Fuzzy Current-Mode Control and Stability Analysis

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FUZZY CURRENT-MODE CONTROL AND STABILITY ANALYSIS

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Abstract

In this paper a current-mode control (CMC) methodology is developed for a buck converter by using a fuzzy logic controller. Conventional CMC methodologies are based on lead-lag compensation with voltage and inductor current feedback. In this paper the converter lead-lag compensation will be substituted with a fuzzy controller. A small-signal model of the fuzzy controller will also be developed in order to examine the stability properties of this buck converter control system. The paper develops an analytical approach, introducing fuzzy control into the area of CMC.

1. Introduction

Fuzzy control has emerged as one of the most active and promising control areas, especially because it can control highly nonlinear, time-variant, and ill-defined systems. The work of Mamdani and his colleagues on fuzzy control was motivated by Zadeh’s work on the theory of fuzzy sets, and its application to linguistics and systems analysis. Layne later modified work by Procyk, Mamdani, and others on the linguistic self-organizing controller to what it is now, Fuzzy Model Reference Learning Control (FMRLC).

Existing CMC techniques primarily employ analog lead-lag compensation to shape the closed-loop gain of the converter (magnitude and phase) in order to achieve certain design criteria, such as stability margins, low output impedance, low audio susceptibility, and response time characteristics like overshoot, settling time, and zero steady-state error. In this paper fuzzy control will be used, instead, to control a 6-kW converter with constant-power or negative-resistance loading. The rest of the design procedure, such as the insertion of the control-stabilizing ramp signal, the inductor current feedback and the design of the slopes of the feedback signals, will follow the same procedures as the traditional CMC design. The existing CMC methodology offers a comprehensive and methodical approach to meeting design criteria in both the frequency and time domains. The approach introduced here offers a design alternative for converter control by incorporating modern nonlinear control design approaches, such as fuzzy control, while still being able to use powerful frequency domain analysis techniques.

Initially, in this paper, the FMRLC approach will be employed to control the converter. Later the control law learned by using FMRLC will be employed using instead a conventional fuzzy controller to control the process. The FMRLC control technique could be used as the final control. However, because the FMRLC exhibits nonstationary nonlinearities, it is not amenable to small-signal, frequency domain analysis. A small-signal model of the converter will be constructed initially to help understand how to develop a heuristic, inverse fuzzy model of the converter, which is needed to employ the FMRLC technique. Later the small-signal model of the converter will be used to help analyze the stability properties of the control system. Sinusoidal sweeps will be applied to the fuzzy controller to construct frequency domain responses by employing fast Fourier transforms (FFT’s). The small-signal transfer functions of the fuzzy controller will be constructed by using pole-zero approximation of the frequency responses.

2. Converter Model

2.1 Large-Signal, Switch-Mode Model

Figure 1 shows the model of a switch-mode, 6-kW buck converter regulator. The power stage equations for the large-signal nonlinear model are

\[
\frac{di}{dt} = \frac{1}{L_f} (v_g - v_o) \tag{1}
\]

\[
\frac{dv_c}{dt} = \frac{i_c}{C_f} \tag{2}
\]

\[
\frac{dl_c}{dt} = \frac{1}{L_c} (v_o - i_c R_c - v_c) \tag{3}
\]

\[
i_o = i_l - i_c \tag{4}
\]

\[
v_o = P_o / i_o \tag{5}
\]
where $R_c$ and $L_c$ are the filter capacitor effective series resistance and inductance, respectively, and $P_o$ is the load power. The nonlinear switch-mode model has two operating modes per conducting cycle: mode 1, when the switch is closed and Eqs. (1) to (5) are active; and mode 2, when the switch is open ($v_s = 0$) and the fly-back diode is conducting.

