Seals Flow Code Development–92

Proceedings of a workshop held at
NASA Lewis Research Center
Cleveland, Ohio
August 5–6, 1992
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A.D. Liang, NASA Lewis Research Center

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SUMMARY

A two-day workshop was held at the NASA Lewis Research Center on August 5 and 6, 1992. The intent of the workshop was to inform the technical community of the seal code development activity sponsored by NASA Lewis and to provide a forum for participants to exchange information on respective activities in seals. We thank the workshop presenters, the participants and the peer committee for their contributions.

Three codes were disseminated to the technical community for beta testing. They are the ICYL (cylindrical seal in incompressible fluids), GCYL (cylindrical seal in compressible fluids) and SPIRALG (spiral grooved gas seal) code. Close to thirty companies requested these codes at the workshop.

Several needs, shortcomings, and problem areas have been delineated from the workshop on the NASA Lewis seals contract with Mechanical Technology Incorporated. The deficiencies include: validation data sets, convection flow contributions (inlet, inertia, turbulence, body forces), surface distortions, dynamics matrices in the CFD code, computational efficiency (speed, storage, hardware), and awareness of current seal user requirements and projected needs.

The positive aspects, however, must not be overlooked. The codes are being worked into a transportable user friendly format. They are available for members of the peer committee and beta-users to apply toward their particular area of expertise. The findings from beta-testing need to be reported to enhance program effectiveness. This will be an on-going activity throughout this contract.

Workshop Chairs:

Anita D. Liang
Robert C. Hendricks
OVERVIEW

SEALS FLOW CODE DEVELOPMENT WORKSHOP

and

BRUSH SEALS SYSTEM WORKSHOP

AUGUST 5-6, 1992

NASA LEWIS RESEARCH CENTER

PROGRAM OBJECTIVE - Develop Codes for Analyzing and Designing Optimized Advanced Seals for Future Aerospace and Advanced Rocket Engine Systems
• OVERVIEW OF NASA CONTRACT NAS3-25644

• CURRENT ISSUES

• PROGRAM STATUS

PROGRAM SCOPE

• SEVEN YEAR EFFORT (NASA Contract NAS3-25644)
• PARALLEL PATHS - Scientific Code and Industrial Codes
• DEVELOPMENT OF A KNOWLEDGE-BASED SYSTEM
• TECHNOLOGY TRANSFER VIA WORKSHOPS
• CODE VALIDATION VIA PUBLISHED DATA, IN-HOUSE TEST WORK AND COOPERATIVE PROGRAMS
TEAM MEMBERS

NASA LeRC
- Julie Carlile
- Bob Hendricks
- Anita Liang
- Margaret Proctor

MTI
- Bharat Aggarwal
- Tony Artiles
- Wilbur Shapiro

CFDRC
- Mahesh Athavale
- Andrzej Przekwas
- Ashok Singhal

PROGRAM ORGANIZATION

MTI
- PROGRAM MANAGER
  - W. Shapiro

MTI PRINCIPALS
- A. Artiles
- B. Aggarwal

CFDRC
- A. Przekwas
- M. Athavale

Task I
- Cylindrical Seals Code

Task II
- Cylindrical Code Augmentation (Labyrinth, Honeycomb, Damper, Brush)

Task III
- Face, Wave, Grooved Seals

Task IV
- Tip, Contact, Non-Continuous Seals
MAJOR TECHNICAL ACTIVITIES

1. DEVELOPMENT OF ANALYTICAL CODES
2. DEVELOPMENT OF EXPERT SYSTEMS
3. INTEGRATION OF CODES AND EXPERT SYSTEMS INTO ONE SINGLE FRAMEWORK

CODE DEVELOPMENT

INDUSTRIAL CODES - TWO-DIMENSIONAL CODES FOR DIFFERENT TYPES OF SEALS

SCIENTIFIC CODE - A THREE-DIMENSIONAL CFD CODE FOR SEAL ANALYSIS

SEAL TYPES - Cylindrical, bushing and ring, face, labyrinth, tip, damping, brush, electro-fluids, and "smart"
INDUSTRIAL KBS

System Supervision Computer Program

Database

Interface to Scientific Version

Bushing Module  Ring Seal Module  Face Seal Module  Labyrinth Seal Module  Dynamic Module  Tip Seal Module  Thermoelastic Module  Damping Seal Module  Magnetic Fluid Seal Module

Tutorial Interface  KBS Interface

Tutorial Industrial Version  KBS Industrial Version

Master Scientific Code

Input Module  Dynamic Module*  Thermoelastic Module*  Electromagnetic Coupling  Guidance and Optimization

*Common with Industrial Knowledge-Based System

SCIENTIFIC KBS

System Supervisor*

Interface to Industrial Version

Data Base*

Input Module  Dynamic Module*  Thermoelastic Module*  Electromagnetic Coupling  Guidance and Optimization

Master Scientific Code
A MODULAR KNOWLEDGE-BASED SYSTEM

Expert Systems

- Optimization
- Seal Selection

Analytical Modules

- Code
- User Interface
- Dynamics
- User Interface

Data Base

Level of Communications Between Modules - - GUI

MAJOR ISSUE FROM 1991

- PORTABILITY OF THE KBS
COMPUTER SYSTEM CONSIDERATIONS

- A DESK-TOP SYSTEM (FOR ALL USER TYPES)
- SUFFICIENT MEMORY FOR CODE EXECUTION AND FOR MULTITASKING
- I/O COMMUNICATIONS WITH THE SCIENTIFIC CODE
- COMPUTING POWER FOR GUI
- PORTABLE SOFTWARE DEVELOPMENT TOOLS
- PRICING

PERSONAL COMPUTERS WITH OS/2 OPERATING SYSTEM
- Intel 30386 or Higher
- Math Coprocessor
- 8 Megabytes of RAM
- 80 Megabyte hard drive

UNIX WORKSTATIONS
- 16 Megabytes of RAM

MACINTOSH/IBM INTEGRATED SYSTEM
PORTABILITY OF SOFTWARE

Fortran and C for Codes

GUI - User Interface and C++ compatible with OS/2 Presentation Manager and OSF/MOTIF

Expert Systems - NEXPERT or CLIPS

STATUS

• SEVERAL INDUSTRIAL CODES HAVE BEEN PRODUCED AND READY FOR DISSEMINATION

• A 3D CFD CODE FOR CYLINDRICAL SEALS HAS BEEN COMPLETED

• THE KNOWLEDGE-BASED SYSTEM FRAMEWORK HAS BEEN DEFINED

• RESULTS AND STATUS OF THE PROGRAM HAVE BEEN REPORTED IN SEVERAL MAJOR CONFERENCES

• SEVERAL COOPERATIVE PROGRAMS HAVE BEEN ESTABLISHED

• A TECHNOLOGY TRANSFER PLAN HAS BEEN FORMULATED
**CODE DELIVERABLES**

<table>
<thead>
<tr>
<th>CODE OR MODULE</th>
<th>APPROXIMATE DELIVERY DATE</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. CFD Cylindrical Code</td>
<td>02/01/92 (09/92)</td>
</tr>
<tr>
<td>2. Augmented CFD Cylindrical Module</td>
<td>02/01/94</td>
</tr>
<tr>
<td>3. CFD Code, Face, Wave, Non-Continuous Module</td>
<td>09/01/95</td>
</tr>
<tr>
<td>4. CFD, Tip, Contact, Non-Continuous Module</td>
<td>09/01/96</td>
</tr>
<tr>
<td>5. GJOURN</td>
<td>02/01/91</td>
</tr>
<tr>
<td>6. ICYL</td>
<td>03/01/91</td>
</tr>
<tr>
<td>7. SPIRALG</td>
<td>01/01/92 (07/92)</td>
</tr>
<tr>
<td>8. IFACE</td>
<td>02/01/92</td>
</tr>
<tr>
<td>9. GFACE</td>
<td>03/01/92</td>
</tr>
<tr>
<td>10. SPIRALI</td>
<td>04/01/92</td>
</tr>
<tr>
<td>11. FACEDY</td>
<td>02/01/93</td>
</tr>
<tr>
<td>12. RINGDY</td>
<td>03/01/93</td>
</tr>
<tr>
<td>13. LABYRINTH</td>
<td>04/01/93</td>
</tr>
<tr>
<td>14. FACECON</td>
<td>02/01/94</td>
</tr>
<tr>
<td>15. DISTORTION</td>
<td>04/01/94</td>
</tr>
<tr>
<td>16. Additional Codes</td>
<td>04/01/95</td>
</tr>
<tr>
<td>17. Industrial KBS</td>
<td>04/01/96</td>
</tr>
<tr>
<td>18. Scientific KBS</td>
<td>04/01/96</td>
</tr>
</tbody>
</table>

**NEAR TERM ACTIVITIES**

- CONTINUE CODE DEVELOPMENT
- ADD TURBULENCE AND INERTIA IN COMPRESSIBLE CODES
- DEVELOP USER INTERFACE FOR THE CFD CODE
- DEVELOP GRAHICAL USER INTERFACE
- DEVELOP EXPERT SYSTEMS
Industrial Code Development

Presented by
W. Shapiro and A. Artiles
Mechanical Technology Incorporated
Latham, New York

Presented to
NASA Seals Workshop
Contract NAS3-25644

5 August 1992

OBJECTIVES

- Compile and generate sets of verified 2D and simplified 3D or 1D codes
- Codes are intended for expeditious parametric studies, analysis, and design of a wide variety of seals
- Integration is accomplished by the industrial KBS; additional functions of the KBS are:
  - User-friendly interaction
  - Contact sensitive and hypertext help
  - Design guidance
  - Expandable data base
<table>
<thead>
<tr>
<th>Code Module</th>
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</thead>
<tbody>
<tr>
<td>GCYL (Gas Cylindrical)</td>
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</tr>
<tr>
<td>ICYL (Incompressible Cylindrical)</td>
<td>03/01/91</td>
</tr>
<tr>
<td>SPIRALG (Gas Spiral Groove)</td>
<td>04/01/91</td>
</tr>
<tr>
<td>CFD Cylindrical Code</td>
<td>07/31/92</td>
</tr>
<tr>
<td>IFACE (Incompressible Face)</td>
<td>12/31/92</td>
</tr>
<tr>
<td>GFACE (Gas Face)</td>
<td>12/31/92</td>
</tr>
<tr>
<td>SPIRALI (Incompressible Spiral Groove)</td>
<td>12/31/92</td>
</tr>
<tr>
<td>FACEDY (Face Dynamics)</td>
<td>09/30/93</td>
</tr>
<tr>
<td>RINGDY (Ring Dynamics)</td>
<td>09/30/93</td>
</tr>
<tr>
<td>LABYRINTH (Gas)</td>
<td>09/30/93</td>
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<tr>
<td>Augmented CFD Cylindrical Module</td>
<td>02/01/94</td>
</tr>
<tr>
<td>FACECON (Face Contact)</td>
<td>02/01/94</td>
</tr>
<tr>
<td>DISTORTION (Thermoelastic Distortion)</td>
<td>04/01/94</td>
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<tr>
<td>Additional Codes:</td>
<td></td>
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<tr>
<td>Brush</td>
<td></td>
</tr>
<tr>
<td>Damping Seal</td>
<td></td>
</tr>
<tr>
<td>CFD Code, Face, Wave, Groove Module</td>
<td>09/01/95</td>
</tr>
<tr>
<td>Industrial KBS</td>
<td>04/01/96</td>
</tr>
<tr>
<td>Scientific KBS</td>
<td>04/01/96</td>
</tr>
<tr>
<td>CFD, Tip, Contact, Noncontinuous Module</td>
<td>09/01/96</td>
</tr>
</tbody>
</table>
Computer Code GCYL
Gas Cylindrical Seals

GCYL CAPABILITIES

- Varying geometries
- Variable or constant grid (30 x 74)
- Shaft eccentricity and misalignment
- Specified boundary pressures and periodic boundary conditions
- Symmetry in axial direction
- Determining load (function of displacement) or seal position to satisfy given load
- Choice of English or SI units
- Frequency-dependent stiffness and damping coefficients
- Inlet and outlet inertia*
- Turbulence*

*To be added.
### CYLINDRICAL GEOMETRIES

- **Cylindrical Multilobe**
  - With or without grooves

- **Cylindrical Rayleigh Step**

- **Tapered in Flow Direction**

- **Rayleigh Step in Direction of Flow**

- **Self-Energized, Hydrostatic**
  - (Inherent compensation, orifice compensation, spot orifices, recesses)

### SEGMENTED RING SEAL

<table>
<thead>
<tr>
<th>Item</th>
<th>Description</th>
<th>Material</th>
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<tbody>
<tr>
<td>1</td>
<td>Segmented Ring</td>
<td>Carbon</td>
</tr>
<tr>
<td></td>
<td>Rayleigh Step</td>
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</tr>
<tr>
<td>2</td>
<td>Spring-Radial</td>
<td>Inconel X-750</td>
</tr>
<tr>
<td>3</td>
<td>Spring-Axial</td>
<td>Inconel X-750</td>
</tr>
<tr>
<td>4</td>
<td>Housing</td>
<td>Stainless Steel 17-4 PH</td>
</tr>
<tr>
<td>5</td>
<td>Cover</td>
<td>Stainless Steel 17-4 PH</td>
</tr>
<tr>
<td>6</td>
<td>Stop Pin</td>
<td>Stainless Steel 17-4 PH</td>
</tr>
<tr>
<td>7</td>
<td>Seal</td>
<td>Teflon</td>
</tr>
<tr>
<td>8</td>
<td>Sleeve</td>
<td>Inconel 718</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Hard Chromium Plated</td>
</tr>
</tbody>
</table>

50-mm Shaft
GCYL OUTPUT

- Clearance distribution
- Pressure distribution
- Leakage at specified flow paths
- Load and load angle
- Righting moments
- Viscous dissipation
- Cross-coupled, frequency-dependent stiffness and damping coefficients
- Plotting routines (pressure and clearance distribution)

COMPRESSIBLE REYNOLDS' EQUATION

\[
\frac{\partial}{\partial \theta} \left( \rho_h^3 \left( \frac{\partial P}{\partial \theta} \right) \right) + \frac{\partial}{\partial Z} \left( \rho_h^3 \left( \frac{\partial P}{\partial Z} \right) \right) = \Lambda \frac{\partial (PH)}{\partial \theta} + \frac{\partial (PH)}{\partial T}
\]

where:

- \( Z = z/R \), \( H = h/C_0 \), \( T = T_0 \), \( P = p/p_0 \),
- \( \Lambda = \frac{6\mu \omega R^2}{\rho_0 C_0^2} \), \( b_0 = \frac{12\mu R^2}{\rho_0 C_0^2} \)
INTEGRAL FORMAT

\[ \int \nabla \cdot \vec{Q} \, dA = \int \vec{Q} \cdot \vec{n} \, dS = \frac{1}{d} \int (PH) \, dA \]

where:

\[ \vec{Q} = H^2 P \frac{\partial P}{\partial \theta} + \Lambda (PH) \]

ASSUMPTIONS

- Laminar flow
  \[ \tau = \mu \frac{dV}{dy} \cdot \frac{dV}{dy} = U/h \]
  where:
  \[ \tau = \text{Shear stress} \]
  \[ \mu = \text{Viscosity} \]
  \[ V = \text{Fluid velocity} \]
  \[ U = \text{Slider velocity} \]
  \[ y = \text{Film height} \]

- Inertia is small and neglected compared to viscous shear

- Pressure across film is constant

- Height of film is small compared to other geometric dimensions; curvature is ignored

- Viscosity is constant

- Gas is isothermal
TURBULENCE

- \( Re = \frac{\rho U h}{\mu} \geq 1000 \)

Where:
- \( \rho \) = Density
- \( U \) = Surface velocity
- \( h \) = Film thickness
- \( Re \) = Reynolds number

- The most common approach to turbulence is to use G factors that modify the viscosity. G factors are dependent on the Reynolds number and pressure gradients
  - Couette Reynolds number: \( Re = h \frac{R_w \rho}{\mu} \)
  - Poiseuille Reynolds number: \( Re^* = h^2 \left| \nabla \rho \right| \rho / \mu^2 \)
  - \( G_x = \min \left[ G_x \left( Re \right), G_p \left( Re^* \right) \right] \)
  - \( G_z = \min \left[ G_z \left( Re \right), G_p \left( Re^* \right) \right] \)

UNWRAPPED SEAL SURFACE

\[ \Delta \theta (1) \]
\[ \Delta \theta (N - 1) \]
\[ J = 1 \]
\[ I = M \]
\[ DZ (M - 1) \]
\[ DZ (1) \]
\[ I = 1 \]
\[ J = N \]
\[ I, M, Z \]
\[ J, N, \theta \]
\[ \theta P \]
FLOW BALANCE EQUATION

\[ Q_{12} \frac{\Delta Z}{2} + Q_{12} \frac{\Delta Z_{1}}{2} + Q_{14} \frac{\Delta \theta_{1}}{2} + Q_{14} \frac{\Delta \theta_{1}}{2} - Q_{54} \frac{\Delta Z_{1}}{2} - Q_{54} \frac{\Delta \theta_{1}}{2} \]

- \( Q_{23} \frac{\Delta \theta_{1}}{2} - Q_{23} \frac{\Delta \theta_{1}}{2} = -\frac{1}{4} (\Delta \theta_{1} + \Delta \theta_{1}) (\Delta Z_{1} + \Delta Z_{1}) \frac{\partial H_{1}}{\partial I} \)

+ \( Q_{\text{source}} \)

Where, for example

and

\[ Q_{12}^{\text{old}} = -H \frac{G_{1}}{\Delta \theta_{1}} (P_{1} - P_{1}) + \Lambda P_{12} H_{1} \]

\[ P_{12} = \frac{P_{1} + P_{1}}{2} \]

NEWTON-RAPHSON LINEARIZATION

\[ F_{1} (P_{1}, P_{2}, P_{3}, \ldots, P_{k}, \ldots, P_{9}) = 0 \]

\( \Box \) The partial derivatives for the Newton-Raphson linearization may be calculated numerically:

\[ \frac{\partial F_{1}}{\partial P_{k}} = \frac{F_{1} (P_{1}, P_{2}, \ldots, P_{k} + \varepsilon/2, \ldots, P_{9}) - F_{1} (P_{1}, P_{2}, \ldots, P_{k} - \varepsilon/2, \ldots, P_{9})}{\varepsilon} \]

\( \Box \) Then the linear equation for determining iterated pressures is:

\[ F_{1} \text{(old)} + \sum_{k=1}^{9} \frac{\partial F_{1}}{\partial P_{k}} \text{ (old)} (P_{k} \text{ (new)} - P_{k} \text{ (old)}) = 0 \]

\( \Box \) The equation is put into the matrix format where \( P_{i} \) is the current pressure being solved for

\[ [C_{i}] \{ P_{i} \} + [E_{i}] \{ P_{1} \} + [D_{i}] \{ P_{1} \} = \{ R_{i} \} \]

The system of equations is solved by the column matrix method.
FREQUENCY-DEPENDENT SPRING AND DAMPING COEFFICIENTS

\[ \int \vec{\nabla} \cdot \vec{Q} \, ds = \int \vec{Q} \cdot \vec{n} \, ds = -\frac{\partial}{\partial t} \int (1 + P) \, H \, dA \]

- Introduce the RHS and perturb clearance and pressure
  \[ H = e^{im}, \quad P' = Pe^{im} \]

  then, perturb the resulting equation with respect to eccentricity to obtain
  \[ \frac{\partial P}{\partial e_k} \]

- The real part of the derivative with respect to eccentricity integrated over the area is stiffness. While the imaginary part divided by \( \sigma \) and integrated over the area is damping

FREQUENCY-DEPENDENT SPRING AND DAMPING COEFFICIENTS (continued)

\[ \int \vec{\nabla} \cdot \vec{Q} \, ds = \int \vec{Q} \cdot \vec{n} \, ds = -\frac{\partial}{\partial t} \int (1 + P) \, H \, dA \]

- The final set of linear difference equations for the complex stiffness pressure derivatives \( \{P_k^*\} \) are obtained
  \[ \begin{bmatrix} C' \end{bmatrix} \begin{bmatrix} P_k^* \end{bmatrix} + \begin{bmatrix} \hat{E}' \end{bmatrix} \begin{bmatrix} P_{k+1}^* \end{bmatrix} + \begin{bmatrix} \hat{B}' \end{bmatrix} \begin{bmatrix} P_{k-1}^* \end{bmatrix} = \begin{bmatrix} R_k \end{bmatrix} - \begin{bmatrix} \hat{C}_k \end{bmatrix} \begin{bmatrix} \hat{P}_k \end{bmatrix} \]
  \[ - \begin{bmatrix} \hat{E}_k \end{bmatrix} \begin{bmatrix} \hat{P}_{k+1} \end{bmatrix} - \begin{bmatrix} \hat{C}_k \end{bmatrix} \begin{bmatrix} \hat{P}_{k-1} \end{bmatrix} \]

  where:
  \[ \begin{bmatrix} C' \end{bmatrix} = \begin{bmatrix} \hat{C}' \end{bmatrix} + i \sigma \begin{bmatrix} \hat{C}' \end{bmatrix} \]
  \[ \begin{bmatrix} R_k \end{bmatrix} = \begin{bmatrix} \hat{R}_k \end{bmatrix} - i \sigma \begin{bmatrix} \hat{R}_k \end{bmatrix} \]
  \[ \hat{R}_k = A_k \frac{\partial H_1}{\partial e_k} (1 + P_i) \]
  \[ \hat{C}_k = HC_1 A_1 + HC_2 A_2 + HC_3 A_3 + HC_4 A_4 \]
  \[ \begin{bmatrix} \hat{C}_k \end{bmatrix} = \frac{[\hat{C}_k]^* + \hat{C}_k}{\eta} \]

- The system of equations is solved by the column method in a directly analogous manner to that used in solving the steady-state equation. The principal difference is that all the matrix operations are performed using complex arithmetic.
### STIFFNESS AND DAMPING COEFFICIENTS

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<thead>
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</thead>
<tbody>
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<td>Excitation Frequency (rpm)</td>
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#### Stiffness Coefficients

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#### Damping Coefficients

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360° cylindrical seal; \( L = 1 \) in.; \( D = 1 \) in.; \( C = 0.001 \) in.; \( \mu = 3 \times 10^{-9} \) lb-sec/in.²; 0 gage pressure at both ends
INLET INERTIA

\[ Q = G \cdot C_0 \cdot A_o \cdot P_s \left\{ \left( \frac{P_R}{P_s} \right)^{2\gamma} \left[ 1 - \left( \frac{P_R}{P_s} \right)^{\frac{\gamma-1}{\gamma}} \right] \right\}^{1/2} \]

where:
- \( C_0 \) = Coefficient of discharge
- \( A_o \) = Orifice area, in.\(^2\)
- \( P_s \) = Upstream pressure, psia
- \( P_R \) = Downstream pressure, psia
- \( \gamma \) = Ratio of specific heats
- \( G_c \) = Gas constant, sec\(^2\)/R
- \( \theta \) = Absolute gas temperature
- \( Q \) = Orifice flow, lb/sec

If \( \left( \frac{P_R}{P_s} \right) \leq P_{CR} \), then \( \left( \frac{P_R}{P_s} \right) = P_{CR} \)

where:
\[ P_{CR} = \left[ \frac{2.0}{\gamma + 1} \right] \left( \frac{\theta}{P_s} \right) \]

INTERNAL HALVING ROUTINE

[Graph showing Orifice Flow Curve with pressure ratio and flow rate values marked]
Computer Code SPIRALG
Spiral-Groove Gas Seals

SPIRAL-GROOVE FACE SEAL

- Direction of Rotation
  - Providing Pumping
  - Grooves Rotate

- Groove Angle
- Groove Depth = GD
- Land Width/Groove Width = γ

SPIRAL-GROOVE CYLINDRICAL SEALS
CAPABILITIES

- Shaft seals and face seals
- Compressible flow
- Finite eccentricity and misalignment
- Four degrees of freedom for shaft seals (three for face seals)
- Frequency-dependent dynamic coefficients
- Arbitrary end pressures
- Predicts load, flow, power loss, dynamic coefficients, shaft displacements, and minimum film thickness

ASSUMPTIONS

- Laminar isothermal flow
- No fluid inertia
- Ideal gas law
- Thin film approximations are valid
- Narrow groove theory
- Linearized time dependence
- Ideal surfaces
TECHNICAL FEATURES

- Finite misalignment
- General algorithm for treating frequency-dependent dynamic coefficients
- Either forces or displacements may be specified in all degrees of freedom
- Optional implementation of automatic numerical damping algorithm
- Optional implementation of Romberg extrapolation algorithm

COORDINATE REFERENCE FRAMES

[Diagram of coordinate reference frames for shaft seal and face seal]
ECCENTRIC SPIRAL-GROOVED SHAFT SEAL

\[ \begin{align*}
\frac{L}{D} &= 1 \\
\beta &= 25^\circ \\
\Lambda &= 10 \\
\delta &= 1 \\
\alpha &= 0.5 \\
\varepsilon &= 0
\end{align*} \]

Spiral Theory

Global and Local Pressures

\[ \Delta p \]

\[ \Delta p_0 \]

\[ \Delta p_1 \]

\[ r \Delta \theta \]

\[ r \Delta \theta_0 \]

\[ r \Delta \theta_1 \]

\[ n_r \]

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GLOBAL AND LOCAL PRESSURE GRADIENTS

- When the number of grooves becomes large, the sawtooth portion of the local pressure variation may be approximated with linear representations

\[
\frac{\Delta p}{\Delta \theta} \approx \frac{\Delta p}{\Delta \theta} + \frac{\Delta p}{\Delta \theta} (\frac{\Delta \theta}{\Delta \theta}) + (1 - \alpha) \left( \frac{\Delta \theta}{\Delta \theta} \right)
\]

\[
\frac{\Delta \theta}{\Delta \theta} = \alpha \text{ and } \frac{\Delta \theta}{\Delta \theta} = 1 - \alpha
\]

\[
\frac{\partial p}{\partial \theta} = \alpha \left( \frac{\partial p}{\partial \theta} \right) + (1 - \alpha) \left( \frac{\partial p}{\partial \theta} \right)
\]

- The corresponding relationship in the traverse direction,

\[
\frac{\partial p}{\partial s} = \alpha \left( \frac{\partial p}{\partial s} \right) + (1 - \alpha) \left( \frac{\partial p}{\partial s} \right)
\]

is obtained in a similar manner.

- The remaining two equations required to solve for the four local pressure derivatives are obtained from continuity considerations.

CONTINUITY CONDITIONS

- Continuity of pressure at groove-ridge interface

\[
\cos \frac{\theta}{r} \left( \frac{\partial p}{\partial \theta} \right) + \sin \beta \left( \frac{\partial p}{\partial \theta} \right) = \cos \frac{\theta}{r} \left( \frac{\partial p}{\partial \theta} \right) + \sin \beta \left( \frac{\partial p}{\partial \theta} \right)
\]

- Continuity of flow at groove-ridge interface

\[
- \frac{h^2}{12 \mu} \left[ \sin \beta \left( \frac{\partial p}{\partial \theta} \right) \right] + \frac{h^2}{2} r(\omega_2 - \omega_1) \sin \beta
\]

\[
- \frac{h^2}{12 \mu} \left[ \sin \beta \left( \frac{\partial p}{\partial \theta} \right) \right] + \frac{h^2}{2} r(\omega_2 - \omega_1) \sin \beta
\]

- Four equations in four unknown local derivatives that can be solved for in terms of global derivatives
FLOW EQUATIONS

- The transverse flow across a ridge groove pair is

\[ q_s = \frac{h_s^2}{12 \mu} \frac{P - P_0}{P_0} \alpha \left( \frac{\partial \rho}{\partial \theta} \right)_0 - \frac{h_s^2}{12 \mu} \frac{P - P_0}{P_0} (1 - \alpha) \left( \frac{\partial \rho}{\partial \theta} \right)_0 \]

- Similarly, the flow in the theta or parallel direction is

\[ q_s = \frac{h_s^2}{12 \mu} \frac{P - P_0}{P_0} \alpha \left( \frac{\partial \rho}{\partial \theta} \right)_0 - \frac{h_s^2}{12 \mu} \frac{P - P_0}{P_0} (1 - \alpha) \left( \frac{\partial \rho}{\partial \theta} \right)_0 \]

\[ + \frac{\omega_1 + \omega_2}{2} \frac{P - P_0}{P_0} [\alpha \eta_0 + (1 - \alpha) \eta] \]

- The squeeze film flow is

\[ q_s = \frac{1}{P_0} (P - \alpha \eta_0 + (1 - \alpha) \eta) \]

- The global flows are expressed in terms of local derivatives, which, in turn, are functions of global derivatives. Thus, global parameters can be used throughout.

