One-Dimensional Coupled Ecosystem-Carbon Flux Model for the Simulation of Biogeochemical Parameters at Ocean Weather Station P

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June 2000
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Acknowledgments

We acknowledge the support provided by NASA’s Ocean Biogeochemistry Program (NASA RTOP 622-51-30). We are thankful to Dr. Paulette Murphy for enlightening discussions regarding the chemical thermodynamics aspects of this work. We are also thankful to Dr. David Antoine for sharing his carbon chemistry Fortran code with us. Finally, we would like to acknowledge Dr. Ina Tegen for the atmospheric dust model results, Moss Landing Marine Labs for the iron data, and Dr. Ragu Murtuggude for providing the simulated (OGCM) ocean currents.

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The global oceans contain approximately 50 times as much CO$_2$ in dissolved forms as that in the atmosphere, while the land biosphere including the biota and soil carbon contains about 3 times as much carbon (as CO$_2$) as that in the atmosphere (Sundquist, 1985). Thus the spatial and temporal variability of CO$_2$ fluxes over the ocean are crucial for projecting the future level of atmospheric CO$_2$.

One of the most important parameters of the oceanic CO$_2$ system is the partial pressure of dissolved carbon dioxide, pCO$_2$, in the surface ocean (Takahashi et al., 1993; Wong and Chan, 1991). The difference between pCO$_2$ in surface seawater and in the overlying atmosphere defines the source and sink areas of CO$_2$ over the global oceans. Since the high latitude waters are probably undersaturated with respect to CO$_2$ in the summer (Keeling, 1968), these oceanic areas could play an important role in climate-CO$_2$ feedback processes by removing large quantities of CO$_2$ from the atmosphere (Wong and Chan, 1991). Temperate and polar oceans of both hemispheres are the major sinks for atmospheric CO$_2$, whereas the equatorial oceans are the major sources for CO$_2$ (Takahashi et al., 1997). Thus, the evaluation of the air-sea exchange of CO$_2$ is crucial to determine local and global balances of carbon in the atmosphere-ocean system.

The evaluation of the atmosphere-ocean CO$_2$ exchange is regulated by the gradient of pCO$_2$ across the air-sea interface, the gas transfer velocity (or piston velocity), and the solubility of CO$_2$ in water. There are a few methods available for evaluating the transfer velocity of CO$_2$ air-sea exchange, which can be obtained by field measurements (Broecker and Peng, 1974) or in the laboratory (Liss, 1988). Field methods were applied using a variety of data sets obtained from numerous experiments, e.g., Barbados Oceanographic and Meteorological Experiment (BOMEX), Geochemical Ocean Sections Study (GEOSECS), and Transient Tracers in the Ocean (TTO) programs (Broecker and Peng, 1971; Peng et al., 1974; Peng et al., 1979; Smethie et al., 1985; Batrakov et al., 1981). Laboratory methods using wind/wave tunnel experiments can be used to relate the wind speeds with the measured transfer velocities (Liss and Merlivat, 1986). This was the approach employed in the Programme Français Océan-Climat en Atlantique Equatorial (FOCAL) described by Andrié et al. [1986], Oudot and Andrié [1986], and Oudot et al. [1987]. In addition to the GEOSECS and TTO programs, there are also some studies on the variability of the oceanic CO$_2$ system in the subarctic Atlantic Ocean (Takahashi et al., 1983; Takahashi et al., 1985), the tropical Atlantic Ocean (Oudot and Andrié 1989), the western Pacific Ocean (Fushimi, 1987; Inoue et al., 1987), the Southern Ocean (Inoue and Sugimura, 1988), and the subarctic North Pacific (Gordon et al., 1971; 1973; Takahashi, 1989; Murphy et al., 1998).

The seasonal and interannual variations of CO$_2$ in the surface oceans are not only affected by the air-sea exchange physical processes but also by the photosynthetic uptake of CO$_2$ by phytoplankton. For instance, spring phytoplankton blooms in the surface waters of the North Atlantic Ocean can cause a precipitous reduction of surface water pCO$_2$, CO$_2$ and nutrients in a span of a couple of weeks. The mechanisms that drive this large biogeochemical variability were modeled by previous investigators (for example; Taylor et al., 1991). In contrast, seasonal changes in CO$_2$ and nutrients are more gradual in the North Pacific and macro-nutrients are only partially consumed in the surface waters of the subarctic North Pacific Ocean (Takahashi et al., 1993).
In this TM, we describe the model functionality and analyze its application to the seasonal and interannual variations of phytoplankton, nutrients, \( pCO_2 \), and \( CO_2 \) concentrations in the eastern subarctic Pacific at Ocean Weather Station P (OWS P, 50° N 145° W). We use a verified one-dimensional ecosystem model (McClain et al., 1996), coupled with newly incorporated carbon flux and carbon chemistry components, to simulate 22 years (1958-1980) of \( pCO_2 \) and \( CO_2 \) variability at Ocean Weather Station P (OWS P). This relatively long period of simulation verifies and extends the findings of previous studies (Wong and Chan, 1991; Archer et al., 1993; Antoine and Morel, 1995a; Antoine and Morel, 1995b) using an explicit approach for the biological component and realistic coupling with the carbon flux dynamics. The slow currents and the horizontally homogeneous ocean in the subarctic Pacific make OWS P one of the best available candidates for modeling the chemistry of the upper ocean in one dimension. The chlorophyll and ocean currents composite for 1998 shown in Figure 1 illustrates this premise. The chlorophyll concentration map was derived from SeaWiFS data and the currents are from an OGCM simulation (R. Murtugudde, personal communication).

