Lidar Performance Analysis

Contract No. NAS8-38609

Delivery Order No. 57

Contract Period 10/23/92 - 11/22/93

Report Date 8/15/94

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Introduction

This report details work carried out under NASA contract NAS8-38609.

Section 1 details the theory used to build the lidar model, provides results of using the model to evaluate AEOLUS design instrument designs and provides snapshots of the visual appearance of the coded model.

Appendix A contains a Fortran program to calculate various forms of the refractive index structure function. This program was used to determine the refractive index structure function used in the main lidar simulation code.

Appendix B contains a memo on the optimisation of the lidar telescope geometry for a line-scan geometry.

Appendix C contains the code for the main lidar simulation and brief instructions on running the code.

Appendix D contains a Fortran code to calculate the maximum permissible exposure for the eye from the ANSI Z136.1-1992 eye safety standards.

1.0 The lidar model

1.1 Description

The coherent lidar model was developed to allow the assessment of various space-based coherent Doppler lidar instruments under consideration at NASA Marshall Space Flight Center as part of the Laser Atmospheric Wind Sounder (LAWS) program. This section describes the theory used in the model.

1.1.1 Principle of operation

A Doppler lidar wind sounder measures the wind velocity at a remote location. It does this by transmitting an optical pulse which has a narrow frequency spread. This optical pulse is backscattered from aerosol targets (for the optical frequencies under consideration here) in the atmosphere. These aerosol particles are moving with the velocity of the local wind field and therefore impart a Doppler shift to the backscattered light. The backscattered light is collected at the lidar receiver and mixed with an optical local oscillator to produce a heterodyne beat signal on a detector. This heterodyne frequency (less any offset between the LO and transmitter laser) is proportional to the velocity difference between the lidar and the aerosol target. For a stationary lidar this difference is due solely to the aerosol velocity along the line of sight of the lidar. For a moving lidar, the lidar velocity along the line of sight of the instrument must be removed to obtain the aerosol velocity.

1.2 Lidar geometry

Figure (1.1) shows the geometry for a coherent lidar at an altitude, \( h \) above a spherical earth of radius, \( R_e \). The line of sight of the instrument makes an angle, \( \theta_n \), called the nadir angle with the vertical from the earth to the lidar. The nadir angle at the surface is \( \theta_{ns} \) and is given by:

\[
\theta_{ns} = \arcsin\left(\frac{R_1}{R_e}\right) \tag{1.1}
\]

where \( R_1 \) is the length of the perpendicular from the line of sight to the earth's center and is given by:

\[
R_1 = H \sin(\theta_n) \quad \text{where} \quad H = R_e + h \tag{1.2}
\]

The range from the lidar to the surface is given by:

\[
R = \left( H^2 + R_e^2 - 2HR_e \cos(\theta_{ns} - \theta_n) \right)^{0.5} \tag{1.3}
\]

For a target at an arbitrary altitude, \( z \) above the earth's surface, the nadir angle at the target and range from the lidar are given by substituting \( (R_e + z) \) for \( R_e \) in equations (1.1) and (1.3) respectively, i.e.
\[ \theta_n(z) = \text{asin} \left( \frac{R_1}{R_e + z} \right) \]  

(1.4)

\[ R(z) = \left( H^2 + (R_e + z)^2 - 2H(R_e + z) \cos (\theta_{nz} - \theta_n) \right)^{0.5} \]  

(1.5)

**Figure (1.1)** The geometry for a space-based lidar.

### 1.3 The coherent lidar signal to noise ratio equation

For an aerosol target at range, \( R \) with uniform backscatter coefficient, \( \beta \) over the dimensions of the transmitted beam, detector noise dominated by Local Oscillator (LO) shot noise the Coherent Laser Radar (CLR) SNR is given by:

\[
\text{SNR} = \frac{U_L T_T T_{TAR} T_A^2 \beta \pi D^2 T_{RAR} \eta c}{8h \nu B R^2 \left[ 1 + \frac{\pi D^2 \eta_{\text{mix}}}{2T_R \rho_0} \right]} 
\]

(1.6)

where \( U_L \) is the laser energy, \( T_T \) is the intensity transmittance of the transmit optics due to aperturing and obscuration, \( T_{TAR} \) is the intensity transmittance of the transmit optics due to losses (absorption, reflection) that are independent of the beam cross-section position, \( T_A \) is the one-way atmospheric attenuation, \( D \) is the effective diameter of the transmit telescope, \( T_{RAR} \) is the intensity transmittance of the receive optics, \( c \) is the speed of light in a homogeneous atmosphere, \( h \) is Planck's constant, \( \nu \) is the laser frequency, \( B \) is the signal bandwidth of the detector, \( \eta_{\text{mix}} \) (some-
times referred to as $\eta_h$) is the CLR mixing efficiency assuming perfect alignment and perfect polarisation matching, $T_R$ is the intensity transmittance of the transmit optics due to aperturing and obscuration, $\rho_0$ is the transverse coherence length of the backscattered optical field at the CLR, and $\eta$ is given by:

$$\eta = \eta_{mix} \eta_A \eta_P \eta_{HQE}$$  \hspace{1cm} (1.7)

where $\eta_A$ is the change in mixing efficiency due to misalignment between the back propagated local oscillator (BPLO) and the signal beam, $\eta_P$ is the BPLO/signal beam polarisation mismatch factor and $\eta_{HQE}$ is the detector heterodyne quantum efficiency. The transverse coherence length of the backscattered optical field is given by:

$$\rho_0 (R) = \left[ \frac{R}{H k^2 \int C_n^2 (x) \left(1 - \frac{x}{R}\right)^{5/3} \, dx} \right]^{-3/5}$$  \hspace{1cm} (1.8)

where $H=2.914383, k=2\pi/\lambda$ ($\lambda$ is the optical wavelength) and $C_n^2(x)$ is the refractive index structure constant at range $x$ from the CLR.

### 1.3.1 Transmitted pulse energy

The term $U_L T_T T_{TAR}$ represents the energy transmitted by the lidar system. The loss mechanism due to the optics has been split into the two terms $T_T$ and $T_{TAR}$ to allow various lidar geometries to be considered. $T_{TAR}$ is simply the product of the intensity transmission efficiencies of the individual optical components in the transmit path. $T_T$ is more complex and its value is dependent on the geometry of the lidar. Various authors [1-4] have shown that different receiver geometries and aperture truncations of the lidar transmit/receive beams will vary the heterodyne efficiency of the lidar system. Rye and Frehlich [3] analysed the optimum aperture truncation required for three lidar geometries. A summary of their results for Gaussian beams and large detector sizes (no detector aperturing effects) is presented in Table (1.1).

<table>
<thead>
<tr>
<th>Geometry</th>
<th>Transmitter</th>
<th>Receiver</th>
<th>Mixing Efficiency</th>
<th>System-Antenna Efficiency</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$r_{trunc}$</td>
<td>$T_T$</td>
<td>$r_{trunc}$</td>
<td>$T_R$</td>
</tr>
<tr>
<td>Wang [2]</td>
<td>1.763</td>
<td>0.955</td>
<td>1.763</td>
<td>0.955</td>
</tr>
<tr>
<td>Rye 1[1]</td>
<td>1.626</td>
<td>0.929</td>
<td>1.626</td>
<td>0.929</td>
</tr>
<tr>
<td>Rye 2[1]</td>
<td>1.736</td>
<td>0.951</td>
<td>1.192</td>
<td>0.758</td>
</tr>
</tbody>
</table>

For a given physical diameter, $D$ the $1/e^2$ spot size, $\sigma$ is related to the truncation radius, $r_{trunc}$ by

$$\sigma = \frac{D}{r_{trunc}\sqrt{2}}$$  \hspace{1cm} (1.9)
and $T_T$ is given by:

$$T_T = 1 - e^{-\left(\frac{D}{2\sigma}\right)^2}$$

(1.10)

**Geometry I:** An untruncated local oscillator is combined with the receiver signal. This is the geometry proposed by Wang and most commonly used in a practical lidar system.

**Geometry II:** The local oscillator is truncated in secondary optics designed to optimise the BPLO field by avoiding its truncation at the receiver aperture. Designated Rye 1 in Table 1.1.

**Geometry III:** An alternative to II. This is the theoretically optimum geometry. The local oscillator is truncated directly by the receiver aperture, but the BPLO is again untruncated. Difficult to implement in a practical scheme as the local oscillator would require a beam diameter greater than that of the collecting telescope. Rye 2 in Table 1.1.

*Figure (1.2)* The three receiver geometries discussed by Rye and Frehlich[3].
The system-antenna efficiency, $\eta_s$, is given by:

$$\eta_s = \eta_{\text{mix}} \frac{A_R}{A_T} T_T$$  \hspace{1cm} (1.11)

where $A_R$ and $A_T$ are receiver and transmitter aperture areas respectively. The lidars under consideration here (monostatic lidars) have a common transmit/receive aperture and therefore $A_R = A_T$ and the system-antenna efficiency is simply:

$$\eta_s = \eta_{\text{mix}} T_T$$  \hspace{1cm} (1.12)

### 1.3.2 Atmospheric attenuation

Atmospheric attenuation of the lidar beam arises from molecular and aerosol absorption and scattering. The Air Force Geophysical Laboratory has an atmospheric transmission/attenuation model based on the Hitran molecular database. This model or an equivalent can be used to generate atmospheric extinction/km as a function of altitude for each of the wavelengths of interest. The lidar model developed here uses these extinction as a function of height profiles to calculate the extinction between the lidar and the target aerosol. The model divides the atmosphere into 0.1 km thick layers from 0 km to 20 km. Above 20 km the extinction is insignificant and can be ignored for the purposes of this model. The atmospheric extinction, $T_A$, from the lidar to a target in the atmosphere is then given by:

$$T_A = e^{\sum \alpha_n l_n}$$ \hspace{1cm} (1.13)

where $n$ is the number of atmospheric layers from 20 km down to the target, $\alpha_n$ and $l_n$ are the extinction coefficient and path length respectively for layer $n$. The path length, $l_n$ in a layer between altitudes $z_1$ and $z_2$ is simply:

$$l_n = R(z_2) - R(z_1)$$ \hspace{1cm} (1.14)

where $R(z)$ is given by equation (1.5).

### 1.3.3 The refractive index structure function.

The WPL-37 refractive index profile [5] is an experimental refractive index structure function profile which has been used in lidar modeling [6]. It can be approximated using:

$$C_n^2(z) = \begin{cases} 
0 & \text{for } z > 20 \text{km} \\
3.66 \times 10^{-17} & \text{for } 20 \text{km} > z > 3 \text{km} \\
1.59 \times 10^{-12} \times z(\text{m})^{-4/3} & \text{for } 3 \text{km} > z > 10 \text{m} \\
7.36 \times 10^{-14} & \text{for } 10 \text{m} > z
\end{cases}$$ \hspace{1cm} (1.15)
Fairall and Frisch of NOAA have developed an analytic model of the refractive index structure function which takes into account location, season and local conditions[7]. This is an extensive model and the reader is referred to their technical memorandum for details, however the following typographical corrections were mentioned by the authors and should be noted:

Equations 19 and 24c on pages 7 and 8 of reference [7] should read:

\[ L = T / (\kappa g) (u_* T_*) \]

and:

\[ h_1(\xi) = 10 (1 - \xi)^{-3/2} (2 - \xi)^{-1} \]

respectively and Table 1 of reference [7] should be altered and added to as follows:-

<table>
<thead>
<tr>
<th></th>
<th>Colorado</th>
<th>Florida</th>
</tr>
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<tbody>
<tr>
<td>Winter</td>
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<tr>
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<td>Day</td>
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<td>Night</td>
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<tr>
<td>( \beta_0 )</td>
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<tr>
<td>10</td>
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<td>2</td>
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<td>0.4</td>
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</tr>
<tr>
<td>( \alpha )</td>
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<td>0.35</td>
</tr>
<tr>
<td>0.9</td>
<td>0.1</td>
<td>0.1</td>
</tr>
<tr>
<td>( u_* )</td>
<td>0.35</td>
<td>0.1</td>
</tr>
<tr>
<td>0.1</td>
<td></td>
<td>0.1</td>
</tr>
<tr>
<td>( R_{net} )</td>
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<td>350</td>
</tr>
<tr>
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<td>-100</td>
<td>700</td>
</tr>
<tr>
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<td>2000</td>
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<tr>
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<td>2000</td>
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<td>303</td>
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<td>263</td>
<td>283</td>
<td>293</td>
</tr>
<tr>
<td>278</td>
<td>288</td>
<td>303</td>
</tr>
</tbody>
</table>

Table (2.2) Parameters for the Fairall and Frisch \( C_n^2 \) model.

Additionally the refractive index structure function for the atmosphere of the ocean trade winds (e.g. off Florida) can be calculated using the Florida summer day parameters with \( \alpha \), changed to 0.93.

Fortran code to generate the experimental WPL-37 \( C_n^2 \) profile and the Fairall and Frisch models was developed (See “Appendix A - Refractive Index Structure Function Calculation” on page 23.). Appendix A also includes plots of these profiles. It can be seen that the model profiles and the WPL-37 profile are in general agreement. For the purposes of the lidar analyses under consideration here, variations in the refractive index structure function have small effects on the lidar SNR and so it was decided that the model would use the WPL-37 profile as a generic profile.
1.4 The efficiency term

This consists of the four terms $\eta_{\text{mix}}, \eta_{A}, \eta_{P}$ and $\eta_{\text{HQE}}$. The mixing efficiency (assuming perfect alignment), $\eta_{\text{mix}}$, is geometry dependant and is given in Table (1.1). The variation of the mixing efficiency as a function of the misalignment angle [9] between the BPLO and signal beams is shown in Figure (1.3), where $D$ is the telescope diameter and $\lambda$ is the optical wavelength.

As has been indicated previously the maximum mixing efficiency is dependant on the geometry used and so for the purposes of the lidar model the alignment efficiency, $\eta_{A}$ was obtained by normalising the data used to plot Figure (1.3) by dividing by the maximum mixing efficiency. The mixing efficiency for a system with misalignment is then given by taking the mixing efficiency due to geometry considerations (Table (1.1)) and multiplying by $\eta_{A}$.

