Parametric Analysis of Cyclic Phase Change and Energy Storage in Solar Heat Receivers

Carsie A. Hall, III, Emmanuel K. Glakpe, and Joseph N. Cannon
Howard University
Washington, DC

Thomas W. Kerslake
Lewis Research Center
Cleveland, Ohio

Prepared for the
32nd Intersociety Energy Conversion Engineering Conference
cosponsored by AIChE, ANS, SAE, AIAA, ASME, and IEEE
Honolulu, Hawaii, July 27—August 1, 1997
PARAMETRIC ANALYSIS OF CYCLIC PHASE CHANGE AND
ENERGY STORAGE IN SOLAR HEAT RECEIVERS

Carsie A. Hall, III, Emmanuel K. Glakpe*, and Joseph N. Cannon
School of Engineering, Howard University, Washington, D.C. 20059
* (202) 806-7741 (Phone) • (202) 806-5258 (Fax)
* glakpe@cldc.howard.edu

Thomas W. Kerslake
NASA Lewis Research Center, Cleveland, Ohio 44135
(216) 433-5373 (Phone) • (216) 433-2995 (Fax)
Thomas.W.Kerslake@lerc.nasa.gov

ABSTRACT
A parametric study on cyclic melting and freezing of an encapsulated phase change material (PCM), integrated into a solar heat receiver, has been performed. The cyclic nature of the present melt/freeze problem is relevant to latent heat thermal energy storage (LHTES) systems used to power solar Brayton engines in microgravity environments. Specifically, a physical and numerical model of the solar heat receiver component of NASA Lewis Research Center's Ground Test Demonstration (GTD) project was developed. Multi-conjugate effects such as the convective fluid flow of a low-Prandtl-number fluid, coupled with thermal conduction in the phase change material, containment tube and working fluid conduit were accounted for in the model. A single-band thermal radiation model was also included to quantify reradiative energy exchange inside the receiver and losses through the aperture. The eutectic LiF-CaF₂ was used as the phase change material (PCM) and a mixture of He/Xe was used as the working fluid coolant. A modified version of the computer code HOTTube was used to generate results in the two-phase regime. Results indicate that parametric changes in receiver gas inlet temperature and receiver heat input effects higher sensitivity to changes in receiver gas exit temperatures.

NOMENCLATURE
A solid cross-sectional area
C specific heat of solid regions
Cₚ specific heat of working fluid
f geometric view factor
h,h* specific enthalpy, heat transfer coefficient
hₜₚ PCM latent heat of fusion
L active tube or cavity length
m mass flow rate
M total number of axial nodes along tube
n outer unit normal
N total number of tubes in receiver
P wetted perimeter
q" heat flux
Q heat transfer rate
r radial location
R thermal resistance
S* geometric shape factor
t time
T temperature
U velocity vector
W width of PCM region
X PCM liquid fraction
z axial location
κ shell loss function
θ dimensionless working fluid temperature
ρ density
σ Stefan-Boltzmann constant
ω turboalternator TAC speed

Subscripts
abs absorbed
ap aperture
avg,max average, maximum
cav receiver cavity
ch finned-tube fluid channel
f working fluid
in, out working fluid inlet, working fluid outlet
ref reference value

Superscripts
n previous time level
n+1 current time level
INTRODUCTION

The present paper is an extension of a previous paper (Hall, Ill et al., 1997) by the present authors, in which a code validation exercise was undertaken. Numerical results generated by the computer code HOTTube, which modeled the thermal performance of the solar heat receiver component of the Ground Test Demonstration (GTD) project at the NASA Lewis Research Center, were compared with available experimental results.

The intermittent nature of solar energy availability for Earth-orbit applications presents a particular challenge for space power management schemes during traversal into Earth's shadow (eclipse phase). One alternative to photovoltaics with battery storage is solar dynamics with latent heat thermal energy storage (LHTES) via solar heat receivers. Solar heat receivers are very instrumental components in the production of electric power via solar dynamic power systems (SDPSs). In a typical operation, the SDPS uses: 1) a concentrator to collect and focus the incident energy onto the aperture plane of a central receiver, 2) a central receiver to collect and distribute, with minimal losses, the reflected energy from the concentrator, 3) working fluid tubes aligned along the periphery of the receiver to absorb the distributed energy as heat, thus, raising the temperature of the working fluid (typically a low-Prandtl-number fluid) flowing through the tubes, 4) a turbine to expand the high temperature working fluid to produce mechanical work via a rotating shaft, 5) a compressor to circulate the working fluid through the working fluid tubes, and 6) an alternator to convert mechanical shaft motion into electric power. A recuperator is added to increase the thermal efficiency of the thermodynamic cycle (typically a closed Brayton cycle as depicted in Fig. 1).

