MEASUREMENT AND INTERPRETATION OF CRUSTAL DEFORMATION RATES ASSOCIATED WITH POSTGLACIAL REBOUND

GRANT NAG5-1930

Semi-annual Status Report No. 3

For the Period 15 March 1993 through 14 September 1993

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December 1993

Prepared for

- National Aeronautics and Space Administration
  - Washington, D.C. 20546
- Smithsonian Institution
  - Astrophysical Observatory
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The Smithsonian Astrophysical Observatory is a member of the Harvard-Smithsonian Center for Astrophysics

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I. Introduction

This project involves obtaining GPS measurements in Scandinavia, and using the measurements to estimate the viscosity profile of the Earth's mantle and to correct tide-gauge measurements for the rebound effect. Below, we report on several aspects of this project.

II. GPS Measurements

The DSGS was occupied in August 1993. This campaign also inaugurated SWF.POS, the Swedish permanent GPS network. Initial results are presented in Johansson et al. [1993], a copy of which is contained in Appendix A.

III. Theoretical Advances

An important technical advance we intend for this project is to use the full three-dimensional site velocity information for inferring geophysical parameters. To this end, we have investigated using VLBI determined baseline length rates in North America to constraining proposed combinations of ice history and earth rheology, and presented this work in Mitrovica et al. [1993], a copy of which is contained in Appendix B.

References


Appendix A. Johansson et al. [1993]
First Results from the Fennoscandian GPS Networks

J.M. Johansson and R.T.K. Jaldehag
Onsala Space Observatory

J.L. Davis and P. Elosegui
Smithsonian Astrophysical Observatory

1993 AGU Fall Meeting
The Swedish Permanent GPS Network for Positioning (SWEPOS)

Collaborative effort between:

The National Land Survey of Sweden
Onsala Space Observatory
Smithsonian Astrophysical Observatory

Applications

Real-Time Navigation

“Low accuracy” positioning

Surveying

Geophysical applications, e.g., Postglacial rebound and correction of tide gauge data (SAO, OSO, U. Toronto)
Stainless steel plate for antenna

Thermostat and electrical heat conductor

Circular concrete pillar, Ø = 30 cm

Insulating material

Outer wall

Concrete plate

4 Iron Rods

Solid Rock

GPS Monument

Concrete Pillar + Steel bolt

GPS Site

The Local Control Network at Esrange
Karlstad - Umeå; Baseline Length = 560 km

WRMS = 2.0 mm

WRMS = 2.5 mm

WRMS = 5.5 mm
Correlation Study

- Using limited data (~60 days), we attempt to obtain measure of temporal correlations

- Method: Group observations into weeks, determine weekly averages

- If errors are uncorrelated day-to-day, errors in weekly averages should be $1/\sqrt{7}$ (0.378) times smaller

- Model for correlations: $r(\Delta t) = \exp[-|\Delta t| / \tau]$

- This model can be used to predict precision of averaged values for different values of $\tau$

- Using ratio of RMS scatters of averaged values to RMS scatters of unaveraged values, we can estimate $\tau$

- Results: $\tau \approx 1$ day ($r < 1\%$ after 5 days)
Prediction: Exponential Correlation

Swepcos Results

RMS Averaged
RMS Unaveraged

Correlation time (days)
Conclusions and Future Work

The results show that the network can be used in geophysical applications such as the DOSE investigation on Postglacial rebound

Smithsonian Astrophysical Observatory
Onsala Space Observatory
National Land Survey of Sweden
University of Toronto

Areas of research

Atmospheric Loading
Troposphere
Ionosphere
Multipath
Anti-Spoofing (AS)
Correlations (power spectra, etc.)
CONSTRAINING PROPOSED COMBINATIONS OF ICE HISTORY AND EARTH RHEOLOGY USING VLBI DETERMINED BASELINE LENGTH RATES IN NORTH AMERICA

