Ethylene Trace-Gas Techniques for High-Speed Flows

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Prepared for the
32nd Aerospace Sciences Meeting and Exhibit
sponsored by the American Institute of Aeronautics and Astronautics
Reno, Nevada, January 10–13, 1994
Ethylene Trace-Gas Techniques for High-Speed Flows

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Abstract

Three applications of the ethylene trace-gas technique to high-speed flows are described: flow-field tracking, air-to-air mixing, and bleed mass-flow measurement. The technique involves injecting a non-reacting gas (ethylene) into the flow field and measuring the concentration distribution in a downstream plane. From the distributions, information about flow development, mixing and mass-flow rates can be determined. The trace-gas apparatus and special considerations for use in high-speed flow are discussed. A description of each application, including uncertainty estimates is followed by a demonstrative example.

Nomenclature

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Quantity</th>
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<tr>
<td>( A )</td>
<td>area</td>
</tr>
<tr>
<td>( D )</td>
<td>diameter</td>
</tr>
<tr>
<td>( f )</td>
<td>friction factor</td>
</tr>
<tr>
<td>( L )</td>
<td>length</td>
</tr>
<tr>
<td>( \dot{m} )</td>
<td>mass-flow rate</td>
</tr>
<tr>
<td>( m_f )</td>
<td>mass fraction</td>
</tr>
<tr>
<td>( M )</td>
<td>Mach number or molecular weight</td>
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<tr>
<td>( N )</td>
<td>number of moles</td>
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<tr>
<td>( \text{ppm} )</td>
<td>parts per million</td>
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<td>( P )</td>
<td>static pressure</td>
</tr>
<tr>
<td>( P_t )</td>
<td>total pressure</td>
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<td>( Re_D )</td>
<td>Reynolds number based on diameter</td>
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<td>( \text{sl/m} )</td>
<td>standard litres per minute</td>
</tr>
<tr>
<td>( \text{sml/m} )</td>
<td>standard millilitres per minute</td>
</tr>
<tr>
<td>( W )</td>
<td>uncertainty of a variable</td>
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<tr>
<td>( \bar{W} )</td>
<td>fractional non-dimensional uncertainty</td>
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<tr>
<td>( v )</td>
<td>volume (mole) fraction</td>
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<tr>
<td>( x, y, z )</td>
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<td>( \bar{x}, \bar{y}, \bar{z} )</td>
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<td>( \alpha )</td>
<td>shock generator deflection angle</td>
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<tr>
<td>( \gamma )</td>
<td>ratio of specific heats</td>
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<tr>
<td>( \rho )</td>
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<td>( \sigma^2_{y}, \sigma^2_{z} )</td>
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<td>( \sigma_{yz} )</td>
<td>covariance</td>
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Subscripts

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<td>( \text{eth} )</td>
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Introduction

In recent years, ethylene trace-gas techniques have been successfully applied to the analysis of fluid flow problems—where the host fluid medium is air—at the NASA Lewis Research Center. The ethylene trace-gas technique is a valuable tool for several reasons: it is relatively inexpensive, it is easy to use, and it is a source of Lagrangian flow-field data. Although others have used ethylene trace-gas techniques before, they have been restricted to applications where the primary velocity component was very low—in all cases the Mach number was less than 0.1. Much of the development of the ethylene trace-gas technique at NASA Lewis has concentrated on extending the applicability to higher speed flows. Some of this development work was reported by Reichert et al.\cite{1,2} where the technique was successfully applied to the analysis of high subsonic air flow through an aircraft transition duct. More recently, the technique has been extended to include the analysis of supersonic flow-fields. At present, the technique has been successfully applied in flows up to Mach 4.

In general, the trace-gas technique involves injecting and tracking a nonreacting discernible foreign gas in the host flow field being investigated. Information about the host flow field is acquired by measuring the concentration of the trace-gas at many locations downstream of the point of injection. In studies where the fluid medium is air, ethylene (\( \text{C}_2\text{H}_4 \)) is a particularly attractive trace-gas for the following reasons:

1. The molecular weight of ethylene, 28.05, is nearly the same as air, 28.97, thus minimizing the effect of buoyancy forces on the motion of the trace-gas.
2. Under normal circumstances, ethylene and other hydrocarbon gases are only found in very minute quantities in air.
3. The mean concentration of ethylene, or any hydrocarbon gas, can be measured very accurately with a flame ionization detector.

