Thermal Modeling and Analysis of a Cryogenic Tank Design Exposed to Extreme Heating Profiles

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THERMAL MODELING AND ANALYSIS OF A CRYOGENIC TANK DESIGN EXPOSED TO EXTREME HEATING PROFILES

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Abstract

A cryogenic test article, the Generic Research Cryogenic Tank, was designed to qualitatively simulate the thermal response of transatmospheric vehicle fuel tanks exposed to the environment of hypersonic flight. One-dimensional and two-dimensional finite-difference thermal models were developed to simulate the thermal response and assist in the design of the Generic Research Cryogenic Tank. The one-dimensional thermal analysis determined the required insulation thickness to meet the thermal design criteria and located the purge jacket to eliminate the liquefaction of air. The two-dimensional thermal analysis predicted the temperature gradients developed within the pressure-vessel wall, estimated the cryogen boiloff, and showed the effects the ullage condition has on pressure-vessel temperatures. The degree of ullage mixing, location of the applied high-temperature profile, and the purge gas influence on insulation thermal conductivity had significant effects on the thermal behavior of the Generic Research Cryogenic Tank. In addition to analysis results, a description of the Generic Research Cryogenic Tank and the role it will play in future thermal structures and transatmospheric vehicle research at the NASA Dryden Flight Research Facility is presented.

Nomenclature

\( \rho \) specific heat, BTU/lbm °R
Gr Grashof number = \( g \beta (T_W - T_V) x^3 / \nu^2 \)
GH\textsubscript{2} gaseous hydrogen
GRCT Generic Research Cryogenic Tank
g gravitational constant, 32.2 ft/sec\textsuperscript{2}
HA85M liquid Hydrogen test case, high temperature applied uniformly to All heat shield quadrants, 85-percent fill level, Mixed ullage condition
HA85S liquid Hydrogen test case, high temperature applied uniformly to All heat shield quadrants, 85-percent fill level, Stratified ullage condition
HB85M liquid Hydrogen test case, high temperature applied to the Bottom heat shield quadrant, 85-percent fill level, Mixed ullage condition
HB85S liquid Hydrogen test case, high temperature applied to the Bottom heat shield quadrant, 85-percent fill level, Stratified ullage condition
HT85M liquid Hydrogen test case, high temperature applied to the Top heat shield quadrant, 85-percent fill level, Mixed ullage condition
HT85S liquid Hydrogen test case, high temperature applied to the Top heat shield quadrant, 85-percent fill level, Stratified ullage condition
\( h \) convective heat transfer coefficient, BTU/ft\textsuperscript{2} sec °R

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Introduction

Transatmospheric vehicles (TAVs) such as the National Aerospace Plane will require a fuselage which can withstand high aerodynamic heating while providing an insulation system. This insulation system must reduce the heat load imposed on liquid hydrogen contained within onboard fuel tanks. Material degradation, which occurs at the elevated surface temperatures associated with aerodynamic heating, restricts or disqualifies the use of many standard cryogenic insulating materials, such as closed-cell foams or vacuum-jacketed multi-layer insulations. Thermal gradients which develop within the walls of the fuel tank can lead to high thermal stresses that affect tank integrity. Therefore, the development of new insulating systems for cryogenic fuel tanks and the validation of tank integrity over a wide range of flight conditions will require extensive testing.

Tankage systems for TAVs have a significant impact on the overall vehicle design and have been the subject of several experimental test programs. These test programs helped to design, fabricate, and obtain experimental validation of liquid hydrogen tankage applicable to vehicles in hypersonic environments. Because of the complex thermal interactions between the cryogenic fuel and the tank structure, the numerical simulation and optimization analysis of tank designs have also been an integral part of experimental test programs.

Personnel at the NASA Dryden Flight Research Facility in Edwards, California are currently involved in the design of the Liquid Hydrogen Structural Test Facility (LHSTF), to be completed in late 1993. When completed, the LHSTF will be able to test various full-scale and sub-scale flight vehicle components in simultaneous cryogenic and high-temperature environments combined with mechanical loads. The LHSTF design consists of a large test cell for evaluating the performance and integrity of proposed TAV fuel tanks and associated insulation systems. In addition, the LHSTF site layout will provide for future capabilities including an actively cooled panel and turbomachinery test capability, altitude simulation, and full-scale vehicle fuselage and integrated systems tests.

In preparation for cryogenic test operations, personnel from NASA Dryden and PRC Inc. (formerly Planning Research Corporation) have designed the Generic Research Cryogenic Tank (GRCT) as the first test article scheduled for testing in the LHSTF. As a research tank, the GRCT was designed to qualitatively simulate the thermal response of a TAV fuel tank exposed to the environment of hypersonic flight. The GRCT was designed to be a sturdy test article capable of withstanding a variety of operational and research tests.

