Effects of Chemistry on
Blunt-Body Wake Structure
V. K. Dogra, J. N. Moss, R. G. Wilmoth,
J. C. Taylor, H. A. Hassan

Reprinted from
AIAA Journal
Volume 33, Number 3, Pages 463-469
Effects of Chemistry on Blunt-Body Wake Structure

Virendra K. Dogra*
ViGYAN, Inc., Hampton, Virginia 23666
James N. Moss† and Richard G. Wilmoth*
NASA Langley Research Center, Hampton, Virginia 23681
and
Jeff C. Taylor‡ and H. A. Hassan§
North Carolina State University, Raleigh, North Carolina 27695

Results of a numerical study are presented for hypersonic low-density flow about a 70-deg blunt cone using direct simulation Monte Carlo (DSMC) and Navier–Stokes calculations. Particular emphasis is given to the effects of chemistry on the near-wake structure and on the surface quantities and the comparison of the DSMC results with the Navier–Stokes calculations. The flow conditions simulated are those experienced by a space vehicle at an altitude of 85 km and a velocity of 7 km/s during Earth entry. A steady vortex forms in the near wake for these freestream conditions for both chemically reactive and nonreactive air gas models. The size (axial length) of the vortex for the reactive air calculations is 25% larger than that of the nonreactive air calculations. The forebody surface quantities are less sensitive to the chemistry than the base surface quantities. The presence of the afterbody has no effect on the forebody flow structure or the surface quantities. The comparisons of DSMC and Navier–Stokes calculations show good agreement for the wake structure and the forebody surface quantities.

Nomenclature

\[ A = \text{base area of cone, } \pi d^2/4 \]
\[ C_D = \text{drag coefficient, } 2D/\rho \omega V_f A \]
\[ C_f = \text{skin-friction coefficient, } 2\tau_f/\rho \omega V_f^2 \]
\[ C_h = \text{heat transfer coefficient, } 2q/\rho \omega V_f \]
\[ \varphi = \text{pressure coefficient, } 2p/\rho \omega V_f^2 \]
\[ D = \text{drag} \]
\[ d = \text{base diameter, } 2 m \]
\[ d_{\text{ref}} = \text{molecular diameter at reference temperature} \]
\[ K_n = \text{Knudsen number, } \lambda/d \]
\[ M = \text{Mach number} \]
\[ M = \text{molecular weight of air, } 28.96 \text{ g/mole} \]
\[ N = \text{Avogadro's number, } 6.02252 \times 10^{26} \text{ particles/kg-mole} \]
\[ N_2 = \text{atomic nitrogen} \]
\[ O = \text{atomic oxygen} \]
\[ O_2 = \text{molecular oxygen} \]
\[ \rho = \text{density} \]
\[ q = \text{heat flux} \]
\[ R_b = \text{cone base radius} \]
\[ R_c = \text{corner radius} \]
\[ R_e = \text{Reynolds number, } \rho V_d/\mu \]
\[ R_{e_{\infty}} = \text{total Reynolds number, } Re_{\infty}(\mu_{\infty}/\mu_{stag}) \]
\[ R_e = \text{cone nose radius} \]
\[ R = \text{universal gas constant, } 8.3143 \text{ J/mole-K} \]
\[ S = \text{speed ratio, } V_f/\sqrt{M/2RT} \]
\[ s = \text{distance along the body surface measured from the stagnation point} \]
\[ \tilde{s} = \text{temperature exponent of the coefficient of viscosity} \]
\[ T = \text{thermodynamic temperature} \]

\[ T_{\infty} = \text{overall kinetic temperature} \]
\[ T_w = \text{surface temperature} \]
\[ u = \text{axial velocity} \]
\[ v = \text{velocity} \]
\[ v = \text{radial velocity} \]
\[ X = \text{mole fraction} \]
\[ x = \text{axial distance from stagnation point measured along symmetry axis} \]
\[ x_a = \text{location of rear stagnation point} \]
\[ x_b = \text{location of wake stagnation point} \]
\[ y = \text{radial distance from symmetry axis} \]
\[ \Gamma = \text{Gamma function} \]
\[ \Delta = \text{size of the vortex, } (x_b - x_a)/d \]
\[ \lambda = \text{mean free path} \]
\[ \mu = \text{dynamic viscosity} \]
\[ \rho = \text{density} \]
\[ \sigma = \text{collision cross section} \]
\[ \sigma = \text{shear stress} \]

