Analysis of Particle Image Velocimetry (PIV) Data for Application to Subsonic Jet Noise Studies

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Abstract

Global velocimetry measurements were taken using Particle Image Velocimetry (PIV) in the subsonic flow exiting a 1” circular nozzle in an attempt to better understand the turbulence characteristics of its shear layer regions. This report presents the results of the PIV analysis and data reduction portions of the test and details the processing that was done. Custom data analysis and data validation algorithms were developed and applied to a data ensemble consisting of over 750 PIV 70mm photographs taken in the 0.85 mach flow facility. Results are presented detailing spatial characteristics of the flow including ensemble mean and standard deviation, turbulence intensities and Reynold’s stress levels, and 2-point spatial correlations.
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Introduction

Global velocimetry measurements were recently taken as part of the Advanced Subsonic Technology (AST) program at NASA Langley Research Center. In these measurements, Particle Image Velocimetry (PIV) was used to measure the flow exiting a heated 1-inch circularly-symmetric subsonic jet. The PIV technique provided spatially resolved velocity measurements in the shear region of the expanding jet that were used to study turbulence and length scale interaction, and their involvement in the jet-noise production process. Data was taken along a plane intercepting the jet centerline, and included instantaneous, fluctuating, and ensemble mean velocity, as well as ensemble standard deviation levels, turbulence intensities, Reynold’s stress, and 2-point correlations.

The specific goal of this effort was to test the feasibility of making in-situ global velocity measurements with the PIV technique in the very harsh environment of a subsonic/transonic jet combustor where temperatures are typically in excess of 500 degrees Farenheit, velocities range from near zero in the entrainment regions to 1.2 mach in the jet core, and vibration and image degradation levels can be severe. Consequently, the PIV analysis processing for this test involved not only evaluation of the basic flow parameters, but determination of image quality levels, measurement accuracy estimates, and data convergence evaluations.

Particle Image Velocimetry (PIV) System Description

The basic PIV measurement process involves taking an instantaneous, double exposure record of seed particles entrained in a flow of interest. Two overlapping laser light sheets are used to illuminate a measurement plane in the flow which has been seeded with neutrally buoyant particles. Digital or photographic records of the tracer seed are then taken, where a delay is introduced between the two laser pulses to allow the particles to move within the exposure. The local velocity, \( u \), can then be determined from the particle image displacement measurements in the film recording using:

\[ u = \frac{\Delta X}{\Delta \tau M} \]  

(1)

where \( \Delta X \) is the local measured particle displacement, \( \Delta \tau \) is the laser pulse separation time, and \( M \) is the system magnification.

The PIV acquisition system used in this effort is depicted in Figure 1. It uses two frequency doubled Nd:YAG lasers each operating at a wavelength of 532nm, energy of 580mj, and 10Hz repetition rates. A 70mm Hasselblad camera system using Kodak Tri-X film was used...
to photograph the flow. The camera used a 350mm focal length lens system operating at F#11, which provided a system magnification of 1:1 and a usable field of view of approximately 55mm² (Figure 2). A custom polarizing image shift cube system was placed just before the lens system to resolve directional ambiguity and increase dynamic range levels. The entire imaging system was placed in a sealed enclosure box that was cooled with air conditioned air. This isolated the lens and camera system from the 580 degree F air that was exiting the jet, while allowing it to be within approximately 1/2 meter from the flow. Seed to the jet was provided through one internal and two external seed insertion systems. The external systems were placed along the outer jet structure approximately 12” before the nozzle exit, while the internal system was coupled to the interior of the jet approximately 1 1/2 meters upstream. The internal system was also heated to match the heated air entering the back of the jet.

