr>
<th>Sample number</th>
<th>Oxide</th>
<th>In0.53Ga0.47As Cap layer</th>
<th>In0.52Al0.48As Donor layer</th>
<th>In0.53Ga0.47As Channel layer</th>
<th>MSE\times10\textsuperscript{-4}</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>4.6±0.1</td>
<td>4.8±0.1</td>
<td>42.2±0.3</td>
<td>53.9±0.7</td>
<td>1.6</td>
</tr>
<tr>
<td>2</td>
<td>2.4±0.1</td>
<td>8.8±0.2</td>
<td>47.9±0.4</td>
<td>56.1±1.0</td>
<td>2.4</td>
</tr>
<tr>
<td>3</td>
<td>2.6±0.1</td>
<td>2.3±0.3</td>
<td>46.4±0.3</td>
<td>51.2±0.6</td>
<td>4.9</td>
</tr>
<tr>
<td>4</td>
<td>10.0±0.04</td>
<td>40.6±0.4</td>
<td>48.4±0.5</td>
<td>54.1±1.4</td>
<td>0.7</td>
</tr>
<tr>
<td>5</td>
<td>1.4±0.1</td>
<td>30.2±0.5</td>
<td>43.4±1.1</td>
<td>41.5±2.1</td>
<td>2.4</td>
</tr>
</tbody>
</table>

110
model. We speculate that the problem in this sample originates from the very thin thickness of the cap layer. The In$_{0.53}$Ga$_{0.47}$As top layer may be too thin for protecting the In$_{0.52}$Al$_{0.48}$As from oxidation, and the sample model shown here did not take this into account. Oxidation problems are encountered in all thin capped MODFET structures (samples No. 1, 2, and 3), where the VASE determined In$_{0.53}$Ga$_{0.47}$As layer thickness is very small (see Table II). The large discrepancy between the nominal and the VASE thicknesses of the donor and channel layers in samples 3 and 4 as compared with that of sample 5 can be explained as follows. Sample No. 5 was grown 10 months after the other two samples. In the meantime, several improvements in the nominal thickness calibrations were implemented, including repositioning of the RHEED gun, adjusting the shutters to reduce transients, and a better correlation between RHEED results and ternary alloy thicknesses. Indeed, for sample No. 5, the nominal and VASE thicknesses are the same to within 8% for all layers.

We also analyzed all MODFET samples using the suggested In$_{0.53}$Al$_{0.47}$As dielectric function from Ref. 6. The results looked unreliable: the MSE were a factor of 5 to 18 higher for the thin In$_{0.53}$Ga$_{0.47}$As capped samples; there was no consistency between sample Nos. 3 and 4; and most thicknesses were far away from the nominal values.

In summary, we have experimentally determined the dielectric function of In$_{0.53}$Al$_{0.47}$As in the range 300–650 nm and have successfully applied it in the determination of the active layers’ thicknesses of MODFET devices lattice matched to InP grown by MBE. This ellipsometric nondestructive characterization of high performance MODFET’s that include In$_{0.53}$Al$_{0.47}$As layers not only provided a confirmation of the nominal layer thickness values, but also identified problems in thickness calibrations during growth, as well as cap layer oxidation problems.

We would like to thank W. Weisbecker and L. W. Kapitan from Quantum Epitaxial Design, Inc., for making three samples and for sending private communication on their system improvements, and to D. E. Aspnes for supplying us with his In$_{0.53}$Ga$_{0.47}$As results in a digital form.

1See, for example, Proceedings of the Third International Conference on InP and Related Materials (IEEE, New York, 1991).

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15Quantum Epitaxial Design, Bethlehem, PA. 18015.
17L. W. Kapitan (private communication).
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Ellipsometric study of metal–organic chemically vapor deposited III–V semiconductor structures

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Abstract

Metal–organic chemical vapor deposition was used to grow epitaxial layers of AlGaAs, GaAs and InGaAs on semi-insulating GaAs substrates. The ternary composition of the thick layers was determined by double-crystal X-ray diffraction (DCXRD). Variable angle spectroscopic ellipsometry was used to characterize several types of structures including relaxed single-component thick films and strained lattice multilayer structures. The thick film characterization included ternary alloy composition as determined by a numerical algorithm and interface quality. The results for the alloy composition were equal to the DCXRD results, to within the experimental errors except for the top layer of a thick AlGaAs film. The strained layer multistructures were analyzed for all layer thicknesses and alloy compositions. For most layers, the thickness was equal to the nominal values, to within the experimental errors. However, in all three In_{0.3}Ga_{0.7}As samples, the indium concentration estimated from the relaxed layer's InGaAs algorithm was around 21%, i.e. much lower than the nominal value. This result indicates a shift in the critical points of the dielectric function, owing to strain effects.

1. Introduction

The most common technique of growing epitaxial III–V semiconductors films on III–V substrates is by molecular beam epitaxy (MBE). However, the technique of metal organic chemical vapor deposition (MOCVD) is more versatile than MBE, as it can be used to grow a larger selection of group V materials, e.g. phosphorus. In addition, MOCVD can produce film growth on several wafers concurrently compared with a single wafer in MBE. The materials of interest in this study are AlGaAs, InGaAs and GaAs, as they are needed to grow the multistucture needed to produce modulation-doped field effect transistors (MODFETs). This MODFET device was developed by MBE in the mid-1980s [1]. MOCVD is being used to grow strained layer InGaAs on GaAs [2, 3] but MOCVD growth of the combination of a AlGaAs layer adjacent to strained InGaAs is not common. The commercial applications of this MODFET are widespread [4], especially for materials grown on GaAs substrates. The conduction channel, made of InGaAs, is under strain. However, if the thickness of the channel is below a critical thickness \( h_c \) [5], the strained layer grows pseudomorphically on GaAs. These strain effects have essentially no effect on the electrical properties of the MODFET, but they can be important for optoelectric applications [6].

The most common technique to calibrate a MOCVD reactor for growth rate and alloy composition is to measure mechanically or by microscopy the layer thickness and to use double-crystal X-ray diffraction (DCXRD) for composition. However, DCXRD needs a relatively thick layer of material to give a reliable value of alloy concentration. A much larger thickness is needed to assume a strain-free layer and to avoid corrections to the X-ray results, as a result of strain.

In this paper we will show several ways that ellipsometry can be used to help in calibrating the MOCVD growth parameters. We will also show instances in which ellipsometry was able to pinpoint problems in the layer composition or interfaces. In addition, a quantitative measure of the strain effect on the dielectric function of In_{0.3}Ga_{0.7}As will be estimated.
2. Experimental details

All samples were grown by MOCVD at Spire Corporation, on semi-insulating GaAs(001) substrates, using low pressure MOCVD in an SPI-MO CVD™450 reactor. The growth temperature and pressure used for all samples were 650 °C and 53 Torr respectively. Source reagents used for these layers include trimethylgallium, trimethylaluminum, and 100% arsine (AsH₃) with a palladium-diffused hydrogen carrier gas. Two sets of samples were selected for ellipsometry work: (a) thick films; (b) MODFET structures. In set a, two aluminum gallium arsenide (AlₓGa₁₋ₓAs) films were supplied from the same run (M4-2128) with an aluminum molar fraction of 18% (averaged over both samples) as measured by DCXRD. The AlₓGa₁₋ₓAs film thickness was 8500 Å; the growth rate for this layer was 2.6 Å s⁻¹. The AlₓGa₁₋ₓAs was protected by a thin (50 Å) GaAs cap. Two aluminum arsenide (InₓGa₁₋ₓAs) compositions were calibrated for Y by DCXRD. The first, M4-2093-2 has an indium concentration of 25.6% and was grown at a rate of 3.5 Å s⁻¹ for a total thickness of 1.75 µm. M4-2116-2 is a 1.8 ptm film of InGaAs with 30% In concentration; the growth rate for this layer was 2.6 As⁻¹. The AlₓGa₁₋ₓAs was protected by a film thickness of 8500 Å; the growth rate for this layer was 2.6 Å s⁻¹. The AlₓGa₁₋ₓAs was protected by a thin (50 Å) GaAs cap. Two aluminum arsenide (InₓGa₁₋ₓAs) compositions were calibrated for Y by DCXRD. The first, M4-2093-2 has an indium concentration of 25.6% and was grown at a rate of 3.5 Å s⁻¹ for a total thickness of 1.75 µm. M4-2116-2 is a 1.8 µm film of InGaAs with 30% In concentration; the growth rate for this composition was slightly higher at 3.5 Å s⁻¹. Set b contains three samples. All have the nominal structure given in Fig. 1, but with slight differences. Two of the samples have a 100 Å InGaAs channel, while one has a 50 Å channel. Also, one sample had originally a 300 Å GaAs cap layer. Some variations in the buffer among the samples were also present, but their thickness was always 1 µm with at least 9000 Å of GaAs. As ellipsometry cannot distinguish easily between doped and undoped material, we show in Fig. 1 also the initial model for ellipsometric purposes.

The ellipsometric technique was described previously [7] and will only briefly be described here. In order to increase accuracy, many measurements were made using two-zone averaging [8] and/or estimating the angle of incidence by using a known sample (GaAs wafer in this case) and obtaining the correct angle by least-squares analysis. We found these corrections to be very small. A model calculation of the ellipsometric parameters tan Ψₜ, cos Δₜ was least-squares fitted to the experimental tan Ψₑ, cos Δₑ, using the Marquardt algorithm to minimize the mean square error σ;

\[
\sigma = (N - P)^{-1} \sum \left( \tan \Psi_{e,i} - \tan \Psi_{t,i} \right)^2 + \left( \cos \Delta_{e,i} - \cos \Delta_{t,i} \right)^2
\]

Here \( N \) is the number of experimental points and \( P \) is the number of free parameters in the model. Data at all relevant experimental angles of incidence and wavelengths are included. The dielectric functions of AlₓGa₁₋ₓAs for any value of the aluminum concentration \( X \) were calculated using the numerical algorithm and the critical points given in ref. 10. The functions needed for InₓGa₁₋ₓAs for all \( Y \) values were calculated using a numerical algorithm similar to that of ref. 10, but using the following critical points (in electron-volts): from ref. 11: \( E_0(Y) = 1.424 - 1.53Y + 0.45Y^2; E_1(Y) \) was taken as a linear approximation between GaAs and the experimental results [12] at \( Y = 0.3, E_2(Y) = 4.8. \) In this numerical calculation we found that very little difference was introduced in the dielectric functions if the \( E_1 \) critical point was exchanged with almost equal energy value of the peak in \( E_1 \), which is much easier to deduce from the experimental result in ref. 12.

3. Results and discussion

All four thick samples were measured as received, in the wavelength range 3200–7500 Å at five angles of incidence each (around 75°). Results for the two InGaAs samples are given in Table 1. As these films were over 1.75 µm thick, we could not penetrate the thickness of the film. Thus we had only two parameters, the top oxide film thickness and the indium molar concentration \( Y \). In Table 1 we show two results for sample M4-2093-2. In the second measurement the value of \( \sigma \) has improved by a factor to 2.5 because of a better angle of incidence definition obtained from measurement of a GaAs wafer.

The results for \( Y \) are basically equal to the experimental DCXRD data, to within both techniques' experimental error, indicating the reproducibility of our results compared with the sample in ref. 12 and the validity of the algorithm. The excellent values for \( \sigma \)

<table>
<thead>
<tr>
<th>NOMINAL STRUCTURE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nominal Structure</td>
</tr>
<tr>
<td>Nominal Structure for Ellipsometry</td>
</tr>
<tr>
<td>t₁</td>
</tr>
<tr>
<td>n GaAs</td>
</tr>
<tr>
<td>300 Å</td>
</tr>
<tr>
<td>n AlₓGa₁₋ₓAs</td>
</tr>
<tr>
<td>i AlₓGa₁₋ₓAs</td>
</tr>
<tr>
<td>100 Å</td>
</tr>
<tr>
<td>i InₓGa₁₋ₓAs</td>
</tr>
<tr>
<td>100 Å</td>
</tr>
<tr>
<td>Buffer</td>
</tr>
<tr>
<td>SI GaAs Substrate</td>
</tr>
</tbody>
</table>

Fig. 1. Nominal structure used for ellipsometry compared with the actual nominal structure. The ternary concentrations \( X \) and \( Y \) are variables in the ellipsometric analysis.
TABLE 1. Best fits for In, Ga, As thick layers, wavelength range 3200–7500 Å

<table>
<thead>
<tr>
<th>Nominal</th>
<th>Best fit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Oxide thickness</td>
<td>--</td>
</tr>
<tr>
<td>In concentration (%)</td>
<td>25.6</td>
</tr>
<tr>
<td>σ</td>
<td>6.4 x 10^{-4}</td>
</tr>
</tbody>
</table>

Oxides denote a smooth film and reliable parameter values. The results for the two AlGaAs films are given in Table 2. Here $t_1 (\text{Å}), t_2 (\text{Å})$ and $t_3 (\text{Å})$ are the oxide, GaAs and AlGaAs thicknesses respectively and $X(\%)$ is the aluminum molar concentration. Comparison of experimental and calculated tan $\Psi$ and cos $\Delta$ for sample M4-2128-3 before etching are shown in Fig. 2. An $\text{H}_3\text{PO}_4:\text{H}_2\text{O}_2:\text{H}_2\text{O} (3:1:75)$ etch was performed on each sample independently. This etch can remove both GaAs and AlGaAs material. After the etch, the samples were measured in a dry nitrogen environment at an angle of incidence of 75°, with two-zone averaging. Two measurements were made on each sample, one immediately following the etch, the other 3 h later. Absolutely no change was observed as a function of the measurement delay time. Table 2 shows that, with the etch, the top oxide layer thickness increased and the AlGaAs thickness decreased as expected. We see two problems with the results in Table 2: the large values of $σ$ compared with Table 1 and the extremely small values of GaAs thicknesses $t_2$ before etch. In addition, the fits given in Fig. 2 reveal very systematic discrepancies between the calculated and the experimental tan $\Psi$ and cos $\Delta$ values in the wavelength range below 5000 Å, i.e. near the surface.

In order to clarify this last problem, we made fits of the data in the range 3200–5500 Å. The results are shown in Table 3. Here $t_4$ is the thickness of an interface layer of $\text{Al}_{0.2}\text{Ga}_{0.8}\text{As}$ with $f_i(\%)$ being the volume fraction of $\text{Al}_2\text{O}_3$. The very small amount of $\text{Al}_2\text{O}_3$ could have been formed either by the aluminum gettering action during deposition or by post-deposition oxidation from the air, through the very thin GaAs cap layer. The penetration depth of light in $\text{Al}_{0.2}\text{Ga}_{0.8}\text{As}$ in this range is always below 2000 Å. Thus, it turns out that the parameter $t_1$ of Table 2 cannot be estimated accurately from results in this restricted wavelength range, and therefore the $\text{Al}_{0.1}\text{Ga}_{0.9}\text{As}$ was treated as a substrate. The most important result from Table 3 is that, before the etch, the top layer of the 8500 Å thick AlGaAs film does not behave like $\text{Al}_{0.2}\text{Ga}_{0.8}\text{As}$, irrespective of the interface model or the quality of fit. It seems that a long MOCVD growth of AlGaAs followed by GaAs gives a poor quality interface layer, showing up in ellipsometry by a larger aluminum concentration in the top layer than in the bulk of the film and a small amount of $\text{Al}_2\text{O}_3$. The etch depth of sample M4-2128-1 was about 125 Å (from Table 2), while that of sample M4-2128-3 was about 225 Å. From Table 3 we see that the $X$ value is reduced with etching, with higher reduction for deeper etch. An approximately 225 Å etch was required to obtain the same quality AlGaAs at the top and bottom interfaces. Then, the ellipsometrically determined values of $X$ for all wavelength range analyses are in excellent agreement with the DCXRD value. This result shows that, except for the top approximately 200 Å layer, the AlGaAs film is of good quality, with the aluminum concentration constant over all the film thickness. We have also performed best fits for the wavelength range 5600–7500 Å. In these cases we always obtained results for $X$ and $σ$ similar to those in Table 2. The large value of $σ$ is probably due to inhomogeneities in the very thick AlGaAs film. This can be seen from the resonances above 6000 Å in Fig. 2, where the experimental and the calculated functions

TABLE 2. Best fits for Al, Ga, As thick films, wavelength range 3200–7500 Å

<table>
<thead>
<tr>
<th>Sample</th>
<th>Etch</th>
<th>$σ$</th>
<th>$t_1 (\text{Å})$</th>
<th>$t_2 (\text{Å})$</th>
<th>$t_3 (\text{Å})$</th>
<th>$X (%)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>M4-2128-1</td>
<td>Before</td>
<td>2.32 x 10^{-3}</td>
<td>13.8 ± 0.7</td>
<td>0.8 ± 2.8</td>
<td>8515 ± 9</td>
<td>20.0 ± 0.1</td>
</tr>
<tr>
<td>M4-2128-1</td>
<td>After</td>
<td>3.23 x 10^{-3}</td>
<td>32.6 ± 1.6</td>
<td>2.5 ± 2.5</td>
<td>8745 ± 9</td>
<td>19.7 ± 0.1</td>
</tr>
<tr>
<td>M4-2128-3</td>
<td>Before</td>
<td>1.87 x 10^{-3}</td>
<td>12.2 ± 0.8</td>
<td>2.5 ± 2.5</td>
<td>8521 ± 10</td>
<td>18.1 ± 0.2</td>
</tr>
<tr>
<td>M4-2128-3</td>
<td>After</td>
<td>1.52 x 10^{-3}</td>
<td>23.9 ± 0.7</td>
<td>23.9 ± 0.7</td>
<td>8521 ± 10</td>
<td>18.1 ± 0.2</td>
</tr>
<tr>
<td>Nominal values</td>
<td></td>
<td></td>
<td>50</td>
<td>8500</td>
<td>18</td>
<td></td>
</tr>
</tbody>
</table>
Fig. 2. Experimental and model calculated values for (a) tan ψ and (b) cos Δ vs. wavelength at three angles of incidence for sample M4-2128-3 before etching.

TABLE 3. Best fits for AlGaAs thick films, wavelength range 3200–5500 Å

<table>
<thead>
<tr>
<th>Sample</th>
<th>Etch</th>
<th>σ</th>
<th>t₁ (Å)</th>
<th>t₂ (Å)</th>
<th>t₃ (Å)</th>
<th>f₁ (%)</th>
<th>X (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>M4-2128-1</td>
<td>Before</td>
<td>1.8 × 10⁻⁴</td>
<td>15.8 ± 0.3</td>
<td>26.0 ± 1.0</td>
<td>—</td>
<td>—</td>
<td>28.8 ± 0.4</td>
</tr>
<tr>
<td>M4-2128-1</td>
<td>Before</td>
<td>7.3 × 10⁻⁵</td>
<td>18.3 ± 0.6</td>
<td>13.1 ± 1.4</td>
<td>78 ± 7</td>
<td>0.8 ± 0.3</td>
<td>30.2 ± 0.5</td>
</tr>
<tr>
<td>M4-2128-1</td>
<td>After</td>
<td>6.6 × 10⁻⁵</td>
<td>31.2 ± 0.3</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>26.2 ± 0.4</td>
</tr>
<tr>
<td>M4-2128-3</td>
<td>Before</td>
<td>2.0 × 10⁻⁴</td>
<td>13.9 ± 0.3</td>
<td>26.3 ± 1.1</td>
<td>—</td>
<td>—</td>
<td>28.1 ± 0.5</td>
</tr>
<tr>
<td>M4-2128-3</td>
<td>Before</td>
<td>9.3 × 10⁻⁵</td>
<td>13.6 ± 0.6</td>
<td>14.6 ± 1.6</td>
<td>75 ± 8</td>
<td>0.7 ± 0.4</td>
<td>29.5 ± 0.6</td>
</tr>
<tr>
<td>M4-2128-3</td>
<td>After</td>
<td>8.5 × 10⁻⁵</td>
<td>22.1 ± 0.2</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>20.5 ± 0.3</td>
</tr>
</tbody>
</table>

Nominal values

50

18
have the same shape, but the magnitudes are a little different.

Results for the three MODFET structures are summarized in Table 4. Preliminary results were given in ref. 9, where no InGaAs algorithm was used. The nominal values were obtained from the prior calibration of deposition rates. The low aluminum concentrations in two of the samples are believed to be related to a possible problem in these particular runs. For all three samples, we found a correlation parameter \( a'_{ij} \) of 0.91–0.95 between the GaAs and the AlGaAs thicknesses. For the samples with the lower \( a'_{ij} \), i.e. MO6-332-1 and MO6-334-1, thicknesses of all layers including both InGaAs and AlGaAs are in excellent agreement with the nominal values. For sample MO6-332-1, with \( a'_{ij} = 0.95 \), the value of the sum of the GaAs and AlGaAs thicknesses is within 7% of the nominal value. For all three samples, we found a correlation parameter \( a''_{ij} \) of 0.91–0.95 between the GaAs and the A1GaAs thicknesses. For the samples with the lower \( a''_{ij} \), i.e. M06-332-1 and M06-334-1, thicknesses of all layers including both InGaAs and AlGaAs are in excellent agreement with the nominal values. For sample MO6-316-1, with \( a'_{ij} = 0.95 \), the value of the sum of the GaAs and AlGaAs thicknesses is within 7% of the nominal value. For all three samples, we found a correlation parameter \( a''_{ij} \) of 0.91–0.95 between the GaAs and the AlGaAs thicknesses. For the samples with the lower \( a''_{ij} \), i.e. M06-332-1 and M06-334-1, thicknesses of all layers including both InGaAs and AlGaAs are in excellent agreement with the nominal values.

From Table 4, the errors in \( Y \) make the results of all three samples overlap, around \( Y = 21\% \).

In order to increase our sensitivity and to decrease the 90% confidence limits on the value of \( Y \), we etched the thick GaAs layer of sample MO6-316-1 and remeasured it at five angles of incidence. An excellent result, with \( \sigma = 8 \times 10^{-5} \), was obtained using a composite top layer, with an oxide layer thickness of 34.7 ± 3.5 Å and a 72 ± 11 Å thick layer composed of a mixture of Al0.2Ga0.8As and (11 ± 4.5)% of Al1O3. The remaining structure included the AlGaAs layer with \( t_1 = 295 \pm 5.6 \) Å and \( Y = 19.8 \pm 0.4 \), and the InGaAs with \( t_4 = 94.3 \pm 5.6 \) Å and \( Y = 21.6 \pm 0.9 \). This result for \( Y \) has the lowest confidence limit. We checked the correlation of \( Y \) with the other parameters, as shown in Table 5 for sample MO6-316-1. No correlation was found, except with the InGaAs layer thickness. In all samples including the etched sample, the InGaAs thicknesses are very near to the nominal values, therefore increasing our confidence in the values of \( Y \). Thus we believe that the value of \( Y = 21\% \) for a coherently strained In0.3Ga0.7As is reliable.

This result can be explained by changes in the critical points \( E_i(Y) \), \( i = 0, 1, 2 \), with strain \( \varepsilon \). Recalling the way the InGaAs algorithm was structured, we expect \( E_i(\varepsilon) \) to change in an opposite way to \( E_i(Y) \), i.e. both \( E_0(\varepsilon) \) and \( E_2(\varepsilon) \) to increase with \( \varepsilon \), while \( E_3 \) will remain constant. The biaxial strain dependence of critical points in III–V semiconductors is treated theoretically in ref. 9 for MBE-grown samples around \( Y = 53\% \). It must be mentioned that the experimental critical thickness \( h_c \) for In0.3Ga0.7As is around 90 Å. Thus the 100 Å InGaAs layer may be more relaxed than the thinner film, and therefore the strain effect is more pronounced for the thinner film. However, as seen from Table 4, the errors in \( Y \) make the results of all three samples overlap, around \( Y = 21\% \).

### Table 4. Best fits for three modulation-doped field effect transistor structure samples, wavelength range 3500–6800 Å

<table>
<thead>
<tr>
<th>Sample</th>
<th>( \sigma )</th>
<th>( t_1 ) (Å)</th>
<th>( t_2 ) (Å)</th>
<th>( t_3 ) (Å)</th>
<th>( X ) (%)</th>
<th>( t_4 ) (Å)</th>
<th>( Y ) (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MO6-316</td>
<td>2.4 \times 10^{-4}</td>
<td>20.5 ± 0.5</td>
<td>337 ± 4</td>
<td>367 ± 6</td>
<td>19.7 ± 0.5</td>
<td>91 ± 13</td>
<td>24.1 ± 2.7</td>
</tr>
<tr>
<td>MO6-316</td>
<td>Nominal</td>
<td>—</td>
<td>300</td>
<td>450</td>
<td>20</td>
<td>100</td>
<td>30</td>
</tr>
<tr>
<td>MO6-332</td>
<td>5.2 \times 10^{-4}</td>
<td>16.3 ± 0.5</td>
<td>93 ± 3</td>
<td>437 ± 4</td>
<td>14.3 ± 0.4</td>
<td>94 ± 6</td>
<td>23.5 ± 2.1</td>
</tr>
<tr>
<td>MO6-332</td>
<td>Nominal</td>
<td>—</td>
<td>100</td>
<td>450</td>
<td>20</td>
<td>100</td>
<td>30</td>
</tr>
<tr>
<td>MO6-334</td>
<td>4.7 \times 10^{-4}</td>
<td>16.9 ± 0.5</td>
<td>99 ± 3</td>
<td>488 ± 5</td>
<td>13.7 ± 0.4</td>
<td>65 ± 14</td>
<td>18.3 ± 3.5</td>
</tr>
<tr>
<td>MO6-334</td>
<td>Nominal</td>
<td>—</td>
<td>100</td>
<td>450</td>
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<td>50</td>
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</table>

### Table 5. Best fits for modulation-doped field effect transistor structure sample MO6-334 using constant indium concentration values

<table>
<thead>
<tr>
<th>( Y ) (%)</th>
<th>( \sigma )</th>
<th>( t_1 ) (Å)</th>
<th>( t_2 ) (Å)</th>
<th>( t_3 ) (Å)</th>
<th>( X ) (%)</th>
<th>( t_4 ) (Å)</th>
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<td>15</td>
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<td>16.6 ± 0.5</td>
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<td>487 ± 5</td>
<td>13.4 ± 0.4</td>
<td>78 ± 8</td>
</tr>
<tr>
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<td>4.68 \times 10^{-4}</td>
<td>16.8 ± 0.5</td>
<td>99 ± 3</td>
<td>488 ± 5</td>
<td>13.6 ± 0.4</td>
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<tr>
<td>18</td>
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<tr>
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<td>16.9 ± 0.5</td>
<td>99 ± 3</td>
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<td>13.7 ± 0.4</td>
<td>63 ± 6</td>
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<tr>
<td>20</td>
<td>4.67 \times 10^{-4}</td>
<td>16.9 ± 0.5</td>
<td>99 ± 3</td>
<td>488 ± 5</td>
<td>13.7 ± 0.4</td>
<td>60 ± 6</td>
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<td>17.1 ± 0.5</td>
<td>100 ± 3</td>
<td>485 ± 5</td>
<td>13.8 ± 0.4</td>
<td>49 ± 5</td>
</tr>
<tr>
<td>30</td>
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<td>17.3 ± 0.5</td>
<td>100 ± 3</td>
<td>483 ± 5</td>
<td>13.9 ± 0.4</td>
<td>43 ± 4</td>
</tr>
</tbody>
</table>
in ref. 13. $E_0(\epsilon)$ is split and both $E_{0}(\epsilon)$ and $E_{1}(\epsilon)$ go up with the strain. We found out, by using several values for $E_0$ in our algorithm, that the calculated value of the InGaAs dielectric function in our experimental range is only slightly dependent on the value of $E_0$ ($E_0$ is below 1.14 eV, for $Y > 20$). Thus, the changes in $E_0$ with strain can be neglected as a first approximation for small values of $\epsilon$. $E_1$ is linear [13] for small $\epsilon$, and so is the $E_1$ dependence on the indium concentration $Y$ for coherently strained layers. Thus the strain dependence can be exchanged for composition dependence in our algorithm approximation. Therefore the measured 30% reduction in the value of $Y$ with strain, together with the assumptions of linearity, gives us a simple way to measure the correct $Y_c$ value from the measured ellipsometric result $Y_e$, using $Y_e = 0.7 Y_c$.

4. Conclusions

A two-prong ellipsometric study of MOCVD-grown layers of AlGaAs and InGaAs was performed, including thick films and strained layer complex structures. The study shows that the ternary composition of thick non-strained layers can be accurately determined to within experimental errors using numerical algorithms. In the case of complex structures, thicknesses of all layers and the alloy composition of non-strained layers can be determined simultaneously, provided that the correlations between parameters is no higher than 0.9.

The composition of strained InGaAs can be estimated from the experimental result using a correction factor based on a linear approximation of the dependence of the critical point $E_1$ on composition and strain.

References

Enhancement of Shubnikov–de Haas oscillations by carrier modulation

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(Received 16 January 1992; accepted for publication 19 May 1992)

A drastic enhancement of the Shubnikov–de Haas (SdH) pattern is obtained by recording the changes in the quantum oscillations of magnetoresistance due to modulation of the carrier concentration. The technique enables measurement of the SdH waveform at relatively high temperatures and in samples with moderate mobilities. The modulated waveform shows selective enhancement of the low-frequency SdH oscillations associated with the upper subband. Thus, we were able to record very clear oscillations generated by a carrier concentration well below $5 \times 10^{10}$ cm$^{-2}$. The theory for this selective enhancement is provided.

Several fundamental aspects concerning transport properties of carriers in a two-dimensional electron gas (2DEG) are still unresolved. As the second subband starts to be populated, does the electron concentration in the ground subband ($n_1$) continue to increase? Is the mobility of electrons in the second subband larger than that at the ground level? Does the carrier mobility drop as soon as the upper subband starts filling up or even before?

The primary techniques for determining most transport parameters are the Shubnikov–de Haas (SdH) oscillatory magnetoresistance, the Hall effect, and conductivity measurements. While the total carrier concentration $n_T$ is obtained from the Hall voltage, the frequency (in 1/B, where B is the magnetic field) of the SdH oscillation renders the electron concentration in the subbands of the 2DEG. The presence of carriers in the second subband is manifested by a superposition of the two frequencies corresponding to the concentration of electrons in the ground subband $n_1$ and in the upper one $n_2$. Most frequently $n_1 < n_2$, and the determination of $n_2$ is extremely difficult, in particular for lower concentrations ($n_2 < 5 \times 10^{10}$ cm$^{-2}$). In this letter, we present a novel technique by which we are able to drastically enhance the SdH pattern. The technique is based on measuring the change in the magnetoresistance due to a carrier generated by a modulated light source. In addition to the overall enhancement of the SdH waveform, the technique has an important property of selectively increasing the amplitude of the slower oscillations due to carriers in the second subband much more than oscillations generated by the ground subband electrons.

The experimental setup used to generate the modulated oscillatory magnetoresistance waveform is a conventional SdH setup with an additional lock-in amplifier and a chopped laser. The sample is cooled down in an open-flow He cryostat with an optical axis to enable excitation of the carriers. The magnetic field is swept up to 1.4 T. The change in the longitudinal voltage drop is measured by a lock-in amplifier with reference frequency provided by the chopper.

Figure 1 shows the raw data obtained using the modulated SdH technique (a), followed by a regular SdH measurement (b). Both measurements were taken at 4.2 K on an InGaAs/AlGaAs high electron mobility transistor (HEMT) structure with a 200 Å In$_{0.15}$Ga$_{0.85}$As well, a 100-Å-wide Al$_{0.15}$Ga$_{0.85}$As spacer, and a $2 \times 10^{18}$ cm$^{-3}$ Si-doped barrier of the same composition. The identical frequency of oscillation of 12.4 T seen in Figs. 1(a) and 1(b) indicates a carrier concentration of $6.01 \times 10^{11}$ cm$^{-2}$ in the 2DEG. The raw modulated waveform is as good as the best computed SdH pattern derived after background subtraction and normalization. The experimentally modulated results are superior to those obtained by taking the numerical
derivative with respect to the magnetic field, as will be discussed below. Figure 2 shows SdH waveforms for the same sample measured at 9.1 K. The enhancement of the waveform by the carrier modulation technique is obvious. The oscillations obtained with this carrier modulation method are very clear at this relatively high temperature, even though the electron mobility is not too large ($\mu_e = 97,000 \text{ cm}^2/\text{V s}$ at 4.2 K).

The technique has an important property of selectively increasing the amplitude of the slower oscillations due to carriers in the upper subband much more than oscillations generated by the ground subband electrons. This selective enhancement is demonstrated in Fig. 3 on an Al$_{0.3}$Ga$_{0.7}$As/GaAs HEMT structure grown on semi-insulating GaAs. The undoped AlGaAs spacer is 60 Å and the dopant concentration is $3 \times 10^{18} \text{ cm}^{-3}$. The measurements are taken at 1.95 K. Figure 3(a) shows the raw data for a regular SdH measurement, from which the modulation at the lower frequency can be extracted only after background subtraction. The raw data for modulated SdH is shown in Fig. 3(b). The amplitude of oscillation at the lower frequency is significantly larger than that generated by the ground subband. The Fourier transform of the modulated SdH shows a very clear peak at a frequency corresponding to a second subband concentration of $9.7 \times 10^{11} \text{ cm}^{-2}$ for the ground one. The Hall concentration $n_T$ is $1.06 \times 10^{12} \text{ cm}^{-2}$ and the Hall mobility is $\mu_e = 410,000 \text{ cm}^2/\text{V s}$.

The selective enhancement can be caused either by an uneven distribution of the carriers between the two subbands, or by the different effect of the excess carriers on the amplitudes of oscillation. The ratio between the oscillatory resistance $\Delta R_{xx}$ and its zero-field value $R_0$ for a two subband system is given by

$$\frac{\Delta R_{xx}}{R_0} = A_1 \frac{\Delta g_1}{g_0} + A_2 \frac{\Delta g_2}{g_0} + B_{12} \frac{\Delta g_1 \Delta g_2}{g_0^2},$$

where $A_1$ and $A_2$ are the amplitudes of oscillations at either frequency while $B_{12}$ represents the intermodulation term. The zero-field density of states is $g_0$ while is oscillatory parts are given by

$$\Delta g_i = 2g_0 \sum_s D_T(sX) \exp \left( \frac{-s\pi}{\omega_c \tau_q} \right) \cos \left( \frac{h \pi n_i}{qB + s\pi} \right),$$

where $D_T(Y) = Y/\sinh(Y)$, $X = 2\pi^2 kT/\hbar \omega_c$, $T$ is the temperature, $\omega_c$ the cyclotron frequency, $\tau_q$, the quantum re-
relaxation time, and \( i = 1, 2 \) denotes the subband. Practically the first Fourier component \( s = 1 \) suffices to describe most oscillations.\(^7\)

The modulation of the carrier concentration results in a change in the oscillatory resistance \( \delta (\Delta R_{xx}) \) given by

\[
\delta \left( \frac{\Delta R_{xx}}{R_0} \right) = \left[ \frac{\partial A_1}{\partial n_1} + \frac{\partial A_2}{\partial g_1} \right] \Delta g_1 + \frac{\partial B_1}{\partial n_1} \Delta g_1 + \frac{\partial B_2}{\partial g_1} \Delta g_2,
\]

where the excess concentration \( \delta n_1 \) is divided between the two subbands as \( \delta n_1 \) and \( \delta n_2 \). A straightforward interpretation for the enhancement of oscillations due to the upper subband would be that the electron concentration at the ground subband remains almost unchanged once the second subband starts getting populated,\(^2\) and therefore, \( \delta n_1 > \delta n_2 \). However, most reported data indicate that the electron concentration in the ground subband continues to increase, as were our measurements on the samples described above. Moreover, it is reported that \( \delta n_1 \) is larger than \( \delta n_2 \). Therefore, this cannot be the cause of the selective enhancement.

Next, the derivative terms in Eq. (3) are investigated. The derivative of the density of state is given by

\[
\frac{\partial \Delta g_i}{\partial n_i} = 2g_0 D_r(X) \exp \left( -\frac{\pi}{\omega_i \tau_i} \right) \frac{\pi}{\omega_i} \frac{\partial \tau_i}{\partial n_i} \cos \left( \frac{h n_i}{q B} + \pi \right) + \frac{h n_i}{q B} \sin \left( \frac{h n_i}{q B} \right).
\]

This result obtained for carrier modulation should be compared with the technique of differentiating with respect to the magnetic field.\(^6\) Taking the derivative with respect to \( B \) results in a multiplication by \( n \), and since \( n_1 > n_2 \), that technique greatly enhances the signal due to the ground subband. It should be emphasized that the carrier modulation technique provides experimentally a derivative with respect to \( n \). Since \( \omega_i = q B/m^* \), both terms in the square brackets in Eq. (4) are multiplied \( 1/16 \). Thus, there is a relative increase in the amplitudes at low fields. The first term depends on the change in quantum relaxation time with subband population. Little data is available on this dependence. A theoretical analysis is provided by Ishihara and Smrcka,\(^9\) from which one can derive that

\[
\tau_{A_1} \propto \left[ \frac{\epsilon_F}{\epsilon_F + \left[ \frac{\epsilon_F - 3 (\epsilon_F/\epsilon_a) \epsilon_F + 2 \epsilon_a]}{\epsilon_F + \epsilon_a} \right] \right]^2,
\]

where \( \epsilon_F \) is the Fermi energy and \( \epsilon_F \) and \( \epsilon_a \) are the energies at which the relaxation time and the conductivity reach their maximum. Since the electron concentration depends linearly on the Fermi level, Eq. (5) can be transformed to a dependence on \( n \). Thus, \( \tau_{A_1} \) increases steeply with increasing population at low values of \( n \) since at low energies the states become localized and resonant scattering dominates. It reaches a maximum at a concentration corresponding to \( \epsilon_a \), and dropping from there on as the electrons can get closer to the scattering impurities.\(^10\) Therefore, the contribution of this derivative term is much larger for the upper subband, with its low concentration. The quantum lifetime of electrons in the ground subband may have reached its peak, i.e., the derivative is close to zero. Thus, the contribution of this term to the oscillations waveform is much larger for the second subband.

The last part to be analyzed is the derivatives of the amplitudes of oscillations and the intermodulation. Expressions for the amplitudes were derived by Coleridge\(^1\) based on the effect of various scattering mechanisms on the relaxation time. It can be shown for the case of \( n_1 > n_2 \) that

\[
A_1 = 2 - \frac{P_{12}}{P_{11} + P_{12}}; \quad A_2 = \frac{P_{12}}{P_{11} + P_{12}},
\]

where \( P_{11} \) is the intraground subband scattering probability and \( P_{12} \) is the intersubband scattering probability. It is clear from the equation that if \( A_2 \) increases, \( A_1 \) decreases and vice versa. Following the drop of mobility at the onset of population of the second subband, the mobility increases with increasing carrier population. Since the dominant scattering mechanism is due to the ionized impurities, this scattering is reduced by additional carriers screening this potential. Thus, it can be deduced that the intrasubband scattering decreases with increased carrier concentration. Reviewing Eqs. (3) and (6), one can expect a positive contribution to the modulated signal generated by carriers in the upper subband due to the positive derivative of \( A_2 \), but a negative contribution to the modulated amplitude by excess carriers in the ground subband since the derivative of \( A_1 \) is negative. The derivatives of the intermodulation are both positive, but as long as the oscillations are not very large (as is usually the case when the modulated SdH technique is used), this term, proportional to the square of the oscillations, is negligible.

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TEMPERATURE INDEPENDENT QUANTUM WELL FET WITH DELTA CHANNEL DOPING

P. G. Young, R. A. Mena, S. A. Alterovitz, S. E. Schacham, and E. I. Haugland

Indexing terms: Field-effect transistors, Transistors, Semiconductor devices and materials

A temperature independent device is presented which uses a quantum well structure and delta doping within the channel. The device requires a high delta doping concentration within the channel to achieve a constant Hall mobility and carrier concentration across the temperature range 300-1.4 K. Transistors were RF tested using on-wafer probing and a constant G_m and F were measured over the temperature range 300-70 K.

Introduction: In most semiconductor devices, the gain changes as a function of temperature. For a high electron mobility transistor (HEMT), as the temperature is lowered, the gain is enhanced due to lower electron scattering while maintaining an acceptable carrier concentration. When designing circuits and devices for applications requiring operation over a large temperature range, this enhancement of the carrier mobility has to be taken into account. Previous studies on delta doped channel structures [1-4] have shown that the delta doping creates band bending within the channel allowing for the quantisation of the carrier states within the doped region.

We propose a temperature independent FET with a heavily delta doped GaAs quantum well channel using molecular beam epitaxy (MBE). In the channel doped structure, temperature independence is achieved via proper ion sheet densities within the channel region that degrades the peak mobility of the carrier but creates a constant mobility and carrier concentration from 300 to 1.4 K. This doping technique is contrary to typical HEMT devices where the doping occurs outside the channel in order to reduce ion scattering at low temperatures.

Device structures and characterisation: The nominal structures grown by MBE for this work are shown in Fig. 1. The conduction channel is a GaAs layer of 150Å confined between two Al0.3Ga0.7As layers to form a quantum well. The channel layer is delta doped in the centre with silicon to nominal concentrations of $8 \times 10^{12}$/cm$^2$ or $6 \times 10^{12}$/cm$^2$. The different dopant concentrations were used to determine the effect of the dopant concentration level on the parametric temperature dependence. The quantum well structure is used to reduce parallel conduction and improve the output conductance of the resulting device.

<table>
<thead>
<tr>
<th>Layer</th>
<th>Concentration</th>
</tr>
</thead>
<tbody>
<tr>
<td>$n^+$ GaAs (350Å)</td>
<td>$1 \times 10^{12}$/cm$^2$</td>
</tr>
<tr>
<td>undoped GaAs (350Å)</td>
<td>$6 \times 10^{12}$/cm$^2$</td>
</tr>
<tr>
<td>undoped AlGaAs (75Å)</td>
<td></td>
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<td></td>
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<tr>
<td>undoped AlGaAs</td>
<td></td>
</tr>
<tr>
<td>semi-insulating GaAs</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 1 Device structure cross-section

Fabrication of transistors and Hall bar structures was carried out using wet mesa isolation techniques. The transistors are a dual, Ti/Au gate design with gate lengths and width of 0.8-1.2 µm and 200 µm, respectively. Ohmic contacts consist of sequentially evaporated Au/Ge/Au/Ni/Au metal.

Testing of the devices was carried out to determine material transport parameters and transistor performance. The transport properties of the structures were measured by Hall and Shubnikov-de Haas (SdH) techniques over a temperature range 300-1.4 K with a maximum magnetic field of 1.4 T and carrier light modulation capability. Transistors were RF tested using an HP8510 ANA and an in-house fabricated cryostat mounted with Design Techniques probes capable of on-wafer probing of the device $S$ parameters down to 65 K.

Results and discussion: Fig. 2a and b show the measured Hall mobility and carrier concentrations for the two devices as a
function of temperature. As can be seen, the Hall mobility for the lower doped structure varied by 27% over the temperature range with maximum a Hall mobility of 2500 cm$^2$/Vs. The temperature dependence below 125 K is consistent with scattering from ionised impurities. The carrier concentration variation of only 5% is considered to be temperature independent and indicates there is no carrier freeze out.

When the delta doping concentration is increased by a factor 3-3 to a nominal level of $6 \times 10^{13}$/cm$^2$, the structure experiences a fluctuation of the electron mobility of only 7% over the same temperature range but at the expense of the magnitude of Hall mobility. The Hall mobility was measured to be $\sim 2000$ cm$^2$/Vs which is a 20% decrease over that of the lower doped sample at room temperature. The carrier concentration also showed a small 5% variation over the temperature range. Thus a stable carrier concentration is obtained over the temperature range for both dopant levels but only the higher doped sample experiences constant Hall mobility.

Finally, very high 2-D carrier concentrations were observed in these structures. For the lower doped sample, a dark Hall electron concentration of $2 \times 10^{12}$/cm$^2$ was measured as compared to a value of $2.7 \times 10^{13}$/cm$^2$ under illumination. The large photoconductivity (PC) effect leads to an enhanced signal of the SdH oscillation enabling quantitative measurements and positively confirm the 2-D character of the carriers. Quantitatively, we found carrier concentrations under illumination for the ground and first excited sub-bands of $2.1 \times 10^{12}$/cm$^2$ and $5.3 \times 10^{11}$/cm$^2$, respectively. This shows that for the low doped sample, only two sub-bands are populated. We could not resolve all the sub-bands by SdH for the higher doped sample, but we expect more sub-bands to be populated. This larger number of populated sub-bands is the main reason for temperature independent mobility, as the electrons in the higher sub-bands are spatially less affected by the ionised impurity scattering [5].

To demonstrate the temperature independence of the structure, FETs made from the highly doped structures were tested from 70 to 300 K. The S parameters were measured on-wafer to determine $F_{max}$ and $G_{max}$ at 5 GHz as a function of temperature. $G_{max}$ and $F_{max}$ are shown in Fig. 3. An average $G_{max}$ of 7-3 dB was measured over the whole temperature range at 5 GHz with a variation of only $\pm 0.35$ dB. The devices were stable across the frequency range and this constant stability appears to be characteristic of the structures with channel delta doping. Results for $F_{max}$ show a similar effect with $F_{max}$ being only affected by system noise and not dependent on temperature.

Conclusion: A device quantum well structure with channel doping has been demonstrated with temperature independent parameters. Electron Hall mobility and carrier concentration were almost constant against temperature independence of the RF performance for the transistors. With $G_{max}$ and $F_{max}$ remaining unchanged over the whole temperature range, the need for temperature compensation is eliminated and cryogenic design of circuits using the room temperature S-parameters is viable.

26th May 1992

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Room-temperature determination of two-dimensional electron gas concentration and mobility in heterostructures

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A technique for determination of room-temperature two-dimensional electron gas (2DEG) concentration and mobility in heterostructures is presented. Using simultaneous fits of the longitudinal and transverse voltages as a function of applied magnetic field, we were able to separate the parameters associated with the 2DEG from those of the parallel layer. Comparison with the Shubnikov-de Haas data derived from measurements at liquid helium temperatures proves that the analysis of the room-temperature data provides an excellent estimate of the 2DEG concentration. In addition we were able to obtain for the first time the room-temperature mobility of the 2DEG, an important parameter to device application. Both results are significantly different from those derived from conventional Hall analysis.

Two of the most important physical parameters governing the performance of devices based on two-dimensional electron gas (2DEG) are the concentration of carriers forming the 2DEG and their mobility. In the past, the main effort was placed on increasing the carrier mobility by separating the doped layer from the conduction channel. This was realized using either homogeneous or planar doping in the barrier while the conduction took place in the channel, i.e., a modulation doped (MOD) structure. Lately the trend is to obtain as high a 2DEG concentration as possible. Dopants are introduced into the channel, drastically reducing the carrier mobility, defeating the concept of a MOD structure. There is a tradeoff between increased doping level and mobility of the carriers in the channel. In all cases, the determination of the 2DEG concentration and mobility is an essential part of the characterization of high speed devices.

Unfortunately the determination of the concentration and mobility of carriers is frequently complicated by the presence of a parallel conducting path, in most cases in the barrier layer, since it is usually heavily doped. Typical room-temperature concentrations in the parallel conduction path, AlGaAs for GaAs based devices, and InAlAs for InP based devices, are of the order of $10^{18}$ cm$^{-3}$. Even though the mobility of these carriers is substantially smaller than that of carriers in the 2DEG, in particular in MOD structures, their presence may significantly modify the Hall coefficient $R_H$ and conductivity data. Thus, it becomes essential to resort to measurements performed at cryogenic temperatures, in order to determine the 2DEG concentration, assuming it remains constant as a function of temperature.

In this letter we propose a technique that enables the determination of the 2DEG concentration using only room-temperature measurements. At the same time the room-temperature 2DEG mobility is derived, which is a parameter of utmost importance in development of high speed devices. The technique is based on recording of both the longitudinal and transverse (Hall) voltages across the sample versus magnetic field, determining the physical magnetoresistance and the change in the Hall voltage as a function of field.

The general expressions for the longitudinal and transverse resistivities as a function of magnetic field $B$ (in the $z$ direction) in the presence of two carriers are given by:

$$\rho_{xx} = \frac{E_x}{J_x} = \frac{D_{12}}{(D_{12}^2 + A_{12}^2)}.$$  \hspace{1cm} (1)

$$\rho_{xy} = \frac{E_y}{J_x} = R_H B = -\frac{A_{12}}{(D_{12}^2 + A_{12}^2)},$$  \hspace{1cm} (2)

with

$$A_i = \omega_c r_i D_i,$$

$$D_{12} = D_1 + D_2,$$

$$A_{12} = A_1 + A_2.$$

In this letter we assume that the carriers in the conduction channel of the heterostructure form a 2DEG and we will denote these carriers with index 1 and those in the parallel path with index 2. The concentrations of the two carriers are $n_i$, their effective masses are $m_i$ and the scattering times are $\tau_i$ with $i = 1, 2$ for the two carriers. $E$ is the electric field while the longitudinal current density is denoted by $J_x$ (see insert in Fig. 1). The Hall concentration and mobility will be denoted by $n_H$ and $\mu_H$ and the Hall scattering factor is assumed to be equal to 1. The magnetic field dependence is introduced through the cyclotron frequency, $\omega_c = eB/m_i$, where $e$ is the electron charge. At zero magnetic field the longitudinal resistivity is equal to the parallel combination of the resistivities of the two carriers, while at very large fields ($\omega_c \tau_i \gg 1$) the Hall concentration is equal to the sum of the two concentrations. If, for example, the two concentrations are of comparable magnitude, but the mobility of the first is much larger than that of the second one, $\mu_1 \gg \mu_2$, the low field Hall concentration equals $n_1$. At high fields, under the same conditions, the longitudinal resistivity is given by:

$$\rho_{xx} \approx n_1/\mu_1 (n_1 + n_2)^2.$$

TABLE I. Carrier concentrations and mobilities for three samples. Concentrations are in $10^{12}$ cm$^{-2}$ and mobilities in cm$^2$/V s.

