MEASUREMENT AND PREDICTION OF BROADBAND NOISE FROM LARGE HORIZONTAL AXIS WIND TURBINE GENERATORS

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ABSTRACT

A method is presented for predicting the broadband noise spectra of large wind turbine generators. It includes contributions from such noise sources as the inflow turbulence to the rotor, the interactions between the turbulent boundary layers on the blade surfaces with their trailing edges and the wake due to a blunt trailing edge. The method is partly empirical and is based on acoustic measurements of large wind turbines and airfoil models. Spectra are predicted for several large machines including the proposed MOD-5B. Measured data are presented for the MOD-2, the WTS-4, the MOD-OA, and the U.S. Windpower Inc. machines. Good agreement is shown between the predicted and measured far field noise spectra.

INTRODUCTION

The machines for which data are presented here and in References 1 through 6 are shown in the photographs of Figure 1. They consist of the MOD-2, the MOD-OA, the WTS-4 and the U.S. Windpower machine. The first three of these are government sponsored. All are self starting, have 2 or 3 blades, rotate in the range 17 to 72 rpm, and normally operate at wind speeds of 3 to 16 m/s.

Some dimensions and operational details are included in the table of Figure 2. MOD-2 is noted to be an upwind machine whereas the others are downwind machines. Rotor diameters range from 17.1 m to 91.4 m, rotor tip speeds from 66.5 to 122.4 m/s, blade areas from 15 to 236 m², and rated power outputs from 50 to 4200 kW. Calculated values are included for the proposed MOD-5B machine for which data are listed at the bottom of Figure 2.

The machines described in Figures 1 and 2 represent wide ranges of size, output power rating and configuration. Resulting differences in their noise production are presented in Figures 3 through 8. Comparisons are made on the basis of one-third octave band spectra, narrow band spectra, dB(A) levels, and perception distances.

Effects of Size and Configuration

The one-third octave band spectra of Figure 3 were measured on axis and normalized to a distance of 100 m from each machine. Definite trends are observed. The spectra exhibit their highest levels at the low frequencies, with general reductions in level as frequency increases. Further, the machines having the highest power output also have the
highest noise levels. This latter trend is particularly evident at the low frequencies.

A comparison of the narrow band noise spectra for large upwind and downwind machines is given in Figure 4. Data are narrow band ($\Delta f = 0.25$ Hz) and are limited to the frequency range below 100 Hz. The general reduction in level with frequency is seen to be about the same for both machines. The WTS-4 machine has a number of discrete peaks in its spectrum, particularly below 50 Hz. These are loading harmonics which occur at integral multiples of the blade passage frequency. Their amplitudes are enhanced because of the tower wake-blade interference encountered in this downwind configuration. In the MOD-2 spectrum only a few discrete peaks are evident and these are believed to be of electromechanical origin. No loading noise harmonics are apparent for this upwind configuration. The relatively lower levels of the MOD-2 spectrum are due in part to its lower tip speed.

Effects of Output Power

The one-third octave band spectra of Figure 5 illustrate the differences in the noise output for the WTS-4 machine at two different power outputs. Data are for the on-axis measuring points for power outputs of 1,000 and 4,000 kW respectively. Higher levels are associated with the higher power output and are seen to occur at frequencies below about 1,000 Hz.

Directivity Effects

Noise measurements for the machines of Figure 1 indicate that the noise radiation patterns are not sharply directional. At equal distances on-axis (upwind and downwind) essentially no differences are observed in either spectral shapes or sound levels. There are, however, consistent differences between measurements made on-axis and in the plane of rotation. Figure 6 shows one-third octave band spectra for the MOD-2 machine. Note that the in-plane data have relatively lower levels at low frequencies and higher levels at high frequencies than do the on-axis data. The result is a cross-over effect as seen in the figure.