The values of atmospheric backscatter, $\beta$ typically used are based on experimental field results using an assortment of lidars with assorted polarisation states. It may therefore be assumed that losses due to polarisation are explicitly accounted for in the use of experimentally derived $\beta$ values and therefore additional losses due to polarisation are likely to be small. However for completeness, the polarisation efficiency, $\eta_{P}$, although set to unity, is included in the model formulation.

The detector heterodyne quantum efficiency, $\eta_{\text{HQE}}$ is the efficiency with which the detector converts coherent photons into photoelectrons at the maximum bandwidth of the signal. For a detector on a spacecraft orbiting at ~7 km/s this corresponds to a bandwidth of ~1.4 GHz at 9 $\mu$m and ~12 GHz at 2 $\mu$m. The heterodyne quantum efficiency is usually significantly smaller than the DC quantum efficiency.
1.5 The velocity estimator

The model uses a parameterised maximum likelihood estimator provided by Dr. Rod Frehlich. The model provides values of the standard deviation of good estimates, \( g \) and the fraction of bad estimates, \( b \) as functions of \( \Phi \), the effective number of photo-electrons detected for fixed values of \( M \), the number of samples and \( \Omega \), the effective number of independent samples per estimate. The values of these parameters are given in Table (3.3). The variation of \( g \) and \( b \) as functions of \( \Phi \) are given by the empirical relations:

\[
\frac{g}{\omega} (\Phi) = \chi \left( 1 + \left( \frac{\Phi}{g_0} \right)^\varepsilon \right)^{-\delta} + \mu (1.16)
\]

and:

\[
b (\Phi) = \left( 1 + \left( \frac{\Phi}{b_0} \right)^\alpha \right)^{-\gamma} (1.17)
\]

Values of \( \chi, g_0, \varepsilon, \delta, \mu, b_0, \alpha \) and \( \gamma \) for various values of \( M \) and \( \Omega \) are listed in Appendix C - Lidar Performance Calculation.
1.6 The lidar scan pattern

The model considers three different scan patterns, a simple conical scan where the whole telescope is pointed off nadir and rotated (the original LAWS scan technique), a conical scan using a rotating nadir pointing telescope with a front refracting element to scan the beam and a line scan mechanism similar to the French BEST scan pattern.

The shot pattern on the ground of the two conically scanned systems is the same, however the performance is different due to a reduction in the effective aperture of the telescope for the refracting element scanner. The effective telescope diameter, $D_{\text{eff}}$ is:

$$D_{\text{eff}} = D \cos (\theta_n) \quad (1.18)$$

and it is this value that is used for the diameter in the SNR equation (1.6).

![Figure (1.4)](image.png)

**Figure (1.4)** Geometry of effective beam diameter dependence on nadir angle.

The line scan technique is discussed in Appendix B- AEOLUS Telescope Geometry on page 32.

1.7 Results of the model

NASA Marshall Space Flight Center is in the process of conducting studies on a small satellite coherent Doppler wind lidar known as AEOLUS (Autonomous Earth Observing Lidar Utility Sensor). The model was used to assess the performance of four concepts under consideration for this instrument. Two of the concepts use a 9 μm CO$_2$ laser device whilst the remaining two concepts use a 2 μm Ho:Tm:YLF laser device. For each of the two wavelength options, two different shot scanning schemes were considered - a dual-telescope bi-perspective line scan scheme and a conical scan using a rotating refractive wedge element. The laser device characteristics were chosen as those most likely to be available for a space mission without incurring a heavy development cost penalty. The parameters used by the lidar model for each of these systems is given in Table (4.4).
<table>
<thead>
<tr>
<th>Parameter</th>
<th>Design 1</th>
<th>Design 2</th>
<th>Design 3</th>
<th>Design 4</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Orbit</td>
<td></td>
<td></td>
<td></td>
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<td>98</td>
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<td>2.06</td>
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<td>0.5</td>
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<td>5</td>
<td>5</td>
<td>%</td>
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<td></td>
<td></td>
<td></td>
<td></td>
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<td>0.5</td>
<td>0.5</td>
<td>m</td>
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<td>30</td>
<td>30</td>
<td>deg.</td>
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<td>0.9</td>
<td>0.9</td>
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<td>0.9</td>
<td>0.9</td>
<td></td>
</tr>
<tr>
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<td>1</td>
<td>1</td>
<td>1</td>
<td></td>
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<tr>
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<td>16.07</td>
<td>3.15</td>
<td>3.64</td>
<td>μrad</td>
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<td>Complex</td>
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<td>Wang</td>
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<td>Wedge</td>
<td>Dual-look</td>
<td>Wedge</td>
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<td>N.A.</td>
<td>12</td>
<td>RPM</td>
</tr>
<tr>
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<td>0.5</td>
<td>0.5</td>
<td>0.5</td>
<td></td>
</tr>
</tbody>
</table>

Table (4.4) AEOLUS designs analysed.

Lidar Performance Analysis
Table (4.4) AEOLUS designs analysed.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Design 1</th>
<th>Design 2</th>
<th>Design 3</th>
<th>Design 4</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Altitude</td>
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<td>300</td>
<td>300</td>
<td>300</td>
<td>m</td>
</tr>
<tr>
<td>Max. horizontal velocity</td>
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<td>30</td>
<td>30</td>
<td>30</td>
<td>m/s</td>
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<tr>
<td>Vertical range resolution</td>
<td>1000</td>
<td>1000</td>
<td>1000</td>
<td>1000</td>
<td>m</td>
</tr>
</tbody>
</table>

The BPL0/signal alignment angle tolerance was chosen to give a value of 0.5 for $\eta_A$. This enables the tolerance requirement for the two wavelengths to be compared. An additional parameter listed in the table is the system margin. Traditionally the predicted and measured performance of coherent Doppler lidars have differed. The system margin is a 3 dB allowance to ensure that the design of the instrument will be adequate for the task. The atmospheric model used for the atmospheric extinction coefficient, $T_A$ was a mid-latitude summer clear aerosol model. This is the only atmosphere model that is included in the model at the moment and the data for this model were supplied by Coherent Technologies Inc., of Boulder, CO. Section shows some generic screen shots of the model (not for one of the four cases listed above). The performance of the lidar is generally characterised by two parameters, the backscatter value at which $b=0.5$ (1.17), i.e the velocity algorithm correctly determines the correct velocity 50% of the time and by $g$ (1.16) the standard deviation of the good velocity estimates about the true velocity. For the systems under consideration here the value of $g$ at $b=0.5$ is always adequate for the task and so the performance of these systems can be characterised by the single parameter, $\beta(50\%)$ the value of aerosol backscatter at which $b=0.5$.

<table>
<thead>
<tr>
<th></th>
<th>Design 1</th>
<th>Design 2</th>
<th>Design 3</th>
<th>Design 4</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\beta(50%)$</td>
<td>$7.8 \times 10^{-9}$</td>
<td>$1.1 \times 10^{-8}$</td>
<td>$5.1 \times 10^{-8}$</td>
<td>$6.8 \times 10^{-8}$</td>
<td>/m-sr</td>
</tr>
</tbody>
</table>

Table (5.5)

It should be pointed out that the AEOLUS design is still being refined.

1.8 Summary

A model of a space-based coherent lidar has been developed and is being used to assess the performance of various instrument designs.
1.9 Screen shots of the model

The following pages show screen shots of various views of the model together with samples of the input parameter dialogs.
### TARGET
- Aerosol altitude: 300 m
- Backscatter (lambda): 1.35E-09 m^-1 sr^-1
- Maximum horizontal velocity: 30 m/s
- Horizontal wind velocity uncertainty: 8 m/s
- Vertical wind velocity uncertainty: 8 m/s
- Wind variance between shots: 8 m/s
- Vertical range resolution: 1000 m
- Target nadir angle: 31.8320 deg
- Line of sight range to this altitude: 407,5826 km
- Coherence length: 20,58645 m
- One way intensity transmission: 8,787387
- Maximum line of sight velocity: 16,82326 m/s

### SIGNAL PROCESSING
- Line of sight range resolution: 1177,8369 m
- Observation time: 7.8523 s
- Time between sample points: 8.1440 s
- Digitisation frequency: 8.9462 MHz
- No. sample points: 64,5263
- Phi: 4.872
- Signal width: 8.3748 MHz
- Omega: 2.9431 m/s
- Sigma/psi: 8.8267 MHz
- No. of shots/ wind estimates: 1
- Bandwidth (wide band): 8.8442 MHz
- Bandwidth (narrow band): 8.3748 MHz
- MLE row no.: 6

### OTHER PARAMETERS
- Satellite velocity: 7784,321 m/s
- Ground track velocity: 7763,123 m/s
- Earth rotation velocity at equator: 453,3357 m/s
- Slant range to ground: 407,917,5 m
- Spot diameter on ground: 18,8383 m
- Time for one orbit: 5461,504 s
- Swath radius (conical/wedge scan): 293008,5 m
- Optimum mirror flip time (line scan): 30,48024 s

### RESULTS
- Wideband SNR: 18.499742 dB
- Narrowband SNR: -8.7298153 dB
- P(bad): 8.4965919 dB
- P(good): 8.5914081 dB
- Sigmae/psi - instrument: 1.6919 m/s
- Sigmae/psi: 1.8799 m/s
- F.O.M. F: 1.9682
- PHI: 4.8721886
This plot is relevant to the half of 'BEST' shot pattern.
One benefit of having the input menus accessible from the button bar is the ability to change the lidar parameters from anywhere within the model. Changing the laser wavelength in this example would cause the extinction plot to automatically be recalculated and displayed for the user when the OK box on the input dialog is selected.
Samples of the other input dialog boxes.
1.10 References


2.0 Appendix A - Refractive Index Structure Function Calculation

2.1 Program structure

Program CN2CALG - main routine, allows user to select $c_n^2$ profile desired, determines routines to be used and calls them, saves results to output file called $c_n^2$.dat. Output is in three columns, first column is altitude in km, second column is $c_t^2$ and third column is $c_n^2$.

Subroutine CLRSCRN(I) - is a utility subroutine that scrolls the output screen by I lines. Called by the main program.

Function WPLCN(Z) - is a function for calculating the WPL-37 $c_n^2$ profile. For this $c_n^2$ case, the $c_t^2$ profile is not generated. Called by the main program.

Function CT2(Z,HP,P0,PBLZ,RNET,USTAR,ALPHA,BETA0) - is a function for calculating the $c_t^2$ value for a given altitude for all cases except the WPL-37 profile. This value is then used to calculate the value of $c_n^2$ (except for WPL-37). Called by the main program.

Function CN2(Z,HP,P0,CT,T0,ZT) - is a function for calculating the $c_n^2$ value at a given altitude for all cases except the WPL-37 profile. Called by the main program.

Function CTPBL(Z,PBLZ,ALPHA,RNET,BETA0,USTAR,T,DAY) - is a function for calculating the $c_t^2$ value in the planetary boundary layer. Called by function CT2.

2.2 Program code

2.2.1 Program CN2CALG

```c
PROGRAM CN2CALG

IMPLICIT NONE

REAL*4 HP,P0,PBLZ,RNET,USTAR,ALPHA,OLDCT,
+ BETA0,T0,ZT,ETA,MAXZ,DZ,Z,CN2,CT,CN,CT2,
+ BETA(12),ALPH(12),U(12),NETR(12),ZPBL(12),
+ TZ(12),TEMP0(12),WPLCN

INTEGER I,N,DAY, ILOCAL,ISEAS,ITIME, INDEX,
+ WPL

PARAMETER (HP=6500.,P0=1000.)
MAXZ=20000.0
N=500
WPL=0
OLDCT=0.0

DATA BETA /2.,10.,1.,10.,0.25,10.,0.35,10.,0.25,0.25,0.25,0.25/,
DATA ALPH /0.2,0.9,0.4,0.9,0.2,0.9,0.9,0.2,0.9,0.93,0.93,0.93/,
DATA U /0.35,0.1,0.5,0.1,0.35,0.1,0.5,0.1,0.35,0.35,0.35,0.35/,
DATA NETR /600.,-100,100.,-100.,700.,-100.,350.,-100.,700.,
+ 700.,700.,700./
DATA TZ /12000.,12000.,7000.,7000.,14000.,14000.,9000.,9000.,
+ 9000.,9000./
```

Lidar Performance Analysis 23
This program calculates the refractive index structure constant, Cn2 for various locations, based on NOAA Technical Memorandum ERL WPL-195 "Diurnal and Annual Variations in Mean Profiles of Cn2". Developed for various locations, seasons, and conditions, the calculation is based on NOAA Technical Memorandum ERL WPL-195 "Diurnal and Annual Variations in Mean Profiles of Cn2". This program developed by Gary Spiers, Center for Applied Optics, University of Alabama in Huntsville. This program calculates the refractive index structure constant, Cn2 for various locations, seasons, and conditions. The calculation is based on NOAA Technical Memorandum ERL WPL-195 "Diurnal and Annual Variations in Mean Profiles of Cn2". This program developed by Gary Spiers, Center for Applied Optics, University of Alabama in Huntsville.

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This program calculates the refractive index structure constant, Cn2 for various locations, seasons, and conditions. The calculation is based on NOAA Technical Memorandum ERL WPL-195 "Diurnal and Annual Variations in Mean Profiles of Cn2". This program developed by Gary Spiers, Center for Applied Optics, University of Alabama in Huntsville.