In this paper, three applications of the ethylene trace-gas technique are described: (1) flow-field tracking, (2) air-to-air mixing, and (3) bleed mass-flow measurement. Schematics of the ethylene trace-gas system for the three applications are shown in Fig. 1.
Fig. 1 Ethylene trace-gas system schematic.
The components of the ethylene trace-gas system can be classified by ethylene supply and injection, gas sampling and pressure regulation, and concentration measurement (see Fig. 1). The major components of the trace gas apparatus are listed in Table 1 and are identified by the circled numbers in Fig. 1. The costs listed in Table 1 are for reference and represent what NASA paid for the components. All components were purchased within the last five years.

The ethylene trace-gas technique relies on the detection of a hydrocarbon gas. It is very important that all components be of the oil-less/grease-less type and not contain any materials that can out-gas hydrocarbons. Prior to assembly, all connecting lines should be flushed with acetone and then blown dry with zero-gas air (air containing less than 0.5 ppm total hydrocarbons). After assembly, all connections should be leak checked.

For accurate measurements, the wind tunnel should also be as hydrocarbon-free as possible. Sources of hydrocarbons in the wind tunnel include oil from compressors, residual oil from flow visualization and residual cleaning solvents. Contamination of the air will show up as a background noise level. The air supplied to the NASA Lewis wind tunnels typically has a background level of 2–3 ppm equivalent ethylene. Residual hydrocarbons on the tunnel surfaces will cause artificially high readings when the sample probe is on the wall.

IMPORTANT SAFETY TIP: The ethylene trace-gas technique involves two potentially hazardous gases: ethylene and hydrogen. For reference, the limits of inflammability in terms of percent volume in air for these gases are given in Table 2. Failure to observe appropriate safety precautions would be bad.

<table>
<thead>
<tr>
<th>Item No. (see Fig. 1)</th>
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<th>Manufacturer/Model No.</th>
<th>Approx. Cost ($)</th>
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<td>2</td>
<td>Auto Flow Control &amp; Display</td>
<td>Edwards/Model 1511 (optional)</td>
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<td>2</td>
<td>Sample Pump</td>
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</tr>
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<td>3</td>
<td>Back-Pressure Regulator</td>
<td>Verilto Corporation/BPR 30</td>
<td>200</td>
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<tr>
<td>4</td>
<td>FID</td>
<td>Gow-Mac Instrument Co./Model 23-500</td>
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</tbody>
</table>

**Table 1 Ethylene Trace-Gas System Equipment**

**Ethylene Trace-Gas Apparatus**

The instrument used to measure ethylene concentration is a flame ionization detector (FID). The FID consists of a small burner within which a fuel and oxidizer are mixed and burned. Hydrogen and zero-gas air, are used as fuel and oxidizer, respectively, so there are no hydrocarbons present in this flame. When the sample is mixed with the flame, hydrocarbons are burned and the carbon atoms become ionized. The carbon ions and electrons pass between two electrodes, decreasing the resistance between the electrodes and thus permitting an electric current to pass. This current is directly proportional to the amount of carbon ions present. The FID responds to both the amount of carbon atoms present in the sample, and the rate at which the sample passes through the detector. This makes it very important to maintain a constant flow rate of sample through the FID. For the FID unit used in the present system (Item 4 in Table 1) the maximum sensitivity occurs when the sample flow rate is maintained at 30 sml/m. This flow rate is set by adjusting the sample pressure P4 which is controlled by a 0–5 psig back-pressure regulator built into the FID unit.

The primary disadvantage to using an FID to measure concentration is the relatively long response times to changes in conditions. Data supplied with the FID unit shows that at the optimum sample flow rate of 30 sml/m, a step input to the unit of 5.3 ppm of methane (CH₄) requires approximately 10 seconds to reach 99.9% of the input concentration. This then represents the lower limit of response time when conditions change. However, what really controls system response is the time required to completely purge the system of an old sample when sample concentration changes. This will be addressed in a later section.