DIMENSIONLESS FLOWS

\[ Q_s = -(1 + \eta) \left[ h_s^2 \left( k_1 \frac{\partial \rho}{\partial \theta} + k_2 \frac{\partial \rho}{\partial \theta} \right) \right] + \Lambda_k R \sin \beta - \Lambda (\alpha \tilde{o} + \tilde{H}_s) R \]

\[ Q_s = -(1 + \eta) \left[ h_s^2 \left( k_1 \frac{\partial \rho}{\partial \theta} + k_2 \frac{\partial \rho}{\partial \theta} \right) \right] - \Lambda_k R \cos \beta \]

where:

- \( P = \frac{P - P_0}{P_0} \)
- \( R = \frac{r}{R_0} \)
- \( \tilde{Q} = \frac{12 \mu R_c}{C^3} \tilde{q} \)
- \( \tilde{t} = \frac{\omega}{2\Lambda} \)
- \( \tilde{H}_s = \frac{h_s}{C} \)
- \( \Gamma = \frac{h_s}{h_0} \)
- \( \tilde{S} = \frac{S}{R_0} \)

and

\[ \Lambda = \frac{6 \mu \omega R_c^2}{P_0 C^3} \]

\[ \tilde{o} = \frac{h_s - h_0}{C} \]

\[ \Lambda = \Lambda \tilde{o} \tilde{o} (1 - \alpha) \sin \beta \]

\[ \alpha = \frac{1}{\tilde{t} + \tilde{t}_0} \]

\[ \tilde{\omega} = \frac{\omega_2 - \omega_1}{\omega_0} \]

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The column matrix containing spiral-groove coefficients, \( k_j(\alpha, \beta, \Gamma) \), is:

\[
k = \begin{bmatrix}
\frac{\alpha (1 - \alpha) (\Gamma^3 - 1)^2 \sin \beta + \Gamma^3}{(1 - \alpha) \Gamma^3 + \alpha} \\
\frac{\alpha (1 - \alpha) (\Gamma^3 - 1)^2 \sin \beta \cos \beta}{(1 - \alpha) \Gamma^3 + \alpha} \\
\frac{\alpha (1 - \alpha) (\Gamma^3 - 1)^2 \cos^2 \beta + \Gamma^3}{(1 - \alpha) \Gamma^3 + \alpha} \\
\frac{(\Gamma^3 - 1)}{(1 - \alpha) \Gamma^3 + \alpha} \\
\frac{(1 - \alpha) \Gamma + \alpha}{\Gamma} \\
\frac{(\Gamma - 1) \sin \beta}{(1 - \alpha) \Gamma^3 + \alpha} \\
\frac{\alpha (1 - \alpha) (\Gamma^3 - 1) \sin \beta \cos \beta}{(1 - \alpha) \Gamma^3 + \alpha} \\
\frac{\alpha (1 - \alpha) (\Gamma^3 - 1) \cos \beta + \alpha \Gamma + (1 - \alpha) \Gamma^3}{(1 - \alpha) \Gamma^3 + \alpha}
\end{bmatrix}
\]
NEWTON-RAPHSON ITERATION

Flow Balance

\[ Q_{12} \Delta S_{12} + Q_{14} \Delta S_{14} + Q_{14} \Delta S_{14} + Q_{14} \Delta S_{14} + Q_{24} \Delta S_{24} - \]
\[ Q_{24} \Delta S_{24} - Q_{23} \Delta S_{23} - Q_{23} \Delta S_{23} - \]
\[ = \frac{\partial}{\partial t} (1 + P_4) (\alpha \delta + H_{4y})_{1/2, j - 1/2} \Delta A_1 + \]
\[ (\alpha \delta + H_{4y})_{1/2, j - 1/2} \Delta A_2 + \]
\[ (\alpha \delta + H_{4y})_{1/2, j - 1/2} \Delta A_3 \]

For Steady State, RHS = 0

\[ F_4 (H_r, P_1, P_2, P_3, P_4, P_6, P_7, P_8, P_9) = 0 \]

Apply Newton-Raphson

\[ F_4 + \sum_{k=1}^{9} \frac{\partial F_i}{\partial P_k} (P_9^{\text{new}} - P_9) = 0 \]

where:

\[ \frac{\partial F_i}{\partial P_k} = F_i (H_r, P_1, \ldots, P_k + \eta, \ldots, P_9) - F_i (H_r, P_1, \ldots, P_9) \]
Flow Balance

\[
\begin{align*}
Q_{12} \Delta S_{12} + Q^*_{12} \Delta S^*_{12} + Q^*_{14} \Delta S^*_{14} - Q_{14} \Delta S_{14} - Q^*_{14} \Delta S^*_{14} &= \\
- Q^*_{45} \Delta S^*_{45} - Q_{23} \Delta S_{23} - Q^*_{23} \Delta S^*_{23} &= \\
= - \frac{\partial}{\partial t} \left( (1 + P_0) \left[ (\alpha + H_i)_{1 + 1/2, j + 1/2} \Delta A_i \\
+ (\alpha + H_i)_{1/2, j + 1/2} \Delta A_4 + (\alpha + H_i)_{1/2, j + 1/2} \Delta A_3 \\
+ (\alpha + H_i)_{1 + 1/2, j + 1/2} \Delta A_2 \right] \right)
\end{align*}
\]

For Steady State, RHS = 0

\[
F_q \left( H_r, P_1, P_2, P_3, P_4, P_5, P_6, P_7, P_8, P_9 \right) = 0
\]

Apply Newton-Raphson

\[
F_q + \sum_{k=1}^{9} \frac{\partial F_q}{\partial P_k} (P_k^{\text{new}} - P_k) = 0
\]

where:

\[
\frac{\partial F_q}{\partial P_k} = \frac{F_q \left( H_r, P_1, \ldots, P_k + \eta, \ldots, P_9 \right) - F_q \left( H_r, P_1, \ldots, P_9 \right)}{\eta}
\]

COLUMN MATRIX FORMAT

- Generate system of equations in the following format:

\[
[C] \{P^{\text{new}}_i\} + [E] \{P^{\text{new}}_i\} + [D] \{P^{\text{new}}_i\} = \{R^i\}
\]

where:

\[
C_{1,ik} = \frac{\partial F_{q1}}{\partial P_{ik,1}}, \\
E_{1,ik} = \frac{\partial F_{q2}}{\partial P_{ik,1}}, \\
D_{1,ik} = \frac{\partial F_{q3}}{\partial P_{ik,1}}
\]

k = -1, 0, 1; i = 2, \ldots, M - 1

- The interior elements of the column vector \(\{R^i\}\) are

\[
\{R^i\} = \sum_{k=-1}^{1} (C_{1,ik} P_{ik,1} + E_{1,ik} P_{ik,1} + D_{1,ik} P_{ik,1}) - F_q
\]

- Equations solved by column or transfer matrix method
Computer Code GFACE
Gas Face Seals

GFACE CAPABILITIES

- Varying geometries
- Variable or constant grid (30 x 74)
- Shaft eccentricity and misalignment
- Specified and periodic boundary conditions
- Determining performance as a function of position or position to satisfy a given load
- Frequency-dependent stiffness and damping coefficients
- English or SI units
FACE SEAL CONFIGURATIONS

Hydrostatic

Circumferential Rayleigh Step

Circumferential Tapered Land

Radial Rayleigh Step

Radial Tapered Land
POLAR GRID MESH SYSTEM

COORDINATE SYSTEM FOR GFACE
GFACE THEORY

REYNOLDS' EQUATION

\[ \frac{\partial}{\partial R} \left( R \rho H^3 \frac{\partial P}{\partial R} \right) + \frac{1}{R} \frac{\partial}{\partial \theta} \left( P H^3 \frac{\partial \rho}{\partial \theta} \right) = \Lambda \frac{\partial (PH)}{\partial \theta} + \frac{\partial (PH)}{\partial T} \]

where:

\[ R = r/r_0, \quad H = h/C_0, \quad T = t/t_0, \quad P = p/p_0, \]

\[ \Lambda = \frac{6 \mu \omega r_0^2}{p_0 C_0^2}, \quad t_0 = \frac{12 \mu r_0^2}{p_0 C_0^2} \]

FLOW-BALANCE CELL AND ASSOCIATED GRID NETWORK
FLOW-BALANCE ACROSS CELL

The net flow through a cell can be expressed as:

\[
Q_{12}^+ \frac{\Delta R_i}{2} + Q_{12}^- \frac{\Delta R_{i+1}}{2} + Q_{i4}^+ \frac{\Delta \theta_i}{2} + Q_{i4}^- \frac{\Delta \theta_{i+1}}{2} - Q_{34}^+ \frac{\Delta R_i}{2} - Q_{34}^- \frac{\Delta R_{i-1}}{2} - Q_{23}^+ \frac{\Delta \theta_i}{2} - Q_{23}^- \frac{\Delta \theta_{i-1}}{2} = Q_{in}
\]

- \(Q_{12}^+\) means the mass flow per unit length across the plus side of cell boundary 1-2, etc.

- The Q's are dimensionless mass flow per unit length, except for \(Q_{in}\), which is a dimensionless source inlet flow.

- In the \(\theta\) direction:

\[
Q = -PH^3 \frac{\partial P}{\partial \theta} \frac{\Delta R}{2} + A RPH \frac{\Delta H}{2}
\]

- In the R direction:

\[
Q = PH^3 \frac{\partial P}{\partial R} \frac{\Delta \theta}{2}
\]

MASS FLOW BALANCE
CELL PRESSURES AND DERIVATIVES

- $Q$ is defined as:

$$Q = \frac{12 \mu G \tau q}{p_0 C_0^2}$$

- Pressures are taken as the average pressure across the boundary. For example:

$$P_{12} = \frac{P_{ij} + P_{i,j+1}}{2}$$

and

$$\left. \frac{\partial P}{\partial \theta} \right|_{12} = \frac{P_{i,j+1} - P_{ij}}{\Delta \theta_i}$$

EXTERNAL MASS FLOW

$$Q_{in} = OFC \times A_0 \times \left\{ \left( \frac{P_R}{P_S} \right)^{2\gamma} \left[ 1 - \left( \frac{P_R}{P_S} \right)^{\gamma - 1} \right] \right\}^{1/2}$$

where:

$$OFC = \frac{12 \mu C_q}{p_0 C_0^2} \sqrt{\frac{2 \gamma G \tau}{\gamma - 1}}$$

$$A_0 = \pi d_0 H_0$$ for inherent compensation

$$A_0 = \frac{\pi d_0^2}{4}$$ for orifice compensation
FLOW CHOKING

If \( \left( \frac{P_R}{P_S} \right) \leq P_{CR} \), then \( \left( \frac{P_R}{P_S} \right) = P_{CR} \)

where:

\[
P_{CR} = \left[ \frac{2.0}{l(\gamma + 1)} \right]^{\frac{\gamma}{(\gamma - 1)}}
\]

Also, if

\[
\frac{P_R}{P_S} > 1.0, \quad \frac{P_R}{P_S} = \frac{1}{P_R/P_S}, \quad \text{and} \quad P_S = P_R.
\]

then this condition implies backflow through the orifice.

NEWTON-RAPHSON ITERATION ON FLOW BALANCE EQUATION

\[
f_{\text{old}}(P_{\text{new}}) + \sum_{k=1}^{5} \frac{\partial f_{\text{old}}}{\partial P_k} (P_k^{\text{new}} - P_k^{\text{old}}) = 0
\]

where the partial derivatives are explicitly determined, e.g.,

\[
\frac{\partial f_{ij}}{\partial P_k} = \frac{f(P_1, P_2, \ldots, P_K + \epsilon/2, \ldots, P_S)_{ij} - f(P_1, P_2, \ldots, P_K + \epsilon/2, \ldots, P_S)_{ij}}{\epsilon}
\]
The linearized Newton-Raphson equations may be written in the form:

\[ C_j \Delta p_j + E_j \Delta p_{j+1} + D_j \Delta p_{j+1} = R_j \]

The column method is used to solve the new pressures in the set of \( m \times n \) equations.

**Viscous Power Loss**

![Diagram of fluid element and seal interface](image)

**a) Seal Interface**

**b) Fluid Element**
VISCOUS FRICTION TORQUE

\[ T_F = \frac{T_1}{\rho_0 CR_0^2} = \int \int H \frac{\partial p}{\partial \theta} Rd \theta dR + \int \int \frac{\Delta}{6} \frac{R^2}{H} Rd \theta dR \]

FLOW ACROSS CIRCUMFERENTIAL LINE

---

FLOW ACROSS CIRCUMFERENTIAL LINE

---
FLOW ACROSS AXIAL LINE

NONUNIFORM CLEARANCE GEOMETRIES

Section A-A
- Radial Taper: Type 1

Section B-B
- Rayleigh Step

Section C-C
- Rayleigh Step

Section D-D
- Circumferential Taper

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MISALIGNED RAYLEIGH-STEP CLEARANCE DISTRIBUTION

OD = 4 in.
ID = 2.5 in.
Clearance = 0.0005 in.
Speed = 5000 rpm

MISALIGNED RAYLEIGH-STEP PRESSURE DISTRIBUTION

OD = 4 in.
ID = 2.5 in.
Clearance = 0.0005 in.
Speed = 5000 rpm
DOUBLE TAPERED-LAND CLEARANCE DISTRIBUTION

OD = 4.505 in.
ID = 3.793 in.
Clearance = 0.0002 in.
Speed = 14,500 rpm

DOUBLE TAPERED-LAND PRESSURE DISTRIBUTION

OD = 4.505 in.
ID = 3.793 in.
Clearance = 0.0002 in.
Speed = 14,500 rpm
## STATUS OF INDUSTRIAL CODES

<table>
<thead>
<tr>
<th></th>
<th>ICYL</th>
<th>GCL</th>
<th>SPIRALG</th>
<th>IFACE</th>
<th>GFACE</th>
<th>SPIRALI</th>
</tr>
</thead>
<tbody>
<tr>
<td>Formulation</td>
<td>C</td>
<td>C</td>
<td>C</td>
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<td>P</td>
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<td>C</td>
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<td></td>
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</table>

C = Complete  
P = In preparation  
ICYL = Incompressible Cylindrical Code  
GCYL = Gas Cylindrical Code  
SPIRALG = Gas Spiral-Groove Code  
IFACE = Incompressible Face Seal Code  
GFACE = Gas Face Seal Code  
SPIRALI = Incompressible Spiral-Groove Code
INCOMPRESSIBLE FLOW CODES   OVERVIEW

W. Shapiro
Mechanical Technology Incorporated
Latham, New York

• OVERVIEW 3 CODES:
  ○ Capabilities
  ○ Status
• ICYL   Cylindrical Seals
  ○ Introduction
  ○ Assumptions
  ○ Formulation & Solution Method
• SPIRALI   Spiral Groove Seals (Cylindrical and Face)
  ○ Introduction
  ○ Assumptions
  ○ Formulation & Solution Method
• IFACE   Face Seals
  ○ Examples
### INCOMPRESSIBLE FLOW CODES — CAPABILITIES

<table>
<thead>
<tr>
<th></th>
<th>ICYL</th>
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<th>SPIRALI</th>
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<tbody>
<tr>
<td>Geometry</td>
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<td>Face</td>
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<td>Turbulent Flow</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
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<tr>
<td>Inertia Inlets</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
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<td>No</td>
<td>Yes</td>
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<tr>
<td>Film thickness</td>
<td>Arbitrary</td>
<td>Arbitrary</td>
<td>Axis-symmetric</td>
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<tr>
<td>Eccentricity</td>
<td>Finite</td>
<td>Finite</td>
<td>Perturbation</td>
</tr>
<tr>
<td>Pressure Pockets</td>
<td>Yes</td>
<td>Yes</td>
<td>No</td>
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<tr>
<td>Spiral Grooves</td>
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### INCOMPRESSIBLE FLOW CODES — STATUS

<table>
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<tr>
<td>KBS Interface</td>
<td>Complete</td>
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</tbody>
</table>
Incompressible Cylindrical Program: Capabilities

ICYL by Dr. Antonio Artiles

- 2-D cylindrical geometry.
- Rotation of rotor and housing.
- Roughness of rotor and housing.
- Laminar or turbulent flow.
- Inertia pressure drop at inlets to fluid film
  - from pressurized pockets
  - from seal ends
- Arbitrary film thickness distribution
  - steps
  - pockets (pressurized or not)
  - tapers
  - preloaded arcs
- Rotor position relative to housing described by four degrees of freedom
  - 2 translational
  - 2 rotational
- User specifies:
  - Rotor lateral position - or - External forces
  - Rotor angular position - or - External moments
  - Pocket pressures - or - orifice size
- Dynamic coefficients
  - 16 stiffness
  - 16 damping
  - critical mass

Incompressible Cylindrical Program: Assumptions

- Isothermal and incompressible flow
- Turbulence: bulk flow model with separate friction factors
- Fluid inertia effects at film entrance use loss coefficients.
- Fluid inertia effects in the film (additional to those inherent in turbulence) are negligible.
- Pressurized pockets deep (constant pressure)
- Surface roughness << film thickness << seal dimensions
- Wall roughness is isotropic
CYLINDRICAL SEAL GEOMETRY SCHEMATIC
(CONCENTRIC ALIGNED POSITION)

SCHEMATIC ILLUSTRATING ROTOR LATERAL AND ANGULAR DISPLACEMENTS
ICYL Program  Governing Equations

Film thickness

\[ H = H_0 - (e_x + ZB) \cos \theta - (e_y - ZA) \sin \theta \]

\[ \frac{\partial H}{\partial t} = - \left( \frac{\partial e_x}{\partial t} + Z \frac{\partial B}{\partial t} \right) \cos \theta - \left( \frac{\partial e_y}{\partial t} - Z \frac{\partial A}{\partial t} \right) \sin \theta \]

momentum

\[ \frac{\langle f, Re_j + f_b Re_b \rangle}{2} U = \frac{H^2}{\mu R} \frac{\partial P}{\partial \theta} + \frac{(Re_j U_j + Re_b U_b)}{2} \]

\[ \frac{\langle f, Re_j + f_b Re_b \rangle}{2} V = - \frac{H^2}{\mu} \frac{\partial P}{\partial Z} \]

continuity

\[ \frac{1}{R} \frac{\partial}{\partial \theta} (UH) + \frac{\partial}{\partial Z} (VH) + \frac{\partial H}{\partial t} = 0 \]
Reynolds numbers, friction factors

\[
Re_i = \frac{\rho H}{\mu} \sqrt{(U-U_j)^2 + V^2}
\]

\[
f'_i = \begin{cases} 
\frac{12}{Re_i}, & Re_i \leq 1000 \text{ (laminar)} \\
\frac{12}{Re_i} (1 - 3 \xi^2 + 2 \xi^3) + f'_i (3 \xi^2 - 2 \xi^3), & 1000 < Re_i < 3000 \\
\frac{12}{Re_i}, & Re_i \geq 3000 \text{ (turbulent)}
\end{cases}
\]

\[
\xi = \frac{Re_i - 1000}{2000}
\]

\[
f'_i = 0.001375 \left[ 1 + \left( \frac{10^4 e_i}{H} + \frac{10^6}{4 Re_i} \right) \right]^{1/3}
\]
ICYL Program ** Boundary Conditions

circumferential ends:
\[ P(Z, \theta) = 0 \text{ and } P(Z, \theta) = 0, \]
or periodic boundary conditions:
\[ P(Z, \theta) = P(Z, \theta_0) \text{ and } U(Z, \theta) = U(Z, \theta_0). \]

left end:
\[ P(-L/2, \theta) = P_i - K_e \frac{1}{2} \rho V_n^2. \]

right end:
\[ P(L/2, \theta) = P_r - K_e \frac{1}{2} \rho V_n^2, \]
or mid-length symmetry:
\[ V(0, \theta) = 0. \]

pocket boundaries:
\[ P(Z, \theta) = P_p - K_e \frac{1}{2} \rho V_n^2. \]

Pressurized Pockets

orifice pressure drop:
\[ P_s - P_p = \text{sgn}(Q_r) \frac{1}{2} \left( \frac{Q_r}{A_s C_d} \right)^2 \]

orifice flow:
\[ Q_r = \int_{S_r} \nabla \cdot \hat{n} \ dS + \int_{A_r} \frac{\partial H}{\partial t} \ dA \]
Discretization of continuity equation

\[-\oint_{S_c} v \cdot \mathbf{n} \, dS = \int_{A_c} \frac{\partial h}{\partial \tau} \, dA\]

Discretization of continuity equation at pressurized boundaries

\[F_{ij} = \frac{\Delta z_i}{2} (u_i h_1 - u_4 h_4) + \frac{\Delta z_{i-1}}{2} (u_2 h_2 - u_3 h_3) + \frac{\Delta \theta_j}{2} (v_i h_1 - v_2 h_2) + \frac{\Delta \theta_{j-1}}{2} (v_4 h_4 - v_3 h_3) - \frac{1}{4} \frac{\partial h_{ij}}{\partial \tau} (\Delta z_i + \Delta z_{i-1}) (\Delta \theta_j + \Delta \theta_{j-1}) = 0\]

Discretization of continuity equation at pressurized boundaries

\[F_{ij} = p_b - p_{ij} - \Lambda_c \max(0,v_n)^2\]

\[= 0\]

\[v_n = \left[ \frac{\Delta z_i}{2} (u_i h_1) + \frac{\Delta z_{i-1}}{2} (u_2 h_2 - u_3 h_3) + \frac{\Delta \theta_j}{2} (v_i h_1 - v_2 h_2) - \frac{\Delta \theta_{j-1}}{2} (v_3 h_3) - \frac{\partial h_{ij}}{\partial \tau} (\Delta z_i + \Delta z_{i-1}) \Delta \theta_j + \Delta z_{i-1} \Delta \theta_{j-1} \right] + \left[ \frac{(\Delta \theta_{j-1} + \Delta z_j) h_{ij}}{2} \right]\]
Evaluation of velocity components

\[
G_u \left[ \frac{\partial p}{\partial \theta}, u, v \right] = \frac{f_j \text{Re}_j + f_b \text{Re}_b}{2} - \text{Re}_j \frac{\partial^2 p}{\partial \theta^2} - (\text{Re}_j \text{Re}_b) = 0,
\]

\[
G_v \left[ \frac{\partial p}{\partial z}, u, v \right] = \frac{f_j \text{Re}_j + f_b \text{Re}_b}{2} + \text{Re}_b \frac{\partial^2 p}{\partial z^2} = 0,
\]

\[
\text{Re}_j = \frac{\text{Re}_j^* h}{12} \frac{(u - 2\Lambda_j)^2 + v^2}{},
\]

\[
\text{Re}_b = \frac{\text{Re}_b^* h}{12} \frac{(u - 2\Lambda_b)^2 + v^2}{},
\]

Evaluation of velocity components

\[
G_u \left[ \frac{p_{i+1,j+1} - p_{i,j}}{\Delta \theta_j}, u^-, \frac{v^- + v^+}{2} \right] = 0
\]

\[
G_v \left[ \frac{p_{i+1,j+1} - p_{i,j}}{\Delta z_i}, \frac{u^- + u^+}{2}, v^- \right] = 0
\]

\[
G_u \left[ \frac{p_{i+1,j+1} - p_{i+1,j}}{\Delta \theta_j}, u^-, \frac{v^- + v^+}{2} \right] = 0
\]

\[
G_v \left[ \frac{p_{i+1,j+1} - p_{i+1,j}}{\Delta z_i}, \frac{u^- + u^+}{2}, v^- \right] = 0
\]
ICYL: Forces, Moments, Torque

\[
\begin{pmatrix}
F_x \\
F_y \\
M_x \\
M_y
\end{pmatrix}
= \int_{-L}^L \int_{0_z}^{0_r} \begin{pmatrix}
\cos \theta \\
\sin \theta \\
-Z \sin \theta \\
Z \cos \theta
\end{pmatrix} P R d\theta dZ
\]

\[
\vec{T} = T \vec{e}_z = \int \int_{A_r} \vec{r} \times \vec{i} dA
\]

\[
= R \int \int_{A_r} (\vec{r} \times \vec{e}_z) dA
\]

\[
T = \frac{P_o R^2}{2C_o} \int \int_{A_r} \left( h \frac{\partial p}{\partial \theta} - f_t R_t (u-2\Delta_t) - f_b R_b (u-2\Delta_b) \right) \frac{1}{72h} d\theta dZ
\]

Solution of Rotor position and pocket pressures.

\[
f_x(r) = -f_{xg}
\]

\[
f_y(r) = -f_{yg}
\]

\[
m_x(r) = -m_{xg}
\]

\[
m_y(r) = -m_{yg}
\]

\[
p_s - p_{p1} = \text{sng}(q_{r1}) \Lambda_{r1} (q_{r1})^2, \quad \text{for pocket 1,}
\]

\[
p_s - p_{p2} = \text{sng}(q_{r2}) \Lambda_{r2} (q_{r2})^2, \quad \text{for pocket 2, etc.}
\]
SPIRALi (Spiral Groove Incompressible Flow) 

**Introduction**

SPIRALi by Dr. Jed Walowit

Spiral groove seals

- Provide:
  - stability
  - increase in-phase\(^1\) component of force
  - decrease out-of-phase component of force
  - load support
  - sealing (pumping against pressure gradient)

- Cylindrical seals → symmetric grooves pump against each other
- Face seals → grooves pump against dam region

---

\(^1\)with the displacement

**Basic Assumptions**

- Isothermal and incompressible flow
- Turbulence: Hirs bulk flow model generalized for separate friction factors
- Film discontinuities use loss coefficients. Inertia effects (additional to those inherent in turbulence) throughout film.
- Circumferential and transient effects use small perturbations to a steady state first order solution for a concentric, aligned seal.
- Surface roughness \(<\) film thickness \(<\) seal dimensions
- Narrow groove theory
  - Neglects edge effects and local inertia effects\(^2\)
  - Valid for large number of grooves \((> > 2\pi n \sin \beta)\)
- Machined surfaces are axisymmetric (except spiral grooves)

---

\(^2\)due to groove to groove pressure variations
SPIRALI  Coordinate system

SPIRALI  Quadratic film variation

60
SPIRALI INTEGRATED EQUATIONS

MOMENTUM (Θ AND s DIRECTIONS):

\[ \rho h \left( \frac{\partial u}{\partial t} + v \frac{\partial u}{\partial s} + \frac{u}{r} \frac{\partial u}{\partial \theta} + \frac{u v}{r} \right) = -\frac{\partial p}{\partial \theta} + \frac{(\tau_b - \tau_a)}{r} \cdot \mathbf{1} \]

\[ \rho h \left( \frac{\partial v}{\partial t} + v \frac{\partial v}{\partial s} + \frac{u}{r} \frac{\partial v}{\partial \theta} - \frac{u^2}{r} \right) = -\frac{\partial p}{\partial \theta} + \frac{(\tau_b - \tau_a)}{r} \cdot \mathbf{1} \]

CONTINUITY:

\[ \frac{1}{r} \frac{\partial}{\partial s} (rvh) + \frac{1}{r} \frac{\partial}{\partial \theta} (uh) + \frac{\partial h}{\partial t} = 0 \]

SPIRALI Shear stresses, shear factors, and Reynolds numbers

\[ \begin{align*}
\text{(a)} & \quad p + \Delta p \\
\text{(b)} & \quad \hat{u}_b \cdot \mathbf{1} \\
& \quad \hat{u}_a \cdot \mathbf{1} \\
& \quad h \\
& \quad r \Delta \theta
\end{align*} \]
 SPIRAL: Shear stresses, shear factors, and Reynolds numbers

\[
\tilde{\tau}_a = \frac{1}{2} \rho |\tilde{\nu} - \tilde{\nu}_a| f_{a}\left(\frac{2\kappa h |\tilde{\nu} - \tilde{\nu}_a|}{\mu}\right) (\tilde{\nu} - \tilde{\nu}_a) = \\
= \frac{1}{4} \frac{\mu}{h} f_{a}(R_a) (\tilde{\nu} - \tilde{\nu}_a),
\]

\[
f_{a}(R_a) = n_0 R_a^{m_0}, \quad f_{b}(R_b) = n_0 R_b^{m_0}
\]

\[
R_a = 2h |\tilde{\nu} - \tilde{\nu}_a| \rho/\mu, \quad R_b = 2h |\tilde{\nu} - \tilde{\nu}_b| \rho/\mu.
\]

<table>
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<th>Turbulent</th>
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<td>(n_0)</td>
<td>24.0</td>
<td>0.0751</td>
</tr>
<tr>
<td>(m_0)</td>
<td>-1</td>
<td>-0.25</td>
</tr>
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</table>

SPIRAL: INTEGRATED DIMENSIONLESS EQUATIONS

MOMENTUM:

\[
\frac{-1}{f} \frac{\partial}{\partial \theta} = \beta' \Phi(\tilde{\nu}, \tilde{\nu}_a, h) + \beta' R^\prime \left(\frac{\alpha \tilde{\nu}}{\partial \xi} + \tilde{\nu} \frac{\partial \tilde{\nu}}{\partial \xi} + \tilde{\nu}^2 + \frac{\alpha^2}{\partial \xi} - \frac{\nu^2}{f}\right),
\]

\[
\frac{-\partial}{\partial S} = \beta' \Psi(\tilde{\nu}, \tilde{\nu}_a, h) + \beta' R^\prime \left(\frac{\alpha \tilde{\nu}}{\partial \xi} + \tilde{\nu} \frac{\partial \tilde{\nu}}{\partial \xi} + \tilde{\nu}^2 + \frac{\alpha^2}{\partial \xi} - \frac{\nu^2}{f}\right),
\]

CONTINUITY:

\[
\frac{1}{f} \frac{\partial (\tilde{\nu} h)}{\partial S} + \frac{1}{f} \frac{\partial (\tilde{\nu} h)}{\partial \theta} + \frac{\partial h}{\partial \xi} = 0
\]
SPIRALI ≈ INTEGRATED DIMENSIONLESS EQUATIONS

where

\[
\Phi(\tilde{u}, \tilde{v}, \tilde{h}) = \frac{(\tilde{u} - \tilde{f}\tilde{w}) R_a f_a(R_a) + \tilde{u} R_b f_b(R_b)}{\tilde{h}^2},
\]

and

\[
\Psi(\tilde{u}, \tilde{v}, \tilde{h}) = \frac{R_a f_a(R_a) + R_b f_b(R_b)}{\tilde{h}^2} \tilde{v}.
\]

SPIRALI ≈ Boundary conditions

\( u_{in}, p_{in} \) at seal inlet:

\[
\tilde{u} = \tilde{u}_{in},
\]

\[
\tilde{p} = \tilde{p}_{in} - \frac{1}{2} \rho^* R^* (1 + \zeta) \tilde{v}^2 \quad @ \quad S = S_{in}.
\]

\( p_{ex} \) at exit:

\[
\tilde{p} = \tilde{p}_{ex} \quad @ \quad S = S_{ex}.
\]

\( S_{in} \) depends on flow direction. \( S_{ex} \) at the opposite side from \( S_{ex} \).
SPIRALI & Continuity conditions

At \( s = s_i \):

\[
(h + \Delta h)v_j = hv,
\]

\[
p_j + \frac{1}{2}p v_j^2 = p + \frac{1}{2}p v^2(1 + \xi).
\]

Jump in film thickness,

\[
\xi = \begin{cases} 
\zeta(R,\tilde{h},\tilde{v}), & \Delta \tilde{h} < 0 \text{ (contraction)} \\
\left(1 - \frac{\tilde{h}}{\tilde{h} - \Delta \tilde{h}}\right)^2, & \Delta \tilde{h} \geq 0 \text{ (expansion)} 
\end{cases}
\]

SPIRALI & Stator with inward pumping grooves

rotor motion

groove
land

Region 2 (grooved)
Region 1 (ungrooved)
SPIRALI - - Spiral groove parameters, global and local pressures

SPIRALI - - First order equations

First order variables, $\tilde{A}(S), \tilde{P}(S), \tilde{U}(S)$ and $\tilde{V}(S)$:

$$
\phi'(\tilde{U},\tilde{V},\tilde{A},l) + R^r \tilde{V} \frac{d\tilde{U}}{dS} = 0 ,
$$

$$
-\frac{d\tilde{P}}{dS} = \tilde{P}^r \psi'(\tilde{U},\tilde{V},\tilde{A},l) + \tilde{P}^r R^r \tilde{V} \frac{d\tilde{V}}{dS} ,
$$

$$
\frac{d(\tilde{r}\tilde{H}\tilde{V})}{dS} = 0 .
$$

Closed form solution:

$$
\tilde{V} = \frac{\tilde{r}_m \tilde{H}_m \tilde{V}_m}{\tilde{r}\tilde{H}} ,
$$
SPIRAL! = Semi-Implicit Algorithm

N differential equations:
\[ \frac{dY_i}{dS} = F_i(S, Y_1, Y_2, \ldots, Y_N), \quad i = 1, 2, \ldots, N, \]

\( Y_i \) dependent variables

\( \{Y^{\text{new}}\} \) at the new position \((S + \Delta S)\)

\( \{Y\} \) at the old position \(S\)

\[ \{Y^{\text{new}}\} = \{Y\} + \Delta S \left( \frac{1}{2} \frac{\partial^2}{\partial Y_i \partial Y_j} \right) \{ F(S + \frac{\Delta S}{2}, Y_1, Y_2, \ldots, Y_N) \}, \]

\[ k_{ij} = \frac{\partial}{\partial Y_j} F_i(S + \frac{\Delta S}{2}, Y_1, Y_2, \ldots, Y_N), \quad i, j = 1, 2, \ldots, N. \]

SPIRAL! = Second order equations

\[ h = \hat{h}(S) + \hat{h}'(S, \theta, \tilde{r}), \quad \bar{u} = \hat{u}(S) + \bar{u}'(S, \theta, \tilde{r}), \]

\[ \bar{v} = \bar{v}(S) + \bar{v}'(S, \theta, \tilde{r}), \quad \bar{p} = \hat{p}(S) + \bar{p}'(S, \theta, \tilde{r}). \]

\[ \frac{1}{\hat{p}'} \frac{\partial \bar{v}'}{\partial \theta} = \hat{R} \left( \frac{\partial \bar{v}'}{\partial \theta} + \bar{v} \frac{\partial \bar{v}'}{\partial S} + \frac{d \hat{u}}{dS} \frac{\partial \bar{v}'}{\partial \theta} + \frac{\bar{U}}{\hat{r}} \frac{\partial \bar{v}'}{\partial \theta} \right) + \phi_0 \bar{u}' + \psi_0 \bar{v}' + \phi_R \hat{h}', \]

\[ \frac{1}{\hat{p}'} \frac{\partial \bar{v}'}{\partial S} = \hat{R} \left( \frac{\partial \bar{v}'}{\partial \theta} + \bar{v} \frac{\partial \bar{v}'}{\partial S} + \frac{d \hat{u}}{dS} \frac{\partial \bar{v}'}{\partial \theta} + \frac{\bar{U}}{\hat{r}} \frac{\partial \bar{v}'}{\partial \theta} \right) + \psi_0 \bar{u}' + \psi_r \bar{v}' + \psi_R \hat{h}', \]

\[ \bar{v} \frac{\partial (\hat{r} \hat{h}')} {\partial S} + \frac{d \bar{v}} {dS} \frac{\partial \hat{r} \hat{h}'} {\partial S} + \frac{d (\hat{r} \hat{h})}{dS} \bar{v}' + \frac{\bar{U}}{\hat{r}} \frac{\partial \hat{h}'} {\partial \theta} + \hat{R} \frac{\partial \bar{v}'} {\partial \theta} + \frac{\hat{r}}{\hat{r}} \frac{\partial \hat{h}'} {\partial \theta} = 0. \]
DEVELOPMENT OF A CFD CODE FOR ANALYSIS OF FLUID DYNAMIC FORCES IN SEALS

Presentation by
A.J. Przekwas and M.M. Athavale
CFD Research Corporation
Huntsville, AL

Presented at
Second Seals Flow Code Development Workshop
NASA Lewis Research Center
Cleveland, OH

August 5, 1992

OUTLINE

• Objectives
• Status Report
• Code Capabilities
• Rotordynamic Coefficient Methods
• Test Results
• Conclusions
OBJECTIVE OF THE PROGRAM

- Develop Scientific 3D CFD Code for (CFDRC)
  - Prediction of Flow and Dynamics in Various Seals
  - Contribute to Data Base
  - Accuracy Standard for Industrial Design Codes

- Compile and Generate Set of Verified (MTI)
  Industrial Codes

- Seal Design Configuration with (MTI)
  - Knowledge Based System (KBS)
  - CAD/CAM and Visualization Tools

OBJECTIVES

- Develop Verified CFD Code for Analyzing Seals

- Required Features Include:
  - Applicability to a Wide Variety of Seal Configurations, such as: Cylindrical, Labyrinth, Face, Tip and Brush Seals
  - Accuracy of Predicted Flow Fields and Dynamic Forces
  - Efficiency (Economy) of Numerical Solutions
  - Reliability (Verification) of Solutions
  - Ease-of-Use of the Code (Documentation, Training)
  - Integration with KBS
CFD CODE REQUIREMENTS

- Scientific Code Required Capabilities
  - 3D N-S Analysis in BFC Grids
  - Stationary and Rotating Frames
  - Incompressible and Compressible Flows
  - Variable Physical Properties
  - Steady-State and Transient Solutions
  - Rotordynamic Coefficients
  - Interfaces with Advanced Preprocessing (Grid-GUI) and Postprocessing Packages