**PIV Analysis Process**

The analysis system used in this test is based on a typical PIV analysis system design and uses autocorrelation processing of 8-bit digitized 128x128 pixel sub-regions of a double exposure PIV photograph. In a double-pulsed, single-frame PIV system, the spatial autocorrelation of \( I(X) \), the transmitted light intensity from the photograph, with particle image separation levels \( s \) is approximated by the spatial average estimator over an interrogation spot:\(^3\)

\[
R(s) = \int I(X)I(X + s)\,dX
\]  
(2)

which consists of five components:

\[
R(s) = R_c(s) + R_p(s) + R_D^+(s) + R_D^-(s) + R_F(s),
\]  
(3)

Here, \( R_c \) is the convolution of the mean intensities and \( R_F \) is the fluctuating noise component of the correlation estimator. They represent noise and background influences to the signal levels and are minimized if possible. The signals of interest are given by the \( R_D^+(s) \) and \( R_D^-(s) \) terms. \( R_D^+(s) \), the correlation of all first images shifted by \( s \) with subsequent unshifted images, and \( R_D^-(s) \), the correlation of all later images shifted \( s \) with prior unshifted images, are identical in form and shape, with \( R_D^+(s) \) centered at the positive mean displacement of the images and \( R_D^-(s) \) centered at the negative mean displacement. The strongest signal component \( R_D^+ \), represents the correlation of particle images with themselves, and has a maximum value when \( s=0 \) and a width comparable to \( \Delta r \), the particle image diameter. The amplitudes of \( R_D^+ \) and \( R_D^- \) are less than half that of \( R_D^+ \) as the correlation between pairs of images is at most half of the correlation of images with themselves.

The computation intensive 2-D spatial autocorrelation calculations were performed in this effort using an Alacron i860 array processor subsystem on an 486/33 IBM PC/AT host computer.
The system is currently capable of processing five displacement vectors per second. Custom processing and control software is used and runs under Microsoft Windows v3.1 and Windows 95. The analysis is completely automated with the exception of user input to a configuration file prior to analysis execution for update of various system parameters. The executable program file is named PIV54.exe with a configuration text file called KODAK54.cfg.

The main system components used in the analysis system include a Kodak Megaplus camera model 1.4, an Epix 4MEG VIDEO Model 10 frame grabber board, an Alacron AL860XP array processor board, and a Unidex 11 3-axis motion control system. In addition, a single 120mm focal length, 40mm diameter, achromatic lens imaged the approximate 6mm x 4mm field of view @ 1:1 imaging to the Kodak camera system. A schematic diagram of the system design is provided in Figure 3. The Kodak Megaplus camera has two primary operating modes: low resolution and high resolution. The low resolution mode was used for this set of tests which provided image capture at 640x480 pixel resolution. The image was transferred by the Epix framegrabber board to PC-AT memory and then to the Alacron array processor memory for autocorrelation processing.

A preliminary analysis system checkout was performed before actual analysis began in order to determine the acquisition and analysis magnification levels, spatial resolution levels, and image distortion levels. The acquisition system magnification of 0.93066x was determined by taking several photographs of a 70mm x 70mm grid (@ 1mm grid spacing) with the PIV acquisition system. These raw grids were then examined with the analysis system, and a comparison was made between the photographs and the raw grid in order to calibrate the acquisition system magnification. Five horizontal and six vertical strips of grid data were extracted across the entire field for both the photograph and the raw grid, where measurements of the grid line separations were made and compared.

The analysis system magnification of 10.0628 microns/pixel was found by examining a precision reticle (1mm long @ 50 micron line resolution) at five position covering the entire field of view. The average positions of 20 lines separated by 50 microns each was measured at each location in the vertical and horizontal directions, where the average of the five locations was used to obtain the overall analysis system magnification.