Calibration of the FID is accomplished by passing a sample of zero-gas air through the unit to establish a zero and then passing a reference ethylene-in-air mixture to set the span. The uncertainty in the concentration of the reference gases is less than 0.5 ppm. The manufacturer of the FID unit quotes an accuracy of ±1.0% of full scale with full scale being 1000 ppm—an absolute uncertainty of ±10 ppm. Since the uncertainty in the calibration mixtures is an order of magnitude lower than the accuracy
of the FID, we can assume that they contribute negligibly to the overall uncertainty.

**Ethylene Supply and Injection**

The ethylene supply system consists of a high-pressure ethylene bottle, a pressure regulator, a pressure relief valve and a mass-flow controller. The pressure regulator reduces the pressure from the high-pressure bottle to a range acceptable to the mass-flow controller. The pressure relief valve protects the mass-flow controller from over-pressure in the event of a regulator failure and should be vented outside to avoid producing a combustible mixture in the test area. The range of the mass-flow controller is primarily dependent on the mass-flow rate of the host flow, but also depends on the objective of the experiment. The mass-flow controller used in the present system (Item 1 in Table 1) features the ability to vary its full scale range anywhere between 5 sml/m and 5 sl/m by simple hardware changes.

Introduction of the ethylene into the host flow may be accomplished by injection probes or through surface taps depending on the objectives of the experiment. The most common injection probe is an L-shaped probe, like a downstream facing Pitot probe. Previous studies that have employed the ethylene trace-gas technique have included the results of experiments designed to measure and minimize disturbances from L-shaped type injection probes. For low speed applications, the L-shaped probe is simply cantilevered into the flow-field. For high-speed subsonic flow, deflection of the probe may become excessive and a catenary design must be used. At supersonic speeds, injection probes may produce unacceptable flow interference so that flush surface taps may be necessary for injection. We should note, however, that injection of the ethylene into a region of spanwise vorticity (the boundary-layer) will always produce some axial vorticity and enhanced mixing. Although this effect can be minimized by using low injection rates through small holes, it should be considered when interpreting results.

**Sampling**

To measure the ethylene concentration downstream of its point of injection, fluid is extracted from the flow-field. This is usually accomplished with a probe much like a Pitot tube, along with the required pumps. One impediment to applying the ethylene trace-gas technique to higher speed flows has been the perceived need for isokinetic sampling of the flow field (i.e., sampling at a velocity through the probe opening that matches the local host flow velocity). Isokinetic sampling is actually not necessary to accurately measure the local concentration of trace-gas in a host gas flow. Injecting trace-gas into the flow field creates an Eulerian concentration field. The local value of the concentration in the flow field does not depend on the rate at which the sample is acquired. However, if the sample velocity through the probe opening greatly exceeds the local host flow velocity the spatial resolution ability of the probe would deteriorate. This is generally not a concern in high-speed flows.

Of much greater concern for high-speed flow applications is delivering the sample to the FID unit at a constant flow rate in a minimum amount of time. Parameters that affect response time are the total volume of the system and the mass-flow rate through the regulation system. To minimize response time, the system volume should be minimized and the mass-flow rate should be maximized. We should point out here that the flow rate through the sample regulation system can and should be greater than the optimum flow rate through the FID unit. Pressure in the system is controlled by a back-pressure regulator (Item 3 in Fig. 1) which controls the sample pressure P3 by venting excess sample. This allows a much more rapid purging of the system than if conventional pressure regulators are used.

System volume can be most effectively minimized by keeping the total distance that the sample must travel to reach the FID unit as short as possible. In particular, the line between the back-pressure regulator and the FID should be kept as short as possible since it is downstream of the “purging” vent of the back-pressure regulator. Minimizing the diameter of the connecting lines between components, will also reduce volume. However, if the diameter becomes too small, the benefits of reduced volume will be negated by increased frictional losses.

