OARE STS-78 (LMS-1) Final Report

James E. Rice
Canopus Systems, Inc.
Ann Arbor, Michigan

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1.0 INTRODUCTION

The report is organized into sections representing the phases of work performed in analyzing the STS-78 (LMS-I) results. Section 1 briefly outlines the OARE system features, coordinates, and measurement parameters. Section 2 describes the results from STS-78. The mission description, data calibration, and representative data obtained on STS-78 are presented. Also, the anomalous performance of OARE on STS-78 is discussed. Finally, Section 3 presents a discussion of accuracy achieved and achievable with OARE. Appendix A discusses the data processing methodology in detail.

1.1 OARE System Features

The Orbital Acceleration Research Experiment (OARE) contains a tri-axial accelerometer which uses a single free-floating (non-pendulous) electrostatically suspended cylindrical proofmass. The accelerometer sensor assembly is mounted on dual-gimbal platform which is controlled by a microprocessor in order to perform in-flight calibrations. Acceleration measurements are processed and stored in the OARE flight computer memory and, simultaneously, the unprocessed data are recorded on the shuttle payload tape recorder. These raw data are telemetered periodically to ground stations at several hour intervals during flight via tape recorder playback (data dumps).

OARE's objectives are to measure quasi-steady accelerations, to make high resolution low-frequency acceleration measurements in support of the micro-gravity community, and to measure Orbiter aerodynamic performance on orbit and during reentry. There are several features which make the OARE desirable for making highly accurate, low-frequency acceleration measurements. OARE is the first high resolution, high accuracy accelerometer flight design which has the capability to perform both bias and scale factor calibrations in orbit. Another design feature is the OARE sensor electrostatic suspension which has much less bias temperature sensitivity than pendulous accelerometers. Given the nature of the OARE sensor and its in-flight calibration capability, OARE stands alone in its ability to characterize the low-frequency environment of the Orbiter with better than 10 nano-g resolution and approximately 50 nano-g on-orbit accuracy.

1.2 Coordinate Systems

Two coordinate systems are used in this report — the OARE axes centered at the OARE sensor proofmass centroid and the Orbiter aircraft body axes centered at the Orbiter's center of gravity. The direction from tail to nose of the orbiter is +X in both systems. The direction from port wing to starboard wing is +Z in the OARE system and +Y in the Orbiter system. The direction from the Orbiter belly to the top of the Orbiter fuselage is +Y in the OARE system and -Z in the Orbiter system. This sensor-to-body coordinate alignment referred to above is the nominal flight alignment and was utilized for OARE data collection during STS-78.

In discussions of OARE calibrations of bias and scale factor, the OARE reference system is used. However, the flight acceleration data are given in the Orbiter body reference system. The sign convention is such that when there is a forward acceleration of the Orbiter (such as the OMS firing), this is then reported as a positive X-axis acceleration, even though a free particle may appear to move in the -X direction relative to the accelerating shuttle. All accelerations given in this report refer to the OARE location.
1.3 Sensor Measurement Parameters

There are three sensor ranges, A, B, and C, for each OARE axis, which are controlled by auto-ranging software logic. The full scale ranges and resolutions (corresponding to one count) are given in Table 1. In any case where the sensor channel is driven into saturation, the output is set to 1.5 times full scale of range A with the sign of the saturation signal included.

Table 1. OARE Sensor Ranges and Resolutions

<table>
<thead>
<tr>
<th>Range</th>
<th>Nominal Full Scale Range in micro-Gs</th>
<th>Y &amp; Z Axes</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>10,000</td>
<td>25,000</td>
</tr>
<tr>
<td>B</td>
<td>1,000</td>
<td>1,970</td>
</tr>
<tr>
<td>C</td>
<td>100</td>
<td>150</td>
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</table>

<table>
<thead>
<tr>
<th>Range</th>
<th>Resolution in nano-Gs SFN in nano-Gs/count</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>X-Axis 30.52</td>
</tr>
<tr>
<td>B</td>
<td>X-Axis 30.52</td>
</tr>
<tr>
<td>C</td>
<td>X-Axis 3.052</td>
</tr>
</tbody>
</table>

2.0 STS-78 (LMS-1) MISSION RESULTS

This section describes the results from STS-78 as derived from post-flight processing of the trim-mean OARE acceleration data stored on the on-board EEPROM. During the mission, preliminary calibrations and accelerations were reported in near-real time by NASA Lewis Research Center using the telemetered data from the payload tape recorder.