An approximate 1mm spatial resolution was desired (1mm x 1mm correlation cell size) at 50% oversampling which would have given a step size of 0.5mm. The field coverage for a typical PIV photograph taken with the 70mm Hasselblad camera has an octagon shape covering and approximate 55mm x 55mm region at 1:1 magnification (see Figure 2). The analysis system magnification factor of 10.0628 microns/pixel was used with the fact that correlations are done at a 128x128 digitized pixel resolution to obtain a spatial correlation resolution size of: 128pixel² * 10.0628micron/pixel = 12880 mm². At 50% over-sampling the vector output resolution is 1/2 the correlation resolution and is 0.644mm (close to the desired 0.5mm resolution) in both the
vertical and horizontal directions. The Kodak Megaplus 1.4 camera was used in low resolution mode and captured 640x480 pixels at a time. This allowed a 6x9 grid (50% oversampled) of 128x128 pixels to be captured at a time giving 54 correlations (i.e. vectors) every time the Megaplus camera captured an image. The corresponding step sizes are then \((6 \times 1.288\text{mm}) = 3.864\text{mm}\) in the vertical direction and \((9 \times 1.288\text{mm}) = 5.796\text{mm}\) in the horizontal direction. For an approximate field coverage of 55mm x 55mm, the required number of steps becomes: \((55\text{mm} / 3.864\text{mm}) = \sim 15\) steps in the vertical direction and \((55\text{mm} / 5.796\text{mm}) = \sim 10\) steps in the horizontal direction. And so, the important numbers used in the analysis configuration/setup were:

- **Spatial resolution of step size**: 0.644mm
- **Step size and step number vertical**: 3.864mm @ 15 steps
- **Step size and step number horizontal**: 5.796mm @ 10 steps

The spatial coverage was \((15 \times 6 \times 0.644\text{mm}) = (10 \times 9 \times 0.644\text{mm}) = 57.3161\text{mm}^2\), with \((10\text{horiz.steps} \times 9\text{vectors}) = 90\) vectors, \((15\text{vert.steps} \times 6\text{vectors}) = 90\) vectors. This gives 90x90 = 8100 vectors per file/film frame.

A basic image distortion check of the PIV PC/AT analysis system was also performed. The results are presented in Figure 4. A computer generated PIV image was used to check the imaging/correlation process across the field of view (FOV) of the Kodak Megaplus 1.4 camera system in low resolution mode. The imaging system currently in use uses a single 120mm achromatic lens to image the PIV photographic field to the 640x480 pixel Megaplus camera field.

The process used to check the distortion present in the imaging system involved correlating the computer generated PIV particle pair field at various positions along the imaging field of view, and measuring correlation peak centroid variations. In order to make sure each portion of the field had the same image field to correlate, the Unidex motion control system was used to move the correlating image field to each distortion check position until the entire field was covered. In total, a 6x9 grid was covered at 50% oversampling (the same grid/oversampling parameters used in a normal analysis). The results show distortion levels of less than 1% with a standard error of approximately 0.41%. The distortion pattern could not be characterized as a pincushion or barrel in nature, but rather had a top-to-bottom tilt structure. This is most likely due to minor deviations in the relative orientation of the object/lens/image planes, which should be perfectly parallel to each other. The errors being introduced to the data by this analysis system distortion are minimal, however, and are within/below the acceptable 1-5% PIV accuracy levels.

The basic analysis process included three steps. First, the film was loaded into the analysis system, where it was aligned so that the horizontal and vertical film positions were lined up with the Unidex motion directions. The film was then moved so that the registration point (a star pattern on the right corner of the nozzle output) was properly aligned. This is depicted in Figure 5. The film
was finally moved to the 0,0 analysis position by moving -45mm in the horizontal direction and +15mm in the vertical direction.

The next step involved setting up the configuration file which is described in more detail below. Once the configuration file was properly setup, the analysis system program was run. This process started an automated autocorrelation analysis routine that moved the film in a stepwise manner 10 positions in the horizontal direction (5.796mm each step), and 15 positions in the vertical direction (3.864mm each step). A low resolution (640x480) Kodak Megaplus image was captured at each position where 50% oversampling provided a 9x6 vector field @ a 128x128 pixel resolution (i.e. correlation) size. The output vector field included an ASCII listing of 11 float numbers representing the horizontal and vertical position of the vector, and the centroid positions and peak values for the top three centroid positions in the search box region.

The autocorrelation algorithm used in this set of tests was originally developed in 1993 with two minor upgrades/revisions occurring in 1994 and 1995, respectively. The processing involves eight sequential steps and include: 1) image thresholding, 2) default image pair inclusion, 3) autocorrelation calculation, 4) zero out DC peak, 5) apply search box restriction, 6) apply centroid threshold, 7) compute centroids, and 8) write data to file.