The mass-flow rate through the system upstream of the back-pressure regulator is a function of the probe diameter and length, the pump capacity, and the impact pressure at the probe face. The probe diameter should be selected to be the largest diameter able to adequately resolve the largest concentration gradients in the flow-field. To maximize the flow rate, a pump should be selected that is able to choke the flow through the sampling probe at all locations in the flow-field. In the NASA Lewis 1×1 ft. Supersonic Wind Tunnel (SWT) tests, a 0.686 mm (0.027 in) I.D. tube was used as a sample probe. The length from the tip to the sample pump was one meter. If we assume that the flow through the probe may be approximated by Fanno line flow, then the variation of Mach number along the probe is given by the following ordinary differential equation:

$$\frac{dM^2}{M^2} = \frac{\gamma M^2(1 + \frac{2}{\gamma-1} M^2)}{1 - M^2} 4f \frac{dx}{D} \quad (1)$$

where $f$ is the friction factor given by:

$$f = \frac{16}{Re_D} \quad (2)$$

if the flow is laminar through the tube. Equation 1 was solved for a range of sample probe inlet total pressures with the condition that the flow be choked at the exit (for maximum mass-flow). Fig. 2 shows the mass-flow
rate and exit pressure as a function of inlet total pressure. With the NASA Lewis 1 x 1 ft. SWT operating at Mach 4 and a core total pressure of 275 kPa (40 psia), the impact pressure at the face of the sampling probe as it rests on the wall is approximately 5 kPa and represents the worst case in terms of pumping requirements. The data of Fig. 2 is replotted as choked mass-flow versus exit pressure in Fig. 3 and compared to the pump manufacturers performance. This plot shows that for all sample probe exit pressures, the pump is capable of delivering the mass-flow required for choked flow, and as a result, the sampling time is kept to a minimum.

**Flow-Field Tracking**

In the flow-field tracking application, the technique is used to deduce information about the flow-field from the trace-gas distribution. Interpretation of the measured trace-gas distributions can range from simple to downright ambiguous. In the simplest case, the technique is used more like a flow visualization technique and the result is simply to find where the fluid that passes through the injection point ends up in the measurement plane. We call this streamline tracking and under most conditions the location of the peak concentration is approximately the location of the streamline that passes through the injection point. From here we can infer information about the turbulence structure and secondary flow by examining the spreading and distortion of the trace-gas distribution. Here is where the ambiguity arises because from the distribution alone it is sometimes difficult to determine the relative importance of convection and diffusion in the mixing of the trace-gas with the host flow. That is, similar distributions may be achieved by different processes, and therefore, additional information acquired by other measurement techniques may be required.

The trace-gas distribution can be quantified by computing the statistical moments of the distribution:

\[ \bar{y} = E[y], \quad \bar{z} = E[z] \quad \text{(mean)} \]  \[ \sigma_y^2 = E[(y - \bar{y})^2] \]  \[ \sigma_z^2 = E[(z - \bar{z})^2] \quad \text{(variances)} \]

\[ \sigma_{yz} = E[(y - \bar{y})(z - \bar{z})] \quad \text{(covariance)} \]

where \( E[\phi] \) denotes the expected value of a variable \( \phi \) and is defined as:

\[ E[\phi] = \frac{\int \phi v dA}{\int v dA} \]  \[ (6) \]

Equation 3 represents the coordinates of the centroid of the distribution and under most conditions will nearly coincide with the coordinates of the peak concentration. The variances, equation 4, are a measure of the spreading of the trace-gas in the \( y \) and \( z \) directions. The covariance, equation 5, represents the orientation of the distribution. For a more complete discussion of the interpretation of the trace-gas distributions, see Reichert \textit{et al.}\textsuperscript{9,10}

With regard to injection, Reichert \textit{et al.} have demonstrated that the rate of injection into the flow-field is largely unimportant. In other words, distributions measured with different injection rates, when normalized by the measured peak concentration, are the same.

