Quantification of Processing Effects on Filament Wound Pressure Vessels

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December 1999
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Summary

A computational simulation procedure is described which is designed specifically for the modeling and analysis of filament wound pressure vessels. Cylindrical vessels with spherical or elliptical end caps can be generated automatically. End caps other than spherical or elliptical may be modeled by varying circular sections along the x-axis according to the end cap shape. The finite element model generated is composed of plate type quadrilateral shell elements on the entire vessel surface. This computational procedure can also be used to generate grid, connectivity and material cards (bulk data) for component parts of a larger model. These bulk data are assigned to a user designated file for finite element structural/stress analysis of composite pressure vessels. The procedure accommodates filament wound pressure vessels of all types of shells-of-revolution. It has provisions to readily evaluate initial stresses due to pretension in the winding filaments and residual stresses due to cure temperature.

Introduction

Filament wound pressure vessels, though simple to fabricate, have relatively complex internal structure especially in the domes. Additional complexities are introduced because of the presence of initial stresses. These stress result from (1) the pretension in the filament tape (wet or prepreg) and (2) the curing process. Accurate description of the local filament location/direction and initial stresses are required for credible evaluation of vessel structural integrity and durability. Computational methods for composite structural stress analyses are available (refs. 1 and 2). These methods have recently been augmented to simulate the local filament location/direction and respective initial stresses. A specific code for that purpose is identified as COBSTRAN for Composite Blade Structural Analysis (ref. 2). The objective of the present article/report is to provide an overview of the COBSTRAN application to filament wound pressure vessels and present some initial results.

The COBSTRAN computer code was developed and used successfully at NASA Glenn Research Center for the design and analysis of composite turbofan (ref. 3) and turboprop blades (ref. 4) and also for composite wind turbine blades (ref. 5). Its application has been extended to include more general models of three-dimensional solid and shell structures and is currently being expanded to include filament wound tank-type structures and/or pressure vessels.

This code combines composite mechanics and laminate theory with a resident data bank of fiber and polymer matrix properties. COBSTRAN is versatile in that it can be used as a preprocessor or post processor with general purpose structural analysis computer codes or stand-alone with its resident general purpose finite element structural analysis module. As a preprocessor for several general purpose finite element structural analysis programs, (COSMIC NASTRAN/MSC/NASTRAN and MHOST (refs. 6 to 8)) COBSTRAN, generates a model with anisotropic integrated laminate material properties. Stress or strain output form the analysis program is provided as input to the COBSTRAN post-processor which uses the composite mechanics and laminate theory routines to calculate individual ply stresses, strains, interply stresses, through-the-thickness stresses and failure margins (ref. 1). As an exception, COBSTRAN may utilize nodal force output from MHOST for post-processing. MHOST is the resident general purpose finite element structured analysis module in COBSTRAN.
COBSTRAN, written in FORTRAN 77, is currently configured and tested for operation on various UNIX based platforms including CRAY X-MP, Silicon Graphics and Hewlett Packard. The COBSTRAN/MHOST code is now available on the PC for automatic pre- and post-processing. The various features of COBSTRAN for filament wound pressure vessels are described in subsequent sections. Input deck setup sample case for a polar winding pressure vessel is illustrated in Appendix A. The corresponding pressure build up due to pretension in the winding filaments is illustrated in Appendix B.

**Composite Analysis**

A COBSTRAN filament winding processing diagram is depicted in figure 1. COBSTRAN is designed to carry out the many linear analysis required to efficiently design and analyze structural components made of multilayered multidirectional fiber composites. Inputs to the COBSTRAN composite analysis are constituent fiber and matrix material properties, factors reflecting the ply fabrication process, and ply orientation and location geometry. COBSTRAN performs the micromechanics, macromechanics and laminate mechanics of these fiber composites. See the COBSTRAN Theoretical/Programmers Manual (ref. 9). The orientation angle of the 11-axis of a ply is shown in figure 2. For each ply designation this orientation angle is internally calculated for each wrap that exists at a finite element grid point. This angle (measured in degrees) is defined in a local composite coordinate system in which the 0.0 degree axis is tangent to the tank surface and whose projection along the structural x-axis which is parallel to the axial axis of the pressure vessel. The composite 33-axis is positive inward normal to the surface. Outputs are the various ply and composite properties, composite structural response (accounting for bending-stretching coupling) and composite stress analysis including the results of combined-stress 'strength failure criteria' and Hoffman's failure criteria. The output from COBSTRAN post-processing is designed to make use of information generated in the preprocessor phase and stored in temporary binary files. Therefore, the COBSTRAN pre- and post-processing problem must be run in sequence on the same machine.