Step 1 involves thresholding the raw image according to a weighted mean of the image intensity level, where the weighting value is provided by the user in the configuration file. The values used in this test varied between 0.9 and 1.05, where raw image values above the product of the average image intensity and the weighting value were set to 255 (the maximum background image value where the PIV images are recorded as black dots on a white background). A set of three very-weak intensity particle images were then included in step 2 in the raw image data array for discerning saturated or totally black image regions on the frame. This step was included to allow void, non-seeded, and obstructed regions of the frame to be easily deleted in the validation process and has no impact on regions with adequate seeding levels present. A standard autocorrelation processing step was then applied to the data in step 3. The autocorrelation DC peak was then zeroed out of the correlation image in step 4 given the user's configuration value for its extent. These values typically ranged from 4-12 pixels extending radially out from the center of the image. Step 5 involved the application of a restricted search box region given user configuration input values for its positioning and extent. Careful consideration and testing was provided in this step to ensure 1) that the box was properly placed, and 2) that its extents allowed for dynamic movement of the particle positions across the entire field of view. Typical search box extents ranged from +/-25 pixels in the axial direction and +/-15 pixels in the transverse direction, which corresponds to velocity dynamic ranges of +600m/s to -200m/s in the axial direction and +/-200m/s in the transverse direction. Step 6 involved application of a user defined centroid threshold level where values below the designated level were set to zero. This level was typically
240 (out of a maximum level of 255). In step 7, a weighted mean centroid computation was then applied to all the remaining correlation peaks in the search box, where correlation patterns with areas > 100 pixels were discarded, and the top three weighted mean centroids were written to file in step 8.

An example configuration file input is provided below. It provides information related to the output file name(s), Kodak Megaplus setup parameters, image thresholding levels, etc.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>software_version_number</td>
<td>1.2</td>
</tr>
<tr>
<td>exposure_level(ms)</td>
<td>90</td>
</tr>
<tr>
<td>#steps_xdimension</td>
<td>10</td>
</tr>
<tr>
<td>#steps_ydimension</td>
<td>15</td>
</tr>
<tr>
<td>output_timefile_name</td>
<td>time54.dat</td>
</tr>
<tr>
<td>image_threshold_level(0-255)</td>
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<tr>
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</tr>
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<td>search_box_xmin(0-128)</td>
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<td>search_box_xmax(0-128)</td>
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<td>pixel_scale_factor(microns/pixel)</td>
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</tr>
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</tr>
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</tr>
<tr>
<td>output_datafile_name</td>
<td>f71r7.dat</td>
</tr>
</tbody>
</table>

PIV analysis system configuration file: **KODAK54.CFG**

The input configuration file supplied various analysis system parameters needed for processing. The system checkout process provided six parameters including the acquisition and analysis magnification factors, the Unidex shift amounts in the x and y directions, and the number of steps in each direction. The initial setup of each roll of film provided ten additional analysis parameters. The exposure level of the Kodak Megaplus camera (in milliseconds) was determined first, where test correlations were used at various exposure levels to optimize the exposure level for a typical frame on a given roll. Image and centroid threshold levels were also evaluated with respect to test correlations at this time. The image threshold factor applies a threshold to the raw image before FFT processing based on the average pixel intensity in the image. The centroid threshold level limits the centroid search to pixel intensity values above a certain level. The DC peak pixels are also zeroed out based on an evaluation of their radial extent out from the correlation image center. Correlation search box limits are then set allowing for movement of the
correlation peak at various positions across the field. And finally, a default peak correlation position is inserted in the event of a totally black or totally white image field.

PIV Data Validation

Following the analysis of all the PIV film frames, a semi-automated PIV vector validation process was performed. These data validation efforts involved two different types of validation processes - individual roll validation and ensemble validation. The individual roll validation processing was done first, and involved several different types of validator algorithms. Two additional ensemble validation steps were then applied to the data that took into account the ensemble mean and standard deviation level at each point in the flow.