2.1 STS-78 (LMS-1) Mission Plan

The STS-78 adaptation parameters anticipated a mission of up to 17 days long. In order to make better use of the calibration time, the software was modified prior to STS-73 so that only C-range calibrations would occur in the "Quiet" mode, and calibrations would occur on all three ranges during the "Normal" mode. Since past experience had indicated that the Scale Factor had minimal variations and that, on-orbit, the instrument remains almost entirely in the C-range, the adaptation parameters were selected to use most of the allotted calibration time for C-range bias calibrations in order to obtain the most accurate measurements possible. When operating in the "Quiet" mode, C-range bias calibrations were performed every 158 minutes, and a bias calibration began within one minute after the "Quiet" mode was asserted. A C-range scale factor calibration was performed after every 15th bias calibration in the "Quiet" mode. In the "Normal" mode, a full bias calibration was performed every 432 minutes, and a full scale factor calibration performed after every 6th bias calibration.

During STS-78, 117 C-range bias measurements were made. Seventeen bias measurements were made on the A and B ranges. There were 10 and 3 scale factor measurements made on the C and A&B ranges, respectively. OARE operated in the Normal mode from MET times of 0 to 95.5 hours and
from about 367.8 hours to the end of the mission. For the remaining time OARE was operated in the Quiet mode.

2.2 STS-78 Actual Mission Description

Launch for STS-78 was at 10:49 a.m. EDT on 20 June 1996. The actual length of the OARE STS-78 mission was nearly 17 days with touch down at 8:37 a.m. EDT on 7 July 1996. The Mission Elapsed Time from launch to touchdown was 405.8 hours, making it the longest Space Shuttle Mission to date. Since the REENTER discrete was never asserted, OARE discontinued collecting data when it reached saturation and could not re-capture the proof-mass. This occurred at 405.38 hours.

All engineering parameter values were within normal range. Hardware performance was normal.

2.3 STS-78 Data Analysis

This section treats the several analyses carried out on the STS-78 flight data and summarizes the significant results. The processed acceleration data have already been delivered to the Microgravity Measurements and Analysis Branch Program (MMAP) at NASA Lewis Research Center.

The Orbital Acceleration Research Experiment (OARE) is designed to measure quasi-steady accelerations from below 10 nano-g up to 25 milli-g where quasi-steady indicates the frequency range from $10^{-3}$ to $10^{-1}$ Hz. To accomplish this, the sensor output acceleration signal is filtered with a Bessel filter with a cut-off frequency of 1 Hz. and cut-off rate of 120 dB per decade. The output signal is digitized at 10 samples per second and is then further processed and digitally filtered onboard the OARE instrument with an adaptive trimmean filter prior to the normal EEPROM storage. The trimmean data samples cover 50 second periods every 25 seconds. The regular 10 sample per second data were recorded on the payload tape recorder.

In flight, the OARE instrument is subjected to higher amplitude and higher frequency accelerations (due to the Reaction Control System (RCS) thrusters, structural vibrations and crew activities) in addition to the quasi-steady accelerations due to the gravity gradient, on-orbit drag, slow shuttle body rotations, and long period venting.

In order to obtain the optimum estimate of the quasi-steady acceleration under these conditions, a robust adaptive estimator has been implemented as part of the OARE analysis system. The particular estimator used is known as the Hogg Adaptive Trimmean estimator [1,2,8]. The bias estimate using the trimmean estimator of the acceleration is critical to the accuracy of acceleration measurements. During all previous missions, the data have been processed using the trimmean estimator because it provides the best estimate of the quasi-steady acceleration.

It has been the conventional wisdom that the quasi-steady acceleration effects are the most relevant to fluid experiments (as well as others) since these experiments have a finite reaction time and are believed to not to be very sensitive to high frequency accelerations. However, although the structural vibrations and crew activities induce only AC components of acceleration, the thruster firings produce a significant DC component of acceleration even though it is mostly high frequency relative to 0.1 Hz. The Trimmean filter tends to exclude these measurements from the 50 second trimmean averages, and thus, these short thruster firings do not normally appear in the trimmean processed data appearing in this report. In order to quantify these effects, the 10 sample per second data recorded on the payload tape recorder would need to be processed. This has not been done in this report, but was done on STS-75 where the EEPROM trimmean data were lost [8].
Thus, for STS-78 (LMS-1) the only measure of acceleration presented is the 50 second trimmean average calculated every 25 seconds as has been done on all previous OARE missions.