Similar data are presented in Figure 7 to show a comparison between the MOD-2 and WTS-4 machines. The data points represent mean $L_{eq}$ (dB(A)) levels for a large number of measurements for both machines. The noise radiation pattern curves in each case are estimated. The MOD-2 machine radiates essentially in a non-directional pattern. The WTS-4 radiation pattern on the other hand shows higher levels on-axis than in-plane. As suggested in Figure 6 the low frequency components are known to be relatively strong on-axis. Thus the skewness of the radiation pattern of the WTS-4 is due to the influence...
of the low frequencies on the Leq values.

![Frequency vs. Sound Pressure Level Diagram](image)

Figure 6. - Comparison of on axis and in plane noise spectra for MOD-2 machine. (P = 2500 kW, r = 100 m.)

Note that the noise is observed at a much greater distance downwind than upwind, in spite of the fact that the noise radiation patterns of Figure 6 are nearly symmetrical. This skewness is due to refraction effects of the mean wind speed gradient, resulting in the formation of shadow zones upwind and propagation enhancement downwind. The distance from the machine to the shadow zone is dependent upon the height of the noise source above the ground surface and the wind speed gradient.

![Noise Radiation Patterns Diagram](image)

Figure 7. - Comparison of a-weighted noise radiation patterns for WTS-4 and MOD-2 machines. (Vw = 7.6-13.4 m/s.)

### Perception Distances

Observations of the radiated noise from a number of different machines and for a range of weather conditions have established a wind related directionality which is illustrated in Figure 8. The data points for the MOD-2 and the WTS-4 machines represent locations at which the noise during steady state operations is observable intermittently.

![Perception Distances Diagram](image)

Figure 8. - Comparisons of perception distances for the WTS-4 and MOD-2 machines. (Vw = 7.6-13.4 m/s.)

### Broadband Noise Prediction

To adequately assess the impact of the wind turbine noise and to aid in the design and siting of machines that are acceptable to the community (Refs. 7 and 8), a thorough understanding of the underlying noise generation phenomena as well as prediction techniques are highly desirable. Current literature on wind turbine noise is limited. Most publications deal with the impulsive "thumping" noise caused by the blade cutting the wake behind its supporting tower, where the rotor is located downwind from the tower (Refs. 9-15). A prediction code for this type of noise is presented in Reference 16. Other possible sources of wind turbine noise are discussed in Reference 5 and some of these noise mechanisms are considered in References 1, 6, and 17-19. Reference 19 compares theory with experimental broadband noise data (Refs. 1 and 2) but results indicate that better prediction techniques are needed. In the next sections a broadband noise prediction scheme for horizontal axis wind turbine generators is presented.

Extensive noise measurements on current, large, horizontal axis wind turbine generators (Refs. 1-6) indicate the presence of three major aerodynamic source mechanisms of broadband noise (Figure 9):

1. Loading fluctuations due to inflow turbulence interacting with the rotating blades.
2. The turbulent boundary layer flow over the airfoil surface interacting with the blade trailing edge.

3. Vortex shedding due to trailing edge bluntness.

Turbulence Characteristics The length scale and the intensity of the inflow turbulence are dependent on meteorological conditions and height above the ground (Ref. 43). A helicopter flying at different altitudes will thus encounter different turbulence conditions, while for any given wind turbine the distance above the ground is fixed. For the wind turbines considered here the turbulence might be considered isentropic which means that fluctuations are approximately the same in all directions (Ref. 44). For horizontal axis wind turbine generators the longitudinal turbulence component is by far most important. This longitudinal component is assumed to be a horizontal sinusoidal gust of the form:

$$w(t) = w e^{i\omega(t/V_w)}$$

where $w$ is the square root of the root mean square turbulence intensity, $\omega$ is the rotational frequency, $t$ is the time and $x$ corresponds to a chordwise distance. The wind structure is strongly dependent on temperature gradient and turbulence ordinarily is stronger in the daytime than at night when the atmosphere is more stable. In this paper a standard day is assumed with a negative temperature gradient as a function of height above the ground. The root mean square turbulence intensity at elevation $h$ is given by (Ref. 45):