Solar heat receivers employing encapsulated phase change materials (PCMs) have the advantage over sensible heat receivers of requiring less mass while producing higher energy storage densities. This, in turn, makes them ideal candidates for energy storage in the space environment where temperatures are sufficiently high and PCMs with high latent heats of fusion become indispensable.


In the present paper, a physical and numerical model is developed to study the cyclic behavior of the solar heat receiver component of the aforementioned GTD system. A parametric analysis is undertaken to delineate sensitivities to controllable and measurable parameters such as receiver gas inlet temperature, receiver heat input, and TAC speed (via an equivalent working fluid mass flow rate). Predicting the changes in thermal performance as a result of changes in parameters is critical in determining changes in the so-called thermal state-of-charge (SOC) of solar heat receivers. Knowledge of the SOC allows for better control strategies relating to power management schemes during such operations as peak power demand and emergency shutdowns with subsequent restarts.

DESCRIPTION OF THE GTD SYSTEM

The Ground Test Demonstration (GTD) project is the world's first full scale demonstration of reliable production of electric power via solar dynamics (SD) technology. This government/industry collaboration is carried out in the NASA Lewis Research Center's large thermal/vacuum facility (tank 6). This facility is equipped to provide simulated solar flux in high vacuum, similar to that which is encountered in Low-earth orbit.
The primary objectives of this project are to demonstrate, using flight prototypical components, that system power delivered and system efficiency both fall within design target. Moreover, most of the hardware used in the GTD system are derived from the SD system designed for the Space Station Freedom program.

The 2 kW (nominal) GTD system consists of an off-axis solar concentrator and solar heat receiver with latent heat thermal energy storage (LHTES), both of which are integrated with a closed Brayton engine (power conversion unit or PCU). A more complete description of the GTD system can be found in the paper by Shaltens and Mason (1996).

GTD SOLAR HEAT RECEIVER MODELING

Problem Description

The physical geometry for the present study is depicted in Fig. 2 and the more detailed single-tube model is shown in Fig. 3. It is assumed that each tube in the solar receiver is imparted with the same incident solar flux; therefore, only a single tube needs to be analyzed, with a subsequent summation over all tubes to quantify the total receiver thermal performance.

![GTD Solar Heat Receiver Design](image)

**Fig. 2** GTD solar heat receiver design (provided by AlliedSignal Aerospace).

**GTD Specifications**

The specifications for the solar heat receiver of the GTD system used for modeling, in which the present numerical results reflect, are as follows:

- effective cavity diameter = 1.56 ft (47.55 cm)
- aperture diameter = 7 in (17.78 cm)
- active tube length = 2 ft (60.96 cm)
- canister outer diameter = 1.78 in (4.52 cm)
- hydraulic diameter = 0.045 in (0.1143 cm)
- number of tubes in the receiver = 23
- number of canisters per tube = 24
- canister material = superalloy Haynes 188
- PCM = LiF-CaF₂
- working fluid = helium/xenon (He/Xe)

The GTD design is essentially a scale-down version of the Space Station Freedom SDPS, which was designed to yield a nominal alternator power output of 35 kWₑ.

**Governing Equations**

The generalized integral equation governing the evolution of the enthalpy per unit mass for a region (denoted as k) is given by

\[
\frac{d}{dt} \int_{V_k} \rho_h h_i dV_i = -\int_{S_k} \rho_h h_i \mathbf{U}_k \cdot \mathbf{n}_k dS_k - \int_{S_k} \mathbf{q}_k \cdot \mathbf{n}_k dS_k \tag{1}
\]

which is coupled to the temperature of the kth region by the general equation of state

\[
h_k - h_{ref} = \int c_k (T_k') dT_k' \equiv c_k (T_k - T_{ref}) \tag{2}
\]

for constant \( c_k \), where each of the k regions is identified as follows: k=1 (outer canister region); k=2 (PCM region); k=3 (inner canister region); k=4 (working fluid tube region); k=5 (working fluid region). In the solid regions and liquid PCM region (due to the assumption of no convective motion), \( \mathbf{U}_k = 0 \).