<table>
<thead>
<tr>
<th>Sample</th>
<th>$n_1$</th>
<th>$n_2$</th>
<th>$\mu_1$</th>
<th>$\mu_2$</th>
<th>$n_H$</th>
<th>$\mu_H$</th>
<th>$n_{SH}$</th>
<th>$\mu_{SH}$</th>
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</thead>
<tbody>
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<td>7570</td>
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<td>5080</td>
<td>1.11</td>
<td>0.96</td>
</tr>
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<td>7710</td>
<td>1920</td>
<td>2.78</td>
<td>5150</td>
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<td>2.92</td>
<td>4060</td>
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</tbody>
</table>

In our experimental setup we recorded the longitudinal voltage and the Hall voltage continuously versus the magnetic field up to the highest field accessible, 1.4 T. Then, using a nonlinear least-squares method we fitted both sets of experimental data simultaneously to Eqs. (1) and (2). Thus we obtained an estimate of the four variables: $n_1$, $n_2$, $\mu_1$, and $\mu_2$. Two problems are faced during this process. First the Hall voltage increases almost linearly with the magnetic field which would result in an improper balance of the computation by underweighting the low field and by overweighting the high field Hall data. To overcome this issue we fitted the Hall coefficient which varies much less with magnetic field. A second problem is present in a simultaneous fitting process when one set of numbers is significantly larger than the other. In this case the latter set would have a marginal effect on the derived parameters. Therefore we introduced a normalization factor. A point in mid-field range was chosen for which the resistivity and Hall coefficient were calculated. The ratio between these figures forms a normalization factor by which the Hall data were multiplied, making these data comparable in magnitude to the resistivity data. Upon completion of the computation the data were renormalized.

Several aspects regarding the accuracy of the procedure were examined. The standard deviation of the parameters derived from the fitting process was found to be better than 0.5%. Second, the procedure was applied to different ranges of magnetic fields to determine the consistency of the results. While the scatter between derived parameters obtained for different ranges was less than 2% at intermediate temperatures (typically between 50 and 200 K), this scatter at higher temperatures may be over 10% in concentration and 5% in mobility. Caution must be taken when choosing the range of fit of the Hall data. Since we fit the Hall coefficient, which is derived from the measured transverse voltage by division with the magnetic field, small errors in the low field data may result in a substantial deviation of the entire fit. Another source of inaccuracy may be due to the presence of a large transverse voltage at zero field. If the parallel concentration becomes much lower than the 2DEG concentration, the accuracy of the values derived for $n_2$ and $\mu_2$ may be worse than 10%. This is frequently the case with better samples at the lowest temperatures (and not exposed to light). Under these conditions, $\mu_2 n_2 > \mu_1 n_1$, so that the conduction data are dom-
inated entirely by the 2DEG carriers. The actual accuracy of the derived 2DEG concentration was evaluated by comparing it to the results obtained from the SdH and Hall experiments performed at liquid helium temperatures.

Table I summarizes the results of the analysis performed on three samples. The samples were MBE grown MOD structures consistent of AlGaAs barrier with 30% Al and a GaAs well. In samples Q12H and Q12I the barrier was delta-doped with Si at a concentration of \(3.5 \times 10^{12}\) cm\(^{-2}\), while in sample Q11A the barrier was homogeneously doped at a concentration of \(10^{18}\) cm\(^{-3}\). Sample Q12I is identical to sample Q12H except that it was removed from the GaAs substrate by an epitaxial liftoff process. The 2DEG concentrations are compared with the concentrations derived from the Shubnikov–de Haas (n\(_{\text{SdH}}\)) oscillations and the Hall data (n\(_{\text{H}}\)) taken at liquid helium temperatures. No second subband population was evident from the SdH data on either sample.

For all the samples examined at room temperature, the derived 2DEG concentration \(n_1\) falls between the measured low-temperature SdH and Hall concentration. The difference between these and the room-temperature Hall concentration is very significant. Altogether the high-temperature Hall data are much closer to that of the parasitic parallel layer. It should be pointed out that this large parallel concentration \(n_2\) is typical for these types of structures. The concentration \(n_2\) drops drastically with temperature and reaches \(2 \times 10^{11}\) cm\(^{-2}\) below 50 K. The relatively larger error in room temperature \(n_1\) for sample Q12H is due to a large zero field transverse voltage (0.1 mV with a current of 2 µA). At the lowest field this voltage is more than half of the recorded signal.

Figure 1 shows the experimental points and the results of the fitting process to the data measured at room temperature on sample Q121. The fit of \(\rho_{xx}\) is excellent, while that of \(R_1\) exhibits some fluctuations at the lowermost magnetic fields, due to the division by \(B\), as explained before. Even for these points, the error is below 2%.

As an extension of the method we used it to estimate the four parameters \(n_1, n_2, \mu_1, \mu_2\) as a function of temperature. Figure 2(a) shows the carrier concentrations and Fig. 2(b) the mobilities as a function of temperature for sample Q12H. The low-temperature 2DEG parameters almost coincide with the Hall data because of the low parallel concentration in this temperature range. It is interesting to note that the mobility of the parallel layer \(\mu_2\) increases as \(n_2\) decreases with descending temperatures. However, \(\mu_2\) remains fairly constant at lower temperatures as might be expected in degenerate semiconductors.

In conclusion we have shown that the simultaneous fit of the magnetic field dependent longitudinal and transverse resistivities can serve as a useful tool in characterization of quantum well structures both enabling room-temperature determination of 2DEG concentration and mobility as well as exploration of the effect of parallel conductance. This may be particularly helpful in better understanding of persistent photoconductivity in these structures.1

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Spectroscopic ellipsometry studies of HF treated Si (100) surfaces

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Both ex situ and in situ spectroscopic ellipsometry (SE) measurements have been employed to investigate the effects of HF cleaning on Si surfaces. The hydrogen-terminated (H-terminated) Si surface was modeled as an equivalent dielectric layer, and monitored in real time by SE measurements. The SE analyses indicate that after a 20-s 9:1 HF dip without rinse, the Si (100) surface was passivated by the hydrogen termination and remained chemically stable. Roughness of the HF-etched bare Si (100) surface was observed, in an ultrahigh vacuum (UHV) chamber, and analyzed by the in situ SE. Evidence for desorption of the H-terminated Si surface-layer, after being heated to ~550 °C in the UHV chamber, is presented and discussed. This is the first use of an ex situ and in situ real-time, nondestructive technique capable of showing state of passivation, the rate of reoxidation, and the surface roughness of the H-terminated Si surfaces.

In the fabrication of ultralarge-scale integrated circuits, preparation of native oxide free Si surfaces, the monitor and control of Si surface passivation and reoxidation are extremely important issues. Aqueous HF etching of Si surfaces removes the surface oxide and terminates the Si surface with atomic hydrogen.\(^1\)\(^2\) The hydrogen termination retards the Si surface oxidation, and protects the surface from chemical attack.\(^3\)\(^4\) Therefore, the HF cleaning of Si surfaces has received increasing attention. However, the properties of hydrogen-terminated (H-terminated) Si surfaces under various conditions, and the degree of surface passivation and reoxidation are still under investigation.\(^5\)\(^6\) In this letter, we report results of ex situ and in situ spectroscopic ellipsometry (SE) studies of HF cleaned Si (100) surfaces.

SE is a surface-sensitive, nondestructive optical technique used to characterize surface overlayer thicknesses, multilayer structures, optical constants of bulk materials, and surface changes.\(^7\)\(^8\) Ellipsometry determines the complex ratio of reflectance \(R_p\) to \(R_s\), defined as

\[
\rho = \frac{R_p}{R_s} = \tan(\psi)e^{i\Delta},
\]

where \(R_p\) and \(R_s\) are the reflection coefficient of light polarized parallel to (\(p\)) or perpendicular to (\(s\)) the plane of incidence, and the values of \(\tan(\psi)\) and \(\Delta\) are the amplitude and phase of the complex ratio.

The pseudodielectric function (\(\varepsilon\)) can be obtained from the ellipsometrically measured values of \(\rho\), assuming a two-phase model (ambient/substrate)\(^9\) regardless of the possible presence of surface overlayers. For samples with surface overlayers or multilayer structures, SE data must be numerically fitted according to an assumed model (e.g., a three-phase model: ambient/surface overlayer/substrate). Assuming such a model, values of \(\psi(hv, \Phi_i)\) and \(\Delta(hv, \Phi_i)\), defined as in Eq. (1), are calculated. Here \(hv\) is the photon energy and \(\Phi\) is the external angle of incidence. A regression analysis is established to vary the model parameters (e.g., layers thicknesses) until the calculated and experimental values match as closely as possible. This process is done by minimizing the mean square error (MSE) function as described in Refs. 10 and 11. In our study, ex situ and in situ SE measurements were made using a Woollam Co. Variable Angle Spectroscopic Ellipsometer (VASE\(^{TM}\)), which was equipped with a beam-chopped, rotating analyzer to increase the stray light rejection and signal to noise ratio.

Si (100) surfaces covered with native oxide from a virgin p-type wafer of 14–22 Ω cm resistivity were employed to study the effects of HF treatments on Si. A piece from the wafer was dipped in 9:1 (volume ratio of deionized water to 49% HF) HF solution for approximately 20 s with no rinse. SE measurements were made in air, at a 75° angle of incidence, before and after the HF dip. During the measurement, the automated polarizer azimuth angle \(\Phi\) was set to vary with changes of the measured \(\psi(hv, \Phi_i)\) to minimize experimental errors in the ellip-

![FIG. 1: \(\psi\) and \(\Delta\) values of ex situ SE measurements on a Si (100) surface: (a) before and (b) after the HF treatment. The solid line represents the experimental data, and the dashed line is the best fit of the SE analysis. Assumed models for the SE analysis, in each case, are sketched with the plots.](image-url)
The spectral scan, ranging from 3000 to 8000 Å, with an srometer system. It was set such that \( P = \psi \) with \( P_{\text{min}} = 10^\circ \). The spectral scan, ranging from 3000 to 8000 Å, with an increment of 100 Å, was completed within 2–3 min. The SE analysis indicated that an approximately 25 Å thick native oxide covered the virgin Si surface as shown in Fig. 1(a). After the HF cleaning, the Si native oxides were removed and the Si surface was terminated with H-silicon bonds. This H-terminated Si surface was modeled as an equivalent dielectric layer described by the optical constants of SiO\(_2\). [for the SE analysis shown in Fig. 1(b)]. The optical constants of Si used for the calculations in the SE regression analysis are from Ref. 14. A typical “thickness” of the H-terminated Si surface (H surface) immediately after the HF cleaning, as indicated by the SE regression analysis, was in the range 14–17 Å. Notice that the thickness referred to here as an H surface was not the actual thickness of the H-surface layer, but the effective thickness of the modeled equivalent dielectric layer of SiO\(_2\), which includes possible Si surface microroughness after HF etching (as discussed below). The value of this thickness as measured by SE was used to monitor the changes in the H surface.

SE measurements were made on this H surface in air at room temperature (RT) over a period of several months after the HF cleaning. Changes in thickness of the H surface were monitored as a function of time as shown in Fig. 2. The figure shows that the H-terminated Si surface remained unchanged for over 2 h, and very little reoxidation took place within 3–4 days. After two months the reoxidized Si surface layer saturates at a thickness of ~33 Å, which is thicker than the native oxide before the HF etching. The SE study indicates that remarkable surface passivation has been achieved by the hydrogen termination of Si surface dangling bonds, which contributes to the retardation of the Si surface oxidation during air exposure. The apparent larger thickness of the reoxidized layer provides a clue to the Si surface roughness after the HF etching.

In situ SE was employed to study changes of the H-terminated Si surface at elevated temperatures and the bare Si surface conditions after HF etching. During the in situ measurements, the ellipsometer was attached to an UHV chamber, fitted with a pair of low-strain fused-quartz windows. A Si (100) sample was introduced into the UHV chamber, and real-time ellipsometric measurements of one set of \( \Psi \) and \( \Delta \) data were made periodically in time (about once every 5 s) at a photon energy of ~4.1 eV, corresponding to the critical point energy \( E_2 \) (i.e., ~4.1 eV for Si at ~550 °C), while maintaining the sample at ~550 °C. These data were converted simultaneously to a pseudodielectric function \( \epsilon = \epsilon_1 + i\epsilon_2 \). In general, it has been established that the peak value of the imaginary part \( \epsilon_2 \) in semiconductors is very sensitive to the presence of surface overlayers (e.g., H surface) and any possible surface defects such as surface microscopic roughness. A reduction of the thickness of surface overlayer or surface roughness leads to increasing values of \( \epsilon_2 \). The highest value \( \epsilon_2 \) corresponds to the cleanest and smoothest bulk surface condition. Therefore, changes in the H surface induced at elevated temperatures can be monitored in real time by measuring the changes of \( \epsilon_2 \).

Figure 3 shows changes in \( \epsilon_2 \) in real time at

![FIG. 3. Real-time (\( \epsilon_2 \)) data from the HF-treated Si (100) surface, inside the UHV chamber, at ~550 °C, near the \( E_2 \) critical-point energy.](image)

In general, it has been established that the peak value of the imaginary part \( \epsilon_2 \) in semiconductors is very sensitive to the presence of surface overlayers (e.g., H surface) and any possible surface defects such as surface microscopic roughness. A reduction of the thickness of surface overlayer or surface roughness leads to increasing values of \( \epsilon_2 \). The highest value \( \epsilon_2 \) corresponds to the cleanest and smoothest bulk surface condition. Therefore, changes in the H surface induced at elevated temperatures can be monitored in real time by measuring the changes of \( \epsilon_2 \).

![FIG. 4. (a) (\( \epsilon_2 \)) spectrum of HF-treated Si at RT, measured by in situ SE, before (dashed line) and after (solid line) being heated to ~550 °C in the UHV chamber. The dotted line is the fit for the rough Si surface model, sketched in (b). (c) A sketch of the H-surface structure, containing the surface roughness formed by HF etching.](image)
~550°C. An obvious increase of \((\varepsilon_2)\) within the first minute at ~550°C indicates the desorption of H-terminated Si surface at ~550°C. A flat plateau followed the desorption of the H surface indicates a stabilized Si surface. The plateau remained unchanged during further extended heating. This also suggests that there is no evidence of the surface quality deterioration (e.g., increasing surface roughness induced by heating) at this elevated temperature.\(^{15}\)

SE data for the H-terminated Si surfaces were taken at RT before and after the heating, as shown in Fig. 4(a). A comparison of the two \((\varepsilon_2)\) spectra at RT, shows a ~7% higher \((\varepsilon_2)\) peak value at the \(E_2\) critical point energy (~4.3 eV at RT) after the heating. This further confirms the desorption of the H surface after heating to ~550°C. The evidence for desorption observed in this experiment is consistent with results obtained by thermally stimulated desorption measurements as described in Ref. 5.

The RT \((\varepsilon_2)\) peak value at the \(E_2\) energy after the desorption of the H surface, as shown in Fig. 4(a) (solid line), is considerably lower than the known value (~46) of Si from literature.\(^{14}\) This indicates a roughened Si surface induced by the HF etching. The surface roughness was modeled as a top Si layer containing 50% voids, as shown in Fig. 4(b). The thickness of this rough Si layer was calculated by the regression analysis, under the assumption of the Bruggeman effective-medium approximation (EMA).\(^{17}\) Good fit was obtained with a thickness of 8.5 Å, as shown in Fig. 4(a) (dotted line). It indicates an approximate 1–2 monolayer surface microroughness formed from the HF etching.

This model of rough Si surface was applied to characterize the H surface measured at RT in vacuum, before the heating, as shown in Fig. 4(c). In this case, the voids were replaced by SiO\(_2\) to model the H termination of the rough Si layer, while the thickness of this rough layer was kept the same as in Fig. 4(b). On top of the rough Si surface, a pure H-surface layer was modeled by the optical constants of SiO\(_2\), as we have discussed previously. The thickness of ~8 Å of this pure H-surface layer was calculated through the regression analysis. Notice that by modeling a rough interface between the top H surface and Si substrate, the top pure H surface has an effective thickness of ~8 Å, which is consistent with an expected monolayer H termination of Si surface.

Same surface-roughness model [as in Fig. 4(c)] was used to reanalyze the ex situ RT SE measurements shown in Fig. 1. The results show a reduced effective thickness of the initial top H surface, after the HF dip, of ~5.4 Å, and a saturated reoxide layer is ~21.7 Å. This value is quite consistent with the thickness of a fresh native oxide surface layer. The small difference between the two initial thicknesses of H surface (i.e., 8.0 and 5.4 Å) are likely due to different degrees of surface roughness of the two individual HF treated Si samples.

In summary, HF treated Si (100) surfaces were investigated by ex situ and in situ SE measurements. The SE analysis indicated that the Si (100) surface was well passivated via a ~20-s 9:1 HF dip with no rinse. Real-time data showed evidence for desorption of the H-terminated Si surfaces at ~550°C in the UHV chamber. Si (100) surface roughness induced by HF etching was observed in a UHV chamber, and analyzed by the in situ SE. It was shown that a ~1–2 monolayer surface roughness was formed after our HF etching. This unique surface characterization, by in situ SE, provides a useful means of studying and monitoring various Si surface conditions after HF cleaning.

The authors wish to thank Dr. Y. J. Chabal and AT&T Bell Laboratories for his helpful discussions. This work was partially supported by NASA-Lewis Grant NAG3-154.

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13. H. R. Philipp, Ref. 9, p. 759.
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HIGH FREQUENCY PERFORMANCE OF Si$_{1-x}$Ge$_x$/Si$_{1-y}$Ge$_y$/Si$_{1-z}$Ge$_z$ HBTs

D. Rosenfeld and S. A. Alterovitz

Indexing terms: Bipolar devices, Transistors, Semiconductor devices and materials

The results of a theoretical study of the performance of high speed SiGe HBTs is presented. The study includes a group of SiGe HBTs in which the Ge concentration in the base is 20% higher than that in the emitter and collector (i.e. $y = x + 0.2$). It is shown that the composition dependences of $f_T$ and the $f_{max}$ are non-monotonic. As the Ge composition in the emitter and collector layers is increased, $f_T$ and $f_{max}$ first decrease, then remain constant and finally increase to attain their highest values.

Introduction: The main interest in SiGe alloys stems from their potential use in high speed heterostructure transistors for microwave and digital switching applications. In the last two decades a large number of HBTs based on III-V materials have been fabricated and characterised. However, it is only during the last few years that material growth and processing techniques compatible with silicon technology have been developed. The new SiGe growth technologies, as well as the recently published promising results of Si/Si$_{1-x}$Ge$_x$/Si HBTs, have generated considerable need among material growers and device engineers for theoretical estimation of the potential performance of these SiGe devices. The composition dependence of the SiGe HBT figures of merit, such as the current gain, the cutoff frequency ($f_T$) and the maximum frequency of oscillation ($f_{max}$), has not been experimentally or theoretically estimated.

In this Letter, the results of a theoretical study of the composition dependence of $f_T$ and $f_{max}$ are presented. In the study, the high frequency characteristics of a series of npn SiGe HBTs with different emitter and collector compositions were calculated. To maintain the advantages of an HBT, the Ge concentration of the base in each of the HBTs was set to be 20% higher than that of the collector and emitter composition (i.e. $y = x + 0.2$). The composition dependences of the emitter-to-collector transit time ($\tau_{ec}$) and the base-resistance collector-capacitance product ($R_b/C_c$) were computed and consequently, the dependences of $f_T$ and $f_{max}$ on the emitter and base compositions were derived.

Geometry and structure: We followed the design rules presented in Reference 1, and obtained device dimensions and dopant concentrations similar to those obtained in Reference 2. The chosen parameters were not meant to project the ultimate performance potential of SiGe HBTs and, therefore, the high frequency figures of merit are somewhat inferior to those recently published [3]. Because the study was comparative in nature all devices examined had the same areas (emitter and base 2 × 8 µm$^2$, collector 20 × 8 µm$^2$), same layer thicknesses (300, 500, 5000, 5000 Å in the emitter, base, collector and sub-collector, respectively), same dopant profiles (10, 300, 5000, and 10$^{17}$ and 10$^{20}$ cm$^{-3}$) and same operating conditions (1V base-collector bias). The HBTs differ in the emitter and collector Ge concentrations and in the base concentration, which was always set to be 20% higher than the former.

Device model and material properties: $f_T$ and $f_{max}$ were analysed using widely used formulas:

$$f_T = \frac{2\pi \cdot \tau_{ec}}{}$$

($) (1)$

$$f_{max} = \frac{(4\pi)^{-1} \cdot (\tau_{ec} \cdot R_b C_c)^{-1/2}}{}$$

($) (2)$

where $\tau_{ec}$ is given by

$$\tau_{ec} = \tau_e + \tau_b + \tau_{eb} + \tau_d + \tau_r$$

($) (3)$

In eqn. 3 $\tau_e$ and $\tau_r$ are the emitter and collector charging times, $\tau_b$ is the base transit time, $\tau_{eb}$ is the transit time associated with the current induced base at high current levels and $\tau_d$ is the transit time through the base-collector depletion region (or collector-subcollector depletion region at high currents).

The above transit times depend strongly on the basic properties of the materials such as dielectric constants, mobilities, saturation velocities, bandgaps and dopant concentrations. The material properties, in turn, depend on the Ge concentration and hence it is expected that $f_T$ and $f_{max}$ will show a dependence on composition.

The SiGe material properties and their composition dependences were adopted from the literature. The resistances, the junction capacitances, and the built-in voltages were calculated using the expressions given in Reference 4. For the composition dependence of the bandgaps, the intrinsic carrier concentrations and the dielectric functions, we use the formulas published in References 5–7, respectively. The bandgap discontinuities and their composition dependences were taken from Reference 8. The expressions for the carrier mobilities in SiGe are based on the theoretical calculation presented in Reference 9. For the saturation velocity of electrons in SiGe alloys we employed a linear fit between the saturation velocities of electrons in Si and Ge. The influence of the high current on the width and location of the base-collector depletion region was calculated according to Reference 10.

Results and discussion: The calculated $f_T$ and $f_{max}$ plotted against the collector current density $J_c$ for several SiGe HBTs, are shown in Figs. 1 and 2. All transistors were identical in

geometry and dopant profile. However, they differed in the compositions of the layers. The emitter and collector compositions were varied from \( X_e = X_c = 0 \) to \( X_e = X_c = 0.8 \) and the base composition varied from 0.2 to 1.

![Figure 2: Maximum oscillation frequency \( f_{\text{max}} \) of \( \text{Si}_{1-x}\text{Ge}/\text{Si}_{1-x}\text{Ge} \) HBTs against collector current density, plotted for values of emitter composition \( X_e = X_c, \) and \( X_c = X_e + 0.2 \)](image)

Figs. 1 and 2 demonstrate the non-monotonic behaviour of both \( f_T \) and \( f_{\text{max}} \). For \( X_e = 0 \) (pure silicon in the emitter and collector), the highest \( f_T \) and \( f_{\text{max}} \) (29 GHz) are obtained at collector currents of 72 kA cm\(^{-2}\) and 162 kA cm\(^{-2}\), respectively. Increasing the emitter and collector compositions to 0.4 (and the base composition to 0.6), the highest \( f_T \) and \( f_{\text{max}} \) decrease to 23 GHz, and are obtained for collector currents of 68 kA cm\(^{-2}\) and 150 kA cm\(^{-2}\). Further increasing the emitter composition to 0.8 (and pure Ge in the base), the peak values of \( f_T \) and \( f_{\text{max}} \) increase to 62 and 100 GHz, obtained for \( J_c = 72 \text{ kA cm}^{-2} \) and \( 162 \text{ kA cm}^{-2} \). Fig. 3 emphasises the non-monotonic behaviour of \( f_T \) and \( f_{\text{max}} \), by showing the \( f_T \) and \( f_{\text{max}} \) values (calculated for \( J_c = 72 \text{ kA cm}^{-2} \) and \( J_c = 172 \text{ kA cm}^{-2} \), respectively), plotted against the emitter composition.

Conclusion: We have demonstrated the non-monotonic behaviour of \( f_T \) and \( f_{\text{max}} \). As the Ge composition in the emitter and collector layers (as well as the base) is increased, \( f_T \) and \( f_{\text{max}} \) first decrease, then remain almost constant and finally increase to attain their highest values.

6th November 1992

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Ellipsometric study of Si₀.₅Ge₀.₅/Si strained-layer superlattices

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We present an ellipsometric study of two Si₀.₅Ge₀.₅/Si strained-layer superlattices grown by MBE at low temperature (500 °C), and compare our results with x-ray diffraction (XRD) estimates. Excellent agreement is obtained between target values, XRD, and ellipsometry when one of two available SiₓGe₁₋ₓ databases is used. We show that ellipsometry can be used to nondestructively determine the number of superlattice periods, layer thicknesses, SiₓGe₁₋ₓ composition, and oxide thickness without resorting to additional sources of information. We also note that we do not observe any strain effect on the E₁ critical point.

Semiconductor superlattices (SL) and strained-layer superlattices (SLS) are most commonly characterized by x-ray diffraction (XRD) and transmission electron microscopy (TEM). Neither of these methods are ideal. The first technique is very accurate, but only directly gives the SL period and an average value of composition,1,2 while the second technique requires very tedious sample preparation and is destructive. In this letter, we will show that variable angle-of-incidence spectroscopic ellipsometry (VASE) as applied to Si₀.₅Ge₀.₅/Si SLS yields simultaneously the SL period, the layer thicknesses, the SiₓGe₁₋ₓ layer composition, the number of periods, and the overlayer oxide thickness. In addition, strain effects on the dielectric function of the SiₓGe₁₋ₓ layer will be estimated by VASE. The effect of strain on the dielectric function of SiₓGe₁₋ₓ grown on silicon is presently an area of active research. Both single wavelength3,4 and spectroscopic5-7 ellipsometry, as well as photoreflectance8 have been used on high Si concentration (x > 0.75) SiₓGe₁₋ₓ thin films, showing conflicting results. Most spectroscopic measurements,6-8 which give an overall picture of the strain on the dielectric function, have estimated the effect of strain on the critical points, particularly E₁ and E₂. The E₁ critical point is a crucial parameter in the energy shift algorithm9 and a change in its position will be reflected in a change of the estimated value of x.10 Published results claim either no change in E₁,8,10 decrease in E₁ with increasing strain,7 or an effective increase.8 In this work, the low Si content (x≈0.5) and small SiₓGe₁₋ₓ layer thickness (~5 nm) of our SLS should make any lattice mismatch effect on E₁ readily detectable.

Two nominally identical 15 period Si₀.₅Ge₀.₅/Si SLS samples, identified here as samples A and B, were grown by molecular beam epitaxy2 (MBE) using a Perkin–Elmer (model 4305) Si MBE system. The growth temperature was 500 °C. The upper layer of each SLS was silicon. Target parameter values are given in Table I. Both samples were measured by XRD, which, together with the knowledge of the shutter opening times, gives the SLS period, the average Si concentration throughout the SLS, and the SiₓGe₁₋ₓ layer thickness. The XRD pattern for sample B was of excellent quality, while that of sample A was somewhat degraded. However, an accurate estimate of the SLS period and average Si concentration in the SLS was obtained for both samples. All results are included in Table I. The average Si concentration is given as x(avg); values determined using shutter timing information are labelled with asterisks. The XRD results show excellent agreement with the target values for both samples.

The VASE measurements were taken with a rotating analyzer ellipsometer described elsewhere.11 This instrument measures the complex reflection ratio ρ=\tan(\Psi)\exp(i\Delta) where \Psi and \Delta are the conventional ellipsometric parameters used to represent the amplitude and phase of ρ. Measurements of the SLS samples were taken over the spectral range 300–760 nm for sample A and 300–780 nm for sample B, both in 5 nm increments. Each sample was measured at three angles-of-incidence: 75°, 76°, and 77°. These incident angles were selected to be near to the principal angle for most of the spectral range, providing maximum sensitivity.12 Experimental results of tan(\Psi) and cos(\Delta) for sample A are shown in Fig. 1; the results for sample B are very similar.

Analysis of VASE data involves a least squares fit of the data to an appropriate model, with the quality of the fit defined by a mean-square-error σ.10 A four parameter model was used to fit the SLS samples. The parameters were: Si and SiₓGe₁₋ₓ layer thicknesses, silicon concentration x in the SiₓGe₁₋ₓ layer, and the native oxide thickness. All periods of the superlattice were assumed to be exactly identical in terms of thicknesses and optical properties. The optical constants of silicon were taken from Ref. 13. There are currently two available databases for SiₓGe₁₋ₓ in the literature.14,15 J. Humlíček et al.14 have published the results of measurements of bulk SiₓGe₁₋ₓ grown by the Czochralski method and also of thick films grown by liquid-phase epitaxy. These measurements cover the entire compositional range. Optical measurements were taken14.
TABLE 1. VASE and XRD analyses of the SLS samples. The ellipsometric fitted parameters are the oxide, Si and SiGe layer thicknesses (d), and the silicon concentration \(x\) of the SiGe layer. The period is the sum of the Si and the SiGe layer thicknesses. \(x(\text{avg})\) is the average silicon concentration in one period.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Source</th>
<th>(d(\text{SiO}_2)) (nm)</th>
<th>Period (nm)</th>
<th>(d(\text{Si})) (nm)</th>
<th>(d(\text{SiGe})) (nm)</th>
<th>(x(\text{avg}))</th>
<th>(x)</th>
<th>(\sigma)</th>
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<td>...</td>
<td>35.0</td>
<td>30.0</td>
<td>5.0</td>
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<tr>
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<td>±0.08</td>
<td>±0.08</td>
<td>±0.04</td>
<td>±0.06</td>
<td>±0.05</td>
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<td>34.8</td>
<td>30.0</td>
<td>5.3</td>
<td>0.922</td>
<td>0.47</td>
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<tr>
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<td>1.83</td>
<td>34.8</td>
<td>29.88</td>
<td>4.67</td>
<td>0.942</td>
<td>0.5690</td>
<td>0.0021</td>
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<tr>
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<td>±0.06</td>
<td>±0.04</td>
<td>±0.04</td>
<td>±0.04</td>
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<tr>
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<tr>
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<td>±1.00</td>
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<td>±0.0022</td>
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<td>Ref. 15</td>
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<td>37.7</td>
<td>32.36</td>
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<td>0.931</td>
<td>0.5145</td>
<td>0.0016</td>
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<td>±0.06</td>
<td>±0.07</td>
<td>±0.05</td>
<td>±0.05</td>
<td>±0.05</td>
<td>±0.0031</td>
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</table>

\(^a\)Estimated from growth times.
\(^b\)Fitted \(\lambda < 650\) nm.
\(^c\)All data fitted.

using a rotating analyzer ellipsometer (RAE). There are several difficulties with this database: first, because RAE does not measure low absorption substrates accurately, data at high wavelengths are unreliable.\(^{14,15}\) Probably for this reason, data are available in the infrared only down to 1.7 eV (729 nm). This is a problem for our analyses, as the silicon layer of the first period is only penetrated for \(\lambda > 370\) nm, so that the information on the superlattice is contained mostly in the high wavelength measurements. Second, the compositions were determined only by ellipsometry,\(^{14}\) using the measurement at the He-Ne line (632.8 nm), where the RAE is inaccurate. Recently, Jellison, Haynes, and Burke\(^{15}\) have published an independent database using the results of measurements of thick (7-8 µm on Si) relaxed Si\(_x\)Ge\(_{1-x}\) films grown by conventional high-temperature chemical vapor deposition. Optical measurements were taken using a two-channel spectroscopic polarization modulation ellipsometer (2-C SPME) which measures low absorption substrates accurately;\(^{15}\) data are available to 840 nm. Compositions were determined by electron microprobe and Rutherford backscattering measurements. This database also covers the entire compositional range. However, there is a variation between a sample grown on a silicon substrate and another sample of similar composition grown on a germanium substrate. Therefore, in our analyses, only Ref. 15 spectra taken from samples grown on silicon will be used. Because the databases of Refs. 14 and 15 show significant differences, each SLS was analyzed using each database and the results will be compared. In order to use the databases, an algorithm for interpolating between the compositions is needed. The energy shift algorithm\(^{15}\) which has been applied previously to Si\(_x\)Ge\(_{1-x}\), using the Ref. 14 database\(^{5,6}\) was used. This algorithm requires the location of the main critical points to be expressed as a function of alloy composition. Because of the significant differences between the databases of Refs. 14 and 15, different critical point functions must be used. For both databases, the indirect band gap function \(E_0(x) = 0.68 + 0.44x\) was used.\(^{16}\) This function, which is a simple linear interpolation between the fundamental indirect band gaps of silicon and germanium, was found to give identical results in our analyses, as compared with more complex \(E_0(x)\) functions, because the range of measurement is far away from \(E_0(x)\). \(E_1(x)\) for the database of Ref. 14 was
given in that reference, while $E_l(x) = 4.39 + 0.03x$ was taken from Ref. 6. For the database of Ref. 15, critical points $E_l(x)$ and $E_2(x)$ were obtained by fitting the spectra to critical point line shapes.\(^\dagger\) $E_l(x)$ was found to be approximately constant at 4.30 eV, while the linear fit $E_l(x) = 2.357 + 0.9393x$ was found to describe $E_l(x)$ well, especially in the range $0.47 < x < 0.85$.

Comparison of experimental VASE and best fit model results using the Ref. 15 database for sample A are shown in Fig. 1. Full numerical VASE results for both samples are given in Table I along with the associated 90% confidence limits. Note that analyses using Ref. 14 are limited to $\lambda < 650$ nm, due to the range of reference data and the nature of the energy shift algorithm. Analyses using Ref. 15 include all measured data. In all cases, the values determined by XRD were used as initial conditions. Statistical analyses of the fits indicated no significant parameter correlations. The results using both Si$_x$Ge$_{1-x}$ databases are very similar, except for the $x$ value of the Si$_x$Ge$_{1-x}$ layers. The composition obtained using Ref. 15 data agrees very well with the XRD results, while the $x$ value obtained using Ref. 14 is about 0.1 higher for both superlattices. This, along with the higher $\sigma$ values obtained using the Ref. 14 database, supports our belief in the greater accuracy of the Ref. 15 database. The XRD data and the VASE results all show a 0.03 difference in the $x$ values between the two samples, strongly indicating this difference is real. This indicates that the precision of both the XRD and VASE techniques for determining the value of Si$_x$Ge$_{1-x}$ composition $x$ is better than 0.03.

XRD can verify the number of periods provided the sample is of extremely good quality. To examine the ability of VASE to verify this parameter, we refitted sample B using the Ref. 15 database assuming 14, 16, and 17 periods. For the 14 period model, $\sigma$ is a factor of 3 higher than the 15 period model and $x$ increases to 0.607. For 16 periods and 17 periods, the $x$ value decreased below 0.47 (the lowest available reference spectrum) and had to be held constant there: the resultant $\sigma$ were 1.2 and 4.2 times higher, respectively. Adding or subtracting a period clearly degrades the fit, either by increasing $\sigma$ or by unreasonably decreasing the composition; we thus conclude VASE can be used to verify the number of periods.

To examine potential parameter correlations, the measurement of sample B was refitted using an initial Si$_x$Ge$_{1-x}$ layer thickness of 6.6 nm and concentration $x = 0.60$, maintaining the XRD value $x(avg) = 0.93$. The fit converged to the same values as given in Table I to four significant digits. This means VASE can separate the Si$_x$Ge$_{1-x}$ layer composition and thickness, i.e., they are not significantly correlated. VASE thus provides an independent verification of shutter opening times, which are used in the XRD analysis.

The strain effect, if any, on the dielectric function will be observed as a shift in the $x$ value. As seen from Table I, using the Ref. 15 database which is deemed more reliable in our wavelength range, we do not observe any strain effect. The good agreement between XRD and the fit using Ref. 15 indicates that the $E_l$ critical point is not strongly affected by the strain, since the energy shift algorithm used was based upon this critical point.\(^\dagger\) The $E_l + \Delta E_l$ and $E_2$ critical points are not checked with this method, as they are weaker and influence the spectrum only above the $E_l$ energy region, where the top period silicon layer largely shields the superlattice.

In conclusion, we have obtained excellent agreement between XRD and VASE results for two Si$_x$Ge$_{0.50}$/Si SLS samples using Ref. 15 data for unstrained Si$_x$Ge$_{1-x}$. We have shown that VASE can be used to determine the number of periods, layer thicknesses, Si$_x$Ge$_{1-x}$ layer composition, and native oxide.

The authors would like to thank G. E. Jellison for providing a diskette of his Si$_x$Ge$_{1-x}$ database and L. D. Warren for assisting with the XRD measurements.

\(^{16}\) E. S. Yang, Microelectronic Devices (McGraw-Hill, New York, 1988).
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Spectroscopic ellipsometric characterization of Si/Si$_{1-x}$Ge$_x$ strained-layer superlattices

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Spectroscopic ellipsometry (SE) was employed to characterize Si/Si$_{1-x}$Ge$_x$ strained-layer superlattices. An algorithm was developed, using the available optical constants measured at a number of fixed $x$ values of Ge composition, to compute the dielectric function spectrum of Si$_{1-x}$Ge$_x$ at an arbitrary $x$ value in the spectral range 1.7 to 5.6 eV. The ellipsometrically determined superlattice thicknesses and alloy compositional fractions were in excellent agreement with results from high-resolution X-ray diffraction studies. The silicon surfaces of the superlattices were subjected to a 9:1 HF cleaning prior to the SE measurements. The HF solution removed silicon oxides on the semiconductor surface, and terminated the Si surface with hydrogen—silicon bonds, which were monitored over a period of several weeks, after the HF cleaning, by SE measurements. An equivalent dielectric layer model was established to describe the hydrogen-terminated Si surface layer. The passivated Si surface remained unchanged for $>2$ h, and very little surface oxidation took place even over 3 to 4 days.

1. Introduction

The Si/Si$_{1-x}$Ge$_x$ strained-layer superlattice (SLS) plays an important role in band-gap engineering and Si-based fast electronic device applications [1,2]. This structure can be grown by low-temperature growth processes, such as molecular beam epitaxy (MBE) or ultrahigh vacuum/chemical vapor deposition (UHV/CVD) [3,4]. In both processes, it is critically important to have tight control on the structural growth parameters such as layer thicknesses, alloy compositions and interfacial roughness. In this paper, we report results of spectroscopic ellipsometry (SE) characterization of layer thicknesses, pseudo-alloy-compositions and surface conditions of Si/Si$_{1-x}$Ge$_x$ SLSs grown by the UHV/CVD technique.

2. Spectroscopic ellipsometry

SE is a non-destructive optical technique. It is extremely sensitive to thickness, alloy composition, and surface and interfacial conditions of the sample structure [5,6]. SE is designed to accu-
rately determine the values of $\tan(\psi)$ and $\cos(\Delta)$, which are the amplitude and projected phase of the complex ratio

$$\rho = R_p/R_s = \tan(\psi) e^{i\Delta},$$

(1)

where $R_p$ and $R_s$ are the complex reflection coefficients of light, measured from the sample, polarized parallel to (p) or perpendicular to (s) the plane of incidence. The results of the SE experimental measurements can be expressed as $\psi(h\nu_i, \Phi_i)$ and $\Delta(h\nu_i, \Phi_i)$ where $h\nu$ is the photon energy and $\Phi$ is the external angle of incidence.

In the simplest case, i.e., the sample can be ideally described as a two-phase model (ambient/substrate), $R_p$ and $R_s$ are the Fresnel reflection coefficients. In the case of multilayer-structured samples, a model has to be assumed, and the SE data must be numerically fitted. The values of $\psi(h\nu_i, \Phi_i)$ and $\Delta(h\nu_i, \Phi_i)$ are calculated as in eq. (1), by an assumed model, for comparison with experimentally measured values. A regression analysis is used to vary the model parameters (e.g., layer thickness or alloy composition) until the calculated and measured values match as closely as possible. This process is done by minimizing the mean square error (MSE) function, defined as:

$$\text{MSE} = \frac{1}{N} \sum_{i,j} \left\{ \left[ \tan(\psi(h\nu_i, \Phi_i)) - \tan(\psi(h\nu_j, \Phi_j)) \right]^2 + \left[ \cos(\Delta(h\nu_i, \Phi_i)) - \cos(\Delta(h\nu_j, \Phi_j)) \right]^2 \right\}. \quad (2)$$

The pseudodielectric function of the sample $\langle \epsilon \rangle$ is obtained from the ellipsometrically measured values of $\rho$, in a two-phase model (ambient/substrate) [5]:

$$\langle \epsilon \rangle = \langle \epsilon_1 \rangle + i\langle \epsilon_2 \rangle$$

$$= \epsilon_0 \left[ \frac{1-\rho}{1+\rho} \right] \sin^2\Phi \tan^2\Phi + \sin^2\Phi \right], \quad (3)$$

regardless of the possible existence of surface overlayers or multilayer structures. The $\epsilon_0$ in eq. (3) represents the ambient dielectric function (e.g., $\epsilon_0 = 1$ in vacuum). To compute the dielectric functions of Si$_{1-x}$Ge$_x$ at an arbitrary $x$ value, we used a group of dielectric functions of bulk Si$_{1-x}$Ge$_x$ measured at fixed $x$ values [7-9], shown in fig. 1, as the basis of our calculation. From fig. 1, it is noticeable that as the $x$ value increases, each critical point of the energy band, such as $E_2$ or $E_1$, shifts by different amounts. Considering the nature of the non-rigid shifts of the $\langle \epsilon \rangle$ spectrum as the $x$ value changes, an energy-shift model [10] is employed to calculate the $\langle \epsilon \rangle$ spectrum for any $x$ values of Ge. This model has been described in detail in ref. [10]. In this procedure the $\langle \epsilon \rangle$ spectrum is computed for an arbitrary $x$ value of Ge by interpolating between the two known adjacent spectra which are above and below the $x$ value, with weighted averages of the two shifted spectra [10]. For Si$_{1-x}$Ge$_x$, three critical-point transitions are considered: $E_2$ ($\sim 4.37$ eV); $E_1$ (2.1-3.4 eV); $E_{g,\text{ind}}$ (0.76-1.1 eV). The $E_{g,\text{ind}}$ is outside the measuring energy range, but it is needed to interpolate the $\langle \epsilon \rangle$ spectrum at photon energies between $E_{g,\text{ind}}$ and $E_1$ [10]. Contributions of $E_1 + \Delta_1$ and $E_2$ to the $\langle \epsilon \rangle$ spectrum are not considered separately here since the positions of these two critical points are very close to that of $E_1$. The energy positions of the critical-point transitions $E_2$, $E_1$, and $E_{g,\text{ind}}$ are given in refs. [11], [7] and [12], respectively:

$$E_2 = 4.372 - 0.069(1-x) \text{ eV}, \quad (4)$$

$$E_1 = 2.108 + 1.134(1-x) + 0.153(1-x)^2 \text{ eV}, \quad (5)$$

$$E_{g,\text{ind}} = 0.8941 + 0.0421(1-x) + 0.1691(1-x)^2 \text{ eV} \quad (0 < x < 0.85), \quad (6)$$

$$E_{g,\text{ind}} = 0.7596 + 1.0860(1-x) + 0.3306(1-x)^2 \text{ eV} \quad (0.85 < x < 1), \quad (7)$$

where $E_{g,\text{ind}}$ refers to the indirect energy gap of Si$_{1-x}$Ge$_x$, with the $X$ and $L$ minima crossing near $x = 0.85$ [12].

Based on this algorithm, the $x$ value was treated as a parameter in fitting the SE data for the Si$_{1-x}$Ge$_x$ SLSs to find the best-fit pseudo-alloy-composition values $x$, regardless of the possible influence of strain.
3. Experimental results and discussions

3.1. Sample surface cleaning and passivation

The Si/Si$_{1-x}$Ge$_x$ SLSs are generally covered with oxides. This oxide surface overlayer has to be modeled for the SE characterization. Si oxide surface is usually modeled as a SiO$_2$ layer for the SE analysis. However, since the oxide overlayer generally consists of roughness, as well as mixtures of constituents it is necessary to remove the surface oxide and clean the Si surface to obtain the better SE characterization results for Si/Si$_{1-x}$Ge$_x$ SLSs. Therefore, SE studies of Si surface HF cleaning were carried out prior to the characterization of Si/Si$_{1-x}$Ge$_x$ SLSs.

p-Type Si wafers (100) of 14–22 Ω·cm resistivity were used to study the effects of HF treatments on Si surfaces covered with native oxide. A piece from the wafer was dipped in 9:1 HF for ~20 s with no rinse. SE measurements were made before and after the HF dip, at a 75° angle
of incidence, as shown in figs. 2a and 2b, respectively. As indicated by the SE analysis, this Si sample was initially covered by a native oxide layer with a thickness of 24.6 Å (fig. 2a). After the 9:1 HF dip, the Si oxides were removed and the Si surface was terminated with hydrogen-silicon bonds. This hydrogen-terminated Si surface was modeled as an equivalent dielectric layer described by the optical constants of SiO$_2$, for the SE analysis shown in fig. 2b. The “thickness” of the hydrogen-terminated Si surface (H-surface), indicated by the SE study, was ~14.6 Å right after the HF cleaning. Notice that the “thickness” referred to here as an “H-surface” was not the actual thickness of the H-surface layer, but the thickness of the modeled equivalent dielectric layer of SiO$_2$. The value of this “thickness” as measured by SE was used to monitor the changes in the H-surface of Si.

SE measurements were made on this H-surface in air at room temperature (RT) over a period of several weeks, after the HF cleaning. Changes in “thickness” of the H-surface were monitored as a function of time as shown in fig. 3. The figure shows that the hydrogen-terminated Si surface remained unchanged for >2 h, and very little surface reoxidation took place within 3 to 4 days. Full reoxidation occurred after two weeks. The SE study indicates that the hydrogen termination of the Si surface dangling bonds effectively retards the Si surface oxidation during air exposure.

3.2. SE characterization of the Si/Si$_{1-x}$Ge$_x$ SLs

Si/Si$_{1-x}$Ge$_x$ SLs with a Ge atomic molar fraction of 8% were grown on Si(100) substrates, at 520°C, by the UHV-17D technique [13]. These Si/Si$_{1-x}$Ge$_x$ superlattices consist of 20 alternating layers, with a nominal thickness of 200 Å for each layer.
The Si/Si$_{1-x}$Ge$_x$ SLSs were subjected to a 9:1 HF dip for ~20 s prior to SE characterization. SE measurements were made in air, with an angle of incidence of 75°, in the spectral range 2.0 to 4.6 eV, with an energy interval of 0.05 eV between data points. A sketch of the assumed model for these superlattices, for SE analysis, is shown in fig. 4. In this model, 10 periods of Si/Si$_{1-x}$Ge$_x$ layers, with thicknesses of $d_2/d_3$, were established on a Si substrate. The top hydrogen-terminated surface layer of thickness $d_1$ was modeled as an equivalent dielectric layer of SiO$_2$, as described in the previous section of this paper. All thicknesses parameters: $d_1$, $d_2$, $d_3$, and the values of pseudo-alloy-composition $x$ were allowed to vary. No interfacial roughness was modeled at this time. Fig. 4 shows the experimental SE data and the best fit from the SE analysis. The best-fit results are: Si 216.6 ± 2.3 Å, Si$_{1-x}$Ge$_x$ 183.9 ± 2.6 Å and $x = 0.0610 ± 0.0008$. These results are in excellent agreement with the values of Si 206 ± 5 Å, Si$_{1-x}$Ge$_x$ 185 ± 5 Å and $x = 0.0825$, from studies of high-resolution double-crystal X-ray diffraction (HRXRD) and cross-sectional transmission electron microscopy (XTEM) by Wang et al. [13]. A MSE value of $3.73 \times 10^{-5}$ indicates a good fit, and it also reflects high quality of this Si/Si$_{1-x}$Ge$_x$ SLS with excellent thickness and composition uniformity, grown by the UHV/CVD technique.

Notice that the $x$ value obtained from SE characterization is smaller than that from HRXRD. This is evidence of the strain effects on the Si$_{1-x}$Ge$_x$ layer. As indicated in ref. [14] and ref. [15], the refractive index of strained Si$_{1-x}$Ge$_x$ tends to shift towards smaller value, which corresponds to unstrained bulk Si$_{1-x}$Ge$_x$ with smaller alloy composition value $x$. It needs to be pointed out that the $x$ value obtained from the HRXRD study considered the strain effects by employing Poisson ratios [13]. The SE measurements seem to magnify the same strain effects on a larger scale. The real reason is not clear.