In studying the GRCT, NASA personnel will gain experience in operating, testing, and analyzing structures in simultaneous cryogenic and high-temperature environments. Operationally, the GRCT will allow NASA personnel to learn how to handle cryogens and the associated equipment required for conducting cryogenic tests. Test operations with the GRCT will help develop and verify instrumentation capable of operating in both cryogenic and high-temperature environments, and help evaluate the thermal performance.
of various insulation systems. To augment analysis efforts, the GRCT will provide test data for refining numerical models developed for simulating the thermal response of cryogenic tanks. Initial tests of the GRCT containing liquid nitrogen will be conducted in the high bay of the NASA Dryden Thermostructures Research Facility with subsequent liquid hydrogen tests conducted in the LHSTF. In addition, the GRCT will be used to perform the LHSTF integrated systems test before testing large and expensive TAV cryogenic fuel tanks.

Numerical models were required to evaluate the thermal performance of the GRCT and to answer various design questions about insulation thickness, purge gas effects, and temperature gradients within the wall of the pressure vessel. To assist in the design and evaluation of the GRCT thermal performance, one-dimensional (1-D) and two-dimensional (2-D) thermal models were created using the Systems Improved Numerical Differencing Analyzer and Fluid Integrator (SINDA'85/FLUINT). The SINDA'85/FLUINT uses a finite-difference solution method for analyzing thermal-fluid systems.

This paper describes the components of the GRCT, the development of the 1-D and 2-D thermal models, and the response of the numerical models to several GRCT liquid hydrogen test scenarios. Transient results for the 1-D and 2-D thermal models are presented with a discussion of the effects the numerical results had on the design of the GRCT.

Overview of the GRCT

Figure 1 shows a perspective view of the GRCT, suspended below a steel support structure, without...
the piping and heat lamps required for testing. Figure 2 shows a cut-away view of the GRCT along the centerline and a section view through the 10-ft center test section. As shown in Figs. 1 and 2, the GRCT consists of a cylindrical stainless-steel pressure vessel (5-ft diameter by 15-ft length by 5/16-in. thick) surrounded by 3 in. of fibrous alumina-silica ceramic insulation blankets (8 lbm/ft$^3$ density) surrounded by a thin Inconel$^\circledR$ heat shield (0.030-in. thick). A purge jacket of 0.005-in. thick nickel foil is located within the insulation at 1.5 in. from the pressure vessel. Purge gas, helium for liquid hydrogen tests and nitrogen for liquid nitrogen tests, will be pumped into the end bell sections of the GRCT and channeled into the inner 1.5 in. of insulation next to the pressure vessel. This purge region serves two purposes. First, since some anticipated liquid hydrogen test scenarios will be conducted in an air atmosphere within the LHSTF, a helium purge region reduces the possibility of a hydrogen leak forming a combustible mixture with air. Second, the purge region eliminates the liquefaction of air or nitrogen (the two LHSTF test cell atmospheres) within the insulation which degrades insulation performance and creates potential safety and maintenance problems.

Fig. 2 Cut-away view of the GRCT and a section view of the test section (not to scale).

Allowing for an adequate ullage (the unfilled portion of a container) for pressure relief, the maximum fill level for the GRCT will be from 85 to 90 percent of the total pressure vessel volume of 267 ft$^3$. A fill–drain line to the pressure vessel simulates the liquid cryogen outflows required during TAV flight profiles for engine and cooling requirements. The fill–drain

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$^\circledR$ Inconel is a registered trademark of Huntington Alloy Products Division, International Nickel Company, Huntington, WV.
line has been sized to provide a maximum cryogen outflow rate of 2 lbm/sec. A pressurization line was incorporated in the pressure vessel design to provide tank pressure maintenance during cryogen outflow. Vent lines, with back-pressure regulators, are used to control the pressure within the pressure vessel and allow a maximum pressure of 45 psia. Instrumentation access is provided for temperature, pressure, and liquid level measurements within the pressure vessel. As a design requirement, the fill–drain, pressurization, vent, and instrumentation penetrations are confined to the hemispherical ends of the GRCT to provide a uniform cylindrical test section clear of penetrations.

During test operations, clamshell quartz lamp heaters will be placed around the suspended GRCT. The quartz lamps will heat the outer heat shields and provide the temperature load on the GRCT. Figure 3 shows the proposed heating profiles to be applied to the heat shields of the GRCT. These temperature profiles represent the temperature loads associated with TAV flight trajectories. A baseline even-heating test case will consist of the high-temperature profile (peak temperature of 1960 °R) uniformly applied to the heat shield. To investigate the effects of nonuniform heating associated with TAV ascent and descent flight trajectories, the two heating profiles shown in Fig. 3 will be applied nonuniformly. To examine temperature effects on the ullage, the high-temperature profile will be applied to the GRCT upper heat shield quadrant (hot-top) while the low-temperature profile (peak temperature of 1260 °R) is applied to the lower quadrant. To examine high-temperature effects on the liquid region, the profiles will be reversed (hot-bottom). During nonuniform heating, the side quadrants of the heat shield will follow a heating profile composed of an average of the high- and low-temperature profiles.