J. X. Mitrovica, J. L. Davis, and I. I. Shapiro

Abstract. We predict the present-day rates of change of the lengths of 19 North American baselines due to the glacial isostatic adjustment process. Contrary to previously published research, we find that the three-dimensional motion of each of the sites defining a baseline, rather than only the radial motions of these sites, needs to be considered to obtain an accurate estimate of the rate of change of the baseline length. Predictions are generated using a suite of Earth models and late Pleistocene ice histories; these include specific combinations of the two which have been proposed in the literature as satisfying a variety of rebound-related geophysical observations from the North American region. A number of these published models are shown to predict rates which differ significantly from the VLBI observations.

Method and Results

In the present analysis we focus on the rates of change of baseline lengths (hereafter "length rates") for sites in North America. We limit our attention to baselines which extend, at least in part, over the near field and periphery of the ancient Laurentide ice sheet. We will not use baselines which include sites on the west coasts of Canada and the contiguous United States, in order to avoid areas of well-known tectonic deformation.

Our predictions of baseline length rates are based on the spectral formalism for computing three-dimensional motions detailed in Mitrovica et al. [1993b], which is appropriate for the surface loading of a spherically symmetric, self-gravitating, linear visco-elastic Earth model. We adopt a spherical harmonic truncation level at degree and order 256 for the surface mass load. The load will be comprised of a model for the late Pleistocene ice sheets, and a gravitationally self-consistent ocean loading component. The former is computed using the pseudo-spectral method of Mitrovica and Peltier [1991]. The Earth models we consider all have an elastic structure given by the Earth model PREM and a Maxwell visco-elastic rheology. The set of radial viscosities used in the calculations are specified below.

Our predictions of baseline length rates are summarized in Figure 2 (solid line) and agree well with the predictions obtained using the specified combination of ice history and radial velocity profile associated with North America.

In the following discussion we refer to a "standard" Earth model which has LT = 120 km, \( v_{LM} = 10^{10} \) Pa s and \( v_{LM} = 2 \times 10^{14} \) Pa s. In Figure 2 (solid line) we summarize predictions of the length rate of the Richmond-Westford baseline for a suite of Earth models identical to the standard model with the exception that \( v_{LM} \) is varied from \( 5 \times 10^{13} \) Pa s to \( 5 \times 10^{15} \) Pa s. The ice loading used in the calculation was based on the recently published ICE-3G deglaciation chronology, which extends...
Appendix B. Mitrovica et al. [1993]
from 18 to 5 kyr before present (Tushingham and Peltier [1991]), and adapted in order to incorporate a growth phase for the late Pleistocene ice sheets (see Mitrovica and Peltier [1993]).

The analysis of Tushingham [1991] represents the only attempt to date to calculate baseline length rates due to glacial isostatic adjustment. However, he assumed that these rates could be accurately computed by considering only radial deformations at the terminating sites. To assess the validity of this assumption, we also show in Figure 2 (dashed line) the component of the baseline length rate due to radial motions at the terminating sites, while the dashed line was computed assuming that only radial motions at these sites contribute to the length rate. The shaded region represents the VLBI determined constraint (±1σ) on the baseline length rate (Table 1).

In Figure 3 we plot the reduced χ² for the comparison of the VLBI baseline length rates with the predictions generated from many Earth models and two ice models. Figure 3a provides results generated using the ice loading adapted from the ICE-3G deglaciation chronology; each curve connects results from a set of Earth models constructed by varying a specific characteristic of the standard model (see caption). The two curves in Figure 3b are distinguished by the ice loading history adopted in the calculation. In particular, we generated the points on the dashed-dotted line using the ICE-1 model of Peltier and Andrews [1976] (adapted in the manner described above).