**Discrete Representations**

It should be stated at the outset that the containment canister outer and inner regions, along with the working fluid tube region, are all considered radially lumped. As a result, the radial index \( j \) corresponding to the representative temperatures of those regions are \( j=1, j=j\text{max}-1 \), and \( j=j\text{max} \) for the outer canister, inner canister, and working fluid tube regions, respectively. The remaining PCM region is divided into \( j\text{max}-3 \) nodes, for each ith axial location along the tube.

Applying Eq. 1 to a control volume at the ith outer canister location (k=1) along the tube results in
is written for the present configuration as
\[
\theta_{i}^{n+1} = \frac{T_{i}^{n+1} - T_{f}^{n+1}}{T_{i}^{n+1} - T_{in}^{n+1}} = e^{-\frac{P_{eh}S^{*}h_{ch}}{m_{eh}c_{p}}}
\]

where \(P_{eh}\) is the channel wetted perimeter, \(m_{eh}\) is the channel mass flow rate, and \(S^{*}\) is a geometric shape factor (estimated to be in the range \(1 \leq S^{*} \leq 1.2\)), used to account for the degree of departure from triangularity of the finned-tube cross-section.

Finally, the net rate of axially convected enthalpy, used in Eq. 7, is expressed as
\[
\dot{Q}_{f_{i}}^{n} = mc_{p}\left(\frac{T_{f_{i+1}}^{n} - T_{f_{i}}^{n}}{R_{\Delta x}}\right)
\]

### Thermal Radiation Model

An energy balance on the \(i\)th node results in the following equation governing the net rate of energy absorbed at the \(i\)th node:
\[
\dot{Q}_{abs_{i}} = \dot{Q}_{r_{i}} + \dot{Q}_{ap_{i}} - \dot{Q}_{shell_{i}}
\]

where for \(i = 1, 2, \ldots, M\)
\[
\dot{Q}_{r_{i}} = \frac{A_{i}}{N} \sum_{j=1}^{M+2} \left(\frac{T_{a_{j}}^{d} - T_{a_{i}}^{d}}{R_{a_{i},j}}\right)
\]

and the receiver shell loss per node is given by
\[
\dot{Q}_{shell_{i}} = \kappa \frac{T_{avg}}{NM}
\]

In this equation, the function \(\kappa(T_{avg})\) is recommended by Ensworth et al. (1996) to be
\[
\kappa(T_{avg}) = b \left(\frac{T_{avg}}{T_{ref}}\right)^{4}
\]

where \(b = 0.82\), \(T_{ref} = 1860\) R (1033 K), and \(T_{avg}\) is the instantaneous, spatially-averaged canister outer surface temperature, given by
\[
T_{avg}(t) = \frac{1}{L_{ext}} \int_{0}^{L_{ext}} T_{i}(z, t) \, dz
\]
Modified HOTTube Code
The numerical results presented in this present paper were generated using a modified version of the computer code HOTTube, which is a transient, time-explicit, axisymmetric total receiver thermal analysis code. HOTTube was initially developed by AlliedSignal Aerospace for the Space Station Freedom solar heat receiver. For a more complete description of modified HOTTube, including grid size and time step requirements, see the paper by Hall, III et al. (1997).

RESULTS AND DISCUSSION
The results presented in this section pertain to a baseline maximum insolation orbit for the orbital altitude corresponding to 92 minutes total orbit time with 28 minutes of eclipse. This maximum insolation of approximately 1.26 suns (1 sun = 1.37 kW/m²) is incidentally, the maximum output capability of the solar simulator lamps of the GTD system. The corresponding rate of energy crossing the aperture plane of the receiver during the simulated sun period is approximately 12.6 kW. Another point of interest is a newly determined SD-Mir design point (determined by AlliedSignal Aerospace), which corresponds to a receiver heat input of 15.1 kW and TAC operating speed of 53,000 RPM. It should be further pointed out that due to the maximum power output capability of the GTD solar simulator lamps, a pseudo-SD-Mir design point was effected (in the GTD experiment) by increasing the sun period to 77 min during the first two cycles to get the equivalent amount of energy into the receiver.

The nominal SD-Mir design point operating speed of the GTD engine’s turboalternator work-producing shaft is 53,000 RPM, which yields a working fluid mass flow rate of approximately 0.3385 lbm/s (154 g/s). A map of TAC speed versus mass flow rate is provided by Shaltens and Mason (1996), from which a linear curve fit performed by the present authors is given by

\[ m = 0.0629 + 5.2 \times 10^{-6} \omega \]

where \( \omega \) is the TAC speed in RPM and \( m \) is the working fluid mass flow rate in lbm/s.