SCIENTIFIC CFD CODE DEVELOPMENT

Task 1: Develop a 3D CFD Code for Cylindrical Seals
- for Annular, Tapered, Stepped
- Verification of Code Accuracy
- Rotordynamic Coefficient Calculations

Task 2: Augmentation of Code for Labyrinth and Damper Seals

Tasks 3 & 4: Augmentation for Other Seal Configurations

Note: Starting CFD Code = REFLEQS (developed by CFDRC under a contract from NASA MSFC/ED32)
STATUS - 1991 WORKSHOP

AT 1991 WORKSHOP - 2D CAPABILITIES

- Collocated Grid Formulation for BFC Grids
- Strong Conservative Formulation of Momentum Equations with Cartesian Components
- Choice of SIMPLE, Modified SIMPLEC
- Higher Order Accurate Temporal Differencing
- Higher Order (2nd, 3rd) Spatial Discretizations Available
- Rotating Grid System for Stator-Rotor Configurations
- Moving Grid Options for Arbitrary Rotor Whirling Analysis

CURRENT STATUS

Accomplishments Since Last Workshop

- All Numerical Models Transferred to 3-D
  - collocated variables
  - higher-order schemes, etc.
- Rotordynamic Coefficient Calculation Methods
  - circular whirl
  - moving grid (numerical scheme)
- Seal Specific User Interface
  - grid generation
  - preprocessing
CURRENT CODE CAPABILITIES

- Seals Code has:
  - Finite Volume, Pressure-Based Integration Scheme
  - Colocated Variables with Strong Conservation Approach
  - High-Order Spatial Differencing - up to Third-Order
  - Up to Second-Order Temporal Differencing
  - Comprehensive Set of Boundary Conditions
  - Variety of Turbulence Models (k-ε, Low Re k-ε, multiple scale k-ε)
  - Moving Grid Formulation for Arbitrary Rotor Whirl
  - Two Possible Ways to Calculate Rotordynamics:
    (i) Circular Whirl (ii) Shaker Method (moving grid)

CODE SYSTEM ENVIRONMENT
FLOW SOLVER STRUCTURE

SEAL SPECIFIC CAPABILITIES

• GUI and Preprocessor - Geared for Seals Problems
• Easy, Quick Geometry Definition and Grid Generation
• Four Types of Cylindrical Seals:
  - Annular, Axial Step-Down, Axial Step-Up, and Tempered
• Pull-Down Menus for Problem Parameter Specification
• One Line Commands for
  - Automatic Grid generation
  - Integrated Quantities: Rotor Loads, Torque, etc.
  - Rotordynamic Coefficient
**ROTORDYNAMIC COEFFICIENTS**

- Relation Between Fluid Reaction Force and Rotor Motion
  - Small Perturbations
  - For Nominal, Centered, Rotor Position

\[
\begin{bmatrix}
-F_y \\
-F_z
\end{bmatrix} = \begin{bmatrix}
K & k \\
-k & K
\end{bmatrix} \begin{bmatrix}
y \\
z
\end{bmatrix} + \begin{bmatrix}
C & c \\
-c & C
\end{bmatrix} \begin{bmatrix}
y' \\
z'
\end{bmatrix} + \begin{bmatrix}
M & 0 \\
0 & M
\end{bmatrix} \begin{bmatrix}
y'' \\
z''
\end{bmatrix}
\]

- **K, k** -- Direct and Cross-Coupled Stiffness Coefficients
- **C, c** -- Direct and Cross-Coupled Damping Coefficients
- **M** -- Lumped Mass (Direct Inertia) Coefficient

**ROTORDYNAMIC COEFFICIENT - METHODS**

Circular Whirl Orbit Method

"Numerical Shaker" Method (with moving grid)
CIRCULAR WHIRL METHOD

- Rotating Frame → Quasi-Steady Solutions
- Calculate Quasi-Steady Solutions
  - 4 or More Whirl Frequencies, \( \Omega_i \)
  - Integrate Pressures for each \( \Omega_i \) to Generate Rotor Loads, \( F_y \) and \( F_z \)
- Curve Fit to Calculate Rotordynamic Coefficients:
  - \( F_y = K + c \Omega - M \Omega^2 \)
  - \( F_z = -k + C \Omega \)

NUMERICAL SHAKER METHOD

Two Approaches to Calculate Coefficients

Integrated Approach

\[
\begin{align*}
F_y &= F_{YS} \sin(\Omega t) + F_{YC} \cos(\Omega t) \\
F_z &= F_{ZS} \sin(\Omega t) + F_{ZC} \cos(\Omega t)
\end{align*}
\]

Successive Time Step Approach

\[
\begin{bmatrix}
F_{Y1} \\
F_{Z1} \\
F_{Y2} \\
F_{Z2}
\end{bmatrix} =
\begin{bmatrix}
y_1 & 0 & \dot{y}_1 & 0 \\
0 & -y_1 & 0 & -\dot{y}_1 \\
y_2 & 0 & \dot{y}_2 & 0 \\
0 & -y_2 & 0 & -\dot{y}_2
\end{bmatrix}
\begin{bmatrix}
k' \\
k \\
C \\
c
\end{bmatrix}
\]

\( K' = K + M \Omega^2 \)

Horizontal Displacement Definition

\( Y = A \sin(\Omega t) + B \cos(\Omega t) \)

\( \Omega \) = Shaker Frequency
\( \omega \) = Rotor Speed
CODE ACCURACY CHECK & VALIDATION

• Extensive Validation Effort
  - Checkout Problems
  - Benchmark Problems
  - Validation Problems
  - Field Problems

CODE ACCURACY AND VALIDATION

• Partial List of Relevant Test Cases
  - Flows in Pipes, Channels, Very Narrow Annulii
  - 2D and 3D Driven Cavity Flows
  - Laminar Flows: Wedge, Duct to 90° Bend
  - Turbulent Flows in Annular and Laybrinth Seals (Texas A&M)
  - Flow in Journal Bearings
DESCRIPTION OF THE FLOW PROBLEM

- Simplified Turbine Cavity Problem:
  - 90 x 130 grid
  - Central Differencing
  - k-ε Turbulence Model

- Cooling Flow Rate Parameter

\[ C_Q = \frac{Q}{(R \nu)} \]

where
- \( Q \) = volumetric flow rate
- \( \nu \) = kinematic viscosity
- \( R \) = cavity radius

NUMERICAL RESULTS

Streamlines

\[ C_Q = 1500 \]
\[ C_Q = 7200 \]
\[ C_Q = 13000 \]
Computational results
Cavity temperatures at three cooling flow rates

SAMPLE PROBLEM DEFINITION

- Annular Seal Geometry (After Nordmann, 1987)
  - Rotor Radius 23.5 mm., Nominal Clearance 200μm
  - Seal Length 23.5 mm.
  - Rotor Speed 1000-5000 rpm

- Flow Conditions
  - Specified ΔP Across the Seal
  - Specified Inlet Loss Coefficient
  - Water Density 996 Kg/m³, viscosity 0.7 x 10⁻³ N-s/m

- Computational Parameters
  - k-ε Turbulence Model
  - N_x * N_r * N_θ = 10 * 5 * 30 Computational Grid
  - 40 Time Steps per Cycle
FLUID REACTION FORCES

- Rotor Speed 3000 rpm, $\Omega = 40$ cps.

Geometry

Time Variation of Fluid Forces

ROTORDYNAMIC COEFFICIENTS

Time Variation of Stiffness Coefficients

Mass Parameter
STIFFNESS COEFFICIENTS

Direct

Cross-Coupled

DAMPING COEFFICIENTS

Direct

Cross-Coupled
Time-dependent pressure field, \( t = nT \).

**TAPERED GAS SEAL (NELSON, 1985)**

- **D** = 65.0 mm
- \( C_e \) = 0.086 mm
- \( C_i \) = 0.172 mm
- 3 L/D ratios: 0.1, 0.2, 0.4

- Compressible, Turbulent, Transonic Flow
### TAPERED GAS SEAL - RESULTS

**Moving Grid Method**

<table>
<thead>
<tr>
<th>L/D</th>
<th>K N/m</th>
<th>k N/m</th>
<th>C N-s/m</th>
<th>c N-s/m</th>
<th>Exit Mach Number</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>948000</td>
<td>19700</td>
<td>11.5</td>
<td>0.016</td>
<td>1.00</td>
</tr>
<tr>
<td></td>
<td>115000</td>
<td>15429</td>
<td>9.94</td>
<td>0.043</td>
<td>1.00</td>
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<tr>
<td>0.2</td>
<td>170000</td>
<td>75700</td>
<td>43.9</td>
<td>0.073</td>
<td>0.96</td>
</tr>
<tr>
<td></td>
<td>212550</td>
<td>60886</td>
<td>38.62</td>
<td>0.09</td>
<td>0.97</td>
</tr>
<tr>
<td>0.4</td>
<td>288000</td>
<td>26700</td>
<td>152</td>
<td>0.27</td>
<td>0.83</td>
</tr>
<tr>
<td></td>
<td>355320</td>
<td>233820</td>
<td>145.9</td>
<td>0.57</td>
<td>0.83</td>
</tr>
</tbody>
</table>

Nelson, 1985 [Present Results]
CONCLUDING REMARKS

• 3D CFD Code has been Developed for Annular Seals
• State-of-the-Art Numerical Methods Employed
  - Colocated Grids, Pressure-Based
  - High Order Differencing
  - Moving Grids
• Several Seal Specific Parameters
  - Rotor Loads, Torque, etc
  - Rotordynamics
• Initial Link with GUI Completed
• Ongoing Validation Effort

CONCLUDING REMARKS (CONTINUED)

• Continue Code Testing & Validation
• Add Treatment for Inlet/Exit Regions
  - Geometry Definition
  - Grid Generation
• Code Extensions
  - Augmentation of Code for Labyrinth Seals
  - Treatment of Damper Seals
• Identified Needs
  - Multi-Domain Capability for Proper Treatment of Inlet/Outlet Plenums
  - Two-Layer k-ε Model for Near-Wall Treatment
Seal Analysis Codes: KBS User Interface

Presented by:

Bharat B. Aggarwal
Lynn Cowper

Mechanical Technology Inc.

Seal Analysis Codes: KBS User Interface

Overview

• KBS Executive
  • Access all seal analysis codes
  • Utility services like printing, browsing, plotting, etc.
  • System maintenance and configuration

• Industrial Codes
  • Prepare input files for analysis codes
  • Run analysis code

• Scientific Code
  • User input tailored for specific seal configurations
  • Four types of Cylindrical seals implemented. Others to be added in phases
  • Prepare input files for preprocessor
  • Run the preprocessor
  • Communication capabilities to be added later
Seal Analysis Codes: KBS User Interface

KBS System Implementation

- Portability Requirements
  - User interest in Unix at the last workshop
  - Elected to support both OS/2 and Unix
  - Unix support for OSF/Motif environment only

- Implementation Strategy
  - C++ and Commonview 3.0 class libraries from Glockenspiel
  - Portable to several Unix platforms with OSF/Motif interface
  - NASA will support IBM, HP, and SUN workstations

Seal Analysis Codes: KBS User Interface

KBS System Requirements

- IBM PC Users
  - Intel 80386 (with 80387) or 80486 based machine
  - 8 Mb RAM
  - 80 Mb Hard Disc
  - OS/2 Version 2.0
  - Will continue supporting OS/2 version 1.3 for another year

- Workstation Users
  - IBM RS/6000, SUN, or HP 700 series workstations
  - 24 Mb RAM
  - 200 Mb Hard Disc
  - Unix with OSF/Motif user interface
Seal Analysis Codes: KBS User Interface

System Architecture: KBS Executive

Seal Analysis Codes: KBS User Interface

System Architecture: Analysis Codes

Industrial Codes

Scientific Code

Graphical User Interface

Preprocessor

ASCII Input File

Preprocessor Input File

Analysis Code

CFD Code

ASCII Output File

CFD Code

87
Seal Analysis Codes: KBS User Interface

KBS Executive: Main Screen

**CFD Seal Categories**

- Bushing and Ring Seals
- Face Seals
- Labyrinth Seals
- Tip Seals
- Damping Seals
- Brush Seals
- Electro-Fluid Seals
- Smart Seals
- Utility Programs

Click On A Seal Category

Seal Analysis Codes: KBS User Interface

KBS Executive: Seal Categories Screen

**CFD Industrial Codes**

- Spiral Groove Gas Seal Analysis Program
- Cylindrical Gas Seal Analysis Program
- Incompressible Cylindrical Seal Analysis Program

Click On A Seal Category
Seal Analysis Codes: KBS User Interface

Industrial Code GCYL: Main Screen

Industrial Code GCYL: Analysis Options Screen
Program IGCYL may be used to analyze a wide variety of seals in a cylindrical coordinate reference frame. The solid ring seal configurations analyzed by the program are shown below:
Seal Analysis Codes: KBS User Interface

Industrial Code GCYL: Plotting Program

![Plotting Program Diagram](image)

Seal Analysis Codes: KBS User Interface

Scientific Code: Main Screen

![Main Screen Diagram](image)
Seal Analysis Codes: KBS User Interface

Scientific Code: Seal Types

Scientific Code: Analysis Options Screen
Seal Analysis Codes: KBS User Interface

Scientific Code: Typical Input Screen

Scientific Code: Solution Control Options
Seal Analysis Codes: KBS User Interface

Scientific Code: Output Options

Summary and Future Plans

• KBS implemented to support both OS/2 and Unix users
• Interactive graphics capability to be added to ease input
• Selection of a standard plot file format
• Implementation of database capability
• New codes to be added as they become available
• Enhancements based on user feedback
BRUSH SEAL BRISTLE FLEXURE AND HARD-RUB CHARACTERISTICS

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SUMMARY

The bristles of a 38.1-mm (1.5-in.) diameter brush seal were flexed by a tapered, 40-tooth rotor operating at 2600 rpm that provided sharp leading-edge impact of the bristles with hard rubbing of the rotor lands. Three separate tests were run with the same brush accumulating over $1.3 \times 10^9$ flexure cycles while deteriorating 0.2 mm (0.008 in.) radially. In each, the test bristle incursion depth varied from 0.130 to 0.025 mm (0.005 to 0.001 in.) or less (start to stop), and in the third test the rotor was set 0.25 mm (0.010 in.) eccentric. Runout varied from 0.025 to 0.076 mm (0.001 to 0.003 in.) radially. The bristles wore but did not pull out, fracture, or fragment. Bristle and rotor wear debris were deposited as very fine, nearly amorphous, highly porous materials at the rotor groove leading edges and within the rotor grooves. The land leading edges showed irregular wear and the beginning of a convergent groove that exhibited sharp, detailed wear at the land trailing edges. Surface grooving, burnishing, “whipping,” and hot spots and streaks were found. With a smooth-plug rotor, post-test leakage increased 30 percent over pretest leakage.

INTRODUCTION

High-performance, lightweight engines require compliant seal configurations to accommodate flexible interfaces. Thus, in many aircraft gas turbine engines and other turbomachines brush seal systems are being proposed to replace labyrinth seals because brush seals are compliant and reliable, leak less, cost less, and enhance rotor stability. Brush seals have been the subject of much recent seals research (refs. 1 to 20).

A brush seal system consists of the brush and a hardened rub ring and can be linear, circular, or contoured (see ref. 20 for a review). The bristles are oriented to make an angle of 30° to 50° with the interface, such as the rotor radius for a circular brush. This design allows the bristles to flex when rotor excursions occur without significant damage to either the rotor or the seal.

A typical brush seal configuration, figure 1 (courtesy of Cross Mfg. Ltd. (ref. 1)) consists of (1) a backing plate (like a sealing dam), (2) a circumferential or linear set of packed wires (fibers or bristles), (3) a pinch plate that serves as a retainer for the brush bristles, and (4) an outside diameter surface that fits tightly to the housing (insert in fig. 1). The flexibility of the fibers and implicitly the performance of this seal are governed by many factors as expressed in terms of similitude parameters (refs. 9 and 20). Among these factors are fiber length and diameter, inclination to the moving surface, surface speed, interface friction, seal diameter, fluid properties, packing density, modulus of elasticity, backing plate clearance, and preload or interference fit.

Typically for a circular brush, the wire or brush materials are superalloys and range from 0.05 to 0.07 mm (0.002 to 0.0028 in.) in diameter. The bristles are approximately 0.96 mm (0.38 in.) long and are aligned at 30° to 50° to the shaft in the direction of rotation. Nominally, there are 98 bristles/mm (2500 bristles/in.) of circumference. The interface is characterized by a smooth (4 to 20 rms), hardened rub surface on the shaft (e.g., $\text{Al}_2\text{O}_3$ or for short duration the uncoated shaft itself). Because brush seals are contact seals with radial interferences ranging from zero to more than 0.25 mm (0.01 in.), ceramic
coatings and superalloy materials are often used to enhance life and minimize wear at elevated surface speeds, temperatures, and pressure drops.

Although brush seals show great promise for future applications, it must be acknowledged that brush seals are most effective as contact seals and that life and wear rates are major concerns. Whereas bristle blowout will cause excessive leakage, bristle loss and debris have a potential for destructive impact on the powerplant. Thus, the issues of bristle pullout, surface rubbing, bristle wear, and debris are qualitatively addressed in this paper.

The authors are aware that other data exist for ranges of interference fits and other configurations, but the results are proprietary.

APPARATUS

The "drill press" apparatus was similar to that described in reference 2. In the tests of reference 2 the 38.1-mm (1.5-in.) diameter brush seal was fixed in a pressure vessel and the rotor was a smooth-surface, tapered plug turning at 400 rpm. Leakage data at various interferences and eccentricities have been reported (ref. 19).

In the tests described herein the 38.1-mm (1.5-in.) diameter brush seal was again mounted in the pressure vessel that simulated the static housing; but for these tests flutes were machined the length of the plug rotor, providing a set of 40 lands and 40 grooves, or a 40-tooth rotor (fig. 2). The lands were 1.638±0.04 mm (0.0645±0.0015 in.) just above the groove at test 3 and 1.582±0.04 mm (0.0623±0.0015 in.) just below the groove at test 1; see rotor sketch on table I. The groove width (fig. 3) averaged 1.397 to 1.422 mm (0.055 to 0.056 in.) with further dimensions provided in tables I and II. Prior to testing the machining tool marks were clear, being axial in the grooves and circumferential on the lands. This rotor provided 40 impacts of the brush bristles per revolution and was rotated at 2600 rpm.

The 38.1-mm (1.5-in.) diameter brush seal (fig. 4) was damaged in a previous series of tests related to reference 2. The damaged section, although quite small and having a "chewed" appearance, increased seal leakage. The seal could no longer be used for leakage tests but was adequate for the tests herein.

The rotor was AISI 304 stainless steel, and the brush bristles were Haynes 25 in the annealed condition. When stainless steel is rubbed during a machining operation, it tends to change from a "gummy" machining material to a surface-work-hardened material. As a result the bristles would be expected to rub-machine the stainless steel, and in turn the stainless steel would be expected to abrasively remove the bristles.

In test 1 the interference was set at 0.025 to 0.050 mm (0.001 to 0.002 in.) with the groove depth at 0.05 to 0.08 mm (0.002 to 0.003 in.). As expected the bristles rub-machined the rotor.

For test 2 the plug rotor was reset to a portion of the surface that was unrubbed. At that point the groove depth was 0.08 to 0.13 mm (0.003 to 0.005 in.). The interference fit between the rotor lands and the brush was 0.05 to 0.08 mm (0.002 to 0.003 in.).

For test 3 the plug rotor was again reset to a portion of the surface that was unrubbed. The groove depth was 0.178 to 0.254 mm (0.007 to 0.010 in.). For this test the rotor was initially set 0.33 mm (0.013 in.) eccentric, but the rotor rubbed the fence (backing washer) slightly. The fence diameter was 39.2 mm (1.544 in.). The rotor was then reset to an estimated static eccentricity less than 0.25 mm
(<0.010 in.). The dynamic eccentricity was estimated to be less than 1 mm (<0.004 in.). No active clearance measurements were made during these tests; these estimates of eccentricities were made from post-test photographs and static measurements. These settings provided a test with significant rotor impacting and incursion at one portion of the seal and no rubbing contact diametrically opposite to that position.

In tests 1 and 2 the smooth rotor and the 40-tooth rotor were assumed to be interchangeable. The repositioning of the stator for test 3 introduced an unaccountable bias that was estimated in order to correlate the measured flow rates. For test 3 the smooth-rotor initial static eccentricity was estimated to be less than 0.15 mm (<0.006 in.), and after test 3 the estimated static eccentricity was less than 0.25 mm (<0.010 in.).

RESULTS

The results are separated into observations of (1) the brush bristle flexure cycles with associated interface damage to the brush seal and the rotor, and (2) the leakage or performance changes.

Bristle Flexure and Interface Damage

Visualization of the rotor-brush interface at creeping surface speeds (under 10 rpm) revealed little groove penetration. In the impact zone the brush stiffness and the low void did not permit a fully deflected or extended set of bristles at the interface. Instead the impact compacted the bristles in the circumferential direction into the brush and spread the bristles in the axial direction at rate of 40 times per revolution.

Time of testing and brush diameters before and after testing for the three tests are presented in table I; additional dimensions are given in table II. The diameters were obtained by inspecting the brush on an optical comparator before and after each test. The chewed area and a few stray wires served as reference positions for measurements.

Optical inspection of the grooves cut by the brush into the stainless steel rotor (test 1) showed that the cut converged from the leading edge to the trailing edge of the land as the wires (bristles) crossed the rotor (fig. 5). Wire grooves were clear cut and debris was evident, as is better shown in the enlargement (fig. 6).

The following groove extents in millimeters (inches) were measured in test 1:

| Width at inlet | 1.52 (0.06) |
| Width at center | 1.3 (0.051) |
| Width at outlet | 1.27 (0.05) |

For test 2 the inlet region at the land leading edge was extensive and not readily characterized, but a general convergence pattern was evident. Similar behavior at the leading edge was noted for test 3.

In order to corroborate the optical results, profilometer results for a typical tooth of the 40-tooth rotor were taken. Wear area and groove depth estimates are provided in table III. Values for the extent of the groove in millimeters (inches) are shown in figures 7 to 9 at a resolution of 0.02 mm/division.
Width within 0.1 mm of inlet ........................................ 0.9 (0.035)
Width at center ............................................................. 0.4 (0.016)
Width within 0.08 mm of outlet ........................................ 0.27 (0.011)

It is evident that the optical values for groove extent were much larger than those from the profilometer. The problem is the scale used in defining the groove depth. For example, at a resolution of 0.01 mm/division the width at the center is 1.15 mm (0.045 in.), but at a resolution of 0.02 mm/division the width at the center is 0.4 mm (0.016 in.). At the smaller resolution the extent of the scratched interface generally agrees with the optical values, but at the larger resolution the extent of the scratched interface is not resolved (i.e., detail is lost).

For the surface asperity resolution used herein the optical method better defined the extent (width) of the damaged interface; the profilometer provided the depth. At one-half the depth resolution only the major grooving was defined.

The first profile, labeled “leading edge,” was taken within 0.10 mm (0.004 in.) of the leading edge and shows a broad damage region with deep grooving for test 2 (fig. 8(a)) and test 3 (fig. 9(a)) but a minor amount of material damage for test 1 (fig. 7(a)). The material buildup adjacent to the groove of test 3 probably occurred during rotor-fence rub. The second profile, labeled “mid section,” was taken midway between the tooth leading and trailing edges. The damage of test 2 (fig. 8(b)) and test 3 (fig. 9(b)) was severe, and a twofold cut has developed in the rotor during test 2. Again moderate damaged was noted for test 1 (fig. 7(b)). The third profile, labeled “trailing edge,” was taken within 5 percent of the trailing edge. The grooving seen in the midsection profile carried through with perhaps some sharpeness of the features near the trailing edge (figs. 7(c), 8(c), and 9(c) for tests 1, 2, and 3, respectively).

The brush bristle impact at the leading edge left material deposits that were magnetic (i.e., from the rotor) and rust color (probably Fe$_3$O$_4$) with a spongelike (or cauliflower) appearance (fig. 10); these deposits are readily seen at higher magnification (80X) in figure 11. Debris was generated by surface machining grooves, “whipping” of the leading edge, burnishing, and sharp trailing edges. The deposited materials were fine, porous, “greasy” to the fingers, and readily removed from the rotor; removal from the bristles was not straightforward. Standard degreasing cleaned but not thoroughly, and ultrasonic cleaning was not attempted. The reasoning was to see if these deposits would inhibit the responsive character of the bristles. The debris can affect both the response and the leakage, but neither effect was observed in these tests. Further work here is warranted.

These deposits also indicate rapid wear-in with a long oxidation period for the “machined out” material. The materials deposited on the groove wall at the land leading edge (fig. 11) and on the groove wall at the land trailing edge (fig. 12) had little or no structure; the defraction spectra were peakless.

It is speculated that the bristles were dragged across the land, with “machined” material adhering to the bristle and then “impacted” off the bristle at the leading edge of the next tooth. Some of the materials were deposited within the groove. Black nodule-like debris tended to adhere to the groove wall at the land trailing edge. This black material and rust-colored materials formed in the groove at the land leading edge.

Stainless steel work hardens so that the cut grooves were probably harder than the parent stainless steel and would wear the annealed Haynes 25 bristles. The smooth grooves, the hot spots, and the hot streaking may indicate that a thin layer of stainless steel flowed plastically as it was machined out (figs. 13 and 14). Because of the incursive impact of the toothed rotor and the heated interface, the
Haynes 25 bristles could lose strength, erode, fracture, or pull out as massive debris. But no pullouts or massive debris was found after any of the three tests. At higher magnification (200X) the tips still appear intact without fracture, but wear is evident and oxidation debris appears to be well adhered to the surface (fig. 15). As further evidence of the bristle wear an examination of the bristle tip surface revealed tip grooving (fig. 16), and the severe impacting on the bristles is shown by erratic wear notches on the bristle surface (fig. 17).

The trailing edge of the land was “cut” clean by the brush in all three tests (fig. 18) in stark contrast to the erratic leading-edge surface, which was whipped by the bristles (fig. 19). Of interest is the contrast between the land surface cuts. Test 1 surface cuts were a simple wear scar; those of tests 2 and 3 were multiple grooves with complex surfaces and burnishing (fig. 20). The most rotor damage appeared from test 2 and the most brush damage from test 3, where the rotor was set eccentric.

These tests, although preliminary and only qualitative, begin to mitigate the fear of brush seal disintegration through bristle flexing as over $1 \times 10^9$ cycles were sustained without failure, fracture, or pullout. However, the required flexures are at least an order of magnitude higher with parameters such as surface speed, temperature, pressure, and materials to be considered.

$$\text{Total flexures} = 222 \text{ hr} \times 60 \text{ min/hr} \times 40 \text{ teeth} \times 2600 \text{ rpm} = 1.38 \times 10^9$$

$$\text{Required eccentric shaft flexures} = 10000 \times 60 \times 1 \text{ (flexure/rotation)} \times 20000 \text{ rpm} = 12 \times 10^9$$

$$\text{Required rotor disk flexures} = 50 \times \text{eccentric shaft flexures}$$

However, bristle flexures raise an equally troubling concern over seal life, because brush seals do wear out. Once these seals begin to reach line-to-line contact, their leakage can be equivalent to that of an advanced labyrinth seal. The sealing margin and competitive edge of the worn brush seal begin to fade. New competitive (lower leakage) configurations for labyrinth, damper, honeycomb, feltmetal, and spiral-groove seals are under investigation. It is clear that long-duration testing at elevated surface speeds and working fluid temperatures are required.

**Correlation of Leakage Data**

Although not the primary objective of this experiment, overall changes in brush leakage were estimated from flow checks before and after testing. In order to determine these leakages the 40-tooth rotor was replaced with a smooth-surface, tapered rotor. Runout errors resulting from rotor interchange were unresolved as were those associated with the static eccentricity of test 3. Measurements characterizing the rotor and brush before and after testing are given in table I. The average depth of the brush-cut groove as well as the estimated clearances are given in tables II and III.

Leakage is characterized in figure 21 in terms of volumetric flow rate as a function of pressure drop across the brush seal before and after each of the three tests. Both pretest and post-test results are provided in the same figure. Because this brush seal was damaged (see APPARATUS section), absolute leakage measurements would require weighing, but the relative leakage should be accurate. The interference fits for the brush seal leakage data for pretests 1 and 2 were nearly the same, resulting in corresponding leakages. While taking data it was found that the brush would stiffen and the pressure drops would increase. Data points illustrating hysteresis (typical in brush seals) are shown. After correcting the post-test 2 data for clearance, these test results agreed with those of post-test 1.
Setting the rotor eccentric in test 3 proved a major problem in cross correlating the leakage results. The estimated initial static eccentricity for the smooth rotor was less than 0.15 mm (0.006 in.), and the smooth rotor and the 40-tooth rotor were assumed to be interchangeable at the same spindle loading. However, the rotor rubbed the fence (backing washer) slightly, requiring an initial static eccentricity of 0.36 mm (0.014 in.) and implying a difference in spindle loading. The rotor was reset to an estimated eccentricity of less than 0.025 mm (0.010 in.). Post-test photographs indicated that the dynamic eccentricity was <0.10 mm (<0.004 in.) and clearly illustrated the fence rub (fig. 22).

For test 3 the repositioning of the stator and the differential spindle loading introduced an unaccountable bias that was difficult to estimate in correlating the leakage results. From the data of reference 19 a relation was found for the change in pressure as a function of eccentricity at a fixed volumetric flow rate. Using this relation and corrections for clearance and assuming a pretest static eccentricity of 0.15 mm (0.006 in.) and a post-test static eccentricity of 0.25 mm (0.010 in.) show that the results of test 3 were overcorrected by 20 percent with respect to the results of tests 1 and 2. Future testing requires instrumentation to overcome these positioning errors. Nevertheless, these leakage data indicate that under conditions of severe brush and rotor wear the brush seal leakage increased 30 percent. And, although brush seal performance degraded, the brush seal did not fail.

SUMMARY OF RESULTS

In three separate tests with a 40-tooth tapered stainless steel rotor operating at 2600 rpm and a 38.1-mm (1.5-in.) diameter brush seal with 0.07-mm (0.0028-in.) diameter annealed Haynes 25 bristles set at a nominal 0.076-mm (0.003-in.) radial interference for each test, the following results were obtained:

1. The bristles withstood over $1 \times 10^9$ cycles without pullout, fracture, or massive debris generation.

2. Rotor grooving up to 0.076 mm (0.003 in.) in depth radially with erratic “whipped” leading-edge surfaces followed by convergent grooving to a clean-cut trailing edge was commonplace for each of the three tests.

3. Most of the debris generated was a fine black material that appeared amorphous, but the rust-colored materials were iron rich and magnetic, implying $\text{Fe}_3\text{O}_4$. The debris was “cauliflower” in form and highly porous with low adhesion, except for that which was fine enough to adhere to the bristles. Those fines were not readily dislodged. Nonuniform fines (or oxidation) adhering to the bristles tended to separate the bristles, increasing porosity, and would enhance leakage paths.

4. Radial bristle losses up to 0.2 mm (0.008 in.) were demonstrated, which if left uncorrected would lead to equivalent or higher leakages than those of labyrinth seals. Bristle loss at elevated surface speeds and temperatures requires further study.

5. Generated debris can impair bristle motion and alter leakage, but within the limitations of this experiment these considerations were not a problem. They remain as issues to be resolved.

6. Under conditions of severe rotor-stator interface damage, the brush seal leakage performance degraded 30 percent, but the seal did not fail.
REFERENCES

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<td>Rotation, deg</td>
<td>0</td>
<td>45</td>
<td>0</td>
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<td></td>
<td></td>
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<td>1.494</td>
<td>1.4918</td>
<td>1.4926</td>
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<td>1.497</td>
<td>1.496</td>
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<td>1.5058</td>
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<td>1.5058</td>
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<td>1.5041</td>
<td>1.5037</td>
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<td>After test 3(^c)</td>
<td>1.504</td>
<td>1.514</td>
<td>1.512</td>
<td>1.5064</td>
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<td>Change, in.</td>
<td>-0.0018</td>
<td>0.0079</td>
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\(^a\)Total test time, 70.3 hr.
\(^b\)Total test time, 43 hr.
\(^c\)Total test time, 109 hr.
TABLE II—ADDITIONAL TEST AND GEOMETRY INFORMATION

[Seal fence inside diameter, 1.543±0.0005 in.
Dimensions are in inches.]