2.2 Small-Signal, Power Stage Model in Continuous Conduction Mode

Figure 2 shows the small-signal continuous conduction mode (CCM) perturbation model of the buck converter power stage. This model is derived from performing state-space average of the nonlinear switch-mode model above, to come up with the large-signal average model, and then perturbing this model to calculate the small-signal perturbation model:

\[
\dot{i}_l = \frac{1}{s L_f} \left( V_g \dot{d} - D V_o - V_o \dot{d} \right) \tag{6}
\]

\[
\dot{v}_o = \left( \dot{i}_l + D \dot{d} \right) Z(s) \tag{7}
\]

\[
Z(s) = \frac{R_l \left( C_f L_c s^2 + R_c C_f s + 1 \right)}{C_f L_c s^2 + R_c C_f s + 1}, \text{ for } R_c \ll R_l \tag{8}
\]

Substituting Eq. (6) into Eq. (7) and after some simplifications:

\[
\frac{\dot{v}_o}{d} = \frac{V_g - V_o}{D} \frac{P_n(s)}{P_d(s)} \tag{9}
\]

where

\[
P_n(s) = \frac{L_f L_c C_f I_l}{s^3} + \frac{L_f C_f I_l R_c}{s^2} + \frac{L_f I_l}{s} + 1 \tag{A}
\]

\[
P_d(s) = \frac{L_f L_c C_f}{B} \frac{s^3}{s} + \frac{R_l L_f C_f}{B} s^2 + \frac{L_f}{s} + 1 \tag{B}
\]

$A = D(V_g - V_o)$, $B = D^2 R_p$ and $D$ is the duty cycle. Similarly, substituting Eq. (7) into Eq. (6) and after some simplifications:

\[
\frac{\dot{i}_l}{d} = \frac{E}{B} \frac{C_f L_c s^2 + \left[ (V_g - V_o) R_c C_f / E \right] s + 1}{P_d(s)} \tag{10}
\]

where $E = V_g - V_o - D I_l$ and $D$, $V_g$, $V_o$, and $I_l$, in Eqs. (6) to (10) represent average quantities over a conduction cycle of the duty cycle, input voltage, output voltage, and inductor current, respectively.

The corresponding lower case variables with the hat represent the perturbation quantities of these variables. Equations (9) and (10) represent the small-signal transfer functions of the duty cycle to the output voltage and the inductor current, respectively. Other transfer functions necessary for a complete CCM model of the converter power stage or the discontinuous conduction mode (DCM) model will not be derived here as this is beyond the scope of this paper. Figures 3 and 4 show frequency responses of Eqs. (9) and (10), respectively, at 100% constant-power load ($-R_l$) with $V_g = 160$ volts, $V_o = 120$ volts, $L_f = 80$ $\mu$H, $C_f = 320$ $\mu$F, $R_c = 20$ $\text{m}$Q, $L_c = 0.5$ BH.

Figure 5 shows the small-signal, control-to-output model in CCM. From Fig. 5 with $G_v = \dot{v}_v / \dot{d}$ and $G_i = \dot{i}_l / \dot{d}$.

\[
\dot{d} = F_m \left[ K_v \dot{v}_v + F_v \dot{v}_v - R_l H_v(s) G_i(s) \dot{d} \right] \tag{11}
\]

\[
\dot{v}_o = G_v \dot{d} \tag{12}
\]

Solving for $\dot{d}$ in Eq. (11) and substituting into Eq. (12) to solve for $\dot{v}_o / \dot{v}_c$ gives

\[
\frac{\dot{v}_o}{\dot{v}_c} = \frac{F_c F_m G_v(s)}{1 + F_m R_l H_v(s) G_i(s) - F_m K_v G_v(s)} \tag{13}
\]

Figure 1.—Switch-mode, 6-kW buck converter regulator.

Figure 2.—Small-signal CCM perturbation model of buck converter power stage.
where, for the buck converter case\textsuperscript{7},

\[
H_c = 1 + \frac{s}{\omega_n Q_c} + \frac{s^2}{\omega_n^2} + K_r = \frac{T_s R_i}{2 L_f}, \quad Q_c = \frac{2}{\pi},
\]

\[
\omega_n = \frac{\pi}{T_s}, \quad F_m = \frac{1}{(S_n + S_p) T_s}, \quad F_c = 1
\]

\(T_s\) is the conduction period in seconds, \(S_n\) is the rising slope of the inductor current feedback, and \(S_p\) is the slope of the stabilizing sawtooth signal. Figure 6 shows a frequency response of Eq. (13) at 100% load with a switching frequency of 40 kHz, \(R_i = 0.02\), \(S_n = 80,000\), and \(S_p = 11,000\).