Solar Receiver Energy Balance
As pointed out in Hall, III et al. (1997), an important consideration in the numerical prediction of the solar receiver’s thermal performance is the instantaneous overall energy balance. This is done to account for every unit of energy crossing the aperture plane per unit time. Fig. 4 is a plot of the solar receiver’s energy budget for the SD-Mir design point. The profile for the rate of energy crossing the aperture plane (labeled \( \dot{Q}_{\text{in}} \)) resembles a square pulse function, which illustrates the switching nature of consecutive sun periods and eclipse periods.

If the receiver is truly balanced, then the sum (labeled \( \dot{Q}_{\text{total}} \)) of the rate of energy extracted by the gas (labeled \( \dot{Q}_{\text{gas}} \)), rate of energy lost by reradiation through the aperture and rate of energy lost through the receiver shell (labeled \( \dot{Q}_{\text{loss}} \)), and rate of energy stored inside the receiver (labeled \( \dot{Q}_{\text{stor}} \)) should also follow this square pulse function. This is indeed the case, as shown in Fig. 4, with a maximum error of less than 3 percent. This small error is primarily due to the receiver shell heat loss approximation.

![Energy Budget for the SD-Mir Design Point](image)

**Fig. 4** Solar receiver energy balance for the SD-Mir design point operating conditions.

![Numerical prediction of maximum canister temperature, average canister temperature, and receiver gas exit temperature over 9 orbit cycles.](image)

**Fig. 5** Numerical prediction of maximum canister temperature, average canister temperature, and receiver gas exit temperature over 9 orbit cycles.
Temperature and Melt Fraction Predictions

Fig. 5 shows the temporal progression of maximum canister outer surface temperature, average canister outer surface temperature, and receiver gas exit temperature from startup to 9 orbit cycles. The receiver heat input is fixed at 15.1 kW and the TAC speed varies from zero at startup to 53,000 RPM. The receiver gas inlet temperature is fixed at 1508 R (838 K).

The transient operation for the orbital simulations performed to reach the SD-Mir design point is detailed as follows:

1) the startup mass flow rate is fixed at 0.005 lbm/s (2.3 g/s) until the maximum canister temperature reaches 1900 R (1056 K), after which it is increased to 0.3385 lbm/s (154 g/s) (this occurs during the 2nd cycle); faster heatup of the receiver is effected as a result;
2) also during startup, the receiver gas exit temperature is fed back to the receiver inlet until the receiver inlet reaches 1508 R (838 K), which is accomplished during the 1st cycle; this is an expedient computational scheme that advances the numerical solution to the point where higher fidelity modeling can be initiated;
3) during the first two cycles, the total orbit period is 105 min with a sun period of 77 min, after which the total orbit period is changed to the baseline 92 min with a sun period of 64 min;

From the figure, it is shown that balanced orbit conditions are reached on the 4th orbit. A balanced orbit is declared when the difference between all calculated temperatures is less than 2 R (1.1 K) between successive sunrise and sunset conditions. It is further observed that over most of the orbit cycles

\[ T_{\text{max}} > T_{\text{out}} > T_{\text{avg}} \]

which is what is typically observed during experimental test runs. In addition, perusal of the numerical data reveals that the maximum canister, average canister, and receiver gas exit temperatures at sunset are approximately 2007 R (1115 K), 1904 R (1058 K), and 1994 R (1108 K), respectively, for the balanced orbits. These temperatures indicate that during the sun period, a local superheat event occurred that caused a sharp rise in receiver gas exit temperature significantly beyond the PCM melting point of 1873 R (1040 K). This is corroborated by the significant rise in receiver gas heat input as shown in Fig. 4, where over the sun period, the gas heat input increases from a steady value of approximately 7.7 kW to approximately 10.2 kW at sunset.

The corresponding fraction of receiver PCM in the liquid phase is illustrated in Fig. 6. Recall that the melting point of LiF-CaF₂ is 1873 R (1040 K) and its latent heat of fusion is 340 Btu/lbm (789 kJ/kg). For the GTD solar heat receiver, the total mass of PCM is 53 lbm (24 kg) which corresponds to a maximum latent storage capacity of 18,020 Btu (19 MJ or 5.3 kW hr). It is observed that the maximum liquid fraction, which occurs on sunset for all representative cycles, reaches a maximum of approximately 61 percent during the heatup phase and 59 percent during the balanced orbit phases. However, at the end of the eclipse phase (sunrise), approximately 12 percent of liquid PCM remains in the receiver for the balanced orbit cycles.