A detailed discussion of the data analysis undertaken for STS-78 is presented in Appendix A with the bias estimates using estimated measurement errors based upon the distributions of the measured data. This mission incorporated a full weighted least squares estimate of bias as was done on STS-73. [6]

The complete digital acceleration data presented in this report, as well as the raw payload tape recorder data at 10 samples per second which have not been processed by the filters, are available from the Microgravity Measurements and Analysis Program (MMAP) at NASA Lewis Research Center.[7]

The temperature environment was relatively benign except for the large temperature excursions during the initial thermal pulse generated during launch on STS-78 and during the maneuvers prior to reentry. The instrument temperature in degrees Celsius (measured on the proofmass housing) is shown in Figure 1.

![Figure 1. STS-78 Instrument (Sensor Head) Temperature.](image)

2.4 Orbiter Body Axis Acceleration Results.

The accelerations measured by OARE at the OARE location in the Shuttle Body Axes coordinate system (X- toward nose, Y -toward the starboard wing, Z -down through the belly) are shown in Figures 2 through 8 for representative time periods.

Figures 2 through 7 show the trimmean acceleration at the OARE location during the entire mission in segments of 72 hours. This measure of acceleration represents the acceleration due to the quasi-steady forces in that the larger short-period pulses are effectively removed from the data by this filter. The acceleration measurement set has small gaps in it as a result of the fact that during bias and scale factor calibrations the normal acceleration measurements are not being made.
Figure 2. OARE Trimmean Estimate of the Quasi-Steady Acceleration from MET 0 to 72 hours.
Figure 3. OARE Trimmean Estimate of the Quasi-Steady Acceleration from MET 72 to 144 hours.
Figure 4. OARE Trimmean Estimate of the Quasi-Steady Acceleration from MET 144 to 216 hours.
Figure 5. OARE Trimmean Estimate of the Quasi-Steady Acceleration from MET 216 to 288 hours.
Figure 6. OARE Trimmean Estimate of the Quasi-Steady Acceleration from MET 288 to 360 hours.
Figure 7. OARE Trimmean Estimate of the Quasi-Steady Acceleration from MET 360 to 432 hours.
These figures are a sample of the acceleration data from STS-78 (LMS-1) at the OARE location. Several things are readily apparent. 1) The quasi-steady acceleration measurements are much less "noisy" during the crew sleep periods, 2) During the crew sleep periods, the acceleration variations due to orbit drag and those due to attitude changes such as that at 92.5 MET hours are readily apparent in the X and Z axis data, and 3) The quasi-steady acceleration levels are normally less than one micro-G.

Figure 8 shows the acceleration data in more detail from MET of 222 to 240 hours. One can see the orbital variations due to drag in more detail from 225 to 232 hours and a possible venting from about 235.3 to 236.7 hours.

However, it is not feasible to present the data with sufficient time and amplitude resolution to meet the requirements of each experimenter in a single report. For additional detail, the complete set of data is available from the PIMS Group at Lewis Research Center. [7] The low frequency accelerations can also be calculated at the experimenter's location by the PIMS group using the OARE measurements and other shuttle parameters.

2.5 STS-78 Anomalous Performance

OARE's performance on STS-78 was similar to that on STS-75, STS-73, STS-65 and STS-62. The Z-axis C-range scale factor calibration was still affected by jitter to a small degree. In addition, the OARE instrument in the C-range continued to show the characteristics of an "electronic bias shift" that was first noted in STS-58 [4]. The electronic bias shift manifested itself with small changes in the pre- and post-rate levels during the scale factor calibration on the Z-axis in the C-range. This electronic bias shift was not apparent in the bias calibrations and appears to be an artifact that occurs only during the scale factor calibration period and, hence, does not affect the Z-axis data collection.

In addition, since the REENTER discrete was not commanded by INCO at JSC prior to reentry, the OARE instrument continued to process data in the Normal mode; in this mode, the processed trimmean filter data are written to the EEPROM memory. If the REENTER discrete has been set, the "raw" (10 sample per second) data would have written to the EEPROM memory during the reentry period.

3.0 OARE ACCURACY ANALYSIS

The OARE instrument provides high resolution measurements of sensor input axes accelerations, 3.05 nano-Gs in the OARE X-axis and 4.6 nano-Gs for the Y and Z axes. The accuracy of these measurements is primarily determined by the degree to which the instrument can be calibrated over the time period of the measurements. Major sources of potential errors are the accuracy obtainable from the bias and scale factor calibrations.