**Coordinate Systems**

COBSTRAN utilizes a right hand rectangular coordinate system for structures (vessel) in which the vessel lies axially along the x-axis (fig. 2). For the filament wound tank modeling the input coordinates are assumed to be on the internal surface of the model which corresponds to the mandrel external surface. These coordinates are automatically transferred to the mid-thickness position in accordance with the thickness of the liner and number of wrap ply generated by COBSTRAN.

**Mesh Generation**

The mesh generation capability in COBSTRAN is designed to create two-dimensional plate type meshes. All meshes are created generally with two-dimensional NASTRAN QUAD4 elements. Under the FWTANK option only quadrilateral elements are created. Tank geometry is defined with user specified circular or elliptical cross-sections by specifying radii and x-axis location. The density of the mesh is controlled by the user input in which the number of circular sections is specified and also the number of elements about the circumference. COBSTRAN calculates the surface geometry and generates a mesh (finite element model) based on this input.

The coordinates of the mesh are first generated on the radii specified by the user input parameters. These dimensions must be the internal dimensions of the vessel since the final thickness of the wraps is not initially known. Following the ply generation and designation of which plies exist at each node, the position of each node is transformed half of the ply stack thickness and normal to the internal surface of the vessel.
Tape Pretension

Filament winding pretension is used to keep the fibers taut and in place in order to prevent fiber wash and fiber wrinkling. However, as the plies build-up the pressure generated by the vessel wall against the mandrel may be high enough to cause mandrel buckling, or liner damage or fiber damage and substantial inner plies wrinkling after mandrel removal. To prevent any or all of those from occurring the winding tension through the ply thickness build-up is varied. This is usually referred to as filament winding or tape programmed pretension.

The external pressure generated by the tape pretension at any ply including the mandrel surface is calculated in accordance with the paper: Residual Stresses in Filament Wound Laminates and Optimum Programmed Winding Tension by C.Y. Liu and C.C. Chamis (ref. 10). Currently the algorithm programmed in COBSTRAN assumes an infinitely stiff mandrel and the pressure is calculated only for hoop plies. The pressure generated by each plys pretension is accumulated as an external pressure in the finite element model when the input request includes the mnemonic ‘PRESSURE LOAD’.

Liner Generation

A liner, usually a thin metal layer, is used at the inner surface of the shell to prevent seepage of the pressure vessel contents through the composite wall thickness. In COBSTRAN the liner is designated by the key word ‘LINER’ in the wrap stack-up section of the input deck and is treated as another ply. The ply designation number is provided on this input line. The thickness of the liner is indicated on the ‘CIRCLE,’ ‘ELLIPSE,’ ‘DSHERE’ or ‘DELLIPS’ lines of the parameter section of the input deck. The number of ply layers required to fill this specified thickness is determined by the code. A sample case input deck setup is illustrated in appendix A. The corresponding pressure build up is illustrated in appendix B. The initial residual stresses are evaluated as described (ref. 11). Both of these must be added to those due to applied internal pressure.

Polar Wrap Generation

A polar wrap is designated by the key word ‘POLAR’ in the wrap stack-up section of the input deck. The angle of the polar wrap is determined by calculating the offset of wrap over the total length of the vessel. The offset is equal to the sum of the radii of both bosses plus the tape width. The polar wrap angle is equal to the arctangent of the offset divided by total vessel length. The number of polar wraps per cycle is determined by dividing the maximum circumference of the tank by the tape width, adjusted for polar wrap angle. The starting angle for a single polar wrap is defined from zero on the positive y-axis incrementing about the x-axis in the positive direction using the right hand rule. If the number of polar pairs is zero only one full circumferential set of wraps will be made. If the number of polar pairs is one, the wrap will be designed as one wrap starting at the designated starting angle and second wrap starting 180° from the starting position. This feature provides wraps at alternating angles over the vessel for each polar pair indicated. If the number of polar pairs is greater than one, the number of pairs are divided into 360° and each pair will be designated as one wrap with the starting angle incremented from the designated starting angle and a second wrap starting 180° from the incremented starting position (fig. 3).