This program calculates the refractive index structure constant, Cn2 for various locations, seasons, and conditions. The calculation is based on NOAA Technical Memorandum ERL WPL-195 "Diurnal and Annual Variations in Mean Profiles of Cn2". This program developed by Gary Spiers, Center for Applied Optics, University of Alabama in Huntsville.
WRITE(*,*)'Please select the time of day:-'
WRITE(*,*)' 1) Daytime'
WRITE(*,*)' 2) Nightime'
READ(*,*) ITIME
IF ((ITIME.LT.1).OR.(ITIME.GT.2)) THEN
  WRITE(*,*)' Please choose a valid time of day!'
  GOTO 12
ENDIF
ENDIF
WRITE(*,*) 'Calculating...
IF (WPL.EQ.0) THEN
  INDEX=(ILOCAL-I)*4+(ISEAS-I)*2+ITIME
  DAY=2-ITIME
  BETA0=BETA(INDEX)
  ALPHA=ALPH(INDEX)
  USTAR=U(INDEX)
  RNET=NETR(INDEX)
  PBLZ=ZPBL(INDEX)
  ZT=TZ(INDEX)
  T0=TEMP0(INDEX)
END IF
OPEN(UNIT=9,FILE='cn2.dat')
DZ=ALOG10(MAXZ)/N
DO 15 I=1,N
  Z=10.**(I*DZ)
  IF (WPL.EQ.1) THEN
    CT=0
    CN=WPLCN(Z)
  ELSE
    ETA= Z/PBLZ
    IF ((ETA .GE. 0.95) .AND. (ETA. LT. 1.0)) THEN
      CT=OLDCT
    ELSE
      CT=CT2(Z,HP,P0,PBLZ,RNET,USTAR,ALPHA,BETA0,
               T0,DAY,ZT)
    ENDIF
    OLDCT=CT
    CN=CN2(Z,HP,P0,CT,T0,ZT)
  ENDIF
  WRITE(9,20) Z/1000,CT,CN
CONTINUE
15 FORMAT(3E15.8)
STOP
END

2.2.2 Subroutine CLRSCRN

SUBROUTINE CLRSCRN(I)
INTEGER J,I
DO 100 J=1,I,1
  WRITE(*,*)
100 CONTINUE
RETURN
END
2.2.3 Function WPLCN

REAL*4 FUNCTION WPLCN(Z)

IMPLICIT NONE
REAL*4 Z

IF (Z.LT.10.) THEN
   WPLCN=7.36*10.**(-14.)
ELSEIF ((Z.GE.10.).AND.(Z.LT.3000.)) THEN
   WPLCN=1.59*10.**(-12.)*Z**(-4./3.)
ELSEIF ((Z.GE.3000.).AND.(Z.LE.20000.)) THEN
   WPLCN=3.66*10.**(-17.)
ELSE
   WPLCN=0.
ENDIF
RETURN
END

2.2.4 Function CT2

REAL*4 FUNCTION CT2(Z, HP, P0, PBLZ, RNET, USTAR, ALPHA, @BETA0, T0, DAY, ZT)

IMPLICIT NONE
REAL*4 HP, P0, DTROP, CTT, CTS, PBLZ, RNET, USTAR, ALPHA, @BETA0, T0, ZT, Z, T, CT, CTPBL
INTEGER DAY

PARAMETER (DTROP=2000., CTT=8.E-5, CTS=1.E-3)
P=P0*EXP(-Z/HP)
IF (Z.LT.ZT) THEN
   T=T0-(T0-216.)*Z/ZT
ELSE
   T=216.0
ENDIF
IF ((Z .LT. (ZT-DTROP)) .AND. (Z .GE. PBLZ)) THEN
   CT2=CTT
ELSEIF ((Z .GE. (ZT-DTROP)) .AND. (Z .LE. (ZT+ DTROP))) THEN
   CT2=(ALOG10(CTS)-ALOG10(CTT))*(Z-ZT)/(DTROP*2)
   CT2=IO''(CT)
ELSE
   CT2=CTS
ENDIF
IF (Z .LT. PBLZ) THEN
   CT2=CTPBL(Z, PBLZ, ALPHA, RNET, BETA0, USTAR, T, DAY)
ENDIF
RETURN
END
2.2.5 Function CN2

```fortran
REAL*4 FUNCTION CN2(Z, HP, P0, CT, T0, ZT)

C IMPLICIT NONE

C REAL*4 HP, P0, Z, CT, T0, ZT, P, T

P=P0*EXP(-Z/HP)
IF (Z.LT.ZT) THEN
  T=T0-(T0-216.)*Z/ZT
ELSE
  T=216.0
ENDIF
CN2=((7.9E-5*P/T**2)**2)*CT
RETURN
END
```

2.2.6 Function CTPBL

```fortran
REAL*4 FUNCTION CTPBL(Z, PBLZ, ALPHA, RNET, BETA0, USTAR, T, DAY)

C IMPLICIT NONE

C REAL*4 Z, PBLZ, ETA, HSO, ALPHA, RNET, BETA0, TSTAR, RHOCP, USTAR
C *L, KARMAN, G, WSTAR, T, THETA, HB, HTB, HT, RT
C INTEGER DAY

PARAMETER (RHOCP=1100, G=9.81, KARMAN=0.4)
ETA=Z/PBLZ
HSO=(1.-ALPHA)*RNET/(1.+1./BETA0)
TSTAR=-HSO/(RHOCP*USTAR)
L=(T*USTAR**2)/(KARMAN*G*TSTAR)
IF (DAY .EQ. 1) THEN
  WSTAR=((-G/T)*USTAR*TSTAR*PBLZ)**(1./3.)
  THETA=-USTAR*TSTAR/WSTAR
  HB=10.*(PBLZ/L)**(2./3.)*((ETA*(1.-7.*Z/L))**(-2./3.)
  HTB=8.*(1.-0.8**ETA)
  IF (ETA .GT. 0.95) THEN
    HT=10.*(-0.05)**(-3./2.)/1.05
  ELSE
    HT=10.*(-1.-ETA)**(-3./2.)/(2.-ETA)
  ENDIF
  RT=-0.2*(1.+3.2*(-L/PBLZ))
  CTPBL=THETA**2*PBLZ**(-2./3.)*(HB+RT*HTB+RT**2*HT)
ELSE
  CTPBL=TSTAR**2*Z**(-2./3.)*(1.+2.7*(Z/L)**(2./3.))
ENDIF
RETURN
END
```

2.3 Plots of output results.
Colorado

Altitude (km)

$10^{-18}$ $10^{-17}$ $10^{-16}$ $10^{-15}$ $10^{-14}$ $10^{-13}$ $10^{-12}$

$C_n^2 (m^{-2/3})$

Winter, Night

Winter

Summer, Night

Summer

Winter, Day

Summer, Day
3.0 Appendix B- AEOLUS Telescope Geometry

This appendix was originally a memo released to the AEOLUS team on 9/29/93.

In this document, nadir always refers to the spacecraft nadir.

![Diagram of AEOLUS Telescope Geometry]

**Figure (1.5) 3-D geometry.**

3.1 Angle definitions

< DEB = \( \theta_n \), the angle between the line of sight and nadir (nadir angle).

< AED = \( \theta_r \), the angle between the left/right component of the line of sight and nadir.

< DEC = \( \theta_p \), the angle between the forward/aft component of the line of sight and nadir.
Consider triangle DEB:

![Diagram of triangle DEB](image)

**Figure (1.6)** Triangle formed by line of sight and nadir.

Thus we have DE and DB in terms of \( L \), the slant range to the ground and \( \theta_n \), the nadir angle. We can fold the triangles ADE and CDE into the ground plane ABCD:

![Diagram of folded triangles](image)

**Figure (1.7)** Folding of triangles ADE and CDE into the ground plane ABCD.
From Figure (1.6) we obtain expressions for ED and DB in Figure (1.7) and from Page (1) we have \( \angle DEC = \theta_F \) and \( \angle AED = \theta_R \). Simple trigonometry gives expressions for AD and CD. ABCD is a rectangle and so AB = CD. AD, AB and BD are related by Pythagoras’ theorem:

\[
AD^2 + AB^2 = BD^2
\]  

(1.19)

substituting gives:

\[
L^2 \cos^2(\theta_n) \tan^2(\theta_R) + L^2 \cos^2(\theta_n) \tan^2(\theta_F) = L^2 \sin^2(\theta_n)
\]

(1.20)

dividing by \( L^2 \cos^2(\theta_n) \) gives:

\[
\tan^2(\theta_R) + \tan^2(\theta_F) = \tan^2(\theta_n)
\]

(1.21)

Thus we have obtained an expression relating \( \theta_n \) to \( \theta_R \) and \( \theta_F \).

3.2 Optimum geometry for wind velocity measurement.

Ideally we would like to resolve the wind velocity components along and perpendicular to the ground track with equal resolution. In Figure (1.7) these components are represented in the ground plane by DC and DA respectively and for them to have equal weighting we should therefore arrange the geometry such that:

\[
DA = DC
\]

(1.22)

Substituting values and simplifying gives:

\[
\theta_R = \theta_F
\]

(1.23)

Substituting back into Equation (1.21) gives:

\[
2 \tan^2(\theta_F) = \tan^2(\theta_n)
\]

(1.24)

rearranging to give \( \theta_F \) as a function of \( \theta_n \):

\[
\tan(\theta_F) = \tan(\theta_n)/\sqrt{2}
\]

(1.25)

3.3 Angle between forward and aft view optical axes

For the dual telescope option, the angle, \( \alpha \) between the forward and aft view optical axes is the angle between the forward and aft lines of sight. As the geometry is symmetric about the line perpendicular to the ground track, this angle is given by \( 2 \angle AEB \). Figure (1.8) shows the geometry for this calculation where \( B' \) is the aft-view point equivalent to \( B \). We see that:

\[
\sin(\alpha/2) = \cos(\theta_n) \tan(\theta_F)
\]

(1.26)

substituting for \( \tan(\theta_F) \) from Equation (1.25) and simplifying gives:

\[
\alpha = 2 \sin^{-1}(\sin(\theta_n)/\sqrt{2})
\]

(1.27)

For AEOLUS we have \( \theta_n = 30 \text{ deg.} \) and therefore \( \alpha = 41.41 \text{ deg.} \) and \( \theta_F = \theta_R = 22.21 \text{ deg.} \).
Figure (1.8) Geometry for telescope axis separation and path length on surface of earth.

3.4 Path length between forward and aft points on the ground.

Figure (1.8) also shows the center of the earth, $C_e$ and the arc of the earth's surface $B'A'B$ between the forward and aft line of sight ground points. We see that $B'AB$ represents the chord linking these two points. From triangle $ABC_e$ we can determine the half-angle subtended at the earth's center, $\gamma/2$ as:

$$\sin(\gamma/2) = \frac{L \cos(\theta_n) \tan(\theta_F)}{R_e}$$

(1.28)

The angle subtended by the earth's arc is $\gamma$ and the length of the arc is given by $R_e \gamma$, where $\gamma$ is in radians. This gives:

[track length] = $2R_e \sin^{-1}(L \cos(\theta_n) \tan(\theta_F)/R_e)$

(1.29)

For the AEOLUS conditions of $\theta_n = 0.5236$ (30 deg), $\theta_F = 0.3876$ (22.21 deg) and $R_e = 6371315$ m we have a line of sight length, $L$ of 407916 m for a 350 km satellite altitude, assuming a spher-
ical earth. This gives a track length of 288498m between the forward and aft line of sight ground points. The ground track velocity is 7303 ms$^{-1}$ and therefore the time to cover this distance will be 39.5 s. This means that to overlap the forward and aft views on the same patch of ground, the instrument should look in the forward direction for 39.5 s before changing to the aft view. At a constant PRF of 10 Hz the separation between pulses on the ground will therefore be 730.5 m, for a 20 Hz pulse rate this separation will reduce to 365.3 m.

3.5 Effect of varying $\theta_n$.

The following plots show the variation of $\theta_R$, $\theta_F$ and $2\alpha$ as the nadir angle, $\theta_n$ varies between 0 deg. and 90 deg.

The first plot shows the dependence of $\theta_R$ on $\theta_F$ for various $\theta_n$.

![Figure (1.9) The dependence of $\theta_R$ on $\theta_F$ for various nadir angles, $\theta_n$.](image)

All of the remaining figures use the optimum geometry, $\theta_R = \theta_F$. It should be noted that for the orbit height under consideration, nadir angles greater than 70 deg. have not been considered as the line of sight does not contact the earth’s surface at larger angles.
**Figure (1.10)** Dependence of fore/aft optical axes angular separation on nadir angle.

**Figure (1.11)** Expansion of Figure (1.10) to show region of interest.
Figure (1.12) Dependence of the ground track length between the fore and aft line of sight ground points on nadir angle.

Figure (1.13) Expansion of Figure (1.12) to show the region of interest.
Figure (1.14) Dependence of forward look time on nadir angle.

Figure (1.15) Expansion of Figure (1.14) to show the region of interest.
4.0 Appendix C - Lidar Performance Calculation

4.1 Description

This appendix lists the code used to generate the lidar model. Unlike conventional programming, spreadsheet programs do not consist of a linear list of commands but a series of expressions at various locations throughout the spreadsheet. The built-in code provided by the spreadsheet vendor enables a user interface to be created with relative ease. The nature of this program centers on looking up values in assorted tables and then performing limited numerical calculations on them is ideally suited to a spreadsheet. Results can then easily be presented to the user through the use of the vendor supplied graph plotting routines.

This program consists of three files:-

- Lidar.WB1 - the main spreadsheet which obtains user inputs, performs calculations and presents results.
- Atmos.WB1 - a spreadsheet containing the atmospheric extinction as a function of altitude for a range of wavelengths.
- Lidar.BAR - a toolbar which is used to provide access to the input routines.

The program is written for the Borland Quattro-Pro for Windows spreadsheet. Each section of the code is contained on a separate notebook page of the spreadsheet. The code on each page is listed below. A 'user’s view' of each page was provided in Section 1.9.

4.2 Using the program

To run the program, the user should place the three files listed above in a common directory. Quattro Pro for Windows should then be started and the file Lidar.WB1 loaded. When loading this program will ask if the user wishes to open supporting hotlinks (this refers to the Atmos.WB1 file). The answer to this question should be ‘OK’. The Lidar.BAR speedbar is loaded as a second speedbar by following the instructions in the Quattro Pro documentation. It is intended to automate the start-up procedure at a later time. Once the program is loaded the user can select input parameters for the various lidar components by ‘clicking’ on the required component button on the speedbar and then changing the values in the dialog boxes. All plots update automatically (unless the user has explicitly turned off automatic update) except for the performance plot which is only updated when the ‘Update Graphs’ button on that page is selected.

At the time of this report additional velocity estimation parameter regimes were still being provided by Dr. Frehlich therefore a routine to automatically select the optimum parameterisation for a pair of $\Omega$ and M values had not been implemented. This means that the user must manually tell the spreadsheet which parameterisation to use. This is done by typing the row number of the closest $\Omega$ M pair on the velocity estimator look-up table into the cell labeled “MLE row no.” on the Results page of the spreadsheet.

The code is still under development with current work concentrating on getting the code operational rather than ‘bullet-proof’ and so none of the help buttons currently provide messages and
the user is not protected from modifying the spreadsheet. A backup copy of the files should therefore be kept in another location.

### 4.3 Variable list

The following table lists the variables used and their locations. Spreadsheet cell references are of the form \([\text{SSNAME}]\text{PGNAME:CELL}\) where \text{SSNAME} is the name of the relevant spreadsheet (defaults to active current spreadsheet if not supplied), \text{PGNAME} is the relevant page of the spreadsheet and \text{CELL} is the cell address on the page.