3.1 Bias Errors

On STS-78, the bias was measured 117 times. From these measurements, the true bias was estimated by the fitting procedure discussed in Appendix A. Potential errors in these bias estimates arise from the statistical nature of the bias measurements as well as from potential systematic errors which have not been identified. Based upon the analysis contained in Appendix A, we estimate that the bias errors are approximately 50 nano-Gs. These are consistent with the earlier analysis contained in the STS-65 Final Report [5].
Figure 8. OARE trimmean estimate of quasi-steady acceleration from MET 222 to 240 hours.
3.2 Scale Factor Errors

In the microgravity environment of the Orbiter, the quasi-steady trimmean acceleration measurements are typically on the order of 1 micro-g or less. Under these conditions, the bias errors are larger than the scale factor errors.

Measurements of the scale factors made during flight and those on the ground are now consistent to within 1 to 2 percent. We estimate the scale factor errors to be about 1 to 2 percent of the measured acceleration. These could be reduced with further study. At a 1 micro-g level, this corresponds to a 10 to 20 nano-G error. These should be added in quadrature with the bias errors. So overall, this gives estimated errors for the on-orbit acceleration measurements of about 50 to 60 nano-Gs.

3.3 Quasi-Steady Acceleration Measurements

As indicated, the primary OARE data recorded on the flight computer is processed through an adaptive trimmean filter. This trimmean filter provides a near optimum estimate of the mean of the quasi-steady acceleration population of measurements over the 50 second sampling period. This estimate is particularly beneficial in the calculation of the bias estimate and the estimate of the quasi-steady acceleration due to orbital drag, gravity gradient, and slow body rotations. However, it tends to reject the effects of crew activity, thruster firings, and other exogenous events. Experimenters may be interested in the regular average of the acceleration measurements over the 50 second sample period or other acceleration measurement metrics. In any case, the regular average and other filters could be applied to the payload tape recorder data for those periods where the data exist.

4.0 REFERENCES


7) Microgravity Measurement and Analysis Program (MMAP) at Lewis Research Center. Program Scientist of Principle Investigator of Microgravity Services (PIMS) is Richard Delombard, (216) 433-5285. E-mail to richard delombard@lerc.nasa.gov. Data file server is beech.lerc.nasa.gov.

APPENDIX A
OARE DATA CALIBRATION AND PROCESSING

This Appendix reviews the methods used to calculate the Orbiter body tri-axial acceleration based on the OARE instrument measurements which were recorded on the EEPROM, downloaded, and then processed by Canopus Systems. The method of estimating the sensor bias has evolved over the past several missions; STS-73 was the first mission where a full weighted least squares methodology has been implemented in estimating the instrument bias. The Appendix begins with the instrument model (A1), discusses the trimmean filter used in processing the raw OARE accelerometry data (A2), presents the weighted least squares estimate of the bias of the instrument (A3) and finally presents a short discussion of Scale Factor calibration (A4).

A1 INSTRUMENT MODEL

The OARE instrument acceleration for each axis and range is calculated from an equation of the form

\[ A_A = -SFC \times SFN \times (CTS - 32768 - BIAS) \] (eq. 1), where

- \( A_A \) is the calibrated actual acceleration in uGs,
- \( SFC \) is the Scale Factor Calibration term,
- \( SFN \) is the Nominal Scale Factor in uGs per count,
- \( CTS \) is the counts out of the instrument A/D converter, and
- \( BIAS \) is the estimated Bias in counts as a function of time and temperature, where each of the terms is dependent upon the particular axis and range.

In the above equation, the number 32768 appears because the 16-bit A/D converter is single-ended; this value is the offset required to obtain a zero measured acceleration for a zero input acceleration when there is no bias.

An Actual Scale Factor \( SFA \) term is defined by

\[ SFA = SFC \times SFN \] (eq. 2).

Values of the nominal scale factor, \( SFN \), are given in Table 1 of the main report for each OARE axis and range. Values of \( SFC \) for the OARE X, Y, and Z axes are approximately 1.02, 1.11, and 1.10, respectively, but are determined through calibration on each STS mission for each axis and range.