**Description of the Thermal Models**

The GRCT design provides a test capability with either liquid nitrogen or liquid hydrogen. The thermal models developed to simulate the response of the GRCT also simulate either liquid nitrogen or hydrogen. However, analyzing the GRCT design focused on the thermal response associated with liquid hydrogen testing and the results presented are confined to liquid hydrogen test conditions.

**One-Dimensional Thermal Model**

The GRCT 1-D thermal model was developed to determine the required insulation thickness and the location of the purge liner. The 1-D model represented a radial section of the GRCT from the liquid hydrogen to the heat shield and accounted for conduction,
convection, and radiation heat transfer. Figure 4 is a schematic of the node and conductor layout used for the 1-D thermal model. A total of 36 nodes, each with a constant 1 ft² area, were used in the model. The thermal conductivity of the Inconel heat shield, insulation, and stainless-steel pressure vessel was tabulated as functions of temperature.\(^7,8\) Heat transfer through the insulation was modeled entirely by conduction, while conduction and radiation heat transfer were included between the heat shield and the outer insulation layer. A constant effective emissivity of 0.53 and a view factor of 1.0 were assumed for the radiation heat transfer between the heat shield and the insulation.

All computational test scenarios were examined assuming a constant tank pressure of 45 psia. Liquid hydrogen was assumed to be in continuous contact with the pressure-vessel wall with nucleate boiling defined as the mode of heat transfer for the wall-to-liquid interface. The heat transfer coefficient between the pressure-vessel wall and the liquid hydrogen was estimated from the corresponding Kutateladze correlation for nucleate pool boiling and tabulated as a function of the temperature difference between the pressure vessel and the liquid cryogen.\(^9\) Nucleate boiling was assumed to produce a well mixed liquid region, which allowed the liquid node to be held at the saturation temperature of hydrogen for 45 psia. The amount of boiloff produced during each time step was calculated by dividing the heat transferred into the liquid node by the enthalpy of vaporization for hydrogen (193 BTU/lbm).

A problem with the insulation thermal conductivity was identified during the 1-D thermal modeling work. Insulating materials are often not well characterized for applications involving large temperature gradients. High-temperature conductivity values are often measured using a small imposed temperature gradient, but materials used within the GRCT will be exposed to gradients in excess of 600 °R per inch. Under these conditions, fiber-to-fiber radiation can contribute to the overall apparent thermal conductivity of the insulation. The impact of purge gas (nitrogen or helium) on the apparent thermal conductivity must also be considered. Gas conduction is the dominant heat transfer mechanism for fibrous insulation systems at atmospheric pressure.\(^10\) Therefore, because helium is more conductive than air, the characteristics of the apparent thermal conductivity for the selected fibrous insulation will change in the presence of a helium purge. A program is currently underway with the National Institute of Standards and Technology (NIST) to measure the apparent conductivity of the GRCT fibrous alumina-silica insulation at high temperature gradients coupled with helium and nitrogen purge gases. The addition
of the resulting apparent conductivity data from NIST will enhance the prediction capability of the thermal models developed for the GRCT.

The NIST data were not available for this study, hence, the manufacturer’s thermal conductivity data for the insulation was used within the GRCT thermal models. However, since the insulation conductivity data were obtained by the manufacturer in an air atmosphere, the effects of a helium purge gas on the insulation thermal conductivity had to be modeled. To estimate the helium purge effects on the fibrous insulation, tabulated data for the thermal conductivity of perlite, a silica powder, for densities from 6 to 9 lbm/ft^3 and for various interstitial gases at one atmosphere were examined. These data showed that the ratio of the perlite thermal conductivity containing helium to that containing nitrogen was approximately three for all densities. Therefore, to simulate the effects of a helium purge gas within the GRCT insulation, the manufacturer’s thermal conductivity data was multiplied by three within the purge region (inner 1.5 in.) and remained unchanged in the outer insulation region (outer 1.5 in.).