Subscripts

\[ \text{ref} = \text{reference value} \]
\[ \text{stag} = \text{stagnation point} \]
\[ w = \text{surface values} \]
\[ \infty = \text{freestream values} \]

Introduction

THERE is a lack of experimental and computational data for blunt-body wake flows under rarefied flow conditions. Precise determination of wake closure is a critical issue for aerobrakes because the low lift-to-drag ratio aeroshell designs impose constraints on payload configuration. The payload must fit into the wake cone to minimize the heating since a heating spike is generally associated with reattachment of the separated flow in the near wake. Because of the complicated nature of the wake flow a perception exists that the wake aerothermodynamics cannot be predicted accurately. A number of fundamental issues exist concerning such flows: 1) What role does thermochemical nonequilibrium play in the near wake? 2) How does the wake structure change as a function of rarefaction? 3) To what limits is the continuum modeling valid as rarefaction in the wake is progressively increased? Only recently, computational investigations of blunt-body wake structure have begun to answer some of the previous questions and to
isolate critical features of the wake structure of planetary probes and aerobrakes.

Generally two methods are used to simulate the wake flows at high altitudes. One is the continuum approach in which a set of model equations is solved numerically, and normally this set is the Navier–Stokes equations. The Navier–Stokes modeling becomes inadequate for large local Knudsen numbers such as those occurring when the relatively high-density forebody flow expands into the wake. The second method is of a molecular nature where a direct physical simulation is done by following the motion and interaction of modeled molecules. This method is equally valid at low and high local Knudsen numbers, and therefore it is more appropriate to simulate the wake flows with the molecular method under rarefied conditions. In the present study, computational codes representative of both methods are used to simulate hypersonic wake flows about a 70-deg blunt cone. The molecular simulations are achieved with Bird’s12–14 direct simulation Monte Carlo (DSMC) method, whereas the continuum simulations are performed using the Navier–Stokes code developed by Olynick and Hassan15 and Olynick et al.16

The purpose of the present paper is to provide an improved understanding of the effects of chemistry on blunt-body wake structure at flight conditions and to compare the results with Navier–Stokes calculations with slip boundary conditions. In addition, the DSMC calculations are also performed for a 70-deg blunt cone with a cylindrical as well as a proposed Mars Environmental Survey (MESUR) Pathfinder probe afterbody configurations.

Computational Method and Boundary Conditions

Both the molecular and continuum methods used in the present calculations are briefly described next.

Molecular Method

The direct simulation Monte Carlo (DSMC) method12–14 is used for the present calculations. The method and requirements for application of DSMC have been presented in previous publications17,18 and are not repeated here.

The computational domain used for the calculations is large enough to capture most of the body disturbance at the upstream and side boundaries. Thus, freestream conditions are specified at these boundaries. The flow at the downstream outflow boundary is supersonic, and vacuum conditions are specified.

The flowfield was divided into 18 regions and a fine grid resolution was used for cells in the wake regions. The cell dimension normal to the body surface in the forebody regions was on the order of half of the local mean free path. The cell dimension normal to the surface in the wake regions was less than the local mean free path. Further, study of grid resolution is given in Appendix A of Ref. 19. Steady state was assumed when the number of simulated molecules in each region achieved a fixed value within fluctuations of 1%. The average number of simulated molecules in a cell was 20 at steady state. The final results were obtained through a time-averaged solution over a large number of time steps.