The output of the A/D converter provides a raw digital acceleration data sample which is effectively processed at a rate of 10 times per second. Data are normally stored on the EEPROM at a rate of once every 25 seconds, and these data represent the trimmean filtered estimate of the quasi-steady acceleration value over a 50-second period.
A2 HOGG ADAPTIVE TRIMMEAN FILTER USED IN PROCESSING OARE ACCELERATION MEASUREMENTS

The OARE instrument is designed to measure the quasi-steady acceleration from below 10 nano-Gs up to 25 milli-Gs and over the quasi-steady bandwidth from $10^{-5}$ to $10^{1}$ Hz. The quasi-steady acceleration components of primary interest are those due to gravity gradient, on-orbit drag, inertial rotations, and perhaps long period venting or gas leaks. However, the instrument is subjected to higher amplitude and higher frequency accelerations (such as structural vibration, station keeping thruster firings, and crew effects) in addition to the quasi-steady accelerations. These higher level accelerations are not well characterized nor statistically invariant over the OARE measurement periods.

In order to obtain a more optimum estimate of the quasi-steady acceleration under the conditions of intermittent thruster firings and crew activities, a robust adaptive estimator has been implemented. For a discussion of robust estimators, see Reference 1. The particular estimator implemented in OARE is known as the Hogg Adaptive Trimmean estimator and is described in more detail in Reference 2.

In essence, the trimmean adaptive filter removes a percentage of the distribution from each tail and then calculates the mean of the remaining distribution. It first measures the departure of the sample distribution from a normal (Gaussian) distribution as measured by a parameter called $Q$, then adaptively chooses the amount of the trim to be used on the distribution, and finally calculates the mean of the remaining distribution after the trim. This filter is designed to remove the effect of a contaminating distribution (such as a thruster firing) superimposed on a normal distribution (of instrument noise, high frequency vibrations, crew activities, quasi-steady accelerations, etc.).

As implemented, $Q$ is defined by the following equation:

$$Q = \frac{[U(20\%) - L(20\%)][U(50\%) - L(50\%)]}{[U(50\%) - L(50\%)]} \quad (\text{eq. 3}),$$

where

$U(X\%)$ is the average of the upper $X\%$ of the ordered sample, and
$L(X\%)$ is the average of the lower $X\%$ of the ordered sample.

In the OARE case, the ordered sample has been a sample of 500 acceleration measurements of the A/D output over a 50-second measurement period.

$Q$ is a measure of the outlier content in the sample. For a Gaussian distribution, $Q$ is 1.75; for samples which have larger tails, $Q > 1.75$. The value of $Q$ is used to estimate the extent that the quasi-steady acceleration measurements may be contaminated by thruster firings, crew activities, etc.

In order to improve the estimate of the quasi-steady acceleration, a trimmean is used to estimate the mean of the quasi-steady population. A trim parameter alpha is determined by the following algorithm:
\[ \alpha(Q) = \begin{cases} 
0.05 & \text{for } Q \leq 1.75 \\
0.5 + 0.35 \times \frac{Q-1.75}{2-1.75} & \text{for } 1.75 < Q < 2.0 \text{ (eq. 4)} \\
0.4 & \text{for } Q \geq 2.0, 
\end{cases} \]

where \( \alpha \) is the fraction of the distribution which is trimmed off each tail of the ordered distribution before the mean of the remainder of the distribution is calculated.

Then, for an underlying distribution of \( n \) points or measurements with a value of \( \alpha \), the trimmean is given by

\[ \text{trimmean} = \frac{X(k+1) + X(k+2) + \ldots + X(n-k)}{(n-2k)}, \text{ (eq. 5),} \]

where \( k = \alpha \times n \text{ (eq. 6)} \) and

\( X(i), X(i+1), \ldots, X(n) \), is the ordered set of \( n \) points making up the sample distribution.

In summary, OARE measures the quasi-steady level of acceleration for each axis every 25 seconds by taking the trimmean of 50 seconds of A/D counts (500 samples in total) according to equations 3 through 6, and then substituting this trimmean for CTS in equation 1. It should be noted that for large pulses in one direction, the effect of the trimmean is to shift the estimate of the mean; it does not preserve the DC component in this case.

The trimmean is particularly appropriate for estimating the bias of the OARE instrument, since one wishes to remove the effect of the thruster on the bias measurement if a thruster firing should occur during the bias measurement period.