The Two-Dimensional Thermal Model

The 2-D thermal model of the GRCT was created to examine the temperature gradients developed within the pressure-vessel wall, refine the calculation of cryogen boiloff, and characterize the thermal behavior of the ullage. The 2-D model represented a 1-ft wide portion of the GRCT cylindrical test section and modeled the hydrogen liquid and ullage regions. Figure 5 is a schematic of the node and conductor layout used for the 2-D thermal model composed of 413 nodes. Twenty-six circumferential locations were defined between the pressure vessel and the heat shield boundaries. At each circumferential location, 15 nodes were used to model the radial and circumferential heat transfer from the pressure-vessel wall, through the insulation, and to the heat shield. Each node within this region had a cross-sectional area and volume proportional to its radial location. The hydrogen contained in the GRCT was modeled by dividing the pressure-vessel cross-sectional area into 12 horizontal sections from top to bottom, with the uppermost horizontal section containing 3 vapor nodes. When the pressure vessel was 85-percent full, the top 5 fluid nodes were vapor and the remaining nodes were defined as liquid (a total of 18 nodes in liquid). Based on results of the 1-D model, only one radial node was defined within the pressure-vessel wall at each circumferential location since the radial temperature gradients were small. The 2-D thermal model assumed a constant tank operating pressure of 45 psia and assumed the liquid hydrogen was well mixed and remained at the prescribed saturated liquid temperature.

The 2-D model simulated the effects of hydrogen boiloff on the ullage, in addition to conduction, convection, and radiation heat transfer. The specific heat of the hydrogen vapor nodes and the boiloff gas were tabulated as a function of temperature. As with the 1-D model, the wall-to-liquid heat transfer coefficient for the liquid hydrogen cases was based on the nucleate pool boiling correlation of Kutateladze however, for stability reasons, the correlation was tabulated as a function of time rather than temperature difference.

Both free and forced convection correlations were considered in modeling the wall-to-vapor heat transfer within the ullage, however, an estimate was made to determine if either was a dominant convection mode or if mixed convection best described the ullage heat transfer. The flow velocity developed by liquid hydrogen boiloff produced laminar-flow forced convection, while the temperature difference between the vapor and the pressure-vessel wall produced free convection. An aid to determine the dominant convective mode of heat transfer was the ratio of the Grashof number to the Reynolds number squared (Gr/Re^2) which provides a measure of the ratio of buoyancy forces (free convection) to inertial forces (forced convection). A flow is considered dominated by free convection if Gr/Re^2 >> 1 and dominated by forced convection if Gr/Re^2 ≪ 1. The liquid hydrogen 85-percent fill level test case yielded a Gr/Re^2 ratio on the order of 1 x 10^5 which suggested that the wall-to-vapor heat transfer was dominated by free convection. Determining whether the free convective flow was laminar or turbulent was deduced from the Rayleigh number (Ra), which is a measure of the ratio of the buoyancy forces to the viscous forces. A free convective flow is considered laminar if Ra < 10^9 and considered turbulent if Ra > 10^9. The Ra for the liquid hydrogen 85-percent fill level test case was on the order of 10^{12} to 10^{14}. As a result, the wall-to-vapor heat transfer within the ullage was modeled as turbulent-free convection and calculated from the temperature difference between the pressure-vessel wall...
and the hydrogen vapor. The form of the turbulent-free convection correlation\(^{(14)}\) used in the 2-D model is given by

\[
h = 0.13 \frac{k}{x} (Gr Pr)^{1/3}
\]

where \(k\) and \(Pr\) were the thermal conductivity and Prandtl number of hydrogen, and \(x\) was a characteristic length (the pressure vessel diameter of 5 ft).

Test cases representing a stratified or well mixed ullage condition were examined by modifying the vapor-to-vapor heat transfer coefficient within the ullage. To verify the GRCT design under worst case conditions, the ullage vapor-to-vapor heat transfer coefficient was modeled by gaseous conduction (corresponding to heat transfer coefficients of \(4 \times 10^{-6}\) to \(2 \times 10^{-5}\) BTU/ft\(^2\) hr °R) which produced a high degree of ullage stratification. To simulate a well mixed ullage, the vapor-to-vapor heat transfer coefficients (based on gaseous conduction) were multiplied by a factor of \(1 \times 10^6\) to yield heat transfer coefficients on the same order of magnitude as the wall-to-vapor free convection coefficients (approximately 9 to 20 BTU/ft\(^2\) hr °R).

Table 1 shows the nomenclature used to identify the conditions of the various liquid hydrogen test cases examined using the 2-D thermal model.
Table 1. Computational test matrix examined with the 2-D thermal model of the GRCT.

<table>
<thead>
<tr>
<th>Arrangement of the heating profiles applied to the heat shield quadrants</th>
<th>Test case identification</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nonuniform heating</td>
<td>(Liquid hydrogen 85-percent fill level)</td>
</tr>
<tr>
<td>High-temperature profile-top quadrant</td>
<td>HT85S</td>
</tr>
<tr>
<td>Low-temperature profile-bottom quadrant</td>
<td>HT85M</td>
</tr>
<tr>
<td>Uniform heating</td>
<td></td>
</tr>
<tr>
<td>High-temperature profile-all quadrants</td>
<td>HA85S</td>
</tr>
<tr>
<td>Nonuniform heating</td>
<td></td>
</tr>
<tr>
<td>High-temperature profile-bottom quadrant</td>
<td>HB85S</td>
</tr>
<tr>
<td>Low-temperature profile-top quadrant</td>
<td>HB85M</td>
</tr>
</tbody>
</table>

Each test case identified in Table 1 describes the type of cryogen modeled, the location of the high-temperature profile, the fill level, and the condition of the ullage. For example, the HT85S identification translates to liquid hydrogen within the pressure vessel, the high-temperature profile applied to the top heat shield quadrant, an 85-percent fill level, and a stratified ullage. All of the other test cases in Table 1 follow a similar nomenclature format.