The results in Figure 3 show that the Earth models and ice histories represented there do not yield predictions with reduced χ² values significantly less than the value for the null hypothesis (3.3). The reasons for this outcome may be some combination of errors in the details of the ice loading histories over North America, the limited class of Earth models considered (see below), and contributions from neglected geophysical processes (e.g., tectonic deformations). Nevertheless, two important conclusions may be made. First, some ice history/Earth model pairings predict length rates which appear to be incompatible with the VLBI determined constraints, and may as a consequence be ruled out. For example, variants of the standard Earth model with LT ≤ 80 or μLM ≥ 3.3 × 10²¹ Pas, together with the ICE-3G deglaciation chronology, yield reduced χ² residuals in excess of 6.6 (or larger than twice the value for the null hypothesis). In contrast, many Earth models do not produce extremely high reduced χ² values, and therefore cannot be rejected.
Fig. 3. The reduced \( \chi^2 \) residual for the VLBI determined baseline length rates in Table 1 relative to the corresponding predictions obtained from a suite of Earth models and ice histories. (a) All curves are computed using the ice loading history adapted from the ICE-3G deglaciation chronology. The solid, dotted, and dashed lines are generated by varying, respectively, \( \nu_{UM} \), \( \nu_{LM} \), and LT of the standard Earth model. The pronounced increase in the reduced \( \chi^2 \), for \( \nu_{LM} \) greater or less than a value near 10\(^2\) Pa s, is due in large part to misfits in the predictions associated with the Richmond-Westford baseline. As an example, increasing \( \nu_{UM} \) from 2 \times 10\(^2\) Pa s to 5 \times 10\(^2\) Pa s results in an increase of the reduced \( \chi^2 \) by approximately 5.2 in Figure 3a. The increased misfit for predictions based on these two lower mantle viscosities, for the Richmond-Westford baseline length rate alone, accounts for 50% of this increase. (Mitrovica et al. [1993a] have found that far field sites, such as Richmond, have motions which are drawn more strongly toward the previously glaciated region (in this case Laurentia) as \( \nu_{LM} \) is increased. This trend gives rise to a transition from a lengthening to a shortening of the Richmond-Westford baseline as \( \nu_{LM} \) is increased.)

From Figure 3 we conclude that the current VLBI data set of North American baseline length rates may be applied to assess the acceptability of specific pairings of ice and Earth models. Inferences of the ice cover over North America, and the rheology below the region, have been a source of active interest and contention in the geophysical literature (see below). In the following we consider a number of ice model/Earth model combinations which have been proposed for the North American region on the basis of a variety of independent geophysical and geological constraints. The defining characteristics of four particular models are given in Table 2.

The column labelled T&P in Table 2 summarizes the model of Tushingham and Peltier [1991, 1992] which combines the standard Earth model and the ICE-3G deglaciation chronology; they have argued that this combination satisfies a globally distributed data base of RSL curves, including those collected in North America. The second model is that of Cathles [1975] (CAT) and includes an ice history that is similar to the ICE-1 model of Peltier and Andrews [1976]. The CAT model

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Model</th>
<th>T&amp;P</th>
<th>CAT</th>
<th>N&amp;L</th>
<th>DMVC</th>
<th>Null</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \nu_{UM} )</td>
<td>1.0</td>
<td>1.0</td>
<td>0.5</td>
<td>1.0</td>
<td>1.0</td>
<td>1.0</td>
</tr>
<tr>
<td>( \nu_{LM} )</td>
<td>2.0</td>
<td>0.9</td>
<td>3.0</td>
<td>1.0-10.0</td>
<td>1.0-10.0</td>
<td>1.0-10.0</td>
</tr>
<tr>
<td>LT (km)</td>
<td>120.0</td>
<td>70.0</td>
<td>100.0</td>
<td>120.0</td>
<td>120.0</td>
<td>120.0</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Baseline</th>
<th>Reduced ( \chi^2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>N2-W</td>
<td>0.3</td>
</tr>
<tr>
<td>R-W</td>
<td>0.4</td>
</tr>
<tr>
<td>G-R</td>
<td>0.2</td>
</tr>
<tr>
<td>G-W</td>
<td>0.2</td>
</tr>
<tr>
<td>A-G</td>
<td>0.4</td>
</tr>
<tr>
<td>G-N1</td>
<td>3.8</td>
</tr>
</tbody>
</table>