Data recorded on the EEPROM and available to support the acceleration calculations include the trimmean of the 50-second distribution every 25 seconds, the \( Q \) of this sample distribution, the Average Deviation from the trimmean of the distribution used to calculate the trimmean, the instrument temperature, the Mission Elapsed Time (MET), and numerous housekeeping parameters.

The widths of the 500 sample distributions (as measured by the standard deviations) are almost entirely due to the environment aboard the shuttle and not due to sensor noise. This is illustrated in the figures of the main report. On STS-78, the whole crew had common sleep periods as can be noted by the small variation in the data obtained during a sleep period. During these periods, the instrument output is extremely quiet as opposed to periods when there is crew activity. On most missions, the crew has been active 24 hours per day and consequently noisier data from a quasi-steady point-of-view resulted.

**A3 BIAS MEASUREMENTS AND ESTIMATED MEASUREMENT ERRORS**

As can be seen in Equation 1, the calculated acceleration depends upon the instrument bias. This is a critical parameter in accelerometers that are designed to measure quasi-steady or DC accelerations below 1 milli-G. For on-orbit conditions, the typical quasi-steady or DC
acceleration is less than 1 micro-G. Thus, the bias estimate is absolutely critical to accurate acceleration measurements in this regime.

The OARE accelerometer uses an electrostatically suspended proofmass in order to minimize the effects of temperature and mechanical suspension hysteresis on the bias. In addition, OARE incorporates a two-axis gimbal calibration table by which the OARE instrument can be calibrated on-orbit for bias and scale factor in each of its three axes.

A3.1 Bias Measurements

The bias measurement for a single axis consists of the following sequence: 1) measuring the acceleration output in trimmean counts for 50 seconds in the normal table position for a given axis (called \(B_{AN}\)), 2) rotating the input axis 180°, and then 3) measuring the acceleration output in trimmean counts (called \(B_{AI}\), for inverted position). Assuming that the actual input acceleration remains constant during this period (about 125 seconds), as might be expected for quasi-steady accelerations, then the bias can be calculated by

\[
B_{AM} = \frac{B_{AN} + B_{AI}}{2} - 32768 \quad \text{(eq. 7), where}
\]

- \(B_{AM}\) is the measured bias for a particular axis,
- \(B_{AN}\) is the bias measurement in the normal position, and
- \(B_{AI}\) is the bias measurement in the inverted position.

During a single mission, the bias is measured for each axis many times for the C-range. These bias measurements then provide the basis for estimating the bias time history throughout the mission. The bias estimates are ultimately determined by fitting a functional form through these bias measurements.

A3.2 Sources of Noise Associated with the Bias Measurement

The sources of noise which contribute to measurement errors on the bias measurements are largely associated with crew activity. The bias measurement accuracy depends upon the input acceleration remaining constant during the time that the bias measurements are being made. The time difference between the two positions used in the bias measurements is about 75 seconds. Clearly, the input acceleration is varying except during the times when the whole crew is asleep. During most missions, one segment of the crew is active at all times. Under these conditions, the bias measurements contain significant measurement errors which cannot be eliminated. A method of estimating the measurement errors on the bias has been developed and is discussed in Reference 5.

A3.3 Bias Estimates Based Upon Weighted Least Squares Fits

The bias was measured 117 times on STS-78 for each of the three axes on the C-range. Using the methodology discussed in Reference 5, estimates of the measurement errors associated with each bias measurement were calculated. The results for the OARE X, Y, and Z axes are
shown in Figures A-1, A-2, and A-3, respectively. The bias measurements are shown along with their associated measurement error bars.

As can be seen, there is considerable variation of the individual bias measurements, but the variation is generally explained by the measurement errors associated with the bias measurements. There are a few bias measurements which are widely separated from the others. These could be a result of thruster firing during the bias sequence. During the times that the crew was sleeping, the bias measurements were more accurate as indicated by the smaller estimated measurement errors.

The bias can be characterized by an initial transient after launch as a function of time and a small dependence upon temperature. In the same manner since STS-62 [3], we have fitted the measured bias data with a function of the following form:

\[
\text{Bias} = A_1 + A_2 e^{-(t/t_0)} + A_3 e^{-t/t_1} + A_4 T \quad \text{(eq. 8)},
\]

where \( A_1, A_2, A_3, A_4, t_0 \) and \( t_1 \) are fitted coefficients, \( t \) is the mission elapsed time in hours, and \( T \) is the instrument temperature in degrees Celsius.