Computational Results

One-Dimensional Results

The 1-D thermal model represented the heat transfer associated with the pressure vessel in contact with liquid hydrogen and did not simulate the heat transfer within the ullage of the GRCT. Therefore, all boiloff calculations within the 1-D results section represent an estimate of the total pressure-vessel boiloff rate based on a 100-percent fill level. The boiloff rate for a 100-percent fill level was calculated by multiplying the 1-D model boiloff rate by the total pressure-vessel internal surface area of 236 ft².

Insulation Thickness

The effect of insulation thickness on the thermal response of the GRCT was examined using the 1-D model. The design criteria for the GRCT required the insulation system to provide a steady-state pressure-vessel wall heat flux of approximately 30 BTU/ft² hr, simulating the ground hold condition of a possible TAV design. In addition, design criteria for the peak wall heat flux required at least an order of magnitude increase from steady-state conditions (to approximately 300 BTU/ft² hr) within the 3000-sec applied heating period.

Using the manufacturer’s thermal conductivity data, Fig. 6 shows the pressure-vessel wall heat flux predicted for liquid hydrogen and insulation thicknesses of 2 to 6 in. The wall heat flux associated with 3 in. of insulation produced a steady-state wall flux of 22 BTU/ft² hr, corresponding to a steady-state boiloff of 27 lbm/hr, and yielded a peak heat flux of 153 BTU/ft² hr which equates to a peak boiloff rate of 187 lbm/hr. The 2-in. insulation thickness produced a steady-state wall heat flux of 33 BTU/ft² hr, however, it produced an excessive peak heat flux and corresponding boiloff rate (384 BTU/ft² hr and 469 lbm/hr) within the 3000-sec heating period. The 4- to 6-in. range of insulation thicknesses yielded low steady-state wall heat fluxes (16 to 11 BTU/ft² hr) and produced virtually no thermal response within the transient heating period. Because of the anticipated increase in wall heat flux associated with using a helium purge, the 2-in. insulation option was eliminated and 3 in. of insulation was selected for the region between the pressure vessel and the heat shield.

Location of the Purge Liner

At one atmosphere, air liquefies at 142 °R and any air within the insulation below this temperature liquefies, degrading insulation performance and creating potential safety and maintenance problems. To eliminate the air liquefaction problem, the nickel foil purge jacket was placed within the insulation at 1.5 in. to ensure the insulation temperature outside the jacket remained above 142 °R. The steady-state hold condition for the GRCT (that is, the GRCT filled with liquid cryogen awaiting the start of a test) produced the lowest insulation temperatures corresponding to the highest probability of
Fig. 6 Pressure vessel wall heat flux as a function of time from the 1-D thermal model with liquid hydrogen and insulation thicknesses from 2 to 6 in.

liquefying air. The liquid hydrogen filled GRCT produced the largest temperature difference between the liquid cryogen and the ambient environment, thereby defining the radial location of the purge jacket.

Figure 7 shows the steady-state and maximum transient temperature distributions through the fibrous insulation with the pressure vessel containing liquid hydrogen. The helium purge was confined to the inner 1.5 in. of insulation next to the pressure vessel. The maximum transient curve shows the peak temperatures that occur within the insulation, while the steady-state curve defines the minimum insulation temperatures associated with the ground hold condition. This

Fig. 7 Steady-state and maximum transient insulation temperature distribution as a function of radial location for a 3-in insulation blanket with a helium purge.
figure shows that with the purge liner located 1.5 in. from the pressure vessel, the temperature of the unpurged region will remain above the air liquefaction temperature.

**Helium Purge Gas Effects**

Figure 8 is a comparison of the pressure-vessel wall heat flux for 3 in. of insulation with and without a helium purge. The addition of the helium purge gas increased the steady-state wall heat flux of the GRCT from 22 BTU/ft$^2$ hr to 33 BTU/ft$^2$ hr, and increased the steady-state boiloff from 27 lbm/hr to 40 lbm/hr. The peak transient wall heat flux increased from 153 BTU/ft$^2$ hr to 312 BTU/ft$^2$ hr corresponding to an increase in peak transient boiloff from 187 lbm/hr to 381 lbm/hr. The helium purge gas not only affected the quantitative values of the wall heat flux and boiloff but also the transient behavior of the system. The helium purge gas decreased the thermal resistance of the inner 1.5 in. of insulation which caused the pressure vessel to respond more quickly to the imposed thermal environment.