$$\omega_r^2 = \int \phi_x d\omega$$

where $\phi_x$ is the longitudinal turbulence spectrum at that elevation and is expressed in terms of a reference turbulence intensity $\omega_r$ (Ref. 45):

$$\phi_x(n, V_w) = \frac{\omega_r^2}{\omega} \left[ 0.164 \frac{\eta}{\eta_0} \right]^{5/3}$$

where $\eta$ is the reduced frequency $V_w/\omega$ and $\eta_0$ has the value of 0.0144 for a longitudinal gust. An expression for the reference turbulence intensity $\omega_r$ as used in the structural analysis of the MOD-2 machine can be obtained from Reference 45:

$$\omega_r = 0.2 \left[ 2.18 V_w^{-.353} \right]^{1.185-.193 \log h}$$

Substitution of Equation (3) in (2) yields, after integration, the root mean square turbulence intensity as a function of only wind-speed and height above the ground:

$$\omega_r^2 = \omega_r^2 \left[ h \left[ \frac{1}{V_w} R(\omega_r, 0.14, \omega_r^2) \right]^{2/3} \right]$$

where $\omega_r$ is given by Equation (4). The longitudinal turbulence spectrum $\phi_x$ has been integrated between a minimum frequency which was chosen very close to zero and a maximum frequency $\omega_{\text{max}}$ which was chosen such that high frequency (small extent) turbulence may be disregarded (Ref. 45).
Far-Field Noise Prediction - The induced fluctuating force $F$ per unit span is related to the horizontal gust by the aerodynamic transfer function $G(k)$:

$$\left(\frac{\dot{F}}{\dot{E}}\right)^2 = \omega_w^2 e^{2i\omega(t-x/v_w)}|G(k)|^2 \quad (6)$$

where $k = (\omega c_0/2V_w)$ and $G(k)$ is based on Osborne's asymptotic solution for the compressible extension of the Sears function (Refs. 28 and 35), which for low frequencies is approximated by:

$$G(k) = \frac{\tau U c_0 dr}{1 + 2\pi k} \quad (7)$$

Lighthill has shown that the sound pressure due to a fluctuating force $F_i$ at a point with coordinates $x_i$ ($i=1,2,3$) is given by the expression (Ref. 46):

$$p(t) - p_o = \frac{x_i}{4\pi r_o^2} \left[ \frac{1}{c_o} \frac{\partial F_i(t-\tau/\sqrt{c_o})}{\partial t} + \frac{1}{r_o} F_i(t-\tau/\sqrt{c_o}) \right] \quad (8)$$

where $c_o$ is the speed of sound and $r_o$ is the distance between the source and receiver. If the source is considered to be a point dipole and the wavelength of the radiated sound is much smaller than the distance $r_o$ to the receiver the expression for the acoustic pressure in the far field formulated by Curle (Ref. 47) may be used:

$$p(\mathbf{r}, t) = \frac{\sin \theta}{4\pi c_o r_o} \int \frac{\partial F(t-\mathbf{r}/\sqrt{c_o})}{\partial t} \quad (9)$$

where $\mathbf{r}$ is the vector from the origin to the receiver location (in the y-z plane) and $\theta$ is the angle between $r_o$ and the z-axis. Substituting Equations (6) and (7) into Equation (9) yields after integration and squaring the mean square sound pressure in the far field as being proportional to:

$$\left| \frac{p}{S} \right|^2 = \frac{K_1(f) B \sin^2 \theta \rho^2 c R}{r_o^2 c_o^2} \frac{U^4}{U} \quad (10)$$