The individual roll validation involved 5 steps for the image-shift calibration frames, and 4 steps for the actual data frames. Both the calibration and data files included a bandpass validator, a local median validator, and a 3x3 mean filter processor. An additional ensemble average and manual vector validator step was then applied to the calibration files, while an additional image-shift removal step was applied to the data files. The vector plots in Figure 6 provide a step-by-step example of the results of each validation step from a raw data file input to the final validated file output.

The bandpass validator was applied first, and was used to remove vectors that were obviously bad. A set of high and low threshold levels were chosen for both the u and v components, and if a vector was outside of these high/low threshold ranges, it was zeroed out. Unfortunately, this step required a considerable amount of user input and judgment, and because of this, very liberal limits were chosen for each roll of film. The executable validation program for this step was HILO.EXE with the threshold levels being provided by the configuration file VALIDATE.CFG.

A local median validator was then applied to the data. In this processing step, a given vector position was compared with the median value of its 8 nearest neighbors. If the absolute value of the difference between the local median and the vector was greater than three times the standard deviation of the 8 nearest neighbors, it was zeroed out. No user input was required for this step. The executable validation program for this step was LOCMED.EXE.

A 3x3 mean filter operation was then applied to the data, which involved evaluating the mean of a vector position and its eight nearest neighbors and replacing that vector position with the mean. This step provided a limited amount of smoothing and interpolation to the data, and like the median validator, required no user input. The executable for this step was 3X3MEAN.EXE.

An ensemble average program was then applied to each roll's image-shift calibration file to obtain an average image shift file for that roll. The executable program for this step was ENSEMBLE.EXE, with file name inputs being provided by the file VALADD.CFG.
A final manual vector extraction validation step was applied to each ensemble averaged calibration file to remove obvious outlying vectors. The resulting calibration files were then subtracted from each data file in an image shift bias removal step. The executable program for this step was UNSHIFT.EXE, with file name inputs being provided by VALIDATE.CFG.

Following the individual roll validation, an ensemble bandpass validator was applied to all the data files, which removed vectors outside a given u and v range relative to a preliminary ensemble mean value at each point. The determination of the threshold u and v ranges required user input, and were ultimately chosen to be +/-125m/s for u and +/-75m/s for v. The final ensemble mean validator compared a given vector position to a new preliminary ensemble mean value, and if the absolute value of the difference between the ensemble median and the vector was greater than three times the ensemble standard deviation, it was zeroed out. The executable programs for these two steps were ENS_HILO.EXE and ENS_MEAN.EXE, respectively.

Like the PIV analysis program, the various validation algorithms required the input of configuration text files for validation parameter setup. The individual roll validators used a text file named VALIDATE.CFG, and the ensemble validator used a text file named VALADD.CFG for file name input/output. An example individual roll configuration input file is provided below:

```
software_version_number 1.1
Use_Local_Mean_Validator (y/n)? y
Use_Local_Median_Validator (y/n)? y
Use_Global_Mean_SD_Validator (y/n)? y
Upper_Threshold_Level for U: -9.5
Lower_Threshold_Level for U: -34.0
Upper_Threshold_Level for V: 50.0
Lower_Threshold_Level for V: 41.0
Number_of_Vectors_in_x_direction: 90
Number_of_Vectors_in_y_direction: 90
Default_peak_Amount_in_x_direction: -0.0001
Default_peak_Amount_in_y_direction: 20.000
Input_File_Name f90r9_v4n
Output_Vector_File_Name f90r9_v4t
Output_Stats_File_Name Stats.dat
Input_Calibration_File_Name r9add46_v6
Standard_deviation_Multiplier: 3.0
```