A flexible GRCT design was needed because of uncertainty in the helium purge effects on the insulation conductivity. Two methods of controlling the pressure-vessel wall heat flux values have been identified in case the helium purge effects produce higher pressure-vessel wall heat flux values than calculated by the thermal model. First, to reduce the wall heat flux values, the heat shield has been designed to accommodate an additional inch of insulation, yielding a total of 4 in. of insulation if required. Second, the heating profiles may be altered to achieve a desired heat flux at the pressure-vessel wall.

**Two-Dimensional Results**

The 2-D thermal model simulated the heat transfer interaction between the ullage and liquid regions of the pressure vessel. Therefore, the total pressure-vessel boiloff rate presented in the 2-D results section for an 85-percent fill level was calculated by multiplying the 2-D model boiloff rate by the ratio of the total pressure-vessel inner surface area (236 ft$^2$) to the 2-D model pressure-vessel surface area (15.7 ft$^2$). In comparing 1-D and 2-D boiloff rates, the 1-D boiloff rate was multiplied by the total wetted surface area of the pressure vessel for an 85-percent fill level (174 ft$^2$).

**Liquid Hydrogen Boiloff**

Figure 9 compares the liquid hydrogen boiloff for the 1-D and 2-D thermal models and the HA85S test conditions.
test conditions. Properly scaled for an 85-percent fill level, the 1-D thermal model yielded a transient boiloff rate similar to the 2-D thermal model. For the HA85S test case, the 2-D thermal model calculated a steady-state boiloff of 32 lbm/hr and a peak boiloff of 305 lbm/hr, compared with 30 lbm/hr and 281 lbm/hr for the 1-D model. Since the additional heat transfer between the ullage and liquid regions was included, the 2-D thermal model provided a more realistic estimate of the transient hydrogen boiloff.

Figure 10 shows a comparison of the liquid hydrogen boiloff as a function of time for the HT85S, HA85S, and HB85S test cases. This figure demonstrates the effect the high-temperature profile location had on the cryogen boiloff rate. The highest liquid hydrogen boiloff rate occurred when the high-temperature profile was applied to all heat shield quadrants which yielded the maximum wetted surface area in contact with high wall heat fluxes. For the nonuniformly applied heating profiles, HB85S yielded a higher boiloff than HT85S. With the high-temperature profile on the bottom quadrant, the liquid hydrogen readily absorbed the wall heat flux and produced boiloff. With the high-temperature profile in the top quadrant, a lower boiloff was produced because the hydrogen vapor simply absorbed the heat and increased in temperature.

**Pressure-Vessel Wall Temperatures**

The maximum wall temperature for the 6 test cases at the 85-percent fill level was determined by examining the transient behavior of the pressure-vessel wall temperature in the ullage. Figure 11 shows the pressure-vessel wall temperature as a function of time for the HT85S test case and for computational nodes 100, 400, and 500. The peak wall temperature of 198 °R occurred at the highest point in the pressure vessel (node 100) at 3600 sec. However, the peak temperatures for each node within the pressure-vessel wall did not all occur at the same time. For example, the peak temperature of node 400, 75 °R, occurred at 2800 sec. This time difference for the peak wall temperatures was caused by the geometric arrangement of the vapor nodes and the resulting boiloff mass distribution.
Fig. 11 Pressure vessel wall temperatures as a function of time for the HT85S test case and computational nodes 100, 400, and 500 with the 2-D thermal model.

The HT85S test case (hot-top profile) yielded the peak pressure-vessel wall temperature because the high-temperature profile on the top heat shield quadrant was combined with the lowest boiloff rate (see Fig. 10). Figure 12 shows the transient temperature of node 100 for the 3 locations of the applied high-temperature profile. As shown in Fig. 12, concentrating the high-temperature profile on the top heat shield quadrant yields the lowest boiloff rate, resulting in less cooling available for the wall and ullage regions, which yielded the highest wall temperatures. Conversely, concentrating the high-temperature profile on

Fig. 12 Pressure vessel wall temperature for node 100 as a function of time for different applied temperature profile arrangements with the 2-D thermal model.

13
the bottom heat shield quadrant yielded a moderate boiloff rate, which coupled with the low-temperature profile in the ullage, produced lower overall wall temperatures.

The liquid hydrogen acted as a thermal sink which maintained the wetted pressure-vessel wall temperatures slightly above the saturation temperature of the hydrogen for all of the applied temperature profile arrangements examined. The magnitude of the wall-to-liquid heat transfer coefficient for liquid hydrogen did not substantially affect the value of the wetted pressure-vessel wall temperatures.