4. Conclusions

Non-destructive optical SE measurements have been used to characterize the Si/Si$_{1-x}$Ge$_x$ SLSs grown by the UHV/CVD technique. Good fits were obtained by SE analysis, with model parameter values consistent with results from HRXRD and XTEM studies. A smaller pseudo-alloy-composition $x$ value is indicative of the strain in the Si$_{1-x}$Ge$_x$ layer. Ex-situ SE studies of HF cleaning show that the hydrogen termination of the Si surface dangling bonds effectively retards surface reoxidation.

Acknowledgement

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References

Abstract

This report discusses the progress for the first year of the work done under the Director's Discretionary Fund (DDF) research project entitled, "Development of Si_{1-x}Ge_{x} Technology for Microwave Sensing Applications". This project includes basic material characterization studies of silicon-germanium (SiGe), device processing on both silicon (Si) and SiGe substrates, and microwave characterization of transmission lines on silicon substrates. The material characterization studies consisted of ellipsometric and magneto-transport measurements and theoretical calculations of the SiGe band-structure. The device fabrication efforts consisted of establishing SiGe device processing capabilities in the Lewis cleanroom. The characterization of microwave transmission lines included studying the losses of various Coplanar transmission lines and the development of novel transitions on silicon. This report discusses, individually, each part of the project and presents the findings for each. Future directions are also discussed.

Introduction

Silicon technology has never been considered viable for microwave applications because of its lack of high frequency active devices and the extremely high dielectric loss associated with silicon substrates. But silicon technology provides many benefits for microwave applications. Among them are: integration with digital circuitry, mature, well-defined processing procedures and low cost. Recently, a new material, SiGe (silicon-germanium), has emerged that can produce high frequency active devices in a silicon based technology. Using SiGe it is possible to fabricate devices with a two-dimensional electron gas (2DEG). This type of structure has advantages in terms of frequency of operation, noise

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performance and performance improvements at low temperatures. To reduce the dielectric losses associated with silicon substrates, it has been theorized that silicon of sufficiently high resistivity must be used [1].

The purpose of this research project is the development and characterization of microwave devices, both passive and active, using newly-developed SiGe technology at frequencies required for microwave sensing applications. This effort has included basic material studies of SiGe, the development of high electron mobility transistor (HEMT) devices and characterization of microwave transmission lines on high resistivity silicon.

In order to carry out the goals of the program, a working group was established consisting of several members of the Solid State Technology Branch. In this manner, people representing different areas of expertise were brought together. Material, device and circuit experts were all present from the onset of the program. This allowed all areas to be taken into account during planning. Since Lewis does not have the facilities necessary to grow SiGe material, industry and universities were relied upon for the preparation of the SiGe samples. Collaboration was established with UCLA, University of Michigan, Cornell University, Hughes and Spire Corporation. These universities and companies have provided HEMT structures, both n-type and p-type, as well as single strained layers for material characterization studies and device fabrication. It was important to find several sources for material preparation because SiGe technology is in its infancy and there are many uncertainties involved in its growth.

The program consisted of three different areas of research while maintaining a common objective among the members of the working group. The research areas consisted of: basic material studies, device processing and, microwave characterization studies. In a relatively short period of time, many of the goals of this three year program have been accomplished. This report describes the progress for the first year and discuss future directions.

Basic Material Characterization Studies

Theoretical Study

The objective of the theoretical study was to gain a better understanding of the relationships between the physical parameters of the layers in a SiGe structure (composition, grading, doping, and mobility), and the device performance parameters (unity current gain frequency and maximum oscillation frequency). The knowledge of these relationships is required in order to design an optimum structure for high-speed, low-temperature applications.

The procedure used to analyze these relationships was to calculate the band structure of the layers and then calculate the performance which results from that band structure. Because of the complexity of the mathematical problem associated with these calculations, as well as some other non-trivial aspects, a collaboration with the Computational Material Lab at NASA Lewis was established. This lab specializes in complicated matter-related numerical calculations. With the help of the Computational Material Lab, the creation of a sophisticated computer code that solves the Poisson equations and calculates the band structure and the currents of SiGe was recently completed. The I-V characteristics of some simple SiGe structures have been calculated and plotted.

Ellipsometry Work

SiGe material samples were obtained from Spire, UCLA, University of Michigan and Hughes. They included: single SiGe strained layers on silicon, Supperlattice SiGe-silicon, and n- and p-type HEMT structures. Only the results obtained for the n-type MODFET
structures provided by UCLA and Spire will be discussed here. These samples consisted of a strained silicon layer for improved carrier confinement and are labeled as follows: 1) Spire D-5983, 2) UCLA MT-115. The results of Ellipsometric characterization of these samples is shown in Table 1.

Ellipsometric characterization of the samples included three steps: measurement, modeling and linear regression analysis. In the first step, the change in the state of polarization of a monochromatic light, that is reflected from the sample, is measured. This change in polarization is represented quantitatively using the ellipsometric parameters \( \varphi \) and \( \Delta \). The measurement was repeated for approximately 50 wavelengths and several angles of incidence. Thus, a large number of experimental \( \varphi \) and \( \Delta \) are estimated. The sample is modeled using the estimated composition and thickness of all the layers in the sample. In the present case, the model consisted of the nominal compositions and thicknesses of all layers as supplied by the sample grower. They are denoted "nominal" in Table 1. The last step included a linear regression least square fit of all the experimental \( \varphi \) and \( \Delta \) to the theoretically evaluated \( \varphi \) and \( \Delta \) associated with the model. The minimization parameters were the composition of the SiGe layer and all layer thicknesses. The theoretical \( \varphi \) and \( \Delta \) associated with the model were calculated using standard Fresnel reflection equations, and published dielectric functions of all material constituents.

The calculation was done using unpublished calibration functions supplied by J. Jellison from Oak Ridge National Laboratories. The dielectric functions supplied by Jellison were interpolated using a numerical algorithm. These functions were measured on relaxed layers of SiGe on silicon. Measurements were done at 3-5 angles of incidence in the range 3000-7500A using 100A steps. The wavelength (\( \lambda \)) range was limited so that the light did not penetrate the SiGe buffer layer into the silicon substrates. The concentration \( x \) in the SiGe top layer and the "substrate" was assumed to be the same and no roughness was assumed. Graphs of the experimental DELTA (\( \Delta \)) and PSI (\( \varphi \)) verses model calculations are shown in Fig. 1a,1b,1c,1d.

The reason the strained silicon layers have a lower thickness than the nominal value is probably due to the fact that the unstrained calibration function was used. This was done, because, as of now, no strained silicon calibration function exists. The results for D-5983 indicate that it was a poor quality sample, because the thickness and composition were very different from the nominal values. In comparison, sample UCLA MT-115 appeared much better.

Magneto-Transport Measurements

The most important characteristic of a HEMT structure is the two dimensional nature of its transport properties. This characteristic enables very high speed, low noise performance in active semiconductor devices. SiGe n-type structures have been shown to have very high mobilities, as high as \( 10^5 \) cm\(^2\)/V.s at low temperatures, which indicate that this is an excellent structure for microwave applications. It is very difficult however, to obtain two dimensionality in this structure since the conduction band discontinuity between silicon and SiGe is very small. This makes it difficult to achieve quantization of the carriers at the interface of the two layers. Two dimensional transport has only been obtained in the n-type structures by growing a strained silicon layer on top of a fully relaxed SiGe layer. The strain pushes down on the conduction band of the higher bandgap silicon layer, relative to the SiGe conduction band and thus makes possible the quantization. High quality strained layers are very difficult to grow as a result of misfit dislocations that arise from the lattice mismatch growth of the epitaxial layers. Because of this, the transport characteristics of the received samples had to be characterized.
N-type SiGe structures have been received from Spire, UCLA, University of Michigan and AT&T. Hall and Shubnikov-de Haas measurements were carried out using a 1.4 Tesla magnet at temperatures from room temperature down to 1.4K. Two dimensional transport was not detected in any of the structures. Therefore, transport must have occurred in either the bulk of the silicon or SiGe layers; as evident by the large carrier freeze-out at lower temperatures and the large magneto-resistance observed in the samples. Carrier freeze-out in a two dimensional electron gas (2DEG) leads to only a small decrease in the carrier concentration. In the structures examined here, the carrier concentration decreased by orders of magnitude as the temperature decreased. For example, the Spire sample went from a concentration of $7.22 \times 10^{12}$/cm$^2$ at 300K to a concentration of $1.5 \times 10^7$/cm$^2$ at 22K. This type of behavior was typical of all the samples. The freeze-out temperature of the samples varied between 20K and 50K.

Two dimensional transport was detected in the p-type structure provided by Hughes. As compared with the n-type structures, two dimensional transport in p-type structures is easier to achieve. This is due to the larger band discontinuity in the valence band of the silicon and SiGe layers. Doping the layers is also more simple for p-type structures and thus more accurately controlled. The mobility increased with decreasing temperature due to a reduction in phonon scattering effects. The drop in concentration is consistent with carrier freeze-out in the quantized states.

These results have been provided to the material suppliers and has led to modifications in their growth process. UCLA is attempting to lower the concentration of the capping layer (used for contact purposes), in order to reduce the band bending that occurs at such high concentrations. At Lewis, there is an attempt being made to etch away some of the doped layers, with the intent of reducing the band bending and increasing the energy discontinuity.

**Device Processing**

Much like the GaAs based high electron mobility transistor (HEMT) technology, SiGe HEMT technology offers the ability to fabricate active devices with low noise and high speed performance. SiGe HEMT technology has the added advantage of silicon’s native oxide for metal-oxide-semiconductor (MOS) devices. The advantages of the MOS structure is the decrease in gate leakage and the improvement in device stability as compared to Schottky barrier structures.

To achieve device fabrication capability at Lewis, initial design and fabrication development projects were conducted. The intention of these projects was to develop processing techniques necessary for the fabrication of devices. Etching of SiGe materials was the first processing step required to achieve device patterning and was also needed to expose material layers for further device fabrication. Experiments were conducted to characterize etch rates for SiGe materials.

To achieve optimum device operation, low resistance contacts are critical. Therefore, development of a contact structure has been investigated. The focus of this research has been on antimony based contacts and ion implantation of the contact regions. Antimony based contacts studies were conducted using metal type, metal thickness, alloy temperature and alloy time as variables to determine optimum contact resistance. Figure 2 illustrates some of the results used to determine the proper contact procedure for SiGe devices. The figure shows the effect of various alloying temperatures on the series resistance on contacts of various composition. Studies were also conducted by ion implanting phosphorus ions into the material to create contact regions suitable for aluminum based contacts. Because a heterostructure is being used, contact to the 2DEG is required to provide ohmic contact to the...
carriers. Ion implantation is used because it creates a conduction path from the upper contact region to the channel.

In order to fabricate MOS type devices, an oxide is necessary. Oxide characteristics were investigated by examining C-V and I-V measurements. To insure that no interdiffusion of the germanium or donor impurity into the silicon channel layer occurred, a low temperature plasma enhanced chemical vapor deposition (PECVD) technique was used. A characteristic C-V curve is shown in Figure 3. It illustrates the ability to invert the channel region under the oxide and good saturation in the accumulation region. Analysis of the interface state density shows a minimum of $3 \times 10^{10}$ states/cm$^2$ using the Terman method. The capacitor turn on voltage can be adjusted via processing techniques to plus or minus 5 volts to compensate for charge screening at the inversion layer of the oxide, thus achieving an effective modulation of the 2D carriers.

This work was then used to fabricate a preliminary transistor design. Ion implantation was used in fabricating the contacts. A cross section of the device structure and a finished device are shown in Figures 4 and 5, respectively. Initial evaluation of the device indicated a suppressed transconductance. This was most likely caused by poor material. Contact and oxide resistivities were acceptable but the modulated carrier concentration was extremely low. This resulted in poor device performance. Future device fabrication will be conducted on improved materials. At that time, rf performance as a function of temperature will be measured.

**Microwave Transmission Line Studies**

To make microwave applications on silicon possible, silicon with sufficiently high resistivity must be used to minimize the dielectric loss. The aim of this segment of the DDF is to investigate the effective dielectric constant ($\varepsilon_{\text{eff}}$) and attenuation of various transmission lines on silicon as a function of resistivity. We investigated Coplanar Waveguide (CPW), Coplanar slotline and Coplanar stripline structures.

The CPW structures were evaluated theoretically and experimentally. The theoretical analysis was based on the expressions in [2] for $\varepsilon_{\text{eff}}$ and attenuation. The data for attenuation is shown in Figure 6. These calculations are for 2$\mu$m gold lines on 203$\mu$m thick silicon wafers. In this figure, dielectric loss is shown as a function of silicon resistivity for CPW lines of various geometries. Conductor loss is not shown because it is independent of the substrate. It can be seen that the loss is independent of CPW geometry. Losses for wafers of low resistivities are extremely high, but they decreases quickly with increasing resistivity. At a resistivity of 3000 ohm-cm, the dielectric loss is approximately 0.1 dB/cm, which is acceptable. The effective dielectric constant, $\varepsilon_{\text{eff}}$ was calculated to be 6.06 for a CPW line, $S=100\mu$m, $W=50\mu$m. Experimentally, the $\varepsilon_{\text{eff}}$ and attenuation were obtained by deembedding these parameters from measurements of several CPW lines on silicon using software from NIST. The theoretical results showed that if silicon with resistivity of 3000 ohm-cm was used, the losses would be comparable with those of the same CPW lines on GaAs (Gallium Arsenide). CPW lines of varying geometries were fabricated on silicon with resistivity of 3000-4000 ohm-cm. The values obtained for $\varepsilon_{\text{eff}}$ and attenuation are shown in Figures 7 and 8 respectively. For the data shown, $S=50\mu$m, $W=25\mu$m, wafer thickness = 300$\mu$m and the gold thickness is approximately 1.7$\mu$m. Although no exact theoretical calculations have been done for these particular lines, the measured values are in the expected range. The noise in both curves around 34 GHz was found to be due to cable resonances.

The Coplanar Stripline and slotline structures were evaluated experimentally using resonator methods (since the NIST deembedding software only works for CPW structures).
These methods were first validated on a much cheaper and easier to handle microwave material - RT Duriod 5810.5. This material has a dielectric constant ($\varepsilon_r$) of 10.5 (silicon has one of 11.7) and a loss tangent of 0.0028. The slotline structure was evaluated using a ring resonator that produces multiple resonances allowing many frequencies to be evaluated. The Coplanar stripline was evaluated using a series gap coupled straight resonator. The results, experimental and theoretical are summarized in Table 2.

In order to test the slotline, a transition from a CPW to the slotline was developed, since CPW lines can be wafer-probed and slotlines cannot. Two different transitions were developed. The first makes use of a finite ground plane coplanar waveguide (FCPW) which is electromagnetically coupled to a slotline. The second makes use of a conventional CPW which is coupled to the slotline with an airbridge. The average measured performance of both transitions (measured using two back-to-back transitions with about 0.8" of slotline in between) on Duroid substrate gave a maximum insertion loss of -1.5 dB and return loss of better than -10 dB over the frequency range of 3 to 8 GHz.

**Second Year Objectives**

The efforts of the second year will focus on continuing the collaboration that has been established with the various universities and corporations. The team at Lewis will work more closely with these organizations in the growth and preparation of the SiGe material structures. Results obtained from ellipsometric and magneto-transport measurements carried out at Lewis, will be used to calibrate the growth process and to further understand the material characteristics of various SiGe structures.

The device processing efforts established during this first year will also be continued. The focus will be on improving the performance of the MOS transistor fabricated here at Lewis. Higher quality material, as well as a more complete understanding of processing procedures, will help make this possible. Once suitable material has been obtained and a device fabricated, the rf performance as a function of temperature, will be characterized using an custom variable temperature cryostat. Dramatic improvement in the rf performance is expected at the lower temperatures because of the increase in the mobility of the majority carriers.

Microwave studies will continue and expand to include the development of passive microwave applications on silicon. This will include determining loss as a function of resistivity for CPW lines and the continuing development of slotline and CPW striplines on silicon. Applications such as: phase shifters and antennas will be developed. This is in preparation for the third year effort which will involve combining the microwave passive with the active devices to form truly integrated SiGe circuits.

**Conclusion**

We have been successful in establishing collaboration with universities and industry for the growth of the SiGe structures. Results obtained from ellipsometric and magneto-transport measurements, carried out at Lewis, were used in the calibration of the growth process as well as to further understand the material characteristics of SiGe. Also, theoretical calculations of the band structure and I-V characteristics of some simple structures, were carried out using a code that was developed at Lewis. We have also been successful in establishing a SiGe device processing capability in the Lewis cleanroom. Preliminary results have been obtained for a MOS transistor device. Finally, we have favorably ascertained the feasibility of silicon as a substrate for microwave applications. Theoretical calculations have shown that transmission line losses are similar to those of GaAs if the substrate resistivity is...
kept above a certain value. We have also evaluated experimentally Coplanar Stripline and slotline structures using resonator methods.

References

Table 1: Results of ellipsometric study of SiGe structures. a) D-5983, mean square error = \(7 \times 10^{-4}\) b) UCLA MT-115, \(\lambda \leq 6400\) angstroms mean square error = \(2 \times 10^{-3}\)

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<td>Silicon</td>
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<td>113±3</td>
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<tr>
<td>Si₁₋ₓGeₓ</td>
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<td>(x=0.233±0.011)</td>
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<td>Substrate</td>
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Table 2: Characteristics of ring resonators on high resistivity silicon a) Slotline b) Coplanar Stripline

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<th>Computed (e_{\text{eff}})</th>
<th>Measured Attenuation</th>
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<th>Frequency (GHz)</th>
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<td>*</td>
<td>4.7451</td>
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Figure 1.—Ellipsometry data.
Figure 2.—Series resistance as a function of temperature for various Au/Sb/Au/Ti contacts on silicon.

Figure 3.—C-V curve of oxide on SiGe.

Figure 4.—Self gate aligned SiGe MOS-MODFET-device structure.

Figure 5.—Self gate aligned SiGe MOS-MODFET finished device.
Figure 6.—Theoretical dielectric losses of CPW lines on silicon as a function of resistivity.

Figure 7.—Measured attenuation.

Figure 8.—Measured effective dielectric constant.
Due to the large size and the number of diffusion pumps, space simulation chambers cannot easily be calibrated by the usual test dome method for measuring backstreaming from oil diffusion pumps. In addition, location dependent contamination may be an important parameter of the test. We have measured the backstreaming contamination in the Space Power Facility (SPF) near Sandusky, Ohio, the largest space simulation vacuum test chamber in the U.S.A. We used small size clean silicon wafers as contamination sensors placed at all desired measurement sites. The facility used diffusion pumps with DC 705 oil. The thickness of the contamination oil film was measured using ellipsometry. Since the oil did not wet uniformly the silicon substrate, two analysis models were developed to measure the oil film: (1) continuous, homogeneous film and (2) islands of oil with the islands varying in coverage fraction and height. In both cases, the contamination film refractive index was assumed to be that of DC 705. The second model improved the ellipsometric analysis quality parameter by up to two orders of magnitude, especially for the low coverage cases. Comparison of the two models for our case shows that the continuous film model overestimates the oil volume by <50%. Absolute numbers for backstreaming are in good agreement with published results for diffusion pumps. Good agreement was also found between the ellipsometric results and measurements done by x-ray photoelectron spectroscopy (XPS) and by scanning electron microscopy (SEM) on samples exposed to the same vacuum runs.

I. INTRODUCTION

The Space Power Facility (SPF) near Sandusky, Ohio is the largest vacuum space simulation test chamber in the U.S.A. The SPF was designed to simulate space environment over a wide range of thermal and vacuum conditions for testing advanced propulsion and space power systems. SPF’s unique size and high vacuum pumping capacity have facilitated testing of complete spacecraft, two-stage medium weight rockets, and upper atmosphere phenomena with minimal wall effects. The facility is operated by NASA Lewis Research Center. Starting in 1994, the Space Station Freedom (SSF) program will require testing of the SSF electrical power system hardware in a simulated space environment. The SPF was chosen for the tests. One of the concerns of testing the SSF electrical power system hardware is the possibility of contaminating the test article, with a possible subsequent reduction in performance. One of the very important possible contamination sources is oil backstreaming, especially of diffusion pump oil. However, other contamination sources, both organic (e.g., from lubricants and paints) and inorganic (e.g., dust particles) can also contribute. Due to the large size of the SPF vacuum chamber and possible temperature gradients, the contamination is expected to be location dependent.

This work was initiated to obtain a reliable quantitative estimate of the contamination in the SPF in a space simulation test. The usual method of measuring oil backstreaming, i.e., the test dome method, could not be used due to the chamber size. Several techniques have been tried, namely ellipsometry, x-ray photoelectron spectroscopy (XPS), residual gas analysis (RGA), nonvolatile residue (NVR) wipe samples, and scanning electron microscopy (SEM). This paper will report in detail the results obtained by ellipsometry. This technique gave location dependent quantitative results which were in qualitative agreement with the XPS and SEM data. To date, the other two methods (RGA and NVR) were not pursued beyond the initial tests and were not used in the final contamination estimate.

The paper is divided into three parts: experimental, results, and discussion. A short description of the SPF and the ellipsometric technique will be given in the experimental part. The second part describes the results obtained using two ellipsometric models, namely the island and the continuous film models, as function of position. The last part includes a discussion of the two models for analyzing the ellipsometric data, and an evaluation of ellipsometry versus the other techniques used in the SPF contamination experiments.

II. EXPERIMENTAL

The Space Power Facility (SPF) vacuum chamber has a 100-ft (30.5-m) diameter and a 121-ft (36.9-m) height. It offers the user 800,000 cubic feet (22,653.477 m³) of usable unobstructed volume. The vacuum system consists of 32 48-in.-diam liquid nitrogen (LN) baffled diffusion pumps mounted in the chamber floor. The diffusion pumps
are backed by a five-stage roughing train consisting of four stages of roots blowers in series and a single stage of three rotary-piston-type mechanical vacuum pumps in parallel. Under dry, clean, empty conditions, the chamber will achieve a pressure of $10^{-7}$ Torr. The pumpdowns conducted during this test program yielded a chamber pressure of $5 \times 10^{-6}$ Torr without complete LN flow to the baffles. The samples for ellipsometry consisted of small clean silicon wafers that were positioned at a variety of locations inside the vacuum chamber. Commercial silicon wafers were cut into roughly $1 \times 1$-cm pieces and were thoroughly cleaned for possible organic and inorganic contamination using the following procedure: boiling tri-chloroethylene, boiling acetone, boiling methanol, 30-s dip in 1:10 HF: $\text{H}_2\text{O}$, and rinse with deionized water. These silicon pieces will be named slides in this paper. For each vacuum pumpdown, slides were located within 2 ft of each diffusion pump and at eight other locations throughout the chamber, at different orientations and distances from the diffusion pumps.

The ellipsometer used in this work is a variable angle spectroscopic unit that was described previously and will not be repeated here. For a detailed description of ellipsometry, see Ref. 3. The instrument measures changes in the polarization of monochromatic light upon reflection from the sample in terms of the ellipsometric parameters $\psi$, and $\Delta$, (or $\tan \psi$, and $\cos \Delta$). Here $\psi$, and $\Delta$, are defined by

$$\tan \psi = \frac{R_\|}{R_\perp}$$

where $R_\|$ and $R_\perp$ are the complex effective reflection coefficients for light polarized parallel and perpendicular to the plane of incidence, respectively. The measurement of $\psi$, $\Delta$, is repeated at a variety of wavelengths (in the range of 3200–7500 Å) and angles of incidence (mostly 75°). The usual method of estimating the thicknesses $d_i$ of one or more overlayers on a substrate when the complex refractive index of all the films and the substrate are known consist of two steps. First, $R_\|$ and $R_\perp$ are calculated assuming continuous, homogeneous films with interfaces parallel to each other and to the substrate. Using Eq. (1), the calculated values $\psi$, and $\Delta$, are estimated. In the second step, a least square minimization procedure is used to find the values of $d_i$ that minimize the function

$$\sigma = (N - P)^{-1} \sum_i \left[ (\tan \psi_{i\|} - \tan \psi_{i\perp})^2 + (\cos \Delta_{i\|} - \cos \Delta_{i\perp})^2 \right].$$

The summation is over all $N$ experimental points, i.e., all wavelengths and angles of incidence. $P$ is the number of free parameters, $d_i$ in this case. In the oil contamination work, several slides, unexposed to the vacuum, were used as reference. They were analyzed in terms of crystalline Si (c-Si) with a $\text{SiO}_2$ overlayer, using published results for the complex refractive index versus wavelength. We obtained $\text{SiO}_2$ thicknesses in the range of 22–34 Å, but the values of $\sigma$ were higher than expected for a perfect $\text{SiO}_2$ film. However, we used this structure as the composite substrate in all our analyses, as it was not the accuracy limiting factor in this study. The oil contaminated samples were analyzed in two ways. First, we assumed a continuous oil film and used the procedure outlined above to find the thickness of this layer on top of the composite substrate. The oil used in the diffusion pumps was Dow Corning 705 (DC 705), which according to the published data has a refractive index of 1.579. This oil has very small absorption in the wavelength range of 3200–7500 Å used here, and thus the constant 1.579 value was used. Some of the results showed very poor fits to this simple model with rather large $\sigma$ values. In parallel, a scanning electron microscope (SEM) was used to observe the morphology of the contaminated samples. The SEM pictures show a discontinuous coverage of the slides. Thus, a second ellipsometric model was used, namely the islands' model. In the islands' model, the characteristic dimensions, i.e., the islands sizes and the interisland distances, are assumed to be much larger than the light wavelength. Thus, one of the main assumptions of the most common model for the optical behavior of a mixture, namely the effective medium approximation (EMA) is violated, and thus EMA and the islands' model do not overlap. In the islands' model, we also assume that the characteristic dimensions are smaller than the coherence length of the incident light. Thus, the reflectivity of the islands and the bare substrate will be independent, but will have to be added up due to the large light coherence length. Both these assumptions are well obeyed in the oil contamination samples for light in the visible and a spectral width of 20 Å. A detailed discussion of the conditions required for the application of the islands' model to the oil contamination problem as compared to the EMA will be given elsewhere. We found that the EMA model is not applicable in this particular case. In the islands' model, the reflected light from the overlayer covered composite substrate and the bare surface are superimposed in a coherent way, i.e.,

$$R_i = f R_{i\|} + (1 - f) R_{i\perp}$$

Here $\nu = p$ or $s$ polarizations, $R_{i\|}$ and $R_{i\perp}$ are the reflection coefficients for the covered and bare surface, respectively, and $f$ is the fraction of the surface covered by the overlayer.

III. RESULTS

Four pumpdowns were performed, with the following durations in hours: 28, 74, 100, and 72. Silicon slides were located at 39 points in the SPF vacuum chamber for each one of the 28-, 74-, and 72-h runs, and at 12 points for the 100-h run. The 32 diffusion pumps were divided into two groups: 16 in the north group and 16 in the south group. Besides the 32 slides located by the diffusion pumps, 7 others were located at important points in the chamber, e.g., east and west doors, top center, crane, RGA location, and others. An example of the way results were summarized is given in Table I. The example shows the ellipsometric analysis results for the 32 slides located by the 32 diffusion pumps: slides 1–16 are in the south side group and slides 17–32 are in the north side group. Besides the
Table I. Ellipsometrically determined oil contamination of all diffusion pumps in the SPF, using two analysis methods.

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<th>Pump number</th>
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<th>Islands' model</th>
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<td>( d , (\text{Å}) )</td>
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</tbody>
</table>

Pump number, Table I has the following columns: the continuous film trigonometric mean square errors (trig MSE) \( \sigma \), and thicknesses \( d \); and the islands' model results, namely the trig MSE \( \sigma \), the average island height \( t \), the island coverage fraction \( f \), and the parameter \( t \cdot f \). The \( t \cdot f \) parameter, measured in Å, is the equivalent oil thickness obtained in the islands' model, and should be compared with the continuous film thickness \( d \). We will use the \( t \cdot f \) parameter as an effective oil thickness throughout this paper. Table I clearly shows that the values of \( \sigma \) for the continuous film model are higher by up to two orders of magnitude as compared to those obtained using the islands' model. However, above \( f = 0.70 \), the islands' model converges into the continuous film model, giving almost the same \( \sigma \) values. A graph of the \( \sigma \) (trig MSE) values versus the islands fraction for the samples in Table I is given in Fig. 1. It shows that the islands' model gives good fits to the experimental data at all coverage fractions \( f \), but the quality of the fits is really excellent for \( f \) values at or below approximately 0.10, with \( \sigma \) at or below 10^{-3}. These excellent fits were also obtained for the 28-h run where all 39 samples had \( f < 0.10 \). In this short run, the islands' model \( \sigma \) values were in the range \( 4 \times 10^{-5} < \sigma < 2.5 \times 10^{-4} \). For comparison, the continuous film model for the 28-h run gave the range \( 3 \times 10^{-4} < \sigma < 1.7 \times 10^{-3} \). A more detailed quantitative comparison of the two models used here will be given elsewhere.10

A SEM picture of one of the slides (No. 32 in Table I) is given in Fig. 2. Several important results were obtained from the SEM picture: (1) Oil contamination gives a dis-
continuous film that covers the substrate in the form of disconnected islands. (2) The coverage value obtained by ellipsometry (0.114) is in good agreement with a visual estimate of 0.1. (3) The ideal islands' model is not completely applicable, as a small part of the islands start to wet the substrate and/or do not maintain their original shape. We repeated the SEM work on some of the slides several months later, and the number of broken up islands grew considerably. In addition, most of the higher coverage samples have a larger percentage of nonideal islands morphology. This fact explains the higher values of $\sigma$ obtained for these samples, as shown in Fig. 1.

Practical application of this method for discontinuous film effective thickness measurement will be enhanced if a simpler model is used. Many ellipsometers can measure the thickness of one continuous film. In Fig. 3 we compare the results of the effective thickness $t/f$ measured in the 72-h "proof of performance" run versus the results for the thickness $d$ obtained from the continuous film analysis on the same slides. We can clearly see two regimes: large and small thicknesses, and a crossover. As expected, at very high coverage fractions, i.e., near the continuous film regime with $f>0.70$, corresponding to films with thicknesses $d$ over 120 Å, the slope of the curve approaches 1. This result is reinforced by another measurement. In addition to the work on the SPF, we tested other vacuum chambers. In one of these tests, highly contaminated samples show continuous film coverage. For example, one sample had the
following results: continuous film model \( d = 229.1 \, \text{Å} \) and \( \sigma = 2.5 \times 10^{-3} \), islands' model \( t = 228.2 \, \text{Å}, f = 1.008, \) and \( \sigma = 2.4 \times 10^{-3} \). In this case, the islands' model is clearly not needed, although it converges to the correct answer, and it corresponds to a slope of 1 in Fig. 3. The small thicknesses regime in Fig. 3 corresponds to small coverage fractions and to a more ideal islands structure. Figure 3 clearly shows a linear dependence of \( t \cdot f \) on \( d \), for \( d < 100 \, \text{Å} \). We also examined the \( t \cdot f \) versus \( d \) relationship for the 28-h run and the result is shown in Fig. 4. A completely linear dependence was obtained, with a slope of 0.77 and a correlation coefficient of 0.990 showing excellent linearity. As will be shown in the discussion part, this result is only applicable for oil contamination work using our experimental 3200-7500-Å wavelength range.

Other observations obtained from analyzing the ellipsometric results were:

1. The slides from the 28-h run had the thinnest films of all four pumpdowns. This run gave an average \( t \cdot f \) value of 15.7 Å versus thicknesses of over 150 Å for other runs. In addition, this run has also the lowest deposition rate.

2. The south side diffusion pump slides show more contamination than the north side group. For example, in the 72-h run, the south side pumps have an average \( t \cdot f \) value of 184 Å versus only 118 Å for the north side group.

3. The oil films thicknesses decrease as the distance from the diffusion pump increases. For example, in the 72-h run, the slides by the diffusion pumps have a 151-Å average thickness versus only 34.2 Å for the other seven slides.

4. Backstreaming rate was calculated directly from the thickness of the oil films on the slides by the diffusion pumps, the length of the run and the oil density. For the three long runs an average backstreaming value of 0.37 \( \times 10^{-6} \, \text{mg/cm}^2/\text{min} \) was obtained. In contrast, the short 28-h run gave only 0.1 \( \times 10^{-6} \, \text{mg/cm}^2/\text{min} \) backstreaming rate.

IV. DISCUSSION

This part is divided in two main sections: (1) Comparison of ellipsometry to other oil contamination characterization methods used in the SPF calibration work, and its applicability for backstreaming estimates. (2) Discussion of the applicability of the continuous film results to quantitative oil contamination analysis.

Comparison of the ellipsometry work with SEM results was already discussed. Comparison with XPS is rather complex, as XPS is an excellent technique for characterizing the type of contaminant, but not as good in estimating the depth of the film. Ellipsometry and XPS are complementary techniques. In the SPF work, the conclusions from the XPS analysis compared to ellipsometry were the following:

1. The oil contamination is probably DC 705, as Si peaks were observed. In the ellipsometry work we used this result, i.e., it was an assumption.

2. For all samples, both the substrate and the silicon oil contamination were observed simultaneously, by XPS, denoting incomplete coverage. In ellipsometry, the islands' model gave much better fits than the continuous film model, pointing to the same result.

3. The short 28-h run gave almost undetectable silicon oil by XPS. Ellipsometry gave an average thickness (i.e., \( t \cdot f \) value) of 15.7 Å for the slides near the diffusion pumps, and 7.4 Å for other locations, accompanied by a very small (\( f < 0.10 \)) coverage.

4. The presence of silicon oil contamination by XPS decreased as distance from the diffusion pumps increased. This result was also found by ellipsometry, as given in the “results” part.

5. XPS shows that the south diffusion pump group had more silicon oil than the north group. This result was also found by ellipsometry, and it was consistent, i.e., it was measured for all four pumpdowns. Even in the case of the 28-h run, the south group had an average thickness (i.e., \( t \cdot f \) value) of 19.7 Å and the north group only 11.7 Å. Thus, an excellent agreement was found between XPS, SEM, and ellipsometry: XPS gave more information on the type of contamination, SEM showed the islands-type morphology, and ellipsometry gave the effective thickness and, thus, the backstreaming rate.

The backstreaming calculated from the ellipsometrically determined film thicknesses \( t \cdot f \) will now be compared with published data obtained for oil diffusion pumps using DC 705 and baffles. The present average result of 0.4 \( \times 10^{-6} \, \text{mg/cm}^2/\text{min} \) is lower than the value 5.3 \( \times 10^{-6} \, \text{mg/cm}^2/\text{min} \) reported by Hablanian on a 6-in. diffusion pump, but is in excellent agreement with the results obtained by Langdon and Fochtman. In Ref. 14, a chevron-baffled diffusion pump gave backstreaming values in the range 0.1-1.0 \( \times 10^{-6} \, \text{mg/cm}^2/\text{min} \), with most of the pumpdowns giving values around 0.5 \( \times 10^{-6} \, \text{mg/cm}^2/\text{min} \). The SPF also uses chevron-baffled diffusion pumps. However, an additional parameter should be considered in the backstreaming comparison and it is the oil molecules' sticking coefficient. The average backstreaming rate of 0.4 \( \times 10^{-6} \, \text{mg/cm}^2/\text{min} \) is based on a sticking coefficient...
near unity for the oil molecules that strike the silicon slide. As the sticking coefficient deviates from unity, the measured backstreaming rate would deviate from the actual rate. Additional work is required to quantify the sticking coefficient. A sticking coefficient would be required for both the oil molecules on silicon slides and oil molecules on oil.

We will now discuss the general applicability of the results shown in Figs. 3 and 4 for the continuous film to quantitative oil contamination analysis. We checked the universality of the experimental slope (0.77) found in Fig. 4 using a simulation. Assuming an ideal oil islands model, we calculated $\psi$, and $\Delta$, in the wavelength range 3200-7500 Å for films with different values of $t$ (300 Å $<$ $t$ $<$ 500 Å) and $f$ (0.02 $<$ $f$ $<$ 0.15), on top of a 22-Å SiO$_2$ on c-Si substrate. From these $\psi$, $\Delta$, values we calculated, using a least square fit, the thickness $d$ of a continuous oil film and the accompanying $\sigma$. We obtained a completely linear $t$ $-$ $f$ dependence on $d$, with a slope of 0.74 and a correlation coefficient of 0.9999 for the linear fit. The values of the calculated $\sigma$ changed in a similar way to the experimental ones, i.e., increasing very fast with increasing coverage fraction $f$. This comparison with theory again shows that our oil contamination samples with low values of $f$, are closely described by the ideal islands model. However, the calculated value of 0.74 for the slope is not universal. We recalculated the same $t$ $-$ $f$ versus $d$ dependence by simulation, using two wavelength ranges: 3200-5300 and 5301-7500 Å. We found only approximate linear dependencies, with slopes of roughly 1.1 and 0.5 for the two wavelength ranges, respectively, and for $f$ $<$ 0.1. In conclusion, the continuous film model generally gives only a rough approximation for the value of the effective oil thickness, and probably an error by a factor of 2 is possible for low coverage fractions. However, for our experimental range, the continuous film approximation is much better, and errors are smaller than 50%.

We will now comment on the anomalous low $t$ $-$ $f$ values for two points in Fig. 3. These points have continuous film thicknesses $d$ near 300 Å. These two points correspond to coverage fractions of 0.51 and 0.38, whereas all other points with $d$ $>$ 240 Å have $f$ $>$ 0.78. This result shows that in the $f$ range around 0.5, the $t$ $-$ $f$ versus $d$ graph also depends on $f$. It turns out that the north and south diffusion pump groups gave slightly different types of islands, with the north group average island height of 429 Å (standard deviation 86 Å), while the south group had an average $t$ $=$ 365 Å (standard deviation 107 Å). Thus, the two groups do not have the same morphology versus thickness, and the crossover between the islands model and the continuous film occurs at different values of the continuous film thicknesses.

V. CONCLUSIONS

A new technique for measuring oil backstreaming and other contamination in large vacuum chambers was demonstrated, namely ellipsometry. This technique can measure thicknesses of both continuous films of contaminants as well as discontinuous, island type of deposits. This last type was found in the DC 705 oil backstreaming experiment in the SPF. In either case, an a priori knowledge of the (complex) refractive index of the contaminants is required. This method is quantitative and it shows excellent agreement with results obtained by XPS and SEM. For an accurate determination of the contamination, the islands model is required. However, relatively good estimates of backstreaming can be obtained by the simplest ellipsometric model of a single continuous contamination film.

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1. Student interns at NASA Lewis Research Center, Cleveland, OH 44135.
12. D. Jayne, as reported in Ref. 1.
The quantum efficiency of HgCdTe photodiodes in relation to the direction of illumination and to their geometry

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In this paper a theoretical study of the effect of the direction of the incident light on the quantum efficiency of homogeneous HgCdTe photodiodes suitable for sensing infrared radiation in the 8–12 µm atmospheric window is presented. The probability of an excess minority carrier to reach the junction is derived as a function of its distance from the edge of the depletion region. Accordingly, the quantum efficiency of photodiodes is presented for two geometries. In the first, the light is introduced directly to the area in which it is absorbed (opaque region), while in the second, the light passes through a transparent region before it reaches the opaque region. Finally, the performance of the two types of diodes is analyzed with the objective of finding the optimal width of the absorption area. The quantum efficiency depends strongly on the way in which the light is introduced. The structure in which the radiation is absorbed following its crossing the transparent region is associated with both higher quantum efficiency and homogeneity. In addition, for absorption region widths higher than a certain minimum the quantum efficiency in this case is insensitive to the width of the absorption region.

I. INTRODUCTION

The present technology of choice for present and future infrared imaging systems is photovoltaic linear arrays and two-dimensional matrices, which can be coupled with a Si signal processor in the focal plane. The extensive interest in thin films of HgCdTe (either grown on a semi-insulating transparent substrate or thinned from bulk material) is associated with the possibility of illuminating the diodes from one side, and connecting the signal processor on the other side.

For the sake of simplicity we shall consider here only diodes in which the photocurrent is dominated by the contribution of photons absorbed only in one side of the diode. This is frequently the case that occurs when the diffusion length in one side of the junction is very short, or when one of the sides is either based on a wide-band-gap material or is too thin to absorb a significant number of photons. Hence, the photodiodes considered here are based on two different quasineutral regions—a transparent region and an opaque region in which the light is absorbed.

Theoretical and technological considerations usually dictate whether to realize frontside-illuminated diodes with a backside signal processor, or backside-illuminated diodes with a frontside signal processor. However, the analysis shows that the crucial parameter determining the quantum efficiency is the distance of the absorption site from the edge of the depletion region, rather than the side of illumination.

Our investigation will focus on two structures shown in Fig. 1. In the first one, presented in Fig. 1(a), the light reaches the transparent side first (TSF), passes through it and through the depletion region and then is absorbed in the opaque side. In the second structure [Fig. 1(b)], the light reaches the opaque side first (OSF), is partly absorbed there, and only then passes through the depletion region and reaches the transparent side.

Most of the present HgCdTe photodiodes fabricated for the purpose of thermal imaging are included within the above two categories as, for example, the following.

Ion-implanted n + p photodiodes fabricated on a thin HgCdTe film: due to the small thickness of the implanted n + region and to the low-minority-carrier lifetime there, the contribution of the n + side to the photocurrent is negligible. As demonstrated by Fig. 1, backside illumination is associated with the OSF configuration, while the frontside illumination is associated with the TSF configuration.

Pn or Np diodes realized on heterostructures: usually a structure of a thin narrow-band-gap material layer between a thin wide-band-gap material layer and a semi-insulating transparent substrate. In the case of a one-dimensional array the light can be introduced from either sides of the diodes, while in the case of two-dimensional arrays the light is usually introduced through the semi-insulating substrate (OSF configuration). Regardless of the direction of the illumination, photons with longer wavelengths are absorbed in the narrow-band-gap material only.

Hg-diffused diodes: realized by diffusing Hg into a heavily doped p-type material, forming a thin n-type area. Due to the short minority-carrier lifetime in the p side, the photocurrent is dominated by the contribution of the light absorbed in the n side. The Hg-diffused diodes are usually illuminated through the n side (therefore, OSF). In the case of a thin epitaxially grown p layer the diodes can be illuminated from the opposite side as well (TSF).

In this paper we present a theoretical study of the quantum efficiency of photodiodes fabricated on homogeneous thin films, to determine which of the two geometries renders higher quantum efficiency. Other figures of merit,
such as noise equivalent temperature difference (NETD) and $D^\text{Z}$ are proportional to the quantum efficiency. For instance, in the case of background limited-in-performance (BLIP) operation, $D^\text{Z}$ is given by

$$D^\text{Z} = \frac{R(\lambda)}{[2q(I_d + I_s)]^{1/2}} \frac{\hbar C(2A_dN_0\eta_{\text{sv}})^{1/2}}{\lambda},$$

(1)

where $R$ is the responsivity of the photodiode, $I_d$ and $I_s$ present the dark current and photocurrent, $A_d$ is the detector's optical area, and $N_0$ is the photon flux. $q$, $h$, and $c$ are constant with their regular meaning. $\eta(\lambda)$ and $\eta_{\text{sv}}$ represent the quantum efficiency at wavelength $\lambda$ and the average quantum efficiency in the relevant spectral region.

The effect of the structure of the device on the quantum efficiency, and the correlation between the quantum efficiency and other figures of merit of the photodiodes, have led to the publication of many works in the literature. van der Wiele\textsuperscript{1} solved the one-dimensional diffusion equation in silicon, and presented the quantum efficiency associated with both frontside and backside illuminations. More recently, Rogalsky and Rutkowski\textsuperscript{4} used the above-mentioned equations, and analyzed the quantum efficiency of a PbSnTe one-dimensional diode. Other interesting works are those by Shappir and Kolodny,\textsuperscript{5} Levy, Schacham, and Kidron,\textsuperscript{4,5} and Briggs\textsuperscript{6} who, based on numerical and analytical approaches, presented computer solutions for the two-dimensional and three-dimensional cases.

Most of the published works do not deal with HgCdTe in particular, and therefore rightly ignore the asymmetrical structure which characterize the HgCdTe diodes. Their published analytical equations, for both frontside or backside cases, are rather complicated and therefore the geometrical dependence is concealed. In addition, the wavelength dependence of the absorption coefficient and the geometrical effects; however, their approach, based on two-dimensional Fourier series, totally concealed the geometrical dependence of the quantum efficiency.

One of the objectives of the theoretical study presented here is to emphasize the geometrical dependence of the quantum efficiency in homogeneous photodiodes and to determine whether the OSF or TSF illumination is preferable. We therefore present in Sec. II a one-dimensional analytical equation which describes the probability of the minority carriers generated at a known distance from the edge of the depletion region, to reach the junction and to participate in the photocurrent. We show that this probability depends strongly on the distance of the absorption site from the edge of the depletion region, and emphasize the importance of absorption close to the junction. In Sec. III we use the above-calculated probability, and Planck's radiation law, and compute the quantum efficiency of OSF and TSF HgCdTe photodiodes in the 8-12 µm region. In Sec. IV we demonstrate the superiority of the TSF geometry by presenting an example based on two HgCdTe photodiodes.

Our study does not take into account effects caused by variation in composition or doping which sometimes occur close to the junction. Thin layers grown by liquid-phase epitaxy and more recently by molecular-beam epitaxy (MBE) or metalorganic chemical-vapor deposition (MOCVD) have composition variation throughout the layer. The resulting electric field accelerates minority carriers toward the junction, regardless of the direction of the illumination, and therefore yields higher quantum efficiencies in both OSF and TSF photodiodes. The gradient in composition results in variations of the absorption coefficient, band gap, intrinsic concentration, and other material parameters, and therefore the complex diffusion equations that yield the quantum efficiency can only be solved using numerical methods. Hence, the study of the quantum efficiency in nonhomogeneous photodiodes is performed separately and will be published elsewhere.

Even though it is shown that the TSF configuration is preferable for photodiodes fabricated on homogeneous material, frequently technological considerations rather than fundamental physical principles dictate the use of the OSF configuration. One of the important technological limitations is that caused by the metal layer which can shield a significant fraction of the incoming light. This limitation, which is usually associated with frontside illumination, can place another limit on the quantum efficiency of both OSF and TSF photodiodes. Consequently, both the TSF and OSF structures are fully analyzed in this paper. The maximal quantum efficiencies as well as the optimal thickness of the absorption volumes, in terms of diffusion lengths, surface recombination velocities, and absorption coefficients, are presented.

II. QUANTUM EFFICIENCY AS A FUNCTION OF ABSORPTION DEPTH

In this section the probability of a minority carrier generated at a distance $x_0$ from the junction to reach the
junction is calculated. This probability is equal to the quantum efficiency associated with photons absorbed at the same distance.

Our assumptions are that both the length and the width of the diode are larger than the diffusion length and therefore the one-dimensional treatment is valid. We also assume low injection conditions, an abrupt junction, a very thin depletion layer, a constant minority-carrier lifetime and a constant dopant concentration along the quasineutral regions.

Let us consider the diode of Fig. 2. Assume that somehow the light is uniformly absorbed only in a narrow n-type volume \( A_j \) at a distance \( X_0 < X < X_1 \) from the edge of the depletion region. In order to calculate the resulting photocurrent, the steady state of the minority-carrier distribution close to the junction must be found, and therefore the continuity equations for the three regions must be solved,

\[
\begin{align*}
D_p \frac{d^2 \hat{P}_1}{d x^2} - \frac{\hat{P}_1}{\tau_p} &= 0, & 0 < x < x_0, \\
D_p \frac{d^2 \hat{P}_2}{d x^2} + G_L &= 0, & x_0 < x < x_1, \\
D_p \frac{d^2 \hat{P}_3}{d x^2} - \frac{\hat{P}_3}{\tau_p} &= 0, & x_1 < x < d_n,
\end{align*}
\]

where \( p_1, p_2, \) and \( p_3 \) are the minority-carrier concentrations. \( d_n, D_p \) and \( \tau_p \) represent the width of the neutral region and the minority-carrier diffusion coefficient and lifetime, respectively. The uniform optical generation rate is given by \( G_L = N_0 \gamma (X_1 - X_0) \), where \( N_0 \) is the induced photon flux.