PIV validation configuration file: VALIDATE.CFG

The validation configuration file supplied three basic parameters for the validator algorithms. Upper and lower bounds were provided for the u and v components in the bandpass validator algorithm, a multiplier was provided for the standard deviation amount in the local median validator, and file input/output names were finally provided.
A final part of the data validation processing involved determining vector validation rates (the percentage of actual good vectors extracted from the data relative to the maximum possible that could be extracted). As previously mentioned, a 90x90 vector grid was analyzed for each frame of film, which gives a total possible vector number of 8100 vectors per file. Because the analysis grid setup (see Figure 2) was slightly bigger than the octagonal frame exposure, the maximum vector number was actually limited to only 6935. The plot presented in Figure 7 reflects this maximum vector rate, where a 100% vector rate indicates all possible analyzed positions produced a validated vector (6935 total vectors). Validation rates ranged from ~10-70% per file, with the majority of files falling between 40-50%, and an overall vector rate of approximately 45%.

Results

As previously mentioned, an evaluation of image and autocorrelation signal qualities was performed as part of this test. An initial set of low speed/cold flow PIV photographs produced images of good to excellent quality across the entire field of view. The introduction of heat and increased flow speeds tended to degrade the image quality, however. Some of these effects are depicted in Figure 8. In particular, a blurring of the particle images was noticed just past the nozzle exit, a lack of image pairs was noticed in certain regions of the field, and image 'quads' were recorded in certain regions of the downstream flow. These were most likely due to thermal gradient, light sheet overlap, and light sheet polarization problems, respectively. The image blurring near the nozzle exit was noticed on all of the hot/high speed flow photographs and was consistent in its position, coverage, and effect. A lack of image pairs was noticed in approximately 1/2 of the hot/high speed photographs and 1/4 of the cold/low speed photos, and tended to be present downstream of the nozzle. Image quads were present in about 1/2 of the hot/high speed photographs and tended to be sporadically placed downstream in the main jet core. Examples of the auto-correlation patterns produced by these various particle image qualities are provided in Figure 9. The images with quads produced multiple correlation peaks, the blurred images produced correlations with increased size and lowered SNRs, and the images with no pairs produced uncorrelated results.

A total of 417 data files were available for ensemble and turbulence statistics calculations. Plots depicting the ensemble mean vector field are provided in Figures 10-15. Transverse and axial vector component contour plots are provided in two of the plots, as well as a contour plot of the number of vectors available for the ensemble at each field point. The executable program used in this processing step was ENSEMBLE.EXE, with filename inputs being provided by the configuration file VALADD.CFG.
The ensemble average velocity at each point was then subtracted away from the instantaneous velocity in each file to produce a fluctuating velocity at that point. The involved applying the executable program FLUCT.EXE to each validated data file to produce a new fluctuating velocity file with the new extension *.fie. An example of the fluctuation velocity output vector field is presented in Figure 16.

Several turbulence statistics calculations were then calculated using the fluctuating velocity files, the results of which are presented in Figures 17-19. They include plots of axial and transverse turbulence intensity levels $<u'u'>$ and $<v'v'>$, Reynold's stress $<u'v'>$, and the number of vectors used in the ensemble for each point in the field. The executable program for this processing was named TURBSTAT.EXE.

Two data convergence tests were also applied to the ensemble averaged data. These included convergence of the ensemble axial velocity mean and convergence of the turbulence intensity $<u'u'>$. Data convergence was determined for flow points in the 1) entrainment region, 2) the shear region, and 3) the jet core region. Results are presented in Figures 20 and 21.

Because the data was taken from a plane through the jet axis centerline, and because of the nature of the circular nozzle configuration, the flow exiting the jet was nearly symmetric about the jet axis. This allowed the ensemble average of the data to be increased by folding the data about the jet axis. Results for this increased data ensemble are provided in Figures 22 thru 26. In an attempt to increase the maximum number of data points available for the final ensemble average, a slightly different validated data set was used for the symmetric folded data set ensemble. This validated data set excluded the final ensemble mean validation step, thus concluding with the ensemble bandpass validation step. By doing this, the maximum ensemble number was increased to over 580 in some locations (versus only ~350 available for the ensemble mean validation step). An additional set of fluctuating velocity files were computed based on this alternate ensemble average file, which were used to calculate turbulence statistics data. An additional data convergence test also was performed for the ensemble mean of this new data set and is provided in Figure 27.