The values in this table were exported from the spreadsheet page Block_Names. Due to differences in the number of columns used in the spreadsheet and here the list is not in strict alphabetical order, where alphabetical order is not followed, a double horizontal line occurs in the table below.

<table>
<thead>
<tr>
<th>Variable Name</th>
<th>Cell Location</th>
<th>Variable Name</th>
<th>Cell Location</th>
</tr>
</thead>
<tbody>
<tr>
<td>ALIGNDAT</td>
<td>Alignment:A36..B173</td>
<td>EPSILON</td>
<td>ML_Estimator:J2</td>
</tr>
<tr>
<td>ALIGN_ANGLE</td>
<td>Instrument:C22</td>
<td>ETA_ALIGN</td>
<td>Alignment:B37</td>
</tr>
<tr>
<td>ALIGN_LOSS</td>
<td>Alignment:E44</td>
<td>ETA_EXTINCT</td>
<td>Extinction:C242</td>
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<td>ETA_HETERODYNE</td>
<td>Instrument:G8</td>
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<tr>
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<td>Results:C2</td>
<td>ETA_HQE</td>
<td>Instrument:G6</td>
</tr>
<tr>
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<td>Extinction:A37</td>
<td>ETA_MISALIGN</td>
<td>Instrument:G10</td>
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<td>CoherenceL:A37</td>
<td>ETA_POLARISE</td>
<td>Instrument:C21</td>
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<tr>
<td>ATTN</td>
<td>Results:C13</td>
<td>ETA_SYSTEM</td>
<td>Instrument:G9</td>
</tr>
<tr>
<td>B</td>
<td>Results:G5</td>
<td>EXTINCTDAT</td>
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<td>FALSESPEC_MSG</td>
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<td>FREQ</td>
<td>Instrument:C14</td>
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<td>G</td>
<td>Constants:B7</td>
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<td>Instrument:G5</td>
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<td>H</td>
<td>Constants:B2</td>
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<td>CoherenceL:C241</td>
<td>HCOHERENCE</td>
<td>Constants:B8</td>
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<td>D</td>
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<td>LAMBDA</td>
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<td>DUTY</td>
<td>Instrument: C11</td>
<td>LOSRANGE</td>
<td>Results: G2</td>
</tr>
<tr>
<td>M</td>
<td>Results: G6</td>
<td>PHI</td>
<td>Results: G7</td>
</tr>
<tr>
<td>MARGIN</td>
<td>Instrument: G24</td>
<td>PLOTMINS</td>
<td>Instrument: G18</td>
</tr>
<tr>
<td>ME</td>
<td>Constants: B5</td>
<td>POLN</td>
<td>Instrument: C21</td>
</tr>
<tr>
<td>MIN_BETA_POINT</td>
<td>Macros: B10</td>
<td>PRF</td>
<td>Instrument: C12</td>
</tr>
<tr>
<td>MIN_PROB</td>
<td>Macros: B11</td>
<td>QE</td>
<td>Instrument: G6</td>
</tr>
<tr>
<td>MLS_CLEAR</td>
<td>Perform: B1..J202</td>
<td>R</td>
<td>Results: C10</td>
</tr>
<tr>
<td>MSG1</td>
<td>messages: B2..B7</td>
<td>RANGE</td>
<td>Extinction: D37</td>
</tr>
<tr>
<td>MSG2</td>
<td>messages: B9..B28</td>
<td>RANGE2</td>
<td>CoherenceL: C37</td>
</tr>
<tr>
<td>MSG3</td>
<td>messages: B30..B50</td>
<td>RE</td>
<td>Constants: B4</td>
</tr>
<tr>
<td>MTS</td>
<td>Results: G2</td>
<td>RECEIVER_DATA</td>
<td>Instrument: G4..G6</td>
</tr>
<tr>
<td>MU</td>
<td>ML_Estimator: K2</td>
<td>RECEIVER_GEOM</td>
<td>Lists: C1..G4</td>
</tr>
<tr>
<td>MULTIPLIER</td>
<td>CoherenceL: F37</td>
<td>RECEIVER_TYPE</td>
<td>Lists: J1..J2</td>
</tr>
<tr>
<td>NADALT</td>
<td>Results: C9</td>
<td>RH00</td>
<td>Results: C11</td>
</tr>
<tr>
<td>NADALT1</td>
<td>Extinction: C37</td>
<td>RO</td>
<td>Instrument: C20</td>
</tr>
<tr>
<td>NADALT2</td>
<td>CoherenceL: B37</td>
<td>RPM</td>
<td>Instrument: G19</td>
</tr>
<tr>
<td>NADIR</td>
<td>Instrument: C18</td>
<td>RSWATH</td>
<td>Results: C26</td>
</tr>
<tr>
<td>NAROW_BANDWIDTH</td>
<td>Results: G13</td>
<td>SAVE_BETA</td>
<td>Macros: B8</td>
</tr>
<tr>
<td>NRG</td>
<td>Instrument: C9</td>
<td>SCANNER_DATA</td>
<td>Instrument: G17..G19</td>
</tr>
<tr>
<td>NSHOTS</td>
<td>Results: G11</td>
<td>SCAN_DATA</td>
<td>Instrument: G17..G19</td>
</tr>
<tr>
<td>ORBH</td>
<td>Instrument: C4</td>
<td>SCAN_FLAG</td>
<td>Scan_Pattern: J39</td>
</tr>
<tr>
<td>ORBINC</td>
<td>Instrument: C5</td>
<td>SCAN_TYPE</td>
<td>Instrument: G17</td>
</tr>
<tr>
<td>ORBIT_DATA</td>
<td>Instrument: C4..C5</td>
<td>SCAN_TYPE_LIST</td>
<td>Lists: J1..J3</td>
</tr>
<tr>
<td>PARAM</td>
<td>Alignment: A37</td>
<td>SIGMAM</td>
<td>Results: G24</td>
</tr>
<tr>
<td>PATH</td>
<td>Extinction: E37</td>
<td>SIGMAS</td>
<td>Results: C7</td>
</tr>
<tr>
<td>Instrument</td>
<td>Constants</td>
<td>Performance</td>
<td>Results</td>
</tr>
<tr>
<td>-----------------</td>
<td>-------------------------</td>
<td>-------------</td>
<td>---------</td>
</tr>
<tr>
<td>PATH2</td>
<td>CoherenceL:D37</td>
<td>SIGMAVLOS</td>
<td>Results:G25</td>
</tr>
<tr>
<td>PBAD</td>
<td>Results:G22</td>
<td>SIGMAV_H</td>
<td>Results:C5</td>
</tr>
<tr>
<td>PERFORMANCE</td>
<td>Perform:A36..E59</td>
<td>SIGMAV_I</td>
<td>Results:G24</td>
</tr>
<tr>
<td>PERFORM_CALC</td>
<td>Macros:B13</td>
<td>SIGMAV_V</td>
<td>Results:C6</td>
</tr>
<tr>
<td>PGOOD</td>
<td>Results:G23</td>
<td>SLANTG</td>
<td>Results:C23</td>
</tr>
<tr>
<td>SNR</td>
<td>Results:G20</td>
<td>TSTEP</td>
<td>Scan_Pattern:B1</td>
</tr>
<tr>
<td>SNR_NARROW</td>
<td>Results:G21</td>
<td>TT</td>
<td>Instrument:G7</td>
</tr>
<tr>
<td>SNR_WIDE</td>
<td>Results:G20</td>
<td>TTAR</td>
<td>Instrument:C19</td>
</tr>
<tr>
<td>SPOTG</td>
<td>Results:C24</td>
<td>T_SPEC_WIDTH</td>
<td>Constants:B9</td>
</tr>
<tr>
<td>SYSTEM</td>
<td>Instrument:G9</td>
<td>V1</td>
<td>Results:C21</td>
</tr>
<tr>
<td>TARGET_ALTITUDE</td>
<td>Results:C2</td>
<td>VEARTH</td>
<td>Results:C22</td>
</tr>
<tr>
<td>TARGET_DATA</td>
<td>Results:C2..C8</td>
<td>VERT_RANGE</td>
<td>Results:C8</td>
</tr>
<tr>
<td>TAU</td>
<td>Instrument:C10</td>
<td>VG</td>
<td>Results:C21</td>
</tr>
<tr>
<td>TE</td>
<td>Constants:B6</td>
<td>VMAXH</td>
<td>Results:C4</td>
</tr>
<tr>
<td>TEST</td>
<td>Extinction:L27</td>
<td>VMAXLOS</td>
<td>Results:C14</td>
</tr>
<tr>
<td>TFLIP</td>
<td>Results:C27</td>
<td>VSAT</td>
<td>Results:C20</td>
</tr>
<tr>
<td>TO</td>
<td>Instrument:C19</td>
<td>VSEARCH</td>
<td>Results:C4</td>
</tr>
<tr>
<td>TORBIT</td>
<td>Results:C25</td>
<td>W</td>
<td>Results:G8</td>
</tr>
<tr>
<td>TRAR</td>
<td>Instrument:C20</td>
<td>WIDE_BANDWIDTH</td>
<td>Results:G5</td>
</tr>
<tr>
<td>TS</td>
<td>Results:G4</td>
<td>WPL37DAT</td>
<td>CoherenceL:A36..F237</td>
</tr>
<tr>
<td>TSCOPE_D</td>
<td>Instrument:C17</td>
<td>\P</td>
<td>Perform:140</td>
</tr>
</tbody>
</table>

### 4.4 Instrument

The following code lists the contents of cells on the instrument page. Text cells contain the initial characters, 'I, ^ and " which indicate left, center and right alignment respectively. Cell contents beginning with a + or @ are calculation cells. All of the cells are visible to the user.

Instrument:C1: 'Instrument Parameters
Instrument:B3: ^ORBIT
Instrument:F3: ^RECEIVER
Instrument:B4: "Orbit height
Instrument:C4: 350
Instrument:D4: 'km
Instrument:F4: "Type
Instrument:G4: 'Complex
Inclination angle: 98°

Detector quantum efficiency: 0.6

Transmit beam intensity fraction: @VLOOKUP($GEOMETRY, $GEOMETRY_TYPES, 1)

Wavelength: 2.065479

Heterodyne efficiency: @VLOOKUP(GEOMETRY, GEOMETRY_TYPES, 2)

Pulse energy: 0.025

System efficiency: +ETA_HETERODYNE*TT

Pulse length: 0.5

Misalignment efficiency: +ALIGN_LOSS

Duty cycle: 0.05

P.R.F.: 10

Spectral width: +T_SPEC_WIDTH

Frequency: +C/LAMBDA

Telescope diameter: 0.25

Scan type: Wedge

Nadir angle: 30°

Plot duration: 1

Telescope rotation rate: 12

Telescope rotation rate: receive optics

Effective diameter: 0.9

Telescope rotation rate: effective diameter

Eiffel (SCAN_TYPE=‘Wedge’, +TSCOPE_D*@COS(@RADIANS($NADIR)), TSCOPE PE_D)
4.5 Results

The following code lists the cell contents of the results page. All of the cells are visible to the user.

```plaintext
<table>
<thead>
<tr>
<th>Results</th>
<th>B1: TARGET</th>
</tr>
</thead>
<tbody>
<tr>
<td>Results</td>
<td>F1: SIGNAL PROCESSING</td>
</tr>
<tr>
<td>Results</td>
<td>B2: Aerosol altitude</td>
</tr>
<tr>
<td>Results</td>
<td>C2: 300</td>
</tr>
<tr>
<td>Results</td>
<td>D2: ( \text{m} )</td>
</tr>
<tr>
<td>Results</td>
<td>F2: Line of sight range resolution</td>
</tr>
<tr>
<td>Results</td>
<td>G2: ( +\text{VERT}_\text{RANGE}/\cos(\text{RAD}^\text{DEG}^\text{NAD}) )</td>
</tr>
<tr>
<td>Results</td>
<td>H2: ( \text{m} )</td>
</tr>
<tr>
<td>Results</td>
<td>B3: backscatter (( \lambda ))</td>
</tr>
<tr>
<td>Results</td>
<td>C3: 4.9E-06</td>
</tr>
<tr>
<td>Results</td>
<td>D3: ( \text{m} / (\text{sr}) )</td>
</tr>
<tr>
<td>Results</td>
<td>F3: Observation time</td>
</tr>
<tr>
<td>Results</td>
<td>G3: ( +\text{LOS}_\text{RANGE}/2 / (C \cdot 10^{-6}) )</td>
</tr>
<tr>
<td>Results</td>
<td>H3: ( \text{us} )</td>
</tr>
<tr>
<td>Results</td>
<td>B4: Maximum horizontal velocity</td>
</tr>
<tr>
<td>Results</td>
<td>C4: 30</td>
</tr>
<tr>
<td>Results</td>
<td>D4: ( \text{m/s} )</td>
</tr>
<tr>
<td>Results</td>
<td>F4: Time between sample points</td>
</tr>
<tr>
<td>Results</td>
<td>G4: ( \lambda / \text{VMAXLOS} \cdot \text{IF}(\text{Instrument}: \text{G}4 = \text{Complex}, 4, 8) )</td>
</tr>
<tr>
<td>Results</td>
<td>H4: ( \text{us} )</td>
</tr>
<tr>
<td>Results</td>
<td>B5: Horizontal wind velocity uncertainty</td>
</tr>
<tr>
<td>Results</td>
<td>C5: 0</td>
</tr>
<tr>
<td>Results</td>
<td>D5: ( \text{m/s} )</td>
</tr>
<tr>
<td>Results</td>
<td>F5: Digitisation frequency</td>
</tr>
<tr>
<td>Results</td>
<td>G5: 1/( \text{TS} )</td>
</tr>
<tr>
<td>Results</td>
<td>H5: ( \text{MHz} )</td>
</tr>
<tr>
<td>Results</td>
<td>B6: Vertical wind velocity uncertainty</td>
</tr>
<tr>
<td>Results</td>
<td>C6: 0</td>
</tr>
<tr>
<td>Results</td>
<td>D6: ( \text{m/s} )</td>
</tr>
<tr>
<td>Results</td>
<td>F6: No. sample points/observatn.</td>
</tr>
<tr>
<td>Results</td>
<td>G6: ( +G3 / \text{TS} )</td>
</tr>
<tr>
<td>Results</td>
<td>B7: Wind variance between shots</td>
</tr>
<tr>
<td>Results</td>
<td>C7: 0</td>
</tr>
<tr>
<td>Results</td>
<td>D7: ( \text{m/s} )</td>
</tr>
<tr>
<td>Results</td>
<td>F7: ( \text{Phi} )</td>
</tr>
<tr>
<td>Results</td>
<td>G7: ( 10^{\text{SNR} / 10} \cdot \text{M} / \text{IF}(\text{Instrument}: \text{G}4 = \text{Complex}, 1, 2) )</td>
</tr>
<tr>
<td>Results</td>
<td>B8: Vertical range resolution</td>
</tr>
<tr>
<td>Results</td>
<td>C8: 1000</td>
</tr>
<tr>
<td>Results</td>
<td>D8: ( \text{m} )</td>
</tr>
<tr>
<td>Results</td>
<td>F8: Signal width</td>
</tr>
<tr>
<td>Results</td>
<td>G8: ( \sqrt{(0.1874 / \tau)^2 + ((\text{SIGMAC}_H / \sin(\text{RAD}^\text{DEG}^\text{NAD})) \cdot 2 / \lambda)^2 + ((\text{SIGMAC}_V / \cos(\text{RAD}^\text{DEG}^\text{NAD})) \cdot 2 / \lambda)^2} )</td>
</tr>
<tr>
<td>Results</td>
<td>H8: ( \text{MHz} )</td>
</tr>
<tr>
<td>Results</td>
<td>B9: Target nadir angle</td>
</tr>
<tr>
<td>Results</td>
<td>C9: ( \text{DEGREES}(\text{ORBH} \cdot 10^3 + \text{RE}) \cdot \sin(\text{RAD}^\text{DEG}^\text{NAD}) / (\text{RE} + \text{ALT}) )</td>
</tr>
<tr>
<td>Results</td>
<td>D9: ( \text{deg} )</td>
</tr>
<tr>
<td>Results</td>
<td>F9: ( \text{Omega} )</td>
</tr>
</tbody>
</table>
```