where $B$ is the number of blades, $R$ is the radius of the rotor, and $K_1(f)$ is a frequency dependent scaling factor. To evaluate this scaling factor, the wind turbine rotor has been modeled as a dipole point source located at the hub and Equation (10) is compared with frequency spectra from the MOD-2 machine for which the noise was largely due to turbulent inflow (Refs. 15 and 16). The location of the peak intensity in the frequency domain is strongly dependent on blade velocity and longitudinal scale of turbulence (Ref. 24). The turbulence is dependent on height above the ground for non-varying meteorological conditions. To account for different hub heights as well as different rotor diameters the location of the peak intensity in the frequency domain is given by:

$$f_{\text{peak}} = S U / (h - 0.7R) \quad (11)$$

where $S$ is the applicable Strouhal number which is obtained from comparison with the measured MOD-2 noise spectra.

Power Output and Windspeed - If the power generated by the wind turbine is known rather than the wind speed, which is needed as input for Equations (4) and (5), it is necessary to know their relationship to enable noise predictions. Reference 48 suggests that for constant rotational speed machines the output power is linearly proportional to the windspeed velocity and pitch angle. Between the cut-in speed and the rated wind speed the power output will vary approximately linearly with windspeed, which can be expressed by the equation:

$$V_w = \frac{P}{P_r}(V_{ra} - V_{ci}) + V_{ci} \quad (12)$$

where $P_r$ is rated power output at the corresponding rated windspeed $V_{ra}$ and $V_{ci}$ is the cut-in windspeed at which no output power is produced. Equations (4), (5), (10), (11) and (12) are utilized to predict the noise spectra due to inflow turbulence for other machines and operating conditions.

Turbulent Boundary Layer-Trailing Edge Interaction

Noise is generated when the blade attached turbulent boundary layer convects into the wake at the trailing edge. Theoretical models of this trailing edge noise for helicopter blades are presented in References 20-22 and 48-60. The experimental and theoretical study in Reference 53 concludes that the trailing edge noise radiated from a local blade segment can be predicted by a first principles theory, which includes local Mach number, boundary layer thickness, length of the blade segment and observer position. A scaling law approach then was used for comparison with the noise radiation data from a stationary two-dimensional isolated airfoil segment. This theory will be utilized to predict the trailing edge noise generated by the blades of large horizontal axis wind turbine generators.

The scaling law prediction of Reference 53 gives for the trailing edge noise spectrum for an isolated airfoil:

$$\text{SPL}_1 = 10 \log \left\{ K_2 U^2 B \delta^2 \left( \frac{S}{r_o} \right)^4 \left[ \frac{S}{S_{\text{max}}} \right]^{1.5} + 0.5 \right]^{-4} \quad (13)$$

where $\text{SPL}_1$ is the one-third octave band sound pressure level, $U$ is the local free stream velocity, $B$ is the number of blades, $\delta$ is the local boundary layer thickness, $S$ is
the airfoil span, \( r_0 \) the distance to the receiver, \( D \) the directivity, \( S \) the Strouhal number and \( K_2 \) is a constant which equals 220 when SI units are used. Equation 13 is essentially the trailing edge noise prediction for a two-dimensional lifting surface in a uniform inflow. To predict the trailing edge noise from a rotating blade the blade is divided into small blade segments, with a length \( s \), each experiencing a different local free stream velocity and each contributing to the noise at the receiver location. Because of the rotation this noise spectrum then is averaged around the azimuth. The local free-stream velocity \( U_x \) is given by:

\[
U_x = 2r_x n
\]

where \( r_x \) is the distance from the local blade section to the center of the hub and \( n \) denotes revolutions per second. The thickness of the turbulent boundary layer at the trailing edge of the airfoil may be approximated by the turbulent boundary layer thickness of a flat plate which is given by (Ref. 62):

\[
\delta = 0.37 \frac{c_x}{(R_{N_x})^{1/2}}
\]

where \( c_x \) is the chord at radius \( r_x \) from the hub and \( R_{N_x} \) is the local Reynolds number. Assuming a linearly tapered rotor blade and neglecting twist, \( c_x \) can be expressed in terms of the root chord \( (c_r) \), tip chord \( (c_t) \), radius \( (r_x) \) and blade diameter \( (D) \):

\[
c_x = c_t + (1 - \frac{2r_x}{D}) (c_r - c_t)
\]