The molecular collisions are simulated by the variable hard sphere (VHS) molecular model. This model employs the simple hard-sphere angular-scattering law so that all directions are equally possible for the postcollision velocity in the center-of-mass frame of reference. However, the collision cross section is a function of the relative energy in the collision. The freestream viscosity and mean free path are evaluated based on N2 species using the VHS collision model with $T_{\text{ref}} = 2880 \, \text{K}$, $d_{\text{ref}} = 3.08 \times 10^{-10} \, \text{m}$, and $\bar{s} = 0.73$. Energy exchange between the translational and internal modes is modeled by the Larsen–Borgnakke statistical model20 with rotational and vibrational relaxation numbers of 5 and 30, respectively.

Continuum Method

The Navier–Stokes solver consists of an axisymmetric three-temperature, five-species implicit code. The set of equations solved consist of global mass, species mass, axial and radial momentum, global energy, rotational, and vibrational energy conservation equations. The code uses Roe’s upwind scheme for the spatial inviscid fluxes, achieving second-order accuracy with the MUSCL scheme. The time integration is accomplished using an implicit lower-upper symmetric Gauss-Seidel (LU-SGS) scheme. This scheme was chosen because it only requires the inversion of a diagonal matrix at each point in the flowfield. With the large number of equations being solved, this is an attractive feature. A complete description of this method and modeling is presented in Ref. 15.

To account for the effects of the Knudsen layer that develops on the surfaces in low-density flows, slip boundary conditions are used. The modeling employed accounts for velocity, temperature, and species concentration slip effects. A more detailed description of the slip boundary conditions used is given in Ref. 16.

As shown in some previous comparisons between solutions using the DSMC method and the Navier–Stokes equations16, a meaningful comparison can be achieved provided the physical modelings employed by the two methods are matched as closely as possible. By doing this, the effects of using different physical models can be deduced, and the differences between the two solution procedures can be better observed. Thus, the chemical kinetic model and relaxation rates employed in the DSMC method17 are also employed in the continuum calculations.

Freestream and Wall Conditions

The freestream conditions considered are those experienced by a typical space vehicle at an altitude of 85 km during Earth entry and are listed in Table 1. Three configurations—1) a 70-deg blunt cone, 2) a 70-deg blunt cone with cylindrical afterbody, and 3) a proposed Mars Environmental Survey (MESUR) Pathfinder probe body—are considered in the present calculations. The base diameter is 2.0 m for each of these configurations. Therefore, the forebody configuration is the same as that proposed15 for the MESUR Network probes (16 total). Since the current MESUR Pathfinder probe has a 2.65-m base diameter, the third configuration is the scaled Pathfinder probe. These configurations are shown in Fig. 1. The freestream parameters along with selected results are summarized in Table 2. The freestream mean free path is based on the VHS model, and it is calculated from the relation (see Ref. 13)

$$\lambda_{\infty} = \frac{(T_{\infty}/T_{\text{ref}})^\alpha}{\sqrt{2\pi n_0 \sigma_{\text{eff}} (2 - \omega)^\alpha \Gamma(2 - \omega)}}$$

$$\omega = \bar{s} - \frac{1}{2}$$

Table 1 Freestream conditions

<table>
<thead>
<tr>
<th>Altitude, km</th>
<th>$\rho_\infty \times 10^6$, kg/m³</th>
<th>$V_\infty$, km/s</th>
<th>$T_\infty$, K</th>
<th>$M_\infty$</th>
<th>$X_{O_2}$</th>
<th>$X_{N_2}$</th>
<th>$\lambda_{\infty}$, mm</th>
</tr>
</thead>
<tbody>
<tr>
<td>85</td>
<td>7.955</td>
<td>7.0</td>
<td>180.65</td>
<td>25.98</td>
<td>0.2372</td>
<td>0.7628</td>
<td>7.189</td>
</tr>
</tbody>
</table>

$^a$ $T_{\infty} = 1000 \, \text{K}$ and $\mathcal{M} = 28.96 \, \text{g/mole}$. 