(a) 40-Tooth rotor

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<tr>
<th>Position</th>
<th>Tooth-to-tooth diameter</th>
<th>Gap-to-gap diameter</th>
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<td>1.523±0.0005</td>
<td>1.485±0.0005</td>
</tr>
<tr>
<td>Bottom of rotor</td>
<td>1.491±0.003</td>
<td>1.483±0.003</td>
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</tbody>
</table>

<table>
<thead>
<tr>
<th>Test case</th>
<th>Top-of-brush wear surface</th>
<th>Bottom-of-brush wear surface</th>
<th>Average</th>
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<tr>
<td>1</td>
<td>0.605</td>
<td>0.632</td>
<td>0.618</td>
</tr>
<tr>
<td>2</td>
<td>.461</td>
<td>.508</td>
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<tr>
<td>3</td>
<td>.325</td>
<td>.303</td>
<td>.344</td>
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(b) Smooth rotor

<table>
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<tr>
<th>Test case</th>
<th>L*</th>
<th>Smooth-rotor diameter</th>
<th>Free brush diameter</th>
<th>Concentric radial clearance</th>
<th>Static eccentricity</th>
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<td>1.4992</td>
<td>1.4932</td>
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<td>1.4992</td>
<td>1.4958</td>
<td>-0.0017</td>
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<tr>
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<td>L2</td>
<td>1.5046</td>
<td>1.4958</td>
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<td></td>
<td>1.5046</td>
<td>1.5049</td>
<td>.0001</td>
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<td>L3</td>
<td>1.5105</td>
<td>1.5049</td>
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<tr>
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<td></td>
<td>1.5105</td>
<td>1.5091</td>
<td>-.007</td>
<td>.013</td>
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*Corresponds to equivalent axial positions of 40-tooth rotor.
### TABLE III—PROFILOMETER RESULTS FOR 40-TOOTH Rotor, Tests 1, 2, and 3

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<tr>
<th>Location</th>
<th>Test</th>
<th>Peak groove depth, $\mu$m</th>
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<td>22</td>
<td>24 910</td>
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<td></td>
<td>2</td>
<td>130</td>
<td>95</td>
<td>141 680</td>
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<tr>
<td></td>
<td>3</td>
<td>130</td>
<td>70</td>
<td>114 370</td>
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<td>Midsection</td>
<td>1</td>
<td>30</td>
<td>17</td>
<td>7 652</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>70</td>
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<td></td>
<td>3</td>
<td>70</td>
<td>27</td>
<td>56 493</td>
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<td>1</td>
<td>25</td>
<td>12</td>
<td>6 610</td>
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<td></td>
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<tr>
<td></td>
<td>3</td>
<td>67</td>
<td>30</td>
<td>56 169</td>
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---

Figure 1.—Circular brush seal. (Courtesy of Cross Mfg. Ltd.)
Figure 2.—Geometry of tapered, 40-tooth rotor.
Figure 3.—Rotor prior to tests (40 lands).

Figure 4.—Brush seal prior to tests (270° mark).
Figure 5.—Rotor surface after test 1. (Arrow shows direction of rotation.)

Figure 6.—Rotor land and groove after test 1.
Figure 7.—Profilometer traces for 40-tooth rotor (test 1).

Figure 8.—Profilometer traces for 40-tooth rotor (test 2).
Figure 9.—Profilometer traces for 40-tooth rotor (test 3).

Figure 10.—Rotor land with debris and rub scars (test 2).
Figure 11.—Rotor leading-edge debris formation (test 2).

Figure 12.—Rotor trailing-edge surface grooving and debris (test 3).
Figure 13.—Rotor leading edge, surface machining, and hot spots (test 3).

Figure 14.—Rotor land hot streaks, hot spots, and surface machining (test 3).
Figure 15.—Brush bristle tips with debris (test 1).

Figure 16.—Brush bristle tip wear patterns (test 2).
Figure 17.—Brush bristle tips and damage (test 1).

Figure 18.—Rotor trailing edge (test 3).
Figure 19.—Rotor leading edge (test 2).

Figure 20.—Rotor trailing edge (tests 1, 2, and 3).
Figure 21.—Pre- and posttest leakage results for smooth rotor.

Figure 22.—Fence damage sustained during test 3.
A split-ring brush seal was fabricated, installed between two labyrinth-honeycomb shroud seals, and tested in the fourth-stage turbine of a T-700 engine. The annealed Haynes 25 bristles rubbed directly against the nonconditioned, irregular René 80 turbine blade shroud surface. A total of 21 hr of cyclic and steady-state data were taken with surface speeds to 335 m/s (1100 ft/s) and shroud temperatures to 620 °C (1150 °F). Wear appeared to be rapid initially, with an orange flash of hot brush fragments during the first engine startup, to minimal after 10 hr of operation. The brush survived the testing but experienced some bristle pullouts and severe bristle wear; some turbine interface wear and possible material transfer was noted. Future design concerns center on tribological behavior at the interface with or without lubricants.

**INTRODUCTION**

Engine testing of brush seals has been reported (e.g., Rolls Royce (ref. 1) and Allison (ref. 2)) that demonstrated performance increases relative to labyrinth seals. These brush seal systems had smooth rotor interfaces (<25 rms) and operated at moderate temperatures and surface speeds. Even though these tests were successful, concern over catastrophic failure of the brush, such as a loss of bristles when subjected to high surface speeds at elevated temperatures, has not been resolved.

The objectives of this program were first to demonstrate that a well-designed and manufactured brush seal could survive the "pounding" of an irregular rotor surface without catastrophic failure, second to illustrate the concept of running a combined brush and labyrinth seal system, and third to acquire metallographic data on bristles subjected to such an environment.

**EXPERIMENTAL BRUSH CONFIGURATION AND INSTALLATION**

A cross-sectional view of the split-ring brush seal configuration is illustrated in figure 1. A major problem in designing retrofit seals is consistency of hardware measurements, and for this experimental engine the seal was crafted to fit.

In order to fit into the existing T-700 engine fourth-stage turbine shroud, the design was required to fit into a radial clearance about half that normally used for brush seals. The 0.071-mm (0.0028-in.) diameter, Haynes 25 bristles were angled 43° to 50° to the interface with about 2500 per inch of circumference (98.4 per millimeter of circumference). The backing washer (or fence) was angled 19° to match the slope of the turbine shroud. The design clearance was -0.51 mm (-0.02 in.) but could range to -1.27 mm (-0.05 in.) diametral (the uncertainty reflecting that of the engine geometry) with an outside diameter of 333.9 mm (13.146 in.) and an inside diameter of 322.3 mm (12.690 in.).
Figure 2 shows several views of the split-ring brush seal, illustrating the joint and the restraining pin hole. Figure 3 shows the unusual brush cross section that was crafted to fit the turbine shroud between the two labyrinth-honeycomb seals. Figure 4 shows a closeup view of the installed brush; and figure 5, an overall view of the installed brush. Figure 6(a) shows the pressure tap locations in one of the shrouds. A thermocouple was installed in each shroud (fig. 6(b)); three of the four were functional. Figures 6(c) and (d) show views of the shroud ring and instrumentation lines.

Assembly of the turbine with the shroud required forcing the brush past the upstream labyrinth tooth without any visual or instrumented guidelines; see figure 7 (power turbine). Forcing the brush over the labyrinth tooth spread the bristles axially into the upstream direction. This type of spreading alters the bristle packing configuration, but the extent of alteration and the degree of spreading are unknown. Post-test results indicated that perhaps two to three upstream bristle rows remained spread with possibly one downstream bristle row in disarray. Still the brush was resilient because the remaining rows appeared to be in position. The flexibility of a brush seal and the abuse it can withstand appear to be significant.

With the brush installed, the turbine shaft was difficult to rotate, requiring 14.7 N-m (130 in.-lbf) of torque. This was a major concern because heat generation could be sufficient to melt the materials at the interface. The geared tooth rotor results (ref. 3), including material smearing, cutting, and local hot spots, indicate that high heat loads and temperatures could be present but would be confined to the interface, with the lowest heat-sinking element (the bristles) absorbing the energy. Therefore, the bristles would fail, but the effects on the power turbine should be benign.

ENGINE OPERATIONS

The T-700 turbine section was assembled and the brush seal test was “piggybacked” on the break-in of the engine. Operations consisted of the standard break-in procedures with data taken under both steady and cyclic conditions. The engine was operated a total of 21 hr, including break-in, steady state, and 10 hr of cycling between ground and flight idle (4-min ground idle and 5-min flight idle). Turbine speeds were 10 000 and 20 000 rpm, and average fourth-stage turbine shroud temperatures were 455 and 566 °C (850 and 1050 °F), respectively. Maximum shroud temperatures were limited to 621 °C (1150 °F). The turbine inlet temperatures were about 139 deg C (250 deg F) higher. The pressure drop measurements across the brush were up to 0.007 MPa (1 psia) and varied from shroud to shroud. An assessment of the effect of the brush seal on engine performance was inconclusive and remains to be investigated further. Neither radial nor axial positions of the rotor were monitored, but such position sensors should be an integral part of the engine dynamics.

Because of concern over the 14.7 N-m (130-in.-lbf) installed torque that was required to rotate the power turbine shaft, after about 10 hr of engine operations the compressor and the power turbine were decoupled. The turbine shaft turned freely but not in reverse. The turbine assembly has 50 shrouded blades with irregularities (radial, to 0.229 mm (0.009 in.); circumferential, to 0.076 mm (0.003 in.); and axial, to 0.051 mm (0.002 in.)) representing protrusions into the brush and the spaces between the blade pairs. It is not known how many cycles were required to “free the bristles,” but at 10 000 rpm and with 24 irregular asperities impacting each bristle (4000 impacts/s at a surface speed of 168 m/s (550 ft/s)) it is assumed that brush break-in was rapid. The annealed Haynes 25 bristles rubbed against hardened René 80 blades and probably wore rapidly during the initial stages of engine break-in.

Furthermore, and of significance to engine designers, a flash was noted upon initial engine ignition that was concluded to be expulsion of brush fragments. This is important because critical components
must be protected against initially high levels of debris generation. Analysis of these and other fragments showed severe oxidation with some degree of stiffness remaining. These fragments are not passive debris; they can cause damage to critical components. The only debris noted in the gear-tooth rotor study (ref. 3) was a “lubricant powder.” Thus, surface speed, rotor roughness, and brush construction play a major role in determining the spectrum of debris generation.

RESULTS AND DISCUSSION

In any potentially destructive situation one attempts to preserve the critical components. Brush bristle wear would degrade performance, but failure of the turbine or a shaft (depending on seal location) could result in engine loss, perhaps catastrophic. So the brush seal becomes the sacrificial component, not only in this case but when running against a coated shaft. The brush seal would then be replaced at discrete intervals, such as during overhauls.

For these tests the brush rubbed the turbine blade shroud asperities smooth and did provide a distinct wear track, perhaps through transfer of material. However, no direct damage was ascribed to the turbine blade shrouds. The engine was immediately returned to service.

Before proceeding to discuss post-test results, we return to the installation of the brush into the power turbine shroud. Figures 4, 5, and 7 show views of the installed brush seal. The brush was designed for an interference of 0.51 mm (0.020 in.) diametral. The actual interference could not be determined, but estimates of the pretest brush clearance were −0.51 to −1.27 mm (−0.02 to −0.05 in.) diametral. Measurements of the shrouds differed as did those for the rotor. Although the differences were only a few thousands of an inch (mils), they represented a significant percentage of the clearance gap. It was also determined that individual blade sets could have a step change of 0.229 mm (0.009 in.) from one blade set to the next. These surface irregularities are shown in the post-test photograph (fig. 8).

Upon initial engine startup, an orange burst was noted and was assumed to be expelled brush bristles (i.e., those that were inadequately attached, were pulled out by rotor irregularities, or were embedded within the blade row gaps during the blind installation and “snapped” or “yanked” or “bent” aside during engine break-in). Residual bristles from the exhaust were photographed (fig. 9). Although they appeared to be highly oxidized and stressed, they were curly and still wirey. The number of residual bristles decreased with operation until none were noted. It is assumed that at this time the bristles and the rotor were in nearly line-to-line contact (i.e., rubbed in). Precooling the bristles during the initial rub-in may mitigate bristle loss and the orange burst.

Turbine speeds to 20 000 rpm and shroud temperatures to 620 °C (1150 °F) were commonplace. These conditions provided an interface speed of 335 m/s (1100 ft/s) or a temperature-velocity (TV) product of over (1100)² with the global target of about (1500)² (in U.S. customary units, feet per second per degree F).

Further assessment of figure 8 shows that the leading edges of the blade sets were polished. Some brush wear was noted and expected because René 80 is hard relative to the annealed Haynes 25 and the heat-sinking capacity of the brush is very small relative to that of the rotating blade sets. The surface irregularities at the rubbing interface can be seen. Although there was some evidence of material transfer, no metallurgical samplings or rotor measurements were taken because of the tight program schedules for the engine operations. This was a major error; however, if there comes a time when the rotor can be
looked at, some of the transferred materials may be found still embedded in the rotor even after it has undergone other program tests for General Electric Co.

Figure 10 illustrates bristle spreading after testing, with a central core of bristles rubbed (probably clip cut and worn to shape). Although the environment was hostile, the brush did not disintegrate, but bristle pullout could be noted in a few places. Some upstream bristles (two or three rows) show spreading and perhaps one row downstream (toward the exhaust). The remainder of the bristles show wear (or cutting plus wear). Detailed estimates of the bristle stubble heights are given in figure 11(a) as taken from the set of photographs in figure 11(b) corresponding to positions (joint, J+1, J+1.5, J+2, J+2.5, J+3, J+3.5, J+4, and J+4.5) shown in figure 11(a). The last two photographs in figure 11(b) correspond to the minimum stubble height, where the rotor actually rubbed the fence (position J+3); the view is looking toward the bristle stubbles to show the rubbed fence. Figure 11(c) shows wear track and fence rub, and figure 11(d) shows the joint wear track.

The following measured diametral parameters in millimeters (inches) were used to establish seal clearances:

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<tr>
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<th>Value</th>
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<td>Pretest brush diameter (no taper)</td>
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<td>Post-test brush diameter (tapered)</td>
<td>324.15 (12.762)</td>
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<td>Differential</td>
<td>2.36 (0.093)</td>
</tr>
<tr>
<td>Pretest rub interface diameter</td>
<td>322.30 to 322.81 (12.689 to 12.709)</td>
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<tr>
<td>Brush pretest interference</td>
<td>0.51 to 1.27 (0.02 to 0.04)</td>
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<tr>
<td>Labyrinth cold clearance</td>
<td>2.29 to 2.46 (0.09 to 0.097)</td>
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<td>Bright region diameter (fig. 8(a))</td>
<td>323.42 (12.733)</td>
</tr>
<tr>
<td>Differential</td>
<td>0.74 (0.029)</td>
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<tr>
<td>Stubble height (fig. 11(a))</td>
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<td>Possible material transfer</td>
<td>0.25 to 0.5 (0.01 to 0.02)</td>
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<tr>
<td>Possible engine eccentricity</td>
<td>0 to 0.8 (0 to 0.03)</td>
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<tr>
<td>Blade shroud height variation</td>
<td>0 to 0.23 (0 to 0.009)</td>
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The average diametral clearance estimates in millimeters (inches) are as follows:

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<th>Parameter</th>
<th>Value</th>
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<tbody>
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<td>Pretest brush clearance</td>
<td>-0.51 to -1.3 (-0.02 to -0.04)</td>
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<tr>
<td>Post-test brush clearance</td>
<td>0 to 0.8 (0 to 0.03)</td>
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<tr>
<td>Post-test labyrinth clearance</td>
<td>2.3 to 2.5 (0.09 to 0.10)</td>
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The engine parameters are as follows:

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<td>Turbine speeds to 20 000 rpm, m/s (ft/s)</td>
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</tr>
<tr>
<td>Maximum turbine shroud temperatures, °C (°F)</td>
<td>620 (1150)</td>
</tr>
<tr>
<td>Temperature-velocity product (approximate; in U.S. customary units ft/s°F; future target, (1500)²)</td>
<td>(1100)²</td>
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</table>

Details of the bristles (fig. 12) show an ingrained wear pattern that is characteristic of a high spot in the rotor which cuts a shallow groove as it wears in. Furthermore, the rotor ran eccentric with respect to the seal either during cycling or steady state or both. Plots of bristle measurements show rubbing of the seal ring at 180° to the pinned point and a step across the joint where the end of the split seal rubbed the rotor.
The blind installation and operation made it difficult to assess intermediate states of wear or the health of the brush or the turbine shroud/brush interface. Although accelerometer measurements were in bounds, no detailed information concerning the orbital dynamics was available.

Metallographic results (fig. 13) illustrate some material migration along the bristle and material transfer both from and to the surface. Material smears seem to be in line with a softer material rubbing a harder material even to the point of melting. Thus, one would conclude that the interface became very hot, but the interface followed the classic Block slider problem, where the penetration depth (radial) is very small. Thus, the thermal effect at the interface appeared to be topical, wearing the brush bristles until line contact with the rotor and smear transfer of both materials occurred. Such evidence is presented in figure 14, for an individual bristle that was clipped from the brush. The clipped end was removed from the interface, and the worn end is representative of interface materials. There are material smears, oxidized spots, and apparent pits. It is not clear how the irregularities of the interface affected these results, but it is clear that materials were transferred.

Metallographic analysis of the sectioned brush will be completed and reported later.

Derby and England (ref. 4) reported excellent brush bristle and coating wear for Alloy A (Ni-Cr-Al-base superalloy solid-solution strengthened) bristles and Triboglide coating. Alloy A is being used in gas turbine hot spots and develops a tenacious \( \text{Cr}_2\text{O}_3 \) and \( \text{Al}_2\text{O}_3 \); yittria-modified oxide layer. Triboglide is a chromium carbide (CrC) containing additives of 12 wt% barium and calcium fluoride solid lubricants. Triboglide is based on the work of Harold Sliney at NASA Lewis but has no silver additive. The tests were performed with 1200 °F air.

Atkinson and Bristol (ref. 5) report better wear for a cobalt alloy rubbing against chromium carbide at room temperature, but their high-temperature (480 °C) result shows nearly equivalent wear for either the cobalt- or the nickel-base alloy. However, the Co-alloy/CrC combination had less leakage under dynamic conditions and better wear at room temperature. The tests were conducted to simulate a CT7-9 compressor discharge seal. The brush was 129 mm in diameter and of standard Cross Mfg. construction.

It is apparent that the composition of both the coating and the bristles needs to be characterized with respect to the working fluid, the operating conditions, and the component life requirements. The importance of surface conditions must be emphasized. Wear decreases after operation because the brush rubs a smoother surface and bristle wear decreases line loading.

Obviously, tribological pairing is important and references 4 and 5 present a good initial look into these problems. Limitations on speed, temperature, and preloading have to be established. Furthermore, limitations on surface asperities have to be established for expedient or commercial engines even though it has been demonstrated that direct bristle rubbing of a smooth shaft could be acceptable for expedient engines (ref. 6).

**SUMMARY OF RESULTS AND CONCLUSIONS**

A split-ring brush seal installed between two labyrinth-honeycomb shroud seals was tested in the fourth-stage turbine of a T-700 engine. The following results were obtained and conclusions drawn:
1. Properly designed brush seals have sufficient integrity to withstand highly irregular surface operations at surface speeds to 335 m/s (1100 ft/s) and shroud temperatures to 620 °C (1150 °F) with a non-centered turbine orbit during steady and cyclic loading.

2. Upon initial engine startup, bristle debris can be expected mostly in the form of fines and some larger elements. The nature and amount of debris should depend on the construction, the surface characteristics (e.g., asperities), the temperature and velocity of the interface, and the bristle preload. Critical components must be protected.

3. The post-test clearance was estimated to be line to line to 0.8 mm (0.03 in.), indicating a well-worn but still functional seal configuration. Accurate determinations of the rotor and stator dimensions along with dynamic displacement measurements are necessary for assessing bristle wear characteristics and seal clearances. A plot of bristle stubble height versus circumferential position revealed some characteristics of the rotor and engine operations.

4. Wear is expected to be initially rapid, then steady, and subsequently decreasing with time of engine operation. Cyclic operations cause more rapid wear of the bristle/rotor interface. Material transfer, smearing, and pitting of the interface are commonplace.

5. Installation torques can be high, but rub-in torques are low. Rotor reversals are not permitted.

6. Tribological pairing is important, and limitations on speed, temperature, preload, and asperities have yet to be established even though direct rubbing of a smooth shaft of an expedient engine appears plausible.

7. Although high installation torques (14.7 N-m; 130 in.-lbf) probably contributed to high bristle wear, the effects on the power turbine were benign even though heat generation and shear were sufficient to transfer materials at the interface. The René 80 is hard and has large heat capacity, and the Haynes 25 bristles are annealed and have small heat capacity. Therefore, the brush bristles failed first.

8. The pressure drop measurements across the brush seal were up to 0.007 MPa (1 psia), but the effect of the brush seal on engine performance was inconclusive and requires further assessment. Radial and axial rotor sensor position monitoring is recommended.

9. Metallographic studies of the brush and rotor are being completed.

REFERENCES
During Installation
brush forced onto rotor (no rotation)

During disassembly brush forced off rotor past labyrinth tooth (no rotation)

Figure 1.—Cross-sectional view of split-ring brush seal configuration. (Brush design with -0.020 in. interference. Dimensions are in inches.)
(a) Overview of brush seal.

(b) Edge view of brush seal.

(c) Split end view.

Figure 2.—Split-ring brush seal.
Figure 3.—Brush seal cross section crafted to fit turbine shroud between two labyrinth-honeycomb seals.

Figure 4.—View of installed brush seal.
Figure 5.—Overview of installed brush seal and power turbine housing.
Figure 6.—Pressure tap and thermocouple locations on shroud seal.

(a) Pressure tap hole.

(b) Thermocouple mount and pressure tap lines.

(c) Shroud ring with three seal segments and instrumentation lines — downstream view.

(d) Shroud ring with three seal segments and instrumentation lines — upstream view.
Figure 7.—Schematic of power turbine.

Figure 8.—Fourth-stage turbine after testing, showing polishing of leading edges.
Figure 9.—Typical brush seal debris found in engine exhaust duct.
(b) Continued.

Figure 9.—Continued.
Figure 9.—Concluded.

Figure 10.—Post-test view of brush seal showing bristle spreading and core of rubbed bristles.
Figure 11.—Post-test bristle stub height and backing washer rub. Bristle diameter, 0.0028 in.
Figure 11.—Continued.

(b) Concluded.
Figure 11.—Concluded.

(c) Wear track and fence rub.

(d) Joint wear track.
Figure 12.—Details of brush seal wear pattern.
Figure 13.—Post-test metallographic results for single bristle.

(a) Bristle 1 spread away from wear track.

(b) Analysis of bristle 1.
(c) Bristle 1 at increased resolution.

Figure 13.—Concluded.
Figure 14.—Post-test metallographic results for bristle tip from wear track.
MSFC Seal and Fluid Film Bearing Activities

Presented by Ted Benjamin
CFD Branch
Aerophysics Division
Structures and Dynamics Laboratory
George C. Marshall Space Flight Center
National Aeronautics and Space Administration

Presented August 6, 1992 at Brush Seals Systems Workshop
Lewis Research Center
National Aeronautics and Space Administration
Overview

- Highly-instrumented SSME HPOTP with hydrostatic bearing on Technology Test Bed
- Cryogenic fluid-film bearing tester
- Damping seal rotor support
- Damping seals for turbomachinery
- Experimental verification of rotordynamic analysis
- In-house CFD analysis

Objective: Demonstrate feasibility of hydrostatic bearings for high pressure cryogenic turbopumps

- Joint Rocketdyne IR&D/MSFC activity
- Retrofit HPOTP pump-end with hydrostatic bearing for ball bearings
- Operated engine at multiple power levels with variable ramps and multiple LO₂ inlet conditions
- Bearing accumulated 723 seconds in 7 tests
- Rotordynamic stability maintained during all operational phases
- Proximity probe data indicated shaft contacted wall during both start and shutdown
- Post-test bearing wear data indicated minimum wear of 0.00109 inches over 7 test series
MSFC Seal Activities

Cryogenic Fluid Film Bearing Tester

Objective: Procure externally fed fluid-film bearing tester to test Earth-to-Orbit sized turbopump bearings in cryogenic fluids allowing for evaluation of bearings in realistic turbopump environment

- Should obtain repeatable and usable data
- Fluids of LH₂, LO₂, H₂O, and surrogates
- Only facility available to evaluate impartially and fully fluid film bearing concepts in cryogenic fluids

Knowledge to be gained:
- Important rotordynamic coefficients
- Material characteristics, tribology of rubbing components
- Basic load capacities

MSFC Seal Activities

Damping Seal Rotor Support

Objective: Obtain test rig to verify internally fed damping bearing predictions, validate rotordynamic codes

- Water as working fluid
- Experimentally determine dynamic coefficients and compare to in-house analytical predictions
- Include parametric changes to mechanical dimensions of seal and bearings as well as to fluid inlet and exit conditions
- Develop understanding of bearing performance as a function of parametric changes and analysis
- Preliminary design complete
MSFC Seal Activities

Damping Seals for Turbomachinery

Objective: Verify dynamic coefficient predictions of damping seals

- Rig used to determine dynamic coefficients of axially fed damping seals
  - 8 seal configurations tested
- Water as working fluid
- In-house bulk-flow codes closely match most of experimentally determined dynamic coefficients
- Performed at Wyle Laboratories

MSFC Seal Activities

Experimental Verification of Rotordynamic Analysis

Objective: Experimentally evaluate damping rotor supports for improvements in suppression of rotor whirl in turbopump

- Tests of 2 externally and 2 internally fed damping bearings in LO$_2$ surrogate fluid
- Provide head-to-head comparison between 4 damping bearing configurations
- Performed under contract to Rocketdyne
- Best combinations of bearing characteristics is candidate for replacing ball bearings in turbine end of SSME HPOTP
In-house CFD Analysis

Objective: Mature CFD for fluid film applications to feed and support one-dimensional flow models

- Three-dimensional analysis on 60° slice of bearing
- Single-phase incompressible Navier-Stokes analysis assuming constant-$\gamma H_z$
- Rotational Reynolds number based on annulus width $= 4.8 \times 10^4$
- Multi-block solution in progress with FDNS code (Chen)
- $K-\varepsilon$ turbulence models
PARTICLE TRACKS
HLS 59/79 Hydrostatic Soaking
Preliminary Solution—45-degree Constant Inlet Angle

PARTICLE TRACKS
HLS 59/79 Hydrostatic Soaking
Preliminary Solution—45-degree Constant Inlet Angle

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MSFC Seal Activities

In-house CFD Analysis
Determination of Rotordynamic Coefficients

- Obtained from axisymmetric CFD results using REFLEQS (CFDRC)
  - Zeroth-order solution
- Presently using perturbation method of Dr. Erian Baskharone (Texas A&M University) and Dr. Steve Hensel (former Texas A&M graduate student) to calculate coefficients
- Currently being applied to ATD HPOTP balance piston cavity
MBFC Seal Activities

Summary

- Technology Test Bed of HROTP hydrostatic bearing was successful
- OAST tasks support range of seal and bearing configurations
  - Internally fed
  - Externally fed
  - Axially fed
  - Emphasis on rotordynamic coefficients and seal performances
- CFD analysis in progress for seal-flow evaluation
Aggressive pursuit of increased performance in gas turbine engines is driving the thermodynamic cycle to higher pressure ratios, bypass ratios, and turbine inlet temperatures. As these parameters increase, internal air system and resultant thermodynamic cycle losses increase. This conflict of reducing internal airflows while increasing thermodynamic efficiency and performance is putting more emphasis on improvements to the internal flow system. One improvement that has been and continues to be pursued by the Air Force for both man-rated and expendable turbine engine applications is the brush seal. This presentation briefly describes both past and current brush seal research and development programs and gives a summary of demonstrator and developmental engine testing of brush seals.

OUTLINE

- PAST R&D PROGRAMS
- CURRENT R&D PROGRAMS
- DEMONSTRATOR ENGINE BRUSH SEALS
- F119 BRUSH SEALS
- SUMMARY
PAST AF BRUSH SEAL R&D PROGRAMS

- **ALLISON: HIGH TEMPERATURE BRUSH SEALS**
  - Inconel X-750 bristles wear better than Haynes 25 in hot dynamic contact with chrome-carbide journal
  - Initial build-up interference effects static leakage
  - Brush seal with hot running clearance has less leakage than 4-knife lab seal at same pressure ratio
  - Report #: WL-TR-91-2005

- **TELEDYNE: BRUSH SEAL DESIGN**
  - Brush seals provide a factor of 3 or more reduction in leakage flow over conventional lab seals
  - Brush seals retain a significantly reduced leakage over lab seals for time periods of limited-life engines
  - Brush seals can survive shaft excursions of over 0.025 inches without any performance loss
  - Report #: WRDC-TR-90-2123

PAST AF BRUSH SEAL R&D PROGRAMS (cont.)

- **TEXAS A&M: BRUSH SEAL ROTORDYNAMICS**
  - Last stage of seal group develops higher pressure drop than previous stages
  - Increasing inlet tangential velocity increases leakage slightly
  - Cross-coupled stiffness coefficient very low and generally negative (stabilizing)
  - Whirl frequency ratio indicates brush seal is extremely stable
  - Rotordynamic coefficients independent of seal spacing and inlet tangential velocity
  - Comparison with 8-cavity lab seal indicate brush seal will generally improve rotordynamic characteristics
  - Report #: WL-TR-91-2013 (original) corrected report in progress
CURRENT BRUSH SEAL R&D PROGRAMS

- EG&G SEALOL
  - Brush Seal Development Program
  - Advanced Brush Seal Development Program (New Start)
- PRATT & WHITNEY
  - High Speed Brush Seal Development Program (New Start)
- IN-HOUSE
  - Brush Seal Leakage Flow Modeling
  - Brush Seal Compressor Shroud Test

BRUSH SEAL DEVELOPMENT PROGRAM
EG&G SEALOL

OBJECTIVE:
Develop a comprehensive design methodology for application of brush seals to man-rated engines

APPROACH:
Conduct parametric testing of design variables for brush seals to define performance, fatigue, oxidation, and wear characteristics

ACCOMPLISHMENTS:
- Examined effect of bristle angle, bristle length, stiffness, staging, and packwidth on hysteresis, ΔP capability, leakage, wear
- Significant hysteresis with speed, but not pressure
- Increased packwidth gave higher ΔP capability, lower leakage
- Multiple Stage Brush Seal Performance
  - Leakage reduction
  - Unequal pressure distribution
    - May be controlled by using mixed stiffness designs
    - Staging with higher packwidth seals most effective
- Tribopair Test and Evaluation
- Evaluating Advanced Designs to Reduce Hysteresis
- Designing Full-Scale Seal for Demonstrator Engine Test

PROJECT ENGINEER: Capt Connie Dowler, 513-255-8210
ADVANCED BRUSH SEAL DEVELOPMENT PROGRAM
EG&G SEALOL

OBJECTIVE:
Develop a comprehensive design methodology for application of advanced, high performance brush seals in man-rated engines

APPROACH:
Conduct experimental characterization of seal design and materials pairs and CFD modeling to maximize single- and multi-stage brush seal ΔP capability and axial and radial excursion accommodation. Investigate feasibility of non-contacting brush seal.

ACCOMPLISHMENTS:
New Start

PROJECT ENGINEER: Lt Carolyn Sunderland, 513-255-8210

HIGH SPEED BRUSH SEAL DEVELOPMENT PROGRAM
Pratt & Whitney

OBJECTIVE:
Provide verification of advanced brush seal technology needed to enable continued application of brush seals in IHPTET Phase II demonstrator engines.

APPROACH:
Conduct an application study using IHPTET Phase II engine design and mission flight cycle to determine surface speed and temperature requirements for brush seals. Design and fabricate brush seals for rig testing to verify their capability to operate at IHPTET Phase II conditions (~ 1400 fps, 1400 F).