3. Fuzzy Current-Mode Control

3.1 FMRLC Current-Mode Control

Figure 7 shows the basic FMRLC structure\textsuperscript{5} with the addition of a pole at the origin placed at the output of the fuzzy controller. The proposed fuzzy controller will be replacing the traditional lead-lag compensation. The gains of the FMRLC controller are tuned on the basis of information gained from an open-loop step response of the process and guidelines generated by the author.\textsuperscript{9-10} For each fuzzy input 11 evenly distributed triangular membership functions are chosen, resulting in 121 rules. Each membership function has a base width of 0.4. For the FMRLC the inverse-model knowledge base of the process needs to be developed. This knowledge base does not necessarily need to exhibit high accuracy; however, it needs to exhibit the right output control directionality. The
inputs to the FMRLC (Fig. 7) are the output voltage error and the output voltage error derivative.

The error derivative is proportional to the output voltage derivative $V_o'$, where the derivative of $V_o$ is approximately proportional to the inductor current $I_I$, from Eq. (2) $V_o' \approx V_o$, and Eq. (4) for $I_o$ is approximately constant over a conduction cycle. From the frequency response of $\hat{i}_i / d$ (Fig. 4), it is evident that the response of the inductor current to the duty cycle is highly undamped. This result was expected, since very little damping was used in terms of the $R_c$ value chosen, purposely, to make the control design more challenging. Therefore, in constructing this knowledge base the elements associated with the error derivative that can cause a sign reversal of the control output variable are zeroed out (Fig. 8). Simulations, not shown here, showed that the time response of the closed-loop system will stall out before the output voltage reaches its reference and that the output voltage will oscillate at that point if these elements of the fuzzy model have other than zero values.

Figure 9 shows the closed-loop step response of the FMRLC system. The reference model of the controller has been modified to automatically reset every time the output voltage recovers and starts moving toward the set point.
order to achieve a damped response. The reference model chosen for this controller is a first-order type with the transfer function

\[ G_r = \frac{\omega_r}{s + \omega_r} \]  

The value of \( \omega_r \) was chosen to approximate the natural frequency of the converter to an open-loop step response. The gains of the FMRLC per the tuning guidelines have been selected with the following values:

\[
\begin{bmatrix}
\kappa_r & \kappa_c & \kappa_r & \kappa_c
\end{bmatrix} = \begin{bmatrix}
0.01 & 2 \times 10^{-7} & 4.3 \times 10^{-5} & 8 \times 10^{-4} \\
0 & 120 & 3000 & 4714
\end{bmatrix}
\]

The FMRLC controller knowledge base was initialized with zeros as its elements, indicating no knowledge of how to control the process initially. The resulting controller knowledge base from the learned control law, which was derived from the step response simulation (Fig. 9), is shown in Fig. 10. This figure also shows, in boxes, the elements modified and the modified values, outside the boxes, to be used as the knowledge base for the straight fuzzy controller (i.e., with the learning mechanism disabled). The modifications are primarily in the region associated with sign reversal of the controlled variable because of the undamped inductor current response. Some values other than zero are allowed near the center region of the knowledge base, where the tendency for sign reversal is not too drastic. This allowance was made to achieve a relatively faster response at the region of the knowledge base that becomes active near steady-state operation of the process.

As mentioned before, the FMRLC controller can be used for the final control of the process. In fact, it shows very good response to step load changes. However, if small-signal analysis is desired, the learning controller is not suitable because the controller nonlinearity is nonstationary.

Figure 9.—FMRLC CMC response with 3.5-kW and 6-kW load changes.

Figure 10.—Learned knowledge base and modified elements (in boxes) used for fuzzy control knowledge base.
3.2 Fuzzy Current-Mode Control

The conventional fuzzy controller has been implemented here for CMC by disabling the learning mechanism in Fig. 7. The control knowledge base learned from applying the FMRLC CMC (Fig. 10 with indicated modifications) was used for the fuzzy CMC controller. Figure 11 shows step responses of the conventional fuzzy CMC system.

4. Stability Analysis of Fuzzy Current-Mode Control

Various nonlinear stability analysis methodologies could be applied for analyzing fuzzy control systems. Some are the Lyapunov’s indirect method, the circle criterion approach, and describing function analysis (DFA). The stability analysis covered in this section is based on the DFA approach supplemented with Bode analysis.