The boundary conditions for the problem are

\[
\hat{P}_1(x) = \frac{n_j^2}{N_p} \left( e^{\gamma v / k T} - 1 \right), \quad \frac{d \hat{P}_1}{dx} \bigg|_{x = d_n} = -S_n \hat{P}_3(d_n),
\]

where \( S_n \) is the surface recombination velocity. Solving the problem for the short-circuit condition, one obtains for the first zone

\[
\hat{P}_1(x) = 2A \cosh \left( \frac{x}{L_p} \right),
\]

\[
A = -\frac{N_0 L_p^2}{D_p (1 + K)} \left( e^{X_0 / L_p} - e^{-X_0 / L_p} - e^{X_1 / L_p} + K e^{-X_1 / L_p} \right),
\]

\[
K = e^{X_0 / L_p} \left( \frac{1 + \beta}{1 - \beta} \right), \quad \beta = S_n L_p / D_p,
\]

where \( L_p \) is the diffusion length of the minority carriers, given by \( L_p = (D_p \tau_p)^{1/2} \). Knowing \( p_1(x) \) the diffusion photocurrent can be obtained by

\[
I_L = -q A D_p \frac{d \hat{P}_1}{dx} \bigg|_{x = 0} = q A n_0 \left( e^{X_0 / L_p} - e^{-X_0 / L_p} - e^{X_1 / L_p} + K e^{-X_1 / L_p} \right) \left( 1 + k \right) \left( X_1 - X_0 \right) / L_p.
\]

The term in the large parentheses represents the fraction of holes that is collected by the junction, and forms the photocurrent. This fraction can be treated as the quantum efficiency of the diode, while illuminated in the way shown in Fig. 2. Rewriting the quantum efficiency as

\[
\eta'(X_0) = \frac{1}{(1 + K)} \left( e^{X_0 / L_p} + K e^{-X_0 / L_p} \right),
\]

we finally obtain

\[
\eta'(X_0) = \frac{1}{(1 + K)} \left( e^{X_0 / L_p} + K e^{-X_0 / L_p} \right),
\]

where \( \eta' \) represents the density of the quantum efficiency of holes generated at a distance \( X_0 \) from the edge of the depletion region. It should be emphasized that this quantum efficiency depends on three parameters only: the carrier's initial distance from the depletion region \( X_0 \), the parameter \( \beta \), and the width of the neutral region \( d_n \). It does not depend on the way in which the light is introduced, or on optical parameters such as the absorption coefficient and the photon's energy.
III. THE OVERALL QUANTUM EFFICIENCIES FOR TSF AND OSF CONFIGURATIONS

Let us assume that the photodiodes of Fig. 1 are illuminated with monochromatic photon flux either from their transparent side (a) or from their opaque side (b). Let us further assume that the reflected photon flux in both geometries is negligible. The generation function due to monochromatic photon flux \( N_0 \), with wavelength \( \lambda \), is given in the TSF case by

\[
G_L(X,\lambda) = \alpha(\lambda) N_0 e^{-\alpha(\lambda)X},
\]

where \( \alpha(\lambda) \) is the absorption coefficient. Similarly, in the OSF configuration the generation function \( G_L \) is given by

\[
G_L(X,\lambda) = \alpha(\lambda) N_0 e^{\alpha(\lambda)(X-d_0)},
\]

where \( d_0 \) is the width of the quasineutral region.

Since the continuity equation is a linear one, Eqs. (9) and (10) can be used to calculate the quantum efficiencies associated with monochromatic photon flux. For the TSF photodiode the quantum efficiency \( \eta_{TSF} \) is given by

\[
\eta_{TSF}(\lambda) = \frac{1}{\alpha L_p} \left[ \frac{1}{1 + \frac{\alpha L_p}{\lambda}} \right] e^{-\alpha L_p} + \frac{\beta}{\lambda} \cosh \left( \frac{d_0}{L_p} \right) \sinh \left( \frac{d_0}{L_p} \right) - \frac{1}{\alpha L_p} e^{-\alpha L_p}.
\]

while for the OSF photodiode the quantum efficiency \( \eta_{OSF} \) is given by

\[
\eta_{OSF}(\lambda) = \frac{1}{\alpha L_p} \left[ \frac{1}{1 + \frac{\alpha L_p}{\lambda}} \right] e^{-\alpha L_p} + \frac{\beta}{\lambda} \cosh \left( \frac{d_0}{L_p} \right) \sinh \left( \frac{d_0}{L_p} \right) - \frac{1}{\alpha L_p} e^{-\alpha L_p}.
\]

Equations (11) and (12), which present the quantum efficiency in terms of surface conditions, dimensions, and absorption coefficients, are widely known and used in the literature,\(^1,7,8\) however, they give the quantum efficiency associated with the uncommon case of monochromatic photon flux. HgCdTe photodiodes packaged in infrared imaging systems are usually exposed to radiation emitted from bodies with temperatures of about 300 K. Hence, the flux is usually composed of photons of different wavelengths as described by Plank's radiation law. Therefore, the relevant quantum efficiency for both the OSF and the TSF cases should be obtained by integrating the relative contributions of all photons. While doing so, the dependence of the absorption coefficient on the photons' wavelength should be taken into account (see the Appendix). Hence,

\[
\eta_T = \frac{\int_{\lambda_{min}}^{\lambda_{max}} \eta_{TSF}(\lambda, T) n(\lambda, T) d\lambda}{\int_{\lambda_{min}}^{\lambda_{max}} n(\lambda, T) d\lambda},
\]

\[
\eta_O = \frac{\int_{\lambda_{min}}^{\lambda_{max}} \eta_{OSF}(\lambda, T) n(\lambda, T) d\lambda}{\int_{\lambda_{min}}^{\lambda_{max}} n(\lambda, T) d\lambda},
\]
FIG. 4. The quantum efficiency of TSF illuminated Hg$_{1-x}$Cd$_x$Te photodiode vs the thickness of the n-type layer with the diffusion length of the holes as a parameter. The bulk composition is $x=0.221$, the hole mobility coefficient is $\mu_p = 1000 \, \text{cm}^2/\text{V} \cdot \text{S}$ (Ref. 16) and the surface recombination velocity is $S_n = 0$.

where $\eta_{\text{TSF}}$ and $\eta_{\text{OSF}}$ are given by Eqs. (11) and (12), $\lambda_{\text{on}}$ and $\lambda_{\text{off}}$ are the system's cut-on and cut-off wavelengths, $n(\lambda, T)$ (photons/cm$^2$ s µm) is the spectral radiant photon emittance of the target as given by Planck's radiation law, and $T$ is the temperature of the target.

IV. RESULTS

Technological considerations rather than fundamental physical principles usually dictate the fabrication of photodiodes based on p-type material, although the longer lifetime of the minority carriers in the n-type material makes it preferable for infrared sensing. However, since our objective is to emphasize the physical and geometrical principles, here we disregard the technological obstacles by assuming that the substrate is a high-quality n-type material. This high-quality material is characterized by high values of both mobility and lifetime of the minority carriers. In addition, we assume in our two example photodiodes excellent surface recombination velocities in both diodes, which yield electrical reflecting conditions for the holes. Hence, the two above-mentioned photodiodes differ only in the direction of illumination.

Figures 4 and 5 show the quantum efficiencies obtained in the two configurations as calculated from Eqs. (13) and (14). Both figures show the quantum efficiency versus the width of the absorption volume with the diffusion length of the minority carriers as a parameter. The hole mobility coefficient was assumed to be $\mu_p = 1000 \, \text{cm}^2/\text{V} \cdot \text{S}$ (Ref. 10) and the surface recombination velocity was assumed to be very low ($S_n = 0$). The hole lifetime varies from 38 nS up to 2 µS which yields minority diffusion lengths from 5 up to 35 µm. We chose Hg$_{1-x}$Cd$_x$Te with $x=0.221$ which yields a reasonable value for the cut-off wavelength (11 µm) for a hole lifetime of 100 nS, at 77 K. Consequently, $\lambda_{\text{on}}$ and $\lambda_{\text{off}}$ were taken to be 8 and 11 µm, respectively.

The superiority of the TSF photodiode in the case of reflecting surface conditions is clearly seen. To begin with, the quantum efficiency obtained for the TSF photodiode is always larger than that obtained for the OSF photodiode. In the case of the material with a minority-carrier diffusion length of 35 µm, the maximal quantum efficiencies obtained are 92% and 87%, for the TSF and OSF configuration, respectively. For materials with shorter diffusion lengths the relative difference between the two configurations is even more significant. For example, in the case where $L_p = 5 \, \text{µm}$, the maximal values of the quantum efficiencies were 54% and 48%, for the TSF and OSF configurations, respectively.

In addition to the differences in the values of the quantum efficiency, the difference in the sensitivity of the two photodiodes to the width of the n-type layer is obviously noticed. It is clearly seen that in the case of the OSF configuration there is an "optimal" thickness of the n-type layer for each value of the diffusion length. It is also clearly seen that the quantum efficiency is rapidly degrading as the n-type layer thickness deviates from its optimal value; however, in the case of the TSF configuration the quantum efficiency reaches a saturation value which is very close to the maximal value. Therefore, the term "optimal thickness" of the n-type layer, used in the OSF illuminated diode, is not valid, and the term "minimal thickness" should be applied.

The strong dependence of the quantum efficiency on the width of the absorption region, as it exists in OSF illuminated photodiodes, is a serious limitation, since the width of the n-type region can vary along an array of photodiodes. This results in a severe nonhomogeneity in the quantum efficiencies and in the performance of the photodiodes. This yields a significant degradation in the system's figures of merit, such as NET. Excellent surface conditions in HgCdTe are not easily
achieved. Most of the published data concerning the surface recombination velocity in n-type material is related to photoconductors. Since the photoconductors require accumulation conditions, the reported data is of no value to Hg$_{1-x}$Cd$_x$Te photodiodes with $x=0.2$, which require a weak depletion condition. Hence, we chose the surface recombination velocity in our example diodes to be $10^4$ cm/s, which is a practical value for p-type material.

Figures 6 and 7 show the quantum efficiencies obtained for $S_n=10^4$ cm/s in the two configurations. Once again, the superiority of the TSF configuration (in terms of high quantum efficiency and homogeneity) is seen very clearly. In addition to the two above-mentioned advantages of the TSF configuration, Figs. 4–7 demonstrate a third one: The TSF illuminated diodes reach a saturation value, and therefore are less sensitive to the surface recombination velocity in the edge of the n-type layer.

Figure 8 shows the maximal quantum efficiency obtained for the OSF configuration with $\beta$ as a parameter, as well as the saturation value of the quantum efficiency obtained for the TSF case (which is close to the maximal value). It should be noted, however, that the surface recombination velocity $S_n$ is not constant along the horizontal axis since the diffusion length is changing, and $S_n=(\beta D_p/L_p)$, as indicated by Eq. (4). Figure 8 demonstrates clearly the two advantages of the TSF illumination case: For the same quality of the material (i.e., the same diffusion length) the quantum efficiency associated with the TSF case is always higher than that associated with the OSF case, and does not depend upon the surface condition.

Figure 9 shows the optimal thickness of the n-type layer versus the hole diffusion length with $\beta=0$, for both TSF and OSF cases. It should be mentioned that in the OSF case, the width drawn in Fig. 9 is the optimal width, and the quantum efficiency rapidly degrades when a different width is applied. In the TSF case, however, the plotted width is the minimal width, and the associated quantum efficiency remains constant for values higher than the minimum.

Figure 9 indicates an additional advantage of the TSF case. For the same diffusion length the thickness of the optimal absorption region associated with the TSF configuration is smaller than that associated with the OSF configuration; hence, there is less diffusion leakage current in the TSF diode.

V. SUMMARY

We have presented a theoretical study of the quantum efficiency of HgCdTe photodiodes fabricated on thin films, with the objective to emphasize the geometrical depen-
FIG. 9. The thickness of the n-type layer (for which the maximal quantum efficiencies are obtained), vs the diffusion lengths of the holes. This thickness is the minimal thickness in the TSF case, and the optimal thickness in the OSF case.

\[ \alpha(x, T, E) = \gamma (E - E_g)^{1/2}, \]  
\[ (A1) \]

where \( E \) is the energy of the photon, \( E_g \) is the band gap, and \( \gamma \) is a coefficient that depends on the material and temperature only. Radiation is absorbed also at energies lower than the band gap, a process known as the Urbach tail.\(^7\) The absorption coefficient associated with the Urbach tail in HgCdTe is given by\(^8\)

\[ \alpha(x, T, E) = \alpha_0 e^{(e^2(E - E_0)/W)}, \]  
\[ (A2) \]

where \( x \) is the composition, \( T \) is the temperature, \( E \) is the energy of the photon, and \( \alpha_0, \sigma, W, \) and \( E_0 \) are fitting parameters. Finkman and Schacham\(^9\) measured the absorption coefficient over the temperature range \( 80 \, \text{K} < T < 300 \, \text{K} \) and obtained

\[ E = \frac{hc}{\lambda} \, (\text{eV}), \]
\[ \alpha_0 = \exp(53.61x - 18.88) \, (\text{cm}^{-1}), \]
\[ \sigma = 3.267 \times 10^4 (1 + x) \, (\text{K/eV}), \]
\[ W = 81.9 + T \, (\text{K}), \]
\[ E_0 = 1.838x - 0.3424 + 0.148x^4 \, (\text{eV}). \]

In a previous work\(^10\) an expression for \( \gamma \) was derived, based on the assumption that the absorption coefficient and its derivative are continuous. Hence,

\[ \gamma = (2\sigma e/W)^{1/2} \alpha_0 e^{(e^2(E - E_0)/W)}, \]  
\[ (A3) \]

where \( e \) is the base of the natural logarithm.

ACKNOWLEDGMENTS

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APPENDIX

The absorption coefficient in semiconductor materials such as HgCdTe is given for energies higher than the band gap by
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SECTION THREE

HIGH TEMPERATURE SUPERCONDUCTIVITY
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Since the discovery of high temperature superconductivity in 1987, NASA Lewis Research Center has been involved in efforts to demonstrate its advantages for applications involving microwave electronics in space, especially space communications. The program has included thin film fabrication by means of laser ablation. Specific circuitry which has been investigated includes microstrip ring resonators at 32 GHz, phase shifters which utilize a superconducting, optically activated switch, an 8x8 32 GHz superconducting microstrip antenna array, and an HTS-ring-resonator stabilized oscillator at 8 GHz. The latter two components are candidates for use in space experiments which will be described in other papers. Experimental data on most of the circuits will be presented as well as, in some cases, a comparison of their performance with an identical circuit utilizing gold or copper metallization.

Thin Film Fabrication

High quality thin films of YBCO have been deposited by means of ablation of stoichiometrically correct targets by a pulsed excimer laser. The facility is shown schematically in Figure 1.

A typical deposition is carried out by evacuating the sample chamber to 3x10^-7 torr or less, warming the substrate to near 500°C, introducing a continuous flow of oxygen (120 sccm) into the chamber, and heating the sample to 775°C. During deposition, chamber pressure is approximately 170 mtorr. The laser wavelength is 248 nm; the energy density is typically 1.5 J/cm²/pulse, with a pulse repetition rate of 4 pps. Following deposition, the oxygen pressure is raised to 1 atm.
atmosphere and the sample allowed to cool prior to removal from the chamber.

Using this technique, strongly c-axis oriented YBCO films have been deposited on strontium titanate, lanthanum aluminate, and MgO. The most useful of these, in terms of the film characteristics and the microwave properties of the substrate, are those on lanthanum aluminate, where a Tc of 90.6K was achieved, with a critical current density of 2x10^6 amps/cm² at 77K. A typical measurement of DC resistance vs. temperature is shown in Figure 2.

Figure 2. Measured DC Resistance of YBCO Film

MICROWAVE CIRCUITS

Microstrip Ring Resonators

Among the first microwave circuits to be fabricated and tested was the microstrip ring resonator at 35 GHz. A schematic diagram of this device is shown in Figure 3.

Figure 3. Microstrip Ring Resonator

Q-values of such devices yield realistic estimates of the microwave performance of superconducting circuits since they reflect both conductor and dielectric losses, as would a functional application. Results for two such resonators, one fabricated from YBCO and the other from Tl₂Ca₂Ba₂Cu₃O₇ (TCBCO), deposited at the University of Cincinnati, are shown in Figure 4.
Both circuits use a normal metal ground plane. It is clear that at 35 GHz, neither superconducting resonator is much superior to an identical gold circuit. At lower temperatures, however, the Q of the YBCO resonator is four to five times that of gold, while the TCBCO one is approximately three times that of gold.

Superconducting Phase Shifters

One device which, in principle, could benefit greatly from the use of superconductivity is the true-time-delay phase shifter. Such a circuit, which is required for electronically steered phased array antennas, switches an RF signal between two alternate paths, one of which is physically longer than the other so as to provide a true time delay phase shift. Such devices, using a field effect transistor as the active switching element, will typically exhibit insertion losses of one or two dB, so that a five bit phase shifter, as would be required in order to obtain phase resolution of 11.5 degrees would suffer a loss of 5 to 10 dB. The use of a superconducting patch as the switching element should provide considerable improvement. The layout for such a phase shifter is shown in Figure 5.
faster switching times are unlikely unless a low thermal conductivity substrate with acceptable microwave properties can be identified. A possible candidate for such a material is yttrium-stabilized zirconia (YSZ), which has been used in the fabrication of another device. Data for this circuit are not yet available.

Microstrip Array Antennas

Dinger 5 has shown that the gain of a multielement microstrip array at millimeter wave frequencies is limited by the ohmic losses in the power divider network, which becomes increasingly complex as the number of radiating elements increases. Work at NASA Lewis, carried out in collaboration with Ball Aerospace, has produced a 64 element (8x8) array antenna operating at 35 GHz. The superconducting film is TCBCO, which is deposited on a two-inch diameter lanthanum aluminate substrate. The TCBCO film was fabricated by Superconductor Technologies Inc., while the array was designed and fabricated by Ball and tested at NASA Lewis. A photograph of the array in its test fixture is shown in Figure 6.

Figure 6. 64-Element Microstrip Antenna Array

Results of gain tests, using the antenna as a receiver are shown in Figure 7.
As is clearly demonstrated, at 35 GHz, the superconducting 8x8 array and power divider network have approximately 2 dB higher gain than an equivalent cooled gold antenna. Relative to a gold array at room temperature, the HTS antenna exhibited an improvement of approximately 5 dB at temperatures below 90K.

HTS-Resonator-Stabilized Oscillator

By using planar resonators fabricated from superconducting films, it should be possible to implement stable microwave oscillators, such as are now designed using crystal oscillators or dielectric-resonator-stabilized oscillators (DRO). Such a structure would be highly amenable to integration with semiconductor components and would have the advantages of reduced circuit complexity and increased reliability, with only a small sacrifice in performance. Typically, one would anticipate unloaded Q's near 10,000 (at 8 GHz) from a planar superconducting resonator, as compared with the 10,000 to 20,000 possible from a DRO, and the 1000 possible for a planar structure using normal metals. Such a Q should make possible a superconductor-stabilized oscillator with a phase noise better than -100dBc/Hz. Although data is not yet available, the design for such a resonator is complete, and is shown in Figure 8.

Figure 8. Layout of an HTS-Resonator-Stabilized Oscillator

CANDIDATE FLIGHT EXPERIMENTS

Shuttle/ACTS Communications Experiment

The antenna described above, combined with an appropriate phase shifter is intended to be the forerunner of a steerable array which can
be installed on the space shuttle to form the receive terminal of an earth-to-geo-leo 30/20 GHz communications link. A schematic representation of the experiment is shown in Figure 9.

![Figure 9. Schematic Representation of ACTS/Shuttle Communications Experiment Using an HTS Antenna](image)

Details of the experiment are described in another paper at this conference.

HTSSE-II

Together with JPL, NASA Lewis is developing a low noise receiver as a candidate to be flown on NRL's HTSSE-II flight experiment. An overall block diagram of the receiver is shown in Figure 10.

![Figure 10. Block Diagram of Lewis/JPL HTSSE-II Receiver](image)

The receiver will employ the superconducting oscillator described earlier in this paper, a superconducting input filter, together with cryogenically-cooled, normal metal low noise amplifier and mixer, both of which will utilize conventional semiconductor components. More details of the experiment are given in another paper at this meeting.
REFERENCES


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Y-Ba-Cu-O SUPERCONDUCTING/GaAs SEMICONDUCTING HYBRID CIRCUITS FOR MICROWAVE APPLICATIONS

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ABSTRACT

We have combined a two pole superconducting bandpass filter with a packaged GaAs low noise amplifier, and have designed, fabricated, and tested a superconducting X-band oscillator. Both circuits have been compared to normal metal circuits at 77K. This paper presents the results of these experiments, technical issues, and potential applications.

INTRODUCTION

Before the discovery of high temperature superconducting (HTS) materials, the integration of low-Tc superconductors with semiconducting devices was not feasible since many semiconducting devices experience carrier freeze-out below 10K. Demonstrations of HTS passive microwave components operating at liquid nitrogen (77K) temperatures [1,2] has enhanced the feasibility of integrating HTS passive components with semiconductors to achieve high performance microwave systems [3]. GaAs and heterostructure microwave semiconducting devices make strong candidates for integration since they have much lower noise figures at 77K [4,5] than at 300K, while the operating temperature of 77K also avoids the problem of carrier freeze-out. To achieve the maximum benefit of HTS materials the level of integration between passive and active elements must be increased to the point where entire systems can operate reliably at liquid nitrogen temperatures for extended periods of time.

Integration of passive HTS devices with semiconductor devices can be achieved from the discrete component level up to the system level. Such a progression is shown in Figure 1. Levels 1 and 2 are now feasible due to the demonstration of high Tc superconducting microwave devices. Level 3 work is in the early stages at the present time. To determine the performance advantages at the subsystem level, we have combined a two pole superconducting bandpass filter with a packaged GaAs low noise amplifier (LNA), and compared its performance with a gold filter/LNA hybrid circuit down to 35K. At the circuit level, we have designed, fabricated, and tested an X-band hybrid superconducting/GaAs oscillator on a single lanthanum aluminate substrate, where a high Q superconducting resonator is used for stabilization of the oscillator. High quality Y-Ba-Cu-O (YBCO) superconducting films were used in both experiments.

BPF/LNA HYBRID CIRCUIT

Several two-pole bandpass filter were designed with a 2.5 percent bandwidth, 0.5 dB passband ripple, and 7.5 GHz center frequency. The filters were fabricated using laser ablated YBCO superconducting films (approx. 5000A) on a 0.01 inch lanthanum aluminate substrate. Gold film deposited by E-beam evaporation on the opposite side of the substrates formed ground planes for the circuits. An identical filter using gold film for the microstrip was also fabricated.

The LNA selected was an Avantek PGM 11421 with a specified bandwidth of 4 to 11 GHz, a gain of 8.0 dB, and a noise figure of 2.5 dB. A diagram of the hybrid is shown in Figure 2. The devices were connected by 0.010 inch gold bond wires to a 50 ohm microstrip line that was fabricated on a 0.01 inch thick Duroid (e=2.3) substrate. Gold film deposited by E-beam evaporation on the opposite side of the substrates formed ground planes for the microstrip. The hybrid was mounted on a brass test fixture using a conductive epoxy. SMA female flange connectors were used for the microstrip to coax transition.

All cryogenic measurements were made inside a closed cycle cryostat which has semi-rigid coaxial cables providing a connection between the...
two temperature environments. An HP 8510B automatic network analyzer (ANA) was used to measure insertion gain or loss. A full two port calibration was performed inside the cryostat so as to move the reference planes of the ANA to the ends of these cables. Since this experiment is concerned only with relative changes in system performance, a two port cal was chosen over a TRL or LRL, that would have moved the reference planes of the ANA onto the test fixture. Noise figure measurements were made on a HP6970A noise figure meter, with loss compensation used to account for the test fixture's contribution to the system noise figure.

The LNA and filters were tested individually to determine their gain or loss and noise figures at T=300K and 77K. The HTS filter showed a significantly smaller insertion loss than the gold filter at 77K, due to the near elimination of conductor loss in the YBCO film compared to the gold conductor. Most of the HTS filter loss is due to the gold ground plane; if it were replaced with HTS material the insertion loss would be nearly eliminated. At 77K the gold hybrid shows a noise figure improvement of 3.5 dB compared to 300K, while the HTS hybrid shows a 5.5 dB improvement compared to gold plane; if it were replaced with HTS material the insertion loss would be lower. The gain of the HTS hybrid is greater than the gain of the gold hybrid due to lower insertion loss in the HTS filter [6].

SUPERCONDUCTING OSCILLATOR

The high "Q" observed in superconducting resonator circuits [7] can be exploited in low noise hybrid oscillator design. These oscillators have the potential to replace dielectric resonator stabilized oscillators in cryogenic applications.

Several hybrid GaAs/superconducting microwave oscillators were fabricated on 1cm³ lanthanum aluminate substrates and tested. The design used a ring resonator in the reflection mode. A ring with a resonant frequency of 10 GHz was placed a quarter wavelength from the drain of the FET, parallel coupled to the output transmission line with a coupling gap 40 microns long. The oscillator output was taken at the drain. The best circuit had an output power of 6.4 dBm at 77K, which corresponds to an efficiency of 10.4%. The layout of the oscillator circuit is shown in Figure 4. For the HTS circuits, the transmission lines, rf chokes (radial stubs), and bias lines were fabricated using YBCO films, only the ground planes were fabricated in gold.

Toshiba low noise GaAs FETs (JS8830-8) were used in the design. Their S-parameters were measured from 4 to 26.5 GHz, over temperatures from 300K to 40K under a bias of Iงาม=10ma and V_short=3V. V_bias was adjusted from -1.04V at 300K to -1.19V at 40K to maintain the desired bias condition. Of all the S-parameters measured, the magnitude of S21 showed the most variation over temperature, due to the increased electron mobility as the temperature was decreased. The S-parameter measurements from 15 to 26.5 GHz were unreliable due to a loss of calibration at those frequencies at the lower temperatures. This was most noticeable in the values for S21. This problem has been reported before [8]. The oscillator circuit design based on the measured S-parameters at 77K, was performed, and then optimized using Touchstone [9].

Both copper and HTS circuits were fabricated and tested for comparison purposes. They were mounted on a brass test fixture inside a closed cycle cryostat. The circuits oscillated at 10 and 20 GHz, the 20 GHz signal was 20 dB below the fundamental. The copper circuit showed little frequency sensitivity to temperature, varying about -70 kHz/K from 25K to 100K. The best HTS circuit showed a sensitivity of -10 MHz/K in the vicinity of 77K. This oscillator worked up to 87K. Figure 5 plots output power vs. temperature for several circuits and Figure 6 shows output frequency vs. temperature.

The frequency of the copper circuit changed very little. The power decreased from 4.5 dBm at 25K to 2.8 dBm at 100K. The efficiency of the circuit at these bias conditions at 77K was 4.1%.

TECHNICAL ISSUES

It should be noted that temperature cycling of devices or systems is probably the most stressful thermal condition that can be placed on them. On the other hand, operation at stable cryogenic temperatures for extended periods of time should enhance the performance of semiconducting devices. Besides lower noise figures, cryogenic operation will in general lead to lower power consumption, longer device life due to the ease with which device power
may be dissipated, and more uniform device characteristics.

Our closed cycle cryocooler relies on a pump to achieve the desired temperature. The pump introduces a vibration into the cold finger on which the device under test (DUT) is mounted. We have found that this vibration can lead to broken external bond wires if insufficient attention is paid to layout and assembly of the DUT. Internal bonds in the packaged device appear to be unaffected. The vibration also caused instability in the HTS oscillator circuit.

CONCLUSIONS

A two-pole HTS BPF/LNA hybrid has been fully characterized at 77K and its performance compared to that of a normal metal hybrid. The hybrid showed a 2.1 dB noise figure improvement and a 0.5 dB gain improvement at 77K as compared to the gold filter/LNA hybrid. Repeated cycling over temperature showed no adverse effects on the hybrid or in the performance of the commercial LNA. There was no loss in the hermeticity of the package. Several other LNAs were also tested and similar results obtained.

The power supply to the LNA's was turned on during the entire time the hybrid was being cooled. The resulting power dissipation inside the package undoubtedly raised the temperature inside the package above 77K and prevented the nitrogen gas backfill from condensing. This was seen as a benefit since condensation of the backfill in the package could have caused short circuits. Also, the primary goal of the experiment was to integrate the HTS BPF with a commercial LNA at 77K, any further system level performance improvement due to cooling the LNA is an added benefit.

The results of superconducting oscillators were presented and their performance compared to that of similar circuits fabricated from copper. The oscillator designs were optimized for operation at 77K, rather than designed for room temperature operation and then cooled.

In deep space communications, radio astronomy and radiometer applications, low noise/low loss requirements are usually met by cooling microwave components. Long term system reliability is also critical, since there is usually no option to service the equipment once it is launched. The ability to integrate larger systems in a cryogenic environment is contingent on reliable unattended performance. Our results on the BPF/LNA hybrid and the superconducting oscillator would indicate that reliable operation is possible without radical departures from present design techniques used for space systems.

REFERENCES

9. EEsof, Westlake Village, CA
Figure 1
Possible levels of integration

Figure 2
BPF/LNA combination

Figure 3
Noise figure for BPF/LNA combination

Figure 4
Oscillator layout

Figure 5
Output power vs. temperature

Figure 6
Output frequency vs. temperature
A high-temperature superconductivity (HTSC) flight experiment from the payload bay of the Space Shuttle Orbiter to the Advanced Communications Technology Satellite (ACTS) is being breadboarded. This proposed experiment, a joint project between the Johnson Space Center and the Lewis Research Center, would use a Ka-band (20 GHz) HTSC phased array antenna and front-end electronics (low-noise amplifier) to receive a downlink communications signal from the ACTS. A conventional receiver demodulates the encoded telemetry signal which is then turned around and transmitted back to ACTS and the ground.

The HTSC phased array has nine 4 x 4 microstrip patch antenna subarrays which when properly phased, provide approximately 24 dB of boresight gain. A 2 x 2 HTSC microstrip patch has been built and tested. A Ka-band receiver, transmitter, modem, encoder, decoder, etc., are now being built and tested. Link analyses and interface problems with the Orbiter are addressed in the paper in addition to the design, fabrication, and testing of various subsystems used in the communication link.

1.0 INTRODUCTION

The recent discovery of high temperature superconductors (HTSC) has focused attention towards the search for applications that will enhance the performance of communications systems. With the natural cooling abilities of space under certain conditions, potential space applications are attractive. One application is the use of HTSC materials in microwave and millimeter-wave feed networks for large antenna arrays. This application could enhance the communications system performance primarily by reducing front-end losses, but also allowing the replacement of bulky waveguide feed structures with smaller, high performance planar structures.
This paper describes a proposed HTSC millimeter-wave communications flight experiment between a Shuttle Orbiter in low-earth-orbit and the Advanced Communications Technology Satellite (ACTS) in geosynchronous orbit. The experiment involves a Ka-band, superconducting phased array antenna with the front-end electronics developed by the Lewis Research Center (LeRC) and the receiver, with appropriate interfaces in an Orbiter's payload bay developed by Johnson Space Center personnel. Breadboard hardware for the various experiment is 1996. The advantages of such an experiment include: (1) the first use of a complete HTSC communications system operating in a manned spacecraft environment, (2) an evaluation of the thermal interfaces, cooling rates, and interfaces required for an HTSC system to work in an operational space environment, (3) provide direct distribution of data from the ground to a spacecraft without the additional hops involved in the present communication links through the Whites Sands facility, and (4) the first utilization of the 19.7 GHz forward link from the ACTS to an orbiting spacecraft.

2.0 SYSTEM CONFIGURATION

The ACTS is an experimental, geosynchronous satellite scheduled to be launched in July 1993 with a 4-year expected operational lifetime. This satellite which has been designed and developed by the LeRC, provides spot beams to fixed ground locations within the United States. It also has a 1.1 meter, computer steerable antenna which can communicate with low-earth orbiting (LEO) spacecraft. The system configuration, as shown in Figure 1, has an uplink subsystems are being built and tested. The expected time-frame for the
signal at 29.5 GHz which is transmitted from the Electronic Systems Test Laboratory at JSC or from the LeRC to the ACTS. The signal is received by the 2.2m antenna on the ACTS, routed via a matrix switch to the 1.1m antenna which transmits the signal at 19.7 GHz to the Orbiter. This is a bent-pipe mode within the ACTS with a 900 MHz IF bandwidth. The maximum Doppler shift during the experiment is approximately 500 MHz which exceeds the capability of the ACTS baseband processing mode (demodulation/modulation).

![Figure 1 - ACTS 20/30 GHz Flight Experiment](image)

The experiment program includes development of the space hardware for the Orbiter as well as ground transmitting equipment needed in the ESTL. In addition, the program includes certification testing and documentation required for flight on the Orbiter, integration into the payload bay, and the interfaces with the other Orbiter equipment. Certification testing includes four areas: thermal vacuum, vibration, structural loads, and electromagnetic interference (EMI). The experiment is categorized as a Class C payload (economically reflyable or repeatable) with no Orbiter impacts in the event of an experiment failure.
A detailed block diagram of the spacecraft equipment is given in Figure 2. The HTSC antenna could be a circular polarized phased array with nine subarrays; each subarray has 4 x 4 microstrip patch antennas. This antenna will be discussed in detail later in the paper. The antenna has approximately 25 dB of gain with a 10° half-power beamwidth. Each of the nine subarray feeds a low-noise amplifier (LNA), followed by a monolithic microwave integrated circuit (MMIC) phase shifter. The phase shifters are controlled by a dedicated antenna controller which takes the Orbiter's state vector available from the payload interface panel and calculates the required phase shifter settings to electronically point the beam. Mechanical pointing requirements, as determined by the 3 dB beamwidth of a subarray, is approximately +/- 15° for boresight alignment.

Figure 2 - Electronic Equipment Onboard the Orbiter

2.1 Ground Equipment

The ground terminal at JSC has a 1.2m parabolic antenna which is manually pointed to the ACTS. A baseband signal, 100 Kbps to 300 Kbps with convolutional encoding, is biphase modulated onto uplink carrier. The type of modulation data has not been determined.
2.2 Spacecraft Receiver

The spacecraft receiver requires either a large sweep bandwidth in order to acquire the doppler shifted signal of +/- 500 MHz with a maximum rate of change of .6 KHz/sec., or the ground transmitter must have a preprogrammed ephemeris to compensate for the doppler shift. It will probably be easier and less costly to doppler compensate on the ground. It has also not been decided whether to record the uplink data for post mission evaluation or to turn around the data and transmit back to the ground via the normal Ku-band Tracking Data Relay Satellite System (TDRSS) link or to use the Ka-band return link of the ACTS.

3.0 LINK PERFORMANCE

The circuit margin calculations for the forward link are shown in Table 1. There is a 3 dB polarization loss in the ACTS/Orbiter link due to the linear polarized ACTS antenna and the circular polarized Orbiter antenna. The ACTS is operating in a bent-pipe configuration with a 900 MHz bandwidth; there could be signal suppression in the satellite's limiter and a power sharing loss in the output power amplifier. However, recent test data taken on a prototype ACTS system indicated little or no power sharing losses or signal suppression (private communications). Accordingly, these losses are zero in the calculations. A coding gain of 5 dB for the data is used to provide 2.9 dB of link margin for 300 Kbps of data.

4.0 THERMAL LOADING

Several thermal loading configurations were calculated for payloads located in the Orbiter's payload bay. The general equation for thermal balance is:

\[ Q_{in} = Q_{out} \]

\[ \text{Solar} + \text{Earth} + \text{System Heating} = \text{Radiation to Space} + \text{Radiation to Payload Bayliner} + \text{Conduction to Orbiter Structure} \]

\[ \alpha_s A_n Q_{solar} + \varepsilon_{ir} A_n Q_{earth} + Q_{system} = \sigma \delta A_n (T_{system}^4 - T_{space}^4) + \sigma \delta A_n (T_{system}^4 - T_{liner}^4) + (kA_{cond}/1)(T_{system} - T_{beam}) \]

where

\( \alpha_s = \text{Solar absorptivity} \)

\( A_n = \text{area of node n} \)
Q_{solar} = 429\text{ BTU/ft}^2/\text{hour}
\varepsilon_{ir} = \text{emissivity of infrared (dependent upon surface coating)}
Q_{earth} = 70\text{ BTU/ft}^2/\text{hour}
Q_{system} = \text{heat dissipation in receiver (assumed 0 watts)}
\sigma = \text{Stefan Boltzmann's Constant}
\mathcal{F} = \text{view factor (percent of viewing surface area)}
T_{system} = \text{temperature environment of HTSC component}
T_{liner} = \text{temperature of payload bay liner}
T_{space} = \text{temperature of outer space (0° Kelvin)}
l = \text{length between two nodes for conduction}
T_{beam} = \text{temperature of payload bay beam that the payload is attached to (+50° to 90°F for sun viewing, +15°F for earth viewing, and -50°F for cold space viewing)}
A_{cond} = \text{effective cross-sectional area of conducting beam (perpendicular to payload structure)}
k = \text{thermal conductivity of attachment beam}

The analyses were performed using the Thermal Radiation Analyzer System (TRASYS) model to produce radiation conductors and heating rates for various orbit attitudes; the TRASYS output is used as an input for Systems Improved Numerical Differencing Analyzer (SINDA) model to calculate temperatures for 136 nodes (points) within the Orbiter's payload bay. Three orbital attitudes are shown in Figure 3: (1) bay to space (cold); \beta = 90^\circ \text{ (polar orbit)}, (2) bay to sun (hot); \beta = 90^\circ \text{ (polar orbit)}, and (3) bay to earth (warm); \beta = 0^\circ \text{ (equatorial orbit)}.
For the earth-facing orbit, the temperature of the earth is 0°F with a heating rate of 70 BTU/ft²/hour; for the sun-facing orbit, the heating rate is 429 BTU/ft²/hour; for the cold (space-facing) orbit, the heating rate is 0 BTU/ft²/hour. With an assumed initial temperature of 70°F, the steady-state results as shown in Figure 4 are:

Case 1 Payload bay to cold space  \( T = -95^\circ F \) (203K)
Case 2 Payload bay to sun  \( T = +128^\circ F \)
Case 3 Payload bay facing earth  \( T = +20^\circ F \)
The reason for the relatively high temperature (-95°F) in the payload bay facing cold space is due to the conduction from warmer parts of the Orbiter to the payload bay. The bottom of the Orbiter is still heated by the sun and there is a finite thermal mass within the Orbiter's structure. It is possible to achieve colder payload bay temperatures by flying in polar orbit with the bottom of the Orbiter facing the earth and the nose towards the sun.

Figure 4 - Thermal Conditions in The Orbiter's Payload Bay

A payload bay temperature of -250°F (113° K) could be achieved with even colder temperatures by using thermal isolator between the equipment and the payload bay structure. Regardless, a small cooling refrigerator will probably be necessary for the HTSC equipment.
5.0 SUPERCONDUCTING ANTENNA ARRAY

The use of HTSC materials in antenna designs will increase any antenna's radiation efficiency by reducing the ohmic losses in the structure. This appears as an increase in the gain of the antenna since gain and radiation efficiency are in direct proportion. The use of HTSC materials will have a negligible effect on the shape of the antenna's radiation pattern.

Although the gain of all normal-metal antennas can be increased to some extent via the use of superconductors, millimeter-wave arrays appear to have the greatest potential for practical improvement. For a corporate-fed array with a uniform excitation across its aperture, the gain of the array is

\[ G(\text{dB}) = 10 \log\left(\frac{4\pi A}{\lambda^2}\right) - \alpha L \]  \hspace{1cm} (3)

where \( A \) is the aperture area, \( \lambda \) is the wavelength of operation, \( \alpha \) is the attenuation (dB/unit length), and \( L \) is the length of the transmission line from the array feed point to any radiating element. Figures 5 and 6 show how the length of the feed lines increase with increasing array size and how the feed network losses affect the gain of the array, respectively. As can be seen, if losses can be neglected (\( \alpha = 0 \)), an arbitrarily large gain can be obtained if the physical size of the array is not limited by other constraints. However, as the length of the array side increases linearly, the length of the path from the array feed point to any element increases exponentially. Eventually, any losses in the feed network become large enough to limit the maximum available gain of the structure. These calculations were done at a frequency of 20 GHz, with lossless radiating elements separated by 1/2 \( \lambda \). The loss value of 0.25 dB/in is typical for room-temperature CU/PTFE microstrip or stripline transmission lines at this frequency. Often, waveguide feed networks are used to reduce loss at the expense of physical size.
Figure 5 - Feed Network Complexity Increases Exponentially as Corporate-Fed Array Side Length Increases Linearly

Figure 6 - Array Gain Versus Size as a Function of Feed Line Losses
Researchers at NASA/LeRC have fabricated and tested a 64-element thallium-film superconducting microstrip array operating at 30 GHz [1]. The array is fabricated on a 10 milli-inch lanthanum aluminate substrate and both the radiating elements and the microstrip corporate feed network share the same side of the substrate. At 77 K, the device has shown a 2 dB higher gain than an identical antenna pattern with gold metallization at the same temperature, and 4 dB higher gain than the room temperature gold antenna.

In the antenna described above, both the feed network and the radiating elements were fabricated from HTSC material. It is known that superconducting patch radiators show only a modest increase in efficiency over that of normal-metal designs unless the patches are fabricated on relatively thin or high-dielectric substrates [2]. In fact, microstrip patch antennas are usually fabricated on thick (~ λ₀/20), low dielectric constant (εᵣ < 10), low-loss (tanδ < 0.001) substrates. The substrates that are presently compatible with HTSC films do not meet all these criteria. A design, presently underway at NASA/JSC, that combines a HTSC stripline feed network and normal-metal patch radiators fabricated on a relatively thick, low dielectric constant substrate is shown in Figure 7.

![Figure 7 - Single Aperture-Coupled Patch Antenna and Test Fixture - Cross Section](image-url)
# Table I

**ACTS-to-Orbiter Link Calculations (300 Kbps)**

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
<th>Remarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. ACTS transmit power, dBw</td>
<td>16.3</td>
<td>43 watts</td>
</tr>
<tr>
<td>2. ACTS transmit circuit loss, dB</td>
<td>-3.0</td>
<td>1.1m antenna</td>
</tr>
<tr>
<td>3. ACTS transmit antenna gain, dB</td>
<td>42.0</td>
<td>Sum 1 thru 3</td>
</tr>
<tr>
<td>4. ACTS transmit EIRP, dBw</td>
<td>55.3</td>
<td></td>
</tr>
<tr>
<td>5. ACTS power sharing loss due, dB to 900 MHz bandwidth</td>
<td>0.0</td>
<td></td>
</tr>
<tr>
<td>6. Spaceloss, dB</td>
<td>-210.5</td>
<td>40744Km, 19.7 GHz</td>
</tr>
<tr>
<td>7. Polarization loss, dB</td>
<td>-3.0</td>
<td>Linear to Circular</td>
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<tr>
<td>8. Pointing loss, dB</td>
<td>-.5</td>
<td>Estimate</td>
</tr>
<tr>
<td>9. Orbiter antenna receive, gain, dB</td>
<td>25.0</td>
<td>9 subarrays; 16 microstrip patches/sub-array</td>
</tr>
<tr>
<td>10. Orbiter receive circuit loss, dB</td>
<td>-0.5</td>
<td>HTSC lines to input LNA</td>
</tr>
<tr>
<td>11. Orbiter total receive power, dBw</td>
<td>-134.2</td>
<td>Sum 4 thru 10</td>
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<tr>
<td>12. System noise temperature, dBk</td>
<td>29.6</td>
<td>NF = 5 dB, Ta = 2900K Boltzmann's Constant</td>
</tr>
<tr>
<td>13. Noise spectral density (No) dB/KHz</td>
<td>-228.6</td>
<td></td>
</tr>
<tr>
<td>14. Received C/No, dBHz</td>
<td>64.8</td>
<td>Lines 11 - (12 + 13)</td>
</tr>
<tr>
<td>15. Bit rate bandwidth, dBHz</td>
<td>54.8</td>
<td>300 Kbps</td>
</tr>
<tr>
<td>16. Received S/N, dB</td>
<td>10.0</td>
<td>Lines 14-15</td>
</tr>
<tr>
<td>17. Theoretical required S/N, dB</td>
<td>9.6</td>
<td>1.8-5 BER</td>
</tr>
<tr>
<td>18. Coding gain</td>
<td>5.0</td>
<td>(R = 1/2, K = 7)</td>
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<tr>
<td>19. Implementation loss, dB</td>
<td>-1.5</td>
<td>Estimate</td>
</tr>
<tr>
<td>20. Demodulation loss, dB</td>
<td>-1.0</td>
<td>Estimate</td>
</tr>
<tr>
<td>21. Required S/N, dB</td>
<td>7.1</td>
<td>Lines 17 - (18+19+20)</td>
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<tr>
<td>22. Link circuit margin, dB</td>
<td>2.9</td>
<td>Lines 16-21</td>
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</tbody>
</table>
6.0 REFERENCES


C-BAND SUPERCONDUCTOR/SEMICONDUCTOR HYBRID FIELD-EFFECT TRANSISTOR AMPLIFIER ON A LaAlO₃ SUBSTRATE

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Abstract—A single-stage C-band superconductor/semiconductor hybrid field-effect transistor (FET) amplifier was designed, fabricated, and tested at 77K. The large-area (1 inch x 0.5 inch) high temperature superconducting (HTS) Ti-Ba-Ca-Cu-O (TBCCO) thin film was rf magnetron sputtered onto a Lanthanum Aluminate (LaAlO₃) substrate. The amplifier showed a gain of 5.75 dB and a 3dB bandwidth of 150 MHz centered at 7.915 GHz at 77K. An identical gold amplifier was also tested at 77K for purposes of comparison, it had a gain of 5.46 dB centered at 7.635 GHz with a 3dB bandwidth of 100 MHz.

I. INTRODUCTION

Since the discovery of high temperature superconductors (HTS) in the Thallium-Barium-Calcium-Copper-Oxide (TBCCO) and Yttrium-Barium-Calcium-Copper-Oxide (YBCO) systems [1,2], the idea of using superconductors in combination with semiconductor devices in hybrid microwave integrated circuits became feasible at liquid nitrogen temperatures [3]. Semiconductor devices such as Metal Semiconductor Field-Effect Transistors (MESFET's) and High Electron Mobility Transistors (HEMT's) have been shown to have improved device characteristics at cryogenic temperatures [4]. With the development of High Tc superconducting thin films, and Gallium Arsenide (GaAs) monolithic microwave integrated circuits high performance superconductor/semiconductor hybrid integrated circuits can now be realized. The use of superconductors and semiconductors together in microwave circuits has been demonstrated recently [5]. By combining superconducting material with semiconductor devices in microwave circuits, improved performance can be achieved in terms of decreased conductor losses, reduced noise figure (NF), and increased gain [6]. Also, by operating the amplifier at cryogenic temperatures, natural increase in gain due to increased conductivity in the transistor at low temperatures can be exploited.

The objective of this work is to determine the advantage of using High Tc superconducting thin films in the input and output impedance matching networks of a GaAs FET microstrip amplifier. In deep space communications and radio astronomy where ultra low-noise amplifiers (LNA's) are very important because very weak signals need to be detected, the use of superconducting matching networks could provide for lower insertion loss, resulting in improved performance. The amplifier design, fabrication, and results are presented in the following sections.

II. AMPLIFIER DESIGN AND FABRICATION

A single-stage microstrip amplifier was designed for a gain of 6 dB at a center frequency of 8 GHz and a 3dB bandwidth of 500 MHz. The amplifier circuit was designed using TOUCHSTONE [7] on a Sun Workstation. For the purpose of obtaining an optimized cryogenic design the Scattering Parameters (S-Parameters) of a Toshiba GaAs transistor were measured at 77K. The S-Parameters are shown in Figure 1.

![Fig. 1 S-Parameters of Toshiba GaAs FET at T= 77K](image-url)
The measured S-Parameter data was used to design the input and output single-stub impedance matching networks. A schematic of the design is shown in Figure 2. Input and output 50Ω feed lines are followed by coupled lines which function as dc blocks. Impedance matching was done using transmission lines of different length and width, and open-circuited shunt stubs to avoid the problem of fabricating high quality wide band short circuits. The grounding of the source terminal of the transistor was performed by using a low impedance transmission line terminated in a low impedance tapered line. The end of the tapered line came to the edge of the substrate and silver paint was applied to this edge in order to provide an rf ground path to the test fixture.

The amplifier matching and dc bias networks were fabricated by rf magnetron sputtering a TBCCO film from a single composite powder target of Tl-Ba-Ca-Cu-O to a thickness of 3750Å onto a 20 mil thick LaAlO3 substrate [8]. Gold contact areas for wire bonding purposes were formed through a lift-off process and 2.5μm of silver was thermally evaporated on the opposite side of the substrate which acted as the ground plane. A Toshiba GaAs FET was mounted on the substrate using silver-filled conductive epoxy and cured at 150°C for 1 hour. A feedback network consisting of a chip resistor and chip capacitor was added to the amplifier design in order to ensure stability because the amplifier had a tendency to oscillate. The FET, chip capacitor, and chip resistor were connected to the appropriate microstrip lines with 0.7 mil diameter gold bond wires. The amplifier was mounted in a brass test fixture inside a cryogenic chamber on a cold-head platform. Inside the chamber semi-rigid coaxial lines connected the input and output ports of the amplifier to the outside of the cryogenic chamber. Input and output 3.5mm SMA female connectors provided a coax to microstrip feed line transition. Silver paint was used to ensure electrical contact between the launcher pin and the microstrip line. A photograph of the amplifier in its test fixture is shown in Figure 3. An identical amplifier using gold film for the microstrip lines and ground plane was also fabricated for use as a comparison to the hybrid amplifier.