ACCOMPLISHMENTS:
New Start

PROJECT ENGINEER: Lt Carolyn Sunderland, 513-255-8210
BRUSH SEAL LEAKAGE FLOW MODEL
FLOW MODEL APPROACH

- 1-D MODEL, WITH RADIAL AND AXIAL FLOW CONSIDERED
- FLOW CORRELATIONS FROM KNUDSEN AND KATZ
  - Laminar Flow
  - Turbulent Flow
  - Transition Flow
- SINGLE CORRELATING PARAMETER: EFFECTIVE THICKNESS
- MODEL 1
  - Linear
  - Square Array Bristle Bed
- MODEL 2
  - Linear
  - Hexagonal Pack Bristle Bed
- MODEL 3
  - Modification of Model 2 to Account for Curvature Effects
  - Effective Thickness Constant Between Journal and Mean Diameter
  - Bristle Bed Configuration Varies
    • Increased Transverse Bristle Spacing
    • Increased Leakage Flow Area at Mean Diameter
    • Hexagonal Pack Bristle Bed

TYPICAL MODEL PERFORMANCE
CHARACTERISTICS

- SHAPE OF \( \phi \) VERSUS \( P_r \) IS EXPECTED CHARACTERISTIC CURVE
- FLOW INCREASES WITH \( B \) AS THE BRISTLE PACK OPENS UP
- TRANSITION FROM LAMINAR TO TURBULENT FLOW NEAR \( P_r = 2 \)
LEAKAGE PERFORMANCE DATA

- HYSTERESIS EFFECT REMOVED
- ALLISON DATA ARE AVERAGED RESULTS FOR SEVERAL SEALS
- TELEDYNE CAE DATA ARE FOR A BASELINE BRUSH SEAL
- CROSS DATA PROVIDED CHECK ON EFFECT OF BRISTLE DENSITY
- NASA LEWIS DATA PROVIDED CHECK ON SEAL DIAMETER EFFECT

BRUSH SEAL LEAKAGE FLOW MODEL
MODEL RESULTS

- WIDE RANGE OF B INDICATIVE OF DIFFERENCE IN ACTUAL SEAL THICKNESS
- B/Bmin INDICATOR OF BRUSH SEAL LEAKAGE EFFECTIVENESS
- EG&G DOUBLE PACKWIDTH SEAL LESS EFFICIENT THAN STANDARD DENSITY SEAL
- CROSS SEAL VERY EFFICIENT
- NASA SEAL LESS EFFICIENT THAN LARGER DIAMETER SEALS
BRUSH SEAL COMPRESSOR SHROUD TEST

- PART OF ADLARF TEST PROGRAM IN COMPRESSOR RESEARCH FACILITY
- TENTATIVELY SCHEDULED TO TEST JAN 93
- INVESTIGATING CAPABILITY OF BRUSH SEAL SHROUD TO IMPROVE
  - BLADE VIBRATIONS (DAMPING)
  - STALL MARGIN
  - EFFICIENCY
- PROJECT ENGINEER: Lt Carolyn Sunderland, 513-255-8210

DEMONSTRATOR ENGINE BRUSH SEAL TESTING

- TESTING TO DATE:
  - PRIMARILY IN TURBINE SECTION
  - HAYNES 25 BRISTLES
  - CHROME CARBIDE OR ALUMINUM OXIDE COATING
  - 20 TO 80% REDUCTION IN LEAKAGE OVER LAB SEALS
  - REDUCED HEAT GENERATION
  - GENERALLY GOOD DURABILITY
  - MAX CONDITIONS: 1275 FPS, 1130 F, 55 PSI ΔP
- FUTURE TESTING:
  - PLANNED FOR ALL DEMO ENGINES (ATEGG, JTDE, JTAGG, ETEC)
  - COMPRESSOR AND IGV LOCATIONS
  - BRUSH SEAL SHROUD
  - HIGHER SURFACE SPEED AND TEMPERATURE (>1400 F, >1400 fps)
F119 BRUSH SEALS

- BILL OF MATERIALS
  - 3 STATIC SEALS
  - HPT & LPT SHROUD

- TECHNOLOGY TRANSITION PLANS
  - HPT (3 Locations)
  - LPT (2 Locations)
  - REPLACE LAB SEALS WITH BRUSH SEALS AT ALL COMPRESSOR INTERSTAGE LOCATIONS
  - 0.9% TFSC IMPROVEMENT (TOTAL)

SUMMARY

- AF COMMITTED TO DEVELOPING AND TRANSITIONING BRUSH SEAL TECHNOLOGY
- EMPHASIZING BRUSH SEAL RIG TESTING (CONTRACT AND IN-HOUSE)
- PUSHING FOR INCORPORATION OF BRUSH SEALS IN ALL DEMONSTRATOR ENGINES
- WORKING WITH PROGRAM OFFICES TO TRANSITION BRUSH SEAL TECHNOLOGY TO OPERATIONAL AND DEVELOPMENT ENGINES
Navy GTE Seal Development Activity

by

Carl P. Grala
Naval Air Warfare Center
Aircraft Division- Trenton

Under the auspices of the Integrated High Performance Turbine Engine Technology Initiative, the Naval Air Warfare Center conducts advanced development programs for demonstration in the next generation of air-breathing propulsion systems. Among the target technologies are gas path and lube oil seals. Two development efforts currently being managed by NAWCAD are the High Performance Compressor Discharge Film-Riding Face Seal and the Subsonic Core High Speed Air/Oil Seal.

The High Performance Compressor Discharge Film-Riding Face Seal Program aims at reducing parasitic leakage through application of a film-riding face seal concept to the compressor discharge location of a Phase II IHPTET engine. An order-of-magnitude leakage reduction relative to current labyrinth seal configurations is expected. Performance goals for these seals are (i) 1200 F air temperature, (ii) 800 feet-per-second surface velocity, and (iii) 600 PSI differential pressure. The two designs chosen for fabrication and rig test are a spiral groove and a Raleigh step seal. Rig testing is currently underway.

The Subsonic Core High Speed Air/Oil Seal Program is developing shaft-to-ground seals for next-generation propulsion systems that will minimize leakage and provide full life. Significantly higher rotor speeds and temperatures will be experienced. Technologies being exploited include, hydrodynamic lift assist features, ultra light weight designs, and improved cooling schemes. Parametric testing has been completed, a final seal design is entering the endurance test phase.
MECHANICAL SYSTEMS TECHNOLOGY
S.O.A. vs FUTURE REQUIREMENTS

SPEED AND TEMPERATURE TRENDS HAVE AN
ADVERSE EFFECT ON MECHANICAL SYSTEMS:
- STRESS CYCLES ACCUMULATE FASTER,
  LIFE IN HOURS GOES DOWN.
- INTERFACIAL HEAT GENERATION GOES
  UP WITH VELOCITY.
- MATERIALS ALLOWABLES DROP WITH
  INCREASING TEMPERATURE.
- REQUIRED WEIGHT REDUCTIONS MAGNIFY
  THE ENVIRONMENTAL CHALLENGE.

CHALLENGE:

- SIGNIFICANTLY EXPAND COMPONENT OPERABILITY
  - SPEED, TEMPERATURE, LOAD

- SIGNIFICANT COMPONENT/SYSTEM WEIGHT REDUCTIONS

- REACT TO CURRENT DESIGN PRACTICE DEFICIENCIES
MECHANICAL SYSTEMS PROJECT
(Task 1: Axial and Radial Bearings)

**FLEET ISSUES ADDRESSED:**
- Increased endurance for extended coverage for ASW/ASUW/AEW/EW/GS/DRUG missions
- Increased standoff range for power projection ashore
- High performance engines for emerging system requirements (AX, NATF, ASTOVL, SSF)
- Improved life cycle cost through improved reliability
- Improved A/C availability

**TECHNOLOGIES:**
- Magnetic bearings
  - Thrust compensation
  - Radial load compensation
- Innovative design
- Improved materials
- Improved dampers

**INNOVATIVE DESIGN**
- Improved materials
- Improved dampers

**SYSTEM PAYOFFS:**

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<td>+11.1%</td>
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MECHANICAL SYSTEMS PROJECT
TASK 2: LUBE OIL SEALS

FLEET ISSUES ADDRESSED:
- Increased endurance for extended coverage for ASW/ASUW/AEW/EW/C3/0RUG missions
- Increased standoff range for power projection ashore
- High performance engines for emerging system requirements (AX, NATF, ASTOVL, SSF)
- Improved life cycle cost through improved reliability
- Improved A/C availability

TECHNOLOGIES:
- Hydrodynamic lift assist
- Extreme lightweight designs
- Improved carbon materials
- Innovative cooling schemes

INNOVATIVE COOLING SCHEMES

HPTET/SAT RELIANCE JDL
GOALS:

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<tr>
<td>WEIGHT</td>
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INNOVATIVE COOLING SCHEMES

HPTET/SAT RELIANCE JDL
SYSTEM PAYOFFS:

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<tr>
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<tr>
<td>FN / WT</td>
<td>-5.2% -11.1% -25.6%</td>
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MECHANICAL SYSTEMS PROJECT
LUBE OIL SEALS

SUBSONIC CORE HIGH SPEED AIR/OIL SEAL

CONTRACTOR: PRATT & WHITNEY

COST: $430 K

OBJECTIVE: Develop shaft-to-ground sump seal systems for IHPTET Phase II conditions that minimize leakage, give full life.

GOALS:
- Phase II Conditions:
  - 600 F PS
  - 60 PSID
  - 750 F AIR
  - 400 F OIL
  - Full life
MECHANICAL SYSTEMS PROJECT
LUBE OIL SEALS

APPROACH:
• ANALYTICALLY ASSESS MULTIPLE SEALS
• DETAIL DESIGN AND FABRICATE THE TWO
  BEST CANDIDATE SEALS
• 25 HRS OPERABILITY EACH, REVISE
• ENDURANCE TESTING

TECHNOLOGIES:
• HYDRODYNAMIC LIFT ASSIST (STEIN)
• ULTRA-LIGHTWEIGHT DESIGN (REXNORD)
• IMPROVED PACKAGING / COOLING

ADVANCEMENT
BEYOND SOA:
• ORDER OF MAGNITUDE LEAKAGE REDUCTION
  RELATIVE TO LAB SEALS (.1% SFC PER)
• 30% SPEED CAPABILITY INCREASE

STEIN HYDRODYNAMIC CIRCUMFERENTIAL
NON-CONTACTING SEGMENTED SEAL

PROS:
- EXTENSION OF SUCCESSFUL
  SEGMENTED RING SEAL
- LOW LEAKAGE
- WEAR TO 6 MILS O.K.
- LIGHTWEIGHT
- WINDBACK ALLOWS MINIMUM
  LEAKAGE AND CONTAMINATION

CONS:
- MINIMAL EXPERIENCE WITH
  HYDRODYNAMIC LIFT GEOM.
  IN CARBON BORE.
- THERMAL CONEING AND
  MISALIGNMENT CONCERNS
MECHANICAL SYSTEMS PROJECT

REXNORD CARTRIDGE-TYPE CONTACTING FACE SEAL

PROS:
- VERY LIGHTWEIGHT LOW DRAG DESIGN IMPROVES SPEED CAPABILITY.
- TOLERANT TO CONEING AND MISALIGNMENT.
- LOW TO MOD. LEAKAGE
- LOW OPERATING LOADS IMPROVE LIFE

CONS:
- NUMEROUS PARTS
- NARROW CARBON NOSE PRESENTS HANDLING DAMAGE RISK
- POSSIBLE LEAKAGE AT VERY LOW DELTA P’s

MECHANICAL SYSTEMS PROJECT

LUBE OIL SEALS

PHASE I OPERABILITY EVAL COMPLETE
- MIXED RESULTS

• STEIN HYDRODYNAMIC CIRCUMFERENTIAL SEAL:
  - STATIC CAL DONE, VERY LOW LEAKAGE
  - RAN SUCCESSFULLY TO 600 FPS, 60 PSID!
  - LEAKAGE CONSISTENTLY LOW, THEN -
    - BROKE EXTENSION SPRING - EASY FIX IN HAND

• REXNORD CARTRIDGE-TYPE FACE SEAL:
  - STATIC CAL COMPLETED (INITIAL SEC. SEAL PROB)
  - VERY SUCCESSFUL THROUGH TWO DYNAMIC TESTS TO 600 FPS, 60 PSID!
  - LEAKAGE TOOK OFF, SEAL FAILED
    - INVESTIGATION IN PROGRESS.

SUMMARY:
- MINOR REVISIONS TO STEIN SEAL, HIGH CONFIDENCE FOR ENDURANCE PHASE
- ASSESSMENT OF REXNORD SEAL IN PROGRESS, ENDURANCE PROSPECTS TBD
- HAVE SHOWN STABLE LOW LEAKAGE OPERATION AT AGGRESSIVE GOAL CONDITIONS FOR BOTH.
MECHANICAL SYSTEMS PROJECT
TASK 3: STATIC & DYNAMIC GAS PATH SEALS

FLEET ISSUES ADDRESSED:
- INCREASED ENDURANCE FOR EXTENDED COVERAGE FOR ASW/ASUW/AEW/EW/C3/DRUG MISSIONS
- INCREASED STANDOFF RANGE FOR POWER PROJECTION ASHORE
- HIGH PERFORMANCE ENGINES FOR EMERGING SYSTEM REQUIREMENTS (AX, N'TF, ASTOVL, SSF)
- IMPROVED LIFE CYCLE COST THROUGH IMPROVED RELIABILITY
- IMPROVED A/C AVAILABILITY

TECHNOLOGIES:
- FILM-RIDING FACE SEALS:
  - HYDRODYNAMIC, HYDROSTATIC
  - BRUSH/FIBER SEALS
  - ABRADABLE SEALS

GOALS:
- NO FORMAL IHPTET GOALS, CONTRIBUTES TO COMPRESSOR & TURBINE GOALS.

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<td>ABRADABLE SEALS</td>
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</table>

| CONTRACTOR:          | ALLISON                             |
| CONTRACT NO.:        | N00140-39-C-2728                   |
| COST:                | $460 K                              |
| OBJECTIVE:           | DEVELOP/DEMO FILM RIDING CD FACE SEAL FOR VERY HIGH PRESSURE RATIO PHASE II ENGINES. |
| GOALS:              | 1200 F AIR                          |
|                     | 800 FPS                             |
|                     | 600 PSID                            |
APPROACH: APPLY FILM-RIDING FACE SEAL CONCEPT TO PM II C.D. APPLICATION, USING IMPROVED DESIGN ANALYTICS, IMPROVED MATERIALS ASSESS MULTIPLE LIFT FEATURES, FABRICATE & TEST

TECHNOLOGIES: •TRANSIENT DYNAMIC FILM ANALYSIS •SPIRAL GROOVE & RAYLEIGH PAD LIFT GEOMETRIES •SILICON CARBIDE PRIMARY RING •IMPROVED PRESSURE BALANCE

ADVANCED BEYOND SOA: REPLACES MULTIPLE LABYRINTH STAGES AT OVER AN ORDER OF MAGNITUDE LESS leakage

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MECHANICAL SYSTEMS PROJECT

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TRANSITION/ APPLICATION:
- PHASE II JTAGG
- APPLICABLE TO ANY HIGH PRESSURE RATIO MACHINE

PAYOFFS:
- SIGNIFICANT CYCLE EFFICIENCY BENEFITS
  + 0.5 % THROUGH REDUCED LEAKAGE

PROGRESS/STATUS:
- FABRICATION OF BOTH SEALS COMPLETE
- STATIC CAL. TESTING OF BOTH SEALS COMPLETE
  - VERY LOW LEAKAGE
- DURING EVALUATION OF CRANE SEAL - RIG INDUCED RUB OCCURRED - SEAL OK; REWORKABLE
- KAYDON SECONDARY SEAL FAILURE OCCURRED AWAITING REVISED HARDWARE
1. Developed opening force versus film thickness curves (F-h curves) at ID (hi) at different speeds for a given set of OD and ID pressures. The constant closing force line intersects each one of the above curves at the corresponding operating point. The slope of a F-h curve at the operating point gives that average film stiffness. (Fig. 1)

2. Developed film thickness profile along the interface at the operating point for a given combination of speed and pressure. This curve combined with the corresponding stiffness value would enable the designer to know whether the seal is operating with a safe and stable film at that speed and pressure. (Fig. 2)

3. Developed the operating film thickness (hi) versus system pressures for different speeds. This family of curves presents the operating film level over the entire envelope of operation in one picture. Hence, an unsafe operation at any off-design condition will become evident. (Fig. 3)

4. Developed leakage versus system pressure curves for different speeds. This family of curves is the most useful one for the purpose of correlating the experimental data with the code prediction. (Fig. 4)

5. Additionally, the code provides the pressure and Mach number distributions along the interface that are printed on a file for each operating point.

6. Seal distortion

Since the seal face distortions are of the same order of magnitude as the average operating film thickness, the code iteratively determines the distortions using a finite element module. (Ref. 1)

7. Design

A finger spring installed in a groove beneath the SiC inner diameter allowed for differential thermal expansion between retainer and seal ring while keeping the ring centered. Round smooth wire bent into shape to give centering force between rotating seal ring and the retainer. Also used to mount retainer on the shaft to accommodate centrifugal growth.

Antimony impregnated carbon graphite stator ring is used. This provides high compressive strength and stability:

The seals are designed to run with a very thin operating film (3-4 μm) to minimize leakage and maximize film stiffness.

For more information

Figure 1. 'F-h' Curves

Figure 2. Film Thickness Profile
Figure 3. System Pressure versus Operating Film Thickness Plots

Figure 4. Leakage Correlation

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The compliant metallic seal combines the noncontact feature of the labyrinth seal, the low leakage of a mechanical seal, and the compliant nature of the brush seal. It consists of several thin metallic elements or leaves mounted within a ring which is press fit into the housing, and in form, sort of resembles a lip seal sections wiping the shaft. A second set of overlapping cover leaves are placed on top of the shaft riding leaves which reduces leakage and provides stiffness. The leaves can be straight or angle cut. The shaft riding fingers are designed with mismatched curvature to provide lift off similar to the Rayleigh lift pads in mechanical seals with leading edge clearances nearly twice those of the trailing edge as shown by Fleming to be optimal for gas flows in convergent seal passages. Leading edge clearances range from 300 to 500 microinches.

Balance pockets beneath the leaves provide fluid film feed to the "Rayleigh lift" surface and the proper balance ratio (mechanical seal) when combined with the static pressure and film pressure. The leaves flex in the radial direction and accommodate thermomechanical behavior as well as axial motion and angular misalignment.

In the static mode, there is a net closing force on the leaves.

The seals were tested to 70 psi at speeds to 16,000 rpm or surface speeds to 330 fps and temperatures from ambient to 440°F. A slow cycle through the rig critical at 10,000 rpm induced a radial vibration response of 0.004 to 0.005 inch were accommodated by the seal.

Preliminary performance data are encouraging demonstrating hydrodynamic liftoff and non contacting operation at pressure and speeds typical of gas turbine engines. The leakage performance data are significantly better than commerical labyrinth and brush seals which should be expected as this design incorporates the features of the low leakage face or mechanical seal along with the flexibility of the brush configuration.

For more information

COMPLIANT METALLIC HYDRODYNAMIC SHAFT GAS SEAL

Typical Pressure Distribution for Straight Cut Compliant Seal
without Slot Cover

dotted lines represent lines of constant pressure between the shaft and the underside of the compliant metallic members
solid lines represent the direction of the flow field

Typical non-rotating pressure distribution thru midpoint of shaft contact length

typical rotating pressure distribution for various finger thicknesses
Angle Cut Compliant Seal with Slot Cover

Figure 3

Straight finger Compliant Seal with Rayleigh Pads and Slot Cover

End View

Sectional View

Viewed from ID

Figure 4

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ACTIVELY CONTROLLED SHAFT SEALS
FOR AEROSPACE APPLICATIONS

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School of Mechanical Engineering
Georgia Institute of Technology
Atlanta, Georgia 30332

NASA Research Grant NAG 3-974
NASA Technical Officer: M. P. Proctor

Helium Purge Assembly

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CONVENTIONAL MECHANICAL SEAL

FLOATING FACE

FIXED FACE

High Pressure

Leakage

Low Pressure

\[ \delta = h_0 \cdot h_1 \]
To Control Sys
From Control Sys
Lox Side
To Control Sys
From Control Sys
Hot Gas Side

Electrode
Piezoelectric Element
Carbon Face
Thermocouple

CONTROLLABLE SEAL

CONED DEFORMABLE FACE ASSEMBLY
FACE HOLDER AND DEFORMABLE FACE ASSEMBLY

Variable Pressure Operation

Leakage versus Voltage – Static Test
Film Thickness versus Voltage — Static Test

Leakage versus Voltage — Rotating Test

Film Thickness versus Voltage — Rotating Test
OBJECTIVES OF THE PRESENTATION:

- Report on the status of the project

- Discussion that will broaden your research and help to interpret results
OBJECTIVES AND ACCOMPLISHMENTS

- Develop verified family of CFD codes for Analyzing Brush Seals
  - idealized (uncompliant) 2D configuration ✓
  - compliant 2D geometry not
  - compliant 3D not

- Experimental Facilities for the adequate code verification
  - stationary bristles (cylinders) ✓
  - moving bristles not

  Additional experiments were designed specifically for code validation and investigation of features to be incorporated in the computer program.

- Qualitative and quantitative analyses of the Fluid Flow in the Brush Seal Configuration
  - flow around one bristle, level 1 ✓
  - flow around several bristles, level 2 ✓
  - flow in the deep tube bundles, level 3 ✓
    (intermediate pitch-to-diameter ratio)
  - flow through uncompliant brush prototypes, level 4 ✓
    (small pitch-to-diameter ratio)

PRESENT CODE CHARACTERISTICS

- finite-difference primary variables (u, v, p) formulation
- collocated grid
- conservative formulation of the momentum equations
- conservative formulation of the pressure equation
- conservative fully populated of the boundary conditions
- steady-state solutions
- transient solutions
- 2nd and 3rd order convective schemes are implemented
- implicit under/over relaxation (if necessary, optional)
- accommodates an arbitrary geometrical configuration in Cartesian coordinates (non-contiguous boundaries)
- regular and nonregular grid
- graphical post-processor capabilities with PV-Wave (Unix)
MODEL ASSUMPTIONS:

- incompressible fluid, constant properties
- isothermal model
- leakage flow
  - $M < 0.3$
  - $Re$ (low, intermediate)
- no shaft rotation
- stationary bristles

DETERMINED FLOW RESISTANCES THROUGH THE BRUSH SEAL

$R_{||}$ - resistance parallel with the bristles
$R_{\perp}$ - resistance normal to the axis of the bristles
3D VIEW OF THE LINEAR BRUSH IN THE CHANNEL

SCOPE OF THE WORK

• development and evaluation of a numerical procedure aimed at
  the solution of the incompressible flow problem through a densely
  packed array of cylindrical pins at low to medium Reynolds numbers

[The method promotes the solution of the 2-D Navier-Stokes
  equations written in a conservative form in primitive
  variables (u,v,p). The numerical implementation follows an implicit
  formulation that uses the alternate direction integration (ADI)
  method applied to a collocated grid. For the pressure solution, the
  two momentum equations are joined by an elliptic Poisson pressure
  equation (Roache, 1981, Ghia et al., 1983).]

The algorithm is applied to:

- the classical analysis of flow and pressure development around a
cylinder
- an array of cylinders located in a square channel

• flow and pressure patterns are discussed parametrically with
  respect to the variation of the Reynolds number.
GOVERNING EQUATIONS

Taking the divergence of the X- and Y-momentum equations and using continuity for simplification, one obtains a pressure equation that appears under a Poisson type format (Roache, 1981).

\[ \nabla^2 p = \frac{\partial^2 (U^2)}{\partial x^2} + 2\frac{\partial^2 (UV)}{\partial x \partial y} - \frac{\partial^2 (V^2)}{\partial y^2} + \left( \frac{\partial D}{\partial t} + \frac{1}{Re} \left( \frac{\partial D}{\partial x} + \frac{\partial D}{\partial y} \right) \right) \]

\[ \frac{\partial D}{\partial t} + \frac{1}{Re} \left( \frac{\partial D}{\partial x} + \frac{\partial D}{\partial y} \right) \]

D is the dilation term, \( D = \frac{\partial U}{\partial x} + \frac{\partial V}{\partial y} \).

During calculations, D represents the residual that has to shrink to zero if continuity is to be satisfied.

Boundary and Initial Conditions for the Momentum Equation.

* The boundary conditions on the lateral solid walls assume non-slip conditions and non-porous walls.

* The inflow velocity is uniform with \( U = 1 \), and \( V = 0 \) (angle of incidence is zero). A reference pressure is assigned to one point on the inflow boundary.

Special Form of Open Boundary Condition (Exit Flow)

(i) the satisfaction of the continuity equation (specifically in the direction of the U velocity),

\[ \frac{\partial U}{\partial x} = - \frac{\partial V}{\partial y} \]

(ii) the condition for fully developed velocity gradient for the vertical component

\[ \frac{\partial V}{\partial x} = 0 \]

(iii) satisfaction of the momentum equation (in the direction of U velocity)

\[ \frac{\partial P}{\partial x} = - \frac{\partial (UU)}{\partial x} + \frac{\partial (UV)}{\partial y} + \frac{1}{Re} \left( \frac{\partial^2 U}{\partial x^2} + \frac{\partial^2 U}{\partial y^2} \right) \]
Boundary Conditions for the pressure Poisson Equation

The dynamic pressures $P_r$ are determined from the balance of the normal forces with the inertia and viscous forces. The effects of the terms $\frac{\partial U}{\partial t}$ and $\frac{\partial V}{\partial t}$ both at inflow and outflow boundaries have been considered negligible. The following formulation is totally independent of the internal boundary configuration, and thus applicable with no restrictions.

$$\frac{\partial P_r}{\partial x} = -1 \left( \frac{\partial(UU)}{\partial x} + \frac{\partial(UV)}{\partial y} \right) - 1 + \frac{1}{Re} \left( \frac{\partial^2 U}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} \right).$$

On the non-contiguous internal boundaries of the pins, in addition to previous equation, one needs to add an expression for $\frac{\partial P_r}{\partial y}$

$$\frac{\partial P_r}{\partial y} = -1 \left( \frac{\partial(UV)}{\partial x} + \frac{\partial(VV)}{\partial y} \right) - 1 + \frac{1}{Re} \left( \frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} \right)$$

At the channel's upper and lower walls the pressure boundary condition takes a simplified form due to the fact that $U = V = 0$.

$$\frac{\partial P_r}{\partial y} = \frac{1}{Re} \left( \frac{\partial^2 V}{\partial y^2} \right)$$

Initial conditions ($T=0$). The input velocities are given as $U = 1$, $V = 0$. The pressures are set initially to an arbitrary and operator chosen constant ($P = P_{ref} = const$).

NUMERICAL IMPLEMENTATION: ADI METHOD

The discretization of the system of governing equations introduced above, follows the use of the ADI applied to a colocated grid. The procedure uses the full direct approximation of each term within the differential equation on every half time step, $\Delta t/2$. One obtains the following system of linear algebraic equations.

$$u^{n+1/2,n+1} = \frac{1}{od} \left( A_{xx}(u)^{n+1/2} + A_{yy}(u)^{n+1/2} + C_{x}(u)^{n+1/2} + C_{y}(u)^{n+1/2} \right)$$

$$v^{n+1/2,n+1} = \frac{1}{od} \left( A_{xx}(v)^{n+1/2} + A_{yy}(v)^{n+1/2} + C_{x}(v)^{n+1/2} + C_{y}(v)^{n+1/2} \right)$$

$$u^{n+1/2} = \frac{1}{od} \left( A_{xx}(u)^{n+1/2} + A_{yy}(u)^{n+1/2} + C_{x}(u)^{n+1/2} + C_{y}(u)^{n+1/2} \right)$$

$$v^{n+1/2} = \frac{1}{od} \left( A_{xx}(v)^{n+1/2} + A_{yy}(v)^{n+1/2} + C_{x}(v)^{n+1/2} + C_{y}(v)^{n+1/2} \right)$$

The spatial derivatives, with the exception of the convection terms and cross-derivatives, are approximated by a second order central finite-difference. For the convection terms the first-order conservative scheme proposed by Torrance(1968) is employed.
Solution Procedure

The solution follows according to the time-dependent alternative-direction method using a tridiagonal matrix elimination. The steps of the solution are as follows:

- solve in the x direction for U velocity at the n+1/2 time step
- solve in the y direction for the U velocity at the n+1 time step
- solve in the x direction for V velocity at the n+1/2 time step
- solve in the y direction for the V velocity at the n+1 time step
- solve the Poisson's pressure equation at the n+1 time step by means of the pseudo-transient method within the set of internal ADI iterations n_{it}=1,...,n_{P}:

(i) in the x direction at the s+1/2 pseudo-time step
(ii) in the y direction at the s+1 pseudo-time step
ACCURACY CONSIDERATIONS

- Qualitative comparison of calculated flowfield with experimental results of Bouard and Coutanceau (JFM, v.101, 1980)

Pressure Drops, \( \Delta P = P_{\text{leading edge}} - P_{\text{trailing edge}} \)

<table>
<thead>
<tr>
<th>( Re_d )</th>
<th>this study</th>
<th>Fornberg, 1980</th>
</tr>
</thead>
<tbody>
<tr>
<td>100</td>
<td>0.689</td>
<td>0.70</td>
</tr>
<tr>
<td>200</td>
<td>0.670</td>
<td>0.63</td>
</tr>
<tr>
<td>300</td>
<td>0.640</td>
<td>0.60</td>
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</table>
FIG. 1 CHARACTERISTIC CONFIGURATION
Effect of Re number

FLOW THROUGH BASIC ARRAY CONFIGURATION 7 ROWS X 11 PINS
A) Re₀ = 100; B) Re₀ = 2000;
C) DETAIL OF FLOW IN THE QUADRANT INDICATED IN FIG. 2A
D) DETAIL OF FLOW IN THE QUADRANT INDICATED IN FIG. 2B
PRESSURE MAPS INSIDE TUBES ARRAYS

LEADING EDGE

TRAILING EDGE

A) LEADING EDGE OF THE ROW, AT $Re_l=100$ AND $Re_h=2000$
B) TRAILING EDGE OF THE ROW, AT $Re_l=100$ AND $Re_h=2000$

Deep bank(72) cylinders, Level 3
NON-DIMENSIONAL PRESSURE MAPS FOR PRESSURE DROPS IN THE BASIC ARRAY CONFIGURATION (7 ROWS X 11 PINS)
A) Reₐ = 100;  B) Reₐ = 2000;

FLOW ACROSS ARRAY OF PINS AT Reₐ = 2000, PTDRₑ = 1, PTDRₑ = 1
A) SIX ROWS
B) CASCADE OF TWO ELEMENTS (THREE ROWS EACH), C = 3d
C) CASCADE OF TWO ELEMENTS (THREE ROWS EACH), C = 3d
VARIATION OF THE FLOW FIELD STRUCTURE WITH THE CHANGE IN THE LONGITUDINAL PITCH
PRELIMINARY CODE VERIFICATION RESULTS

3 rows of pins

<table>
<thead>
<tr>
<th>Re</th>
<th>P (psi)</th>
<th>P(Pa)</th>
<th>(U^2)</th>
<th>(\Delta P) (nond)</th>
</tr>
</thead>
<tbody>
<tr>
<td>91.3</td>
<td>2.263</td>
<td>15,602</td>
<td>7.09</td>
<td>2200.</td>
</tr>
<tr>
<td>195 exp. 4.02</td>
<td>27,758</td>
<td>32.16</td>
<td>863.0</td>
<td>926.0 (7% difference)</td>
</tr>
<tr>
<td>num. 4.31</td>
<td></td>
<td></td>
<td></td>
<td>926.0</td>
</tr>
<tr>
<td>327 exp. 6.82</td>
<td>47,056</td>
<td>91.29</td>
<td>516</td>
<td>650 (26% difference)</td>
</tr>
<tr>
<td>num. 8.6</td>
<td></td>
<td></td>
<td></td>
<td>650</td>
</tr>
</tbody>
</table>

Oil temperature: \(T=70\) F  
Oil density=950 kg/m³  
Fluid velocities: 8.6 cm/sek  
18.5 cm/sek  
31.0 cm/sek

Brush Design Applications

Pressure Drop Estimation For the Characteristic Brush Section

\[ \frac{\partial u}{\partial z} = 0, v = 0 \quad \text{symmetry velocity conditions} \]

inflow  
\[ u = 1 \]

outflow  
\[ \text{Re}_f = 20 \]

Converged Solution, \(n_H = 5000\)

Non-dimensional Pressure Drop, \(\Delta \tilde{P}\)

Iteration number, \(n_H\)

History of the Pressure Drop Convergence, \(\text{Re}_f = 20\)

\[ \text{PTDR}_{25} = \text{PTDR}_{25} = 13.4 \]
CONCLUSIONS:

- approximate mathematical model with distributed parameters and without porous media assumption
- developed and evaluated a new computational algorithm for the solution of N-S equations in \((u,v,p)\) formulation
- systematic analyses of the fluid flow in the brush sea components
- typical pressure and velocity distributions were estimated
- nonlinear behaviour of the pressure drop vs PTDR\(_L\)
- Pressure paradox for highly recirculative flows
- Capabilities of calculation of the pressure drop for a given bristle geometry and a typical brush segment
- PTDR is extremely influential in the nature of the overall flow inside the array and the subsequent pressure drops
- Pressure distribution inside the brush is non-symmetrical and varies across the cross section
- New information on the flow structure within tube bundles. Butterfly flow formation, near wall jets that are instrumental in the butterfly formation.
- transients are negligible, \(Re<1000\)
DYNAMICS OF FACE SEALS FOR HIGH SPEED TURBOMACHINERY

Simon Leefe
Project Engineer
BHR Group Ltd.
Cranfield, Bedford, MK43 0AJ, England

ABSTRACT

Face seals in rocket engine fuel and oxidiser turbopumps have been the subject of intense investigation for over 25 years. Whilst advances have been made in the understanding of thin film lubrication between seal faces; valuable data has been produced on the friction and wear of material pairs in cryogenic environments; pioneering work has been done on the effect of lubricant phase change in seals; and many improvements have been made in mechanical seal design, relatively superficial attention has been given to the vibrational dynamics of face seals in high-speed turbomachinery.