To illustrate a high-speed flow-field tracking application, results from a crossing oblique shock-wave and boundary-layer interaction are presented.\textsuperscript{15} A schematic of the experiment with reference coordinates is shown.
in Fig. 4. Supersonic flow \(M=3.44\) passes between two sharp-edged plates at equal, but opposite, angles of attack to the flow. The resulting oblique shock-waves cross on the centerline and interact with the boundary layer \(\delta_0 = 3\) cm developing on the \(y=0\) surface. Ethylene is injected through a surface static pressure tap at the location indicated by the "x" and the concentration is measured in the indicated plane near the plate trailing edges. Volume fraction contours in the measurement plane are shown in Fig. 5 for various plate deflection angles. The volume fraction contour levels and the maximum volume fraction level indicated in the plot have been normalized by the peak concentration observed in the undisturbed boundary layer of the tunnel traveling the same axial distance (21.4 cm). For deflection angles of \(2^\circ\) and \(6^\circ\), the location of the peak concentration remains on the surface, but is laterally displaced from the point of injection due to flow turning produced by the plates. Compared to the \(a = 2^\circ\), the \(a = 6^\circ\) case shows a greater degree of spreading which is due to larger turbulence intensities resulting from a deceleration of the local boundary layer flow by the adverse pressure gradient generated by the oblique shock-waves. In the vicinity of \(y/\delta_0 = 0.2\) and \(z/\delta_0 = 1.2\) for the \(a = 6^\circ\) case, the contours are distorted by a vortex that is known to be generated in a supersonic compression corner.\(^\text{16}\) For a deflection angle of \(9^\circ\), the flow separates and the resulting large scale turbulent mixing greatly dif- fuscs the ethylene trace. Under these conditions (flow separation), the location of the peak concentration can not be assumed to coincide with the streamline passing through the injection location. And speaking of separation, a variation of the flow-field tracking technique is the detection of reverse flow by injecting through a tap in the wall and sampling upstream. Flow reversal has occurred when the sample contains ethylene.

**Air-to-Air Mixing**

For air-to-air mixing applications, the injected air stream (see Fig. 1) is seeded with ethylene to a known concentration. The unseeded (stream 1) and seeded (stream 2) streams are allowed to mix and the ethylene concentration in the mixing region is measured. When properly calibrated, the analyzer displays the volume (mole) fraction of ethylene, which for the present case is nearly equivalent to the mass fraction. Concentration levels measured in the mixing region, when normalized by the volume fraction of the seeded stream, gives the volume fraction of the seeded stream in the measurement plane:

\[
V_2 = \frac{N_2}{N_{\text{total}}} = \frac{(N_{\text{eth}}/N_2)}{(N_{\text{eth}}/N_1)} = \frac{V_{\text{eth}}}{V_{\text{eth},\text{ref}}}
\]

where \(N\) is the number of moles.

Like the flow-field tracking application, the rate of injection of the ethylene is unimportant. It is very im- portant, however, to know the concentration of ethylene in the injected stream before it is injected. To monitor the injected stream concentration, a reference sample line is teed into the regular sample line with a solenoid (see Fig. 1) which is occasionally energized to ensure that the reference concentration is not drifting.

Interpretation of the results for this application is very straight-forward. The resulting distribution computed from equation 7 represents the mean mixing of the
two-streams and is very useful as a validation of CFD mixing models. A word of caution, however, is in order. The response time to analyze a sample is too long to represent anything other than a long time average of the concentration. That is, from the results there is no way of knowing if the two streams are mixed at the molecular level or if large eddies alternating between the two streams are passing the sample probe. This can be very important if the two streams represent reacting gases.

The fractional non-dimensional uncertainty associated with equation 7 is given by:

\[
\overline{W}^2_{v_2} = \left( \frac{W_{v_2}}{v_2} \right)^2 = \left( \frac{\partial \ln v_2}{\partial \ln v_{\text{eth}}} \cdot \frac{W_{v_{\text{eth}}}}{v_{\text{eth}}} \right)^2 + \left( \frac{\partial \ln v_2}{\partial \ln v_{\text{eth},\text{ref}}} \cdot \frac{W_{v_{\text{eth},\text{ref}}}}{v_{\text{eth},\text{ref}}} \right)^2
\]

where \( W \) is the absolute uncertainty of a variable. Substituting the expressions for the partial derivatives yields:

\[
\overline{W}^2_{v_2} = \sqrt{\left( 1.0 \cdot \frac{W_{v_{\text{eth}}}}{v_{\text{eth}}} \right)^2 + \left( -1.0 \cdot \frac{W_{v_{\text{eth},\text{ref}}}}{v_{\text{eth},\text{ref}}} \right)^2}
\]