![Fig. 1 Blunt cone and afterbody configurations.](image)
Comparison of DSMC and Navier–Stokes Results
Comparisons of the chemical compositions from DSMC and Navier–Stokes calculations are shown in Fig. 2. Figures 2c and 2d show that the Navier–Stokes calculations predict slightly lower values of atomic oxygen and atomic nitrogen in the wake region compared with the DSMC results. The mole fraction of atomic oxygen in the wake region predicted by Navier–Stokes (with slip boundary condition) calculations is about 12% lower than that calculated by DSMC simulations (Fig. 7a), whereas the mole fraction of atomic nitrogen predicted by the Navier–Stokes calculations is about 18% lower near the base, and this difference decreases gradually in the downstream direction (Fig. 7b).

The radial nondimensional density and axial velocity profiles (Figs. 4a and 4b) show very good agreement between DSMC and the Navier–Stokes calculations in the wake region. Figure 8 shows that both the DSMC and the Navier–Stokes calculations predict a steady vortex in the wake region, and furthermore both calculations predict the same size (axial length), $\Delta = 0.77$ (Fig. 5).

Comparisons of DSMC and Navier–Stokes (with slip boundary condition) calculations of the surface pressure and surface heating rate are shown in Figs. 6a and 6b. These surface quantities are shown in semilog scale as a function of nondimensional distance ($s/R_n$) along the surface measured from the stagnation point to give better perspective of the magnitudes along the base plane. Along the forebody, Navier–Stokes and DSMC results are in good agreement for both pressure and heating rate. The surface pressure and heating rate along the base surface calculated by Navier–Stokes calculations are generally higher than the DSMC results (Figs. 6a and 6b).
DSMC Calculations of the Blunt Body with Afterbody Configurations

DSMC calculations were also performed for a 70-deg blunt cone with two afterbody configurations: 1) a cylindrical afterbody and 2) a proposed afterbody configuration of the MESUR Pathfinder probe. These afterbody configurations were included to examine the impact on the surface heating and the flowfield features.

Figures 9a and 9b show streamline plots for the cylindrical and MESUR afterbody configurations, respectively. It can be seen from these figures that the cylindrical afterbody has developed two steady vortices (Fig. 9a), whereas for the MESUR afterbody only one steady vortex exists in the wake as shown in Fig. 9b. The comparisons of surface pressure, heat transfer, and skin-friction coefficients for the blunt body and two afterbody configurations are shown in Figs. 10a–10c, respectively. The distributions of surface pressure and heat transfer coefficients on the MESUR afterbody surface are very close to the distributions on the base surface of the blunt body (Figs. 10a and 10b), whereas for the cylindrical afterbody the heat transfer rate distribution on much of the afterbody surface is small compared with blunt-body base and MESUR afterbody surfaces.

Concluding Remarks

Axisymmetric DSMC and Navier–Stokes (with slip boundary conditions) calculations of flows about a 70-deg blunt cone have been performed for flow conditions experienced by a space vehicle at an altitude of 85 km and a velocity of 7 km/s during Earth entry. Particular emphasis is given to the effects of chemistry on the near-wake structure and the surface quantities. The surface quantities of the afterbody surface are also analyzed.

Essentially, all of the molecular oxygen and about half of the molecular nitrogen are dissociated before reaching the body surface. There is species separation among heavy (N₂) and light (O and N) species as the flow expands into the wake region. The density in the wake for the nonreacting gas model is slightly lower than the reacting model. The wake stagnation point for the reacting gas lies downstream of the nonreacting gas wake stagnation point. The base heating rate for the nonreacting gas is 240% larger than that of the reacting gas model with a noncatalytic surface. The comparison of the wake results predicted by the DSMC and the Navier–Stokes calculations shows good agreement for the flowfield quantities. The surface pressure and heating rate along the base surface calculated by the Navier–Stokes calculations are generally higher than the DSMC results. The presence of the afterbody has no effect on the forebody flowfield or the surface quantities.

Acknowledgment

Support for V. K. Dogra by NASA Contract NAS1-19237 is gratefully acknowledged.
References