III. MEASUREMENTS AND RESULTS

An HP8510B Vector Network Analyzer and a model 22C Cryodyne closed-cycle refrigeration system made by CTI-
Cryogenics were used to measure the S-Parameters of the amplifiers at 77K. The amplifier was mounted in the cryogenic chamber and the semi-rigid coaxial lines were connected to the input and output ports respectively. The chamber was evacuated to 50 milli torr and the transistor was biased. The corresponding S-Parameters were measured and recorded. The forward gain of the hybrid and gold amplifiers are shown in Figures 4 and 5 respectively.

A comparison of the results obtained for the hybrid amplifier and the gold amplifier are shown in Table 1. Even though the results of the two circuits are not exactly comparable because of the differences in the impedance of the two materials it can be seen from Table 1 that the hybrid amplifier results were closer to the original design goals. This is because the properties of the superconducting material, such as thickness and resistivity, were taken into account in the design.

IV. CONCLUSIONS

A single-stage TBCCO/GaAs FET amplifier was fabricated and its S-Parameters were measured at 77K. An identical gold film amplifier was also fabricated and characterized at 77K. The hybrid amplifier showed a gain of 5.75 dB at a center frequency of 7.915 GHz while the gold amplifier showed a gain of 5.46 dB at a center frequency of 7.635 GHz. The hybrid amplifier was 1.0 inches long and 0.5 inches wide.

ACKNOWLEDGMENTS

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REFERENCES


Table 1. Comparisons of Results of Hybrid and Gold Amplifiers at 77K

<table>
<thead>
<tr>
<th>Amplifier Type</th>
<th>Gain (dB)</th>
<th>Center Frequency (GHz)</th>
<th>3dB Bandwidth (MHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hybrid, T=77K</td>
<td>5.75</td>
<td>7.915</td>
<td>150</td>
</tr>
<tr>
<td>Gold, T=77K</td>
<td>5.46</td>
<td>7.635</td>
<td>100</td>
</tr>
</tbody>
</table>


10 GHz YBa$_2$Cu$_3$O$_{7-\delta}$ superconducting ring resonators on NdGaO$_3$ substrates

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Abstract. YBa$_2$Cu$_3$O$_{7-\delta}$ thin films were formed on NdGaO$_3$ substrates by laser ablation. Critical temperatures greater than 89 K and critical current densities exceeding 2 x 10$^6$ A cm$^{-2}$ at 77 K were obtained. The microwave performance of films patterned into microstrip ring resonators with gold ground planes was measured. An unloaded quality factor six times larger than that of a gold resonator of identical geometry was achieved. The unloaded quality factor decreased below 70 K for both the superconducting and gold resonators due to increasing dielectric losses in the substrate. The temperature dependence of the loss tangent of NdGaO$_3$ was extracted from the measurements.

1. Introduction

A major area of interest for application of high-temperature superconductors is microwave electronics. The characterization of these materials at microwave frequencies is important for understanding their potential for practical use. Strontium titanate (SrTiO$_3$), a cubic pervoskite, has been used as a substrate for the formation of a thin film of high-temperature superconductor [1] and films on SrTiO$_3$ have among the best DC properties. However, its large dielectric constant and loss tangent make it unsuitable for microwave applications.

Lanthanum aluminate (LaAlO$_3$), which has a similar structure to SrTiO$_3$, has been widely used as the substrate for microwave applications of thin film YBa$_2$Cu$_3$O$_{7-\delta}$ (YBCO). This substrate has a lattice mismatch with YBCO of less than one per cent. LaAlO$_3$ has a loss tangent of less than 10$^{-4}$ at 10 GHz [2] and a dielectric constant of 24.5 [3] below the critical temperature ($T_c$) of YBCO. However, LaAlO$_3$ has a second-order phase transition around 500°C [4]. This causes the substrate to have a high density of twinning and may have a detrimental effect on the microwave performance of the YBCO films.

A search for crystals with similar lattice dimensions reveals that neodymium gallate (NdGaO$_3$) is a promising substrate [4, 5]. NdGaO$_3$ is a perovskite which has about 0.8% lattice mismatch with the YBCO superconductor. Furthermore, the dielectric constant of NdGaO$_3$ is comparable to that of LaAlO$_3$, and this crystal is twin free [6, 7]. The crystal has a second-order phase transition at 950°C which is higher than the typical processing temperature of in situ annealed high-temperature superconductors.

Recently, there have been reports on the growth of epitaxial YBCO films on NdGaO$_3$ [8, 9, 10]. The microwave properties of YBCO superconducting films deposited on NdGaO$_3$ have been measured by other researchers [11]. However, to our knowledge, no measurements on resonators fabricated using the YBCO film on NdGaO$_3$ have been reported at frequencies higher than 5 GHz or as a function of temperature.

In this report, YBCO superconducting thin films were deposited on (001) NdGaO$_3$ and patterned into ring resonators. The advantage of a ring resonator over a linear resonator is that the ring resonator does not have radiation losses from an open end. The reflection coefficients of the resonator were measured as a function of temperature. The unloaded quality factors at 10 GHz were calculated and the effective surface resistance was extracted from the loaded Q-factors. Further, the loss tangent of NdGaO$_3$ was determined as a function of temperature.

2. Sample preparation

A two-inch (5.1 cm) diameter, 20 mils (0.51 mm) thick, (001) NdGaO$_3$ substrate, polished on both sides, was cut into typical sizes of 1 cm x 1 cm and 0.8 cm by 0.4 cm for microwave and DC transport characterization, respectively. YBCO thin films were deposited on to the substrates by laser ablation. Prior to deposition of the films, the substrates were cleaned in acetone and methanol with ultrasonic agitation for 5 minutes each. They were then rinsed in deionized water (DI) for 5 minutes followed by 1 minute in DI:HCl (10:1). Lastly, the substrates were rinsed in DI water for 5 minutes and blown dry with filtered nitrogen.

Ablation was performed with a KrF excimer laser. The 248 nm illumination was focused to a typical spot size of 7 mm x 3 mm on a one inch diameter, 95% dense YBCO target. The energy density at the target was 0.8 J cm\(^{-2}\). The target was rotated at 7 rpm and the laser spot was scanned from the centre to the edge of the target with a period of 65 s. The substrate was mounted with silver paste on a three inch diameter heater located 6 cm away from the target. Depositions were performed with a laser pulse rate of two per second. After the sample was loaded, the vacuum chamber was evacuated to 5 x 10\(^{-7}\) Torr while the substrate was heated to the deposition temperature, which was controlled through a thermocouple embedded in the heater. Oxygen was introduced to the chamber to a pressure of 170 mTorr during deposition. The duration of the depositions was typically one hour. After the deposition, the temperature of the heater was ramped down to 450°C at a rate of 2°C min\(^{-1}\) while the oxygen pressure was increased to 1 atm. The substrates were held at this temperature for 2 hours and then ramped down at a rate of 2°C min\(^{-1}\).

Following the deposition of the films, their resistance was measured as a function of temperature. This measurement was done in a closed cycle cryostat using a four-probe method. One micron diameter gold wires were ultrasonically bonded directly to the surface of the superconductor for these measurements. A constant current of 0.1 mA was passed through the two outer leads while the voltage across the inner two leads was measured.

For measurement of the critical current density (\(J_c\)), the films were patterned into a 10 µm and 5 µm wide, 2.77 mm long meander test structure. Positive photolithography was used to form the structure on the superconductor films using Shipley 1400-31 positive photoresist. The YBCO films were etched in dilute H\(_3\)PO\(_4\) (100:1).

Lift-off photolithography was employed to form metal contacts on the superconductor. Patterns were formed with Shipley AZ1400-37 photoresist. A 15 minute soak in chlorobenzene prior to development was used to form a reentrant photoresist profile for the lift-off. After deposition of 0.7 µm of silver and 0.3 µm of gold, a 15 minute soak in N-methyl-2-pyrrolidone was used to swell the photoresist. The lift-off of the excess metal was completed by soaking the samples in warm acetone for 10 minutes. 1 µm diameter gold wire was bonded to the metal contacts for electrical connections. The resistance versus temperature of the patterned test structure was measured using 1 µA of current. Below the critical temperature (\(T_c\)), the critical current was measured by increasing the amount of the current to the sample until the measured voltage exceeded the 1 µV cm\(^{-1}\) criteria.

YBCO films on 1 cm x 1 cm substrates were patterned into ring resonators by standard photolithographic steps as described above. The geometry of the resonator is shown in figure 1. The dimensions were: width of the microstrip (\(w\)) = 99 µm, gap size

![Figure 1. Layout of the microstrip ring resonator.](image)

![Figure 2. Resistance as a function of temperature of sample F.](image)

From table 1 it can be seen that the critical temperature after patterning is usually slightly higher than that before patterning. This is probably a result of non-uniformity in the film and the location of the measurement. Prior to patterning, the measurements were
Table 1. Deposition temperature and dc properties of YBCO films.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Td (°C)</th>
<th>Tc (K) before</th>
<th>Tc (K) after</th>
<th>t (µm)</th>
<th>Jc × 10^-6 (A cm^-2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>715</td>
<td>87.1</td>
<td>88.3</td>
<td>0.37</td>
<td>1.50</td>
</tr>
<tr>
<td>B</td>
<td>735</td>
<td>87.9</td>
<td>88.5</td>
<td>0.26</td>
<td>0.22</td>
</tr>
<tr>
<td>C</td>
<td>745</td>
<td>88.0</td>
<td>88.1</td>
<td>0.35</td>
<td>2.25</td>
</tr>
<tr>
<td>D</td>
<td>755</td>
<td>87.4</td>
<td>86.6</td>
<td>0.38</td>
<td>0.45</td>
</tr>
<tr>
<td>E</td>
<td>785</td>
<td>-</td>
<td>87.5</td>
<td>0.24</td>
<td>0.44</td>
</tr>
<tr>
<td>F</td>
<td>785</td>
<td>88.6</td>
<td>89.7</td>
<td>0.30</td>
<td>resonator</td>
</tr>
<tr>
<td>G</td>
<td>785</td>
<td>87.8</td>
<td>87.3</td>
<td>0.38</td>
<td>resonator</td>
</tr>
</tbody>
</table>

Performing the wire bonding directly to the films with the contacts located near the edge of the sample to prevent mechanical damage in the centre. The patterned test structures, on the other hand, were located near the centre of the samples suggesting that the quality of the films was higher near the centres than at the edges. Sample D was unintentionally over etched. Its critical temperature showed a decrease after patterning.

If the samples are ranked according to critical temperature after patterning it can be seen that, with the exception of sample B, higher critical current densities correspond to higher critical temperatures. Sample B, which had a relatively high critical temperature, also had the lowest critical current density. Inspection of this sample with an optical microscope revealed a large particle in the 10 µm wide YBCO line used for the critical current density measurement. This probably accounts for the anomalously low Jc.

The scattering parameters of the ring resonators fabricated on samples F and G were measured as a function of temperature. The magnitude of S11 is plotted as a function of frequency for sample G at 79 K in figure 3, showing the resonance at 10.14 GHz. The unloaded quality factor of the resonance was determined from the S11 data using the 3 dB frequencies, resonant frequency, reflection coefficients on and off resonance and phase information to account for the coupling coefficients and coupling losses. The details of the technique are described elsewhere [12-14]. The unloaded quality factors (Q0) were determined as a function of temperature for samples F and G at 10 GHz. At 77 K they had unloaded quality factors of 326 and 876 respectively. Note that although sample F had a higher critical temperature, sample G had better microwave performance. This is probably a result of surface morphology. A rough film will exhibit more loss than a smooth film with otherwise identical properties [15]. The surface of sample F had cloudy spots, which we have correlated with roughness by optical and scanning electron microscopy on other samples.

The unloaded quality factors of samples F and G are plotted as a function of temperature in figure 4. As expected, Q0 increases rapidly as the temperature is decreased below Tc. However, as the temperature is further decreased Q0 reaches a maximum and then decreases. This is particularly apparent in sample G, which had the higher Q0. This phenomenon was observed when the measurement was performed with either increasing or decreasing temperatures. The measurements were repeatable. This is quite different from the expected behaviour, such as observed for YBCO resonators on LaAlO3 substrates, for which Q0 tends to levels off but not decrease at low temperatures. This suggests that the losses in the NdGaO3 substrate increase as the temperature is decreased.

To verify that the decrease in the quality factor is due to the substrate and not due to the properties of YBCO on NdGaO3, the reflection coefficient for a gold resonator on NdGaO3 was also measured from 20 K to room temperature. The results of this measurement are shown in figure 5. The decrease in Q0 at low temperatures was observed here as well. To facilitate comparison with the superconducting resonators, the data for the gold resonator below 90 K are also plotted in figure 4.
values of the resistivity of thin films of gold. For the second technique we used conductor quality factors obtained from measurements on the gold resonator by three techniques. The first two were not successful. For the first technique we calculated the expected conductor quality factor from measured DC values of the resistivity of thin films of gold. For the second technique we used conductor quality factors obtained by scaling values measured at 35 GHz, reported in reference [14], to 10 GHz. The loss tangent of the dielectric was then calculated from the unloaded quality factor of the gold resonator using

\[ \tan \delta = \frac{1}{Q_d} = \frac{1}{Q_{oAu}} - \frac{1}{Q_{cAu}} \] (1)

where \( \tan \delta \) is the loss tangent, \( Q_d \) is the dielectric quality factor and \( Q_0 \) and \( Q_c \) are the unloaded quality factor and conductor quality factor respectively. The loss tangent is actually proportional to \( 1/Q_d \) but the constant of proportionality is very near unity in this case and is assumed to be unity hereafter. Both of these techniques produced values of \( \tan \delta \) that implied greater loss in the dielectric than the total measured loss for samples F and G, that is \( Q_d < Q_0 \), which is inconsistent. This is most probably due to the difficulty in scaling the surface resistance of gold for the frequency changes since the effects of non-idealities such as surface roughness were neglected.

The data shown in figure 4 suggest that near \( T_c \) the losses are dominated by those in the superconductor while at low temperatures the losses in the substrate dominate. We can take advantage of this to help separate the two components of the loss. Young et al have reported \( \tan \delta = 3 \times 10^{-4} \) for \( \text{NdGaO}_3 \) at 77 K [11] and 5 GHz. We have used this value as a starting point in an iterative technique for extracting the temperature dependence of the loss tangent from the unloaded quality factors of sample G and the gold resonator. The technique basically consists of the following steps.

(i) Extrapolate the conductor loss at low temperature from its value at 77 K.
(ii) Estimate the dielectric loss below 70 K, where it is dominant, from the unloaded quality factor and the extrapolated conductor loss.
(iii) Use a curve fit to extrapolate the dielectric loss above 77 K to \( T_c \).
(iv) Use the extrapolated dielectric loss to recalculate the conductor loss between 77 K and \( T_c \) and use a curve fit to refine the estimate of the conductor loss from 0 K to \( T_c \).
(v) Use the refined estimate of conductor loss to redefine the dielectric loss from 0 K to \( T_c \).
(vi) Compare the resulting dielectric loss tangent at 77 K to the reported value of \( 3 \times 10^{-4} \), adjust the initial estimate of conductor loss at 77 K, and repeat the process.

The extrapolation of conductor loss is based on the two-fluid model for losses in superconductors while the extrapolation of dielectric loss is based on a fit to an exponential. A detailed description of the procedure follows. The values reported in the description are for the final iteration of the process.

Using a starting estimate of \( 4.4 \times 10^{-4} \) for the loss tangent \( \left( 3 \times 10^{-4} \right. \) for the first iteration), the conductor quality factor for sample G at 77 K is found to be 1425 through equation (1). The quality factor of the superconducting resonator varies little for temperatures sufficiently below \( T_c \). (77 K is not quite far enough below \( T_c \). This accounts for the difference between the starting estimate of \( 4.4 \times 10^{-4} \) for the final iteration and the value of \( 3 \times 10^{-4} \) with results at the end of the iteration.) Assuming \( Q_{cG} \), the conductor quality factor of sample G, has a value equal to that at 77 K for all lower temperatures allowances determination of a first estimate of the loss tangent of the substrate. It is shown on a semi-logarithmic plot in figure 6. The loss tangent was found to fit quite well

\[ \tan \delta = Ke^{-\gamma T} \] (2)

over this temperature range. \( T \) is the absolute temperature and \( K \) and \( \gamma \) are fitting parameters. The results of the fit were used to extrapolate the loss tangent above 77 K to \( T_c \). The conductor quality factor is changing rapidly above 77 K, where the subtractive approach of equation (1) assuming \( Q_c \) constant would be invalid.

The loss tangents calculated from this fit were then used in equation (1) to extract an estimate of \( Q_{cAu} \) the conductor quality factor of the gold resonator, as a function of temperature. An estimate of the surface resistance of the gold films, \( R_{Au} \), was calculated from \( Q_{cAu} \) through equation (3) [16, 17].

\[ R_{Au} = \frac{4\pi Z_0}{B} \frac{\pi}{4h} \left( \frac{1}{Q_{cAu}} \right) \] (3)

\[ B = 1 - \frac{\pi w_u^2}{4h} \] (4)

\[ C \left( 1 - \frac{1}{\pi w_u} \right) \] (5)

\( Z_0 \) is the characteristic impedance of the resonator. The data were then used to find the value of \( \gamma \) by finding the value of 3 that best fit the data though equation (2).

\[ \tan \delta B = Ke^{-\gamma T} \] (2)
Figure 6. First estimate of the loss tangent of NdGaO₃ from 20 K to 70 K obtained by assuming the conductor quality factor of sample G is constant below 77 K. The circles are the data and the full line is the exponential fit.

\[ D = 2 \left( \pi + \ln \left( \frac{2h}{t} \right) \right) / \pi w' \]  \hspace{1cm} (6)

\[ w' = w + \frac{t}{\pi} \left( \ln \left( \frac{2h}{t} \right) + 1 \right). \]  \hspace{1cm} (7)

\( Z_0 \) is the characteristic impedance of the microstrip, \( \lambda \) is the guided wavelength and \( t \) is the thickness of the gold film.

Using equation (1) with the gold resonator and sample G we can write

\[ \frac{1}{Q_{cG}} = \frac{1}{Q_{cAu}} - \left( \frac{1}{Q_{oAu}} - \frac{1}{Q_{cG}} \right) \]  \hspace{1cm} (8)

Also, for a superconducting microstrip with a gold ground plane we have

\[ \frac{1}{Q_{cG}} = \frac{\lambda}{\pi} \alpha_{cG} = \frac{\lambda}{\pi} B'((C' + D') R_{cG} + C'R_{cAu}) \]  \hspace{1cm} (9)

where \( \alpha_{cG} \) is the conductor loss in sample G, \( R_{cG} \) is the effective surface resistance of the superconductor in sample G and \( B', C' \) and \( D' \) are determined from equations (4) to (7) using the thickness of the superconductor in sample G. Combining equations (3), (8) and (9) yields

\[ R_{cG} = \frac{B (2C + D) - B' C'}{B' (C' + D')} R_{cAu} \]  \hspace{1cm} (10)

\[ \frac{4 \pi Z_0}{B' (C' + D')} \frac{\pi}{\lambda} \left( \frac{1}{Q_{oAu}} - \frac{1}{Q_{cG}} \right) \]

which was used to estimate the effective surface resistance of the superconductor in sample G. The surface resistance calculated here is an effective value since corrections for the actual current distribution in the superconductor are not made [18].

A fit to the effective surface resistance thus determined was performed using the following equation

\[ R_{cG} = R_0 + A (T/T_c)^4 \left( 1 - (T/T_c)^3 \right)^{3/2} \]  \hspace{1cm} (11)

\[ = R_0 + Af(\tau). \]  \hspace{1cm} (11)

The first term, \( R_0 \), is a residual surface resistance, the second term is the surface resistance from the two fluid model [19] and \( \tau = T/T_c \). The fitting parameters were \( R_0 \) and \( A \). The effective surface resistances determined from equation (10) are shown in figure 7. The line shows the result of the fit. The data points shown correspond to temperatures from 70 to 85 K, the region in which the effective surface resistance is rapidly changing and the losses are dominated by the superconductor. The effective surface resistances at lower temperatures were not included to minimize the influence of errors in the estimation of the dielectric losses. The dielectric losses are large at low temperatures, and errors there could dominate the results of the fit. While equation (11) oversimplifies the temperature dependence of the surface resistance near \( T_c \), where the penetration depth and the film thickness are comparable, it does allow an improvement in the extraction of \( \tan \delta \) at low temperatures. The results of this fit are used to include the temperature dependence of \( Q_{cG} \) below 77 K, which was previously assumed constant.

Equation (10) was used to recalculate the surface resistance of gold using \( R_{cG} \) calculated from the fit and the measured values for \( Q_{cAu} \) and \( Q_{cG} \). New values for the conductor quality factor for the gold resonator were then calculated using equation (3). Finally equation (1) was used to determine the loss tangent as a function of temperature. The value at 77 K was compared with \( 3 \times 10^{-4} \) and, if needed, an adjustment to the original estimate of the conductor quality factor of sample G at 77 K was made and another iteration was performed. Figure 8 shows the loss tangent of NdGaO₃ as a function of temperature after the final iteration. The loss tangent is seen to increase by more than a factor of five from 77 K to 22 K.

The effective surface resistance of sample F was calculated using equation (10). The effective surface resistances for both superconducting resonators and the surface resistance of the gold resonator are plotted as a function of temperature in figure 9.
5. Conclusions

YBa$_2$Cu$_3$O$_{7-x}$ thin films were formed on NdGaO$_3$ substrates by laser ablation. The best films had critical temperatures greater than 89 K and critical current densities exceeding $2 \times 10^6$ A cm$^{-2}$ at 77 K. Two films were patterned into microstrip ring resonators with gold ground planes. The better of the two resonators had an unloaded quality factor of 876 at 77 K, which was six times larger than that of a gold resonator of identical geometry. The unloaded quality factor increased to 910 at 70 K but then decreased as the temperature was further lowered. Qualitatively similar temperature dependence was observed for the gold resonator indicating that the losses at low temperature were being dominated by dielectric losses in the substrate.

The temperature dependence of the loss tangent was extracted from the measured quality factors of the gold and superconducting resonators for temperatures from 22 K to 80 K. The method employed to extract the temperature dependence of the loss tangent uses a previously reported value of $3 \times 10^{-4}$ at 77 K [11]. The loss tangent was found to increase from $3 \times 10^{-4}$ at 77 K to $1.7 \times 10^{-3}$ at 22 K. These loss tangents are large compared to those for LaAlO$_3$, particularly at low temperatures, and LaAlO$_3$ is a better substrate than NdGaO$_3$ for microwave applications of high-temperature superconductors.

Acknowledgments

The authors are grateful to Mr Norman Rohrer for his assistance with the microwave measurements. This research was supported by the National Aeronautics and Space Administration under Award No. NCC-3-197.

References

[5] Synoptics, Synthetic Crystal and Optical Products Data sheet
ABSTRACT

Microwave properties of sputtered Ti-Ca-Ba-Cu-O thin films were investigated by designing, fabricating and testing microstrip ring resonators. Ring resonators designed for 12 GHz fundamental resonance frequency, were fabricated and tested. From the unloaded Q values for the resonators, the surface resistance was calculated by separating the conductor losses from the total losses. The penetration depth was obtained from the temperature dependence of resonance frequency, assuming that the shift in resonance frequency is mainly due to the temperature dependence of penetration depth. The effective surface resistance at 12 GHz and 77 K was determined to be between 1.5 and 2.75 mΩ, almost an order lower than Cu at the same temperature and frequency. The effective penetration depth at 0 °K is approximately 7000 Å.

1. INTRODUCTION

Among the high Tc materials, thallium based superconductors are very attractive for electronic applications, as they have shown the highest Tc\(^1\), high Jc\(^2-3\), and the lowest values for microwave surface resistance(Rs)\(^3-4\). The foremost applications of high Tc thin films is

expected to be in the area of 'passive microwave devices' such as resonators, filters and delay lines. High Tc superconductors have a greater impact on passive microwave devices because of their lower surface resistance in thin films of high Tc superconductors, compared to Cu and Au, corresponding to higher Q and improved performance in passive microwave devices. The second advantage is the frequency independent penetration depth as compared to frequency dependent skin depth in normal conductors. This means, dispersion introduced in superconducting components will be negligible upto frequencies as high as 1 THz. Compact delay lines\(^5\), filters\(^6\), and resonators are possible, with lower losses.

This paper addresses the design, fabrication and characterization of Tl\(_2\)Ca\(_1\)Ba\(_2\)Cu\(_2\)O\(_x\) (2122) thin film based microstrip ring resonators.

2. EXPERIMENTAL

A microstrip ring structure resonates if its electrical length is an integral multiple of the guide wavelength. A simple ring resonator device was designed which consisted of a ring structure separated from the feed line by a small coupling gap. The size of the coupling gap determines the coupling between the feed line and the ring resonator. A ring resonator designed for 10 mil thick LaAlO\(_3\) substrates (\(\varepsilon_r = 24.5\)), for a fundamental resonance at 12 GHz is shown in figure 1.

![Fig.1 The ring resonator device designed for 12 GHz resonance](image-url)
In the figure, the linewidth of the ring and the microstrip feed line is \( W = 5.6 \) mils, the coupling gap \( G = 1.75 \) mils, and the mean radius of the ring \( R = (R_1 + R_2)/2 = 77 \) mils. The characteristics impedance of the microstrip is 41 Ohms at 12 GHz. The design of the ring resonator has been described by Chorey et al\(^7\).

TI\text{Ba}\text{Ca}\text{CuO} ring resonators were fabricated by patterning 0.3 \( \mu \)m thin films using AZ 1421 positive photoresist photolithography and wet chemical etching techniques. The fabrication and patterning of Ti\text{Ba}\text{Ca}\text{CuO} thin films is described in detail elsewhere\(^8\). The ring resonators were annealed using our standard annealing procedures\(^8\text{-}\text{9}\). The samples were divided into two groups: one set of samples with 1 \( \mu \)m gold film on the bottom side of the LaAlO\(_3\) substrate for the ground plane formation and the second set with 0.3 \( \mu \)m Ti\text{Ba}\text{Ca}\text{CuO} superconducting thin film ground plane. The ground plane side superconductor was deposited and post-processed using our routine post-deposition methods, after the microstrip ring resonator was fabricated on the top side.

A ring resonator was mounted in a gold plated Copper test fixture of 1" wide, 2" long and 1" thickness. The test fixture was placed on the cold head of the helium gas closed cycle cryogenic system. Connections to the HP 8720 network analyzer were made using a 0.141" semi-rigid co-axial cable of 50 ohms characteristic impedance. Before measurements were performed on ring resonators, standard one port calibration was performed at room temperature.

The resonator quality factor (Q) was obtained from the swept frequency reflection measurements\(^7\text{-}\text{10}\). The unloaded Q is obtained by separating the external losses in the feed line and due to coupling. The loaded Q and the unloaded Q are related through the reflection coefficients at resonance and far from the resonance\(^10\). The determination of whether the resonator was overcoupled or undercoupled was made from the Smith chart and also the phase response of the resonator. Typically, the ring resonators were overcoupled. Measurements for the superconducting
resonator were performed at the fundamental resonance frequency of 12 GHz, and an input power level of -30 dBm.

3. RESULTS

Unloaded $Q$ versus temperature characteristics for an all-superconducting ring resonator is shown in figure 2. The curve A is the data for the high Tc thin film ring resonator with a superconducting ground plane. For comparison, data for the gold resonator is also shown in curve B.

![Figure 2](image_url)

**Fig. 2.** The unloaded $Q$ vs Temperature for an all-superconducting resonator

The unloaded $Q$ of the ring resonator with superconducting ground plane is approximately four times higher than the gold resonator at 65 °K. In addition, the unloaded $Q$ of the superconducting ring resonator shows an increasing trend in $Q$ with decreasing temperature, whereas the superconducting ring resonators with gold ground plane show a saturation of $Q$ at low temperatures due to the dominance of ground plane conductor losses.

The effective surface resistance ($R_s$) of the superconducting thin films, were obtained from ring resonator quality factor ($Q$) measurements. By separating the conductor and dielectric losses, the $R_s$ was calculated using the standard microstrip loss equations described by Pucel et al\textsuperscript{11}. The $R_s$ at 12 GHz, and 77 °K was determined to be typically between 1.5 and 2.75 mΩ, almost an order lower than $R_s$ of Cu at the same temperature and
frequency. The swept frequency reflection measurements performed at several temperatures, is also used in determining the penetration depth of the TlCaBaCuO superconducting thin films. The resonance frequency was measured at each temperature for ring resonators. A typical measured resonance frequency shift with respect to temperature for a superconducting ring resonator with approximately 1 \( \mu \text{m} \) thick gold ground plane is shown in figure 3.

![Graph showing resonance frequency vs temperature](image)

Fig.3. Resonant frequency vs Temperature characteristics for a resonator

The shift in resonance frequency with temperature is mainly due to the temperature dependence of the penetration depth of the superconductor. Thus, the resonance frequency shift is an indirect method of determining the penetration depth. From the figure, the change in resonance frequency below 70 °K is almost negligible. The detailed analysis of this figure to determine the penetration depth of the superconducting thin films, is given in the next section.

4. ANALYSIS AND DISCUSSIONS

The phase velocity of a superconducting microstrip transmission line with a superconducting ground plane is given by\(^{12}\),

\[
v_{ph} = \frac{c}{\sqrt{\varepsilon_{\text{eff}}}} \left\{1 + 2\frac{\lambda}{h} \coth \left(\frac{t}{\lambda}\right)\right\}^{-0.5}
\]

--- \(\text{eq}(1)\)

where \(c\) is the velocity of light, \(\varepsilon_{\text{eff}}\) is the effective dielectric constant, \(h\) is
the substrate thickness, \( t \) is the thickness of the microstrip, \( \lambda \) the penetration depth of the superconducting microstrip. The penetration depth is temperature dependent based on the Gorter-Casimir relationship\(^{13}\) ie.,

\[
\lambda(T) = \lambda(0)*[1-(T/Tc)^4]^{-0.5}
\]

--- > (2)

for temperature \( T \) less than \( T_c \). \( \lambda(0) \) is the penetration depth at \( T = 0 \) °K. The resonance frequency of the ring resonator is given by the equation

\[
f = n*\nu_{ph}/(2*L)
\]

--- > (3)

where \( f \) is in GHz, \( L \) is the mean circumference of the ring in mm, and \( n \) is the integer order of resonance. From the temperature dependence of resonance frequency measurements and the above equations, the best value of \( \lambda(0) \) was determined to be 6890 Å. The typical value ranges between 7000 Å and 8000 Å. Since the thin films are only 0.3-0.4 \( \mu \)m thick, the penetration depth depends upon the properties of the superconductor through the entire film.

A theoretical model based on the Phenomenological loss Equivalence Method (PEM) approximation\(^{14,15}\) was employed to determine the theoretical variation of conductor losses with temperature for the cases of superconducting microstrip/gold ground plane, and superconducting microstrip/superconducting ground plane. Both these cases were compared to the attenuation constant of a gold microstrip on LaAlO\(_3\) substrate.

The attenuation constant for a superconducting microstrip is calculated from the formula\(^{15}\),

\[
a = (T/Tc)^4/[1-(T/Tc)^4]^{3/2} \times \frac{G_1}{4} \times \frac{\sigma_n}{Z} \times w^2 \times \mu^2 \times \lambda(0)^2 \times \coth(X)
\]

\[
+ X \cosec^2(X) \text{ Np/m}
\]

--- > (4)

where \( X = A \times \frac{G_1}{A(0)} \times [1-(T/Tc)^4]^{1/2} \).

\( G_1 \) is the geometric factor given by the equation

\[
G_1 = \frac{1}{(\pi h)^2}[1-(W_e/(4h))^2][1/2 + h/W_e + h/(\pi W_e)\ln(2h/t)]
\]

--- > (5)

\( W_e \) is the effective width of the microstrip, and \( A \) is the area of cross-section of the microstrip, \( T \) is the measurement temperature below \( T_c \), and \( \lambda(0) \) the penetration depth at 0 °K of the superconductor.

The parameters assumed for the calculations are the relative dielectric
constant ($\varepsilon_r$) of LaAlO$_3$ to be 24.5$^7$, the loss tangent (tan $\delta$) of LaAlO$_3$ to be $8.3\times10^{-5}$ below 100 °K$^7$, the substrate thickness (h) of 10 mil, the width of the microstrip (W) of 142 $\mu$m, corresponding to a characteristic impedance of 41 ohms at 12 GHz, the thickness of the superconducting microstrip(t) to be 0.3 $\mu$m, the ground plane thickness of 1 $\mu$m for gold ground plane and 0.3 $\mu$m for superconducting ground plane, the zero resistance Tc of the TICaBaCuO thin films was to be 100 °K, and the normal conductivity at Tc ($\sigma_n$) of $1.5\times10^6$ S/m.

The ground plane conductor losses can be calculated by the same method, using the geometric factor $G_2$ instead of $G_1$ in the equation 4.

$$G_2 = \frac{1}{2\pi h} \times [1-(W_e/4h)^2]$$

Figure 4 shows temperature variation of the attenuation due to conductor losses for a gold microstrip (curve A), a superconducting microstrip with a gold ground plane (curve B), and a superconducting microstrip with a superconducting ground plane (curve C) as determined using equations 4-6.

---

**Fig.4.** Theoretical attenuation loss vs temperature characteristics for superconducting microstrip with gold ground plane (B), and superconducting ground plane (C), compared to a gold microstrip (A).
The diagram in the left is for $\lambda(0)$ of 6000 Å, and the one in the right is for $\lambda(0)$ of 7000 Å. The figures show lower attenuation for the microstrip with superconducting ground plane (curve C) compared to the one with gold ground-plane (curve B), below 77 °K.

The surface resistance of the superconducting thin film can be obtained from the attenuation equation

$$R_s = \frac{2}{Z_0} \frac{\alpha}{G} \quad \text{---> (7)}$$

where $Z_0$ is the characteristic impedance of the microstrip.

The microwave properties of TlCaBaCuO thin films obtained from the ring resonator measurements were used in designing a reflection type hybrid phase shifter circuit based TlCaBaCuO thin film components and GaAs MESFETs. The design of the superconducting microstrips included the effects due to complete field penetration in the films. The phase bits were designed for 90 and 180 degrees phase shift, operating at 4 GHz center frequency, 25% bandwidth and phase error less than 5 degrees. Each phase bit consists of a 3 dB Lange coupler, impedance transforming networks and GaAs MESFET switches. A 180 degrees phase bit circuit was fabricated and tested using gold microstrip. The circuit showed a phase shift of 180.06 degrees at 3.9277 GHz. The insertion loss of the circuit was as low as -2.12 dB in the off state of the switching devices, and -2.523 dB in the on state. The input and output reflection losses were above 10 dB. The results of the superconductor/semiconductor hybrid phase shifters will be published elsewhere.

5. SUMMARY

The microwave properties of TlCaBaCuO thin films were investigated by designing, fabricating and characterizing a microstrip ring resonator. The resonator was designed for a fundamental resonance frequency of 12 GHz, and for fabrication on 10 mil thick LaAlO$_3$ substrates. Ring resonators with gold ground plane of 1 μm thickness and TlCaBaCuO superconducting
ground plane of 0.3 μm thickness were fabricated and characterized at cryogenic temperatures. The unloaded Q for the superconducting resonators were above 1500 at 65 °K, compared to 370 for a gold resonator. The surface resistance of the TlCaBaCuO thin films obtained by separating conductor losses from the Q measurements is typically between 1.5 and 2.75 m-Ohms at 12 GHz and 77 °K, almost an order lower than Cu and Au at the same temperature and frequency. The penetration depth at 0 °K, was calculated from the resonance frequency shift with temperature measurements. The typical values for the penetration depth at 0 °K is approximately between 7000 and 8000 Å.

The conductor losses in the superconducting microstrips with superconducting ground plane were compared to the ones with gold ground plane using a theoretical model called the Phenomenological loss Equivalence Method (PEM). This model predicted lower conductor losses for the microstrip with superconducting ground plane, below 77 °K.

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REFERENCES


Conductor-Breaked Side Resonators

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Member

A new conductor-breaked open microstrip resonator was realized at 9.5 GHz by laser ablation and off-axis sputtering of YBa$_2$Cu$_3$O$_x$ thin films on LaAlO$_3$ substrates. The resonator was fabricated and characterized at 9.5 GHz using network analyzers. The unloaded quality factor ($Q_0$) of the resonator was measured as 470 with a bandwidth of 2%. The resonator was placed in a gold fixture and used in a temperature-controlled environment to study the effect of a conductor-breaked side resonator.
CONDUCTOR-BACKED COPLANAR WAVEGUIDE RESONATORS OF Y-Ba-Cu-O AND Ti-Ba-Ca-Cu-O ON LaAlO₃

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Abstract—Conductor-backed coplanar waveguide (CBCPW) resonators operating at 10.8 GHz have been fabricated from Ti-Ba-Ca-Cu-O (TBCCO) and Y-Ba-Cu-O (YBCO) thin films on LaAlO₃. The resonators consist of a coplanar waveguide (CPW) patterned on the superconducting film side of the LaAlO₃ substrate with a gold ground plane coated on the opposite side. These resonators were tested in the temperature range from 14 to 106 K. At 77 K, the best of our TBCCO and YBCO resonators have an unloaded quality factor (Qₖ) 7 and 4 times, respectively, larger than that of a similar all-gold resonator. In this study, the Qₖ's of the TBCCO resonators were larger than those of their YBCO counterparts throughout the aforementioned temperature range.

I. INTRODUCTION

Since their discovery in 1986, high transition temperature superconducting (HTS) compounds have been employed in the development of passive microwave transmission structures such as resonators, filters, and delay lines [1-3]. Ease of fabrication and performance reliability are two requirements that these HTS compounds should meet in order to be used in microwave circuits. Because of its geometrical attribute of having the ground planes on the same surface as the signal transmission line, coplanar waveguide (CPW) structures are advantageous for HTS-based microwave integrated circuits. When a good conducting layer is deposited on the opposite side of the CPW supporting substrate the structure is known as a conductor-backed coplanar waveguide (CBCPW).

Recently, reports on YBCO-based CPW and CBCPW resonators have been published [4-7]. Until now, a comparative study to determine which type of HTS compound is more appropriate for the optimization of these structures for microwave applications has not been done. In this paper we present our results on the performance of CBCPW resonators fabricated from TBCCO and YBCO thin films on LaAlO₃.

II. EXPERIMENTAL

Figure 1 shows a schematic representation of the CBCPW resonators analyzed in this study. The TBCCO resonators were custom made by Superconductor Technologies Inc. from laser ablated films (~800 nm thick) deposited onto 1.0x1.0x0.05 cm (100) LaAlO₃ substrates. The YBCO resonators were patterned by us on laser ablated (NASA-Lewis) and magnetron sputtered (Conductus Inc.) thin films (~350 nm) on LaAlO₃ substrates of the aforementioned dimensions and crystallographic orientation. The pattern shown in Fig. 1 was transferred to the HTS films using standard photolithography techniques followed by a "back-etching" process using a 1% phosphoric acid (H₃PO₄) solution. The ground plane on the opposite side of the substrate was formed by successive evaporations of a 150 Å thick chromium layer and a ~2.5 μm thick gold layer. A similar all-gold CBCPW resonator, with its CPW layer ~ 1.2 μm thick, was also fabricated for comparison purposes. The testing of the resonators was done by mounting them on a brass test fixture bolted to the cold finger of a closed-cycle-helium-gas refrigerator and enclosed inside a vacuum can with feedthroughs to allow coupling between the resonator and a coaxial waveguide. The coupling between the coaxial line and the resonators was achieved through an SMA launcher. The center pin of the connector was placed in direct contact with the feed line that tapered from 0.559 mm to the width of the center conductor over a length (L1) of 1.000 mm. Coupling to the resonator was achieved across a gap (G1) 0.050 mm wide. The reflection coefficient of the resonators was measured using an HP-8510C network analyzer, and was used
Fig. 1 Top view of the conductor-backed coplanar waveguide resonator (9.230x9.230 mm). P1=0.533 mm, P2=0.559 mm, L1=1.000 mm, L2=7.020 mm, W=0.530 mm, S=0.200 mm, G1=0.050 mm, G2=0.530 mm, and G3=0.630 mm. The relative dielectric constant ($\varepsilon_r$) of the substrate is 22. The crosshatched sections represent the HTS material.

to determine the unloaded quality factor ($Q_u$) of the resonator according to the procedure described in [8]. Before the beginning of each measurement cycle the network analyzer was calibrated with short, open, and load standards.

In order to improve the contact between the launcher and the feed line, silver contacts (~250-300 nm thick) were evaporated onto the end of the feed line and the coplanar ground planes. Immediately after the evaporation the resonators were annealed in flowing oxygen (~1 SLM). The YBCO resonators were annealed at 450°C for 1 hr, and cooled afterwards at a rate of 2°C/min to room temperature. The TBCCO resonators were annealed at 450°C for 10 min, followed by a rapid cooling on a firebrick. The contact resistivity was measured by a three-point probe method, and was found to be $-2.7 \times 10^4$, $9.0 \times 10^4$, and $4.5 \times 10^6 \Omega \text{cm}^2$ for the laser ablated YBCO, the magnetron sputtered YBCO, and the TBCCO films, respectively. The transition temperature ($T_c$) of the resonators measured before and after silver contacts deposition and annealing using a standard four-point probe technique.

### III. RESULTS

Table 1 shows a summary of the results of the characterization of the CBCPW resonators. The $T_c$ values and film thicknesses correspond to measurements performed after patterning and annealing of the films. The $Q_u$'s versus temperature of the resonators analyzed in this work are shown in Fig. 2.

<table>
<thead>
<tr>
<th>Film</th>
<th>Thickness (nm)</th>
<th>$T_c(K)^a$</th>
<th>$Q_u$</th>
<th>$R_e$(m$\Omega$)$^b$</th>
<th>$f$GHz$^c$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Au</td>
<td>1200</td>
<td>84.0</td>
<td>110</td>
<td>24.0</td>
<td>10.803</td>
</tr>
<tr>
<td>1 (YBCO)</td>
<td>310</td>
<td>91.1</td>
<td>412</td>
<td>6.4</td>
<td>10.805</td>
</tr>
<tr>
<td>2 (YBCO)</td>
<td>350</td>
<td>89.9</td>
<td>470</td>
<td>5.6</td>
<td>10.755</td>
</tr>
<tr>
<td>3 (YBCO)</td>
<td>350</td>
<td>103.5</td>
<td>471</td>
<td>5.6</td>
<td>10.742</td>
</tr>
<tr>
<td>4 (TBCCO)</td>
<td>800</td>
<td>103.0</td>
<td>577</td>
<td>4.6</td>
<td>10.750</td>
</tr>
<tr>
<td>5 (TBCCO)</td>
<td>800</td>
<td>104.2</td>
<td>823</td>
<td>3.2</td>
<td>10.680</td>
</tr>
</tbody>
</table>

$^a$ dc transition temperature after patterning and annealing.

$^b$ Unloaded quality factor.

$^c$ Effective surface resistance.

$^d$ Resonance frequency.

These data were found to be independent of applied power within the range of -5.0 to -26.0 dBm. The lowest $Q_u$ observed in this study for any of the HTS resonator corresponded to a laser ablated (LA) YBCO film (sample 1, Tab. 1). This film exhibited a $T_c=84 K$ after annealing, and although Scanning Electron Microscopy (SEM) micrographs showed a smooth surface, some porosity was noticeable on one of the coplanar ground planes which gave it a hazy appearance. A very smooth surface was also observed for YBCO sample 2, also laser ablated, but not for YBCO sample 3 (magnetron sputtered, MS) which exhibits outgrowths on its surface ranging in size from 1-3 $\mu$m. Note that in spite of their different surface morphologies, the $Q_u$'s of these...
two resonators were comparable which shows that surface roughness does not necessarily equate to a poorer microwave performance, at least for YBCO thin films deposited by the two techniques considered here. This is consistent with microwave results obtained by power transmission measurements in the same type of YBCO thin films [9]. The highest Q's amongst the YBCO resonators were exhibited by sample 3. Its Q_e at 77 K was 470 which is ~4.3 times better than that of the gold resonator at the same frequency and temperature. This value is lower than reported Q_e's for YBCO-based CPW resonator at the same temperature and at frequencies close to 10 GHz [6]. The lower Q_e may be due to the effect of adding a back conductor to the CPW structure. However, direct comparison between different resonant structures should be done cautiously due to the differences in their geometrical configuration. X-ray diffraction (XRD) analysis showed that the YBCO films considered here have a crystallographic orientation where the c-axis is predominantly oriented perpendicular to the substrate plane. No evidence of change in the XRD patterns was observed for these films after the annealing process.

The TBCCO resonators shown in Table 1, are representative of two different deposition batches, with samples 4 and 5 originating from the same batch and sample 6 from a separate batch. From Fig. 2 it can be seen that the Q_e's for the TBCCO resonators were larger than those obtained for their YBCO counterparts. For the best TBCCO resonator (sample 6, Fig. 2) a Q_e of 823 was obtained at 77 K. This value is ~7.4 times that of the gold resonator and is ~1.75 times larger than the Q_e of our best YBCO resonator. It was observed that after the annealing the Q_e's of the resonators increased (almost by a factor of 2 for sample 6) with respect to those obtained before the annealing. The enhanced Q_e's can be correlated with an increase in oxygen content in the films as reflected by the rise in T_c, with respect to that measured before the annealing process. For the YBCO films this increase was ~1.0-1.3 K while for the TBCCO films it was ~2.0-3.0 K. Observe that for the YBCO resonators (especially for the two laser ablated ones) the discrepancies in Q_e's are well correlated with their T_c values. However, for the TBCCO resonators, although the difference between their T_c values after the annealing was less than 1.3 K, and the temperature at which a measurable resonance was first observed was almost the same (~105 K), still there was a large discrepancy between their respective Q_e's. This difference can be associated with the morphology of the films. The XRD patterns contain only the (00l) reflections for both the 2212 and the 2223 phases. Based upon the relative peak intensities it appears that the films are similar in composition and composed primarily of the 2212 phase. However, SEM analysis revealed that samples 4 and 5 are characterized by a "terrace-like" surface morphology which is absent in sample 6. As such, we believe that the effective thickness of sample 4 and 5 is less than that of sample 6 and thus is responsible for their lower Q_e's.

The effective surface resistance (R_s) for the YBCO and TBCCO HTS films was determined from the unloaded quality factor [10]. The surface resistance of the all-gold resonator was determined from measurements of the dc resistivity (p) and using the expression R_s=(\mu_0 p/2)\omega, where \mu_0 is the permeability of free space and \omega=2\pi f, where f is the frequency. Values of R_s at 77 K for the HTS-based and all-Au based CBCPW resonators are shown in Tab. 1. Note that the lowest R_s for YBCO is ~0.25 of that for Au, and compares well with those reported by others [6,10] if we assume that the R_s of the superconductor is proportional to the square of the frequency. For TBCCO, our lowest R_s is ~0.13 of that for Au. However, the R_s values obtained in this study for our best TBCCO resonator is ~6 times larger than the value obtained by others from ring resonators fabricated on films from the same source as ours (R_s=6 mΩ at 35 GHz and 77 K; R_s~0.5 mΩ at 10 GHz and 77 K, assuming a R_s=\alpha f) [1]. This may be explained in terms of the current distribution in the conductors of the resonator. In the CPW section of the CBCPW resonator the currents are concentrated near the edges of both the center conductor and the ground planes. Therefore this structure is more sensitive to defects at the edges of the conductors that may arise during the patterning process, resulting in an increase in R_s [11].

IV. CONCLUSIONS

Conductor-backed coplanar waveguide resonators have been patterned on YBCO and TBCCO HTS thin films on LaAlO_3. These resonators were tested in the temperature range from 14 to 106 K. Unloaded quality factors Q_e as high as 823 and 470 were obtained at 77 K and 10.8 GHz for TBCCO and YBCO resonators, respectively. The highest Q_e's at 77 K for the TBCCO and YBCO resonators were nearly a factor of 7 and 4, respectively, better than that of an all-gold resonator of the same geometry at the same temperature and frequency. In this study, the Q_e's of the TBCCO resonators were larger than those of their YBCO counterparts throughout the aforementioned temperature range. Our results support the observation that a high T_c does not always correlate with a good microwave performance. In addition, they suggest that the TBCCO films may be the material of choice for cryogenic microwave applications given the fact that there is still room for improvement of aspects such as the porosity of the films. However, more work is necessary to correlate Q_e with porosity for films having similar T_c's.

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REFERENCES


A 10 GHz Y-Ba-Cu-O/GaAs Hybrid Oscillator Proximity Coupled to a Circular Microstrip Patch Antenna

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Abstract—A 10 GHz hybrid Y-Ba-Cu-O/GaAs microwave oscillator proximity coupled to a circular microstrip antenna has been designed, fabricated and characterized. The oscillator was a reflection mode type using a GaAs MESFET as the active element. The feedline, transmission lines, rf chokes, and bias lines were all fabricated from YBa2Cu3O7−δ superconducting thin films on a 1 cm × 1 cm lanthanum aluminate substrate. The output feedline of the oscillator was wire bonded to a superconducting feedline on a second 1 cm × 1 cm lanthanum aluminate substrate, which was in turn proximity coupled to a circular microstrip patch antenna. Antenna patterns from this active patch antenna and the performance of the oscillator measured at 77 K are reported. The oscillator had a maximum output power of 11.5 dBm at 77 K, which corresponded to an efficiency of 10%. In addition, the efficiency of the microstrip patch antenna together with its high temperature superconducting feedline was measured from 85 K to 30 K and was found to be 71% at 77 K, increasing to a maximum of 87.4% at 30 K.