The local Reynolds number is defined by:

\[
R_{N_x} = \frac{U_x c_x}{\nu}
\]

where \( \nu \) is the kinematic viscosity. The directivity pattern of the radiated trailing edge noise, for an observer in the vertical \( (y=0) \) plane perpendicular to the rotor plane is given by dipole like behavior from Reference 53:

\[
D(\theta, \frac{\pi}{2}) = \frac{\sin^2 \theta}{(1+M \cos \theta)^2} \left[ 1 + (M - M_C) \cos \theta \right]^2
\]

where \( \theta \) is the angle between the source-observer line and its projection in the ground plane. The convection Mach number of the turbulence, \( M_c \), is set to an average value of .8 M as suggested in Reference 53. To correct for the directivity of the source outside the \( y=0 \) plane, the source is assumed to be a dipole radiator in those directions and the directivity function is one proposed by Fink (Ref. 63):

\[
D(\theta, \psi) = \sin^2 \psi D(\theta, \frac{\pi}{2})
\]

where \( \psi \) is the angle between the source-observer line and its projection in the \( y=0 \) plane. The Strouhal number in Equation 13 is defined as the ratio of frequency \( (f) \) times the boundary layer thickness \( (\delta) \) and the undisturbed free stream velocity \( (U_x) \):

\[
S = \frac{f \delta}{U_x}
\]

The peak Strouhal number, \( S_{\text{max}} \), associated with trailing edge noise equals .1 (Refs. 63-65 and 53). Although a different value is reported in Reference 52, in the present study a value \( S_{\text{max}} = 0.1 \) is adopted.

Trailing Edge Bluntness Vortex Shedding Noise

Vortex shedding behind the trailing edges of thick struts has been studied in References 54-56. This phenomenon produces noise as the coherent vortex shedding causes a fluctuating surface pressure differential across the trailing edge. This was established in Reference 52 as being an important source of self-noise for airfoils with blunt trailing edges. The vortex shedding frequencies observed in References 54-56 had a peak Strouhal number of about .24 when based on the trailing edge thickness and a velocity dependence of approximately \( U_x^2 \). This peak Strouhal number compares well with the ones found by other researchers who studied the vortex shedding behind wings, flat plates and circular and noncircular bodies (Refs. 23, 49, 52, and 57-60). In all cases, the turbulent boundary layer displacement thickness \( (\delta^*) \) is much smaller than the characteristic dimension \( (t) \) from which the vortices are shed \( (t/\delta^* \geq 40) \). Experimental results from noise measurements on several trailing edge configurations in the NASA Langley Quiet-Flow Facility, however, indicated that for a trailing edge bluntness of equal thickness or smaller than the displacement thickness of the boundary layer a Strouhal number of .1 is applicable (Ref. 52). It was shown that the overall sound pressure level of the noise generated at the blunt trailing edge follows a \( U_x^2 \) dependence. Using the directivity pattern presented in Reference 53, the following scaling laws are derived for the one-third octave band sound pressure levels in the acoustic far field:

for \( t/\delta^* > 1 \):

\[
\text{SPL}_{1/3} = \frac{K_{BU} t s \sin^2 \theta \sin^2 \psi}{(1 + M \cos \theta)}
\]

and

\[
f_{\text{max}} = \frac{U_x}{0.25 t + \delta^*}
\]

for \( t/\delta^* < 1 \):

\[
\text{SPL}_{1/3} = \frac{K_{BU} 5.3 t s \sin^2 \theta/2 \sin^2 \psi}{(1 + M \cos \theta)^3} \left[ 1 + (M - M_C) \cos \theta \right]^2
\]