The manufacturer of the FID unit quotes an accuracy of 1.0% of full scale. With the FID unit set for a full scale range of 1000 ppm and the reference concentration of stream 2 set at 1000 ppm (the FID has a 100% overrange) equation 9 reduces to:

\[
\overline{W}^2_{v_2} = \sqrt{\left( \frac{W_{v_{\text{eth}}}}{v_{\text{eth}}} \right)^2 + 10^{-4}}
\]

This equation is plotted in Fig. 6 and shows the fractional uncertainty in the calculated volume fraction of Stream 2 as a function of the fractional uncertainty in the measured volume fraction of ethylene. The dashed portion of the curve is unattainable since you can never measure an ethylene concentration greater than the concentration in the injected stream.

As an example of an air-to-air mixing application, the results of a wall-mounted hypermixing nozzle test are shown in Fig. 7. In this example, supersonic flow (\( M=2.96, \delta_0 = 2.7 \) cm) passes over a contoured injector nozzle designed to enhance mixing through the generation of streamwise vorticity. The supply line to the injector nozzle was seeded with ethylene at a location approximately 60 supply line pipe diameters (pipe I.D.=5.08 cm) upstream from the injector plenum to ensure thor-
ough mixing. The ethylene concentration is measured in planes downstream of the nozzles and, when normalized by the reference injected concentration, yields the volume fraction of injected fluid. Volume fraction results for the hypermixing model have been used by Lee\(^{19}\) to validate the RPLUS computer code and by Davis\(^{20}\) to validate the SPARK-PNS computer code.

**Mass-Flow Measurement**

The ethylene trace-gas technique can be used as an alternative way of measuring bleed mass-flow rate when conditions are such that mass-flow measurement by other means is deemed unreliable. This situation may occur when the pressure and Reynolds number are very low and calibrated orifices lose accuracy. To apply the ethylene trace-gas technique to this problem, the bleed flow is seeded with ethylene at a known mass-flow rate. The bleed flow is then sampled at a downstream location where the ethylene is thoroughly mixed with the bleed stream. In a mixture of ethylene and air, the mass fraction of ethylene is defined in terms of the volume fractions as:

\[
m_{\text{eth}} = \frac{M_{\text{eth}}v_{\text{eth}}}{M_{\text{eth}}v_{\text{eth}} + M_{\text{air}}v_{\text{air}}} = \frac{M_{\text{eth}}v_{\text{eth}} + M_{\text{air}}(1 - v_{\text{eth}})}{M_{\text{eth}}v_{\text{eth}} + M_{\text{air}}(1 - v_{\text{eth}})}
\]

(11)

where \(M\) is the molecular weight of the gas. The mass fraction of ethylene can also be expressed in terms of the mass-flow rate of ethylene and air as:

\[
m_{\text{eth}} = \frac{\dot{m}_{\text{eth}}}{\dot{m}_{\text{eth}} + \dot{m}_{\text{air}}}
\]

(12)

Equating equations 11 and 12 and rearranging yields the following expression for the mass-flow of air:

\[
\dot{m}_{\text{air}} = \frac{M_{\text{air}}}{M_{\text{eth}}} \left( \frac{1 - v_{\text{eth}}}{v_{\text{eth}}} \right) \dot{m}_{\text{eth}}
\]

(13)

For accurate measurements, the bleed mass-flow must be steady and the ethylene must be thoroughly mixed. Steady flow can be ensured if a choke point is located somewhere in the bleed line—either the bleed plates themselves or through a valve if the plates are to be operated unchoked. One of the advantages of this technique is that the results are independent of the quality of the flow in the bleed line, i.e. the flow need not be uniform or assumed to have a particular velocity profile.