![Figure 1. Chlorophyll and ocean currents composite for 1998 based on SeaWiFS data and OGCM simulations, respectively. The black dot denotes the location of OWS P.](image-url)
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1.0 MODEL DESCRIPTION

The model consists of a previously verified (McClain et al., 1996) four-component ecosystem model, coupled with newly added carbon dioxide and oxygen components. The ecosystem model is physically forced by sea surface temperature (SST) and mixed layer depth values originating from the Garwood mixed layer model (Garwood, 1977). A description of the mixed layer model validation and application to the forcing of the ecosystem model is given in McClain et al. [1996] and is not reproduced here. The ecosystem model has some modifications which are explicitly defined in McClain et al. [1998] and McClain et al. [1999]. In addition to these modifications, two new components, iron (Fe) and dissolved organic carbon (DOC), were added to the model. Previous studies (Maldonado et al., 1999; Boyd et al., 1996; Martin et al., 1989) showed that the phytoplankton growth in the subarctic Pacific is generally iron limited. We added the iron component to obtain more accurate simulations of nitrate, phytoplankton and community production. The DOC component was added to more accurately reproduce the seasonality of the net community production via the respiration of DOC by bacteria during the fall-winter period. In addition, the light penetration model uses a different spectral set of water absorption (a_w) coefficients and phytoplankton specific absorption (a_p) coefficients. Figure 2 shows the spectral variability of these coefficients. The clear sky irradiance is modified to account for the observed cloud cover by applying a power law correction (McClain et al., 1996) tuned to yield the observed climatological monthly mean surface irradiances (Dobson and Smith, 1988). The climatological monthly irradiance, obtained by averaging the daily mean irradiance for each month and for the entire period of simulation (1960-1980), is shown in Figure 3. The seasonal variability shown in Figure 3 agrees with the values given by Dobson and Smith [1988]. The coefficient for the cloud attenuation formulation of McClain et al. [1996], given by

\[ E_o = E_{	ext{clear}} [1 - 0.53 \text{Cld}^{0.5}] \]

was changed from 0.53 to 0.45 to better match the climatological cloudy sky radiation \( E_o \) of Dobson and Smith [1988]. This new coefficient also provided an improved match of the simulated SST with the observed values. The cloud cover (Cld, in oktas) was obtained from OWS P observations.

The following system of coupled differential equations simulates the dynamics of phytoplankton nitrogen (P), zooplankton nitrogen (Z), ammonium (NH₄), nitrate (NO₃), iron (Fe), dissolved organic carbon (DOC), total carbon dioxide (CO₂), and oxygen (O₂) stocks within the upper ocean:

\[
\frac{\partial P}{\partial t} + w \frac{\partial P}{\partial z} + \frac{\partial \sigma P}{\partial z} - \frac{\partial}{\partial z} \left[ K \frac{\partial P}{\partial z} \right] = GP - mP - r_P P - IZ \tag{2}
\]

\[
\frac{\partial Z}{\partial t} + w \frac{\partial Z}{\partial z} - \frac{\partial}{\partial z} \left[ K \frac{\partial Z}{\partial z} \right] = (1 - \gamma)IZ - (g + hZ)Z - r_Z Z \tag{3}
\]

\[
\frac{\partial \text{NH₄}}{\partial t} + w \frac{\partial \text{NH₄}}{\partial z} - \frac{\partial}{\partial z} \left[ K \frac{\partial \text{NH₄}}{\partial z} \right] =
\]

\[
(a_p m + r_P P + \pi_1 G) P + [a_z (g + h_z) + r_z + c_{pel} \gamma I] Z - A_N + k_{rc} \text{DOC} \frac{N}{C} \tag{4}
\]

\[
\frac{\partial \text{NO₃}}{\partial t} + w \frac{\partial \text{NO₃}}{\partial z} - \frac{\partial}{\partial z} \left[ K \frac{\partial \text{NO₃}}{\partial z} \right] = -\pi_2 GP + A_N \tag{5}
\]
Figure 2. Spectral light absorption coefficient for sea water ($a_w(\lambda)$) and specific chlorophyll absorption coefficient ($a_p^*(\lambda)$) adopted in the spectral downwelling irradiance model formulation.