\( ^{\dagger} \) Ice models are discussed in text.
\( ^{\dagger\dagger} \) \( \nu_{UM} \) and \( \nu_{LM} \) are in units of 10\(^{21}\) Pa s.
was meant to satisfy the constraints imposed by the sea level record in North America, and the decay time inferred from that record. In contrast to these inferences, Nakada and Lambeck [1991] (N&L) have argued for a large (factor of 60) viscosity jump between the upper and lower mantle. The N&L model was based on fits to sea level curves in the Hudson Bay region, and their global ice model (ARC3 + ANT3) adopts the ICE-1 chronology over North America. The final model, labelled DMVC (Deep Mantle Viscosity Contrast), denotes a model characterized by an order of magnitude increase in viscosity at 1900 km depth in the mantle. Above 1900 km depth the viscosity is $10^{23}$ Pa s. This viscosity model was proposed by Mitrovica and Peltier [1992] as one which might reconcile the sea level record over Hudson Bay, and the independent inferences of viscosity provided by data associated with mantle convection (see Mitrovica and Peltier, 1992, for details). The Mitrovica and Peltier [1992] calculations adopted the ICE-3G deglaciation history.

The remaining rows of Table 2 provide the total reduced $\chi^2$ for the VLBI determined length rates in Table 1 relative to predictions based on the models described above (see row “All 19”), as well as the contribution to this reduced $\chi^2$ from predictions for each of the six baselines considered in Figure 4. The lowest (total) reduced $\chi^2$ values are obtained for the models DMVC and T&P. These reduced $\chi^2$ values are, however, indistinguishable, at the 95% confidence limit, from each other and from the value for the null hypothesis.

As a consequence of its low reduced $\chi^2$ the combination of ice history and Earth rheology proposed by Tushingham and Peltier [1991, 1992] cannot be ruled out by the VLBI constraints. The pairing proposed by Cathles [1975] yields a reduced $\chi^2$ about double the T&P value; the results in Table 2 suggest that the CAT model performs particularly poorly in regard to predictions of length rates for the NRAO 140'-Westford and Algonquin Park - Gilmore Creek baselines. Figures 3 and 4 indicate that the reduced $\chi^2$ residual might be lower if the thickness of the lithosphere in the Cathles [1975] model was increased. Indeed, an increase of LT to 120 km in the CAT model has been found to lower the reduced $\chi^2$ value below 4.

The total reduced $\chi^2$ computed for the N&L ice history/Earth rheology is relatively much higher. The predicted length rate of the Richmond - Westford baseline is a primary contributor to the misfit associated with this model. Indeed, the Nakada and Lambeck [1991] model predicts a shortening of approximately 2 mm/yr for the Richmond - Westford baseline length rate, which differs significantly from the observational constraint. The location of Richmond, in the far field of the Laurentide ice sheet, suggests that the viscosity model proposed by these authors would almost certainly have to be altered in order to satisfy the VLBI determined constraint on the Richmond - Westford baseline.

The reduced $\chi^2$ associated with the model DMVC is about 25% lower than the value for the null hypothesis. The result indicates that a relatively large viscosity contrast with depth within the lower mantle is not ruled out by the VLBI determined constraints on the baseline length rates listed in Table 1. Furthermore, it indicates that the sensitivity of the reduced $\chi^2$, to variations in $\nu_{3/2}$ (Figure 3), is more accurately identified as a sensitivity to variations in viscosity above 1900 km depth in the lower mantle (see also Mitrovica et al., 1993a).

Acknowledgements. This work was supported by an NSERC of Canada Research Grant, NASA grant NAG5-1930, and by the Smithsonian Institution.

References