I. INTRODUCTION

The application of high temperature superconducting (HTS) thin films to microwave circuits is advantageous since the films have a lower surface resistance than gold or copper at microwave frequencies. Passive circuits such as ring resonators [1], [2], filters [3], transmission lines [4], and antennas [5] fabricated from HTS films have shown substantial improvements in performance over identical circuits fabricated with normal metals. Several authors have suggested that HTS technology may be very beneficial in phase-array antenna systems [6], [7]. To date, a limited amount of work in the area of passive microstrip antennas has been reported [5]. However, for HTS to be useful in phased array antennas, active circuits such as oscillators, phase shifters and power amplifiers, will need to be integrated with radiating elements so that beam control and/or scanning may be realized. Because of the limited amount of available space in high frequency arrays, some authors have suggested the use of an active patch antenna as the radiating element. By using active patch antennas, the problem of rf distribution to each radiating element is minimized and space is made available for phase shifters and power amplifiers.

In this paper, we report a first demonstration of an HTS/GaAs hybrid active patch antenna consisting of a hybrid oscillator on one substrate, and a feedline proximity coupled to a circular microstrip patch antenna on a second substrate. The patch antenna was printed on aluminas (εr = 9.9) to reduce the effective permittivity seen by the radiator. The performance of this active antenna was measured at 77 K.

II. DESIGN

Since our objective was to implement the entire oscillator on a single substrate to be cooled to 77 K, the S-parameters of the transistors were first obtained by measurements at cryogenic temperatures for use in the design of the oscillator. The active device used in the oscillator was a low noise MESFET with a gate length of 0.25 μm (Toshiba GaAs MESFET, part no. JS8830-AS). The S-parameters of the FET for the frequency range of 2 GHz to 26 GHz were measured over a range from room temperature (300 K) to 40 K. The magnitude and angle of the S-parameters at 10 GHz as a function of temperature are shown in Fig. 1. The S-parameters as a function of frequency at 300 and 77 K will be presented elsewhere [8]. Of the S-parameters, the largest change in magnitude as a function of temperature occurred for the S21 values. This was due to an increase in the electron's mobility at the reduced temperatures. The variation in phase of S11 and S22 was the only other major change. The percent change of the magnitude and phase of the S-parameters at the design frequency of 10 GHz due to the change in the temperature from 300 K to 77 K is listed in Table I.

The oscillator was designed using simulations performed with a commercially available software package (Touchstone) under the assumption that the drain current would be held at Ii = 10 mA, and that the temperature would be held at 77 K. The design used a parallel coupled ring resonator in the matching network off the drain for the frequency stabilization. Using the small signal S-parameters that were measured at 77 K, the input reflection coefficient at the drain was made very large by

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Fig. 1. Magnitude and angle of the $S$-parameters of the GaAsFET at 10 GHz as a function of temperature. The magnitude of $S_{12}$ has been magnified by a factor of 10 for clarity.

Figure 1.

TABLE I

PERCENT CHANGE OF THE $S$-PARAMETERS FROM 300 K TO 77 K AT 10 GHz

<table>
<thead>
<tr>
<th></th>
<th>$S_{11}$</th>
<th>$S_{12}$</th>
<th>$S_{13}$</th>
<th>$S_{22}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Magnitude</td>
<td>Phase</td>
<td>Magnitude</td>
<td>Phase</td>
<td>Magnitude</td>
</tr>
<tr>
<td>3.4%</td>
<td>16.2%</td>
<td>25.6%</td>
<td>8.4%</td>
<td>4.8%</td>
</tr>
</tbody>
</table>

varying the length of the transmission lines on the source and the gate. The selected lengths of the transmission lines from the source and gate were 1.57 mm and 2.79 mm, respectively. Both were open-circuited lines. The ring resonator, with a fundamental resonant frequency of 10 GHz, which was used to select the frequency of operation was placed at a distance from the drain of the transistor, parallel coupled to the output transmission line using a 40-µm wide coupling gap. The matching network, including the ring resonator, was designed such that the magnitude of the real part of the impedance of the matching network was less than the magnitude of the real part of the impedance looking into the drain of the FET. The magnitude of the imaginary part of the impedance was equal to zero at the resonant frequency. With this criterion met, the 10-GHz oscillation will start upon proper biasing of the FET. The output of the oscillator was taken off the drain. The physical layout of this reflection mode oscillator is shown in Fig. 2.

The antenna used for this investigation was a circular microstrip patch which was proximity coupled to a microstrip feedline. The feedline for the antenna was patterned on a second substrate for two reasons: this method allowed for the testing of both the oscillator and the antenna separately to determine their performance, and secondly, a HTS thin film with an area large enough to pattern the entire circuit was available.

The resonant frequency of the circular antenna patch was found from the formula [9]:

$$f = \frac{1.841 c}{2 \pi a_e \sqrt{\varepsilon_{eq}}}$$

where $a_e$ is the effective radius of the patch

$$a_e = a \left[ 1 + \frac{2d}{\pi a e_{eq}} \left( \ln \frac{a}{2d} + \left( 1.41 \varepsilon_{eq} + 1.77 \right) e_{eq} \right) \right]^{1/2}$$

Here, $d$ is sum of the thickness of the two substrates between the patch and the ground plane and $a$ is the physical radius of the patch. Because the patch was printed on an alumina ($\varepsilon_1 = 9.9$) substrate with a thickness of 254 µm while the feedline and ground plane were on lanthanum aluminate ($\varepsilon_2 = 23$) with a thickness of 508 µm, the value for the net $\varepsilon_{eq}$ of this dual layer substrate to use in (1) and (2) was found using a static capacitor model

$$\varepsilon_{eq} = \frac{3 \varepsilon_1 \varepsilon_2}{2 \varepsilon_1 + \varepsilon_2}$$

to be 16.0, resulting in the diameter of the patch equaling 4.02 mm. Measurements showed that a slightly larger diameter of 4.71 mm resulted in a resonance closer to the desired frequency of 10 GHz. The resonant frequency of the patch was tuned to match the output frequency of the oscillator by adjusting the position of the patch over the feedline.

III. EXPERIMENTAL DETAILS

An HTS film was patterned into the oscillator using standard positive photolithographic techniques and etched with an aqueous solution of deionized water: $H_2PO_4 :: 100 : 1$. This film was a commercially purchased film deposited using an off-axis sputtering technique and had a critical temperature of 88.6 K after patterning. Contacts to the superconductor for the rf output and wire bonding pads were made of silver with a gold overlayer patterned by lift-off photolithography. Wire bonding pads were located at the bias pads as well as at the ends of the transmission lines near the FET. The GaAs FET was epoxied onto the substrate and wire bonds were made to
the transmission lines with 0.7 mil gold wire by ther-
mosonic bonding. A copper ground plane with a thickness
of 2.4 \( \mu \text{m} \) was deposited on the backside of the substrate.

A second HTS thin film was used for the antenna
feedline. A YBa_2Cu_3O_7-x thin film was deposited by
pulsed laser deposition onto this substrate [10]. The film
had a critical temperature of 86 K. This film was pat-
terned in the same way as the oscillator into a 50 ohm
transmission line that was 160 \( \mu \text{m} \) wide and 5 mm in
length. A silver/gold contact was deposited at the end of
the feedline for ribbon bonding, and a 2-\( \mu \text{m} \) copper
ground plane was evaporated on the backside of the
substrate. An alumina substrate with the patt:ned an-
tenna patch was placed on top of the feedline and held in
place with small amounts of fingernail polish at the edges.

The performance of the oscillator was measured on a
spectrum analyzer at 77 K by mounting the circuit in a
sealed brass test fixture and submerging the fixture in
liquid nitrogen. Details of the procedures used for mea-
surement will be presented elsewhere [8]. The antenna
with its HTS feedline was measured by placing the circuit
on a copper test fixture and mounting the fixture on the
second stage of a closed cycle gas refrigerator. A high
density polyethylene radome served as a vacuum chamber.
Details of the experimental apparatus and procedures
have been presented earlier [5].

The efficiency of the antenna together with its HTS
feedline was measured using the Wheeler Cap method
[11]. To do this, the input impedance of the antenna at
resonance was measured with and without a radiation
shield from 30 K up to 85 K. The efficiency (\( \eta \)) was then
calculated as:

\[
\eta = 1 - \frac{R_w}{R_{wo}}
\]

where \( R_w \) and \( R_{wo} \) are the input resistances with and
without the radiation shield, respectively. For this work,
an aluminum cap with an inner dimension of 12-mm
wide \( \times \) 12-mm deep by 6.8 mm high was used as the
radiation shield. Electrical contact to the test fixture was
ensured with silver paint.

The oscillator and antenna circuits were then mounted
with silver paint onto a brass test fixture. The rf connec-
tion between the two substrates was made by ribbon
bonding to the contacts on the feedline of antenna and
the output of the oscillator (Fig. 3). The test fixture was
then mounted in the closed-cycle gas refrigerator and
covered with the high density polyethylene radome. An
X-band horn attached to a pivoting arm served as the
receive antenna to measure the radiation pattern of the
active patch antenna in the far field as a function of angle.

IV. RESULTS AND DISCUSSION

The output power and frequency of operation of the
hybrid oscillator were measured to verify its performance
before bonding the oscillator to the antenna circuit. The
maximum power attainable from the oscillator at 77 K
was 11.5 dBm at a bias of \( V_{ds} = 4.0 \text{ V} \) and \( V_{gs} = 0.0 \text{ V} \).

The sensitivity of the frequency to temperature was
\( -10 \text{ MHz/K} \) at 77 K. Detailed results of the measurements
performed on this oscillator as a function of temperature
and bias will be presented elsewhere [8]. For the active
antenna measurements at 77 K, the FET was biased at
\( V_{ds} = 0.5 \text{ V} \) and \( V_{gs} = -0.5 \text{ V} \) which gave a current of
\( I_d = 12 \text{ mA} \). For this bias condition, the frequency of the
signal was 10.082 GHz with an output power of \(-2.0 \text{ dBm}\).
The efficiency of the oscillator was 10.5%. The
power of the second harmonic at 20.16 GHz was 35 dB
less than the fundamental signal at 77 K.

The efficiency of the antenna was measured before
bonding the antenna to the oscillator circuit. The effi-
ciency as a function of temperature is shown in Fig. 4. As
expected, the efficiency rises dramatically as the HTS film
becomes superconducting and then increases slowly as the
temperature decreases, due to the increase in the conduc-
tivity of the HTS feedline. This trend was in agreement
with the measured performance of HTS ring resonators.
The efficiency reaches a maximum of 87.4% at 30 K.

The measured antenna patterns with the superconduct-
ing oscillator driving the antenna are shown in Fig. 5,
along with the patterns predicted for the co-polarization
by the cavity model [12]. The H-plane shows good agree-
ment with the model, while the E-plane deviates substan-
tially due to surface waves and the feedline, neither of
which are accounted for in the model used. This is in
agreement with results published by Schaubert et al. [13]
which demonstrated that antennas on high permittivity
substrates are characterized by perturbations in the E-
plane pattern. The 12 dB dip in the E-plane and the cross
polarization patterns at an angle of 15 degrees was almost
certainly due to radiation interference from the resonator
and microstrip lines on the oscillator.

V. CONCLUSION

The performance of a 10 GHz active antenna employ-
ing a Y-Ba-Cu-O superconducting feedline and resonator
stabilized oscillator has been demonstrated for the first
time. The patch antenna and the hybrid oscillator were
fabricated on separate LaAlO_x substrates. The measure-
ments on the antenna showed that it was 71% efficient
at 77 K and 87.4% efficient at 30 K. The oscillator had a
maximum power of 11.5 dBm and was 10.5% efficient at
Fig. 4. Efficiency of the patch antenna as a function of temperature measured from 30 K to 85 K. The efficiency at 77 K was 71%.

Fig. 5. Radiation patterns for the patch antenna at 77 K. a) H-plane radiation patterns comparing the cavity model (solid line) with the co-polarization data (open circles) and also displaying the cross-polarization data (open squares). b) E-plane radiation patterns comparing the cavity model with the co-polarization data and also displaying the cross-polarization data.

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PERFORMANCE OF TiCaBaCuO 30 GHz 64 ELEMENT ANTENNA ARRAY

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Abstract—A 64 element, 30 GHz, microstrip antenna array with corporate feed network was designed and built on a .254 mm (10 mil) thick lanthanum aluminate substrate. One antenna pattern was fabricated from gold film, and a second pattern used TiCaBaCuO high temperature superconductor. Both antennas used gold ground planes deposited on the reverse side of the substrate. Gain and radiation patterns were measured for both antennas at room temperature and at cryogenic temperatures. Observations agree well with simple models for loss and microwave beam width, with a gain on boresight of 20.3 dB and beam width of 15 degrees for the superconducting antenna.

I. INTRODUCTION

When microstrip antenna design [1] is extended to microwave frequencies above 30 GHz, certain difficulties become apparent. Losses due to surface waves [2] and radiation [3] become more significant than at lower frequencies. Both of these losses may be reduced by decreasing the thickness of the substrate, drawing the ground plane closer to the microstrip traces. However, the trace widths must also be reduced in order to maintain a given transmission line impedance. The narrower lines have high resistive losses when conventional metals are used to form the traces. For copper traces on a .152 mm (6 mil) thick sapphire substrate, for example, a 30 GHz phased array with 40 dB directivity will have more than 25 dB of loss [4]. In order to reduce these resistive losses, high temperature superconducting (HTS) materials may be used to form the feed networks for high gain phased array antennas [5]. When a high quality HTS film on .254 mm (10 mil) lanthanum aluminate (LAO) is used instead of copper for a 30 GHz antenna of 40 dB directivity, the loss is only 3 dB [4]. This paper describes the design, construction, and performance of the first 30 GHz, 64 element phased array antenna that uses an HTS feed network. The successful implementation of HTS circuits with this relatively low gain antenna supports the position that high gain millimeter wave antennas would benefit from use of the new superconductors.

II. ANTENNA DESIGN

A. General Design

For ease in fabrication, and in order to compare HTS performance with copper performance, we selected an array design with 64 rectangular patches arranged in an 8 x 8 square pattern (Fig. 1). Element spacing was 4500 μm, which is slightly less than one-half of the free space wavelength. This reduced spacing allowed us to place the entire array on a 50.8 mm (2 inch) diameter wafer of LAO, without appreciably changing the radiation pattern of the antenna. Wafer thickness was chosen to be .254 mm (10 mils), with a gold ground plane on the reverse side. The corporate feed network uses 50 ohm lines, which are split to the patch elements by means of six levels of quarter wave microstrip transformers. The relative dielectric constant of LAO is approximately 24 [6], which results in a microstrip line width of 92 μm for this geometry.

Fig. 1 Layout of patch elements and feed network for the 30 GHz phased array antenna. Wafer diameter is 50.8 mm (2 inches).

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Because of the uncertainty in material properties and the application of microwave design rules for substrates with high dielectric constant, we designed, fabricated, and tested single patches at 15 GHz first, in order to determine the validity of our models for devices on LAO at MMW frequencies. We then extended the design to 30 GHz patches, which were then used in arrays. The patches are rectangular, with width \( W \) and length \( L \) (Fig. 2). A microstrip line feeds directly to a notched input of depth \( d \). The calculation of the patch resonance frequency is not difficult, but an accurate calculation of patch impedance is nontrivial. We use a Mixed Potential Integral Equation (MPIE) approach [7]. This is one of several 'full wave' models, which should give good values for patch impedance, surface wave components, and radiation patterns. The patch impedance is needed in order to couple the microwave power efficiently into the patch. The antenna efficiency is determined in part by the resistive losses of the patch, and also by the energy lost to surface waves.

The edge impedance of a rectangular patch on LAO is very high, requiring the use of the notch, which allows coupling near the center of the patch, where the impedance goes to zero. We select a point where the impedance is 100 ohms, and use a quarter wave transformer to match the 50 ohm input line to this point. Typical values are \( W=3000 \mu m \), \( L=2000 \mu m \), and \( d=782 \mu m \) for a resonance frequency of 14.84 GHz, and theoretical input impedance of 78 ohms. The measured impedance in this case was 72 ohms. For the 64 element array, we used patches with \( W=1350 \mu m \), \( L=900 \mu m \), and \( d=337 \mu m \). These elements have a predicted resonance frequency of 31.25 GHz, and input impedance of 100 ohms.

The high dielectric constant of LAO means that even a .254 mm (10 mil) substrate is electrically thick. While the cutoff frequency for propagation of the TE\(_2\) surface wave mode is about 60 GHz, the TM\(_0\) mode is supported at all frequencies. This can be a source of energy loss. We have calculated the radiation efficiency of a single patch, using an electric surface current model [8] to estimate the surface wave losses. At 15 GHz, the single patch efficiency is about 84 percent. At 30 GHz, the efficiency drops to about 60 percent.

In theory, the efficiency of an array can be improved considerably over this value by carefully placing the radiating elements at the correct distance apart, so that the surface wave components destructively interfere. The spacing can also be chosen so that the spatial part of the radiation constructively interferes. Both are possible at the same time because the wavelength of the surface waves is nearly one fifth of the free space wavelength. In practice, however, the presence of the feed network makes it difficult to predict the exact propagation constants in the structure, so that surface waves can be suppressed.

### III. FABRICATION

The preliminary single patches at 15 GHz and 30 GHz were fabricated at Ball using 4 \( \mu m \) thick gold on .254 mm (10 mil) thick LAO, with a titanium adhesion layer. Both plate up and etch down processes were used. Gold ground planes were deposited on the reverse side of the LAO. The diced patches were soldered with indium to gold plated metal carriers made of Alloy 48, which matches the coefficient of thermal expansion of the LAO. The carriers were then mounted in a test fixture, using gold ribbon bonds to microstrip launchers, which in turn were bonded to 'V-type' microwave connectors.

The 64 element array was patterned by Superconductor Technologies, Inc. on a 50.8 mm (2 inch) diameter, .254 mm (10 mil) thick LAO. One array was formed with 3 \( \mu m \) thick gold film, using a titanium-tungsten adhesion layer, and a second array was formed with \( Tl_2CaBa_2Cu_2O_8 \) high temperature superconductor. Both arrays used a gold ground plane deposited on the reverse side of the LAO. The 50 ohm microstrip feed line, as shown in Fig. 1, passes to the edge of the wafer, where a gold ribbon bond is made to a microstrip launcher. In the case of the HTS array, a gold contact strip is deposited over the superconductor near the end of the wafer, for bonding purposes. As with the single patches, the wafer is soldered to a gold plated fixture using an indium alloy. On both the gold and the HTS arrays, line widths were held to a tolerance of about 3 \( \mu m \). Substrate thickness variations were less than .025 mm (1 mil).
The resonance frequency of both the gold and the HTS arrays was measured at Ball, at both room temperature and liquid nitrogen temperatures. The gold array was resonant at 30.7 GHz (room temperature) and 31.1 GHz (77 K). The HTS array was resonant at 30.55 GHz (77 K). A calibrated gain measurement of the gold array was made at Ball, at room temperature. The measured gain, on resonance and on boresight was 15.6 dBi (H-plane). The 3 dB beam width was 13 degrees. The relative gain of the gold and HTS antennas at cryogenic temperatures was then measured at NASA Lewis Research Center. We express the normalized gain, $G$, of an antenna in terms of the usual S-parameters:

$$G = \frac{|S_{21}|^2}{1 - |S_{11}|^2}$$

(1)

Then the efficiency of the HTS antenna relative to the gold antenna is just

$$e_{HTS-Au} = \frac{G_{HTS}}{G_{Au}}$$

(2)

Fig. 3 gives the efficiency of the HTS antenna relative to the gold antenna at 300 K and also relative to the gold antenna at the same temperature as the HTS antenna. At 77 K, the HTS antenna is 4.7 dB higher gain than the gold antenna at room temperature. We therefore conclude, using the calibrated gain measurements of the gold antenna, that the gain of the HTS antenna at 77 K is 20.3 dBi. This is to be compared with the maximum possible gain (no losses) of 22.2 dBi. The inferred loss of 1.9 dB can easily be attributed to losses in the microwave connectors, gold ground plane, and surface waves. Indeed, the predicted maximum loss due to surface waves alone is 2.2 dB. Using a simple model of resistive losses in the feed network, we expect the gold antenna losses at 300 K to be 3.8 dB, and 2.2 dB at 77 K. Similarly, we expect the HTS losses to be 0.4 dB at 77 K. The measured gains are in reasonable agreement with these estimates.

Fig. 4 and Fig. 5 give the E-plane and H-plane radiation pattern measurements for the HTS antenna at 77 K. These two measurements are in excellent agreement with the predicted patterns, showing the first side lobes at -13 dBc, with good symmetry. The slight skewing of the central lobe may be attributed to asymmetry in the measurement fixture.
V. SUMMARY

The measured performance of a 30 GHz, 64 element phased array antenna with a superconducting feed network agrees well with theory. The antenna loss is only 1.9 dB, and the radiation patterns behave as predicted. These results support the contention that significant gain improvements are possible in a high gain millimeter wave antenna that uses an HTS feed network.

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Microwave properties and characterization of co-evaporated BSCCO thin films

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Abstract. An extensive characterization of Bi—Sr—Ca—Cu—O (BSCCO) thin films deposited by co-evaporation on LaA103 and SrTiO3 substrates has been performed. The films had a $T_c$($R = 0$) of ~78 K, and were predominantly c-axis oriented, with critical current densities ($J_c$) at 4.5 K of $1.6 \times 10^6$ and $1.1 \times 10^6$ A cm$^{-2}$, for the samples on SrTiO3 and LaAlO3 respectively. The microwave properties of the films were examined by three techniques. The complex conductivity ($\sigma^* = \sigma_1 - j\sigma_2$) and the magnetic penetration depth ($\lambda$) were measured by power transmission at 30.6 GHz; the surface resistance ($R_s$) was measured using a cavity resonator at 58.9 GHz, and the transmission line losses were determined by measuring the quality factor ($Q$) of a linear microstrip resonator at 10.4 and 20.2 GHz. The complex conductivity for the film on LaA103 was determined to be $(2.0 - j1.0) \times 10^5$ S m$^{-1}$ at 77 K. It was observed that in the superconducting state $\sigma_1$ deviates from both the Bardeen–Cooper–Schrieffer (BCS) theory and the two-fluid model. Values of $\lambda$ were found to be ~2.0 and 1.1 µm at 77 K and 20 K respectively, and were obtained for the film on LaA103. The value of $\lambda$ at 20 K was approximately three times larger than that of BSCCO single crystals. $R_s$ values of 865 and 1391 mΩ were obtained for the films on SrTiO3 and LaAlO3, respectively, at 77 K and 58.9 GHz. Unloaded $Q$ factors at 20 K of ~1100 and 800 at 10.4 and 20.2 GHz respectively, were measured for the BSCCO resonator. Unloaded $Q$ values of 290 and 405 at 20 K were obtained at 10.4 GHz and 20.2 GHz respectively, for an all gold (Au) resonator.

1. Introduction

High transition temperature superconductors (HTS) have potential for microwave applications due to their low loss and dispersion as compared with typically used conductors such as copper (Cu) and gold (Au). Therefore, it is not surprising that to date a large number of measurements at microwave frequencies on HTS properties such as surface resistance ($R_s$), complex conductivity ($\sigma^* = \sigma_1 - j\sigma_2$), and magnetic penetration depth ($\lambda$), have been reported. Most of the work so far has been performed on the YBa$_2$Cu$_3$O$_{7-δ}$ (YBCO) compound [1–7], mainly because of its single phase and simplicity of fabrication. However, studies of the Bi–Sr–Ca–Cu–O (BSCCO) compound have been performed by several research groups since this material offers the advantage of being relatively insensitive to exposure to atmosphere and handling, and because of its great stability with respect to thermal cycling [8]. In spite of the number of studies on BSCCO thin films, data on $R_s$ and $\sigma^*$ at microwave frequencies are still scarce [9, 10].

In this paper we report on the structural, DC and microwave properties of two BSCCO thin films deposited by co-evaporation on LaA103 and SrTiO3 substrates. The films were characterized by scanning electron microscopy (SEM), x-ray diffraction (XRD) analysis, by DC transition temperature ($T_c$) and critical current density ($J_c$) measurements. The microwave properties of the films were determined from $R_s$ measurements using resonant cavity techniques, and power transmission measurements. The $R_s$ of the film on LaA103 was also measured using a linear resonator.
method, since knowledge of the microwave signal propagation along transmission lines is of interest for practical microwave applications.

2. Structure and dc properties

Our measurements were made on BSCCO superconducting films approximately 3000 Å thick deposited by co-evaporation on to (100) LaAlO$_3$ and (100) SrTiO$_3$ substrates 0.010 in thick. The details of the BSCCO film preparation can be found elsewhere [11]. The $T_c(R = 0)$ of the films was determined using standard four-point-probe measurement techniques. $T_c$ values of 78.2 and 78.0 K were measured for the films on SrTiO$_3$ and LaAlO$_3$ respectively (figure 1). Both films have a transition width ($\Delta T$) of $\sim$10 K, which is consistent with previously reported resistivity data for BSCCO thin films [12]. The zero temperature intercept ($R_s$) is lower for the film on SrTiO$_3$, and suggests a higher degree of c-axis texturing, where the c axis is perpendicular to the substrate plane.

Figure 2 shows SEM micrographs of the films under study. The observed surface roughness is typical of films grown by high temperature ex-situ anneal. However, surface roughness alone has not been shown to be detrimental to microwave properties of HTs thin films [7, 13]. Note that the background structure shows the plate-like structure typical of the BSCCO system. The typical grain size for these films was between 2 and 10 μm. XRD analysis of these films showed that they were predominantly oriented with the c axis perpendicular to the film plane, although unknown peaks were observed in both samples, as shown in figure 3. The c-axis lattice parameter agrees within 1 per cent of that corresponding to single crystals [14].

Magnetization hysteresis measurements were performed using a Quantum Design Magnetic Property Measurement System (MPMS). For these measurements, rectangular samples were cut from the films on SrTiO$_3$ and LaAlO$_3$, and the samples were oriented with the a-b plane normal to the magnetic field (H). Figure 4 shows magnetization hysteresis loops for both films.
Using Bean's model [15], and assuming a circular current path, we obtained $J_c$ values at 4.5 K of $1.6 \times 10^6$ and $1.1 \times 10^6$ A cm$^{-2}$ for the films on SrTiO$_3$ and LaAlO$_3$ respectively. $J_c$ values for both films are listed in Table 1 as a function of temperature. Note that for all temperatures the $J_c$ obtained for the film on SrTiO$_3$ is larger than that for the film on LaAlO$_3$, which may be a result of better epitaxy on the SrTiO$_3$ substrate. In addition, the $J_c$ values for both films at 40 K agree well with the $J_c \sim 1.5 \times 10^5$ A cm$^{-2}$ reported at 40 K for laser-ablated BSCCO thin films (~3000 Å) on MgO [12].

### 3. Characterization of BSCCO films at microwave frequencies

#### 3.1. Power transmission measurements

Power transmission measurements were performed on the samples at frequencies from 26.5 to 40.0 GHz (Ka-band), and at temperatures from 300 to 20 K. The details of the experimental configuration and measurement procedures have been previously reported [7]. The main components of the experimental apparatus are an HP-8510B network analyser and a closed-cycle helium gas refrigerator, both controlled by an HP 900-216 computer. The network analyser is coupled to the refrigerator by Ka-band rectangular waveguides. The measurement technique compares the transmitted signal with the incident microwave signal to determine the power transmission coefficient. All the measurements were made under vacuum (<10$^{-3}$ Torr) in a vacuum can with input/output ports for the waveguides designed for the refrigerator. Inside the vacuum can the sample was oriented perpendicular to the microwave source by clamping it between two waveguide flanges thermally connected to the cold head of the refrigerator through a gold-plated copper plate. The film side of the sample was directed towards the incident microwave signal. The system was calibrated before the beginning of each measurement cycle to account for the impedance and spurious reflections of the waveguide network. Background attenuation and phase corrections were made by subtracting the transmitted power as a function of temperature in the absence of the sample from the data obtained with the sample in place.

Figure 5 shows a plot of the magnitude ($P$) and relative phase ($\Delta \theta = \theta_{300} - \theta(T)$, with $\theta_{300}$ the phase value at room temperature) at 30.6 GHz of the fractional transmitted power for the film on the LaAlO$_3$ substrate.
substrate as a function of temperature. Since in this type of measurement the signal also interacts with the substrate, similar types of measurement were not performed with the film on SrTiO₃ because of the extreme temperature sensitivity of its dielectric constant and loss tangent [16, 17]. LaAlO₃ has more stable properties and has proved to be a suitable substrate for microwave applications [18, 19]. Observe that in the normal state Σ₁ shows metallic behaviour, while Σ₂ is close to zero as expected for a good conductor. When the superconducting transition begins (we refer to this temperature as T₆₅, which in this case is ~88 K), both conductivities increase rapidly. As the temperature decreases, Σ₁ increases to a maximum and then decreases quickly to the extent that we were unable to determine its value for temperatures below ~74 K, while Σ₂ increased monotonically. This behaviour is consistent with that reported for YBCO and other BSCCO thin films [7, 20, 21]. The same temperature behaviour for Σ* was observed for measurements at other frequencies within the Ka-band. From figure 6(a) it can be seen that the behaviour of Σ₁ in the superconducting state does not follow that expected from the two-fluid model approximation [22] where,

\[ \Sigma_1(T) = \Sigma_1(T/T_c)^4 \]

and \( \Sigma_2 \) is the conductivity at \( T_c \). The measured data also deviated from \( \Sigma_1 \) calculated using the BCS-based Mattis-Bardeen equations [23]

\[ \Sigma_1 = \sigma_0 [2\Delta/k_B T]^{-1} \exp[-\Delta/k_B T] \ln(\Delta/\hbar\omega) \quad \hbar \omega \ll 2\Delta \]

where \( k_B \) is Boltzmann's constant, \( \omega = 2\pi f \) is the angular frequency, and \( \Delta \) is the energy gap.

The values of \( \Sigma_2 \) can be used to determine \( \lambda \) by using the expression \( \lambda = (1/j\mu_0\sigma_j)^{1/2} \), valid for homogeneous superconductors. \( \lambda \) values of ~1.97 and 1.09 µm at 77 and 20 K respectively, were obtained for the film on LaAlO₃. The value of \( \lambda \) at low temperature is less than that obtained in ion-beam-deposited BSCCO thin films on MgO (\( \lambda \sim 1.3 \mu m \)) [20], and compare well with those obtained using microstrip transmission lines fabricated with the same type of co-evaporated BSCCO films used in this study (\( \lambda(0) \sim 1.11 \mu m \)), where \( \lambda(0) \) is the magnetic penetration depth at
However, the values of $\lambda$ are still large when compared with those reported for BSCCO single-crystals ($d(0) \sim 0.3$ µm) [25–27].

### 3.2. Surface resistance measurements

#### Cavity method

The $R_s$ of the films was measured by monitoring the change in the quality factor ($Q$) of a cylindrical, $TE_{011}$ mode copper cavity, resonant at 58.9 GHz, with one of its end walls replaced with the BSCCO thin film. Using an HP-8510B network analyser and Ginzton's impedance method the loaded $Q$ ($Q_L$) of the cavity was determined by measuring the reflection coefficient. Knowing $Q_L$, the unloaded quality factor ($Q_u$) of the cavity was obtained and the $R_s$ of the BSCCO films were computed by the method in [28]. As shown in Figure 7, the $R_s$ of the BSCCO films decreased monotonically with temperature for $T/T_c > 0.75$, levelling off at lower temperatures. Note that, except for very low temperatures, the $R_s$ for the film on SrTiO$_3$ is less than that of its counterpart on LaAlO$_3$. Values of $R_s$ of 865 and 376 mΩ for the film on SrTiO$_3$, and of 1391 and 370 mΩ for the film on LaAlO$_3$ were obtained at 77 and 20 K respectively. The $R_s$ values at low temperatures are almost one-fifth of those measured at lower frequencies on BSCCO films on MgO using microstrip and cavity resonator techniques ($\sim 25$ mΩ at 7 GHz and 25 K; $R_s \sim 1770$ mΩ at 58.9 GHz assuming $R_s \propto f^{-2}$ dependence) [29]. They are also almost an order of magnitude less than those recently obtained by others from ring microstrip resonators fabricated on e-beam deposited BSCCO films on MgO using microstrip and cavity resonator techniques ($\sim 34$ mΩ at 4.2 K, 6 GHz, and 12 dB m incident RF power; 3276 mΩ at 4.2 K, 58.9 GHz, using $R_s \propto f^{-2}$) [30]. Since the $R_s$ of the film is larger than that of Cu for all temperatures (for very pure Cu and at 77 K, $R_s \sim 21.6$ mΩ at 58.9 GHz; the measured $R_s$ value for a Cu sample at 77 K using the cavity was $\sim 45.4$ mΩ) the flat part of the curve may be associated with residual losses in the film and not with limitations in the sensitivity of the cavity, in contrast to measurements of good quality YBCO thin films on LaAlO$_3$ [7].

#### Linear resonator method

Microstrip transmission line resonators were fabricated and tested to examine the losses of the BSCCO films in a structure that can be used in potential HTS passive microwave circuits such as filters, resonators or delay lines. The microstrip structure is shown in figure 8 and consisted of the BSCCO superconducting strip separated from a gold ground plane by the 0.010 in LaAlO$_3$ substrate (figure 8(a)). The strip width ($W$) was 300 µm with a length ($L$) of 7 mm (figure 8(b)). This resulted in a 30 Ω line impedance with the fundamental ($L = \lambda/2$) resonant frequency at 10.4 GHz and a second harmonic ($L = \lambda$) at 20.2 GHz. The resonant strip was capacitively coupled to a 30 Ω feed line by a 75 µm wide gap ($G$). Transition from the coaxial test cables to the microstrip feed line was accomplished by a coaxial 'spark-plug' launcher. The circuit was tested using an HP 8510B network analyser and a closed-cycle refrigerator for cooling. The test cable was calibrated up to the spark-plug launcher using coaxial open, short, and load standards. The calibration was performed at room temperature but was used at low temperatures as well since only minor shifts in the calibration with decreasing temperature were observed. The reflection coefficient ($S_11$) was measured at temperatures from $-20$ K upwards, giving the loaded $Q$ of the circuit. Using the impedance method [31, 32] the unloaded $Q$ was extracted from the reflection data.

Figure 9 shows a plot of the unloaded $Q$ values against temperature for the superconducting and an identical gold (Au) resonator at 10.4 and 20.2 GHz. The $Q$ values of the Au resonator are relatively flat over this temperature range with the $Q$ values at 20.2 GHz larger than those at 10.2 GHz, as expected for a conductor loss-limited transmission line resonator where $Q \propto f^{1/2}$, and $f$ is the frequency. A measurable response for the HTS resonators began just below the $T_c(R = 0)$ value measured for the films. As seen in figure 9, the $Q$ values increased with decreasing temperature and exceeded the $Q$ values of the Au resonator around 60 to 65 K. However, the BSCCO unloaded $Q$ values above $\sim 60$ K
Au circuit Q at 10.4 GHz and 20 K, and approximately reaching values of approximately four times that of the increasing down to the lowest temperatures measured. The Q values of the superconducting resonator kept Au) leads to overall higher conductor loss and lower Q. These R, values are less than those for the Au resonator because the thinner BSCCO film (0.3 μm for BSCCO; 1.5 μm for Au) leads to overall higher conductor loss and lower Q.

The unloaded Q values of the resonator may be used to estimate the R, of the BSCCO thin film [32]. The R, values obtained at 10.4 and 20.2 GHz, and the R, values corresponding to Au are plotted in figure 10. R, values at 73 K of 13 and 22 mΩ were obtained for the BSCCO at 10.4 and 20.2 GHz respectively. At 20 K, R, was ~0.75 and 2.9 mΩ at 10.4 and 20.2 GHz respectively. These R, values are less than those for the Au film at the same frequencies and temperatures, and are approximately eight times smaller than earlier values (~25 mΩ at 25 K) reported at 7 GHz [29]. Also plotted in figure 10 are the values of R, for the BSCCO thin film at 20.2 GHz obtained assuming a R, oc f dependence, where f is the frequency, and using the experimental values measured at 10.4 GHz. Note that although there is a noticeable discrepancy between the measured and calculated R, values at 20.2 GHz at T near Tc, the agreement between the two sets of values improves at temperatures far below Tc.

4. Discussion

We have characterized co-evaporated BSCCO thin films on SrTiO3 and LaAlO3 substrates. We have compared the films in terms of their Tc and Jc values, surface morphology and XRD patterns. It was observed that, although both films have similar dc Tc, the film on the SrTiO3 substrate has a larger Jc from 4.2 to 40 K, a smoother surface morphology, and lower R, than its counterpart on LaAlO3. From the power transmission measurements we have shown that the conductivity in the superconducting state does not follow either the BCS or two-fluid model temperature dependence. However, the observed increase in R, for T < Tc is consistent with the observation of Ho et al [20] (for ion-beam-deposited BSCCO thin films on MgO at 60 GHz) who suggested that this trend below Tc is either an intrinsic temperature dependence of the homogeneous superconductor or the manifestation of the response of a composite consisting of superconducting regions growing in a normal conducting matrix. In the case of our films, although σ1 increases very quickly upon cooling the sample below ~88 K, we also observed that, contrary to the observations by Ho et al [20], it reaches a maximum at T not far below Tc** and then falls very quickly. This behaviour may be due to the better quality of the co-evaporated films under study as compared with those analysed by Ho et al [20], which have Tc ~ 68 K and Jc ~ 5 x 10^4 A cm^-2 at 10 K. Thus it may be reasonable to assume that as the quality of the material improves, i.e., as the normal conductor fraction in the material decreases, the behaviour below Tc could actually approach that expected from the two-fluid model. A more rigorous analysis should be performed along this line in the future.

From the R, values obtained using the resonant cavity technique, one can see that the values at 77 K for the films on SrTiO3 and LaAlO3 are approximately 12 and 20 times, respectively, larger than those of pure Cu and Au at room temperature, and about 8 and 13 times, respectively, that of a Au-plated Cu sample. However, the R, measured at 10.4 GHz using the linear resonator patterned on the film on LaAlO3 (~13 mΩ) is similar to that of pure Cu and pure Au at the same frequency and temperature (R, Cu ~ 10 mΩ, R, Au ~ 14.3 mΩ), and lower than that of its Au counterpart (~23 mΩ). We
found that when the $R_s \propto f^2$ dependence was used to determine the $R_s$ of the BSCCO film at 20.2 GHz using the resonator technique, the agreement between the calculated and measured values at this frequency improved for temperatures far from $T_c$. However, when the same approach was used to determine the $R_s$ at 58.9 GHz ($R_s \sim 13 \text{ m}\Omega$ at 10.4 GHz, and $\sim 417 \text{ m}\Omega$ at 58.9 GHz) the resulting value was approximately one-third of that obtained by the cavity technique at temperatures near 77 K. This discrepancy becomes worse for lower temperatures. This deviation is not unexpected since we are dealing with an heterogeneous system in which the different components (superconducting, normal and possibly insulating) do not necessarily respond to frequency changes in the same way and therefore may alter the frequency dependence of the microwave losses that one expects for a homogeneous superconductor. In addition it will be interesting to see how the different measurement techniques contribute to the deviation especially when it has been suggested by others that calibration differences in different techniques to measure $R_s$ can contribute to the lack of correlation between $R_s$ values in HTS thin films [33].

We have also obtained $\lambda$ for the BSCCO films under discussion. Low temperature values for $\lambda \sim 1.0 \mu m$ were obtained. Although these values compare favourably with those obtained by others in BSCCO films, they are still approximately three times the values reported by others for BSCCO single crystals. This may be due to the inhomogeneity of the films under study as shown by the unknown peaks observed in the x-ray pattern (figure 3). It has been shown by others that non-superconducting inclusions and weak link effects result in an increase of $\lambda$ [34]. The fact that the low temperature $\lambda$ is large compared with the values typically obtained at low temperatures for YBCO thin films ($\sim 0.14-0.3 \mu m$ [5-7]) may impose limitations in the use of this type of BSCCO thin film for microwave applications. In normal conductors, in order to have low conductor losses, the conductor thickness must be at least three times larger than the normal skin depth ($\delta$). If, as in the YBCO films, the superconducting properties of the BSCCO films deteriorate as the film thickness goes beyond 0.5 $\mu m$, then it is clear that improvements in the BSCCO film growth are still necessary. Therefore careful study of the various microwave transmission lines, in terms of the contribution to total losses (i.e., conductor, substrate and radiation losses [35]) must be performed to determine, in view of the limitations described above, for which of these structures the BSCCO HTS film would be more suitable.

Nevertheless, since the values of $T_c$ and $J_c$ are greater than those of other BSCCO thin films deposited by other techniques, we believe that the microwave data presented here are representative of state-of-the-art BSCCO films. In view of this we can see that this type of film offers some possibilities for microwave applications at low frequencies (i.e., $\leq 20 \text{ GHz}$), but potential applications at frequencies around $60 \text{ GHz}$ and above will require further improvements in the material.

5. Conclusions

We have characterized co-evaporated BSCCO thin films on SrTiO$_3$ and LaAlO$_3$. The $J_c$ values measured for these films are better than or equal to those reported by others for state-of-the-art BSCCO films deposited by other techniques. From the microwave power transmission measurements we were able to determine $\sigma^*$; it was found that the temperature dependence of $\sigma^*$ for $T < T_c$ deviates from both the BCS theory and the two-fluid model. The low temperature values of $\lambda$ agreed with those reported by others for BSCCO films, but were approximately three times larger than those of BSCCO single crystals. $R_s$ values for the BSCCO thin films were measured at 10.4, 20.2, and 58.9 GHz. From the $R_s$ data it is evident that the low-$T_c$ phase BSCCO thin films could offer possibilities for microwave applications at low frequencies ($\leq 20 \text{ GHz}$), but applications at frequencies around $60 \text{ GHz}$ and above will require further improvements in the material. To our knowledge this is the first time a microwave characterization in terms of the transport parameters most relevant for transmission line applications has been performed on the same BSCCO film and in the frequency range from 10 to 60 GHz.

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PROCESSING, ELECTRICAL AND MICROWAVE PROPERTIES OF SPATTERED Tl-Ca-Ba-Cu-O SUPERCONDUCTING THIN FILMS

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Abstract—A reproducible fabrication process has been established for TlCaBaCuO thin films on LaAlO3 substrates by rf magnetron sputtering and post-deposition processing methods. Electrical transport properties of the thin films were measured on patterned four-probe test devices. Microwave properties of the films were obtained from unloaded Q measurements of all-superconducting ring resonators. This paper describes the processing, electrical and microwave properties of Tl2Ca1Ba2Cu2Ox (2122) phase thin films.

I. INTRODUCTION

The high temperature superconducting thin films show great promise for electronic applications at 77 °K. Since the discovery of high Tc materials, there has been a substantial progress in the applications such as SQUIDs, passive microwave devices, IR detectors and interconnections in microelectronics. Among the high Tc materials, the TlCaBaCuO compound has proven to possess the highest Tc of 125 °K[1], and hence offers a wide margin of temperature range for applications at 77 °K. Thin films of TlCaBaCuO compound have shown Tc as high as 120 °K, and critical current density (Jc) greater than 10^6 A/cm^2 at 77 K[2]. Also, TlCaBaCuO thin films, primarily of 2122 phase have shown 2122 phase have shown surface resistance (Rσ) about 80 times lower than Cu at 10 GHz and 77 °K[3]. This research work primarily addresses a reproducible processing method for TlCaBaCuO thin films of 2122 phase, electrical transport measurements and also microwave ring resonator measurements.

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II. PROCESSING OF TlCaBaCuO THIN FILMS

The TlCaBaCuO thin films were sputter deposited on (100) LaAlO3 substrates from a single composite powder target in a CVC model 601 rf magnetron sputtering system. The target was a Tl enriched Tl2Ca2Ba2Cu3Ox (2223) powder target, with 20% excess Tl2O3 to compensate for the loss of Tl during post-processing steps and to maintain sufficient composition for several deposition runs. The sputter depositions were performed at an rf power density of 0.7 W/cm^2, and the chamber pressure at 5 mTorr, in a pure argon atmosphere. The thin films were deposited at a deposition rate of approximately 30 Å/min. The sputter deposited thin films of 0.3-0.5 µm thickness were post-processed in two steps: first, sintering in air at 850 °C for 12-15 minutes in an optimum Tl2O partial pressure, and the second, annealing in oxygen flow at 750 °C. These steps were performed in a box furnace with samples placed in an enclosed platinum crucible. The Tl2O partial pressure was provided by placing 2223 pellets inside the crucible. Both the steps were performed with the same number of pellets placed inside the crucible. The Tl2O partial pressure provided during the sintering process establishes the phase in the thin films. The details of the post-processing steps have been reported earlier[4-5].

To provide the optimum Tl2O partial pressure during the post-processing steps, a simple technique was used to monitor the reduction in Tl content in the as-deposited thin films, after each sputtering run. Percentage reduction in Tl content from run to run was obtained by Auger Electron Spectroscopy (AES) surface analysis on the as-deposited samples. This percentage reduction in Tl gives an approximate estimate of additional Tl2O partial pressure needed for the post-deposition processes. The estimated additional Tl2O partial pressure was provided...
by adding additional 2223 pellets in the crucible. This technique has yielded reproducible high $T_c$ and high $J_c$ thin films. The annealed thin films were essentially smooth in morphology. The superconducting thin films were characterized by X-ray diffraction (XRD) analysis to determine the phase purity. XRD spectra obtained on a TlCaBaCuO thin film is shown in figure 1. The characteristic peaks of 2122 and 2223 phases were present. The 2122 phase with c-axis oriented growth was the dominant phase in the thin films, as determined from the XRD data.

![XRD spectra obtained on an annealed TlCaBaCuO thin film showing c-axis oriented 2122 and 2223 peaks.](image)

**Fig.1** XRD spectra obtained on an annealed TlCaBaCuO thin film showing c-axis oriented 2122 and 2223 peaks.

### III. ELECTRICAL TRANSPORT PROPERTIES

Electrical transport measurements were performed on patterned four-probe test devices 10, 25 and 50 µm wide, and 1 mm long. The test devices were patterned on as-deposited TlCaBaCuO thin films using standard positive photoresist photo-lithography, and wet chemical etching in a weak phosphoric acid. Positive photoresist AZ 1421 was used for the photo-lithography. The etching solution was a 1:100 phosphoric acid:D1 H2O heated to about 75 °C. The etch rate was approximately 30 Å/min. The patterned samples were post-processed using our standard procedures described above.

For reliable electrical measurements, a process for making low resistance gold contacts on TlCaBaCuO thin films was established. First, metal bonding pads were formed by thermally evaporating 6000 Å thick gold film on the superconducting pads of the four-probe device. The samples were annealed at 600 °C for 15 minutes in an oxygen flow of 1 liter/min, followed by a slow furnace cooling for 30 minutes after the furnace was switched off. Gold wires were bonded to the pads using an ultrasonic wedge bonder. Typically, the four-probe test devices showed zero resistance $T_c$ between 97 and 100 °K. The measurements were performed at a constant applied current of 10 µA. The contact resistance obtained from the I-V measurements of the four-probe devices is typically a few mΩ at temperatures below $T_c$. The specific contact resistivity was approximately $3.65 \times 10^{-5}$ Ω·cm² at 90 °K, and below $10^{-8}$ Ω·cm² at 77 °K.

The zero-field transport current density ($J_c$) measurements were performed using dc and pulsed current techniques, using a 1 µV/mm electric field criterion. Figure 2 shows the $J_c$ vs temperature measurements obtained on two four-probe test devices. Zero-field $J_c$ greater than $10^5$ A/cm² at 77 °K was obtained in the four-probe devices tested.

![Zero-field $J_c$ vs Temperature for two different TlCaBaCuO thin films measured using 1 µV/mm criterion.](image)

**Fig.2** Zero-field $J_c$ vs Temperature for two different TlCaBaCuO thin films measured using 1 µV/mm criterion.

### III. MICROWAVE PROPERTIES

The microwave properties of the TlCaBaCuO thin films were obtained indirectly by measuring the unloaded Q of all-superconducting ring resonators. A ring resonator was designed for a fundamental resonance at 12 GHz. The device consisted of a ring structure separated from the feed line by a small coupling gap. The figure 3 shows a ring resonator designed for fundamental resonance at 12 GHz, for 10 mil
thick LaAlO$_3$ substrates ($\varepsilon_r = 24.5$). In the figure, the linewidth of the ring and the microstrip feed line is $W = 5.6$ mils, the coupling gap $G = 1.75$ mils, and the mean radius of the ring $R = 77$ mils.