Hoop Wrap Generation

A hoop wrap is designated by the key word ‘HOOP’ in the wrap stack-up section of the input deck. The hoop wrap generated by this designation exists only over the cylindrical portion of the vessel. The HOOP ANGLE is measured from a normal to the cylinder x-axis and the tape center line. If the HOOP ANGLE is given as 0.0, the angle of the wrap will be calculated as the arctangent of the tape width, adjusted for overlap, divided by the tank circumference. The number of wraps for each HOOP call is equal to the tape width divided into the circumference. One hoop wrap consists of one wrap in the positive x-direction over the length of the cylindrical section and a wrap in the negative x-direction over the cylindrical section thus generating alternating ply angles. The starting angle for a single hoop wrap is defined from zero on the positive y-axis incrementing about the x-axis in the positive direction.
using the right hand rule. The subsequent wraps are incremented by the ratio of the number of wraps divided into 360°. The tape tension generates an equivalent external pressure on the vessel which will exist in the finite element deck if the PRESSURE LOAD option is called in the COBSTRAN input deck (fig. 1). A mandrel pressure built-up for a specific vessel is illustrated in figure 4.

**Helical Wrap Generation**

A helical winding, designated by the key worked ‘HELICAL’ in the wrap stack-up section of the input deck, is generated for a given circuit. A circuit is defined as one complete wrap starting at the boss going around the opposite boss and returning to the original boss. The final position at the starting boss is determined by the tank shape and helical angle used. This final position is the starting position for the next circuit. The incrementing of each circuit and the tape width is included in the program. The helical wrap generated by this designation exists over the entire vessel. The HELIX angle is measured from the cylinder x-axis and the tape centerline. One circuit consists of one wrap in the positive x-direction over the length of the vessel from boss to boss and a continuous wrap in the negative x-direction from boss to boss thus generating alternating ply angles. The starting angle for each helix call is defined from zero on the positive y-axis incrementing about the x-axis in the positive direction using the right hand rule (fig. 5). COBSTRAN/FWTANK can accommodate filament would shells with other shapes-of-revolution (ref. 12) (see also fig. 6).

**Property Input**

Two options are available. Option one uses user-supplied ply properties. This option indicates that the unidirectional layer properties are known and will be user-supplied input. Plies are identified by ply designation number. Option two uses constituent material properties and composite micromechanics to determine ply properties: The appropriate ply designation, the type of fiber and matrix must be specified. Fiber and matrix types from the COBSTRAN resident DATABANK that are most similar to those of the actual ply should be selected. COBSTRAN will use the ply properties exactly as they are entered, but any other material properties will be calculated from the fiber and matrix properties as given in the DATABANK (ref. 1).

**Conclusions**

An overview is described of a computational simulation procedure to evaluate filament wound pressure vessels. The procedure uses composite mechanics with finite element structural analysis. Unique features of the procedure include internally calculated filament/location direction, dome built-up thickness and pressure build-up due to pre-tension winding. Polar, helical and other filament wound patterns are accommodated as well as all types of sells-of-revolution. The initial stresses due to pre-tension and cure temperature are evaluated from the pretension pressure built-up and the vessel cure temperature. Sample input deck is illustrated in appendix A and pressure built-up in appendix B for a polar wound pressure vessel for a 40-ply vessel the average pressure built-up is 30 psi.
Appendix A
Input Deck Setup for Polar-Wound Pressure Vessels