Sensitivity to Receiver Gas Inlet Temperature

Fig. 7 Effect of receiver gas inlet temperature on receiver gas exit temperature over 9 orbit cycles for the pseudo-SD-Mir design point.
Shown in Figs. 7 and 8 are the relative sensitivities of receiver gas exit temperature and average canister surface temperature to receiver gas inlet temperature. Sensitivities are shown for an increase in receiver gas inlet temperature from 1508 R (838 K) to 1608 R (893 K). For this case, the receiver heat input is fixed at 12.6 kW and the TAC speed is held at 53,000 RPM, which corresponds to a gas mass flow rate of 0.3385 lbm/s (154 g/s). It appears that the receiver gas exit temperature is more responsive to the change in receiver gas inlet temperature, as expected. This is primarily due to the smaller thermal interaction time scale for the gas than for the diffusion time scale through the solid layers of canister material and PCM. In fact, over the balanced orbit cycles, the 100 R (56 K) increment in receiver inlet temperature effects a 118 R (66 K) increase in receiver gas exit temperature at sunset and a 99 R (55 K) increase in average canister surface temperature at sunset. These are increases over that which occurs at sunset for a receiver inlet temperature of 1508 R (838 K). The corresponding changes for sunrise conditions over the balanced orbit cycles result in a 202 R (112 K) increase in receiver gas exit temperature and a 171 R (95 K) increase in average canister surface temperature. Also observed in the figures are the qualitative changes in the shapes of the temperature profiles, which for the higher gas inlet temperature, results in a A-shape over the entire orbit period. This is an indication that the system moves away from orbital steady-state conditions.

The sensitivities to changes in receiver heat input are illustrated in Figs. 9 and 10. For these cases, the receiver gas inlet temperature is fixed at 1508 R (838 K) and the TAC speed is held at 53,000 RPM, which corresponds to a gas mass flow rate of 0.3385 lbm/s (154 g/s). The receiver heat input is varied from the pseudo-SD-Mir design point value of 12.6 kW to the actual SD-Mir design point value of 15.1 kW. In the balanced orbit regime, the additional 2.5 kW results in an increase in receiver gas exit temperature of 122 R (68 K) at sunset and an increase of
194 R (108 K) at sunrise. Similarly, the additional 2.5 kW causes an 84 R (47 K) increase in average canister surface temperature at sunset and a 112 R (62 K) increase at sunrise. In Fig. 9, the qualitative A-shape is retained for the receiver gas exit temperature whereas in Fig. 10, there is a departure from the A-shape trend for the average canister surface temperature. This departure is attributed to a local superheat event that occurred in one of the containment canisters.

CONCLUSIONS
A physical and numerical model of the solar heat receiver component of NASA Lewis Research Center's Solar Dynamic (SD) Ground Test Demonstration (GTD) project has been developed. A parametric study was performed to delineate changes in receiver gas exit temperature and average canister surface temperature due to changes in receiver gas inlet temperature and receiver heat input. Results showed that receiver gas exit temperatures were more sensitive to changes in receiver gas inlet temperatures than to changes in receiver heat input. It was also shown that changes in receiver heat input effects a higher sensitivity to changes in receiver gas exit temperatures.

ACKNOWLEDGMENT
The work reported in this paper was sponsored by a grant to Howard University from the NASA Lewis Research Center under grant number NAG3-1907.

REFERENCES

### Abstract

A parametric study on cyclic melting and freezing of an encapsulated phase change material (PCM), integrated into a solar heat receiver, has been performed. The cyclic nature of the present melt/freeze problem is relevant to latent heat thermal energy storage (LHTES) systems used to power solar Brayton engines in microgravity environments. Specifically, a physical and numerical model of the solar heat receiver component of NASA Lewis Research Center’s Ground Test Demonstration (GTD) project was developed. Multi-conjugate effects such as the convective fluid flow of a low-Prandtl-number fluid, coupled with thermal conduction in the phase change material, containment tube and working fluid conduit were accounted for in the model. A single-band thermal radiation model was also included to quantify reradiative energy exchange inside the receiver and losses through the aperture. The eutectic LiF-CaF₂ was used as the phase change material (PCM) and a mixture of He/Xe was used as the working fluid coolant. A modified version of the computer code HOTTube was used to generate results in the two-phase regime. Results indicate that parametric changes in receiver gas inlet temperature and receiver heat input effects higher sensitivity to changes in receiver gas exit temperatures.