While examining the ullage heat transfer, various constant values for the wall-to-vapor convective heat transfer coefficient (from 0.5 to 100 BTU/ft² hr °R) were considered. This sensitivity analysis showed that the wall-to-vapor heat transfer coefficient had a minor effect on the pressure-vessel wall and fluid temperatures. Conversely, the magnitude of the vapor-to-vapor heat transfer coefficient (affecting the degree of mixing) greatly influenced the resulting pressure-vessel wall and fluid temperatures. Of all the modes of heat transfer occurring within the pressure vessel, the condition of the ullage vapor (well mixed or stratified) had the most pronounced effect on the pressure-vessel wall temperatures. A stratified ullage yielded higher pressure-vessel wall temperatures and circumferential temperature gradients while a well mixed ullage yielded lower wall temperatures and circumferential temperature gradients.

Figure 13 shows the pressure-vessel wall temperature distribution for the HT85S and the HT85M test cases. For the HT85S test case, the pressure-vessel wall temperatures are shown at 0 sec (steady-state) and at 3600 sec (peak temperature). The pressure-vessel wall temperatures decreased circumferentially from $S = 0$ ft (node 100, top of the pressure vessel) to $S = 2.6$ ft (node 500) with the heat flowing from the hot upper wall region to the cold wall region in contact with the liquid hydrogen. Figure 13 also provides an estimate of the circumferential temperature gradients that exist within the pressure-vessel wall. Comparing the temperature distributions for the HT85S and HB85M test cases shows the decrease in the pressure-vessel wall temperatures and temperature gradients when the ullage was well mixed.

![Figure 13](image_url)

Fig. 13  Steady-state and peak pressure vessel wall temperatures as a function of circumferential location for stratified and mixed ullage conditions with the 2-D thermal model.
Vapor Temperatures

Figure 14 shows the vertical temperature distribution of the fluid and vapor nodes at selected times for the HT85S and HT85M test cases. The heating profiles influenced the amount of cryogen boiloff which then influenced the vapor temperatures and the corresponding wall temperatures. Node 3000 (the top vapor node) reached a peak vapor temperature of 188 °R at 3600 sec, which was 10 °R cooler than the adjacent wall nodes (see Fig. 11). The temperature gradient associated with the stratified ullage and its change over time is readily apparent in Fig. 14. For a well mixed ullage condition there was virtually no temperature gradient through the vapor region as shown in Fig. 14. The time dependence of the fluid and vapor node temperatures was qualitatively similar to the time dependence of the wall temperatures shown in Figs. 11 and 12.

Pressure Vessel Circumferential Temperature Gradients

The circumferential temperature gradients developed within the pressure-vessel wall were a strong function of the location of the applied heating profiles. The 2-D thermal model was used to examine the peak thermal gradients developed within the pressure-vessel wall for the 85-percent fill level and determine if they were below the design criteria of 112 °R/ft prescribed by the structural analysis done by PRC personnel.

Table 2 shows the peak and average circumferential temperature gradients developed within the pressure-vessel wall for the different applied heating profiles with stratified and well mixed ullages. The circumferentially averaged temperature gradients were calculated from the pressure-vessel temperature gradients in contact with the ullage at the time the peak gradients occurred (typically 2500 to 5000 sec).
Table 2. Peak and average circumferential temperature gradients within the pressure-vessel wall for stratified and well mixed ullages.

<table>
<thead>
<tr>
<th>Test cases</th>
<th>Pressure vessel circumferential temperature gradients (°R/ft)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Peak</td>
</tr>
<tr>
<td>Stratified ullage</td>
<td></td>
</tr>
<tr>
<td>HT85S</td>
<td>116.1</td>
</tr>
<tr>
<td>HA85S</td>
<td>99.9</td>
</tr>
<tr>
<td>HB85S</td>
<td>54.3</td>
</tr>
<tr>
<td>Well mixed ullage</td>
<td></td>
</tr>
<tr>
<td>HT85M</td>
<td>21.0</td>
</tr>
<tr>
<td>HA85M</td>
<td>25.4</td>
</tr>
<tr>
<td>HB85M</td>
<td>13.0</td>
</tr>
</tbody>
</table>

The peak gradient always occurred as a spike that was significantly larger than the rest of the gradients in the ullage. These temperature gradient spikes were the result of several simplifying assumptions built into the 2-D model, including the degree of vapor-to-vapor coupling and the distribution of boiloff vapor (for cooling) available to each tank wall node. Circumferentially averaging the ullage temperature gradients reduced the effects of the simplifying model assumptions. Therefore, the averaged values were considered to be more appropriate for design assessment. The average temperature gradients for the stratified ullage case were considerably less than the design criteria. A well mixed ullage yielded average temperature gradients which were considerably lower than for a stratified ullage and were well below the design criteria.

Pressure-Vessel Wall Heat Flux

Table 3 shows the peak and average pressure-vessel wall heat fluxes with liquid hydrogen for stratified and well mixed ullages. The average wall heat fluxes were calculated from the nodes in contact with liquid or vapor at the time the corresponding peak wall heat fluxes occurred.