The following deck setup demonstrates the application of tape pretension for a 5 in. radius cylindrical tank with no end domes. The wall thickness applies only to the liner, the final thickness is determined following the application of all wraps. The grid locations are then translated to the mid-thickness point of the ply stack-up. The 'TRANS' and 'BOUND' parameters apply only to a request for a 'MHOST' model and are ignored by the 'MSC NASATRAN' model selection in the option deck.

```
TITLE= DEMONSTRATION PROBLEM NO. 22B
TITLE= MODELING OF CYLINDER WITH NO DOMES
TITLE= USING EZREAD OPTION AND 'CIRCLE' FORMATS
TITLE= ALUMINUM LINER 0.02 THICK + HOOP WRAPS
TITLE= FIRST HOOP STARTING AT 0.0 DEGREES Y-AXIS
PREPROCESSOR

$DIAG 16 54
$DIAG 98 $ FILL MDES ARRAY WITH WRAP NUMBER NOT COMPOSITE ID
$ FOR DEBUGGING ONLY: NOT FOR MATERIAL ANALYSIS
$DIAG 59 $ DO NOT PRINT INTERNALLY GENERATED CIRCULAR CONTOUR
PRTOUT $ PRINT ALL ELASTIC PROPERTIES
FWTANK $ FILAMENT WOUND TANK MODELING
MHOST $ FORMAT OF THE MODEL GENERATED
SICAN $ THE ICAN AND MICRO OPTIONS ARE REQUIRED
$MICRO $ FOR USING THE ICAN CODE FOR PRE- AND POST-PROCESSING
ECHO $ DISPLAY THE INPUT DECK
PROPERTY INPUT $ SPECIFY PROPERTIES FOR INNER LINER
PRESSURE LOAD $ GENERATE PRESSURE LOADING DATA
ENDOPTIONS $-------------------DELIMITER--------------------------------------
IMAT 1 $ MATERIAL PROPERTY TYPE
NDES 8 $ NUMBER OF PLY DESCRIPTIONS
NYSPACES 14 $ NUMBER OF CHORDWISE SPACES NOT NECESSARILY EQUAL
NPLY = 8 $ NUM AXES DIREC
$NSM 2 $ STRAIN MAGNIFICATION OPTION FOR POSTPROCESSING
$ 
$ NAME SECTION SPACES TO X-STA HELIX RADIUS WALL PRESS
$ NUMBER NEXT SEC ANGLE THICK INT/EXT
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$ 
$ NAME SECTION SPACES TO X-STA RADIUS WALL PRESS
$ NUM NEXT SEC ANGLE THICK INT/EXT
$ 
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$ CIRCLE 2 1 2.0 5.0 .02 00.0 0.0
$ CIRCLE 3 1 4.0 5.0 .02 00.0 0.0
$ CIRCLE 4 1 6.0 5.0 .02 00.0 0.0
$ CIRCLE 5 1 8.0 5.0 .02 00.0 0.0
$ CIRCLE 6 0 10.0 5.0 .02 00.0 0.0
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$ 
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$ 
$ NAME SECT ROT RADIAL NUM AXIS DIREC
$ 
$ TRANS 1 1 2
$ TRANS 2 1 2
$ TRANS 3 1 2
```

NASA/TM—1999-209434
TRANS 4 1 2
TRANS 5 1 2
TRANS 6 1 2

$ NAME SECT DOF(MAX 6 WITH A SPACE BETWEEN EACH) NUM
$ BOUND 1 1
$ BOUND 7 1
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$ STK-ORDER DESIGNATION WIDTH OVERLAP ANGLE ANGLE TAPE

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30.0E+03 30.0E+03 30.0E+03 30.0E+03 7.2E+03 0.011E-06 12.5E-06

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Appendix B
Pressure Built-Up Due to Pretension in a Polar-Wound Pressure Vessels

Tape Tension Analysis per Chris Chamis paper

- $a$: inside radius of mandrel
- $b$: outside radius of mandrel
- $c$: outside radius of laminate
- $B = 0$ if mandrel is infinitely stiff
- $E$: Young's Modulus
- $\theta$: Tangential direction
- $r$: Radial direction
- $F$: Modulus of orthotropic material

\[
E_e = 1.94 \times 10^7 \quad E_r = 1.38 \times 10^6 \quad F = 7.33 \times 10^5
\]

\[
S = \sqrt{(E_e / E_r)} = 3.74614
\]

\[
\alpha = S - (E_e/F) - B = -2.27 \times 10^1
\]

\[
\beta = S + (E_e/F) + B = 3.02 \times 10^1
\]

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Press = \( \frac{(T\alpha\beta)}{E} \) * LN \( \frac{b*b-a'a}{2*b*b} \)

\[
B = \frac{E_e}{F} (1 - \mu_m)b*b + (1 + \mu_m)a'a
\]

\[
\frac{E_e}{F} \sum (b*b-a'a)
\]

- Total pressure
- Mandrel pressure, psi

Number of plies
References

Figure 1.—COBSTRAN filament winding process diagram.

Figure 2.—Fiber composite geometry relative to COBSTRAN coordinate system.
Figure 3.—Tank with Spherical Endcaps.

Figure 4.—Mandrel pressure built-up due to filament winding pretension—resulting in initial stresses.
Figure 5.—Tank with Elliptical Endcaps.

Figure 6.—Elliptical shell used to verify interply shear.
**Abstract**

A computational simulation procedure is described which is designed specifically for the modeling and analysis of filament wound pressure vessels. Cylindrical vessels with spherical or elliptical end caps can be generated automatically. End caps other than spherical or elliptical may be modeled by varying circular sections along the x-axis according to the end cap shape. The finite element model generated is composed of plate type quadrilateral shell elements on the entire vessel surface. This computational procedure can also be used to generate grid, connectivity and material cards (bulk data) for component parts of a larger model. These bulk data are assigned to a user designated file for finite element structural/stress analysis of composite pressure vessels. The procedure accommodates filament wound pressure vessels of all types of shells-of-revolution. It has provisions to readily evaluate initial stresses due to pretension in the winding filaments and residual stresses due to cure temperature.