The unloaded $Q$ of the superconducting ring resonator is approximately four times higher than the gold resonator at 65 °K. The ring resonators offer an indirect method for measuring the surface resistance ($R_s$) of superconducting thin films. By separating the conductor and dielectric losses, the $R_s$ of the Tl$_2$Ca$_3$Ba$_2$Cu$_2$O$_{x}$ thin films were calculated using the standard microstrip loss equations described by Pucel et al.[7]. The effective $R_s$ at 12 GHz and 77 °K was determined to be typically between 1.5 and 2.75 m$\Omega$, almost an order of magnitude lower than the $R_s$ of Cu at the same frequency and temperature. The lowest surface resistance reported in Tl$_2$Ca$_3$Ba$_2$Cu$_2$O$_{x}$ thin films to date is 0.130 m$\Omega$ at 77 K and 10 GHz[3].

The swept frequency reflection measurements performed at several temperatures, were also used in determining the effective penetration depth in the Tl$_2$Ca$_3$Ba$_2$Cu$_2$O$_{x}$ thin films. The shift in resonance frequency with temperature is mainly due to the temperature dependence of the penetration depth in the superconducting thin film. The velocity of a superconducting microstrip line with a superconducting ground plane is given by[8],

$$v_{ph} = c\sqrt{\varepsilon_{eff}(1+2(\lambda/h)\coth(t/\lambda))^{-0.5}} \quad (1)$$

where $c$ is the velocity of light, $\varepsilon_{eff}$ is the effective dielectric constant, $h$ is the substrate thickness, $t$ is the thickness of the microstrip, $\lambda$ the penetration depth of the superconducting microstrip. The penetration depth is temperature dependent based on the Gorter-Casimir relationship, ie.,

$$\lambda(T) = \lambda(0)[1-(T/Tc)^{4}]^{-0.5} \quad (2)$$

for temperature $T$ less than $Tc$. $\lambda(0)$ is the penetration depth at $T = 0$ °K. The resonance frequency of the ring resonator is given by the equation

$$f = n v_{ph}/(2L) \quad (3)$$

where $f$ is in GHz, $L$ is the mean circumference of the ring in mm, and $n$ is the integer order of resonance. From the above equations, the lowest value of the effective $\lambda(0)$ was determined to be 6890 Å. The typical value ranges between 7000 Å and 8000 Å. Since the thin films were only 0.3-0.4 μm thick, the penetration depth depends upon the properties of the superconductor through the entire film. This may be a reason for the higher penetration depth. The typical values of penetration depth reported in literature is between 4000 and 8000 Å in TI 2122 phase thin films[9-10]. The higher value of penetration depth is also an indication of the film quality. Improvements in film quality should yield lower effective
IV. SUMMARY

A reproducible fabrication process has been established for TICaBaCuO thin films of 2122 phase on LaAlO3 substrates. Zero resistance $T_c$ as high as 100 °K, and the zero-field $J_c$ as high as $5 \times 10^5$ A/cm² were obtained in four-probe test devices. The surface resistance of the TICaBaCuO thin films obtained by separating the conductor losses from $Q$ measurements in ring resonators is typically between 1.5 and 2.75 mΩ at 12 GHz and 77 °K. The effective penetration depth at 0 °K, calculated from the resonance frequency shift with temperature measurements was typically between 7000 and 8000 Å.

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[10] Private Communications with Dr. Felix A. Miranda of NASA Lewis Research Center.
Electrical-transport properties and microwave device performance of sputtered TlCaBaCuO superconducting thin films

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TI-Ca-Ba-Cu-O high-temperature superconducting thin films were deposited on lanthanum aluminate substrates, by rf magnetron sputtering and postannealing methods. A reproducible fabrication process with low-resistance metal contacts has been established for high-Tc and high-Jc TlCaBaCuO thin films after patterning using standard microelectronic photolithography and wet chemical etching techniques. Low-resistance gold contacts on TlCaBaCuO thin films were obtained by annealing in an oxygen flow of 1 l/min followed by a slow furnace cooling. Specific contact resistivity was approximately $10^{-10}$ $\Omega$ cm$^2$ below 77 K. High transition temperatures as high as 100 K, and current density at zero magnetic field greater than $10^5$ A/cm$^2$ are routinely obtained in 0.3–0.5 $\mu$m TlCaBaCuO thin films. The morphology studies of the films using scanning electron microscopy show the correlation between $J_c$ and the microstructure of the films. Films with featureless morphology have larger zero-field transport currents. The microwave properties of TlCaBaCuO thin films were investigated by designing, fabricating, and characterizing microstrip ring resonators with a fundamental resonance frequency of 12 GHz on 10-mil-thick lanthanum aluminate (LaAlO$_3$) substrates. Ring resonators with a superconducting ground plane of 0.3 $\mu$m thickness and a gold ground plane of 1 $\mu$m thickness were fabricated and characterized in the temperature range of 60–95 K. Typical unloaded quality factors $Q$ for the ring resonators at 12 GHz were above 1500 at 65 K, compared to an unloaded $Q$ of 370 for a gold ring resonator. A surface resistance as low as 1.5 m$\Omega$ at 12 GHz and 77 K was obtained in 0.3 $\mu$m TlCaBaCuO thin films using the ring resonator $Q$ measurements. Typical values of penetration depth at 0 K in the TlCaBaCuO thin films were determined to be between 7000 and 8000 Å using the temperature variation of resonance frequency measurements.

I. INTRODUCTION

Since the discovery of a copper-oxide high transition temperature ($T_c$) superconductor by Bednorz and Muller in January 1986, there has been substantial progress in superconducting electronics. Several new compounds such as YBaCuO, Bi-Sr-Ca-Cu-O, and TlCaBaCuO have been found to be superconducting above 90 K, thus making it feasible for electronic applications at liquid-nitrogen temperature (77 K). Currently, worldwide research is underway for developing high-$T_c$ superconducting electronics. Already rapid progress has been made for applications of high-$T_c$ materials in areas such as superconducting quantum interference devices (SQUIDs), passive microwave devices, IR detectors, and interconnections in microelectronics.

Among the high-$T_c$ materials, the TlCaBaCuO compound has proven to possess the highest $T_c$, which means a wide margin of operational range is available for electronic applications at 77 K. The TlCaBaCuO thin films are very attractive for electronic applications, as they have shown high $T_c$ and high critical current density $J_c$. Fabrication of TlCaBaCuO thin films on lanthanum aluminate (LaAlO$_3$) substrates has been reported by the authors. LaAlO$_3$ substrates have a good c-axis lattice match with TlCaBaCuO thin films to permit highly c-axis-oriented growth of TlCaBaCuO superconducting thin films. The dielectric constant of LaAlO$_3$ is 24.5 (Ref. 15) and the loss tangent is approximately 8.3 x 10$^{-5}$ at 77 K. The growth of TlCaBaCuO thin films on LaAlO$_3$ substrates offers promising applications in the area of microwave electronics. The only disadvantage of TlCaBaCuO compound is the toxicity of thallium (TI) which needs very careful processing and handling procedures. For microelectronic and microwave applications of TlCaBaCuO thin films, it is very important to establish a reproducible fabrication process for superior electrical and microwave properties.

The foremost applications of high-$T_c$ thin films is expected to be in the area of “passive microwave devices” such as resonators and filters. High-$T_c$ superconducting thin films have lower surface resistance $R_s$ compared to Cu and Au, corresponding to higher $Q$ and improved performance in passive microwave devices. TlCaBaCuO thin-film-based passive microwave devices have shown superior...
performed. Chang et al.\textsuperscript{5} have reported a surface resistance at least an order smaller than Cu at 77 K and 9.5 GHz. Bourne et al.\textsuperscript{6} reported a 1 ns microstrip delay line using thin films of TlCaBaCuO, again a factor of 10 improvement in loss was observed at 3.29 GHz and 77 K. Hammond et al.\textsuperscript{7} reported a TlCaBaCuO microstrip resonator and its power handling performance at 77 K. At effective power levels in the resonator up to 100 W, the Q was still three times higher than a silver resonator at 2.6, 5.2, and 7.3 GHz. Linear resonators with loaded Q as high as 15 000 at 5 GHz have been demonstrated.\textsuperscript{8}

This paper describes the processing and electrical transport measurements for achieving reproducible high-\(T_c\) high current density \(J_c\), low microwave surface resistance \(R_s\), TlCaBaCuO thin films on LaAlO\(_3\) substrates, for microelectronic applications. A method for fabricating low-resistance contacts on TlCaBaCuO thin films for reliable electrical transport measurements is also addressed. The microwave properties of TlCaBaCuO thin films were investigated by designing, fabricating, and characterizing microstrip ring resonators for 12 GHz fundamental resonance frequency. This paper describes the results of these investigations.

II. EXPERIMENTAL

TlCaBaCuO thin films were sputter deposited from a single composite powder target in a CVC model 601 rf sputtering system operating at 13.56 MHz. The system was operated in the rf magnetron mode to improve the sputtering yields at low working pressures. The depositions were performed in a "sputter up" configuration on substrates placed face down. The Tl\(_2\)Ca\(_2\)Ba\(_2\)Cu\(_3\)O\(_x\) powder target was prepared by the solid-state reaction of stoichiometric amounts of high-purity BaO, CaO, CuO, and TlO\(_2\) (in the ratio 2:2:2:3) powders. The target was enriched with 20\% excess TlO\(_2\) to compensate for the loss of Tl during the postprocessing of the thin films, and to maintain sufficient composition for several deposition runs. The powder target was spread over an 8-in.-diam copper plate which was part of the cathode assembly, and pressed to obtain a uniform surface. The (100) LaAlO\(_3\) substrates were degreased in acetone, methanol, rinsed in de-ionized (DI) water, and blown dry using nitrogen before loading into the vacuum chamber. Depositions were performed at a rf power density of 0.7 W/cm\(^2\), and a chamber pressure at 5 mTorr, in a pure argon atmosphere. The thin films were deposited to a thickness of about 3000–5000 Å, at a deposition rate of approximately 30 Å/min, as determined by Dektak profilometer thickness measurements. The detailed fabrication process has been described earlier by the authors.\textsuperscript{12}

The sputter-deposited thin films of 0.3–0.5 \(\mu\)m thickness were postprocessed in two steps: first, sintering in air at 850 °C (to create the Tl\(_2\)O liquid phase), in an excess Tl partial pressure; and second, annealing in flowing oxygen at about 750 °C in an excess Tl partial pressure. These processes were performed in a small box furnace with the samples placed in an enclosed platinum crucible in the free-surface configuration described by Ginley et al.\textsuperscript{11}

The thin films were placed on a Tl\(_2\)Ca\(_2\)Ba\(_2\)Cu\(_3\)O\(_x\) pellet, with the film side facing the free surface in an enclosed platinum crucible. A second pellet was placed on a platinum wire mesh, approximately half an inch above the thin-film surface. The pellets provided the excess Tl partial pressure inside the crucible, mainly to minimize the loss of Tl from the thin films. The details of the post-processing heat treatments has been reported earlier.\textsuperscript{11,12} For reproducible processing of TlCaBaCuO thin films, it was necessary to provide the optimum Tl partial pressure during postdeposition processes. A simple technique was used to monitor the reduction in Tl content in the as-deposited thin films, after each sputtering run. The percentage reduction in Tl content from run to run was obtained through Auger electron spectroscopy (AES) surface analysis on the as-deposited samples. The percentage reduction in Tl content compared to a standard reference 2223 pellet gives an approximate estimate of additional Tl partial pressure needed during the postdeposition processes. The estimated additional Tl partial pressure was provided for the postdeposition processes by adding additional 2223 pellets in the crucible. This technique has yielded reproducible high-\(T_c\) and high-\(J_c\) films.\textsuperscript{14}

For the electrical-transport measurements, four-probe test devices were designed with linewidths of 10, 25, and 50 \(\mu\)m for electrical-transport measurements. The voltage sense lines are 1 mm apart.

FIG. 1. The geometry of four-probe test devices with linewidths of 10, 25, and 50 \(\mu\)m for electrical-transport measurements. The voltage sense lines are 1 mm apart.
etching techniques. Positive photoresist AZ 1421 was used for the lithography. The as-deposited TiCaBaCuO thin films on LaAlO₃ substrates were prebaked at 180 °C for 20 min before the photoresist was spun. The photoresist AZ 1421 was spun on to a thickness of about 1 µm. The samples were soft baked at 90 °C for 20 min, followed by exposure to UV light in a mask aligner. The photoresist was developed in a 1:5 developer:DI H₂O solution for 45 sec. The samples were postbaked at 85 °C for 15 min to complete the photolithography process. A 1:90 phosphoric acid:DI H₂O solution was used for chemically etching the films. The solution was kept at a constant temperature of 75 °C. The etch rate was approximately 40 Å/min. After the etching process was completed, the photoresist was removed by immersing the samples in acetone for 25 s, followed by a 30 s rinse in DI H₂O. The patterned samples were postprocessed using our standard methods described above.

For electrical measurements on the test devices, metal bonding pads were formed by thermally evaporating 6000-Å-thick gold film on the superconducting pads, through a shadow mask. In order to obtain low-resistance contacts, the samples were annealed in an oxygen flow of 1 l/min, for about 15 min at 600 °C, followed by slow furnace cooling for 30 min after the furnace was switched off. The samples were removed when the furnace temperature was approximately 300 °C. Gold wires of 1 mil diameter were bonded to the gold pads using a Kulicke and Soffa Model 4123 ultrasonic wedge bonder. The bonding process did not require sample heating. For redundancy, multiple bonds were attached on the contact pads.

The zero-resistance Tc of the test devices was determined by measuring the resistivity versus temperature characteristics. The critical transport Jc was measured using dc and pulsed-current techniques, using a 1 µV/mm electric-field criterion. A Keithley model 181 nanovoltmeter and a Keithley model 224 current source were used for the dc transport measurements. The specimen temperature was controlled using a Lakeshore model 805 temperature controller, connected to a closed-cycle helium gas refrigeration system. The error in temperature measurement was less than 0.25 K. Thermal equilibrium was established before measurements at each temperature below Tc. The dc current method was not used above a current density of 10⁶ A/cm², since sample heating at higher currents could cause the films to crack before measurements could be completed.

The pulsed current measurements were performed using two EG&G PARC 5210 lock-in amplifiers, a HP 214B pulse generator, and an adjustable current source capable of supplying 1 A. The pulse generator supplies a 10 V, 1 KHz pulse train with a 10% duty cycle. The pulsed current is applied to the test device, and the corresponding voltage pulse is measured across the sample using the lock-in amplifiers. The amplitude of the current pulse at which the voltage across the sample exceeds 1 µV yields the critical current at a particular temperature. The pulsed current measurements were compared to the dc values at as many temperatures as possible to insure the accuracy and comparability of the two methods. The morphology of the finished TiCaBaCuO devices was examined in an ISI SX-30 scanning electron microscope (SEM). The morphology was evaluated in order to study the correlation between Jc and the microstructure of the films.

A microstrip resonator is a useful device for measurement of dispersion, phase velocity, and effective dielectric constants of dielectric substrates. Ring resonators are being widely used for realizing filters, and stabilization of oscillators. A microstrip ring structure resonates if its electrical length is an integral multiple of the guide wavelength. A simple ring resonator device was designed that consisted of a ring structure separated from the feed line by a small coupling gap. The size of the coupling gap determines the coupling between the feed line and the ring resonator. Loose coupling is desired to minimize excessive loading effects. A ring resonator designed for 10-mil-thick LaAlO₃ substrates (εr=24.5), for a fundamental resonance at 12 GHz is shown in Fig. 2. In the figure, the linewidth of the ring and the microstrip feed line is W=5.6 mils, the coupling gap G=1.75 mils, and the mean radius of the ring R=(R1+R2)/2=77 mils. The characteristics impedance of the microstrip is 41 Ω at 12 GHz. The details of the design of the ring resonator have been described by Chary et al. A TiCaBaCuO ring resonators were fabricated by patterning 0.3 µm thin films using AZ 1421 positive photore sist photolithography and wet chemical etching techniques similar to the process used for fabricating the four-probe test devices described above. The ring resonators were annealed using the same annealing procedure described above. The samples were divided into two groups: one set of samples with 1 µm gold film on the bottom side of the LaAlO₃ substrate for the ground plane formation and a second set with a 0.3 µm TiCaBaCuO superconducting thin-film ground plane. The ground plane side superconductor was deposited and postprocessed using our routine postdeposition methods described above, after the microstrip ring resonator was fabricated on the top side.

A ring resonator was mounted in a gold-plated copper test fixture of 1 in. wide, 2 in. long, and 1 in. thick. The test fixture of 1 in. wide, 2 in. long, and 1 in. thick. The test
FIG. 3. The resistivity vs temperature characteristics of a patterned TiCaBaCuO thin-film test device, after lithography, chemical etching, and annealing, showing the onset of $T_c$ at 106 K and zero resistivity at 98.5 K.

 fixture was placed on the cold head of the helium gas closed-cycle cryogenic system. Electrical connection to the feed line was obtained by mechanical contact of a launcher at the input side of the test fixture. Connections to the HP 8720 network analyzer were made using a 0.141 in. semirigid coaxial cable of 50 Ω characteristic impedance. Before measurements were performed on ring resonators, standard one-port calibration was performed at room temperature. The calibration was performed using an open, a short, and a broadband load to effectively remove the test system imperfections introduced by the interconnecting cables, adapters, etc. The calibration was also valid at lower temperatures.

III. RESULTS

The resistivity versus temperature characteristics of a 50-µm-wide four-probe test device is shown in Fig. 3. The measurements were taken at a constant applied current of 10 µA. The onset of superconductivity occurred at 106 K, and the device showed zero resistance at 98.5 K. The room-temperature resistivity was $1.5 \times 10^{-3}$ Ω cm. Zero resistance $T_c$ between 97 and 100 K is routinely obtained. The $T_c$ is low because of the Ti$_2$Ca$_2$Ba$_2$Cu$_3$O$_x$ (2122) phase, which is the dominant phase in these films. The thin films were also characterized by x-ray-diffraction analysis (XRD), and the results showed the characteristic peaks of 2122 and 2223 phases. The 2122 phase with c-axis-oriented growth was the dominant phase in the TiCaBaCuO thin films, as determined from the XRD data. The details of the XRD analysis are reported by the authors elsewhere.

The contact resistance obtained from four-probe resistance measurements is typically a few mΩ, at temperatures below the $T_c$. The specific contact resistivity calculated from the four-probe resistance measurements range from $3.65 \times 10^{-5}$ Ω cm$^2$ at 90 K, to $10^{-10}$ Ω cm$^2$ below 77 K. These results were reproducible from sample to sample and are comparable with the results for Au contacts on YBaCuO high-temperature superconducting thin films.

FIG. 4. Typical zero-field current density $J_c$ vs temperature characteristics of a TiCaBaCuO four-probe test device obtained using the 1 µV/mm electric-field criterion.

Figure 4 shows the typical zero-field current density $J_c$ versus temperature measurements obtained on the four-probe test devices. Current densities at zero magnetic field as high as $5 \times 10^5$ A/cm$^2$ at 77 K an approximately $1 \times 10^6$ A/cm$^2$ at 60 K were obtained. The resistivity of the sample calculated from the $I-V$ measurements is approximately $2.38 \times 10^{-11}$ Ω cm at 77 K, much lower than any normal conductors at this temperature. The surface morphology of one of the test devices is shown in Fig. 5. The surface was essentially featureless and very smooth, typical of high-quality films. The current density of such films exceeded $10^5$ A/cm$^2$ at 77 K. Films with numerous intergrain boundaries showed lower current densities below $10^4$ A/cm$^2$ at 77 K.

The resonator quality factor $Q_r$, the ratio of the energy stored in the resonator to the energy dissipated in the resonator, was obtained from swept frequency reflection mea-

FIG. 5. Scanning electron micrograph of a TiCaBaCuO thin-film surface showing a smooth featureless morphology. The marker is 2 µm long.
The unloaded $Q$ value is a figure of merit for a resonator, and is inversely proportional to the total losses in the circuit. The measured $Q$ (called the loaded $Q$) is a measure of the circuit losses including the coupling loss and the loss through the feed line. The actual $Q$ of the ring resonator (called the unloaded $Q$) is a measure of the losses only in the resonator. The unloaded $Q$ is obtained by separating the external losses in the feed line and due to coupling. The loaded $Q$ and the unloaded $Q$ are related through the reflection coefficients at and far from resonance. The derivation for the relationship between the loaded $Q$ and the unloaded $Q$ is described by Aitken. A computer program was written to compute the unloaded $Q$ values from the measured loaded $Q$ and the magnitude of reflection coefficients at and far from resonance. The determination of whether the resonator was overcoupled or undercoupled was made from the Smith chart and also the phase response of the resonator. Typically, the ring resonators were overcoupled. Measurements for the superconducting resonator were performed at the fundamental resonance frequency of 12 GHz and an input power level of $-30$ dBm.

Unloaded $Q$ versus temperature characteristics for two ring resonators is shown in Fig. 6. Curve A is the data for the high-$T_c$ thin-film ring resonator with a superconducting ground plane. For comparison, data for the gold resonator with a gold ground plane is shown by curve B. The unloaded $Q$ of the ring resonator with superconducting ground plane is approximately four times higher than the gold resonator at 65 K. In addition, the unloaded $Q$ of the superconducting ring resonator shows an increasing trend in $Q$ with decreasing temperature, whereas the superconducting ring resonators with gold ground plane show a saturation of $Q$ at low temperatures due to the dominance of ground plane conductor losses.

The superconducting ring resonators offer an indirect method for measuring the surface resistance $R_s$ of the superconducting thin films. This microwave surface resistance is the fundamental quantity responsible for the conductor losses at high frequencies. The $R_s$ of sputtered thin films were obtained from ring resonator quality factor $Q$ measurements. By separating the conductor and dielectric losses, the surface resistance of the TiCaBaCuO thin films was calculated using the standard microstrip loss equations described by Pucel, Masse, and Hartwig. The $R_s$ at 12 GHz and 77 K was determined to be typically between 1.5 and 2.75 mΩ, almost an order of magnitude lower than $R_s$ of Cu at the same temperature and frequency.

The swept frequency reflection measurements performed at several temperatures are also used in determining the penetration depth of the TiCaBaCuO superconducting thin films. The $R_s$ value is the frequency at which the magnitude of the reflection coefficient is at the minimum. The resonance frequency was measured at each temperature for ring resonators. A typical measured resonance frequency shift with respect to temperature for a superconducting ring resonator with an approximately 1-µm-thick gold ground plane is shown in Fig. 7. The shift in resonance frequency with temperature is mainly due to the temperature dependence of the penetration depth of the superconductor. Thus, the resonance frequency shift is an indirect method of determining the penetration depth. From the figure, the change in resonance frequency below 70 K is almost negligible. The superconducting resonators with a 0.3-µm-thick superconducting ground plane showed a slightly higher dependence of resonance frequency with temperature due to the temperature dependence of penetration depths of the top and the ground plane superconductors. A detailed analysis of this figure to determine the penetration depth of the superconducting thin films is given in the following section.

**IV. ANALYSIS AND DISCUSSIONS**

The data from the zero-field current density $J_r$ measurements shown in Fig. 4 were analyzed to investigate the...
dependence of $J_c$ with the temperature ratio $T/T_c$. The slope of the log $J_c$ vs log$(1-T/T_c)$ characteristics is an indication of the type of the superconductor. The slope of the line obtained from our measurements was approximately 1.5 for temperatures between 50 and 80 K. The $(1-T/T_c)^{3/2}$ dependence of $J_c$ is consistent with earlier reports in high-$T_c$ thin films. This indicates that the thin films may contain grain boundaries that are either insulating or behave like a normal metal, or the thin films may be polycrystalline in nature. The presence of grain boundaries and weak flux pinning in T1CaBaCuO thin films may be the main reasons for the lower $J_c$ in T1CaBaCuO thin films compared to epitaxial in situ grown YBaCuO thin films. However, among the polycrystalline high-$T_c$ thin films, T1CaBaCuO thin films have shown superior electrical properties and hence are very attractive for electronic applications.

The penetration depth of T1CaBaCuO thin films can be determined from the resonance frequency versus temperature measurements, by comparing the experimental data shown in Fig. 7 with theoretical calculations. The resonance frequency shift in the ring resonators is assumed to be due to the change in penetration depth with temperature. Neglecting the effects due to the substrate contraction at lower temperatures, the penetration depth was extracted from the resonance frequency shift as discussed below.

The phase velocity of a superconducting microstrip transmission line with a superconducting ground plane is given by

$$v_{ph} = \frac{c}{\sqrt{\varepsilon_{eff}[1 + 2\lambda/h \coth(t/\lambda)]^{-0.5}}, \quad (1)$$

where $c$ is the velocity of light, $\varepsilon_{eff}$ is the effective dielectric constant, $h$ is the substrate thickness, $t$ is the thickness of the microstrip, and $\lambda$ is the penetration depth of the superconducting microstrip. The penetration depth is temperature dependent based on the Gorter–Casimir relationship, i.e.,

$$\lambda(T) = \lambda(0) \left[ 1 - \left( \frac{T}{T_c} \right)^4 \right]^{-0.5}, \quad (2)$$

for temperature $T$ less than $T_c$. $\lambda(0)$ is the penetration depth at $t=0$ K. The resonance frequency of the ring resonator is given by the equation

$$f = \pi v_{ph} / (2L), \quad (3)$$

where $f$ is in GHz, $L$ is the mean circumference of the ring in mm, and $n$ is the integer order of resonance. From the temperature dependence of resonance frequency measurements and the above equations, the best value of $\lambda(0)$ was determined to be 6890 Å. The typical value ranges between 7000 and 8000 Å. This is an approximate estimate for the penetration depth along the $c$ axis in the T1CaBaCuO thin films. Since the thin films are only 0.3-0.4 µm thick, the penetration depth depends upon the properties of the superconductor through the entire film. This may be a reason for the high penetration depth. Also, the patterned thin films have rough edges, and hence the penetration depth obtained using the above technique is an averaged value over the whole film area.

The surface resistance of the TiCaBaCuO superconducting thin films determined from the ring resonator $Q$ measurements was compared with the theoretical surface resistance versus temperature characteristics for a given penetration depth. A theoretical model based on the phenomenological loss equivalence method (PEM) approximation was employed to determine the theoretical variation of conductor losses and the surface resistance with temperature for the superconducting microstrip/gold ground plane, and superconducting microstrip/superconducting ground plane. Both these cases were compared to the attenuation constant of a gold microstrip on LaAlO$_3$ substrate.

The attenuation constant for a superconducting microstrip is calculated from the formula

$$\alpha = (T/T_c)^4 \left[ 1 - \left( \frac{T}{T_c} \right)^4 \right]^{3/2} (G_1/4) (\sigma_n/Z) \times \frac{w^2 \mu^2 [\lambda(0)^3 \coth(X) + X \csc^2(X) (Np/m)], \quad (4)}{\pi^2 (2h/\lambda) \ln(2h/\lambda)}$$

where $X = A [G_1/\lambda(0)] \left[ 1 - \left( \frac{T}{T_c} \right)^4 \right]^{1/2}$. $G_1$ is the geometric factor given by the equation

$$G_1 = 1/((\pi h) [1 - (W_0/4h)^2]) [1/2 + h/W_0 + h/(\pi W_0 \ln(2h/\lambda))], \quad (5)$$

where $W_0$ is the effective width of the microstrip, $A$ is the area of cross section of the microstrip, $T$ is the measurement temperature below $T_c$, and $\lambda(0)$ the penetration depth at 0 K of the superconductor.

The parameters assumed for the calculations are the relative dielectric constant $\varepsilon_r$ of LaAlO$_3$ of 24.5, the loss tangent (tan $\delta$) of LaAlO$_3$ of 8.3 X 10$^{-5}$ below 100 K, the substrate thickness $h$ of 10 mil, the width of the microstrip $W$ of 142 µm, corresponding to a characteristic impedance of 41 Ω at 12 GHz, the thickness of the superconducting microstrip $t$ of 0.3 µm, the ground plane thickness of 1 µm for a gold ground plane and 0.3 µm for a superconducting ground plane, the zero resistance $T_c$ of the TiCaBaCuO thin films of 100 K, and the normal conductivity at $T_c$ ($\sigma_n$) of 1.5 X 10$^8$ S/m.

The ground plane conductor losses can be calculated by the same method, using the geometric factor $G_2$ instead of $G_1$ in Eq. (4),

$$G_2 = 1/((2\pi h) [1 - (W_0/4h)^2]). \quad (6)$$

Figure 8 shows temperature variation of the attenuation due to conductor losses for a gold microstrip (curve A), a superconducting microstrip with a gold ground plane (curve B), and a superconducting microstrip with a superconducting ground plane (curve C) as determined using Eqs. (4)–(6). The upper diagram is for $\lambda(0)$ of 6000 Å, and the lower diagram is for $\lambda(0)$ of 7000 Å. Figure 8 shows the lower attenuation for the microstrip with superconducting ground plane (curve C) compared to the one with gold ground plane (curve B) below 77 K.
The surface resistance of the superconducting thin film is obtained from the equation

\[ R_s = \frac{2Z_0}{G_1}, \quad (7) \]

where \( Z_0 \) is the characteristic impedance of the microstrip. The theoretical temperature variation of surface resistance of the superconducting microstrip with a superconducting ground plane determined using Eq. (7) is shown in Fig. 9, for \( \lambda(0) \) of 6000 Å (curve C) and 7000 Å (curve B). For comparison, the surface resistance of a 1-µm-thick gold microstrip (curve A) on a LaAlO\(_3\) substrate is plotted for the same microstrip geometry. The \( R_s \) calculated from the measured \( Q \) values of an all-superconducting ring resonator on a LaAlO\(_3\) substrate (curve D) is also plotted in Fig. 9. The \( R_s \) obtained from the ring resonator \( Q \) measurements (curve D) deviates from the theoretical temperature dependence as seen in the figure. Since the TlCaBaCuO thin films do react with the LaAlO\(_3\) substrate, it is possible that the region of interaction contributes to additional losses.

\[ \text{FIG. 8. Theoretical temperature variation of attenuation due to conductor losses for a gold microstrip (1-µm-thick gold for both sides: curve A), a superconducting microstrip (0.3 µm) with a gold ground plane (1 µm) in curve B, and a superconducting microstrip (0.3 µm) with a superconducting ground plane (0.3 µm) in curve C. The penetration depth at 0 K was assumed to be 6000 Å for the upper diagram and 7000 Å for the lower diagram.} \]

\[ \text{FIG. 9. Theoretical temperature variation of surface resistance for the all-superconducting ring resonator, for penetration depths at 0 K of 6000 (curve C) and 7000 Å (curve B). The surface resistance calculated from the measured } Q \text{ values of the resonator is also shown in curve D. For comparison, the surface resistance of a gold microstrip is plotted in curve A.} \]

V. SUMMARY

TlCaBaCuO superconducting thin films were fabricated on LaAlO\(_3\) substrates by rf magnetron sputter deposition in a pure argon plasma and by using postannealing techniques. A reproducible fabrication process has been established for TlCaBaCuO thin films on LaAlO\(_3\) substrates for high-\( T_c \) and high-\( J_c \) characteristics. The TlCaBaCuO thin films were patterned into four-probe test devices using standard microelectronic lithography and wet etching techniques. Low-resistance gold contacts on TlCaBaCuO thin films were obtained by annealing at 600 °C in an oxygen flow of 1 1/min followed by a slow furnace cooling for about 30 min. The critical current density measurements were performed using dc and pulsed current techniques under the electric-field criterion of 1 µV/mm. The zero-resistance \( T_c \) between 97 and 100 K are routinely obtained in patterned TlCaBaCuO thin films. Zero-field current density \( J_c \) as high as \( 5 \times 10^5 \) A/cm\(^2\) were obtained in four-probe test devices. The specific contact resistivity measured when the sample is superconducting ranges from \( 3.5 \times 10^{-5} \) Ω cm\(^2\) at 90 K, to \( 10^{-10} \) Ω cm\(^2\) below 77 K.

The microwave properties of TlCaBaCuO thin films were investigated by designing, fabricating, and characterizing a microstrip ring resonator. The resonator was designed for a fundamental resonance frequency of 12 GHz, and for fabrication on 10-mil-thick LaAlO\(_3\) substrates. Ring resonators with a gold ground plane of 1 µm thickness and a TlCaBaCuO superconducting ground plane of 0.3 µm thickness were fabricated and characterized at cryogenic temperatures. The unloaded \( Q \) for the superconducting resonators were above 1500 at 65 K, compared to 370 for a gold resonator. The surface resistance of the TlCaBaCuO thin films obtained by separating conductor losses from the \( Q \) measurements is typically between 1.5
The typical values for the penetration depth at 0 K are approximately between 7000 and 8000 Å. The penetration depth at 0 K was calculated from the resonance frequency shift with temperature measurements. This model predicted lower conductor losses for the microstrip with a superconducting ground plane compared to the ones with gold ground plane using a theoretical method. The conductor losses in the superconducting microstrips with superconducting ground plane were compared to gold ground plane substrate using a theoretical model called the phenomenological loss equivalence method (PEM). This model predicted lower conductor losses for the microstrip with a superconducting ground plane, below 77 K. A theoretical temperature variation of the surface resistance \( R_s \) for different penetration depths was obtained for all-superconducting microstrip (with superconducting ground plane). The \( R_s \) obtained from the \( Q \) measurements in the ring resonators deviates from the theoretical temperature dependence. This is possibly because of additional losses introduced in the devices due to interaction between the TlCaBaCuO thin films and the LaAlO\(_3\) substrates. Nevertheless, the polycrystalline TlCaBaCuO thin films have almost an order-of-magnitude lower surface resistance compared to gold at 80 K. The design of the ring resonator was not optimized for the highest \( Q \), but the results of our investigations show that TlCaBaCuO ring resonator devices fabricated with a superconducting ground plane do show higher \( Q \) compared to a gold resonator below 90 K, proving their usefulness for all-superconducting microwave circuit applications.

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The effect of fluctuations on the electrical transport behaviour in YBa$_2$Cu$_3$O$_{7-x}$

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Abstract. The excess conductivity behaviour of highly oriented YBa$_2$Cu$_3$O$_{7-x}$ thin films prepared by both coevaporation and laser ablation has been studied in detail in the reduced-temperature range $9 \times 10^{-4} < t < 1$. The excess conductivity in all the films studied was found to diverge sharply near $T_c$, in agreement with the conventional mean-field theory. However, the detailed temperature dependence could not be fitted to either the power-law or the logarithmic functional forms as predicted by the theory. The excess conductivity of all the films was found to be exponentially dependent on the temperature over nearly three decades for $9 \times 10^{-4} < t < 10^{-1}$, in contradiction to the mean-field theory.

1. Introduction

The rounding of the superconducting phase transition has been conventionally attributed to fluctuations in the magnitude and lifetime of the order parameter. By considering fluctuations of magnitude less than the order parameter in the Ginzburg-Landau (GL) theory, a critical temperature region was predicted in which the GL theory will not be valid. For temperatures greater than the critical limit the excess contribution $\Delta \sigma$ to electrical conductivity is estimated using the mean-field value of the order parameter in the time-dependent GL (TDGL) theory. The excess conductivity $\Delta \sigma$ is defined as $\sigma_{\text{exp}} - \sigma_{\text{calc}}$ where $\sigma_{\text{exp}}$ is the experimentally observed electrical conductivity and $\sigma_{\text{calc}}$ the conductivity due to normal-electron scattering alone in the absence of superconducting fluctuations. It is found to follow a power-law-type temperature dependence given by

$$\Delta \sigma(T) \propto (t)^{-\eta}$$

(1)

where $t$ is the logarithm of the reduced temperature given by $\ln(T/T_{c}^{mf}) \approx [(T - T_{c}^{mf})/T_{c}^{mf}]$ for $t < 1$ ($T_{c}^{mf}$ is the mean-field transition temperature) and $\eta$ a constant which depends on the dimensionality of conduction [1]. For three-dimensional (3D) conduction it is $\frac{1}{2}$ and for two-dimensional (2D) conduction it is 1. Hence the temperature dependence of $\Delta \sigma$ has been extensively studied in order to determine $\eta$ and, thus, the dimensionality of order parameter fluctuations, the nature

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of contributions to excess conductivity and also to estimate the coherence length. In the case of YBa$_2$Cu$_3$O$_{7-x}$, equation (1) has been extensively used to determine the dimensionality of $\Delta \sigma$ in the range $10^{-3} < t < 1$ and it has been reported to be 3D, 2D and quasi-2D crossing over to a 3D behaviour close to $T_c$ [2]. Recently, however, it was found that $\Delta \sigma$ does not exhibit the classical power-law dependence on $t$ in the mean-field regime but instead has a logarithmic dependence [3]. The deviation from normal behaviour of the specific heat of an untwinned single crystal was also found to exhibit a logarithmic temperature dependence in the range $10^{-4} < t < 10^{-1}$ by Regan et al [4]. The contribution of fluctuations to diamagnetic susceptibility in bulk pellets on the other hand was found to obey the predictions of conventional GL theory [5]. Howson et al [6] have studied the variation in thermoelectric power up to $T_c$ in single crystals and found that it exhibits an anomalous peak near $T_c$ because of the presence of 3D divergent fluctuations. This large body of experimental results clearly indicates that the phenomenon of fluctuations and the length of the critical region in the oxide superconductors is still not completely understood.

In the present work we report the systematic study of $\Delta \sigma$ in highly oriented YBa$_2$Cu$_3$O$_{7-x}$ thin films prepared by two different techniques: coevaporation and laser ablation. The study of fluctuation effects requires the background or normal-state contribution to the overall conductivity to be accurately determined. Hence the normal-state behaviour was analysed in terms of both the linear metallic conduction phenomenon and the more recent resonating-valence-bond (RVB) model [7]. It was found that the film with the lowest room-temperature resistivity follows metallic conduction behaviour while the other films follow the RVB model. The temperature variation in $\Delta \sigma$ for all the films was found to deviate completely from that predicted by the conventional GL-based models.

2. Experimental methods

The thin films of YBa$_2$Cu$_3$O$_{7-x}$ were deposited onto SrTiO$_3$ (100) substrates by two methods: coevaporation and laser ablation. In the coevaporation, Y and Cu were electron beam evaporated while BaF$_2$ was resistively evaporated onto a cold substrate in an oxygen ambient. The thickness of the as-deposited film is 0.5 $\mu$m. The films were later annealed at 850$^\circ$C in wet flowing oxygen to form the superconducting phase. In the case of laser ablation the film (0.3 $\mu$m thick) was deposited onto a heated substrate in an oxygen atmosphere from a sintered YBa$_2$Cu$_3$O$_7$ target. Structural characterization of the films was done by scanning electron microscopy and large-angle x-ray diffraction. The DC transport behaviour as a function of $T$ was studied by the standard four-probe method. Thin Au wires attached to the film surface by In solder were used as leads for electrical characterization. These provided very-low-resistance ohmic contacts to the film surface. In the transition region, data points were taken at 0.2 K intervals to facilitate accurate analysis. The normal-state conductivity $\sigma_{\text{calc}}$ for $T < 110$ K was determined by extrapolation of the regression-fitted data in the range 110 K < $T$ < 180 K.

3. Results

The microstructure of the two coevaporated films (C1 and C2) were completely different although they were deposited and annealed under apparently identical conditions.
Film C1 has long cylindrical grains of about 0.25 µm diameter. The grains are highly oriented with their a–b plane along the film plane. Film C2, however, has a basket-weave-type grain morphology with an aspect ratio of about 16 in the film plane. The x-ray diffraction spectrum shows that the film has both c-axis- and a–b-axis-aligned grains along the film normal. The a–b-axis-aligned grains, however, were restricted to the top surface of the film [8]. The laser-ablated film (L) also shows a highly oriented cylindrical grain morphology similar to that of film C1. The film has a mirror-like smooth surface morphology, indicating that the surface roughness is much less than those of the coevaporated films.

![Resistivity vs Temperature](image)

**Figure 1.** The variation in the resistivities $\rho$ of the three films with temperature $T$.

The variation in the resistivities $\rho$ with temperature of the three films C1, C2 and L shows a sharp transition into the superconducting state (figure 1). The transition width, defined as the width at half-maximum of the temperature-derivative curve, is about 0.4 K for all the films. The parameters that are important in any systematic study of $\Delta\sigma$ are

(i) determination of the mean-field transition temperature $T_{c}^{\text{mf}}$ and
(ii) determination of the background or normal-state transport contribution to the overall conductivity.

It has been shown that the inflection temperature in the $\rho-T$ curve can be
approximated as the mean-field transition temperature \([9, 10]\). This criterion was used in the determination of \(T^{mf}_c\) for the films and is given in table 1.

<table>
<thead>
<tr>
<th>Sample</th>
<th>(T_c(0)) (K)</th>
<th>(T^{mf}_c) (K)</th>
<th>(\Delta T_c(0)) (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>C1</td>
<td>91.1</td>
<td>91.5</td>
<td>0.4</td>
</tr>
<tr>
<td>C2</td>
<td>90.5</td>
<td>91.4</td>
<td>0.5</td>
</tr>
<tr>
<td>L</td>
<td>90.2</td>
<td>90.5</td>
<td>0.3</td>
</tr>
</tbody>
</table>

4. Discussion

The low-temperature superconductors are of strong-coupling BCS type and their normal-state behaviour can be estimated using a linear temperature dependence for \(\rho\) based on the conventional electron scattering mechanisms. However, the scattering mechanisms in the normal state of the oxide superconductors are not clearly known. Both the Fermi-liquid-based models which predict a linear temperature dependence and the non-Fermi-liquid-based models are currently used to fit the normal-state transport behaviour [11]. According to the non-Fermi-liquid-based RVB model, the charge carriers are assumed to be confined to the Cu-O a-b planes of the crystal, thus leading to metallic conduction behaviour along the planes and phonon-activated hopping conduction in between the planes. The overall resistivity \(\rho(T)\) in such an hypothesis is given by an expression of the form

\[
\rho(T) = aT^{-1} + bT
\]

where \(a\) and \(b\) are temperature-independent constants. In the present analysis, the \(\rho-T\) data of all the films were fitted to both the linear temperature dependence of the type \(\rho(T) = \rho(0) + bT\) and the RVB dependence, equation (2), using the least-squares regression-fitting routine in the range 110 K < \(T\) < 180 K. It was found that the best fit to film C1 was the linear relation while that for films C2 and L was the RVB-type relation. However, only the linear coefficient \(b\) of the two films C2 and L is in reasonable agreement with that predicted by the RVB model. The values of \(a\) in equation (2), 442.1 and 925.8 \(\mu\Omega\) cm K, are orders of magnitude lower than the predicted values. The linear temperature coefficients \(b\) for the three films are 0.186 \(\mu\Omega\) cm K\(^{-1}\), 0.294 \(\mu\Omega\) cm K\(^{-1}\) and 1.584 \(\mu\Omega\) cm K\(^{-1}\), respectively. These values are well within the average values observed for single crystals [2, 3] and indicate the phase purity of the films. Using the simple Drude relation for metallic conduction given by \(\rho(T) = (3\pi\hbar/2)/e^2k_F^2l\) where \(l\) is the quasi-particle mean free path, \(e\) the electron charge, \(\hbar\) the Planck constant and \(k_F \approx 4.46 \times 10^7\) cm\(^{-1}\) [12] the Fermi wavevector, the 'metallic parameter' \(k_F/l\) can be estimated for the three films. These were found to be 17, 7 and 14 for films C1, C2 and L, respectively, at 120 K, indicating that all the three films are very much on the metallic side of the Ioffe–Regel limit. This clearly shows that the microscopic conduction mechanism in these materials above \(T_c\) is not completely understood, although a mathematical fit
to the RvB model can be obtained. Recently, on the basis of mid-infrared phonon spectroscopy [13] and transport [14] studies on polycrystalline pellets it has been reported that the contribution from fluctuations persists up to temperatures as high as $2T_c$. This corresponds to the 'fluctuation onset' temperature, indicating that the lifetime of the superconducting fluctuations is finite and large even at $2T_c$, for which there is no direct experimental evidence at present.

The excess conductivity $\Delta \sigma(T) = \sigma_{exp}(T) - \sigma_{calc}(T)$ determined using the relation $\rho(T) = \rho(0) + bT$ for film C1 and equation (2) for films C2 and L was found to diverge sharply as $T$ approaches $T_c^{mf}$. This is in qualitative agreement with the conventional theory which predicts a divergence of the magnitude of the order parameter fluctuations at $T$ close to $T_c^{mf}$. The critical temperature region $t$ in which the TDGL theory is not applicable can be estimated using typical values for YBa$_2$Cu$_3$O$_7$; $T_c^{mf} = 91$ K, the zero-temperature upper critical field $H_{c2}(0) = 674$ T and the GL parameter $K = 200$ [15], and therefore $t$ is found to be about $2 \times 10^{-2}$. For $t \geq 2 \times 10^{-2}$, $\Delta \sigma(T)$ can in principle be determined using equation (1) (power-law dependence of $\Delta \sigma$ on $t$). Although the rate of decay of the fluctuating superconducting pairs is explicitly considered in obtaining equation (1), their effect on the quasi-particle conductivity is not considered. An additional term has been proposed to equation (1) by Maki and Thompson (as quoted by Skocpol and Tinkham [16]) to account for the effect of fluctuations on the quasi-particle conductivity and it was found to be four times equation (1) in the case of 3D conduction and $(e^2/8\hbar d)(t-\delta)^{-1} \ln(t/\delta)^{-1}$ for 2D conduction, where $\delta$ is the pair-breaking parameter and $d$ the film thickness. The criterion for 2D conduction is $d/\xi(T) \ll 1$ where $\xi(T)$ is the superconducting coherence length. In the present case, even $d/\xi(0)$ for all the three films is much greater than unity and hence 2D conduction can be completely ruled out. The addition of an extra term to equation (1) changes only the magnitude of $\Delta \sigma(T)$, leaving the power-law temperature dependence intact. In the present work, however, $\Delta \sigma(T)$ for all the three films determined from the experimental data does not show a power-law dependence on $t$ as predicted in the range $9 \times 10^{-4} < t < 4 \times 10^{-1}$; this can be clearly seen in figure 2. It has a continuously changing curvature which has been observed earlier. However, the previous reports have inferred changes in the dimensionality of electrical transport on the basis of linear fits to small portions of the curve [2].

The above method of analysis relies on the accurate determination of $T_c^{mf}$. In the case of oxide superconductors, the fluctuation effects on the conductivity are spread over a large temperature range compared with the conventional superconductors because of their extremely short coherence length $\xi$ and the high value of $T_c(0)$. Hence the accurate determination of $T_c^{mf}$ is difficult. An alternative method of analysing the fluctuation effects which does not depend on $T_c^{mf}$ has been used in the case of TI–Ba–Ca–Cu–O thin films and single crystals [17, 18]. According to this method, equation (1) can be rewritten as

$$[\Delta \sigma(T)]^{-1/\eta} = D^{-1/\eta}[(T - T_c^{mf})/T_c^{mf}] \quad (3)$$

where the constant $D$ is given by $e^2/32\hbar \xi(0)$ for 3D conduction and $e^2/16\hbar d$ for 2D conduction. Differentiating and rearranging equation (3) gives

$$\ln[-d(\Delta \sigma)/dT] = \ln(D^{-1/\eta}/T_c) + (1 + 1/\eta)\ln(\Delta \sigma). \quad (4)$$

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The dimensionality $\eta$ can be deduced from the slope of the $\ln[-d(\Delta \sigma)/dT]$ versus $\ln(\Delta \sigma)$ plot and using equation (4). Figure 3 shows $\Delta \sigma$ plotted according to this modified scheme. It can be clearly seen that even this alternative methodology which is independent of $T_c^{mf}$ does not give conclusive evidence for the dimensionality of conduction in these films. Even according to this modified scheme of analysis the data exhibit a continuous curvature in the whole range and the dimensionality can be inferred only by fitting small portions of the excess conductivity. The recent electrical transport, mid-infrared phonon spectrum and heat capacity studies have clearly shown that the ‘onset’ temperature for fluctuations can be as high as about $2T_c$. The onset of fluctuations in the electrical transport behaviour has been attributed to the quasi-2D Maki-Thompson correction factor which has a logarithmic temperature dependence [3, 14]. The $\Delta \sigma$-values in the present work, however, could not be fitted satisfactorily to a logarithmic temperature dependence. The $\Delta \sigma(T)$ data are replotted as shown in figure 4 and it can be clearly seen that $\Delta \sigma(T)$ has an exponential dependence on $t$: $\Delta \sigma(T) \propto \exp(t^{-\alpha})$ where $\alpha$ is the slope in the range $9 \times 10^{-4} < t < 10^{-1}$ for all the three films. This clearly illustrates two important points.

(i) The TDGL theory underestimates the critical temperature region by at least an order of magnitude.

(ii) The mean-field approximations are not valid in the case of YBa$_2$Cu$_3$O$_{7-z}$.