BHR Group Ltd. (formerly BHRA) has recently completed the first stage of a study, commissioned by the European Space Agency, to investigate this area. This has involved the development of a two-dimensional adiabatic, turbulent lubrication model for thick gas film applications, the production of an integrated mathematical model of gas seal vibrational dynamics for thin film applications, implementation in software, the undertaking of an experimental programme to validate software against variations in operating conditions and design variables, and suggestions for improved seal design.
CURRENT PROJECTS

- Applications
  - rotary
  - reciprocating
  - static
- Technology
  - experimental
  - analytical
  - design studies
- Organisation
  - direct contract
  - consortium + Dept. of Trade and Industry
  - consortium + EEC
  - independent consortium
**FLUID SEALING TECHNOLOGY**

Independent facilities and expertise:

- **Seal Analysis:** thermal, mechanical, lubrication
- **Seal testing:** oil, water, gas, cryogens, contaminants
- **Pump Loops:** oil, water, slurry, water/air
- **Site Measurements:** fixed, portable
- **Design Audit:** analysis, critical review
- **Rig Manufacture:** design, build, modification

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**PROJECT STRUCTURE**

```
<table>
<thead>
<tr>
<th>FLUID FILM</th>
<th>STRUCTURAL DISTORTION</th>
<th>SEAL RING DYNAMICS</th>
</tr>
</thead>
</table>
```

- **Seal Tests**
  - Data from
  - Validated by
  - **INTEGRATED COMPUTER MODEL**
    - **PARAMETRIC STUDY**
      - **RECOMMENDATIONS**

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TURBOPUMP SEALING

FACE SEAL OPTIONS:
- Plain
- Hydrostatic
- Self-acting

LITERATURE SURVEY
MAIN FINDINGS - SEALING PRACTICE

Limit of demonstrated success of plain face seals in LOX (NASA 1979)

Self-acting face-seals in LOX (NASA evaluation)
Plain face-seals in LOX (demonstrated success)
Plain face seals in LH2 (Japanese test programme)
Plain face seals in GN2 (BHRG test programme)
LITERATURE SURVEY

MODELLING - FILM LUBRICATION ANALYSIS

Laminar, isothermal - Reynolds equation
• Liquid films - treatment of cavitation
• Gas films - grid design (adaptive, graded, etc.)
  - algorithm design (implicit, alternating, multigrid, 'interior co-location', etc.)

Turbulent lubrication - Hirs' bulk flow
- Constantinescu
- Ng & Pan

Non-isothermal (higher Mach number) compressible flow
• 1-D (radial) adiabatic model with radial taper and entrance effects - Zuk

Two-phase (boiling interface) films
• 1-D models
• Stability approached from consideration of equilibrium film thickness vs. opening force curves (i.e. not from dynamic analysis)

LITERATURE SURVEY

MODELLING - DYNAMICS

• $[K]$ and $[C]$ matrices from fluid film analysis
  then dynamics as a separate problem

• Integrated analysis - fluid film forces and moments calculated at each timestep

• Excitation mechanisms

• Number of vibrational degrees-of-freedom

• Thermal and vibrational transients - 3 or 4 orders of magnitude difference in timescale - separate problem
**SCOPE OF MODEL**

- Concentrate initially on DYNAMICS
- Gas seal assumed (2-D transient 2-phase prohibitive within commercial constraints)
- Transient structural distortions
- Full transient lubrication analysis
- Turbulent, adiabatic AND laminar, isothermal leakage flow
- Choked exit conditions catered for
- 4 vibrational degrees of freedom
- Mechanical damping

**MATHEMATICAL MODEL**

**TURBULENT, ADIABATIC FLOW**

Radial and circumferential velocities:

\[ u_r = -\frac{G_r}{\eta} \left( \frac{2p}{r_2} - \frac{1}{r_2} \right) \]

\[ u_\theta = -\frac{G_\theta}{\eta} \left( \frac{2p}{r_2} - \frac{1}{r_2} \right) \]

where \( I_p = \frac{p R^3}{2} \)

and \( G_r \) and \( G_\theta \) from Hirs' bulk flow turbulent lubrication theory (or \( \approx 1/12 \), laminar)

Given in terms of Reynolds numbers "as seen by" rotor and stator (different)

Shear stresses from these Reynolds numbers

2-D adiabatic energy equation relates pressure to circumferential shear stress for density at current timestep

Iterate round instantaneous equations

Timestepping

Substitute \( u_r \) and \( u_\theta \) in continuity equation as "known" and find density at next timestep

Use film thickness, \( h \), at mid-timestep throughout procedure
MATHEMATICAL MODEL
LAMINAR, ISOTHERMAL FLOW

Compressible Reynolds equation with ideal gas assumption

\[
\frac{\partial}{\partial t} \left( \rho \frac{\partial \mathbf{u}}{\partial x} \right) + \frac{\partial}{\partial x} \left( \rho \mathbf{u} \mathbf{u} \right) = \frac{\partial}{\partial x} \left( \frac{-p + \rho \mathbf{u} \mathbf{u}}{\rho} \right) - 6 \mu \frac{\partial \mathbf{u}}{\partial x} - 12 \eta \frac{\partial}{\partial x} \left( \frac{\partial \mathbf{u}}{\partial x} \right)
\]

Time discretisation:

\[
\frac{\partial}{\partial t} \left( \rho \mathbf{u} \right) + \frac{\partial}{\partial x} \left( \rho \mathbf{u} \mathbf{u} \right) = \frac{\partial}{\partial x} \left( \frac{-p + \rho \mathbf{u} \mathbf{u}}{\rho} \right) - 6 \mu \frac{\partial \mathbf{u}}{\partial x} - 12 \eta \frac{\partial}{\partial x} \left( \frac{\partial \mathbf{u}}{\partial x} \right)
\]

No energy equation required

Velocities and shear stresses from pressure gradients

- Check exit Mach number distribution for condition
  \[ M = \frac{1}{\sqrt{\gamma}} \]  (isothermal flow)

- Check Reynolds number distribution for condition
  \[ \text{Re} > \text{Re}_{\text{critical}} \]  (laminar flow)

EXCITATION MECHANISMS

- Rotor misalignment
- Shaft axial vibration
- Rotor eccentricity
- Face coning
- Face waviness
MATHEMATICAL MODELLING

FACE CONING

Sources:
- Pre-lapped taper and clamping forces
- Bellows load
- Rotor centrifugal inertia
- Change in ambient temperature for seal ring assemblies
- Sealed pressure differential
- Interfacial heat generation
- Interfacial pressure distribution

MATHEMATICAL MODELLING

INTERFACIAL PRESSURE CONING

1. F.E. Analysis

2. Pressure distn. over P.D. grid - circumfl. average
   uniform pressure over annular rings corresponding to F.E. mesh

3. Use influence coefficients to calculate face coning
   \[ \psi = \sum_{k} c_k \cdot p_k \]
VIBRATIONAL DEGREES OF FREEDOM

MATHEMATICAL MODELLING
DYNAMICS

Equations of motion time-discretized by Newmark's method:

\[ \left[ M \right]^{-1} \left[ p \right]_{n+1} = \frac{1}{\delta^2} \left[ \left[ x \right]_{n+1} - 2 \left[ x \right]_n + \left[ x \right]_{n-1} \right] + \frac{1}{\delta} \left[ \left[ v \right]_{n+1} - \left[ v \right]_n \right] \]

Collect terms in \([x]_{n+1}\) and solve:

\[ [x]_{n+1} = \left[ I \right] - \frac{1}{\delta^2} \left[ [M]^{-1} \left[ F \right]_n \right] + \frac{1}{\delta} \left[ [M]^{-1} \left[ \left( [K]_n - [K]_{n+1} \right) \right] \right] \]

Inertia and stiffness matrices, \([M]\) and \([K]\), are diagonal
in the absence of lateral stiffness, so that inverses are trivial.
### Mathematical Modelling

#### Timestepping

<table>
<thead>
<tr>
<th>Computation</th>
<th>Uses</th>
<th>To Predict</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fluid film shape</td>
<td>$h_{n+1/2}$, $h_{n-1/2}$</td>
<td>$h_{n+1}$, $h_{n-1}$</td>
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<tr>
<td>Fluid film pressure distribution, $p$</td>
<td>$p_n$, $p_{n+1/2}$, $p_{n-1/2}$</td>
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<td>Velocity and shear stress distributions</td>
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<tr>
<td>Coning</td>
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<td>$p_{n+2}$, $v_{n+2}$</td>
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<tr>
<td>Fluid film forces and moments</td>
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<td>$F_{n+1}$, $v_{n+1}$</td>
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<tr>
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<tr>
<td>Dynamics</td>
<td>$(x)_n$, $(x)_n$</td>
<td>$(x)<em>{n+1}$, $(x)</em>{n+1}$</td>
</tr>
</tbody>
</table>

- = Output of fundamental importance

---

#### Mathematical Modelling

**Approach to Thermal Transient Coning**

**Problem**

Thermal diffusion timescale
2-4 orders of magnitude slower than timescale of vibrational dynamics

**Solution**

- Off-line thermal transient F.E. analysis provides coning as a function of time
- Coning-time curve 'sampled' at user-specified intervals to provide quasi-steady coning for vibrational analysis
Bellows Damper, leakage path.

Stator Assembly Mating Ring

Plain-faced balanced mechanical seals

Bellows-type flexibly-mounted stator ring

Rigidly-clamped rotor ring

Coulomb friction vibration dampers
TEST PROGRAMME

SCOPE
- 42 tests covering:
  - face sealing
  - rotor eccentricity
  - rotor out-of-squareness
  - degree of damping

- Effects of high and low temperature investigated
- Tests at high speed (60,000 rpm)
- All tests on typical plain face seal, modified to suit required conditions (face diameter = 30mm)

FACILITY
- Hot gas (to around 220°C) supply
- Cold gas supply (boiling to room temp)
- Liquid cryogen supply possible
- High pressure (rated to 20 bar) up to 14000 rpm
- High speed (60,000 rpm) at lower pressure
TEST PROGRAMME
MISALIGNMENT AND ECCENTRICITY

MISALIGNMENT

ECCENTRICITY

Accurate tracking of run-out

Stability reached quickly
ANIMATION SEQUENCE

AREAS SUITABLE FOR FURTHER DEVELOPMENT

- Liquid lubricant film
- Cavitating film
- Mechanical contact
- Circumferential EHD
- Different spring and secondary seal types
- Floating rotor types
- Ring seal geometries
Dynamic Coefficients for Multiple Brush Seals

From notes and discussion of talk by D. Childs Texas A&M Univ.
by R.C. Hendricks

The cross sectional view of the Dressman-Childs apparatus is given as figure 1. This is the same apparatus as described by Childs et al., ref. 1, and used to determine the rotordynamic coefficients for a variety of seal configurations and test conditions. The working fluid is compressed air.

The experimental test sections for four, five, and six brush seal configurations are illustrated in figures 2, 3, and 4 respectively, see ref. 2.

While the dynamics of the 4-stage system was reported by Connors et al. ref. 3, with good reliability, the results of the extensions to other brush seal sets has not proven satisfactory. The data are inconsistent, e.g., the leakage for 4-brushes is less than for 6-brushes, however for all cases, the whirl frequency ratio was near or less than zero. But again the performance of the 4-brush configuration was dynamically better than that of the other configurations.

These results are not yet resolved and as such are given to provide the Seals Workshop with some information about multiple brush configurations - at least be aware that multiple brush seals require attention even though dual brush seals are operating with high resolve, there are only a few results for more than two brushes in the literature and NO other dynamic data to determine or assess rotordynamic coefficients.

For more information


   Experimental Rotordynamic Coefficient Results for a 5-Stage Brush Seal TRC-SEAL-7-92 #353, May 92.
   Experimental Rotordynamic Coefficient Results for a 6-Stage Brush Seal TRC-SEAL-8-92 #354, May 92.
   Turbomachine Laboratories, Texas A&M Univ., College Station Texas 77843

Table 1 Test Points

<table>
<thead>
<tr>
<th>Rotor Speed (rpm)</th>
<th>Inlet Pressure $P_i$ (bar)</th>
<th>Pressure Ratio $P_n$</th>
<th>Inlet Pressure in the Direction of Rotor Rotation</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 - 5000</td>
<td>1 - 7.90</td>
<td>1 - 0.55</td>
<td>1 - None</td>
</tr>
<tr>
<td>2 - 12000</td>
<td>2 - 13.4</td>
<td>2 - 0.46</td>
<td>2 - Intermediate</td>
</tr>
<tr>
<td>3 - 16000</td>
<td>3 - 18.3</td>
<td>3 - 0.25</td>
<td>3 - High</td>
</tr>
</tbody>
</table>

4-Stage Brush Seal

Figure 8 Geometry and dimensions of seal insert, all dimensions in millimeters

Fig. 8 illustrates the brush seal insert geometry used in this study.

Uncertainty Analysis

An experimental uncertainty analysis based on Holman (1978) for the measured experimental values is used in this study. The expression for the total uncertainty of a measured value is given below in equation (8).
Uncertainty Analysis

An experimental uncertainty analysis based on Holman (1978) for the measured experimental values is used in this study. The expression for the total uncertainty of a measured value is given below in equation (8).
RESULTS OF CRYOGENIC BRUSH SEAL TESTING

Presented by J. Scharrer, Rocketdyne

and

R.C. Hendricks, National Aeronautics and Space Administration

Five-Brush Seal Configuration Leakage as a Function of Pressure for Selected Rotor Speeds

![Graph showing leakage as a function of pressure and rotor speed.]

Schematic and Section View of Multifunction Tester

(Note: Some probes are not shown for clarity.)
1. Introduction

In the last decade, brush seals have emerged to be one of the most promising technologies for the reduction of leakage flow in gas turbine engines. Recent bench tests indicate a possibility of an order of magnitude reduction in leakage flow over multiknife labyrinth seal, Holle and Krishnan (1990). Additional potential for performance benefit arises from mechanical and maintenance considerations. The efficiency of a labyrinth type seal depends upon the clearance between the tip of the knife and the bore but this radial clearance may be difficult to control due to thermal and dynamic conditions. A brush seal on the other hand is compliant, and hence has the ability to recover after excursions, Flower (1990). An important question that remains to be answered is the relationship between brush configuration/operation parameters and some measure of its compliance. One measure of compliance is the clearance that develops between the bristle tips and the rotating element due to the pressure differential across the seal and due to the aerodynamic drag.

We attempt in this paper to develop a model for the flow through brush seals and determine their elastic behavior in order to predict the dependence of brush/journal clearance on geometry and operating conditions. Several idealizations regarding brush seal configuration, flow conditions and elastic behavior are made in the analysis in order to determine closed form parametric dependence. This formulation assumes that there is no initial interference between the bristle tip and the rotor. Also interbristle, bristle-backing plate and bristle-rotor friction is neglected. The bristle bundle or the brush seal as it is alternately called is assumed homogeneous and isotropic on a macroscopic scale so that a physical property like permeability is uniform. The fluid is assumed to be homogeneous, incompressible, viscous and is flowing under steady conditions.

A schematic of a brush seal is shown in figure 1. If the nominal bristle-shaft interference is absent then under static conditions the bristles may deflect axially due to the imposed pressure differential. This axial deflection may create a clearance permitting leakage flow in excess of that which occurs through the porous matrix.
formed by the bristle bundles. Under dynamic conditions the Couette flow created by shaft motion could be strong enough to cause bristle deflection and once again a clearance may develop.

The paper proposes a means to determine this clearance (or at least describe its parametric dependence on geometry and operating conditions) under static as well as dynamic conditions. The study can be thought of as consisting of three separate modeling efforts. First a flow model that describes the coupled parallel flow through the porous medium made of bristle bundles and the clearance region. This development follows the earlier work of Beavers and Joseph (1967), Beavers et al. (1970), Williams (1978) and Rudraiah (1985). This model provides the macroscopic description of the flow field, i.e., a filter velocity in the porous medium. Second, a model to relate this macroscopic flow field to a local flow field and its associated drag on the bristle is developed. This model also permits us to determine an expression for the permeability in order to characterize the physical property of the bristle bundle in absence of an experimentally determined value. The forces on a single bristle due to this macroscopic flow field are then estimated assuming idealized microscopic flow behavior and a phenomenological description of drag on a bristle. Third, the elastic behavior is modeled to estimate the deflection of the bristle tip due to the flow field or the impressed axial pressure differential. A description of the clearance would in principle require a simultaneous solution of the three models. It is, however, assumed here that the physical property permeability remains unchanged both due to the presence of leakage flow through and around the bristle bundle as well as due to the deformation of the bristles themselves. Given this, it is then necessary to solve only the flow and elastic models simultaneously to determine the clearance.

2. **Circumferential Deflection**

To determine the circumferential deflection of the bristles we must first estimate the forces on each bristle. The forces in the circumferential direction are due to drag caused by the flow around the bristle bundle. This flow is in turn driven by the Couette flow in the bristle-shaft clearance as a result of the circumferential slip velocity of the shaft itself. In the absence of a clearance, the shaft motion imposes a circumferential velocity boundary condition directly at the bristle-shaft interface. A model to determine the flow field in both these circumstances is introduced next. This development assumes that the clearance $h_0$ if any is known. Its actual value will be determined later along with considerations of the elastic behavior.
2.1 Flow Model

Let us consider the geometry shown in figure 2, with a porous medium of height \( h \) underlying a channel formed by a clearance of height \( h_o \). The clearance is bounded above by an impermeable wall moving to the right at \( U_0 \) and the porous region is bounded below by an impermeable stationary wall. The formulation presented here follows that in Rudraiah (1985). The basic equations describing the flow are obtained after the following approximations are made.

i) The fluid is homogeneous and incompressible.

ii) The flow in the channel and in the porous medium is driven by a shear produced due to the motion of the upper plate. This flow is steady, laminar and fully developed.

iii) The porous medium formed of bristle bundles is homogeneous and isotropic on a macroscopic scale.

iv) The flow in the porous medium is adequately described by the Brinkman equations and this flow is coupled to the channel flow by a boundary condition given by Williams (1978).

Following Rudraiah (1985), we write equations for \( u \), velocity in the gap and \( \hat{u} \), filter velocity in the porous medium as:

\[
\frac{d^2 u}{dy^2} = 0 \quad \text{and} \quad \frac{d^2 \hat{u}}{dy^2} - \frac{1}{\lambda k} u = 0
\]

(1)

where \( \lambda \) is a positive constant and \( k \) is the permeability of the porous medium. The velocity \( \hat{u} \) in the porous medium is related to \( u \) by

\[
u = (1-\phi) \hat{u}
\]

(2)

where \( (1-\phi) \) is the porosity. Following Williams (1978), at the clearance-porous medium interface we assume that:

\[
\frac{du}{dy} = (1-\phi)\lambda \frac{d\hat{u}}{dy}
\]

(3)

The remaining boundary conditions are the usual no-slip conditions at impermeable walls and are:
Solving (1) subject to (2), (3) and (4) we obtain the velocity distributions in the clearance and the porous regions to be

\[
\begin{align*}
\hat{u} &= u_0 \left[ 1 - \frac{\lambda \delta (h_0 - y)}{(\tanh \delta h + \lambda \delta h_0)} \right] \quad y > 0 \\
\hat{u} &= \frac{u_0}{(1-\phi)(\tanh \delta h + \lambda \delta h_0)} \left[ \sinh \delta y + \frac{\cosh \delta y}{\coth \delta h} \right] \quad y < 0
\end{align*}
\]

where \( \delta = (\lambda k)^{-1/2} \). Here \( \delta h = h (\lambda k)^{-1/2} \gg 1 \) is used. This relies on \( \lambda \) to be of order unity and \( h \) to be a macroscopic length scale assumed to be several times greater than \( k^{1/2} \) (which is typically of order \( d_0 \), the characteristic dimension of the porous matrix, i.e. bristle diameter). Hence we may approximate \( \hat{u} \) by

\[
\hat{u} = \frac{u_0}{\eta} e^{\delta y} \quad y < 0
\]

where \( \eta = (1-\phi)(1+\lambda \delta h_0) \). The exponential behavior of the filter velocity implies that it decays to the Darcy value (which in this case is zero) within a boundary layer of length scale \( 1/\delta \), where \( 1/\delta \) is of the order of \( k^{1/2} \).

Here \( \hat{u} \) represents a filter velocity, a macroscopic quantity defined in order to avoid the more difficult question of what is the true velocity of the fluid in the porous region between the bristles. We now make certain idealizations about the bristle bundle geometry and subsequently model the flow through the interbristle pores in order to determine the viscous drag force directly as a function of the filter velocity.

2.2. Permeability Model

The drag force on a bundle of cylindrical bristles clearly depends upon the flow through the pores which in turn depends upon the particular geometric configuration. Let us first examine the situation for two particular geometric arrangements. Let us assume that the cross-section of the bundle remains same in the direction along the bristle axis and that the flow is normal to these axes. Let \( \phi \) be the solidity or here the area fraction and \( Z \) be the number of nearest neighbors.
Then \( \phi \) and \( Z \) are respectively \( \pi/4 = 0.79 \) and \( 4 \), for a square array and \( \pi/2\sqrt{3} = 0.907 \) and \( 6 \) for a hexagonal array. For these arrays there is no possibility of any transverse flow since all neighboring cylinders are in contact. Typical solidities \( \phi \) for brush seals are between 0.7 and 0.8, indicating a fairly close packed geometry. It is very likely that the manufacture of bristle bundles and their relative movement in the presence of leakage flow lead to bristle configurations that are close to random. A particular means to generate a closely packed random array is by the following two step process, described by Sangani and Yao (1988). In the first step, the process of dropping a large number of equal-diameter cylinders in a container is simulated. Note that in the configuration so generated any cylinder is in contact with its nearest neighbors. Let \( \phi_t \) be the solidity of such a closely packed random array. Berryman (1983) summarizes the results of several simulations and reports \( \phi_t \) in the range of 0.81-0.89, with most studies quoting a value of approximately 0.82. Sangani and Yao (1988) have also simulated such arrays recently with up to 1600 cylinders in a container and they report a value of \( \phi_t = 0.824 \) and \( Z = 4.2 \). In the second step, the diameters of all the cylinder centers are shrunk by a constant amount \( 2\varepsilon r \), while keeping the location of all cylinder centers fixed. Here \( r \) is the bristle radius. The value of \( \varepsilon \) is chosen so that the new configuration has the measured solidity \( \phi \). For this special kind of array the gap between neighboring cylinders is uniform and is given by \( 2\varepsilon r \) where

\[
\varepsilon = 1 - \left( \frac{\phi}{\phi_t} \right)^{1/2}
\]  

(7)

The resistance offered to the flow by the gap between pairs of nearly touching cylinders determine the overall drag and hence the effective permeability of the medium. The analysis below is due to Sangani (1990). The pressure drops as fluid squeezes through a gap of width \( 2\varepsilon r \) at a volume flow rate \( Q \), as shown in figure 3. Here \( Q \) is the two-dimensional volume flow rate. The profile of the cylinder surface can be approximated by

\[
\frac{f(x)}{r} = \varepsilon + \frac{x^2}{2r^2} \quad \text{for} \quad \frac{x}{r} \to 0 \left( \varepsilon^{1/2} \right)
\]

(8)
Assume that inertia terms are negligible and that the viscous forces in the streamwise direction are small compared to those in the normal direction. Hence the equation governing the x-direction velocity component \( \hat{u} \) reduces to

\[
\frac{\mu}{\partial y^2} = \frac{dp}{dx}
\]  

(9)

Integrating the above equation with \( \hat{u} = 0 \) at \( y = f(x) \) and \( \partial \hat{u} / \partial y = 0 \) at \( y = 0 \) we obtain

\[
\hat{u} = -\frac{1}{2\mu} \frac{dp}{dx} [f^2(x) - y^2]
\]  

(10)

Integrating the above velocity profile over the gap and identifying it with volume flow rate \( Q \), we obtain

\[
(\Delta p) \text{ gap} = \frac{9\pi \mu Q}{8\sqrt{2}} \frac{e^{-s/2}}{r^2}
\]  

(11)

Thus the force exerted per unit length and width in direction of flow is \( \Delta p \). The direction of flow however is normal to the line segment joining the centers of the cylinder pair in question. If such a line segment is oriented at an angle \( \theta_i \) as shown in figure 4, then the force vector \( F_i \) per unit length arising over width \( 2r \) due to each gap for volume flow rate \( Q_i \) is given by

\[
F_i = \frac{9\pi \mu Q_i}{8\sqrt{2}} \frac{e^{-s/2}}{r^2} (2r)
\]  

(12)

The component of the force (per unit length) in the direction of mean flow (assumed to be along \( \theta_i = 0 \)) is then obtained after noting that \( Q_i = (2\hat{u} \sin \theta_i) r \)

\[
F_{11} = |F_i| \sin \theta_i = \frac{9\pi \mu e^{-s/2}}{8\sqrt{2}} 2\hat{u} \sin^2 \theta_i
\]  

(13)

Here \( \hat{u} \) is the filter velocity or the superficial velocity. Hence, the mean force \( <F_1> \) is given by

\[
<F_1> = \frac{9\pi \mu \hat{u} Z}{8\sqrt{2}} e^{-s/2}
\]  

(14)
where \( Z \) is the average number of nearest neighbors and the mean value of \( \sin^2 \theta_i \) averaged over all \( \theta_i \) is \( 1/2 \). If the number of cylinders per unit cross-section area is \( 4\phi/\pi d_0^2 \) where \( d_0 \) is the diameter then

\[
|\nabla p_1| = \langle F_1 \rangle = \frac{4\phi}{\pi d_0} \frac{9Z\phi u}{2\sqrt{2}} \varepsilon^{-5/2} \frac{\hat{u}}{d_0^2} \tag{15}
\]

If one was interested in the permeability \( k \) of the medium defined as \( k = \mu \hat{u}/|\nabla p_1| \), then

\[
k = \frac{2\sqrt{2}}{9Z\phi} d_0^2 \varepsilon^{5/2} \tag{16}
\]

which is identical to the expression in Sangani and Yao (1988) except for \( \phi \) in the denominator.

### 2.3 Elastic Behavior Model

The expression in (15) permits us to calculate \( |\nabla p| \), as a function of the filter velocity \( u \) which may vary along the bristle axis as given by (6). Hence, we are in a position to determine the loading on the bristle due to the inter-bristle flow driven by the Couette flow in the clearance region. We define a co-ordinate system shown in figure 5. The deflection of the bristle tip, \( \Delta t \), can be obtained from straightforward application of linear elasticity theory. The radial component of the deflection \( h_0 = \Delta t \cos \beta \) is then the clearance, and is given by

\[
h_0 = \Delta t \cos \beta = \frac{9Z}{2\sqrt{2}} \varepsilon^{-5/2} \frac{\mu u_0 \cos \beta}{\eta} \frac{1}{(\sin \beta)^3} \frac{1}{E I} \frac{1}{\delta} \frac{h^3}{3} \tag{17}
\]

Recall that \( \eta = (1-\phi) (1+\lambda \delta h_0) \), \( \delta = (\lambda \kappa)^{-1/2} \), \( I = \pi d_0^4/64 \). Since the above equation is implicit in \( h_0 \), consider \( h_0 \gg k^{1/2} \) first, so that \( \lambda \delta h_0 \gg 1 \) providing an explicit form,

\[
\left( \frac{h_0}{d_0} \right)^2 = \frac{9Z}{2\sqrt{2}} \left[ 1 - \sqrt{\phi/\phi_t} \right]^{-5/2} \frac{\mu u_0}{(1-\phi)} \frac{k}{d_0^2} \frac{\cos \beta}{(\sin \beta)^3} \frac{h^3}{3E I} \tag{18}
\]

If permeability \( k \) is experimentally determined for the medium then that measured value can be used in the above expression. The recommended values of \( \phi_t \)
and \( Z \) are 0.82 and 4.2 for a random array of cylinders. Hence the expression is valid for \( \phi < \phi_t (=0.82) \). If, however, \( k \) is not known, permeability can be estimated from (16) allowing us to determine \( h_0 \) from

\[
\left( \frac{h_0}{d_0} \right)^2 = \frac{\mu_0}{\phi(1-\phi)} \frac{\cos\beta}{(\sin\beta)^3} \frac{h^3}{3EI} \quad h_0 \gg \sqrt{k}
\]  

(19)

In the absence of any clearance \( h_0 \) vanishes and any initial increase in \( h_0 \) must occur with \( h_0 << k^{1/2} \). Under circumstances that permit us to assume \( \lambda \delta h_0 << 1 \) we obtain

\[
\frac{h_0}{d_0} = \frac{9Z}{2\sqrt{2}} \left[ 1 - \sqrt{\frac{\phi}{\phi_t}} \right]^{-5/2} \frac{\mu_0}{(1-\phi) d_0} \frac{\sqrt{\lambda k}}{(\sin\beta)^3} \frac{h^3}{3EI}
\]  

(20)

Once again \( k \) can either be measured or evaluated from equation (16). In the above expression in addition to \( Z \) and \( \phi_t \) we also need an empirical estimate for the constant \( \lambda^{1/2} \). The constant \( \lambda^{1/2} \) can be identified with \( \alpha \) in Beavers and Joseph (1967) and is a dimensionless quantity depending on the material parameters which characterize the structure of the porous medium within the boundary region where the filter velocity decays to zero, its Darcy value. The value of \( \alpha \) reported by Beavers and Joseph are for Foametal and Aloxite, with effective pore sizes varying between 0.013 inches and .045 inches. The value of \( \alpha \) for these materials was found to vary between 0.1 and 4 with lower values observed at lower pore sizes.

Preliminary estimates of the clearance due to tangential loading can be made from either (19) or (20) and if it turns out that \( h_0 \) is of the order of \( k^{1/2} \) then the quadratic equation (17) can be solved for \( h_0 \). Before discussing the results for the tangential deflection we will develop the analysis for axial deflection. This will permit us to determine their relative magnitudes and establish conditions under which, it may be possible to neglect the clearance due to deflection in one of the directions.

3. Axial Deflection

The axial deflection of the bristles is due to the pressure differential along the axis of the rotating element. It is the purpose of the brush seal to minimize what would otherwise be a leakage flow due to this pressure differential. The axial loading on the bristle is straightforward to estimate since the pressure differential impressed upon the bristle bundle can be assumed to remain unaltered in the presence of leakage flow. If the pressure differential is \( \Delta p = P_h - P_e \) over the width \( w \) of the
bristle bundle (in the axial direction) then the force per unit length, \( q \), acting on the bristle is given by \( q = \Delta P \frac{d_o^2}{w} \). This force acts uniformly over the overhanging length \( a \) of the bristle, i.e. exposed portion between the backing ring of inner diameter \( D_b \) and the shaft, diameter \( D_s \). Since the bristle bundle is clamped at the retaining plate inner diameter \( D_r \), the bristle behavior can be modeled as a bar clamped at origin and simply supported at \( D_b \) with an overhanging distributed load between \( D_b \) and \( D_s \). If we define \( L \) to be the bristle length between the retaining ring ID and the backing ring ID, \( L = (D_r - D_b)/2 \sin \beta \) then the bristle geometry with its axial loading diagram is as shown in figure 6. We wish to determine the displacement, \( \Delta h \), due to the axial deflection of the unloaded member, as shown in figure 7. This quantity is the clearance produced due to the axial loading and would be observed in a static leakage test. In dynamic tests the clearance would be produced by a combination of effects, the tangential as well as the axial loading.

Linear elasticity theory assumes small angles of rotation for the beam and thus would only permit the calculation of the vertical displacement \( \Delta v \) while \( \Delta h \) would remain zero. Typical axial loading and the bristle length to diameter ratios are however, such that it becomes necessary to use large deflection theory in order to model the problem. Thus the differential equation of the deflection curve becomes

\[
\frac{d^2y}{dx^2} \left[ 1 + \left( \frac{dy}{dx} \right)^2 \right]^{3/2} = -\frac{M(x)}{EI}
\]  

(21)

The exact shape of the elastic deflection curve given by the solution to this equation, is called the elastica. The mathematical solution to the problem of determining the elastica has been obtained for many different types of beams and loading conditions, see Frisch-Fay (1962). The solutions to the specific loading of interest here was not available in the existing literature. A particular difficulty is that the problem is statically indeterminate and the reaction force where the bristle is simply supported is unknown. While a linear theory may provide a value of the reaction, it will be approximate at best. This value, however, could be of use as an initial guess in an iterative determination of the reaction force into vertical component \( R \) and horizontal component \( R\tan \theta \), where \( \tan \theta \) is the bristle slope at the support, see figure 7. To determine \( \Delta h \) we need to solve for the elastica and...
terminate the curve at a point where the length of the curve is \((L + a)\). Here we assume that any elongation of the bristle is negligible or of an order smaller than that under consideration. In the deformed position of the bristle the axial loading is no longer applied over the overhang initial length \('a'\) but over the overhang length \(a' = a - \Delta_h\) in the deformed position. The direction of the axial force, however, continues to remain vertical in the deformed position.