Some fluctuations of the image shift bias being introduced into the data were also noticed from film roll to roll, and film frame to frame, which could have an effect on data quality. A study of the amount of fluctuations present, and their effect on the data was consequently done the results of which are presented in Figures 28 thru 30 and Table 1. The Frame-to-Frame variation is depicted in Figure 28 for film Roll #9 which had 15 calibration shots to work with. The axial and transverse image shift values are shown for 9 positions (see Figure 30 for the relative position locations) and showed a positive linear relationship as the frame number increased. An approximate 1.5m/s increase was noticed from frame to frame. A study of the variation of image shift across the field of view using the same 9 points (Figure 29) indicated absolute variations ranging from +5 m/s increase in the lower left corner position for the transverse component, to +
28 m/s for the left axial component position. No real patterns could be discerned. Roll-to-Roll variations are shown in Table 1 where the average standard deviation of each roll was computed. These standard deviation values ranged from 4.88m/s-25.9m/s for the axial component and 4.01m/s to 16.14m/s for the transverse component. Average standard deviations of 13.48m/s and 8.51m/s were computed from these values, respectively. This gives an average standard deviation magnitude of: \(\sqrt{13.48^2 + 8.51^2} = 15.94\text{m/s}\), which gives an indication of the errors being introduced by the image shift, in that the ensemble mean of these calibration frames were used for data reduction, and deviations away from this mean were also present in the data sets. This provides an error estimate due to the image shift variations of 15.94/385 = 4.14% relative to the maximum velocity range of 385m/s in the flow.

Because vector validation rates were only 40-50%, a gaussian filter/interpolation algorithm was developed and applied to the available 417 data files. The algorithm applies a gaussian weighting function for positions in the vector field that do not have vectors present, and uses the 10 nearest neighbors for interpolation. The gaussian weighting gives vector positions close to the center position strong weighting in the interpolation process and positions further away less and less weighting according to a gaussian profile. Vector positions that have valid vectors are not subjected to the interpolation/filtering operation and are left unchanged. The program took the final validated data set (*.fin) as input and output the results in files with the extension *.gfn. A new set of fluctuating velocity files was evaluated using these new interpolated files and were given the file extensions *.gfl. An example of the gaussian interpolator is presented in Figure 31 where the original *.fin file is shown at the top of the figure and the gaussian filter/interpolator output is shown on the bottom.

A 2-point correlator algorithm was finally developed and applied to the gaussian interpolated fluctuating velocity files for several positions in the shear region of the flow. The algorithm calculates 5 NxN matrices according to \(<u'_i u'_j>, <u'_i v'_j>, <v'_i u'_j>, <v'_i v'_j>, and <ij>\), where i and j go from 0 --> N, u' and v' represent the fluctuating velocities at neighboring positions in the flow, and < > represents the ensemble averaging process. The algorithm takes the input from a configuration file named 2PTCOR.CFG, and has an executable file name of 2PT_COR.EXE. The 2-point correlations were calculated for a position in the upper shear region of the flow corresponding to 12.88mm above the jet centerline and 5.15mm downstream of the nozzle. Results are presented in Figure 32.

**Summary**

Over 750 70mm PIV photos were analyzed in the subsonic flow exiting a 1” circular nozzle in an attempt to better understand the turbulence characteristics of its shear layer regions. Custom data analysis and data validation algorithms were developed and applied to a data
ensemble. Results are presented detailing spatial characteristics of the flow including ensemble mean and standard deviation, turbulence intensities and Reynold's stress levels, and 2-point spatial correlations.

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References

Figure 1. Particle Image Velocimetry acquisition system.

Figure 2. Image Field of View coverage.

Figure 3. PIV PC/AT Analysis system.

Figure 4. Analysis system image distortion results.

Figure 5. Image registration and setup.
Figure 6. PIV data validation processing steps.
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Figure 18. Turbulence intensity $<v'v'>$. 