4.1 Describing Function Analysis

First, some background will be presented in computing the describing function. For an input \( e(t) = C \sin(\omega t) \) to the nonlinear fuzzy controller there will be a periodic output \( u(t) \). Expanding \( u(t) \) into a Fourier series results in

\[
u(t) = \frac{a_0}{2} + \sum_{n=1}^{\infty} \left[ a_n \cos(n\omega t) + b_n \sin(n\omega t) \right]
\]

The Fourier coefficients \( a_n \) and \( b_n \) are functions of \( C \) and \( \omega \) and are determined by

\[
a_n = \frac{1}{\pi} \int_{-\pi}^{\pi} u(t) \cos(n\omega t) dt
\]

\[
b_n = \frac{1}{\pi} \int_{-\pi}^{\pi} u(t) \sin(n\omega t) dt
\]

Assuming that the fundamental component \( u_1(t) \) is dominant (i.e., \( a_0 \) and the higher order harmonics can be neglected), then

\[
u(t) \approx u_1(t) = a_1 \cos(\omega t) + b_1 \sin(\omega t) = M(C, \omega) \sin(\omega t + \phi(C, \omega))
\]

where

\[
M(C, \omega) = \sqrt{a_1^2 + b_1^2}, \phi(C, \omega) = \arctan\left( \frac{a_1}{b_1} \right)
\]

Equation (19) can be written in complex form as

\[
u_1 = M(C, \omega)e^{j[\omega t + \phi(C, \omega)]} = (b_1 + ja_1)e^{j\omega t}
\]

The describing function of the nonlinear fuzzy controller is defined to be the complex ratio of the fundamental component representing the controller nonlinearity to the input sinusoid

\[
N(C, \omega) = \frac{u_1}{C \sin(\omega t)} = \frac{M(C, \omega)e^{j[\omega t + \phi(C, \omega)]}}{Ce^{j\omega t}} = \frac{1}{C} (b_1 + ja_1)
\]

Therefore, the nonlinear controller can be treated as if it were a linear element in a closed-loop control system consisting of the controller \( N(C, \omega) \) and the process \( G(j\omega) \) represented by Eq. (13). The harmonic balance equation of this closed-loop control system is

\[
G(j\omega)N(C, \omega) + 1 = 0
\]

This equation can also be written as

\[
G(j\omega) = -\frac{1}{N(C, \omega)}
\]

If the closed-loop system has any limit cycles, its amplitude and frequency can be predicted by solving Eq. (23). If there are no solutions, there are no harmonic oscillations. However, solving Eq. (23) can be quite complex, especially for higher order systems, and it is best to solve this equation graphically by plotting \(-1/N(C, \omega)\) against \(G(j\omega)\) and finding its intersection points. A limit cycle to exist the intersection must occur at the same frequency \( \omega \). The values \( C \) and \( \omega \), at this intersection point, are the amplitude and frequency of the harmonic oscillation. If points near the intersection and along the increasing \( C \) side of the curve \(-1/N(C, \omega)\) are not encircled by the curve \(G(j\omega)\), the corresponding limit cycle is stable. Otherwise, the limit cycle is unstable.

For experimental evaluation of the fuzzy controller describing function, first the fuzzy controller will be excited with sinusoidal frequency sweeps of different amplitudes to compute the control output \( u(t) \). The input sinusoidal sweep function is constructed here as

\[
e(t) = C \sin(2\pi\omega t)
\]
where

\[ \alpha = 1 + \frac{(f_s - f_f)}{f_s} t_c \]

and \( f_s, f_f, \) and \( t_c \) are the starting frequency of the sinusoidal sweep, the final frequency, and the simulation time, respectively. The minimum sweep frequency is chosen to be at least a decade below the expected crossover frequency of the closed-loop gain, and the maximum sweep frequency is chosen to be equal to the subharmonic frequency (i.e., half the switching frequency). After the control outputs are computed for different values of \( C \), FFT’s are used to compute transfer function estimates of Eq. (21) as

\[ N(C,\omega) = \frac{P_{eu}(C, \omega)}{P_{ee}(C, \omega)} \tag{25} \]

where \( P_{eu} \) and \( P_{ee} \) are the cross spectrum of \( e \) and \( u \) and the power spectrum of \( e \), respectively.