Table 3. Peak and average pressure-vessel wall heat fluxes with liquid hydrogen for stratified and well mixed ullages.

<table>
<thead>
<tr>
<th>Test cases</th>
<th>Wall-to-vapor heat fluxes (BTU/ft² hr)</th>
<th>Wall-to-liquid heat fluxes (BTU/ft² hr)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Peak</td>
<td>Average</td>
</tr>
<tr>
<td>Stratified ullage</td>
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<tr>
<td>HT85S</td>
<td>348.9</td>
<td>241.9</td>
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<tr>
<td>HA85S</td>
<td>378.2</td>
<td>309.3</td>
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<tr>
<td>HB85S</td>
<td>140.7</td>
<td>112.5</td>
</tr>
<tr>
<td>Well mixed ullage</td>
<td></td>
<td></td>
</tr>
<tr>
<td>HT85M</td>
<td>340.6</td>
<td>318.5</td>
</tr>
<tr>
<td>HA85M</td>
<td>342.2</td>
<td>340.7</td>
</tr>
<tr>
<td>HB85M</td>
<td>138.6</td>
<td>114.3</td>
</tr>
</tbody>
</table>
The location and magnitude of the peak wall heat flux within the ullage depended on several factors, including the applied high-temperature profile location and the geometric arrangement of the vapor nodes affecting boiloff mass distribution. Averaging the ullage temperature gradients reduced the effects of the simplifying model assumptions. Consequently, the average wall-to-vapor heat flux provided a more realistic indication of the expected wall heat flux. For the hot-top and even heating test cases more heat was transferred into the ullage than for the hot-bottom test cases. Ullage mixing increased the wall-to-vapor heat flux for the hot-top and even heating cases, but had no effect on the hot-bottom cases.

The magnitude of the peak wall-to-liquid heat flux was not dependent on the arrangement of the liquid nodes, but the location of the peak wall-to-liquid heat flux depended on the location of the applied high-temperature profile. For the hot-top and even heating cases, the peak heat flux occurred at the top wall node in contact with the liquid cryogen (node 500) because of the additional heat transferred from the ullage. For the hot-bottom heating cases, the peak wall-to-liquid heat fluxes occurred at the bottom of the pressure vessel. The condition of the ullage, whether stratified or well mixed, did not affect the wall-to-liquid heat fluxes within the pressure vessel.

Concluding Remarks

The one-dimensional and two-dimensional thermal models successfully analyzed the thermal behavior of the Generic Research Cryogenic Tank for several test cases. The insulation thickness around the pressure vessel was sized at 3 in. to provide a steady-state heat flux of 33 BTU/ft² hr and produced a peak transient heat flux of 312 BTU/ft² hr which occurred within the 3000-sec heating period. The purge jacket was located 1.5 in. within the insulation to eliminate the liquefaction of air which would degrade insulation performance. Large temperature gradients within the wall of the pressure vessel could lead to large thermal stresses, but the average circumferential temperature gradients of the test cases examined were well below the allowable design value of 112 °R/ft. Refining the cryogen boiloff calculation and subsequently the heat flux into the cryogen defined the thermal performance of the Generic Research Cryogenic Tank more accurately. Mixing in the ullage lowered vapor temperatures by as much as 140 °R and had a much greater effect on thermal behavior of the ullage than either heating profile location or wall-to-vapor heat transfer characteristics.

The thermal analysis identified several characteristics that affected the thermal behavior of the Generic Research Cryogenic Tank. The characteristics of ullage mixing, the location of applied high-temperatures, and the helium-insulation apparent thermal conductivity all influenced the behavior of the Generic Research Cryogenic Tank. Improvement of subsequent thermal simulations will be the focus of the thermal conductivity tests at the National Institute of Science and Technology and much of the future testing with the Generic Research Cryogenic Tank.

References

A cryogenic test article, the Generic Research Cryogenic Tank, was designed to qualitatively simulate the thermal response of transatmospheric vehicle fuel tanks exposed to the environment of hypersonic flight. One-dimensional and two-dimensional finite-difference thermal models were developed to simulate the thermal response and assist in the design of the Generic Research Cryogenic Tank. The one-dimensional thermal analysis determined the required insulation thickness to meet the thermal design criteria and located the purge jacket to eliminate the liquefaction of air. The two-dimensional thermal analysis predicted the temperature gradients developed within the pressure-vessel wall, estimated the cryogen boiloff, and showed the effects the ullage condition has on pressure-vessel temperatures. The degree of ullage mixing, location of the applied high-temperature profile, and the purge gas influence on insulation thermal conductivity had significant effects on the thermal behavior of the Generic Research Cryogenic Tank. In addition to analysis results, a description of the Generic Research Cryogenic Tank and the role it will play in future thermal structures and transatmospheric vehicle research at the NASA Dryden Flight Research Facility is presented.