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Results: G9: \( +W \cdot G3 \)
Results: H9: \( 'm/s \)
Results: B10: "Line of sight range to this altitude
Results: C10: \( \sqrt{(\text{SOLBH} \cdot 10^3 + \text{SRE})^2 + (\text{SRE} + \text{ALT})^2 - (2 \cdot \text{SOLBH} \cdot 10^3 + 2 \cdot \text{SRE}) \cdot \cos(@\text{RADIANS}(\text{NADALT} - \text{NADIR}))} / 1000 \)
Results: D10: \( '\text{km} \)
Results: F10: "Coherence length
Results: C11: \( +C0HERENCE \)
Results: D11: \( 'm \)
Results: F11: "No. of shots/ wind estimate
Results: G11: 1
Results: F12: "Bandwidth (wide band)
Results: G12: \( 4 \cdot \text{VMAXLOS} / \text{LAMBDA} \)
Results: H12: \( '\text{MHz} \)
Results: B13: "One way Intensity Transmission
Results: C13: \( +\text{ETA_EXTINCT} \)
Results: F13: "Bandwidth (narrow band)
Results: G13: \( +W \)
Results: H13: \( '\text{MHz} \)
Results: B14: "Maximum line of sight velocity
Results: C14: \( +\text{VSEARCH} \cdot \sin(@\text{RADIANS}(\text{NADALT})) \)
Results: D14: \( '\text{m/s} \)
Results: F14: "MLE row no.
Results: G14: 6
Results: F19: "OTHER PARAMETERS
Results: F19: "RESULTS
Results: B20: "Satellite velocity
Results: C20: \( \sqrt{\text{G} \cdot \text{ME} / (\text{ORBH} \cdot 10^3 + \text{RE})} \)
Results: D20: \( '\text{m/s} \)
Results: F20: "Wideband SNR
Results: G20: \( 10^\*\log((\text{NRG} \cdot \text{TT} \cdot \text{TO} \cdot \text{ATTEN} \cdot \text{BETA} \cdot \pi \cdot \text{D}^2 \cdot \text{RO} \cdot \text{SYSTEM} \cdot \text{ETA_MISALIGN} \cdot \text{POLN} \cdot \text{QE} \cdot \text{C} \cdot \text{MARGIN}) / (8 \cdot \pi \cdot \text{FREQ} \cdot 10^6 \cdot \text{SGS12} \cdot 10^6 \cdot (\text{R} \cdot 1000) \cdot (1 + (\text{D}^2 \cdot \text{RHO0}))^2)) \)
Results: H20: \( '\text{dB} \)
Results: B21: "ground track velocity
Results: C21: \( \text{VSAT} \cdot \text{RE} / (\text{ORBH} \cdot 10^3 + \text{RE}) \)
Results: D21: \( '\text{m/s} \)
Results: F21: "Narrowband SNR
Results: G21: \( 10^\*\log(10^\*\text{SNR} / 10) + 2 \cdot \text{VMAXLOS} / (\text{LAMBDA} \cdot \text{W}) \)
Results: H21: \( '\text{dB} \)
Results: B22: "Earth rotation velocity at equator
Results: C22: \( 2 \cdot \pi \cdot \text{RE} / \text{TE} \)
Results: D22: \( '\text{m/s} \)
Results: F22: "(bad)
Results: G22: \( \text{ARRAY}((1 + (\text{PHI} + @\text{ML_Estimator:D} \cdot @\text{STRING(G14,0)})^\*@\text{ML_Estimator:E} \cdot @\text{STRING(G14,0)})) \)
Results: B23: "Slant range to ground
Results: C23: \( \sqrt{(\text{ORBH} \cdot 10^3 + \text{RE})^2 + \text{RE}^2 - (2 \cdot \text{ORBH} \cdot 10^3 + 2 \cdot \text{RE}) \cdot \cos(@\text{RADIANS}(\text{NADALT} - \text{NADIR}))} \)
Results: D23: \( 'm \)
Results: F23: "P(good)
Results: G23: 1 - PBAD
Results: B24: "Spot diameter on ground
Results: C24: \( 6 \cdot \text{SlantG} / (\pi \cdot (\text{LAMBDA} \cdot 10^6 - 6 \cdot \text{SLANTG}) \cdot (\text{PI} \cdot (\text{D}^2 / 2)^2) \) \)
Results: D24: \( 'm \)
Results: F24: "\text{sigmavlos - instrument}
Results: G24: \( \text{G10} \cdot \text{W} \cdot \text{LAMBDA} / 2 \)
Results: H24: \( '\text{m/s} \)
Results: B25: "Time for one orbit
Results: C25: \( 2 \cdot \pi \cdot \text{ORBH} \cdot 10^3 \cdot \text{RE} / \text{VSAT} \)
Results: D25: \( 's \)
Results: F25: "\text{sigmavlos}
Results: G25: \[
\sqrt{\frac{\text{SIGMAV}_I^2 + \text{SIGMAS}^2}{\text{NSHOTS}* (1-\text{PBAD})}} \]

Results: H25: 'm/s

Results: B26: "Swath radius (conical/wedge scan)"

Results: C26: \[
2*\text{RE}^*\text{RADIANS}*(\text{NADALT}-\text{NADIR})/2
\]

Results: D26: 'm

Results: F26: "F.O.M."

Results: G26: \[
\left(\frac{\text{ATTEN}^2}{\text{RE}^2}\right)\text{SIN}*(\text{RADIANS}*(\text{NADALT}))*10^6
\]

Results: B27: "Optimum mirror flip time (line scan)"

Results: C27: \[
\text{RE}/\text{VI}*\text{ASIN}*(\text{SLINTG}*(\text{SIN}*(\text{RADIANS}*(\text{NADIR} ))/\left(\sqrt{2}\right)*\text{RE})
\]

Results: D27: 's

Results: F27: "PHI"

Results: G27: +PHI

4.6 Scan pattern

The following code lists the contents of the Scan_Pattern page. The user sees two plots, one of the scan pattern and the other of the beam separation for the line scan pattern.

The following lines appear above the plots.

```plaintext
Scan_Pattern:A1: 'tstep
Scan_Pattern:B1: 1/(PLOTMINS*60/600)
Scan_Pattern:C1: 'Hz
Scan_Pattern:D1: 'Shot Pattern at Equator
Scan_Pattern:I1: 'Fore/Aft Look Separation Dependence on Latitude
```

The following line is visible to the user below the plots.

```plaintext
Scan_Pattern:I33: 'This plot is relevant to the half of 'BEST' shot pattern.'
```

The remaining lines are out of sight from the user and are used to calculate the scan pattern. The model assumes that the satellite starts from 0 deg. latitude and 0 deg. longitude. Columns B and C calculate the spacecraft latitude and longitude, column D calculates the telescope pointing angle with respect to the spacecraft velocity vector and, columns E and F calculate the position of the lidar beam on the ground (in km.) from the 0 deg. latitude, 0 deg. longitude position. Columns G and H calculate the beam separation for the line-scan pattern as a function of latitude. A total of 600 shot positions are calculated.

```plaintext
Scan_Pattern:B36: 'satellite track
Scan_Pattern:D36: 'angle
Scan_Pattern:B37: 'long
Scan_Pattern:C37: 'lat
Scan_Pattern:E37: 'long
Scan_Pattern:F37: 'lat
Scan_Pattern:G37: 'separation
Scan_Pattern:H37: 0
Scan_Pattern:B38: +SA38/TSTEP*$V1*$COS(@RADIANS(180-$ORBINC))/1000+SA38/
\$TSTEP*$VEARTH*$COS(@RADIANS($LATITUDE))/1000
Scan_Pattern:C38: +SA38/TSTEP*$V1*$SIN(@RADIANS(180-$ORBINC))/1000
Scan_Pattern:D38: @IF(@MOD(SA38/TSTEP,STORBIT)>STORBIT*$DUTY,0,@IF($SCAN_-
FLAG=1,**$RPM*SA38/TSTEP**0,0,0,0,0,0,0),0,@RA-
DIANS(135),@RADIANS(45)))
Scan_Pattern:E38: +SA38/STSTEP*$V1*$COS($PI-$RADIANS($ORBINC)+$D38)/1000
Scan_Pattern:F38: +SC38/$SRSWATH*$SIN($PI+$RADIANS($ORBINC)+$D38)/1000
Scan_Pattern:G38: 0
Scan_Pattern:H38: +$VEARTH*$STFLIP*$COS($RADIANS($G38))/1000
```

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The lines A40 - H40 are repeated, with column A being incremented by 1 each row and column G being incremented by 5 each row down to the following rows:

This completes the line-scan beam separation calculation and from this point only the shot pattern calculation is repeated until:

This line-scan beam separation calculation and from this point only the shot pattern calculation is repeated until:
4.7 Extinction

The following is a list of the code on the Extinction page. The user sees a plot of the one-way and two-way transmission of the atmosphere over the altitude range 0-20 km. The following lines are visible to the user beneath the plot.

Extinction:D33: 'Optical transmission from satellite to target, laser wavelength is
Extinction:K33: +LAMBDA
Extinction:L33: 'um

The following lines are not visible to the user and are used to calculate the the one-way and two-way atmospheric extinction. Column A contains the altitude above the earth's surface (incremented in 0.1 km steps), column C contains the nadir angle at that altitude (accounting for the earth's curvature), column D contains the range from the satellite to the altitude and column E the path length from one altitude increment to the next. Column F contains the atmospheric extinction at the current altitude, column G the product of the path length and extinction, column H the summation of the path length/extinction products from the spacecraft to the current altitude. Column I contains the one-way extinction to the altitude and column J the two-way extinction.

Extinction:A36: 'Altitude
Extinction:B36: 'Index
Extinction:C36: 'Nadaltl
Extinction:D36: 'range
Extinction:E36: 'path
Extinction:F36: +LAMBDA
Extinction:G36: "lamda*pathl
Extinction:I36: 'One Way
Extinction:J36: 'Two Way
Extinction:A37: 0
Extinction:B37: 1
Extinction:C37: @DEGREES(@ASIN((ORBH*10^3+RE)*@SIN(@RADIANS(NADIR))/(RE+ALTITUDE*1000)))
Extinction:D37: @SQRT((ORBH*10^3+RE)^2+(RE+ALTITUDE*1000)^2-2*ORBH*10^3+2*RE)*(RE+ALTITUDE*1000)*@COS(@RADIANS(NADALT1-$NADIR)))/1000
Extinction:E37: 0
Extinction:F37: @HLOOKUP($LAMBDA, [\QPW\LIDAR\ATMOS\$MLS_CLEAR, $B37]
Extinction:G37: 0
Extinction:H37: @SUM($G37..$G$237)
Extinction:I37: @EXP(-H37)
Extinction:J37: ÷I37^2
Extinction:A38: 0.1
Extinction:B38: 2
Extinction:C38: \( \text{DEGREES} \left( \text{ASIN} \left( \text{ORBH} \times 10^3 + \text{RE} \right) \times \text{SIN} \left( \text{RADIANS} \left( \text{NADIR} \right) \right) / \left( \text{RE} + \text{SA38} \times 1000 \right) \right) \)

Extinction:D38: \( \text{SQRT} \left( (\text{ORBH} \times 10^3 + \text{RE})^2 + (\text{RE} + \text{SA38} \times 1000)^2 - (2 \times \text{ORBH} \times 10^3 + 2 \times \text{RE}) \times (\text{RE} + \text{SA38} \times 1000) \times \text{COS} \left( \text{RADIANS} \left( \text{SC38} - \text{NADIR} \right) \right) \right) / 1000 \)

Extinction:E38: \(+\text{RANGE} - \text{D38} \)

Extinction:F38: \( \text{HLOOKUP} \left( \text{SLAMBDA}, \left[ \text{QPW} \text{\& LIDAR\& ATMOS} \right] \text{MLS\_CLEAR}, \text{B38} \right) \)

Extinction:G38: \(+\text{E38} \times \text{F38} \)

Extinction:H38: \( \text{SUM} \left( \text{G38}..\text{G237} \right) \)

Extinction:I38: \( \text{EXP} \left( -\text{H38} \right) \)

Extinction:J38: \( +\text{I38}^2 \)

A38 - J38 are repeated (with suitable incrementing) until:

Extinction:A236: 19.9

Extinction:B236: 200

Extinction:C236: \( \text{DEGREES} \left( \text{ASIN} \left( \text{ORBH} \times 10^3 + \text{RE} \right) \times \text{SIN} \left( \text{RADIANS} \left( \text{NADIR} \right) \right) / \left( \text{RE} + \text{SA236} \times 1000 \right) \right) \)

Extinction:D236: \( \text{SQRT} \left( (\text{ORBH} \times 10^3 + \text{RE})^2 + (\text{RE} + \text{SA236} \times 1000)^2 - (2 \times \text{ORBH} \times 10^3 + 2 \times \text{RE}) \times (\text{RE} + \text{SA236} \times 1000) \times \text{COS} \left( \text{RADIANS} \left( \text{SC236} - \text{NADIR} \right) \right) \right) / 1000 \)

Extinction:E236: \(+\text{SD235} - \text{D236} \)

Extinction:F236: \( \text{HLOOKUP} \left( \text{SLAMBDA}, \left[ \text{QPW}\&\text{\& LIDAR}\&\text{\& ATMOS} \right] \text{MLS\_CLEAR}, \text{B236} \right) \)

Extinction:G236: \(+\text{SE236} \times \text{SF236} \)

Extinction:H236: \( \text{SUM} \left( \text{SG236..SG237} \right) \)

Extinction:I236: \( \text{EXP} \left( -\text{H236} \right) \)

Extinction:J236: \(+\text{I236}^2 \)

Extinction:A237: 20

Extinction:B237: 201

Extinction:C237: \( \text{DEGREES} \left( \text{ASIN} \left( \text{ORBH} \times 10^3 + \text{RE} \right) \times \text{SIN} \left( \text{RADIANS} \left( \text{NADIR} \right) \right) / \left( \text{RE} + \text{SA237} \times 1000 \right) \right) \)

Extinction:D237: \( \text{SQRT} \left( (\text{ORBH} \times 10^3 + \text{RE})^2 + (\text{RE} + \text{SA237} \times 1000)^2 - (2 \times \text{ORBH} \times 10^3 + 2 \times \text{RE}) \times (\text{RE} + \text{SA237} \times 1000) \times \text{COS} \left( \text{RADIANS} \left( \text{SC237} - \text{NADIR} \right) \right) \right) / 1000 \)

Extinction:E237: \(+\text{SD237} - \text{D237} \)

Extinction:F237: \( \text{HLOOKUP} \left( \text{SLAMBDA}, \left[ \text{QPW}\&\text{\& LIDAR}\&\text{\& ATMOS} \right] \text{MLS\_CLEAR}, \text{B237} \right) \)

Extinction:G237: \(+\text{SE237} \times \text{SF237} \)

Extinction:H237: \( \text{SUM} \left( \text{SG237..SG237} \right) \)

Extinction:I237: \( \text{EXP} \left( -\text{H237} \right) \)

Extinction:J237: \(+\text{I237}^2 \)

The following lines set up a search criteria and locate the extinction value for the altitude of interest (entered on the Results page).

Extinction:A241: ‘Search Criteria
Extinction:C241: ‘Result
Extinction:A242: ‘Altitude
Extinction:C242: ‘Result
Extinction:A243: ‘ALTITUDE
Extinction:C243: ‘(ALTITUDE/1000)
Extinction:C245: ‘This page searches the extinction database to find the altitudes that are greater
Extinction:C246: ‘than the target altitude. The values of extinction for the path length through each
Extinction:C247: ‘0.1 km altitude band up to 20 km are summed. The value
Extinction:C248: ‘obtained is the value of
Extinction:C249: ‘(alpha\*path length) which is used to calculate the one way
Extinction:C250: ‘extinction through
Extinction:C251: ‘the atmosphere.

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### 4.8 Coherence length

The following code lists the contents of the cells on the page CoherenceL. The user sees a plot of the WPL-37 $C_n^2$ profile and a plot of the transverse coherence length as a function of altitude from the earth's surface. Column A contains the altitude, column B the nadir angle at that altitude, column C the range from the satellite to that altitude and column D the path length through an altitude increment. Column E calculates the refractive index structure function, $C_n^2$ at the altitude and columns F and G calculate the transverse coherence length.

<table>
<thead>
<tr>
<th>Column</th>
<th>Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>A36</td>
<td><code>Altitude1</code></td>
</tr>
<tr>
<td>B36</td>
<td><code>Nadir2</code></td>
</tr>
<tr>
<td>C36</td>
<td><code>range2</code></td>
</tr>
<tr>
<td>D36</td>
<td><code>path2</code></td>
</tr>
<tr>
<td>E36</td>
<td><code>Cn2</code></td>
</tr>
<tr>
<td>A37</td>
<td>0</td>
</tr>
<tr>
<td>B37</td>
<td><code>@DEGREES(0ASIN((ORBH*10^3+RE)*0SIN(0RADIANS(NADIR))/(RE+ALTITUDE1^1000)))</code></td>
</tr>
<tr>
<td>C37</td>
<td><code>@SQRT((SORBH*10^3+RE)^2+(RE+ALTITUDE1*1000)^2-(2*SORBH*10^3+2*RE)^2*(RE+ALTITUDE1*1000)*0COS(0RADIANS(NADALT2-NADIR))/1000)</code></td>
</tr>
<tr>
<td>D37</td>
<td>0</td>
</tr>
<tr>
<td>E37</td>
<td><code>@IF(ALTITUDE1&gt;20,0,0IF(ALTITUDE1&lt;0.01,7.36*10^-14,0IF(ALTITUDE1&lt;3,1.59*10^-12*(ALTITUDE1*1000)^(-4/3),3.66*10^-17)))</code></td>
</tr>
<tr>
<td>F37</td>
<td><code>@IF(RANGE2&gt;$R,0,PATH2*10^3*CN2*(1-RANGE2/$R)^((5/3))</code></td>
</tr>
<tr>
<td>G37</td>
<td><code>((HCOHERENCE*(2*0PI/(0LAMBDA*10^-6))^2)*SUM(F37..0F$237))^-3/5</code></td>
</tr>
<tr>
<td>A38</td>
<td>0.1</td>
</tr>
<tr>
<td>B38</td>
<td><code>@DEGREES(0ASIN((ORBH*10^3+RE)*0SIN(0RADIANS(NADIR))/(RE+SA38*1000)))</code></td>
</tr>
<tr>
<td>C38</td>
<td><code>@SQRT((SORBH*10^3+RE)^2+(RE+SA38*1000)^2-(2*SORBH*10^3+2*RE)^2*(RE+SA38*1000)*0COS(0RADIANS(0S38-0NADIR))/1000)</code></td>
</tr>
<tr>
<td>D38</td>
<td><code>+5C37-5C38</code></td>
</tr>
<tr>
<td>E38</td>
<td><code>@IF(SA38&gt;20,0,0IF(SA38&lt;0.01,7.36*10^-14,0IF(SA38&lt;3,1.59*10^-12*(SA38*1000)^(-4/3),3.66*10^-17)))</code></td>
</tr>
<tr>
<td>F38</td>
<td><code>@IF(SC38&gt;$R,0,SD38*10^3*SE38*(1-SC38/$R)^((5/3))</code></td>
</tr>
<tr>
<td>G38</td>
<td><code>((HCOHERENCE*(2*0PI/(0LAMBDA*10^-6))^2)*SUM(F38..0F$237))^-3/5</code></td>
</tr>
<tr>
<td>A39</td>
<td>0.2</td>
</tr>
<tr>
<td>B39</td>
<td><code>@DEGREES(0ASIN((ORBH*10^3+RE)*0SIN(0RADIANS(NADIR))/(RE+SA39*1000)))</code></td>
</tr>
<tr>
<td>C39</td>
<td><code>@SQRT((SORBH*10^3+RE)^2+(RE+SA39*1000)^2-(2*SORBH*10^3+2*RE)^2*(RE+SA39*1000)*0COS(0RADIANS(0S39-0NADIR))/1000)</code></td>
</tr>
<tr>
<td>D39</td>
<td><code>+5C38-5C39</code></td>
</tr>
<tr>
<td>E39</td>
<td><code>@IF(SA39&gt;20,0,0IF(SA39&lt;0.01,7.36*10^-14,0IF(SA39&lt;3,1.59*10^-12*(SA39*1000)^(-4/3),3.66*10^-17)))</code></td>
</tr>
<tr>
<td>F39</td>
<td><code>@IF(SC39&gt;$R,0,SD39*10^3*SE39*(1-SC39/$R)^((5/3))</code></td>
</tr>
<tr>
<td>G39</td>
<td><code>((HCOHERENCE*(2*0PI/(0LAMBDA*10^-6))^2)*SUM(F39..0F$237))^-3/5</code></td>
</tr>
</tbody>
</table>

A39 - G39 are repeated (with suitable increments) until:

<table>
<thead>
<tr>
<th>Column</th>
<th>Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>A236</td>
<td>19.9</td>
</tr>
<tr>
<td>B236</td>
<td><code>@DEGREES(0ASIN((ORBH*10^3+RE)*0SIN(0RADIANS(NADIR))/(RE+SA236*1000)))</code></td>
</tr>
<tr>
<td>C236</td>
<td><code>@SQRT((SORBH*10^3+RE)^2+(RE+SA236*1000)^2-(2*SORBH*10^3+2*RE)^2*(RE+SA236*1000)*0COS(0RADIANS(0S236-0NADIR))/1000)</code></td>
</tr>
<tr>
<td>D236</td>
<td><code>+5C235-5C236</code></td>
</tr>
<tr>
<td>E236</td>
<td><code>@IF(SA236&gt;20,0,0IF(SA236&lt;0.01,7.36*10^-14,0IF(SA236&lt;3,1.59*10^-12*(SA236*1000)^(-4/3),3.66*10^-17)))</code></td>
</tr>
<tr>
<td>F236</td>
<td><code>@IF(SC236&gt;$R,0,SD236*10^3*SE236*(1-SC236/$R)^((5/3))</code></td>
</tr>
</tbody>
</table>

Lidar Performance Analysis 51
The following lines set up a search criteria table and determine the refractive structure function at the altitude of interest given on the Results page.

```

CoherenceL:A239: 'Search Criteria
CoherenceL:A240: 'Altitude
CoherenceL:C240: 'Result
CoherenceL:A241: +ALTITUDEI>=$ALT/1000
CoherenceL:C241: ($HCOHERENCE*(2*@PI/(SLAMDBA*10^(-6)))^2*DSUM(WPL37-DAT,5,A240..A241))^(-3/5)
```

### 4.9 Alignment

The following code lists the contents of the Alignment page. The user sees a plot of loss due to misalignment. Columns A and B contain a parameterised misalignment loss curve. Column B contains the misalignment loss as a function of the parameter, αD (π/λ) where α is the misalignment angle between the signal and BPLO, D is the optical beam diameter and λ is the lidar operating wavelength. Cells D37 - E44 contain a search table to find the two values of αD (π/λ) which straddle the misalignment angle given on the Instrument page. A linear interpolation between these two values is then performed to obtain the misalignment loss. Columns L and M contain the misalignment loss (column M) as a function of angle (column L) for the wavelength given on the Instrument page. These are the values plotted in the graph shown on this page.
This page searches the misalignment database to find the values that straddle the angular misalignment. A linear interpolation is then used between these two points to determine the misalignment loss. The use of a linear interpolation
The formulae in columns A,B,L and M are repeated until the data for the plot (columns L and M) are completed:-

```
Alignment:A156: 19.5
Alignment:B156: 0.00023224357861854
Alignment:L156: +A156*$LAMBDA/(@PI*$D)
Alignment:M156: 1-B156
Alignment:A157: 20
Alignment:B157: 0.0002147988979521
Alignment:L157: +A157*$LAMBDA/(@PI*$D)
Alignment:M157: 1-B157
```

The remaining rows then contain the rest of the misalignment look-up table until:-

```
Alignment:A172: 95
Alignment:B172: 1.95731733773E-06
Alignment:A173: 100
Alignment:B173: 1.67746225269E-06
```

**4.10 Performance**

The Perf page contains two plots, one of the wideband and narrowband SNR as a function of backscatter and one of the velocity error and probability of correct detection as a function of backscatter. The SNR plot contains a button which causes these graphs to be updated. The data for these plots is generated by the macro given in and is placed in cells A36 E59. Column A contains the backscatter value, B/C the wideband and narrowband SNR respectively and D and E contain the probability of a good estimate and the velocity error respectively.

Unlike the other plots which update themselves automatically when one of the relevant lidar parameters changes, these plots only update when the user clicks on the “Update Graphs” button. This will be discussed later.

This is the last page of direct relevance to the casual user - the remaining pages contain coding and although currently visible to the user they could be made invisible to prevent accidental alteration.

**4.11 Constants**

The following code lists the contents of the cells on the Constants page:-
4.12 Maximum likelihood estimator

This page contains a look-up table for the maximum likelihood estimator. The table is shown below together with the column and row assignments.