Figure A-1. Bias Measurements and Fitted Estimate for OARE X-Axis on STS-78.
A weighted least squares procedure was used to determine the coefficients for the C-range. As part of the fitting procedure, several data points (0, 4, and 3 for the X, Y, and Z axes, respectively) which were significantly off the fitted curve were removed from those included in the fit and the fitting procedure was repeated for the C-range fits. The plots show all the data points whether they were included in the fit or not. Also for the B and A ranges, a weighted least squares procedure was used. Results from these fits are shown in Table A-1.
Table A-1. STS-78 Bias Fits to EEPROM Data.

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<td>C</td>
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<td>C</td>
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<tr>
<td>Number of Measurements</td>
<td>17</td>
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<td>114</td>
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The bias calculated by equation 8 is then used to estimate the actual bias during the mission as a function of MET and instrument temperature. This bias is then used to calculate the actual acceleration using equation 1. We believe that the error in the acceleration measurements associated with this bias estimation procedure is about 50 nano-Gs. The error could be further reduced if there were more quiet periods during the mission when a low noise bias calibration could be performed.

**A4 SCALE FACTOR CALIBRATION**

Scale factor measurements are made by applying a known non zero signal to the sensor and electronics for each channel and each range. These measurements may be contaminated by noise in the external environment or by internal noise in several forms.

For OARE, the method of scale factor calibration involves rotating the Motor/Table Subsystem (MTS) (sometimes called "the table") at a known angular rate \( \omega \) with a fixed sensor to center-of-rotation offset radius \( r \). The known signal is thus the controlled centripetal acceleration. While collecting scale factor data, the sensor also experiences a bias (assumed constant) and is exposed to an external signal. Data collected before and after the scale factor slew assists in removing the bias and external signal effect.

The basic scale factor measurement model is shown in Figure A-4.

![Figure A-4. Scale Factor Measurement Model](image)

From this model, the \( k^{\text{th}} \) measurement \( y_k \) is given by

\[
y_k = \frac{rw^2 + s_k}{SF} + b_k \quad (\text{eq. 9}),
\]

where \( s_k \) is the signal at the \( k^{\text{th}} \) measurement time and \( b_k \) is the internal bias at the \( k^{\text{th}} \) measurement time. We assume that \( \omega \) is constant throughout the slew. We also assume that \( s_k \) contains two components: (1) an acceleration signal which is fixed with respect to the MTS base throughout the slew and (2) a noise input with zero mean. To eliminate noise, consider averages of the measurements over the data set (with length \( n \))

\[
\overline{y} = \frac{rw^2 + \frac{1}{n} \sum_{i=1}^{n} s_i}{SF} + \overline{b} \quad (\text{eq. 10}),
\]

where \( (\cdot) \) is the average value of \( (\cdot) \).
From this equation we can find the actual scale factor $SF_A$. Here, $\bar{y}$ is the average of the measurements and $r\omega^2$ is known. The remaining unknown, $s_k$, is a combination of the external signal and noise. This is related to the midpoint measurement (MP). During the slew, the sensor records varying magnitudes of the external signal. The bias and centripetal acceleration, however, remain fixed in magnitude. If the measurements are centered around the midpoint, the midpoint measurement can be used to estimate this external signal and remove it from the scale factor equation. It can be shown that the influence that the external signal and bias have on the scale factor measurements is related to the sinc function ($\sin(x)/x$) of the angular travel. The actual scale factor can then be found from the following equation:

$$\frac{1}{SF_a} = \frac{\bar{y} - MP(\sin(\delta)/\delta) - (1 - (\sin(\delta)/\delta))b}{r\omega^2}$$  \hspace{1cm} (eq. 11).

The scale factor calibration is $SF_C = SF_A / SF_N$, where $SF_N$ is the nominal scale factor.

Scale factor calibrations were calculated for all three OARE axes and the three ranges. The results are shown in Table A-2.

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*This Scale Factor Correction was computed from the B range measurement.
REFERENCES


The report is organized into sections representing the phases of work performed in analyzing the STS-78 (LMS-1) results. Section 1 briefly outlines the OARE system features, coordinates, and measurement parameters. Section 2 describes the results from STS-78. The mission description, data calibration, and representative data obtained on STS-78 are presented. Also, the anomalous performance of OARE on STS-78 is discussed. Finally, Section 3 presents a discussion of accuracy achieved and achievable with OARE. Appendix A discusses the data processing methodology in detail.