Solution to the problem described above requires us to integrate (21), with a moment distribution function \(M(x)\) given by

\[
M(x) = qa' \left(\frac{a}{2} + L - x\right) - R(L - x) - R\tan \theta y \quad 0 < x < L
\]

\[
M(x) = \left(\frac{q}{2}\right) (L + a' - x)^2 \quad L < x < L + a
\]  \(\text{(22)}\)

where \(a'\) and \(\tan \theta\) are unknown and are determined as part of the solution \(y(x)\). The reaction force, however, is still unknown because the problem is statically indeterminate. This difficulty is easily overcome, especially since the solution is perhaps most easily obtained on a computer. An initial guess of \(R\) is made from linear theory. The preliminary solution thus obtained however, will in general fail to pass through the support at \((L,0)\). The magnitude of the reaction force is gradually changed until the elastica does pass through, \((L,0)\). It is convenient to normalize \(x\) and \(y\) with length \(L\), i.e. \(x^* = x/L\) and \(y^* = y/L\). Dropping asterisk now equations (21) and (22) become

\[
y''/\left(1+y^2\right)^{3/2} = -M(x) \quad \text{with} \quad y(o) = 0 \quad y'(o) = 0, \quad \text{where}
\]

\[
M(x) = C_{eff} \left\{ \frac{1}{2} + (1/a') (1-x) \right\} - \alpha (1-x) - \alpha \tan \theta y \quad 0 < x < 1
\]

\[
M(x) = \left(\frac{C_{eff}}{2}\right) (1/a')^2 (1 + a' - x)^2 \quad 1 < x < 1 + a/L
\]  \(\text{(23)}\)

where \(C_{eff} = C (a'/a)^2\), \(C = qa^2L/EI\) and \(\alpha = RL^2/EI\)

The problem shown above was solved numerically for various values of the loading parameter \(C\) and the overhang ratio \(a/L\). The elastica curves for \(a/L = 0.2\) are shown in figure 8. Note that the axis in the \(y\)-direction is stretched considerably for clarity. The quantity of interest here is the clearance \(\Delta_h\), the variation of which with loading parameter \(C\) is shown in figure 9 for several overhang ratios \(a/L\). Note that the small deflection theory value of \(\Delta_h\) is identically zero for all \(C\). We observe that the departure from this value as loading is increased depends upon the overhang parameter. It turns out that for typical gas turbine applications brush seals may be operating in a parameter range where \(\Delta_h\) is rapidly increasing with \(C\) and \(a/L\).
The actual value of the reaction force is not of immediate interest once the axial deflection is known, however, it may be of use in the following manner. Earlier analysis to determine the circumferential deflection assumed that the friction at the bristle-backing ring interface was negligible. The bristle orientation under axial loading shown in figure 8 indicates that the only point of contact may be at the inner edge of the backing ring where the normal force acting on the bristle is given by \( R \cos \theta \). An estimated value of the static Coulomb friction coefficient would permit an approximate evaluation of the tangential restraining force. This force would act on the bristle layer in contact with the backing ring. While in this paper we do not account for this friction force in the calculation of the circumferential deflection the value of \( R \) and \( \theta \) may prove useful for future work.

4. Discussion

Under dynamic conditions the actual deflection would be due to both the circumferential and axial loads and a vector sum of forces has to be used to solve the three-dimensional elastica problem. Additional simplification is possible if we can demonstrate that the deflection in one of the directions is small compared to the other. An explicit expression for their relative magnitude is not available because of the lack of a closed form formula for the axial deflection.

The numerical results of figure 9 establish that the behavior of \( \Delta h (C, a/L) \) is indeed nonlinear, and may be of importance in the design of brush seal systems. In addition to the expected non-linearity in the response to loading parameters \( C \) the displacement \( h \) is also sensitive to \( a/L \) ratios. Thus it is not just the overhang length that is relevant even though it is the length exposed to a pressure differential but also the size of the retaining plate. The analysis carried out here while making several idealizations may provide insight into the dependence of the clearance on geometry and operating conditions.

ACKNOWLEDGMENTS

I would like to thank Dr. Prithwish Basu of E G & G Sealol for introducing the author to the problem and providing significant insight along the way. I am also grateful to Mr. Albert Bonamio and Dr. Hayri Cabuk for some of the calculations reported here.
BIBLIOGRAPHY


Figure 1 Schematic of Brush Seal System.

Figure 2 Physical model of clearance channel bounded by shaft on one side and porous bristle bundle on other.
Figure 3: Schematic of Volume Flow $Q$ through a gap of size $2r$.

Figure 4: A pair of neighbouring cylinders in a random array.

Figure 5: Schematic diagram of clearance region and the porous bristle bundle matrix. Velocity distributions in each are shown at left. Bristle displacement is normal to its axis.

$h_o = A \cos \beta$
Figure 6 Axial loading diagram for a single bristle.

Figure 7 Schematic diagram showing the deformed shape of the bristle under axial loading. Horizontal displacement is such that the length of the bristle is unchanged under loading.

Figure 8 Computed Bristle shapes for axial loading C. The overhang ratio $a/L = 0.1$. 
Figure 9: Clearance generated due to axial loading for various values of $C$. $a/L = 0.2, 0.4, 0.6$.

Figure 10: Variation of the normalized reaction force $R^*$, where $R^* = (R\sqrt{L/\pi I})/C_{eff}$. 

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Brush Seals For Turbine Engine
Fuel Conservation

Contract No. N00140-90-C-3199
W. Voorhees, U.S. Navy/NAWC Program Engineer

August 6, 1992

Presented At:
Brush Seal System Workshop
NASA Lewis Research Center
Cleveland, Ohio

R. Korzun
W. Ostergren

GE Aircraft Engines
Lynn, Massachusetts
GEAE Brush Seal Program Presentation Summary

Brush Seals for Turbine Engine Fuel Conservation

General Electric Aircraft Engines (GEAE) has an ongoing program sponsored by NAWC (Contract No. N00140-90-C-3199) for the evaluation of brush seals. This is a summary of the program status as presented during the Brush Seal System Workshop at the NASA Lewis Research Center in Cleveland, Ohio on August 6, 1992 by Ron Korzun.

The objective of the program is to design, procure and test brush seals intended to be suitable for replacing the inner and outer balance piston seals in the T407 turboprop engine. An existing T407 low pressure turbine rig was modified to conduct the brush seal testing. The rig which includes the power turbine shaft accurately simulates the dynamics of the engine. A picture and cross section of the rig are shown in Figures 1 and 2.

**Figure 1. T407 Rig Assembled in Test Platform**

The design of the seals was conducted with the assistance of the seal supplier EG&G Sealoil. Some design parameter and features are presented in Figures 3 and 4.

**Figure 2. T407 IBP and OBP Brush Seal Dynamic Test Rig**

**Figure 3. Seal Design and Fit - Ups**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>OBP</th>
<th>IBP</th>
</tr>
</thead>
<tbody>
<tr>
<td>Brush Seal Inner Diameter Cold (B)</td>
<td>1.88</td>
<td>1.88</td>
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<tr>
<td>Brush To Runner Diameter Interference - Cold (I)</td>
<td>0.06</td>
<td>0.06</td>
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<tr>
<td>Brush To Runner Diameter Interference - Hot (I)</td>
<td>0.10</td>
<td>0.10</td>
</tr>
<tr>
<td>Brush Axial Width (C)</td>
<td>0.26</td>
<td>0.26</td>
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<tr>
<td>Backing Plate (GAP)</td>
<td>0.051</td>
<td>0.044</td>
</tr>
<tr>
<td>Diameter Interference Fit With Stator Support - Cold (A)</td>
<td>0.006</td>
<td>0.004</td>
</tr>
<tr>
<td>Maximum Stress - Seal Support</td>
<td>10 KSI</td>
<td>25 KSI</td>
</tr>
<tr>
<td>Maximum Stress - Brush Seal</td>
<td>13 KSI</td>
<td>17 KSI</td>
</tr>
</tbody>
</table>

* At 55 KSI, Nominal Fit Up
The test plan calls for cyclic test to evaluate the leakages at operating pressures and temperatures. The test plan also calls for the evaluation of the effect of seal pack width and rotor eccentricity. The brush seal design goals are to achieve or exceed a 50% leakage reduction versus labyrinth seals. This must be accomplished without affecting rotor life. The test will also evaluate runner coating wear, heat generation and corrosion.

The project is carried out under the direction of Bill Voorhees, the NAWC Project Engineer with the assistance of Guy Ullman, the NAVAIR Project Engineer and Carl Grala, the NAWC Component Engineer. At GEAE Warren Ostergren is the program manager. Ron Korzun is the design engineer and Bert Campbell is the test engineer. EG&G Sealol’s support has come from program manager, Chuck Nevola and design engineer, Bob Johnson.

As of the August review, the build of the test rig for its initial testing was in process. GEAE looks forward to presenting the results of the test program during a future NASA workshop.

---

Program Objective

Design, Procure, And Test Brush Seals Intended To Be Suitable For Replacing The Inner And Outer Low Pressure Balance Piston Labyrinth Seals In the T407 Turboprop Engine.
Program Approach

- Design And Procure Brush Seals
- Modify And Instrument An Existing T407 Low Pressure Turbine Test Rig
- Conduct Cyclic Tests To Evaluate Seal Leakage At Operating Pressures And Temperatures
- Evaluate Effect Of Seal Pack Width And Rotor Eccentricity

Project Organization

NAWC Project Engineer
Bill Voorhees

GEAE Program Manager
Warren Ostergren

EG&G Sealol Program Manager
Chuck Nevola

GEAE Design Engineer
Ron Korzun

NAVAIR Project Engr.
Guy Ullman

GEAE Test Engineer
George Fischer
Bert Campbell

GEAE Assembly & Test
Frank Emmith
Charlie Cooke

NAWC Component Engr.
Carl Grall

GEAE Seal Consultant
Brent Bristol
Brush Seal Design Goals

- Achieve or exceed predicted leakage reduction versus labyrinth seals
  - OBP - 59% Reduction
  - IBP - 45% Reduction

- Rotor part life not limited by brush contact
  - Runner coating wear
  - Heat generation
  - Corrosion

T407 IBP and OBP Brush Seal Dynamic Test Rig

RIG OPERATING BOUNDARY CONDITIONS

IBP Discharge Air
W = .006 - .022 PPS

OBP Seal Discharge Cavity
400-720 °F
14.9-16.3 PSIA

OBP Discharge Air
W = .009 - .040 PPS

Rig Inlet Air
W = .015-.062 PPS

Balance Piston Inlet Cavity
216-527 °F
26.3 - 63.7 PSIA

IBP Seal Discharge Cavity
293-530 °F
15.6 - 30.0 PSIA

Rotor Speed Range, 5,500-15,000 RPM
Power Turbine Rotor Assembly

Exhaust Frame Stator Assembly With Brush Seals Installed
Exhaust Frame/Outer Housing Assembly

T407 Rig Assembled In Test Platform
Key Brush Seal/Rig Features

- Spacer Arms Used To Position Seals In 2 Locations On Runner
- Chromium Carbide Runner Coating Compatible With Haynes 25 Bristles
- Axial Retention Sleeves With Locking Pin
- INCO 625 Support With HAST-X Brush Seal Backing Plates Gives Best Growth Compatibility To Avoid Errant Rig Leakages

Outer Balance Piston Brush Seal
### Inner Balance Piston Brush Seal

![Image of Inner Balance Piston Brush Seal]

### Seal Design and Fit - Ups

<table>
<thead>
<tr>
<th>Parameter</th>
<th>QR P</th>
<th>IRP</th>
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<tr>
<td>Brush Seal Inner Diameter Cold (B)</td>
<td>10.1&quot;</td>
<td>5.6&quot;</td>
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<tr>
<td>Brush To Runner Diametral Interference - Cold (B)</td>
<td>.006</td>
<td>.008</td>
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<td>Brush To Runner Diametral Interference - Hot (B)</td>
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<td>.010</td>
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<td>Brush Axial Pack Width (C)</td>
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<td>Backing Plate GAP (D)</td>
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<td>.044</td>
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<tr>
<td>Diametral Interference Fit With Stator Support - Cold (A)</td>
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<td>.004</td>
</tr>
<tr>
<td>*Maximum Stress – Seal Support</td>
<td>18 KSI</td>
<td>25 KSI</td>
</tr>
<tr>
<td>*Maximum Stress – Brush Seal</td>
<td>13 KSI</td>
<td>17 KSI</td>
</tr>
</tbody>
</table>

* At SS IRP, Nominal Fit Up

- Brushes Maintain Contact With Rotor At All Operating Conditions
- Backing Plate Distance Sized For Worst Case Conditions Expected In Field
- Backing Interference Maintained At All Operating Conditions - Avoid Leakage
- Stress Is Acceptable - Below .2% Yield Strength
## Brush Seal Data Used To Size
### T407 Brush Seals

<table>
<thead>
<tr>
<th>Test Conditions</th>
<th>GE</th>
<th>Sealol</th>
<th>Technical Literature</th>
</tr>
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<tbody>
<tr>
<td>Pressure Drop</td>
<td>0-80</td>
<td>15-25</td>
<td>20</td>
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<tr>
<td>Temperature (F)</td>
<td>70</td>
<td>70</td>
<td>600</td>
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<tr>
<td>Surface Speed (Ft/S)</td>
<td>430</td>
<td>375</td>
<td>668</td>
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</table>

<table>
<thead>
<tr>
<th>Seal Parameters</th>
<th>GE</th>
<th>Sealol</th>
<th>Technical Literature</th>
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</thead>
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<tr>
<td>Diameters</td>
<td>5.1, 11.3</td>
<td>5.4</td>
<td>5.1</td>
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<tr>
<td>Backing Plate Height</td>
<td>.04-.130</td>
<td>.047</td>
<td>.02,.03</td>
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<tr>
<td>Pack Thickness</td>
<td>.018-.027</td>
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<td>.027</td>
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<td>Bristle Diameter</td>
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<tr>
<td>Bristle Angle</td>
<td>45-56</td>
<td>36-56</td>
<td>45</td>
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<tr>
<td>No. Of Stages</td>
<td>1</td>
<td>1</td>
<td>1, 2</td>
</tr>
</tbody>
</table>

- The above ranges stated are for the test data which was readily available (10/91) to use in evaluating the T407 Seals.
- Additional studies are continually in process at GEAE (Ruston) and at Sealol

## Brush Seal Test Data - Flow Parameter
### Versus Pressure Parameter

![Graph](attachment:image.png)

Press param \((1-(Pd/Pu)^2)^{0.5}\)
## Test Plan Schedule

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>ASO</td>
<td>N</td>
</tr>
<tr>
<td>I.</td>
<td>Break In Testing – 1st Set</td>
<td>50 hrs</td>
</tr>
<tr>
<td>II.</td>
<td>Cyclic &amp; Endurance Testing - 1st Set</td>
<td>150 hrs</td>
</tr>
<tr>
<td>III.</td>
<td>Cyclic &amp; Endurance Testing - 2nd Set</td>
<td>150 hrs</td>
</tr>
<tr>
<td>IV.</td>
<td>Alternate Seal Design Testing</td>
<td>50 hrs</td>
</tr>
<tr>
<td>V.</td>
<td>Eccentricity Testing - 3rd Set</td>
<td>50 hrs</td>
</tr>
</tbody>
</table>

*Test Plan Includes Extensive Testing On Three Sets Identical Seals And One Alternate Design.*

## Summary

- OBP And IBP Brush Seal Designs Completed And Fabricated
- LPT Dynamics Rig Modifications Completed
- Test Plan Defined
- Test Cell Checkout Completed
- Testing To Begin In August
Tribopair Evaluation of Materials for Brush Seal Applications

From notes and discussion of talk by J. Derby, EG&G
by R.C. Hendricks

Derby and England investigated several brush seal system tribopairs from bristle materials Haynes 25, Inconel 718, and proprietary materials called Alloys A, B, C, D, and E and coatings chromium carbide, Triboglide, tungsten carbide, chromium oxide, aluminum oxide, Tribaloy, Tribomet T-104C.

Haynes 25 is a cobalt chromium nickel tungsten based superalloy that forms an oxide resistive Cr2O3 film.

Inconel 718 is a precipitation hardenable nickel chromium superalloy good to 1300 F.

Alloy A (Ni Cr Al base superalloy solid-solution strengthened) is being used in gas turbine hot spots and develops a tenacious Cr2O3 and A12O3, yittria-modified oxide layer.

Alloy B (solid-solution, and carbide strengthened Ni Cr, W based superalloy) with good strength at elevated temperatures developing an Cr2O3 oxide film that is enhanced by lanthanum, and used in combustion cans.

Alloy C (mechanically alloyed, oxide dispersion strengthened, Fe, Cr, Al based superalloy) has excellent resistance to oxidation due to a tenacious Y2O3 stabilized A12O3 and Cr2O3 film, good to perhaps 2100 F.

Alloy D (solid-solution strengthened by addition of W and precipitation of M6 and M23C6 carbides Co, Cr, W, Ni based superalloy) is one of the first sheet alloys developed for aircraft engines. Adding lanthanum is reported to modify the protective oxide layer up to 2000 F.

Alloy E (age hardened Ni, Mo, Cr based superalloy without gamma prime precipitate and hardening believed based on Ni2(cr,Mo) stoichiometry) with service temperatures to 1400 F.

Although not reported Haynes 125 is known to have a higher use temperatue but more data are required on tribological pairing.

Chromium carbide has superior wear and friction performance. Sprayed coatings contain Cr3C2 and Cr7C3 mixtures produce an increase in hardness. The CrO was applied using HVOF.

Triboglide is a CrC containing additives of 12 wt. percent barium and calcium fluoride solid lubricants based on the work of Sliney at NASA-LeRC. Spray parameters (standoff, angle, powder size, feed rate, temperature) were investigated and use of HVOF was preferred.

Tungsten carbide contains a Co binder and exhibits phases WC, W2C, and Co3W3C with decarbonization of some WC above 900F. Union Carbide D-Gun was preferred with 8-percent Co binder.
Chromium oxide has higher friction but used within the industry has low thermal expansion and thermal conductivity.

Aluminum oxide was applied using air plasma spray (APS) with a bond coat of 0.001-0.002 inch.

Tribaloy T-800 is a Co based with Mo, Cr, and Si additives and APS and HVOF applied followed by a heat treatment.

Tribaloy T-104C is Co based that is electrodeposited such that CrC particles are codeposited in the coating. Exhibits good friction and wear characteristics and is almost entirely metallic (good rotor adherence).

The tests were performed using a 2.0 inch diameter, 0.040 inch-two-lobed-cam rotor at 1200F at speeds of 10, 20, and 30 krpm, providing about 15E9 fatigue cycles. The interface was assumed to be line to line at the mean equivalent diameter although no preload information was given.

In a second of tests at 0-pressure drop, conducted at 2, 20, 40, and 60 krpm at 800F the nominal brush-rotor clearance was -0.010 inch-radial.

Inconel 718 and Haynes 25 bristles form unstable Cr2O3 layers with leading edge alloy fractures. Alloy A is least damaged by fatigue cycles and most oxidative resistant.

Oxide coatings exhibit microfracturing and grain pullout which promotes wear and cobalt alloy bristles performed poorly due to a transformation from hexagonal close to face centered at 400C (750F).

Alloy A/Triboglide (15-20 microinch Ra) provided good friction behavior vs sliding speed (varies from 0.14 to 0.25) with Inco 718/Triboglide constant at 0.3. The Haynes 25/Triboglide is good at surface speeds of 100 to 350 ft/s while Haynes 25/CrC increased linearly from 0.23 to 0.45 at 500 ft/s.

As an editorial note, there does exist some transition from hexagonal close pack to cubic crystal structure between 350 C and 400 C. Within this temperature range the wear increases and is up to ten times higher in a vacuum (ref. 2). In air the formation of oxides tends to mitigate wear and for low sliding speeds wear actually decreases as temperature is increased (ref. 3). However data at both elevated temperature and surface speed are needed.

For more information


DAMPING SEAL BEARINGS

George L. von Pragenau, Huntsville/Alabama, (205) 536-6832
### ABOUT TECHNOLOGY

Technology is a state of readiness to realize dreams beyond our limits.

Lasting technology comes by faith in God, his inspiration, loving care, risk, stamina, patience, labor, cooperation, appreciation, and liberty.

Technology thrives on sound engineering; yet dares old limits, seemingly in conflict, to find ways outside the status quo to a brighter future.
HIGH PRESSURE TURBOPUMP WHIRL DATA

HIGH PRESSURE FUEL TURBOPUMP
HPFTP 2106R3 50 % WHIRL

HIGH PRESSURE OXYGEN TURBOPUMP
HPOTP 0303 90 % WHIRL

BASIC ROTORDYNAMIC MODEL

\[
\begin{align*}
F_y &= K_y - (c_0)^2 M + s C + s^2 M_r + \omega \omega \\
F_z &= -Q - c_0 (C + s^2 M)
\end{align*}
\]

\[
\begin{align*}
F_1 &= \text{EXTERNAL ROTOR FORCES} \\
C &= \text{SEAL INDUCED DAMPING} \\
K_1 &= \text{BEARING+SEAL STIFFNESSES} \\
M_r &= \text{ROTOR MASS PLUS M} \\
Q &= \text{ROTOR SPEED IN RADIANS} \\
M &= \text{SEAL FLOW INDUCED MASS} \\
Q &= \text{OTHER WHIRL DRIVERS} \\
s &= \text{LAPLACE OPERATOR RADIANS} \\
v &= \text{COUETTE FLOW VELOCITY} \\
w &= \text{ROTOR SURFACE SPEED}
\end{align*}
\]
ROTOR SPEED LIMIT

RESONANCE FREQUENCY (RADIANS) 
\[ \omega_o = \left( \frac{(K_y + K_z + (\frac{Q}{C})^2 + (CQ2M)/C)}{2Mr} \right)^{0.5} \]

DETERMINANT AT RESONANCE 
\[ D_o = [CQ + Q/C]^2 + [C^2 + (CQ2M)^2] - \omega_o^2 [C^2 + (CQ2M)^2] - \frac{(K_y - K_z)^2}{4} \]

STABILITY CONDITION (\( D_o < 0 \)) 
\[ [CQ + Q/C]^2 + [C^2 + (CQ2M)^2] < \omega_o^2 [C^2 + (CQ2M)^2] + \frac{(K_y - K_z)^2}{4} \]

SPEED LIMIT FOR UNIFORMITY 
\[ Q < \left( \omega_o - \frac{Q}{C} \right) / C = Q_o \quad \text{for} \quad K_y = K_z \]

APPROXIMATE SPEED LIMIT 
\[ Q < \frac{\omega_o}{C} \quad \text{for} \quad K_y = K_z \text{ and } \omega_o * C >> Q \]

AT THE WHIRL ONSET SPEED \( Q_o \) THE ROTOR BECOMES UNSTABLE AND WHIRLS. NOTICE THAT HIGH DAMPING \( C \) AND A LOW COUETTE FACTOR \( c \) INCREASE THE SPEED LIMIT. DAMPING SEALS MEET BOTH REQUIREMENTS. TYPICALLY \( c \) IS 0.20. FOR SMOOTH SEALS AND JOURNAL BEARINGS \( c \) IS 0.50.

DAMPING SEAL
EARLY IN 1976 THE HIGH PRESSURE FUEL TURBOPUMP (HPFTP) SPEED LIMIT WAS 22,000 RPM TO AVOID A 175 Hz SUBSYNCHRONOUS ROTOR WHIRL. THE REQUIRED OPERATIONAL SPEED IS 36,000 RPM.

STIFFER BALL BEARING SUPPORTS AND TWO STIFFER SMOOTH SHAFT SEALS (INSTEAD OF LABY SEALS) RAISED THE 1st CRITICAL SPEED TO 18,000 RPM AND THE WHIRL TO AN INTERMITTENT 300 Hz.

DAMPING SEALS WERE INVENTED 1981 TO ELIMINATE THE 50 % SUBSYNCH WHIRLS OF SMOOTH SEALS. DAMPING SEALS WERE INSTALLED 1989 IN THE HPFTP. COULOMB FRICTION DEVICES WERE ABANDONED.

ONE HIGH PRESSURE OXYGEN TURBOPUMP (HPOTP) EXPLODED 8 SEPTEMBER 1977 FROM A 95 % SUBSYNCHRONOUS WHIRL, CAUSED BY INTERNAL ROTOR FRICTION, THE MOST VIOLENT WHIRL-DRIVER.

SINCE THE 1st REFLIGHT, DISCOVERY ON 29 SEPTEMBER 1988, EVERY HPOTP FLIGHT PUMP HAS DAMPING SEALS IN THE PREBURNER PUMP (PBP) INLET AND DISCHARGE TO AVOID THE 95 % WHIRL.

HIGH BALL WEAR LIMITS THE HPOTP TO 2 FLIGHTS AND IGNITED A FIRE 23 JUNE 1989 IN A TEST. TESTS W/O BALL BEARINGS CONFIRMED THAT DAMPING SEALS ARE SUPERIOR HIGH SPEED BEARINGS.
HPOTP DAMPING SEAL BEARING ENGINE TESTS WITH BALL BEARINGS

CAGE HARMONIC AMPLITUDE SUM (9-5-89)

HPOTP PUMP END BEARING TEST SAMPLE

<table>
<thead>
<tr>
<th>HPOTP ENGINE TEST NO.</th>
<th>TIME SUM</th>
</tr>
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<tbody>
<tr>
<td>0307# NUMBER</td>
<td>SEC.</td>
</tr>
<tr>
<td>R3</td>
<td>2105</td>
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<tr>
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<td>502</td>
</tr>
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</tr>
<tr>
<td>R4</td>
<td>0210</td>
</tr>
<tr>
<td>R4</td>
<td>**</td>
</tr>
</tbody>
</table>

* BALL BEARING PRELOAD AND SUPPORT WAS LOST AT 3509 SEC. OF TEST TIME.
** PUMP END BEARING TEST TIME WAS 5829 SEC. WITH 2320 SEC. (8 STARTS AND 9 STOPS) ON THE DAMPING SEAL BEARING. THE TURBINE END BEARING REACHED 8303 SEC. TEST TIME.

HPOTP DAMPING SEAL BEARING ENGINE TESTS W/O BALL BEARINGS

NASA MSFC AND ROCKETDYNE CONDUCTED 7 SUCCESSFUL ENGINE TESTS FROM 12 MARCH TO 11 JUNE 1992 WITH THE DAMPING SEAL BEARING FUNCTIONING AS A HIGH PRESSURE SHAFT SEAL, CRITICAL DAMPER, AND STIFF BEARING; REPLACING A Laby. SEAL AND PREBURNER PUMP (PBP) DUPLEX BALL BEARING.

0.008 INCH Y PROXIMITY PROBE TONY R. FIORUCCI TTB 29, 12 MARCH 92

STALL: 13Hz 21Hz 34Hz 80Hz 27Hz 21Hz 16Hz 7Hz 4Hz
SPEED: 21,600RPM 27,600 16,800RPM (LINED UP WITH ABOVE TIME SCALE)
HYDROSTATIC BEARING

DAMPING BEARINGS

STATOR FEED VERSION

ROTOR FEED VERSION

254
SEALS & BEARINGS DYNAMIC & LEAKAGE DATA

<table>
<thead>
<tr>
<th>SEALS AND BEARINGS</th>
<th>STIFFNESS (MN/m, kN/m)</th>
<th>DAMPING (kNs/m, lb s/in)</th>
<th>WHIRL FREQUENCY nja</th>
<th>LEAKAGE (kg/s, lb/s)</th>
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<tr>
<td>HPOTP PBP DUPLEX BALL BEARING</td>
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<td>3.5 (20)</td>
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<td>2.7 (6)*</td>
</tr>
<tr>
<td>HPOTP PBP DISCH.LABYRINTH SEAL</td>
<td>3.5 (20)</td>
<td>4.0 (23)</td>
<td>0.50</td>
<td>2.3 (5)</td>
</tr>
<tr>
<td>HPOTP PBP DISCH.DAMPING SEAL</td>
<td>100 (580)</td>
<td>53 (300)</td>
<td>0.19</td>
<td>2.7 (6)</td>
</tr>
<tr>
<td>HPOTP TURBINE HYDROSTATIC BEARING</td>
<td>1100 (6000)</td>
<td>400 (2300)</td>
<td>0.50</td>
<td>18 (39)</td>
</tr>
<tr>
<td>HPOTP TURBINE DAMPING BEARING</td>
<td>1200 (6800)</td>
<td>670 (3800)</td>
<td>0.27</td>
<td>9.1 (20)</td>
</tr>
<tr>
<td>HPFTP SMOOTH SEAL</td>
<td>68 (390)</td>
<td>28 (160)</td>
<td>0.50</td>
<td>0.6 (1.4)</td>
</tr>
<tr>
<td>HPFTP DAMPING SEAL</td>
<td>26 (150)</td>
<td>44 (250)</td>
<td>0.17</td>
<td>0.3 (0.7)</td>
</tr>
<tr>
<td>HPFTP TURBINE ROLLER BEARING</td>
<td>610 (3500)</td>
<td>none</td>
<td>n/a</td>
<td>1.1 (2.5)*</td>
</tr>
<tr>
<td>HPFTP TURBINE HYDROSTATIC BEARING</td>
<td>510 (2900)</td>
<td>89 (510)</td>
<td>0.50</td>
<td>2.3 (5.0)</td>
</tr>
<tr>
<td>HPFTP TURBINE DAMPING BEARING</td>
<td>530 (3000)</td>
<td>160 (920)</td>
<td>0.18</td>
<td>1.1 (2.5)</td>
</tr>
</tbody>
</table>

* LEAKAGE THROUGH BALL AND ROLLER BEARINGS ARE COOLANT FLOWS. HPOTP IS THE HIGH PRESSURE OXYGEN TURBOPUMP. PBP IS THE PREBURNER PUMP OF THE HPOTP. HPFTP IS THE HIGH PRESSURE FUEL TURBOPUMP. HPOTP AND HPFTP DATA ARE FOR 30,000 RPM AND 36,000 RPM, RESPECTIVELY.
## Generic Bearing Comparison

<table>
<thead>
<tr>
<th>ITEMS</th>
<th>BEARING TYPES</th>
<th>BALL</th>
<th>ROLLER</th>
<th>HYDROSTATIC</th>
<th>DAMPING</th>
</tr>
</thead>
<tbody>
<tr>
<td>MOVING PART COUNT</td>
<td>33, duplex</td>
<td>17</td>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>DN, BORE mm x RPM</td>
<td>&lt; 2×10⁶</td>
<td>&lt; 2×10⁶</td>
<td>&lt; 10⁷</td>
<td>&lt; 10⁷</td>
<td></td>
</tr>
<tr>
<td>HOOP STRESS MPa (ksi)</td>
<td>172 (25)</td>
<td>310 (45)</td>
<td>n/a</td>
<td>n/a</td>
<td></td>
</tr>
<tr>
<td>HERTZIAN ST. MPa (ksi)</td>
<td>2412 (350)</td>
<td>2412 (350)</td>
<td>41 (6)</td>
<td>41 (6)</td>
<td></td>
</tr>
<tr>
<td>PRECISION μm (mil)</td>
<td>0.5 (0.02)</td>
<td>0.5 (0.02)</td>
<td>25 (1)</td>
<td>25 (1)</td>
<td></td>
</tr>
<tr>
<td>ROLLING STABILITY</td>
<td>skidding</td>
<td>skewing</td>
<td>n/a</td>
<td>n/a</td>
<td></td>
</tr>
<tr>
<td>HIGH SIDELOAD</td>
<td>wear</td>
<td>skewing</td>
<td>ok</td>
<td>ok</td>
<td></td>
</tr>
<tr>
<td>WHIRL ONSET SPEED</td>
<td>limit</td>
<td>limit</td>
<td>limit</td>
<td>none</td>
<td></td>
</tr>
<tr>
<td>BEARING DAMPING</td>
<td>negligible</td>
<td>none</td>
<td>high</td>
<td>high</td>
<td></td>
</tr>
<tr>
<td>BEARING TILTING</td>
<td>&lt; minute</td>
<td>&lt; minute</td>
<td>&gt; minute</td>
<td>&gt; minute</td>
<td></td>
</tr>
<tr>
<td>DEADBAND/TIGHT FIT</td>
<td>conflict</td>
<td>conflict</td>
<td>relaxed</td>
<td>relaxed</td>
<td></td>
</tr>
<tr>
<td>FAILURE MODE</td>
<td>catastrophic</td>
<td>catastrophic</td>
<td>benign</td>
<td>benign</td>
<td></td>
</tr>
<tr>
<td>BEARING LIFE LIMIT</td>
<td>wear</td>
<td>skewing</td>
<td>none *</td>
<td>none *</td>
<td></td>
</tr>
</tbody>
</table>

* NO WEAR AT FULL SPEED. ONLY OCCASIONALLY LIGHT BRUSHING AT LOW SPEED IN START AND STOP.

### Outlook

GOD'S LIBERATING CREATIVITY IS JOYFULLY ACKNOWLEDGED IN FAILURE TO RECOVER (& IN SUCCESS).

DAMPING SEALS SUPPRESS ROTOR WHIRL AS PROVEN WITH SPACE SHUTTLE MAIN ENGINE (SSME) PUMPS.

DAMPING SEAL BEARINGS PROVED TO BE SUPERIOR HIGH SPEED BEARINGS IN SEVERAL SSME TESTS.

DAMPING SEAL & BEARING SIZES AND FLOWS READILY RETROFIT SEALS, BALL AND ROLLER BEARINGS.