and

\[
f_{\text{max}} = \frac{U_x}{t + \delta^*}
\]
where $K_3$ and $K_4$ are scaling constants. The constant $K_4$ has been obtained by comparing Equation (23) with the blunt trailing edge noise measurements from Figure 40 in Reference 52, which were first converted to one-third octave band data. The constant $K_3$ has been determined by equating Equation (21) and (23) for the case that the trailing edge bluntness is of the same thickness as the displacement thickness of the turbulent boundary layer. For most practical purposes the displacement thickness and the boundary layer thickness are related by:

$$\delta^* = \frac{\delta}{\delta_{BL}}$$

Equations (21) through (25) are used to predict the noise from wind turbine blades with blunt trailing edges using the same calculation procedure as for turbulent boundary layer trailing edge interaction noise.

To assess the relative importance of all three major aerodynamic noise sources (Figure 9) predictions have been made for a MOD-2 machine at a distance of 100 m on-axis. The noise contributions due to turbulent inflow, trailing edge bluntness and turbulent boundary layer trailing edge interaction relative to the total noise is depicted in Figure 10. The turbulent inflow related noise dominates the spectrum at the low frequencies and is broad in character while turbulent boundary layer trailing edge interaction noise becomes relatively more and more important when moving up the frequency scale. Noise due to trailing edge bluntness is confined to a more restricted frequency band with its center frequency related to the thickness of the trailing edge. All predictions are limited to the acoustic far field, on-axis and without distinction between upwind and downwind directions as no propagation effects are incorporated.

To show that reasonable agreement can be obtained between broadband noise predictions and far field noise measurements, comparisons have been made for four horizontal axis wind turbines with quite different physical characteristics (Figures 1 and 2). Also various distances, number of blades and power outputs are shown to give a good comparison with actual measured data. Figure 11 shows predictions and measurements for two downwind machines, MOD-OA and WTS-4, at different distances and different power outputs. Only the noise due to turbulent inflow is dependent on the actual power output (actually the turbulence intensity) as evidenced by the results depicted in Figure 11. Other noise source mechanisms are only dependent on rotational speed. The effect of the trailing edge bluntness of the three blades of the U.S. Windpower machine is shown in Figure 12 where the sharp peak around 2000 Hz in the noise spectrum disappears after the trailing edges have been sharpened.

![Figure 10](image10.jpg)

![Figure 11](image11.jpg)

![Figure 12](image12.jpg)
The predicted noise spectrum of a MOD-2 upwind machine at rated power is depicted in Figure 13 along with measured data points showing good agreement. In the same figure a broadband noise prediction is presented for a MOD-5B machine, at rated power, on axis, 200 m away from the hub. The difference is shown for a machine with sharp trailing edges and for the case that the blade trailing edges have the same bluntness as the MOD-2 machine. The noise signature of the MOD-5B is predicted to be 2-3 dB higher than the MOD-2 over the whole frequency range, both operating at rated power.

Figure 13. - Predicted on-axis broadband noise spectra for two upwind machines. (r = 200 m.)

CONCLUDING REMARKS

Noise measurements and observations have been presented for four large horizontal axis wind turbine generators with quite different characteristics in size and configuration. Effects of output power, directional radiation effects (up-, down-, and cross wind) and noise perception distances have been discussed based on field measurements. A method has been presented for predicting the broadband noise spectra of horizontal-axis, constant rotational speed machines, based on contributions from noise due to inflow turbulence, turbulent boundary layer-trailing edge interaction noise and noise due to a blunt trailing edge. Good agreement is shown between predictions and far field noise measurements of the four large wind turbine generators for various operating conditions. The prediction method includes the effects of distance from the machine, output power (windspeed), number of blades and tower and blade geometry. Broadband noise is predicted only on-axis and the method does not distinguish between upwind and downwind. Propagation effects other than distance are not included in the present prediction formulation.

REFERENCES


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