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Figure 20. Data convergence of ensemble mean.

Figure 21. Data convergence of $<u'u'>$. 

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Figure 26. Symmetric folded $<v'v'>$.

Figure 27. Symmetric folded data convergence.
I Frame-to-Frame Image Shift Variation

Figure 28. Variation of frame-to-frame image shift.

Axial

Transverse

Variation of Image Shift Across Field

Figure 29. Variation of image shift across field of view.

Data extraction positions

Figure 30. Measurement locations.

### Roll-to-Roll Image Shift Variations

<table>
<thead>
<tr>
<th>Film Roll</th>
<th>Mean U (m/s)</th>
<th>Mean V (m/s)</th>
<th>Min/Max U</th>
<th>Min/Max V</th>
<th>ave SDU (m/s)</th>
<th>ave SDV (m/s)</th>
<th>SD Mag (m/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Roll 7</td>
<td>23.996</td>
<td>398.195</td>
<td>38.7/12.9</td>
<td>407.6/385.6</td>
<td>6.735</td>
<td>4.011</td>
<td>5.773</td>
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<tr>
<td>Roll 8</td>
<td>-7.272</td>
<td>257.088</td>
<td>-13.9/2.4</td>
<td>265.4/247.7</td>
<td>4.884</td>
<td>4.574</td>
<td>4.729</td>
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<tr>
<td>Roll 11</td>
<td>41.053</td>
<td>400.279</td>
<td>53.7/28.4</td>
<td>407.1/388.3</td>
<td>13.941</td>
<td>9.493</td>
<td>11.417</td>
</tr>
<tr>
<td>Roll 16</td>
<td>4.308</td>
<td>344.766</td>
<td>-2.7/23.2</td>
<td>348.7/335.7</td>
<td>6.893</td>
<td>5.665</td>
<td>6.779</td>
</tr>
<tr>
<td>Roll 17</td>
<td>-46.874</td>
<td>108.034</td>
<td>-63.1/35.4</td>
<td>85.6/122.6</td>
<td>15.326</td>
<td>16.135</td>
<td>15.731</td>
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<tr>
<td>Roll 18</td>
<td>-142.734</td>
<td>612.915</td>
<td>-152.2/134.2</td>
<td>614.1/604.1</td>
<td>25.993</td>
<td>9.058</td>
<td>17.525</td>
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<tr>
<td>Roll 20</td>
<td>56.397</td>
<td>454.381</td>
<td>63.9/48.5</td>
<td>445.2/458.4</td>
<td>18.464</td>
<td>9.529</td>
<td>13.862</td>
</tr>
<tr>
<td>Roll 22</td>
<td>-147.581</td>
<td>436.143</td>
<td>-154.9/134.4</td>
<td>442.3/431.7</td>
<td>14.542</td>
<td>9.349</td>
<td>11.946</td>
</tr>
</tbody>
</table>

Table 1. Variation of image shift across film rolls.
Figure 31. Gaussian interpolator results.
417 file ensemble
12.88mm above centerline
5.15mm downstream

Figure 32. Two-Point correlation results.
4. TITLE AND SUBTITLE
Analysis of Particle Image Velocimetry (PIV) Data for Application to Subsonic Jet Noise Studies

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13. ABSTRACT (Maximum 200 words)
Global velocimetry measurements were taken using Particle Image Velocimetry (PIV) in the subsonic flow exiting a 1 inch circular nozzle in an attempt to better understand the turbulence characteristics of its shear layer region. This report presents the results of the PIV analysis and data reduction portions of the test and details the processing that was done. Custom data analysis and data validation algorithms were developed and applied to a data ensemble consisting of over 750 PIV 70 mm photographs taken in the 0.85 mach flow facility. Results are presented detailing spatial characteristics of the flow including ensemble mean and standard deviation, turbulence intensities and Reynolds stress levels, and 2-point spatial correlations.

14. SUBJECT TERMS
Particle Image Velocimetry, Jet Noise, 2-point Correlations

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