Figure 12 shows the transfer function estimates for different sweep amplitudes. MATLAB was used to compute these transfer functions in Eq. (25). These transfer functions were approximated with poles and zeros by drawing the corresponding straight-line asymptotes. A slope transition of the transfer function indicates first- or second-order zeros or poles depending on the direction and order of the transition. The damping of the second-order responses is a measure of the sharpness of the response transition. Occasionally, final adjustments need to be performed to match the phase responses of Eq. (25), not shown here. On this basis the transfer function approximations for the responses of Eq. (25), displayed in Fig. 12, are of the form

\[ N_a(C, s) = K \frac{P_{eu}(C, s)}{P_{ad}(C, s)} \tag{26} \]

where \( P_{eu}(C, s) \) and \( P_{ad}(C, s) \) are the approximation polynomials of the numerator and denominator, respectively. All the polynomials, as a function of the sweep amplitude \( C \), are found to have the same general characteristic as

\[ P_{eu}(s) = \left( \frac{s^2}{\omega_c^2} + \frac{2\zeta_1 s}{\omega_c} + 1 \right) \left( \frac{s^2}{\omega_2^2} + \frac{2\zeta_2 s}{\omega_2} + 1 \right) \left( \frac{s^2}{\omega_3^2} + \frac{2\zeta_3 s}{\omega_3} + 1 \right) \]

where

\[ \omega_c = \frac{f_s - f_f}{t_c} \]

and \( \zeta_1, \zeta_2, \zeta_3 \) are zero damping factors.

Figure 13 shows a frequency response based on FFT’s (Eq. (25)) and its approximation (Eq. (26)) for \( C = 2.0 \). The approximations have less accuracy at low frequencies. However, the low-frequency response will have little influence approximately one frequency decade above, where the main interest of the response lies (i.e., at the neighborhood of the crossover frequency), as will be seen later. For the transfer function approximations shown in Fig. 14 corresponding to Eq. (26) the parameters of the transfer functions are

\[
\begin{bmatrix}
 K_1 & K_2 & K_3 & K_4 & K_5 & K_6 & K_7 & K_8 & K_9 & K_{10} \\
 0.1 & 3000 & 625 & 720 & 1770 & 375 & 850 & 6000 & 29 & 28.57 \\
 2.0 & 3000 & 325 & 450 & 720 & 1770 & 375 & 850 & 4000 & 29 & 32.60 \\
 20. & 3000 & 325 & 450 & 720 & 1770 & 375 & 850 & 3000 & 25 & 29.60 \\
 60. & 1500 & 325 & 450 & 720 & 1770 & 375 & 850 & 3000 & 29 & 26.54
\end{bmatrix}
\]

As discussed before, Eq. (23) is solved graphically by plotting its Nyquist, Fig. 15, of \( G(j\omega) \) represented by Eq. (13) and \(-1/N(C,\omega)\), where \( N(C,\omega) \) is represented by

![Figure 12](image1.png)

![Figure 13](image2.png)
Figure 14.—Approximated transfer functions of fuzzy controller by applying sinusoidal sweeps of different amplitudes.

The overall input-to-output transfer function of the closed-loop system will have the characteristic equation of $G(s)N(s) + 1 = 0$, the same as Eq. (23). From this characteristic equation it is observed that when $\mathcal{L}_{cl} = -1$, or in phasor terms $\mathcal{L}_{cl} = 0$ dB (180°), the characteristic equation and therefore the overall closed-loop transfer function will have a zero denominator. Therefore, the system will be unstable for $\mathcal{L}_{cl} = -1$. The difference, between the actual phase angle of $\mathcal{L}_{cl}$ and 180° at the point where $\mathcal{L}_{cl}$ crosses 0 dB, is defined as the system stability phase margin. Similarly, the gain margin of the system is defined to be the difference between 0 dB and the actual magnitude of $\mathcal{L}_{cl}$ when the phase of $\mathcal{L}_{cl}$ crosses 180°. When the system phase and/or gain margins are relatively small, the system will normally exhibit an oscillatory response, similar to an underdamped response with increased sensitivity.