<table>
<thead>
<tr>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>F</th>
<th>G</th>
<th>H</th>
<th>I</th>
<th>J</th>
<th>K</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Omega M b0 alpha gamma chi g0 epsilon delta mu</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>20</td>
<td>4.6308</td>
<td>1.1923</td>
<td>1.2535</td>
<td>0.9145</td>
<td>6.2318</td>
<td>1.3798</td>
<td>0.5307</td>
</tr>
<tr>
<td>3</td>
<td>1</td>
<td>25</td>
<td>6.6127</td>
<td>1.1843</td>
<td>1.573</td>
<td>0.887</td>
<td>4.3866</td>
<td>2.2939</td>
<td>0.2345</td>
</tr>
<tr>
<td>4</td>
<td>3</td>
<td>30</td>
<td>9.6148</td>
<td>1.18</td>
<td>2.0453</td>
<td>0.9001</td>
<td>3.5357</td>
<td>3.1954</td>
<td>0.1401</td>
</tr>
<tr>
<td>5</td>
<td>3</td>
<td>35</td>
<td>13.067</td>
<td>1.1495</td>
<td>2.5687</td>
<td>0.8758</td>
<td>4.2848</td>
<td>2.5322</td>
<td>0.2026</td>
</tr>
<tr>
<td>6</td>
<td>3</td>
<td>40</td>
<td>14.003</td>
<td>1.1862</td>
<td>2.7099</td>
<td>0.8854</td>
<td>3.5066</td>
<td>4.0879</td>
<td>0.1054</td>
</tr>
<tr>
<td>7</td>
<td>6.7</td>
<td>20</td>
<td>0.2318</td>
<td>4.0951</td>
<td>0.0196</td>
<td>0.2138</td>
<td>17.454</td>
<td>1.1469</td>
<td>0.8738</td>
</tr>
<tr>
<td>8</td>
<td>6.7</td>
<td>25</td>
<td>0.7783</td>
<td>5.6302</td>
<td>0.0499</td>
<td>0.5362</td>
<td>19.252</td>
<td>0.9637</td>
<td>1.2103</td>
</tr>
<tr>
<td>9</td>
<td>6.7</td>
<td>30</td>
<td>2.2702</td>
<td>1.5914</td>
<td>0.4216</td>
<td>0.7402</td>
<td>12.063</td>
<td>1.1882</td>
<td>0.8432</td>
</tr>
<tr>
<td>10</td>
<td>6.7</td>
<td>35</td>
<td>5.7615</td>
<td>1.1484</td>
<td>1.1356</td>
<td>0.8928</td>
<td>9.3993</td>
<td>1.2744</td>
<td>0.708</td>
</tr>
<tr>
<td>11</td>
<td>6.7</td>
<td>40</td>
<td>9.832</td>
<td>1.0981</td>
<td>1.8154</td>
<td>0.9536</td>
<td>7.7512</td>
<td>1.4531</td>
<td>0.544</td>
</tr>
</tbody>
</table>

4.13 Lists

This page contains small look-up tables used by the program. The tables are shown below, together with their row/column assignments. The first table is a list of wavelengths for which there are entries in the extinction database spreadsheet, ATMOS.WB1. This table appears as the pick list in the laser wavelength entry box.
The following table lists the available receiver geometries and their beam truncation factors.

<table>
<thead>
<tr>
<th></th>
<th>A</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2.012552</td>
</tr>
<tr>
<td>2</td>
<td>2.021842</td>
</tr>
<tr>
<td>3</td>
<td>2.065479</td>
</tr>
<tr>
<td>4</td>
<td>2.091282</td>
</tr>
<tr>
<td>5</td>
<td>9.1145187</td>
</tr>
<tr>
<td>6</td>
<td>9.21969</td>
</tr>
<tr>
<td>7</td>
<td>9.249946</td>
</tr>
<tr>
<td>8</td>
<td>10.591043</td>
</tr>
</tbody>
</table>

This small table is used in the receiver selection box to choose between complex and real receiver geometries (this affects the signal processing).

<table>
<thead>
<tr>
<th></th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>F</th>
<th>G</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Geometry</td>
<td>Tt</td>
<td>etah</td>
<td>gamma</td>
<td>gammat</td>
</tr>
<tr>
<td>2</td>
<td>Wang</td>
<td>0.955</td>
<td>0.42</td>
<td>0.802</td>
<td>0.802</td>
</tr>
<tr>
<td>3</td>
<td>Matched Rye</td>
<td>0.929</td>
<td>0.457</td>
<td>0.87</td>
<td>0.87</td>
</tr>
<tr>
<td>4</td>
<td>Unmatched Rye</td>
<td>0.951</td>
<td>0.461</td>
<td>1.186</td>
<td>0.815</td>
</tr>
</tbody>
</table>

The next table lists the available scanning options and is used by the scanner input dialog.

<table>
<thead>
<tr>
<th></th>
<th>I</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Complex</td>
</tr>
<tr>
<td>2</td>
<td>Real</td>
</tr>
</tbody>
</table>

The next table lists the available scanning options and is used by the scanner input dialog.
4.14 Macros

The following table is a coded macro to calculate and plot the performance plots (Section 4.10). It is executed when the user clicks on the “Update Graphs” button on the SNR plot. Column A contains variable names and labels, column B contains the actual coding or the variable contents and column J contains comments on the macro steps.

<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>J</th>
</tr>
</thead>
<tbody>
<tr>
<td>THIS MACRO RECALCULATES THE INSTRUMENT PERFORMANCE AS A FUNCTION OF BACKSCATTER</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>AND UPDATES THE PERFORMANCE GRAPHS SO THAT ONLY PERFORMANCE FOR VALUES OF PROBABILITY &gt; min_prob ARE PLOTTED. THIS IS BECAUSE THE VELOCITY ESTIMATION THEORY IS UNCERTAIN FOR PROBABILITIES LESS THAN THIS. IN PRACTICE IT IS UNLIKELY A LIDAR OF SUCH POOR SINGLE SHOT PERFORMANCE WOULD BE BUILT!</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>save_beta</td>
<td>1E-06</td>
<td></td>
</tr>
<tr>
<td>beta_count</td>
<td>24</td>
<td></td>
</tr>
<tr>
<td>min_beta_point</td>
<td>50</td>
<td></td>
</tr>
<tr>
<td>min_prob</td>
<td>0.2</td>
<td></td>
</tr>
<tr>
<td>perform_calc</td>
<td>{EDITGOTO perform:A1}{LET $save_beta, $BETA}</td>
<td>Store beta value</td>
</tr>
<tr>
<td></td>
<td>{FOR beta_count,0.23,1,beta_calc}</td>
<td>Repetitive calculation loop, increments beta value pointer</td>
</tr>
<tr>
<td></td>
<td>{LET $BETA,$save_beta}</td>
<td>Restore beta to original value</td>
</tr>
</tbody>
</table>

Dual-look

Conical

Wedge
<table>
<thead>
<tr>
<th>A</th>
<th>B</th>
<th>J</th>
</tr>
</thead>
<tbody>
<tr>
<td>16</td>
<td>(WINDOWSOFF) (GraphEdit SNR)</td>
<td>Turn window updating off and edit the SNR graph</td>
</tr>
<tr>
<td>17</td>
<td>[SERIES.Data_Range 1, +&quot;Perform:B&quot; &amp; @ STRING(min_beta_point,0) &amp; &quot;,..B59&quot;)</td>
<td>Change graph series to match new performance</td>
</tr>
<tr>
<td>18</td>
<td>[SERIES.Data_Range 2, +&quot;Perform:C&quot; &amp; @ STRING(min_beta_point,0) &amp; &quot;,..C59&quot;)</td>
<td>Only performance for values of probability &gt; 0.2 are plotted</td>
</tr>
<tr>
<td>19</td>
<td>[SERIES.Data_Range &quot;XAxisLabelSeries&quot;, +&quot;Perform:A&quot; &amp; @ STRING(min_beta_point,0) &amp; &quot;,..A59&quot;)</td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>(Series.Go) (WindowClose)</td>
<td>Instigate graph changes and close edit window</td>
</tr>
<tr>
<td>21</td>
<td>(GraphEdit Vel_error)</td>
<td>Edit velocity error/probability graph</td>
</tr>
<tr>
<td>22</td>
<td>[SERIES.Data_Range 1, +&quot;Perform:E&quot; &amp; @ STRING(min_beta_point,0) &amp; &quot;,..E59&quot;)</td>
<td>Change graph series to match new performance</td>
</tr>
<tr>
<td>23</td>
<td>[SERIES.Data_Range 2, +&quot;Perform:D&quot; &amp; @ STRING(min_beta_point,0) &amp; &quot;,..D59&quot;)</td>
<td>Only performance values for probability &gt; 0.2 are plotted</td>
</tr>
<tr>
<td>24</td>
<td>[SERIES.Data_Range &quot;XAxisLabelSeries&quot;, +&quot;Perform:A&quot; &amp; @ STRING(min_beta_point,0) &amp; &quot;,..A59&quot;)</td>
<td></td>
</tr>
<tr>
<td>25</td>
<td>(Series.Go) (WindowClose)</td>
<td>Instigate graph changes and close edit window</td>
</tr>
<tr>
<td>26</td>
<td></td>
<td></td>
</tr>
<tr>
<td>27</td>
<td>beta_calc = BETA, @INDEX(performance,0,beta_- count)</td>
<td>Set beta to value in performance table</td>
</tr>
<tr>
<td>28</td>
<td>(CALC)</td>
<td>Calculate performance</td>
</tr>
<tr>
<td>29</td>
<td>[LET +&quot;perform:B&quot; &amp; @ STRING(beta_- count+36,0),snr_wide]</td>
<td>Store wideband SNR in performance table</td>
</tr>
<tr>
<td>30</td>
<td>[LET +&quot;perform:C&quot; &amp; @ STRING(beta_- count+36,0),snr_narrow]</td>
<td>Store narrow band SNR in performance table</td>
</tr>
<tr>
<td>31</td>
<td>[LET +&quot;perform:D&quot; &amp; @ STRING(beta_- count+36,0),pgood]</td>
<td>Store probability of good estimate in performance table</td>
</tr>
<tr>
<td>32</td>
<td>[LET +&quot;perform:E&quot; &amp; @ STRING(beta_count+36,0),sigmav_i]</td>
<td>Store velocity error in performance table</td>
</tr>
<tr>
<td>33</td>
<td>[IF pgood&lt;min_prob] [LET min_beta_point,(beta_count+36)]</td>
<td>If probability is &lt; 0.2 increment minimum beta pointer.</td>
</tr>
</tbody>
</table>
4.15 Other pages

The spreadsheet also contains two other pages - Messages and Block Names. The Messages page will contain help messages which are accessible to the user (not currently implemented) whilst the Block Names page contains a tabulation of the variable names assigned to cell locations. This page is not required for operation of the program but is included to assist in the further development of the program.

5.1 Program structure

Program EYES92 - main routine, allows user to select the MPE (Maximum Permissible Exposure) as :-

- a function of wavelength for a fixed pulse length or
- a function of pulse length for a fixed wavelength or
- a function of velocity resolution over a wavelength range (approximation).

The program saves the results to the data file mpevsl.dat (mpe vs wavelength) or mpevst.dat (mpe vs. pulse length). The output is in two columns, the first contains the variable (pulse length (s) or wavelength (μm)) and the second contains the MPE (J/cm²).

Function MPE92(LB,T) - is the function that calculates the MPE for a given wavelength, LB in microns and a given pulse length, T in seconds. Called by the main program.

Subroutine CLRSCRN(I) - is a utility subroutine that scrolls the output screen by I lines. Called by the main program.

5.2 Program code

5.2.1 Program EYES92

```fortran
PROGRAM EYES92
IMPLICIT NONE
REAL*4 RESL,MIN,MAX,STEP,VAL,RESULT,LB,TP,MPE92,T
INTEGER*2 OPTION
CHARACTER*11 FILNAM
CALL CLRSCRN(40)
WRITE(*,*),' 1992 ANSI STANDARD EYE SAFETY CALCULATIONS'
WRITE(*,*) 'Gary D. Spiers'
WRITE(*,*) 'Center for Applied Optics'
WRITE(*,*) 'University of Alabama in Huntsville'
WRITE(*,*) 'Huntsville'
WRITE(*,*) 'AL 35899'
WRITE(*,*) '(205) 895 6030 ext. 448'
WRITE(*,*) 'This program calculates the maximum permissible'
WRITE(*,*) 'exposure (MPE) in J/cm^2 for direct ocular exp-
WRITE(*,*) 'osure, intrabeam viewing to a laser beam. The '
WRITE(*,*) 'valid wavelength range is 0.4-1000 microns and'
WRITE(*,*) 'the valid pulse durations (half amplitude po-
WRITE(*,*) 'ints) are ins to 3000s. Pulses shorter than ins'
WRITE(*,*) 'are treated as ins pulses at present due to '
WRITE(*,*) 'inadequate safety data. All calculations are '
WRITE(*,*) 'based on the ANSI Standard Z136.1-1992.'
WRITE(*,*) 'Type the return key to continue'
```
CALL CLRSCRN(40)

100 WRITE(*,*), 'Three options are available:'
WRITE(*,*) '1) MPE as a function of wavelength for a ' fixed pulse length.' OR'
WRITE(*,*) '2) MPE as a function of pulse length for a ' fixed wavelength.' OR'
WRITE(*,*) '3) MPE as a function of velocity resolution over a wavelength range.'
WRITE(*,*) 'ENTER OPTION NUMBER:'
READ(*,*) OPTION
WRITE(*,*)
IF ((OPTION .NE. 1) .AND. (OPTION .NE. 2) .AND. (OPTION .NE. 3)) THEN
WRITE(*,*) 'Please use a valid option number!!!!'
GOTO 100
ELSIF (OPTION .EQ. 1) THEN
WRITE(*,*) 'ENTER PULSE LENGTH (MICROSECONDS):-' READ(*,*) TP
T=TP*0.00000001
IF ( T .LT. 1E-9) THEN
WRITE(*,*) 'Pulse length set to 1ns.' T =1E-9
ENDIF
IF (T .GT. 3000) THEN
WRITE(*,*) 'Pulse length set to 3000s.' T =3000
ENDIF
ELSIF (OPTION .EQ. 2) THEN
130 WRITE(*,*) 'ENTER WAVELENGTH (MICRONS):-' READ(*,*) LB
IF ((LB .LT. 0.4) .OR. (LB .GT. 1000)) THEN
WRITE(*,*) 'The wavelength must be in the range 0.4-1000 microns.'
GOTO 130
ENDIF
140 WRITE(*,*) 'ENTER THE MINIMUM AND MAXIMUM PULSE LENGTHS OF INTEREST (microseconds):-' READ(*,*) MIN,MAX
IF ((MIN .LT. 0.001) .OR. (MAX .GT. 3000) .OR. (MAX .LT. MIN)) THEN
WRITE(*,*) 'Please provide valid values in the range 0.001 to 3000 microseconds!'
GOTO 140
ENDIF
ELSIF (OPTION .EQ. 3) THEN
150 WRITE(*,*) 'ENTER VELOCITY RESOLUTION (m/s):-' READ(*,*) RESL
IF (RESL .LE. 0.0) THEN
WRITE(*,*) 'The velocity resolution must be a positive number.'
GOTO 150
ENDIF
ENDIF
IF (OPTION .NE. 2) THEN
WRITE(*,*)
WRITE(*,*) 'Now set up wavelength range of interest.' WRITE(*,*) 'Wavelength increment is 5nm.'
200 WRITE(*,*)
WRITE(*,*) 'ENTER MINIMUM AND MAXIMUM WAVELENGTH'
WRITE(*,*) '(MICRONS): -'
READ(*,*) MIN, MAX
WRITE(*,*)
IF (MIN.LT.0.4) .OR. (MAX.GT.1000) .OR. (MAX.LT.MIN)) THEN
WRITE(*,*) 'Please provide valid values in the range'
WRITE(*,*) '0.4 to 1000 microns!!!!'
GOTO 200
ENDIF
WRITE(*,*) 'The data will be written to the file mpevsl.dat.'
FILNAM='mpevsl.dat'
ELSEIF (OPTION .EQ. 2) THEN
WRITE(*,*) 'The data will be written to the file mpevst.dat.'
WRITE(*,*) 'The pulse length increment is 5 ns.'
FILNAM='mpevst.dat'
ENDIF
OPEN(I, FILE=FILNAM)
STEP=0.005
DO 300 VAL = MIN, MAX, STEP
IF (OPTION .EQ. 1) THEN
LB=VAL
ELSEIF (OPTION .EQ. 2) THEN
T=VAL*0.000001
ELSEIF (OPTION .EQ. 3) THEN
LB=VAL
T=LB*1E-6/(2*RESL)
ENDIF
RESULT=MPE92(LB,T)
IF (OPTION NE. 2) THEN
WRITE(I,*) LB,RESULT
ELSEIF (OPTION .EQ. 2) THEN
WRITE (I,*) T,RESULT
ENDIF
CONTINUE
STOP
END