The underestimation of the critical region has been attributed to the large contribution of the higher-order fluctuation corrections [19]. In the critical region, $\Delta \sigma$ is predicted to diverge as $t$ goes to 0 with a temperature dependence similar to that in the mean-field region but with an exponent different from $\eta$ based on the 3D $XY$ model [20]. The results of the present work, however, cannot be understood even according to these models.
5. Conclusions

The macroscopic and microscopic properties of the oxide materials in their superconducting state are being extensively studied. Many models have already been proposed to explain these properties. However, the normal-state behaviour remains the least studied to date. The only phenomenological model that has been proposed to explain the normal-state electron transport behaviour is the RVB model. The results of the present work indicate that it is insufficient to explain the transport behaviour above $T_c$. The linear and hopping coefficients obtained for the two films which obey the RVB expression for conductivity are much lower than the values predicted by the model.

The excess conductivity in the mean-field region of the three films studied does not obey the temperature dependence predicted by the TDGL theory. Even though such a behaviour has been observed before, the results are still fitted to the TDGL theory and the dimensionality of the electrical transport determined. However, we find that the excess conductivity is better represented by an exponential relation and that there is no model at present, macroscopic or microscopic, which can explain this type of behaviour. Hence the dimensionality of electrical transport is still inconclusive. The onset temperature for fluctuations observed in the present work, $t \approx 0.1$, agrees with that observed by Regan et al [4], indicating that the length of the critical region is larger than that predicted by the theory. However, the functional dependence on temperature is found to be different.

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Ellipsometric study of ambient-produced overlayer growth rate on YBa$_2$Cu$_3$O$_{7-x}$ films

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An ellipsometric study of ambient-reaction-produced BaCO$_3$ overlayer growth on laser-ablated YBa$_2$Cu$_3$O$_{7-x}$ is presented as a function of time. The effects of the anisotropy of YBa$_2$Cu$_3$O$_{7-x}$ on the ellipsometric data inversion process are discussed, and it is concluded that with certain restrictions on the data acquisition method, the anisotropic substrate can be adequately modeled by its isotropic pseudodielectric function for the purpose of overlayer thickness estimation. It is found that after an initial period of rapid growth attributed to the chemical reaction of the exposed surface bonds, the BaCO$_3$ overlayer growth is linear at 1–2 Å per day. This slow growth rate is attributed to the complexity of the BaCO$_3$ forming reaction, together with the need for ambient reactants to diffuse through the overlayer.

I. INTRODUCTION

Previously,$^1$ we have reported results of ellipsometric measurements of the pseudodielectric function of YBa$_2$Cu$_3$O$_{7-x}$ (YBCO) prepared by laser ablation and co-evaporation. We also reported observing growth of a transparent overlayer on the laser-ablated films. This overlayer growth has been observed by other experimenters$^2$ and has been determined to be BaCO$_3$ resulting from interaction between YBCO and CO$_2$ in humid air,$^3$ a conclusion with which we concurred. In this article we report systematic ellipsometric measurements of the growth rate of this overlayer on laser-ablated films exposed to air. We discuss the effects of the anisotropy of the YBCO substrate on the ellipsometric inversion process and show that by fixing certain ellipsometer settings the effects of the anisotropy can be minimized. We further show that under these restrictions the YBCO substrate can be approximated by its isotropic pseudodielectric function for the purpose of estimating the transparent overlayer thickness. Finally, we present the results of the overlayer growth time dependence measurements and discuss the results in light of the chemical mechanism which is believed to create the overlayer.

II. EXPERIMENT

Samples were prepared by laser ablation$^1$ using an excimer laser operating at 248 nm, energy density of 1.5 J/cm$^2$/pulse, with 4 pulses per second. The target was a sintered 25-mm-diam YBCO pellet located 8 cm from the sample at 45° to the laser beam. The beam was rastered up and down 1 cm over the target using an external lens on a translator. The films were deposited on strontium titanate (SrTiO$_3$), zirconium dioxide (ZrO$_2$), and lanthanum aluminate (LaAlO$_3$) substrates, which were mounted on a stainless-steel plate heated to 775 °C. The oxygen pressure was 170 mTorr throughout the deposition. X-ray diffraction showed the films to be c-axis aligned. Comparison$^1$ of our measured pseudodielectric functions with published data$^4$ also indicated our films closely approximated c-axis-aligned YBCO single-crystal material. Critical temperatures for the films were about 86 K. Film thicknesses averaged about 3000 Å.

The rotating analyzer spectroscopic ellipsometer system$^5$ reflects monochromatic linearly polarized light off the sample and measures the complex reflection ratio $\rho$:

$$
\rho = \frac{E_{p,r}}{E_{s,r}} = \left( \frac{E_{p,l}}{E_{s,l}} \right) \left( \frac{E_{s,l}}{E_{p,l}} \right) \tan(\theta),
$$

where $E_{p,r}$ and $E_{s,r}$ are the parallel and perpendicular components (with respect to the plane of incidence) of the reflected electric field intensity, $E_{p,l}$ and $E_{s,l}$ are the corresponding quantities for the incident light, and $\theta$ is the incident light polarization azimuth, i.e., $\tan(\theta) = E_{s,l}/E_{p,l}$. The rotating analyzer ellipsometer actually measures the $E_{p,r}/E_{s,r}$ ratio, while the $E_{s,l}/E_{p,l}$ ratio is determined by a fixed polarizer azimuth $\theta$. Two films, identified here as samples A and B, both deposited on strontium titanate, were selected for systematic monitoring of overlayer growth. These samples were cleaned with a bromine etch (1% Br/ethanol solution for 30 s followed by ethanol and blow drying)$^6$ to remove the overlayer, and were measured less than 10 min after cleaning, and periodically thereafter. Both samples were left mounted throughout the growth monitoring period to maximize precision. The samples were monitored for a period of 4–10 days after cleaning, and were exposed to the air throughout the monitoring period. Each sample was etched two different times to determine repeatability, giving four etches in all. Additionally, sample A was mechanically cleaned and measured periodically over a period of 106 days to examine long-term overlayer growth. Here the sample was not left mounted continuously but rather mounted periodically for measurements; hence the precision is poorer for this long-term monitoring. Between measurements, the sample was left exposed to air. Overlayer growth measurements were taken at a fixed angle of incidence: 65° for the first etch of

each sample and 70° for the second etch and also for the long-term monitoring of sample A; the wavelength range varied slightly but was always within the range 3200–8000 Å (1.55–3.87 eV). The polarizer azimuth θ was held constant at 24° for the first etches and also for the long-term monitoring of sample A; 20° was used for the second etch of each sample. These polarizer values have been shown to provide maximum precision, i.e., |ρ| = tan(θ).  

III. RESULTS

Figure 1 shows ⟨ε⟩, the real part of the pseudodielectric function, for several representative measurements taken before and after the first etch of sample A. The pseudodielectric function is the apparent dielectric function of the sample, i.e., the dielectric function of an equivalent isotropic bulk material calculated using an isotropic two-phase (ambient/substrate) model.  

The pseudodielectric function ⟨ε⟩ is obtained directly from the ellipsometrically measured complex reflectance ratio ρ, using the formula

\[ ⟨ε⟩ = ε_a \sin^2(ϕ) + \sin^2(ϕ)\tan^2(ϕ) \left[ \frac{1 - ρ^2}{1 + ρ^2} \right] \]  

In the above equation ε_a is the dielectric function of the ambient (ε_a = 1 for air), ϕ is the experimental angle of incidence, and ρ is the ellipsometrically measured quantity defined previously. For an ideal two-phase system, ⟨ε⟩ = ε_p, the substrate dielectric function. However, (2) defines the pseudodielectric function ⟨ε⟩ for all cases. The lowest curve in Fig. 1 is the measurement taken prior to the bromine etch. The highest curve is the measurement taken immediately after the etch. The curves in between are measurements taken at later times. The magnitude of ⟨ε⟩ decreases with increasing time. The measured quantity ⟨ε⟩ is expected to be a continuous function of overlayer thickness, and computer simulation using an isotropic substrate whose pseudodielectric function was similar to our measurement ⟨ε⟩ (Ref. 6) showed that the magnitude of the real part of the pseudodielectric function ⟨ε⟩ in our range of measurement decreased with increasing overlayer thickness, as shown in Fig. 2. This is in accordance with our measurements: The large increase in ⟨ε⟩ magnitude immediately after etching indicates removal of the overlayer, and the steady decrease in magnitude as time increases indicates overlayer growth. Similar results are seen for the other growth monitoring measurements. Figure 3 shows the same information for the second etch of sample B in a different form. Here the real part of the pseudorefRACTIVE index ⟨n⟩ (⟨ε⟩ = ⟨n⟩^2) at incident light wavelength of 4900 Å is plotted as a function of time. Again, a steady decrease in the magnitude of the real part with increasing time is seen. This effect of a transparent overlayer on the real part of ⟨n⟩ was also verified by computer simulation. Both the actual measurement of ⟨ε⟩ and the computer simulations of ⟨ε⟩ show that the effect of the overlayer is much more pronounced at higher photon energies (lower wavelengths). This is because the low-energy light penetrates deeper into the substrate, making it less sensitive to the overlayer.

IV. DATA ANALYSIS AND DISCUSSION

From the pseudodielectric function of single-crystal YBCO (Ref. 6) we estimate the light penetration depth in the range of measurement to be under 750 Å, making the
YBCO film the effective substrate for ellipsometric purposes. To obtain estimates of the overlayer thicknesses, it is necessary to invert the ellipsometric data. Because of the mathematical complexity of this inversion process, a least-squares fit is usually performed.10 A model of the system must be formulated, and appropriate model parameters optimized in the least-squares sense with respect to the measurement. Such a model typically consists of a layered structure atop an optically thick substrate. Abrupt interfaces are assumed, and layers are assumed to be isotropic and homogeneous with regard to thickness and optical properties.11 For overlayer measurements, the pseudodielectric function of the specific substrate to be studied is typically measured prior to overlayer deposition after sufficient cleaning to approximate the two-phase model. The overlayer is then introduced and the sample remeasured and analyzed with a three-phase (ambient/overlayer/substrate) model, using the pseudodielectric function of the initial uncontaminated surface measurement to model the substrate optical properties. This process provides a built-in correction for imperfections in the substrate which would not be accounted for by the use of standard reference data. Additionally, if the sample is left mounted on the ellipsometer between initial measurement of the substrate pseudodielectric function and subsequent measurement of the three-phase system, as was done in this study, effects of substrate inhomogeneity are also minimized by guaranteeing that the optical constants used to model the substrate are optimum for the specific location at which overlayer measurements are being taken.

In the present case, the above procedure is complicated by the fact that YBCO is a biaxially anisotropic material.12 The pseudodielectric function is calculated assuming an isotropic two-phase system, and thus it cannot completely describe the optical properties of the anisotropic substrate, which should be described by a dielectric tensor.12 To investigate the possible effects of this anisotropic substrate on the measurement of a transparent overlayer, we took two approaches: First, we performed computer simulations of untwinned single-crystal YBCO to determine which system parameters are affected by the anisotropy and to what degree. This provided information on how best to set up the overlayer measurement to minimize potential inaccuracies caused by the anisotropy, as well as providing bounds on the anisotropy-induced error. Second, we performed experimental measurements to identify to what degree the anisotropy effects predicted by computer simulation for untwinned single-crystal YBCO were actually seen in the laser-ablated YBCO films. These films are not single crystals but rather consist of microscopic grains of c-axis-oriented YBCO crystals with the a and b crystal directions aligned with the strontium titanate substrate crystal directions.2,13 There will be a high degree of twinning in the a-b plane.2,13 We expect this type of crystal structure to reduce the observable effects of the anisotropy.

The computer simulations of ellipsometric measurements of untwinned single-crystal YBCO were based upon the biaxial substrate model developed by Graves.11,13 This model calculates the complex amplitude reflection coefficients for a biaxially anisotropic substrate oriented such that one crystal axis is perpendicular to the sample surface while the second crystal axis is perpendicular to the plane of incidence of the light. In the present case, the YBCO films are predominantly c-axis aligned, so that the c axis is perpendicular to the sample surface as required by the Graves model. The dielectric tensor components of YBCO were taken from Kircher et al.12 Simulations were done using the c axis perpendicular to the interface and either the b axis perpendicular to the plane of incidence (abc orientation) or the a axis perpendicular to the plane of incidence (bac orientation). Physically this corresponds to measurement of an untwinned single crystal of YBCO, for which the maximum observable anisotropy effect would be expected. Comparison of the pseudodielectric function of abc-oriented simulations with the pseudodielectric function of bac-oriented simulations shows the effect of a 90° rotation on the measurement of such a single crystal. We performed these simulations at an angle of incidence of 65°, and found that the difference between the abc-oriented crystal pseudodielectric function and the bac-oriented crystal pseudodielectric function is enormous, with differences between the real and imaginary parts of (ε) of the two orientations exceeding the absolute magnitude of these quantities. For example, at the wavelength 5500 Å, (εr) = 3 for the abc orientation, while (εr) = 1 for the bac orientation. Additionally, the shape of the two spectra differed significantly. In contrast, our measurements of laser-ablated YBCO films as a function of sample azimuth showed variation in (εr) and (εi) of less than 0.3 all cases, and the shape of the spectra measured at different sample azimuths was very similar. The dependence of the ellipsometric measurement on sample azimuth has been reduced significantly by the complex crystal structure of the laser-ablated films, but it is still detectable, as shown by these measurements.

We next simulated the pseudodielectric function of untwinned single-crystal YBCO with no overlayer at various angles of incidence. Our simulations showed that the pseudodielectric function is a strong function of the ellipsometer angle of incidence for both the abc orientation and the bac orientation, with variation in spectral magnitudes greater than 15% for incident angle variation from 65° to 75°. The variation of the pseudodielectric function for each orientation was in opposition: the real part of (n) increased with increasing angle of incidence for the abc orientation, whereas it increased with increasing angle of incidence for the bac orientation. For comparison, we measured numerous films at various angles of incidence. The measured pseudodielectric function was found to vary by 5% or less. Again, the effect of the anisotropy has been greatly reduced by the complex film structure, but has not been completely eliminated.

In our third simulation, we determined bounds on the error that can be expected in using an isotropic three-phase model to analyze a system with an anisotropic substrate. Using the anisotropic model, we simulated ellipsometric data for various overlayer thicknesses (overlayer n = 1.55 k = 0) at an angle of incidence of 70°. This generated data
was then inverted using the isotropic three-phase model to obtain the overlayer thickness, using the simulated pseudodielectric function of the anisotropic substrate with no overlayer as the effective isotropic substrate. Simulation results are given in Fig. 4. The reference line in this graph is the ideal result, i.e., the overlayer thickness determined by the isotropic model exactly equals the overlayer thickness simulated on the anisotropic substrate. The absolute error is 20% or less, and the calculated thickness is directly proportional to the actual thickness. Thus, use of the isotropic model in this case may result in some error in the absolute growth rate, but the shape of the growth curve will be correct. As with the angle-of-incidence variation, the effects of the two orientations abc and bac oppose each other, with the abc-oriented crystal resulting in an underestimated thickness while the bac-oriented crystal results in an overestimate. In view of our previous results showing significant reduction in the observed effect of YBCO anisotropy in the laser-ablated films, the boundaries shown in Fig. 4 are expected to greatly overestimate the actual overlayer measurement error.

One potential effect of substrate anisotropy on ellipsometric measurements that cannot be studied using the Graves model is the effect of off-diagonal components of the reflectance matrix which result when the crystallographic axes are not aligned with the optical axes as required by Graves model. In general, the relationship between the incidence electric-field vector and the reflected electric-field vector is given by

\[
\begin{bmatrix}
E_{rp}' \\
E_{rs}'
\end{bmatrix} =
\begin{bmatrix}
R_{pp} & R_{ps} \\
R_{sp} & R_{ss}
\end{bmatrix}
\begin{bmatrix}
E_{pi} \\
E_{si}
\end{bmatrix}
\]  

(3)

Equation (3) states that the reflected complex amplitudes are related to the incident complex amplitudes by a 2x2 reflection matrix. This matrix is a property of the sample and is a function only of wavelength and angle of incidence. For either an isotropic system or a biaxially anisotropic system with the axial alignment specified for Graves model \(R_{ps}=R_{sp}=0\) and the ellipsometrically measured ratio \(\rho\) reduces to \(\rho = R_{pp}/R_{ss}^{1/11}\). Thus, \(\rho\) is a function only of the reflection matrix, which is a property of the sample. In the case of a biaxially anisotropic system in which the optical axes and crystallographic axes do not coincide, \(R_{ps}\) and \(R_{sp}\) are not generally zero. The measured ratio \(\rho\) can be written as

\[
\rho = \frac{E_{rp}}{E_{rs}} = \frac{R_{pp} + R_{ps} \tan(\theta)}{R_{sp} + R_{ss} \tan(\theta)} \tan(\theta)
\]  

(4)

The ellipsometric measurement in this case is a function of both the reflectance matrix and the polarizer azimuth \(\theta\). We measured the effect of the polarizer azimuth setting both on a laser-ablated YBCO film and also on an isotropic reference sample. The reference sample was an amorphous carbon film on silicon, similar to samples described in Ref. 7. The film was nearly transparent \((k < 0.13)\) with thickness \(\sim 1950\) Å. For such a sample the amplitude and phase of \(\rho\) oscillates slowly (one complete cycle in our spectral range), so that we could locate spectral regions where the measured \(\rho\) of the YBCO film could be compared with measured \(\rho\) values of similar magnitude and phase for an isotropic system. The polarizer azimuth was varied between 20° and 70°. In this range, the variations of \(\rho\) for the isotropic sample are within the experimental error. For the YBCO film the variations in \((\epsilon_1)\) and \((\epsilon_2)\) are less than 8% of the amplitude between polarizer values of 20° and 70°. Between 20° and 45° the changes are less than 4%. Again, a small but observable effect of the anisotropy is seen in the laser-ablated film.

Based upon the above results, we used the measurement and analysis procedure outlined previously for isotropic systems, with the additional constraints of using a fixed angle of incidence and a fixed polarizer azimuth, so as to avoid any measurement variations not directly attributable to surface changes. Also, since each sample was left mounted throughout the overlayer growth measurement, the sample azimuth remained unchanged. The overlayer was modeled as a transparent dielectric material with refractive index of 1.55,^{1} and the YBCO substrate was modeled by the pseudodielectric function measured immediately after etching. The resultant overlayer thickness
TABLE I. Results of linear regression analysis applied to growth monitoring results analyzed by an isotropic three-phase model. Only measurements taken after 12 h or longer were included in the fit. \( R \) is the correlation coefficient; \( R = 1 \) is a perfect fit. \( m \) denotes mechanically cleaned.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Etch</th>
<th>Hours</th>
<th>Rate ( \times 10^{-4} )</th>
<th>Intercept ( \times 10^{-4} )</th>
<th>( R )</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>1</td>
<td>266</td>
<td>1.62</td>
<td>5.03</td>
<td>0.983</td>
</tr>
<tr>
<td>A</td>
<td>2</td>
<td>95</td>
<td>2.12</td>
<td>6.62</td>
<td>0.983</td>
</tr>
<tr>
<td>A</td>
<td>m</td>
<td>2577</td>
<td>0.95</td>
<td>2.29</td>
<td>0.981</td>
</tr>
<tr>
<td>B</td>
<td>1</td>
<td>214</td>
<td>2.01</td>
<td>1.80</td>
<td>0.985</td>
</tr>
<tr>
<td>B</td>
<td>2</td>
<td>192</td>
<td>0.87</td>
<td>6.42</td>
<td>0.937</td>
</tr>
</tbody>
</table>

*The rate in \( \AA/\text{day} \).

*The intercept in \( \AA \).

versus time plot for the first etch of sample A is given in Fig. 5. Two distinct regions are seen. For about the first 5 h the overlayer grows rapidly. When the overlayer reaches \( \sim 5 \AA \) the growth slows and becomes linear, with a growth rate of 1.62 \( \AA \) per day, as determined by linear regression. Results for the other three etches were similar in shape. The four etch results plus the long-term monitoring of sample A after mechanical cleaning were each fitted to a linear model for overlayer measurements taken after 12 h, i.e., in the linear region. The results are shown in Table I. In this table, the intercept is the \( y \) intercept of the regression line; this gives an estimate of the thickness reached in the initial rapid growth region. The initial growth period stops at about 2–6 \( \AA \), i.e., about one monolayer. In the linear region, the growth rate is in the range 1–2 \( \AA \) per day, which is below one monolayer per day.

The type of growth curve observed here on YBCO is different from the logarithmic curve typically observed in the oxidation of semiconductors, such as the oxidation rate of silicon and gallium arsenide measured by Lukes. The type of growth curve observed here on YBCO is different from the logarithmic curve typically observed in the oxidation of semiconductors, such as the oxidation rate of silicon and gallium arsenide measured by Lukes. In the case of oxidation, the ambient reactant \( O_2 \) is plentiful, and the overlayer growth rate is controlled by the diffusion rate of oxygen through the growing oxide overlayer. In the present case, the YBCO overlayer is believed to be produced by the following chemical reactions:

\[
3\text{H}_2\text{O} + 2\text{YBa}_2\text{Cu}_3\text{O}_7 \rightarrow \text{Y}_2\text{BaCuO}_3 + 3\text{Ba(OH)}_2 + 5\text{CuO} + 0.5\text{O}_2, \tag{5}
\]

Balanced equation for the growth of YBCO thin films due to exposure to air. After formation of an initial monolayer, the growth proceeds linearly and rather slowly, e.g., 1–2 \( \AA \) per day. This information should be useful in appraising the effect of air exposure on various sample processing steps, such as making electrical contacts. In the process, we considered the effects of substrate anisotropy on overlayer estimation and have presented a method of estimating overlayer growth on an anisotropic substrate.

**ACKNOWLEDGMENTS**

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Magnetic flux relaxation in YBa$_2$Cu$_3$O$_{7-x}$ thin film: thermal or athermal

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Abstract

The magnetic flux relaxation behavior of YBa$_2$Cu$_3$O$_{7-x}$ thin film on LaAlO$_3$ for $H || c$ was studied in the range 4.2–40 K and 0.2–1.0 T. Both the normalized flux relaxation rate $S$ and the flux pinning energy $U_0$ exhibit a weak field dependence at low temperatures ($T < 20$ K). Within this regime $S$ and $U_0$ are observed to increase continuously from $1.0 \times 10^{-9}$ to $2.0 \times 10^{-7}$ and 45 to 130 meV respectively, as the temperature $T$ increases from 4.2 to 20 K. While $S$ is observed to decrease in proportion to $kT$ for $T < 20$ K, it does not extrapolate to zero at $T = 0$, which is in contradiction to the thermally activated flux creep and vortex glass models. This behavior is discussed in terms of the athermal quantum tunneling of flux lines. The magnetic field dependence of $U_0$, however, is not completely understood.

1. Introduction

In type II superconductors the pinning of magnetic flux lines is responsible for the lack of dissipation during the flow of high current densities. The pinning is caused by various types of defects, i.e. grain boundaries, twins, point defects and inhomogeneities. The observation of a high degree of mobility of these flux lines in the oxide superconductors [1–3] has stimulated many theoretical studies and has led to the proposal of several models. According to the conventional thermal flux motion model [4, 5] the magnetization relaxes logarithmically with time $t$ for $t < t_c$, where $t_c$ is a crossover time given by $t_c = \tau_{\text{hopping}} \exp[U/kT]$. $\tau_{\text{hopping}}$ is the flux line hopping time ($10^{-6}$–$10^{-12}$ s), $U$ is the net flux pinning energy, $k$ is the Boltzmann constant and $T$ is temperature. At $t > t_c$, or for high $T$, the motion of flux lines attains a steady state and the magnetization relaxes exponentially with $t$ [6]. However, the observation of logarithmic decay even at large values of $T$ and the non-linear behavior of the relaxation rate has led to many alternative models for the nature of the pinning energy $U$ [7–9].

An alternative description of dissipation in high temperature superconductors is the vortex glass model [10, 11]. In this model there is a truly superconducting state in the presence of high magnetic fields below the glass transition temperature. Within this regime the sample voltage is predicted to vanish exponentially with decreasing current. Recently, the vortex glass model has been used to explain the apparent temperature independent value of $S = 0.02–0.035$ reported by many researchers [12].

In the present work, the relaxation of screening-current-induced magnetization in a YBa$_2$Cu$_3$O$_{7-x}$ thin film has been studied as a function of temperature $T$ and external field $H$. The magnetization is found to relax logarithmically up to $10^6$ s for $T$ as high as 0.45 $T_c$, where $T_c$ is the superconducting transition temperature. $S$ appears to saturate with increasing temperatures for $T > 20$ K. This observation is consistent with the predictions of the vortex glass model; however the $[\ln(t)]^{-1}$ time dependent relaxation appropriate to the model is not observed. For $T \leq 20$ K, $S$ is observed to decrease linearly with decreasing $T$ but does not extrapolate to zero at $T = 0$. The linear dependence of $S$ on $T$ in the low-$T$ region is consistent with both the thermally activated creep and vortex glass models. The finite value of $S$ at $T = 0$ obtained by extrapolation cannot be explained by either model and is discussed in terms of "quantum tunneling" or the "athermal flux motion" model [13]. We also observe $U_0$ to decrease with increasing $H$ for all temperatures and fields used.
although the $1/H$ dependence suggested by Yeshurun and Malozemoff [1] is not observed.

2. Experimental methods

The YBa$_2$Cu$_3$O$_{7-x}$ thin film, approximately 0.3 µm thick, was deposited by the pulsed laser ablation technique onto a heated (100) LaAlO$_3$ substrate. The film texture was determined by the standard $\theta-2\theta$ scan and rocking curve, and shows that the grains are preferentially aligned with their c-axis along the plane normal. The film has a smooth surface and the average grain size, determined by scanning electron microscopy, is approximately 0.25 µm. The superconducting transition temperature $T_c(0)$ determined by the standard four probe d.c. technique is 88.5 K with a transition width of ca. 1.0 K.

The magnetization and magnetic flux relaxation was studied using a commercial SQUID magnetometer. Hysteresis loops were made at various temperatures for $H \parallel c$, from which the critical current $J_c$ was determined. The values at 4.2 K and 77 K were $2.4 \times 10^7$ A cm$^{-2}$ and $1.0 \times 10^6$ A cm$^{-2}$ respectively. Such values are typical of high quality films. The data collection procedure is described in detail in ref. 3. The diamagnetic transition temperature determined from the field-cooled magnetization of 2 mT applied along the c-axis was found to be 88.5 K and is the same as that determined by the electrical transport method.

3. Results

The relaxation of the screening-current-induced magnetization at $H = 0.2$ T, 0.4 T, 1.0 T and 2.0 T applied perpendicular to the orthorhombic $ab$ plane of the crystals was studied in the temperature range $0.05 T_c < T < 0.45 T_c$. The magnetization was found to relax logarithmically with $t$ up to $10^4$ s at all the temperatures and fields studied. The relaxation rate $dM/d \ln t$ is shown in Figs. 1(a) and 1(b) as a function of $T$ and $H$ respectively. It may be observed in Fig. 1(a) that $dM/d \ln t$ exhibits a maximum at approximately 10 K. Such behavior has been observed in grain aligned powdered YBa$_2$Cu$_3$O$_{7-x}$ specimens [2] and attributed to partial flux penetration when $H < H^*$, where $H^*$ is the field at which the magnetization reaches the maximum at a given temperature. In our relaxation measurements, however, $H > 2.5H^*$ for all temperatures and fields used. We therefore believe the films are fully penetrated by the flux and that the films are in the critical state. The relaxation rate $dM/d \ln t$ normalized by the initial magnetization $M_0$ at $t_0$ eliminates the uncertainties associated with the determination of the demagnetization factor, and allows the possible determination of the pinning energy $U_0$. In analyzing the results of the present work, $t_0$ is taken to be $10^3$ s so that the relaxation is in the logarithmic regime. Figures 2(a) and 2(b) show the normalized relaxation rate $1/M_0 dM/d \ln t = S$ as functions of $T$ and $H$ respectively.

4. Discussion

In a typical relaxation measurement, the net flux pinning energy $U$ is zero at $t = 0$ and increases rapidly with $t$. The time dependence of $U$ is implicitly contained
of $T$ when $U_0 \gg kT \ln(t_0/t_{hop})$. Since $U_0$ must go to zero as $T \to T_c$, it also predicts a divergence or an upward curvature for the $S$ curve as $T$ increases. From Fig. 2(a) it can be seen that $S$ is approximately linear in $T$ for $T \leq 20 \text{K}$, and takes on a weaker temperature dependence for higher temperatures. This type of behavior has been observed before in magnetization studies on single crystals, aligned powders and thin films [1–3]. The flux pinning energy $U_0$ obtained from eqn. (2) by considering $t_{hop}$ to be typically $10^{-8}$ s is shown in Fig. 3(a). At every field $U_0$ is an increasing, convex function of temperature. The observation that $U_0$ is an increasing function of temperature rather than a decreasing function of temperature has led Hagen and Griessen [14] to propose that a distribution of $U_0$ values exists in these materials.

within the screening current $J$ which equals $J_c$ at $t = 0$. The driving force for the motion of these flux lines is a combination of flux line interaction, thermal activation and the flux line gradient (Lorentz force). In the conventional thermally activated flux motion model, $U$ is assumed to be a linear function of $J$ and to have a depth $U_0$ when $J = 0$. This leads to the classical relation [4, 5, 9] for $t \gg t_{hop}$,

$$M(t) = M(0)[1 - \{kT/U_0\} \ln(t/t_{hop})]$$

(1)

The relaxation rate normalized by the initial magnetization can be obtained from the above relation and is given as

$$1/M_0 dM/d\ln t = S = -kT/[U_0 - kT \ln(t_0/t_{hop})]$$

(2)

According to the above relation, $S$ is a linear function

Fig. 2. The relaxation rate normalized by the initial magnetization $M_0$; (a) as a function of temperature $T$; (b) as a function of external field $H$. See caption of Fig. 1 notation.

Fig. 3. The flux pinning energy $U_0$ obtained using eqn. (2) shown as a function of temperature (a) and external field (b). See caption of Fig. 1 notation.
In the vortex glass state, dissipation from the formation of vortex loops results in a magnetic relaxation of the form [12]

$$M(t) = M(0)[1 + (\mu k T/U_0) \ln(t/\tau_{\text{hop}})]^{-1/\mu}$$

(3)

where \(\mu\) is the glass exponent. For times which are short compared with \(\tau_{\text{cr}}\) and where \(\mu = 1\), eqn. (3) becomes equivalent to eqn. (1) and the resulting \(S\) is given by eqn. (2). In other words, at low temperatures the predictions of the activated flux creep and vortex glass are identical and in qualitative agreement with the data of Fig. 2(a). At times which are long compared with \(\tau_{\text{cr}}\) (or equivalently at higher temperatures) the vortex glass model predicts that \(M \propto [\ln(t)]^{-1}\) and \(S\) takes on a temperature independent value given by \(S = -[\ln(t/\tau_{\text{hop}})]\). Malozemoff and Fisher [12] argue that the nearly constant value of \(S\) reported in the literature is a consequence of the logarithmic dependence of \(S\) on the observation time. The data of Fig. 2(a) show that our values of \(S\) fall within the range of values observed by Malozemoff and Fisher, and that \(S\) tends to saturate for all fields as the temperature is increased. The latter fact is in qualitative agreement with the vortex glass model. While we have qualitative agreement with the temperature dependence predicted by the vortex glass model we do not observe the concomitant \([\ln(t)]^{-1}\) relaxation. Instead the magnetization decays as \(\ln(t)\) at all temperatures used in this study.

Recently, substantial magnetic relaxation has been reported at temperatures as low as 0.1 K in \(\text{YBa}_2\text{Cu}_3\text{O}_{7-x}\) grain aligned powder [15] and at 1.6 K in \(c\)-axis aligned thin film [16] for \(H\) applied along the \(c\)-axis. In the present work, however, 4.2 K was the lowest \(T\) at which the relaxation behavior was studied. In the low temperature limit both the thermally activated creep and the vortex glass models predict (eqn. (2)) that \(S\) vanishes as \(T \rightarrow 0\). Extrapolation of the data (Fig. 2(a)) to \(T = 0\) results in a non-zero \(S\), in contradiction to both models. This behavior has also been observed in molybdenum disulfides for \(T < 0.2 T_c\) by Mitin [13]. He has proposed that the observed relaxation results from quantum tunneling or hopping of the flux line segments across the potential barrier separating two pinning centers, and is athermal in nature. The hopping time for this process was estimated to be ca. \(10^{-12}\) s, which is comparable to \(\tau_{\text{hop}}\) used in the present analysis. This phenomenon is similar in principle to the electron transport mechanism in disordered semiconductors [17]—quantum tunneling crossing over to thermal activation as \(T\) increases and domination of the highest rate process at any given \(T\). At present there is no single model incorporating both these processes.

The magnetic field \(H\) dependence of \(U_0\) is shown in Fig. 3(b). As can be seen from this figure, the \(H\) dependence of \(U_0\) changes continuously as \(T\) is increased. From this figure we observe that \(U_0\) is weakly field dependent for \(T \lesssim 20\) K. At all temperatures however, \(U_0\) is observed to decrease with increasing field. On the other hand Xu et al. [2] observed \(U\) to increase with increasing fields for the same range of temperatures used in this experiment. Recent studies of the field dependence of \(U_0\) in grain aligned [18] and single crystal [19] \(\text{YBa}_2\text{Cu}_3\text{O}_{7-x}\) have shown \(U_0\) to increase with increasing fields at low temperatures and to decrease with increasing \(H\) for \(T \sim T_{\text{irr}}\), where \(T_{\text{irr}}\) is the irreversibility temperature. This has been attributed to the variation of pinning strength, creation of field induced pinning centers and granularity. The disparity of the various field dependencies clearly shows that \(H\) dependence of \(U_0\) is also not completely understood at present.

5. Conclusions

The temperature and magnetic field dependence of the flux pinning energy in a \(c\)-axis oriented \(\text{YBa}_2\text{Cu}_3\text{O}_{7-x}\) thin film have been investigated. The observed linear temperature dependence of \(S\) at low temperatures is consistent for both the thermally activated flux creep and the vortex glass models. The observed non-linear temperature dependence of \(S\) for \(T \geq 20\) K is in agreement with the vortex glass model, but we do not observe the expected \([\ln(t)]^{-1}\) decay as predicted in this model. The behavior in the \(T = 0\) limit, however, cannot be understood in terms of either model. At present one must resort to considering an athermal flux line tunneling mechanism for motion at \(T = 0\). It therefore appears that no single model adequately describes the temperature, time, and field dependence of the magnetic relaxation in \(\text{YBa}_2\text{Cu}_3\text{O}_{7-x}\) thin films.

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References

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BIOGRAPHIES
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Samuel A. Alterovitz received a Ph.D. degree in Solid State Physics in 1971 from Tel Aviv University, Israel. After a 2-year postdoctoral appointment at the University of Illinois, Urbana, Illinois, he joined the staff of the Physics Department at Tel Aviv University where he achieved the rank of tenured associated professor. In both places he worked on properties of superconducting materials, especially critical currents and critical fields. In 1981 he accepted a position in the Electrical Engineering Department at the University of Nebraska, Lincoln, Nebraska, as senior engineering research scientist. In 1983 he transferred to NASA Lewis Research Center where he is now a senior research scientist. He played an important role in developing new materials (e.g., InGaAs) for high-speed, low-noise, high-efficiency electronic devices. He also developed ellipsometry for novel and multilayer structures. He is now working on epitaxial lift-off technique development, materials and devices for extended temperature electronics applications, and on further applications of the ellipsometric technique. Dr. Alterovitz has authored over 120 papers in referred journals and over 110 meeting presentations and has edited three books. Dr. Alterovitz is a member of the American Physical Society, the Materials Research Society, and the American Vacuum Society.

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**Alan N. Downey** joined NASA Lewis Research Center in 1977 as a co-op student. He received his B.S.E.E. degree from Cleveland State University in 1979, and his M.S.E.E. degree from the University of Toledo in 1983. In 1979 he joined the Space Communications Division of Lewis. From 1979 to 1985, he was engaged in microwave measurements and solid-state technology research, followed by a 3-year hiatus in the Communications Projects Branch as Experiments Manager for the Applications Technology Satellites Program. Mr. Downey returned to the Solid State Technology Branch in July 1989. His current research interests include the RF characterization of novel High Electron Mobility Transistor (HEMT) structures at cryogenic temperatures, Monolithic Microwave Integrated Circuits (MMIC) applications, and micromachined passive electronic components for submillimeter wave radiometry.

**Edward J. Haugland** received his B.S. degree in Physics from the University of Minnesota, and M.S. and Ph.D. degrees in Solid State Physics from Case Western Reserve University. He joined NASA Lewis Research Center in 1980 as a member of the Solid State Technology Branch. Since that time, he has been involved with experimental research on electrical properties of III-V semiconductor materials, heterostructures, and SiC. Dr. Haugland was responsible for contracts concerning development of high-power Impact Ionization Avalanche Transit Time (IMPATT) diodes and Monolithic Microwave Integrated Circuits (MMIC) power amplifiers. Dr. Haugland is a member of the American Physical Society.
Thomas J. Kascak received a B.S.E.E. degree from Case Western Reserve University in 1959 and joined Union Carbide Corporation where he was concerned with performance and reliability aspects of dry cell and alkaline batteries. Mr. Kascak received an M.S. degree in Physics in 1965 from John Carroll University, Cleveland, Ohio. From 1966 to the present, he has been employed at the Lewis Research Center in Cleveland, Ohio. At NASA he has been involved in several work areas, starting with research on thermonic heat to electric power conversion devices. In 1973 he transferred to the Launch Vehicles Division where he had contract management responsibilities dealing with the guidance equipment for the NASA Atlas/Centaur launch vehicle systems. In 1980 he transferred to the Space Electronics Division where he has been involved in various aspects of microwave and millimeter wave solid-state devices and circuits. He had responsibilities for formulating and managing several NASA sponsored contractual efforts involving MMIC development programs. One of these efforts, a 20-GHz MMIC Transmit Module, resulted in the R&D Magazine IR-100 Award. For the last few years, he had the responsibility for the setup of the Division's in-house solid-state facilities. Recently he has managed a contractual effort involving the pulsed laser deposition of high-Tc superconducting YBCO films on sapphire substrates for use in microwave/millimeter wave applications.

Mr. Kascak has authored papers on thermionic direct energy conversion devices, 20- and 30-GHz MMIC devices, and MMIC based phased array antennas. Mr. Kascak is a member of the American Vacuum Society (AVS).

Regis F. Leonard received his Ph.D. degree in Physics from the Carnegie Institute of Technology in 1963 and came to NASA Lewis Research Center that same year. Since that time, he has completed 10 years of basic research concerning the physics of nuclear structures. For 6 years, Dr. Leonard worked toward the development of a unique Lewis facility that uses neutron radiation to treat cancer patients. For the last 11 years, he has helped develop technology in support of NASA's communications programs. This assignment includes work on the ACTS proof-of-concept (POC) technology program and, as head of the RF Systems Section, the development of an in-house communications system test capability for the ACTS POC hardware. For the last 6 years, he has served as Chief of the Solid State Technology Branch. Dr. Leonard is responsible for NASA's MMIC technology development program—an active, in-house, solid-state, research program—and a sizeable university grant program which supports basic research as applicable to solid-state electronics.
Rafael A. Mena received his B.S. degree in Electrical Engineering in 1988 from the University of Texas at El Paso, and an M.S. degree in Solid State Physics in 1990 from Arizona State University. While at Arizona State University, he made theoretical calculations on the effect of a magnetic field on the optical properties of semiconductor alloys. In 1990 he joined the Solid State Technology Branch at NASA Lewis Research Center as a full-time employee. His current interests lie in both the theoretical and experimental investigation of the electrical properties of novel semiconductor materials.

Felix A. Miranda received his B.S. degree in Physics from the University of Puerto Rico in 1983, an M.S. degree in Physics from the Rensselaer Polytechnic Institute in 1986, and a Ph.D. degree in Physics from Case Western Reserve University in 1991. He joined NASA Lewis Research Center in March 1991 as a member of the Solid State Technology Branch. Since then he has been involved with experimental research on millimeter and microwave properties of High Transition Temperature Superconducting (HTS) thin films and HTS-based passive microwave devices. Dr. Miranda is a member of the American Physical Society and the Institute of Electrical and Electronics Engineers.
Carlos R. Morrison received his B.S. degree in Physics with honors, and a minor in Mathematics from Hofstra University in 1986. While attending Hofstra, he was elected to membership in the Sigma-Pi-Sigma National Physics Honor Society, the Kappa-Mu-Epsilon National Mathematics Honor Society, and the Society of Physics Students. He received an M.S. degree in Physics from the Polytechnic Institute of New York in 1989 and, in September of that year, joined NASA Lewis Research Center where he worked briefly in Reliability and Quality Assurance. He then transferred to the Solid State Technology Branch in January 1990. In September 1992, he was awarded a U.S. patent for the “Morrison’s Temporal Device,” which is a type of headband for use in relieving headaches. Currently, Mr. Morrison is involved with plasma deposition of thin films.

George E. Ponchak received his B.E.E. from Cleveland State University in 1983 and his M.S.E.E. from Case Western Reserve University in 1987. He joined NASA Lewis Research Center in July 1983. Since joining NASA, he has been responsible for research and development of microwave/millimeter wave transmission lines and passive elements. Mr. Ponchak has developed many coplanar waveguide (CPW) circuit elements including several novel CPW to rectangular waveguide transitions, CPW pin diode switches, and CPW discontinuity equivalent circuit models. Mr. Ponchak has coauthored 22 papers on these topics. He is currently interested in the development of dielectric waveguides and micromachined waveguides for millimeter and submillimeter wave circuits. In addition, he has been responsible for the management of several MMIC development contracts. Mr. Ponchak is currently pursuing a Ph.D. in Electrical Engineering at the University of Michigan.
John J. Pouch received his Ph.D. from Wayne State University in Detroit, Michigan, in 1981. Since 1983 he has been involved in surface science and plasma processing at the NASA Lewis Research Center.

Robert R. Romanofsky received his B.S. degree in Electrical Engineering from Pennsylvania State University and his M.S. degree in Electrical Engineering from the University of Toledo. Mr. Romanofsky has been employed in the Space Electronics Division of NASA Lewis Research Center since 1983. He spent 1 year at NASA Headquarters in Washington, D.C., as the acting program manager for superconductivity and RF communications. His work has involved microwave transmission line research and device characterization and modeling. Recently, he has been investigating microwave applications of high-temperature superconductivity.
David Rosenfeld received his B.S., M.S., and Ph.D. degrees in Electrical Engineering from the Technion-Israel Institute of Technology in 1983, 1985, and 1989, respectively. In 1989 he joined Kidron Microelectronics Research Center the Technion where he researched the properties of low band-gap materials used for infrared imaging systems, focusing on the connections between the material parameters, the device properties, and the performance of the complete imaging system. Currently, Dr. Rosenfeld holds a National Research Council Fellowship and is researching the properties of SiGe heterostructures.

Samuel E. Schacham received his B.S. degree in Mathematics and Physics with honors in 1971, and an M.S. degree in Physics in 1973 from Bar Ilan University, Israel. He performed research work on nonlinear optical effects in liquid crystals at the Weitzmann Institute and Bar Ilan University. He received a Ph.D. degree in Biomedical Engineering in 1978 from Northwestern University working on applications of lasers to microendoscopy. From 1978 to 1981, he was the manager of the optic group at Fibronics, Ltd., Haifa, Israel. From there he joined the Department of Electrical Engineering at the Technion in Haifa. In 1988 he was a visiting scientist at MCNC Research, Triangle Park, North Carolina, working on optical interconnects as part of the packaging group. Presently, he is with NASA Lewis Research Center as a National Research Council Senior Research Associate. His present research interests are in the physical properties of quantum structures and narrow band-gap semiconductors. His list of publications include 54 papers in international scientific journals and referred conferences.
Ajit K. Sil received his B.S. degree from Calcutta University, India, and emigrated to the United States where he was employed by Oakwood Downriver Medical Center. He received his second B.S. degree in Electronic Engineering Technology in 1988 from Wayne State University. He joined NASA Lewis Research Center in July of 1989 as a member of the Solid State Technology Branch. Mr. Sil works with microwave integrated circuits and solid-state devices. He is currently working toward his M.S.E.E. degree at Cleveland State University.

Rainee N. Simons received his B.S. degree in Electronics and Communications Engineering from Mysore University, India, in 1972, and an M. Tech. degree in Electronics and Communications Engineering from the Indian Institute of Technology in 1974. In 1983 he received a Ph.D. degree in Electrical Engineering from the Indian Institute of Technology. He started his career in 1979 as a Senior Scientific Officer at the Indian Institute of Technology. From 1985 to the present, he has been with the Solid State Technology Branch of NASA Lewis Research Center, as a National Research Council Research Associate from 1985 to 1987, as a Case Western Reserve University Research Associate from 1987 to 1990, and as a senior research engineer for Sverdrup Technology, Inc. from 1990 to the present. At NASA, Dr. Simons’ research has included microwave and millimeter wave semiconductor devices, circuits and antennas, space terahertz technology, optical control of semiconductor devices, and superconductivity. Dr. Simons is the author of a book entitled “Optical Control of Microwave Devices.” He has received the distinguished alumni award from his alma mater and several NASA Tech Brief and Group Achievement awards. Dr. Simons is a senior member of IEEE.
Mark A. Stan received his B.S.E.E. degree in 1978 from the University of Akron. He was employed by the Allen-Bradley Company as a digital circuit design engineer until 1980 when he returned to graduate school at Case Western Reserve University to study the physics of melting in two-dimensional systems. He completed work for his M.S. degree in 1982 and Ph.D. degree in 1988. In 1987 Dr. Stan began research work at NASA Lewis Research Center in the areas of characterization and growth of high-temperature superconductors. Currently, Dr. Stan is a Resident Research Associate. He is a member of the American Physical Society, the Materials Research Society, and the Institute of Electrical and Electronic Engineers.

Stephan Stecura received his M.S. degree in Physical Chemistry in 1957 from Western Reserve University, and a Ph.D. degree in Solid-State Reaction Kinetics-Thermodynamics in 1965 from Georgetown University. From 1958 to 1965 at College Park Metallurgy Center, he studied the kinetics of crystallographic transformation and the high-temperature properties of oxides by high-temperature, x-ray diffraction techniques. He designed and built high-temperature, x-ray diffraction equipment and was invited to present the high-temperature, x-ray diffraction, arc-image furnace (capable of reaching 3000 °C in air) at the International Crystallographic Society meeting. Since 1965 he has been with NASA Lewis Research Center. Dr. Stecura's work here on heat pipes led him to determine the corrosion mechanism and the true solubilities of containment metals and alloys in alkali metals. He developed thermal barrier systems for the protection of alloy components at very high temperatures, up to 1600 °C, on air-cooled components. Currently, he is studying the properties of superconducting materials and trying to identify substrate materials for superconducting films. Dr. Stecura is recognized as an authority on the thermal barrier system technology that he developed. For his work in this field, he has received two IR-100 awards, one major Space Act award, and three major patents. He has written more than 30 original publications and is a member of the American Ceramic Society.
Susan R. Taub received her B.S. degree in Electrical Engineering Technology in 1988, and an M.S. degree in Electrical Engineering in 1990 from Temple University. In 1988 and 1989, she worked for AT&T Bell Laboratories developing PSPICE compatible models for power Metaloxide Semiconductor Field Effect Transistor (MOSFET's). She joined the Solid State Technology Branch of NASA Lewis Research Center in 1990 and is currently involved in the design and characterization of MMIC’s and the investigation of HEMT performance at cryogenic temperatures. Ms. Taub is a member of IEEE.

Joseph D. Warner received his M.S. degree in Physics from Carnegie-Mellon University in 1977. From 1977 to 1981, he performed research on magnetic phase transition at low temperature. Since that time, he has been with NASA Lewis Research Center where he characterized various insulators on GaAs and was among the first to demonstrate growth of GaAs by laser-assisted Organo-Metallic Chemical Vapor Deposition (OMCVD) at temperatures below 500 °C. Presently, he has set up a laser ablation experiment to grow high-temperature superconducting thin films. In 1989 he received a NASA Achievement Award for his part in establishing a high-temperature superconductor program at NASA Lewis. Mr. Warner has authored papers on magnetic phase transitions, electrical properties of insulation films on III-V compounds, laser-assisted growth of GaAs and AlGaAs, and properties and growth of high-temperature superconductors. Mr. Warner is a member of the American Physical Society, the American Vacuum Society, and the Materials Research Society.
Paul G. Young earned his Ph.D. in Electrical Engineering in 1993 from the University of Toledo, a M.S. in Electrical Engineering from the University of Cincinnati in 1987, and a B.S.E.E. from the University of Toledo in 1985. From 1987 to 1990, he was employed by Harris/RCA in the Solid State Division as a technical staff member. He has been active in the areas of III-V compound semiconductor process development with an emphasis on InP self-gate aligned MOSFET structures and GaAs MODFET structures. Presently, his research interests are in epitaxial liftoff MODFET devices, SiGe n-MODFET and TBT structures, cryogenic on-wafer measurement of devices, SCC MESFET devices for RF high-power applications, and high-temperature devices.
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<td>The digest is a collection of papers written by the members of the Solid State Technology Branch of NASA Lewis Research Center from June 1992-June 1993. The papers cover a range of topics relating to superconductivity, MMIC's, coplanar waveguide, and material characterization.</td>
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