Figures 16 and 17 show the closed-loop gain responses, based on the converter transfer function (Eq. (13)) and the fuzzy controller transfer function (Eq. (26)), at 100% power and at the borderline between CCM and DCM, respectively. In both Figs. 16 and 17 the converter has less phase margin for larger values of $C$. For instance, for $C = 60$ the phase margins are -9° and -5°, respectively, for loads of 6 kW and 650 W. At low values of $C$ the corresponding phase margins for high and low power levels are -36° and -20°, respectively. Theoretically, the gain margins are infinite in all cases, since the phases do not cross the 180° line. However, there is another measure of stability, conditional stability, which in brief is a measure of how close the phase approaches 180° while the magnitude approaches 0 dB. Not shown here, the phase margins can be improved by adjusting the values of the membership functions (Fig. 10 at the center region of the knowledge base) to move them closer to the origin.
Figure 16.—Closed-loop gain of the buck converter with fuzzy CMC control at 6 kW.

will make the response more damped, but slower, with a little more overshoot. Of course, improving the filter design, which was purposely underdamped, is another way to improve the stability margins.

4.2.2 Output impedance.—Another important measure of system performance is the converter output impedance. A source supplying a single or an aggregate load, as a system, will be subjected to additional stability criteria at the source-load interface as

\[ G_f(s) = G_s(s)G_l(s)\left[1 + \frac{Z_o(s)}{Z_l(s)}\right] \] (28)

where \( G_s(s), G_l(s), \) and \( G_f(s) \) are the input-to-output transfer functions of the overall system, the source, and the load, respectively; \( Z_o(s) \) is the source output impedance; and \( Z_l(s) \) is the load input impedance. For the power converter in Fig. 1 its open-loop output impedance, which is the source impedance of the output filter, including the inductor effective series resistance \( R_{in} \), is

\[ Z_p(s) = R_{in} \frac{C_f L_f s^2 + R_c s + 1}{C_f L_f s^2 + C_f R_c s + 1} \] (29)

for \( L_f \gg L_c \) and \( R_c \gg R_{in} \). The closed-loop output impedance is

\[ Z_o(s) = \frac{Z_p(s)}{1 + L_c(s)} \] (30)

where \( Z_p(s) \) is the open-loop output impedance (i.e.,

\[ Z_p = \left. \frac{V_o}{i_o} \right|_{d=0} \).
Figure 18 shows the closed-loop output impedance of the converter at power levels of 6 kW and 650 W and for \( C = 1.0 \), with a parasitic value of \( R_{in} \). The phase of the impedances in Fig. 18 needed to be unramped. A complete analysis will include the output impedance at different values of \( C \) and an actual load impedance, to study the stability margins of the system. For such an analysis the phase margin, measured at the intersecting points of the two impedances and based on Eq. (28), will be computed as the addition of the load impedance phase minus the source impedance phase subtracted from 180°. The output impedance can also be improved by redesigning the output filter.

5. Concluding Remarks

In this paper fuzzy control was applied to traditional current-mode control (CMC) by replacing the typical lead-lag compensation design. It was demonstrated that, with proper design of the Fuzzy Model Reference Learning Control (FMRLC), very good time responses to load step changes can be obtained even with a highly undamped power converter design. The control knowledge base learned with the FMRLC was used to develop a straight fuzzy controller for the converter in order to conduct small-signal analysis. The paper demonstrated the ability to conduct small-signal analysis of the converter with fuzzy control by developing a small-signal model of the fuzzy controller using sinusoidal sweeps and fast Fourier transforms. The small-signal analyses conducted by employing the describing function and Bode analysis showed the feasibility of applying fuzzy control to CMC, while still employing powerful traditional analysis tools.

References

In this paper a current-mode control (CMC) methodology is developed for a buck converter by using a fuzzy logic controller. Conventional CMC methodologies are based on lead-lag compensation with voltage and inductor current feedback. In this paper the converter lead-lag compensation will be substituted with a fuzzy controller. A small-signal model of the fuzzy controller will also be developed in order to examine the stability properties of this buck converter control system. The paper develops an analytical approach, introducing fuzzy control into the area of CMC.