5.2.2 Function MPE92

REAL*4 FUNCTION MPE92(LB,T)
REAL*4 CA,CB,T1, LB, CC, T
C
IF ((LB .GE. 0.4) .AND. (LB .LT. 0.7)) THEN
CA=1
ELSEIF ((LB .GE. 0.7) .AND. (LB .LT. 1.05)) THEN
CA=10**(2.0*(LB-0.7))
ELSEIF ((LB .GE. 1.05) .AND. (LB .LT. 1.4)) THEN
CA=5
ENDIF
C
IF ((LB .GE. 0.4) .AND. (LB .LT. 0.55)) THEN
CB=1
ELSEIF ((LB .GE. 0.55) .AND. (LB .LE. 0.7)) THEN
CB=10**(15*(LB-0.55))
ENDIF
C
IF ((LB .GT. 1.05) .AND. (LB .LE. 1.15)) THEN
CC=1.0
ELSEIF ((LB .GT. 1.15) .AND. (LB .LE. 1.2)) THEN
CC=10**(18*(LB-1.15))
ELSEIF ((LB .GT. 1.2) .AND. (LB .LE. 1.4)) THEN
ENDIF
CC = 8
ENDIF

IF ((LB .GE. 0.55) .AND. (LB .LE. 0.7)) THEN
  T1 = 10^10**(20*(LB-0.55))
ENDIF

IF (LB .LE. 0.7) THEN
  IF (T .LE. 1.8E-5) THEN
    MPE92 = 5E-7
  ELSEIF ((T .GT. 1.8E-5) .AND. (T .LE. 1E4)) THEN
    MPE92 = 1.8*T**0.75*1E-3
  ELSEIF ((LB .LT. 0.55) .AND. (T .LE. T1) .AND. (T .LE. 1E4)) THEN
    MPE92 = 0.01
  ELSEIF ((LB .GT. 0.55) .AND. (T .LT. T1) .AND. (T .LE. 1E4)) THEN
    MPE92 = 5*CB*0.001
  ELSEIF ((LB .GT. 0.55) .AND. (T .GT. T1) .AND. (T .LE. 1E4)) THEN
    MPE92 = 0.01
  ELSEIF ((LB .GE. 0.4) .AND. (T .GT. 1E4) .AND. (T .LE. 3E4)) THEN
    MPE92 = CB*I.8*T**0.75*0.001
  ELSEIF ((LB .GT. 0.7) .AND. (LB .LE. 1.05)) THEN
    IF (T .LE. 1.8E-5) THEN
      MPE92 = 0.1
    ELSEIF ((T .GT. 1.8E-5) .AND. (T .LE. 1E3)) THEN
      MPE92 = 0.56*T**0.25
    ELSEIF ((T .GT. 1E3) .AND. (T .LE. 3E4)) THEN
      MPE92 = 0.1
    ELSEIF ((LB .GT. 1.05) .AND. (LB .LE. 1.4)) THEN
      IF (T .LE. 5E-5) THEN
        MPE92 = 5*CC*I.8*T**0.75*0.001
      ELSEIF ((T .GT. 5E-5) .AND. (T .LE. 1E3)) THEN
        MPE92 = 320*CA*0.001
      ELSEIF ((T .GT. 1E3) .AND. (T .LE. 3E4)) THEN
        MPE92 = 0.1
      ELSEIF ((LB .GT. 1.4) .AND. (LB .LE. 1.5)) THEN
        IF (T .LE. 1E-3) THEN
          MPE92 = 0.1
        ELSEIF ((T .GT. 1E-3) .AND. (T .LE. 1E3)) THEN
          MPE92 = 0.56*T**0.25
        ELSEIF ((T .GT. 1E3) .AND. (T .LE. 3E4)) THEN
          MPE92 = 0.1
        ELSEIF ((LB .GT. 1.5) .AND. (LB .LE. 1.8)) THEN
          IF (T .LE. 1E-7) THEN
            MPE92 = 0.1
          ELSEIF ((T .GT. 1E-7) .AND. (T .LE. 1E3)) THEN
            MPE92 = 0.1
          ELSEIF ((LB .GT. 1.8) .AND. (LB .LE. 2.6)) THEN
            IF (T .LE. 1E-3) THEN
              MPE92 = 0.1
            ELSEIF ((T .GT. 1E-3) .AND. (T .LE. 1E3)) THEN
              MPE92 = 0.56*T**0.25
            ELSEIF ((T .GT. 1E3) .AND. (T .LE. 3E4)) THEN
              MPE92 = 0.1
            ELSEIF ((LB .GT. 2.6) .AND. (LB .LE. 1E3)) THEN
              IF (T .LE. 1E-7) THEN
                MPE92 = 0.1
              ELSEIF ((T .GT. 1E-7) .AND. (T .LE. 1E3)) THEN
                MPE92 = 0.1
              ELSEIF ((LB .GT. 1E3) .AND. (LB .LE. 3E4)) THEN
                MPE92 = 0.1
5.2.3 Subroutine CLRSCRN

SUBROUTINE CLRSCRN ( I )
INTEGER J, I
DO 100 J=1, I, 1
WRITE(*,*)
100 CONTINUE
RETURN
END

5.3 Sample plot of data

Eye Safety Limits
(0.5 μs pulse length)
6.0 Appendix E - Eye Safety Analysis

The following paper was presented as Paper TuA6 at the 7th. Coherent Laser Radar Applications and Technology Conference, Paris, France, 19th-23rd July 1993.
Eye Safety Considerations For Selecting The Wavelength of a Space Based Coherent Doppler Wind Lidar

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Introduction
This paper derives an expression for the eye safety of a coherent doppler wind lidar starting from the signal to noise ratio (SNR) equation. The intensity at the eye of a potential observer and the proposed 1993 ANSI eye safety standard are folded in to produce an eye danger index.

Theory
The SNR from an aerosol target (subscript a) at range, R_a, from a lidar operating at a wavelength, λ, is given by:

$$SNR(\lambda) = \frac{\pi D_B^2 U_L \eta (\lambda) K_{ta}(\lambda) K_{ra}(\lambda) c \beta_a(\lambda) T_t(\lambda) T_r(\lambda)}{8 h v B(\lambda) R_a^2 \left[ 1 + \left( \frac{D_B}{2 \rho_{0a}(\lambda)} \right)^2 \right]}$$

(1)

where $U_L$ is the laser pulse energy at the laser, $K_{ta}(\lambda)$ and $K_{ra}(\lambda)$ are the atmospheric transmission of the transmit and receive beams, $c$ is the speed of light, $\beta_a(\lambda)$ is the atmospheric backscatter coefficient, $T_t(\lambda)$ and $T_r(\lambda)$ are the transmittance of the transmit and receive optics, $h$ is Planck's constant, $v$ is the laser frequency, $B(\lambda)$ is the processing noise bandwidth and $\rho_{0a}(\lambda)$ is the transverse field coherence length. $\eta(\lambda)$ is the efficiency of the lidar which is given by:

$$\eta(\lambda) = \eta_s(\lambda) \eta_\alpha(\lambda) \eta_p(\lambda) \eta_q(\lambda) \eta_u(\lambda)$$

(2)

where $\eta_s(\lambda)$, $\eta_\alpha(\lambda)$, $\eta_p(\lambda)$, $\eta_q(\lambda)$ and $\eta_u(\lambda)$ are the lidar system, misalignment, polarisation, effective heterodyne quantum and unexplained loss efficiencies respectively. For a Gaussian beam
the $1/e^2$ intensity diameter of the transmitted beam, $D_B$, is optimised relative to the telescope physical diameter, $D_T$, when [1]:

$$D_B = 0.802D_T$$  \hspace{1cm} (3)

The processing noise bandwidth, $B(\lambda)$ is:

$$B(\lambda) = \frac{2V_s}{\lambda}$$  \hspace{1cm} (4)

where $V_s$ is the velocity search window.

The intensity, $Q_e$ at the eye of an observer (subscript e) at a distance, $R_e$, from the lidar, including diffraction but assuming negligible spreading of the beam by refractive turbulence is given by:

$$Q_e(\lambda) = \frac{4\pi D_B^2 U_L K_{le}(\lambda) T_r(\lambda) M}{16R_e^2 \lambda^2 + \pi^2 D_e^4}$$  \hspace{1cm} (5)

where $K_{le}(\lambda)$ is the atmospheric transmission to the observer and $M$ is a factor to account for the transverse intensity distribution of the optical beam. For example, for a fixed pulse energy, the intensity on the axis of a Gaussian beam is twice that of a uniform beam with the same diameter and therefore $M=2$ for a Gaussian profile.

An eye danger index $X(\lambda)$ can be defined by:

$$X(\lambda) = \frac{Q_e(\lambda)}{Q_{mpe}(\lambda)}$$  \hspace{1cm} (6)

where $Q_{mpe}(\lambda)$ is the proposed 1993 ANSI eye safety standard maximum permissible exposure (MPE) value shown in Figure (1a) for a 1μs pulse length. For values of $X(\lambda) > 1$ the lidar exceeds the ANSI specification. Combining Equations (1,2,4-6) gives:

$$X(\lambda) = \frac{16SNR(\lambda) hV_s MR^2 K_{le}(\lambda) T_r(\lambda) 4\rho_{0a}(\lambda) + D_B^2)}{\eta(\lambda) K_{ra}(\lambda) K_{le}(\lambda) T_r(\lambda) \lambda^2 \beta_{st}(\lambda) Q_{mpe}(\lambda) \rho_{0a}(\lambda)^2 (\pi^2 D_B^4 + 16\lambda^2 R_e^2)}$$  \hspace{1cm} (7)

Figures (1b) and (1c) show the value of $X(\lambda)$ over the wavelength range 1-12 μm for a space based lidar and an earth based observer using the parameters listed in Table (1). The calculations assume a spherical earth, a lidar altitude of 525 km, a 45° nadir scan angle, an aerosol target at an altitude of 10 km and an observer on the ground. The minimum detectable SNR was taken as -13.2 dB, independent of wavelength. Both a $\lambda^{-2}$ (Figure (1b)) and a $\lambda^{-1}$ (Figure (1c)) dependence of backscatter on wavelength were used to represent typical values near 10 km altitude. The backscatter was anchored to a value of $5 \times 10^{-11}$ (m-sr)$^{-1}$ at 9.11 μm, again a typical value for 10 km. A laser pulse length of 1 μs was assumed when determining the MPE values. For wavelengths shorter than 2.6 μm the MPE does not depend on pulse length for pulses of width 1 ns - 50 μs, and only a weak pulse length dependence exists for wavelengths longer than 2.6 μm. The transverse coherence length has a $\lambda^{6/5}$ dependence and was anchored to a value of 58 m at 9.11 μm. The wavelength dependent atmospheric transmission is not suited to a simple expression and a constant

---

value of 0.86 was assumed for the atmospheric transmission to the observer. Atmospheric extinction to the aerosol target was assumed to be negligible.

<table>
<thead>
<tr>
<th>SNR(λ)</th>
<th>-13.2 dB</th>
</tr>
</thead>
<tbody>
<tr>
<td>h</td>
<td>6.62607 x 10^{-34} Js</td>
</tr>
<tr>
<td>V_s</td>
<td>50 ms^{-1} or ± 25 ms^{-1}</td>
</tr>
<tr>
<td>T_r(λ)</td>
<td>0.95</td>
</tr>
<tr>
<td>M</td>
<td>2</td>
</tr>
<tr>
<td>β_a(λ)</td>
<td>5 x 10^{11}/(m-sr) @ 9.11 μm</td>
</tr>
<tr>
<td>Q_{mpe}(λ)</td>
<td>ANSI standard (Figure 1a)</td>
</tr>
<tr>
<td>R_a</td>
<td>754.2 km</td>
</tr>
<tr>
<td>R_e</td>
<td>775.9 km</td>
</tr>
<tr>
<td>D_T</td>
<td>1.5 m</td>
</tr>
</tbody>
</table>

| η_s(λ)   | 0.46 |
| η_a(λ)   | 0.5  |
| η_p(λ)   | 1    |
| η_q(λ)   | 0.4  |
| η_u(λ)   | 0.5  |
| K_{ra}(λ) | 1   |
| K_{ta}(λ) | 1   |
| K_{te}(λ) | 0.86 |
| θ_{0a}(λ) | 58 m @ 9.11 μm |

Table 1: Parameter values used to calculate Figures (1b) and (1c).

Discussion
We have combined the coherent lidar SNR equation with the ANSI eye safety standard to arrive at an expression for eye danger index. Equation (7) is valid for any location of a coherent Doppler lidar, aerosol target and human observer; however Figures (1b) and (1c) apply only to the specific space based configuration described in Table 1. For the space based configuration, the parameters in Equation (7) with the largest dynamic range are λ, Q_{mpe}(λ) and β(λ). Limitations of the existing calculations are the use of wavelength independent terms for misalignment loss, atmospheric transmission, SNR threshold, detector quantum efficiency and exponent for the backscatter wavelength dependence.

References
Figure 1a) The MPE for a 1 μs pulse. b) and c) The eye danger index for the two backscatter dependencies on wavelength discussed in the text.
**Title and Subtitle**

Lidar Performance Analysis

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**Type of report and Period covered**

Final report 10/23/92 - 11/22/93