DAMPING SEAL & BEARING OFFER COMPARATIVELY INFINITE LIFE AND SIMPLIFY TURBOPUMP DESIGNS.

CRITICAL SPEEDS BECOME NONCRITICAL AND CATASTROPHIC FAILURE MODES BECOME RATHER BENIGN.

DILEMNAS BECOME DESIGN OPTIONS AND FABRICATION/ASSEMBLY/MAINTENANCE OFFER GREAT SAVINGS.

NASA AND ROCKETDYNE HAVE THE OPPORTUNITY TO SAVE $10 MILLION/YEAR ON SHUTTLE FLIGHTS.
CROSS-FORCES FROM LABYRINTH SEALS. MECHANISMS AND UPSTREAM COUPLING

By

Knox Millsaps
and Manuel Martinez-Sanchez

MIT, Gas Turbine Laboratory

OUTLINE

- EXPERIMENTAL DATA AND THEORETICAL ANALYSIS OF ROTORDYNAMIC FORCES IN SINGLE-CAVITY LABYRINTHS.

- PARAMETERS VARIED: INLET SWIRL, PRESSURE RATIO, WHIRL SPEED, SPIN SPEED, SEAL LENGTH, LAND SURFACE (SMOOTH VS. HONEYCOMB).

- DATA WERE SEAL CAVITY REAL-TIME PRESSURE DISTRIBUTIONS

MAJOR FINDINGS

- PRESSURE FORCES ARE SUM OF IDEAL COMPONENT, PROPORTIONAL TO RELATIVE SWIRL, PLUS FRICTION-INDUCED COMPONENT, PROPORTIONAL TO SWIRL CHANGE.

- THE IDEAL COMPONENT VANISHES WHEN FLUID SWIRL EXACTLY FOLLOWS TRAVELLING WAVE OF GAP VARIATION DURING WHIRL. THIS COMPONENT IS SOLELY RESPONSIBLE FOR DAMPING.

- THE VISCOUS COMPONENT ALTERS CROSS-STIFFNESS, BUT NOT DAMPING.

- DAMPING DATA CAN BE EXTRACTED FROM STATIC TESTS WITH VARYING SWIRL.

- UPSTREAM NONUNIFORMITIES DUE TO SEAL ECCENTRICITY STRONGLY FEED BACK INTO CAVITY PRESSURE PATTERN.
CROSS-FORCE MECHANISMS

(1) INVISCID
- WITH ECCENTRIC ROTOR, TANGENTIAL FLOW IN CAVITY SEES VARYING CROSS SECTION
- IN REGIONS OF INCREASING AREA, CONTINUITY REQUIRES ADDITIONAL FLOW TO BE BROUGHT FROM UPSTREAM (OR A REDUCED DISCHARGE DOWNSTREAM)
- THIS THEN MEANS LOW P IN THESE AREAS, WHICH INTEGRATES TO FORWARD-WHIRLING FORCE.
- THIS ARGUMENT ASSUMES CONSTANT VELOCITY. BERNOULLI EFFECTS MODIFY (REDUCE) IT, BUT BASICS REMAIN
- THE RELEVANT TANGENTIAL VELOCITY IS WITH RESPECT TO THE WHIRLING FRAME, I.E., V* - ΩR. THIS IS THE ORIGIN OF DAMPING (FORCE = 0 WHEN V* = ΩR)

(2) VISCOUS
- BECAUSE OF WALL FRICTION, V* (IN CAVITY) CAN BE SMALLER (OR LARGER, AT HIGH ω) THAN V*i (INLET)
- ASSUMING V* < V*i, INCOMING LEAKAGE FLUID ENERGIZES CAVITY FLOW (dp/dθ > 0)
- MORE FLOW ENTERS IN WIDER GAP REGION, SO P PEAKS 90° AFTER IT. THIS RESULTS IN FORWARD-WHIRLING FORCE
- NOTE ESSENTIAL VELOCITY HERE IS V*i - V*, REGARDLESS OF Ω. SO THIS FORCE COMPONENT IS INDEPENDENT OF WHIRL (NO DAMPING)
Figure 2.6: Test section schematic showing the geometry and flow variables when the swirl vanes feed into an upstream swirl cavity. Also shown is the leakage path to the large center cavity.

SIMPLIFIED THEORETICAL PREDICTIONS

ASSUMING UNIFORM INLET AND EXIT CONDITIONS, AND NEGLECTING A FEW MINOR TERMS, WE CALCULATE

\[ F_n = \frac{1}{2\mu_1 \ell \Delta P} \left( K - \frac{\alpha^1}{\alpha} \right) \left( \frac{\ell}{\delta} \right) \]

\[ F_r = \frac{1}{2\mu_1 \ell \Delta P} \left( \frac{\ell h}{\delta} \right) \left( \frac{\ell}{\delta} \right) \left( \frac{\ell h}{\delta} \right) \left( \frac{\ell}{\delta} \right) \left( \frac{\ell h}{\delta} \right) \left( \frac{\ell}{\delta} \right) \]

WHERE \( K = \frac{\delta}{\mu_1 \delta} \) (SENSITIVITY OF CARRY-OVER TO GAP)

\( \alpha = \frac{\delta}{\delta} \) (SEAL DIVERGENCE, EQUAL TO 1 FOR US)

\( V_i \) = INLET TANGENTIAL VELOCITY

\( V^* \) = CAVITY TANGENTIAL VELOCITY

\( V_x \equiv \sqrt{\Delta P/P} \) = AXIAL FLOW SPEED IN GAP

\( \Omega \) = WHIRL SPEED

NOTE: \( C_n = -R \frac{\partial F_n}{\partial \Omega} \) THIS YIELDS CXX FROM STATIC DATA
Table 7.1 The first column shows the cross-stiffness correlation for all builds and the static data of Beckert [28]. The next two columns show the total force and frictional component evaluated at \( \Omega_d = 300 \text{ rpm} \) and design pressure ratio. The next column is the measured nondimensional direct damping coefficient. The final two columns give the damping calculated from the cross-stiffness coefficient and the average value that was directly measured.

| BUILD# | \( \frac{\beta_d}{\beta} \) | \( F_{x|y|z} \) | \( F_{y|x|z} \) | Correlation | From Static | Measured |
|--------|-----------------|-----------------|-----------------|--------------|-------------|-----------|
| 2      | 0.372           | 7763            | 953             | 0.289        | 22.70       | 19.95     |
| 3      | 0.416           | 77521           | 3162            | 0.371        | 82.19       | 75.80     |
| 4      | 0.283           | 20901           | 3162            | 0.347        | 56.13       | 48.54     |
| 5      | 0.338           | 7053            | 953             | 0.231        | 20.23       | 18.81     |
|        | Composite       |                 |                 | 0.357        |             |           |
| Data   | 0.357           |                 |                 | 0.423        |             |           |
| of     |                 |                 |                 | Benzker     |             |           |
|        | 0.269           |                 |                 |             |             |           |

Figure 4.3: Cross section of nested spindle Spin/Whirl producing rotating rig and test section assembly.

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Figure 4.8: Layout of the coret facility showing the drive systems for both the spin and whirl.

<table>
<thead>
<tr>
<th>VANE ANGLE</th>
<th>PRESSURE RATIO</th>
<th>SPIN SPEEDS ( \omega ) (Hz.)</th>
<th>WHIRL SPEEDS ( \Omega ) (Hz.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0°/plate</td>
<td>1.57, 1.38, 1.60</td>
<td>0.75, 0.72, 0.74</td>
<td>0.75, 0.72, 0.74</td>
</tr>
<tr>
<td>15°/plate</td>
<td>1.51, 1.39, 1.43</td>
<td>0.71, 0.69, 0.72</td>
<td>0.71, 0.69, 0.72</td>
</tr>
<tr>
<td>30°</td>
<td>1.51, 1.39, 1.44</td>
<td>0.71, 0.69, 0.72</td>
<td>0.71, 0.69, 0.72</td>
</tr>
<tr>
<td>60°</td>
<td>1.35, 1.40, 1.48</td>
<td>0.69, 0.67, 0.70</td>
<td>0.69, 0.67, 0.70</td>
</tr>
<tr>
<td>90°</td>
<td>1.35, 1.41, 1.50</td>
<td>0.69, 0.67, 0.70</td>
<td>0.69, 0.67, 0.70</td>
</tr>
<tr>
<td>120°</td>
<td>1.13, 1.21, 1.27</td>
<td>0.67, 0.65, 0.68</td>
<td>0.67, 0.65, 0.68</td>
</tr>
<tr>
<td>0°/plate</td>
<td>1.12, 1.22, 1.28</td>
<td>0.67, 0.65, 0.68</td>
<td>0.67, 0.65, 0.68</td>
</tr>
</tbody>
</table>

Table 5.5: Test Matrix for build #3.
<table>
<thead>
<tr>
<th>VARIABLE</th>
<th>ABSOLUTE UNCERTAINTY</th>
<th>RELATIVE UNCERTAINTY</th>
<th>COMMENTS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kolute Sensitivity, $S^a$</td>
<td>±7.1 Pa</td>
<td>±1.1 - ±2.3% of $p$</td>
<td>Linearity, hysteresis and calibration</td>
</tr>
<tr>
<td>Repeatability $p$</td>
<td>$2\sigma_p = 0.304$ N</td>
<td>$2\sigma_p = 0.144$ N</td>
<td>95% Confidence</td>
</tr>
<tr>
<td>$P_c = 0.2$</td>
<td>±0.144 N</td>
<td>±0.144 N</td>
<td>mass flow, alignment, repeatability, calibration</td>
</tr>
<tr>
<td>$V_c = 28.4 \pm 15^\circ$</td>
<td>7.2 %</td>
<td>7.2 %</td>
<td>Total accuracy</td>
</tr>
<tr>
<td>Build #3 design</td>
<td>$2\sigma = 0.144$ N</td>
<td>$2\sigma = 0.144$ N</td>
<td>95% Confidence</td>
</tr>
<tr>
<td>$p$, $P^<em>$, $P'^</em>$</td>
<td>±344 Pa Max</td>
<td>±0.1 % MAX</td>
<td>1275 RPM</td>
</tr>
<tr>
<td>Spin speed $\omega$</td>
<td>±2.1 RPM</td>
<td>±0.1 % MAX</td>
<td>620 RPM</td>
</tr>
<tr>
<td>Whirl speed $\Omega$</td>
<td>±4.5 RPM</td>
<td>±0.1 % MAX</td>
<td>820 RPM</td>
</tr>
<tr>
<td>Temperature $T$</td>
<td>1° F</td>
<td>0.3 %</td>
<td>To calculate density</td>
</tr>
<tr>
<td>$\rho$ and $\frac{\rho}{\omega}$</td>
<td>±0.3 mils</td>
<td>±0.3 mils</td>
<td>Most probable error due to non-circularity of orbit and casing.</td>
</tr>
<tr>
<td>$\rho_R$</td>
<td>±0.001 in. MAX</td>
<td>0.5 % MAX</td>
<td>Machining tolerances</td>
</tr>
<tr>
<td>$\rho_{ax}$</td>
<td>±0.008 in.</td>
<td>±67% - 50%</td>
<td>Uncontrolled axial clearance</td>
</tr>
</tbody>
</table>

Table 5.8: Table of uncertainties used in calculating the overall confidence interval for the force data.

**TYPICAL RESULTS FOR ZERO INLET SWIRL**

- **DATA SHOWN FOR CONF. #3 (SMOOTH, LONG SEAL)**
- **RESTORING DIRECT FORCE, INDEPENDENT OF SWIRL, SCALING WITH $\Delta p$**
- **STABILIZING CROSS FORCE, ZERO AT ZERO WHIRL RATE, PROPORTIONAL TO WHIRL**
- \[ \frac{F_c}{ \Delta p} \sim \frac{\Omega R}{ \sqrt{\Delta p}} \quad \text{, SO DATA CAN BE COLLAPSED TO ONE LINE} \]
Figure 7.13: Experimentally obtained direct force, $F_N$, vs. the whirl frequency, for five different inlet pressures, $v_0 = 1.27, 1.38, 1.47, 1.69$ and 1.79. These data are from build #3 with 0° inlet swirl and $\omega = 0$.

Figure 7.14: Experimentally obtained cross force, $F_T$, vs. the whirl frequency, for five different inlet pressures, $v_0 = 1.27, 1.38, 1.47, 1.69$ and 1.79. These data are from build #3 with 0° swirl and $\omega = 0$.
RESULTS WITH INLET SWIRL

- NONZERO CROSS FORCE AT ZERO WHIRL \((K_\nu = 0)\).
- EFFECT OF WHIRL SAME AS BEFORE.
- SINCE \(F_r \sim \Delta p\) AND BOTH, TANGENTIAL VELOCITY AND \(\Omega R\) SCALE AS \(\sqrt{\Delta p}\), PLOT OF \(\frac{F_r}{\Delta p}\) VS. \(\frac{\Omega}{\sqrt{\Delta p}}\) STILL COLLAPSES DATA.
- SLOPE \(\frac{\partial(F_r/\Delta p)}{\partial(\Omega/\Delta p)}\) IS THE SAME AS WITH ZERO INLET SWIRL.
SWIRL INCREASES \(K_{xy}\), DOES NOT AFFECT \(C_{xy}\).

Figure 7.17: Experimentally obtained direct force, \(F_n\), vs. the whirl frequency for five different pressure ratios. These data are from build #3 with 8.9° inlet swirl and \(\omega = 0\).

Figure 7.18: Experimentally obtained cross force, \(F_T\), vs. the whirl frequency, for five different pressure ratios. These data are from build #3 with 8.9° inlet swirl and \(\omega = 0\).

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SHAFT ROTATION - THE FRICTIONAL EFFECT

- ROTATION IN THE INLET SWIRL DIRECTION REDUCES CROSS-FORCE $K_{xy}$ (AND VICE-VERSA)
- REDUCTION IS THE SAME AT ALL WHIRL SPEEDS (NO CHANGE IN DAMPING $C_{xx}$)
- EFFECT DUE TO VARIATIONS OF THE TANGENTIAL VELOCITY CHANGE $V^* - V_j$ BETWEEN INLET AND GLAND
Figure 7.19: Experimentally obtained direct force, $F_N$, vs. the whirl frequency for five different spin rates, $\omega = 1.53$. These data are from build #3 with $8.6^\circ$ inlet swirl.

Figure 7.20: Experimentally obtained cross force, $F_T$, vs. the whirl frequency, for five different spin rates, $\omega = 1.47$. These data are from build #3 with $8.6^\circ$ inlet swirl.

Figure 7.21: Experimentally obtained direct force, $F_N$, vs. the whirl frequency for five different spin rates, $\omega = 1.55$. These data are from build #3 with $21.4^\circ$ inlet swirl.

Figure 7.22: Experimentally obtained cross force, $F_T$, vs. the whirl frequency, for five different spin rates, $\omega = 1.55$. These data are from build #3 with $21.4^\circ$ inlet swirl.
EFFECTS OF HONEYCOMB LAND

- SOME REDUCTION (~25%) OF CROSS FORCE, PROBABLY DUE TO CARRYOVER DISRUPTION. THEORY GIVES 17% REDUCTION WITH $k = 0$.

- MAJOR REDUCTION, EVEN REVERSAL, OF DIRECT FORCE (BECOMES NEGATIVE SPRING). SINCE $F_N$ DUE ALMOST ENTIRELY TO CARRYOVER DISRUPTION.

- DATA SHOWN FOR CONF. #4 (LONG, HONEYCOMB) FOR COMPARISON TO #3 (LONG, SMOOTH)

- EFFECTS FOR SHORT SEAL (#5 VS. #2) ARE WEAKER.

![Figure 7.23: Experimentally obtained direct force, $F_N$, vs. the whirl frequency for five different pressure ratios. These data are from build #4 with 0° inlet swirl and $ω = 0$.](image)

![Figure 7.24: Experimentally obtained cross force, $F_T$, vs. the whirl frequency, for five different pressure ratios. These data are from build #4 with 0° inlet swirl and $ω = 0$.](image)

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NON-DIMENSIONAL ROTORDYNAMIC COEFFICIENTS

- FORCES FITTED AS
  \[ \frac{F_x}{f} = -K_u - C_u \Omega + M_u \Omega^2 \]
  \[ \frac{F_r}{f} = K_u - C_u \Omega \]

- COEFFICIENTS MADE NONDIMENSIONAL BY
  \[ K'' = \frac{K_u \delta_i}{\ell R (P_i - P_f)} \]
  \[ C'' = \frac{C_u \delta_i}{\ell R \sqrt{P_i (P_i - P_f)}} \]

![Figure 7.29: The effect of pressure ratio on the nondimensional direct stiffness coefficient, \( K''_{xx} \), for builds #2 (narrow rotor-smooth land), #3 (wide rotor-smooth land), #4 (wide rotor-honeycomb land), and #5 (narrow rotor-honeycomb land). The inlet swirl for all cases is \( \Omega = 0^\circ \) and \( \eta_1 = 0.1407 \).](image)

![Figure 7.30: The effect of pressure ratio on the nondimensional cross stiffness coefficient, \( K''_{xc} \), for build #2, #3, #4, and #5. All were taken with the 15° swirl orifice plate and \( \eta_1 = 0.1407 \).](image)
EFFECTS OF UPSTREAM NONUNIFORMITIES

- PREVIOUS STUDIES HAVE ASSUMED UNIFORM $P_i, V_i$

  OUR RESULTS STRONGLY SUGGEST THIS IS NOT IN GENERAL A GOOD ASSUMPTION

- SINCE EFFECT NOT SUSPECTED, NO PRESSURE DATA WERE TAKEN UPSTREAM, AND NO SPECIAL CARE WAS TAKEN TO MEASURE OR MAINTAIN A CONSTANT AXIAL GAP IN UPSTREAM FACE SEAL (NOMINAL ~ 10 mil)

- LINEARIZED THEORY IGNORING UPSTREAM EFFECTS PREDICTS ALL TRENDS CORRECTLY, BUT YIELDS $K_{xy}, C_{xx}$ VALUES 2-3 TIMES TOO LOW

- THIS SAME DISCREPANCY HAD BEEN PREVIOUSLY NOTED BY SEVERAL RESEARCHERS WHEN TRYING TO CALCULATE $\delta P$ IN THE FIRST CAVITY OF MULTICAVITY SEALS
UPSTREAM NONUNIFORMITIES - CONTINUED

- MODEL WAS EXTENDED BY EXPLICITLY COUPLING THE INLET CAVITY CONDITIONS TO THOSE IN THE SEAL CAVITY, SOLVING FOR BOTH SIMULTANEOUSLY.

- RESULTS SHOW VERY LARGE INCREASES OF $K_{xy}$ AND $C_{xx}$ (FACTORS OF 3-5) IF INLET CAVITY DOES NOT LEAK INTO HUB AREA.

- ALLOWING FOR AN AXIAL GAP INTO A UNIFORM HUB VOLUME REDUCES THESE FACTORS, BUT FOR OUR NOMINAL 10 mil GAP, THE FACTORS ARE STILL 2-3.

- WE ALSO REDUCED FIRST-CAVITY DATA OF BENCKERT-WACHTER. DISCREPANCY BETWEEN DATA AND THEORY CAN BE REMOVED IF AN AXIAL GAP OF ~ 10 mil IS CONSISTENTLY ASSUMED.

NOTE: THE SAME THEORY PREDICTS PRESSURE IN CAVITIES OTHER THAN 1ST TO WITHIN $\pm$ 15%

---

![Graph](image-url)

Figure 3-41: Ratio of direct damping with upstream coupling to that with no coupling vs. swirl cavity to seal gland area ratio. The maximum occurs at 1.35 and the damping ratio comes to within 1% at a area ratio of 75.

![Graph](image-url)

Figure 3-42: Predicted direct and cross force at $\theta = 0$ from the fully coupled model vs. the relative axial clearance ratio, $\frac{h}{D}$. The geometry is the same as for build #3. $\psi = 1.4, \alpha = 15^\circ, \epsilon_1 = 0.1407$ and $\omega = 0$. 

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Table 7.2 Comparison of the data of Brockert and Wachtler (28) to the coupled model predictions. All cases are for standard conditions. \( p_i = 1.28 \) (bar), \( p_o = 1 \) (bar) and \( \alpha = 28.4^\circ \). The first column shows the experimental value. The second column gives the value predicted with full coupling, that is no leakage flow. The third column has the predictions for constant upstream boundary conditions. The last column gives the value of the axial space needed for the model to match the experimentally obtained value.

<table>
<thead>
<tr>
<th>CONFIG</th>
<th>( F_r(\text{meas.}) )</th>
<th>( F_r(\delta_\text{i} = 0) )</th>
<th>( F_r(\delta_\text{i} = \infty) )</th>
<th>Matched ( \delta_\text{i} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>10.28(N)</td>
<td>10.28(N)</td>
<td>4.99(N)</td>
<td>0.008&quot;</td>
</tr>
<tr>
<td>2</td>
<td>8.28(N)</td>
<td>10.15(N)</td>
<td>4.25(N)</td>
<td>0.011&quot;</td>
</tr>
<tr>
<td>3</td>
<td>11.91(N)</td>
<td>15.51(N)</td>
<td>4.09(N)</td>
<td>0.015&quot;</td>
</tr>
</tbody>
</table>

Figure 7.34: \( K_{xy}^\infty \) vs. \( \sigma \) for the experimental data and theory. The axial gap, \( \delta_\text{i} \), is used as a parameter. All experimental values fall between the theory with \( 0.004"(0.0001\text{m}) < \delta_\text{i} < 0.017"(0.0004\text{m}) \). The top thick line is for full coupling (i.e. no leakage). The bottom one is for uniform inlet conditions (i.e. no coupling). The calculations are for build #3 geometry.
DISCUSSION

- The sensitivity of cross-forces to upstream conditions will necessitate accounting for these in design work.
- This was relatively simple for our geometry (no blades), but will not be simple for realistic turbine shroud geometry.
- These nonuniformities are themselves due to the rotor eccentricity, so not a-priori known.
- More research is needed in this area.

CONCLUSIONS

LABYRINTH CROSS-FORCE MECHANISMS CLARIFIED

- Inviscid (kinematic) effects responsible for damping, damping insensitive to spin.
- Viscous mechanism affects cross-stiffness, not damping.
- Damping can be extracted from static data.
- Induced upstream non-uniformities can more than double cross forces. This needs to be accounted for.
- Direct forces mainly due to carryover variations
- Honeycomb land reduces direct forces strongly, cross-forces weakly.
A variable temperature model which considers squeeze film effects and thermal transients that was developed for two phase flows (1, 2) was extended to examine the axial stability of two-phase mechanical seals that tracks the axial response through position and velocity of the rotor from the perturbed state (3).

Step increases in film thickness usually engendered a response that decayed as the rotor asymptotically approached the initial steady state condition.

Step decreases in film thickness that are large enough brought about monotone opening (seal failure) and other forms of failure through film collapse or "popping open" due to the onset of instabilities.

In certain conditions the response to small step decreases leads to stable film thicknesses and rotor goes to steady state or some orbital state.

Small amounts of coning tend to stabilize the configuration, even for large disturbances. The magnitude of the thermal response parameter is important to response time and overshoot.

Model is limited through 1-D heat transfer and a conjugate solution would appear more appropriate and must incorporate the thermomechanical behavior of the seal rotor and stator interface, which includes seal "waviness." The distinct liquid-vapor boiling interface and laminar flow assumptions are also limitations, but the "smeared" two-phase interface with flow turbulence and transient behavior is quite complex but necessary for a better understanding of the dynamics.

For more information


High pressure compressor delivery brush seal of the international aero engines (IAE) V2500-A1 gas turbine engine

The V2500-A1 is the first production aero gas turbine to be certificated with brush seals. The engine has brush seals in three positions of which the HPC seal discussed in this short presentation has the most arduous duty.

Foil 1 shows the Rolls-Royce brush seal development "milestones" prior and subsequent to the entry into service of the V2500-A1 in 1989. Prior to the 1970's the potential of brush seals was known but limited by materials (early tests were conducted with Nylon bristles). Extensive R&D was conducted during the 1970's, continuing in parallel with demonstrator engine testing in the early 1980's. By the mid 1980's sufficient technology and confidence in brush seals had been acquired to commit to application and development in the civil V2500-A1 engine with certification and entry into service in the late 1980's.

Foil 2 shows the HPC brush seal in relation to the HPC delivery, the seal providing control of turbine zone ventilation and temperatures, lower sfc, and in conjunction with the labyrinth shown, a balance piston, for control of bearing thrust load.

Foil 3 and 4 show constructional details of the brush seal and its associated journal, with Foil 5 showing the nominal operating conditions which are quite arduous. Rolls-Royce experience shows that to obtain good seal life it is essential to finish the journals aluminium oxide coating by grinding and lapping to a surface finish of better than 0.5 micrometers CLA.

The V2500-A1 engine designed with this HPC delivery, and two other, brush seals was successfully developed and certificated, Foil 6. During development the seals were found to quickly run in to a stabilised condition and provided the journal coating surface finish was good the seal would run indefinitely. Whilst craze/axial cracking of the aluminium oxide coating was observed this has not so far proved to be a problem.

Foil and 8 show the service experience to date. No unscheduled removals of brush seals have occurred and the intention is not to remove seals for inspection until 5,000 engine cycles, (current high time engine is 3,600 cycles). A few engines have been stripped for other reasons and visual inspection of the seals on these engines have been shown the seals to be in good condition.

With the successful development and encouraging service experience of brush seals in the V2500-A1, Rolls-Royce will continue in the 1990's to exploit the advantages of brush seals through R&D, demonstrator engines and further engine applications.
R-R BRUSH SEAL DEVELOPMENT "MILESTONES"

PRE 1970's – POTENTIAL OF BRUSH SEALS KNOWN BUT LIMITED BY MATERIALS

1972 – R & D OF BRUSH SEALS
1980's – DEMONSTRATOR ENGINE TESTS
1985-1988 – DEVELOPMENT FOR A CIVIL ENGINE APPLICATION
1989 – SERVICE APPLICATION IN CIVIL ENGINE
1990's – CONTINUING R & D AND APPLICATIONS

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V2500-A1 HPC DELIVERY BRUSH SEAL
V2500-A1 HPC DELIVERY BRUSH SEAL DETAILS

1. THE JOURNAL

- JOURNAL DIAMETER - 315 mm
- JOURNAL COATING - PLASMA SPRAYED ALUMINIUM OXIDE
- FINISHED BY GRINDING AND LAPPING TO A SURFACE FINISH OF BETTER THAN 0.5 MICRO METERS CLA.

2. THE BRUSH SEAL

- NUMBER OF SEALS IN SERIES - 2
- BRISTLE FIT AT BUILD - RADIAL CLEARANCE
- BRISTLE LAY ANGLE - 45°
- BRISTLE LENGTH - 15 mm
- BRISTLE WIRE DIAMETER - 0.071 mm NOMINAL
- NUMBER OF BRISTLE ROWS PER SEAL - 11
- BRISTLE DENSITY - 2250 TO 2650 PER 25 mm
- BRISTLE WIRE MATERIAL - HAYNES 25
- BACKING RING CLEARANCE - 1.2 mm (RADIAL)
3. OPERATING CONDITIONS

- SURFACE VELOCITY - 250 m/s
- DIFFERENTIAL PRESSURE - 430 kPa
- TEMPERATURE - > 550 °C

V2500-A1 HPC DELIVERY BRUSH SEAL DETAILS

DEVELOPMENT/CERTIFICATION

- THE V2500-A1 ENGINE WAS SUCCESSFULLY DEVELOPED AND CERTIFICATED WITH BRUSH SEALS

- OBSERVATIONS FROM THE DEVELOPMENT PROGRAMME:
  - SEALS QUICKLY RUN IN TO A STABILISED CONFIGURATION AND THEREAFTER, IF THE ROTOR CONDITION IS GOOD, THE SEAL WILL RUN INDEFINITELY
  - CRAZE/AXIAL CRACKING OF THE ALUMINIUM OXIDE JOURNAL COATING AT THESE EXACTING TEMPERATURES AND SPEEDS IS NORMALLY SEEN
  - BRISTLES WAXED OPEN FOR ENGINE ASSEMBLY
V2500-A1 HPC DELIVERY BRUSH SEAL IN SERVICE

1. RUNNING EXPERIENCE (TO END MAY 1992)

- 77 A1's IN SERVICE
- TOTAL HOURS 354,300
- TOTAL CYCLES 212,100
- HIGH TIME HOURS 7200*
- HIGH TIME CYCLES 3600*

*NOT SAME ENGINE – DIFFERENT USEAGE

2. SEAL CONDITION

- FIRST SCHEDULED SERVICE REMOVALS WILL NOT TAKE PLACE BEFORE 5,000 CYCLES
- NO UNSCHEDULED REMOVALS OF BRUSH SEALS
- ON ENGINES STRIPPED FOR OTHER REASONS THE CONDITION OF THE BRUSH SEALS HAS BEEN GOOD

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BACKGROUND

TEXTRON SPECIALTY MATERIALS DEVELOPS AND PRODUCES ADVANCED FILAMENTS AS REINFORCEMENTS FOR CERAMIC AND METALLIC MATRICES

- BORON MONOFILAMENT - CVD
- SILICON CARBIDE MONOFILAMENT - CVD
- CARBON FIBER TOWS
- TiB₂, TiBC, BN, Si₃N₄, FIBERS + COATINGS
STRENGTH COMPARISONS OF ADVANCED MATERIALS

- GRAPHITE/POLYMIDE
- ALUMINUM METAL MATRIX
- TITANIUM METAL MATRIX
- FIBER CERAMIC MATRIX COMPOSITE
- CARBON-CARBON
- VARIOUS CARBIDES, NITRIDES
- SUPER ALLOYS
- STEEL
- REFRACTORY METALS

* COATING STATE-OF-THE-ART TEMPERATURE LIMIT

TEXTRON Specialty Materials

TURBINE ENGINE APPLICATIONS FOR FIBER REINFORCED METALS

- FAN BLADE AND DISKS
- COMPRESSOR BLADES AND DISKS
- EXHAUST CASING
- VARIABLE GEOMETRY NOZZLES
- STATORS
- POWER SHAFT
- CASE AND CORE SUPPORT STRUCTURE

TEXTRON Specialty Materials
SILICON CARBIDE ON CARBON FILAMENT

- 500 Ksl, 58 Msi (STRENGTH & STIFFNESS)
- DENSITY, 0.110 LD/IN³
- HIGH TEMP STABILITY > 1800° F USE TEMP
- CARBON CORE FOR HIGH STRENGTH/LOW COST
- COMPATIBILITY WITH METALS

SILANES - LOW COST
FASTER DEPOSITION RATES
PROVEN REACTOR TECHNOLOGY

TEXTRON Specialty Materials
**CVD CONTINUOUS SILICON CARBIDE MONOFILAMENT**

<table>
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<th>FIBER DIAMETER</th>
<th>MODULUS</th>
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<tbody>
<tr>
<td>2 MIL</td>
<td>45 - 47 Msi</td>
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<tr>
<td>2.5 MIL</td>
<td>53 Msi</td>
</tr>
<tr>
<td>5.6 MIL</td>
<td>59 - 60 Msi</td>
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**SCS-6 Tensile Strength at Temperature**

![Tensile Strength Graph]

- **Tenile Strength at Temperature (Kpsi)**
- **Temperature °C**

*TEXTRON Specialty Materials*
Figure 15. Plot Young's modulus (GPa) of fiber made at 2912°F (1600°C) from DDS and hydrogen, versus temperature (°C) compared with literature data (ref. 24, 25). Good agreement is evident. Gulden work was on CVD material.
Comparison of creep rates at various loads for CVD and single crystal materials.
From G. Coman AF Report August 1990

\[ \text{Figure 7} \]

<table>
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<th>Temperature (°C)</th>
<th>Creep Rate (sec^-1)</th>
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<tbody>
<tr>
<td>1450</td>
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</tr>
<tr>
<td>1800</td>
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sc = single crystal  
a = alpha  
b = beta

FIBER SUMMARY

- FIBERS IN PRODUCTION (SCS-2™, 6, 8 AND 9)
- SCS-6™ - STANDARD FIBER FOR TITANIUM & CERAMICS
- SCS-9™ - DEVELOPMENT OF 3 mil DIAMETER FIBER
  - MADE ≤ 100 LBS
- PLANNED PRODUCTION FOR 1992 ≤ 500 LBS. (SCS-6™, 8 & 9)
- PLANT CAPACITY ≤ 1500 LBS/YEAR (BUILDING CAPACITY ≤ 20-30K LB/YEAR)

TEXTRON Specialty Materials
A two-day meeting was conducted at the NASA Lewis Research Center on August 5 and 6, 1992, to inform the technical community of the progress of NASA Contract NAS3-25644. This contract was established in 1990 to develop industrial and CFD codes for the design and analysis of seals. Codes were demonstrated and disseminated to the user community for evaluation. The peer review panel which was formed in 1991 provided recommendations on this effort. The technical community presented results of their activities in the area of seals, with particular emphasis on brush seal systems.