The propagation of uncertainty in measuring mass-flow via equation 13 can be expressed in fractional non-dimensional form as:

\[
\frac{W_{\dot{m}_{\text{air}}}}{\dot{m}_{\text{air}}} = \sqrt{\left( \frac{1}{1 - v_{\text{eth}}} \cdot \frac{W_{\dot{m}_{\text{eth}}}}{v_{\text{eth}}} \right)^2 + \left( \frac{W_{\dot{m}_{\text{eth}}}}{\dot{m}_{\text{eth}}} \right)^2}
\]

(14)

Since the (thoroughly mixed) volume fraction of ethylene is typically very small \((v_{\text{eth}} \ll 1)\), equation 14 simplifies to:

\[
W_{\dot{m}_{\text{air}}} = \sqrt{(W_{v_{\text{eth}}})^2 + (W_{\dot{m}_{\text{eth}}})^2}
\]

(15)

Equation 15 is plotted in Fig. 8 and shows the fractional uncertainty in the calculated mass-flow rate of air as a function of the fractional uncertainty of the measured ethylene flow rate and volume fraction assuming that the calibration gas uncertainty is negligible.

To verify the validity of equation 13, a small scale simulation of a bleed line was tested. Shown schematically in Fig. 9, a 4.5 meter length of 1.2 cm I.D. vacuum tube was used to simulate the bleed line. A valve was placed on the upstream end of the tube and the downstream end was connected to a vacuum pump. A reference mass-flow meter was placed in the middle of the tube. Ethylene was injected just downstream from the valve and a sample was taken from just upstream of the pump. Also placed in the line just downstream of the valve was a 15 cm mixing element. The air mass-flow rate was varied between 20 and 60 slm and at each set point of air mass-flow, the ethylene mass-flow was adjusted until a reading of 500 ppm was obtained in the sample. Fig. 10 shows a plot of air mass-flow versus ethylene mass-flow. The data are shown reduced with two different calibration gases. One calibration gas was 505 ppm of ethylene \((C_2H_4)\) and the other was 476 ppm of propane \((C_3H_8)\). The analyzer can be calibrated to

Fig. 8 Fractional uncertainty of the calculated air mass-flow rate.

Fig. 9 Schematic of the bleed mass-flow rate experiment.
propane if the reading is scaled by 1.5—the ratio of carbon atoms in the molecules—so that 476 ppm propane is equivalent to 714 ppm ethylene. The different distributions resulting from the different calibration gases imply that either one of the calibration gases is not within specification or the FID unit has a non-linear response. A second FID unit was tested with virtually the same results. Nevertheless, the results are encouraging and with more refinement the technique should be a practical alternative to measuring mass-flow when other methods fail.

Concluding Remarks

Several applications of the ethylene trace-gas technique for diagnostic studies in high-speed flows have been presented. The primary advantage of the ethylene trace-gas technique is its simplicity and relatively low cost. Set-up time and post-test processing of the data is minimal. The primary limitation to the technique is the relatively long response times to changes in concentration, thus making the technique applicable only in steady flows. There are, however, two ways to increase the productivity of testing time. First, the use of a sampling probe rake with multiple trace-gas systems is a viable method to reduce testing time. The data for the air-to-air mixing example shown in Fig. 7 was accumulated using two trace-gas systems. In larger facilities, the cost of an additional system is easily offset by the reduction in the cost of wind-tunnel running time. The second method to increase productivity is to integrate the measurements with pressure type measurements. Pitot pressure can be recorded with the sampling probe if a solenoid is placed in the line to switch to a pressure transducer (actually, two solenoids are required since dead-heading the sample pump can extinguish the hydrogen flame in the FID). Another variation is to sample from the center tube of a three-hole cobra probe or a five or seven hole flow angle probe.

Acknowledgment

The authors would like to gratefully acknowledge Dr. W. R. Hingst, Dr. W. Faulkner, J. Bodner and B. Ramsey for their helpful contribution. We would also like to acknowledge D. Stark, A. Kane and G. Hurd for assembling the trace-gas system.

References


# Ethylene Trace-Gas Techniques for High-Speed Flows

**Abstract**

Three applications of the ethylene trace-gas technique to high-speed flows are described: flow-field tracking, air-to-air mixing, and bleed mass-flow measurement. The technique involves injecting a non-reacting gas (ethylene) into the flow field and measuring the concentration distribution in a downstream plane. From the distributions, information about flow development, mixing, and mass-flow rates can be determined. The trace-gas apparatus and special considerations for use in high-speed flow are discussed. A description of each application, including uncertainty estimates, is followed by a demonstrative example.