Figure 3. Comparison between the climatological daily averaged cloudy sky surface solar irradiance from Dobson and Smith [1988] and model simulation.
A flow chart of the coupled model, showing the interaction between its major components, is shown in Figure 4. Table 1 summarizes the parameters used in Equations (2) through (9) and derived quantities. The ratios $CN$, $O_{2}/C$ are the carbon-to-nitrogen and oxygen-to-carbon Redfield ratios (106:16, 138:106), respectively. The iron-to-nitrogen ratio is assumed to be 19.8 µmol/mol. The Kroenecker delta ($\delta(z=0)=1$; $\delta(z>0)=0$) is used to denote that the carbon dioxide and oxygen fluxes ($FCO_2$ and $FO_2$, respectively) are applied at the air-sea interface only. Details of the Ekman upwelling ($w_e$) and vertical diffusion ($K_v$) formulations, the numerical method to solve the coupled differential equations, and the various parameters used by the ecosystem model components are given in McClain et al. [1996]. The Ekman upwelling profile function was modified to account for depth attenuation below the Ekman depth ($D_e$). The formulation for $D_e$ (Pond and Pickard, 1978) as a function of wind speed $W$ and latitude $f$, the shape function $R(z)$, and the vertical velocity are given by:
\[ D_e = \pi \left( \frac{2K_e}{f} \right)^{1/2} \]  
(10a)

\[ D_e \approx \frac{4.3W}{[\sin(\phi)]^{0.5}} \]  
(10b)

\[ R(z) = \left[ 1 - \cos \left( \frac{\pi z}{2D_e} \right) e^{-\frac{\pi z}{D_e}} \right], \quad \text{for} \ z \leq D_e \]  
(11)

\[ R(z) = \left[ 1 - \left( \frac{z-D_e}{z_{max}-D_e} \right)^{15} \right] \cos \left[ \frac{\pi (z-D_e)}{2(z_{max}-D_e)} \right], \quad \text{for} \ z > D_e \]  
(12)

\[ w_c = w_0 \cdot R(z) \]  
(13)

Equation 10b \textit{(Pond and Pickard, 1978)} produces nearly identical values of \( D_e \) as the standard Ekman formula given in Equation 10a. The standard formula introduced numerical instabilities, so Equation 10b was used. The shape function \( R(z) \) is constructed based on McClain \textit{et al.} [1996] for the portion above \( D_e \) (equation 11). For \( z > D_e \), \( R(z) \) is formulated such that continuity at the inflection points \( z=D_e \) and \( z=z_{max} \) is maintained, and that \( R(z) \) decreases to zero monotonically towards \( z=z_{max}=350 \) meters (equation 12).

The net community production, \( N_p \), is defined as the summation of all sources and sinks of nitrate and ammonium in equations (3) and (4):

\[ N_p = (a_p m + r_p - G) P + [a_z (g + h_z) + r_z + c_{pel} \gamma I] Z + k_{rc} DOC \frac{N}{C} \]  
(14)

The ratio \( N/C \) is 16:106 (Redfield ratio). The effective growth is a function of the maximum growth \( (G_0) \), light limitation \( (L_{lim}) \), and nutrient limitation \( (N_{lim}) \):

\[ G = \beta \; G_0 \; e^{(k_{gp} T)} \]  
(15)

\[ \beta = E_{lim} \min (N_{lim}, F_{e, lim}) \]  
(16)

\[ E_{lim} = 1 - \exp \left( -\frac{E_{in}}{I_{k_{max}}} \right) \]  
(17)

\[ F_{e, lim} = \frac{F_e}{(K_{F_e} + F_e)} \]  
(18)

\[ N_{lim} = NH_{4, lim} + NO_{3, lim} \]  
(19)

\[ NO_{3, lim} = \frac{NO_3}{(K_{NO3} + NO_3) (K_{NH4} + NH_4)} \; (1 - NH_4) \]  
(20)

\[ NH_{4, lim} = \frac{NH_4}{(K_{NH4} + NH_4)} \]  
(21)
2.0 MODEL FORCING AND BOUNDARY CONDITIONS

The Neumann boundary condition, $\partial X/\partial z=0$, is applied at both the surface and lower (350 m) model domain boundaries for $P$ and $Z$. Initial profiles of temperature and $NO_3$ were obtained from winter and annual climatologies (Conkright, et al., 1994), respectively. Depth-independent initial concentrations of $P$ and $Z$ are 0.2 and 0.1 mmol N m$^{-3}$, respectively. Observed fall profiles of $NH_4$ were used as initial conditions (Frost, 1993). At the lower boundary, fixed values equal to 0.0 and 41.5 mmol N m$^{-3}$ were applied to $NH_4$ and $NO_3$, respectively. The Neumann condition was applied at the surface.

For $TCO_2$ and $O_2$, climatological values at the surface and at the bottom were used to construct the initial linear profiles (surface $TCO_2=2050$ mmol m$^{-3}$ and bottom $CO_2=2100$ mmol m$^{-3}$; surface $O_2=320$ mmol m$^{-3}$ and bottom $O_2=100$ mmol m$^{-3}$). A fixed value equal to the initial condition was applied at the lower boundary. The following formulations for the $CO_2$ and $O_2$ gas exchanges were applied in the form of flux boundary conditions ($FCO_2$ and $FO_2$ in mmol m$^{-2}$ d$^{-1}$) at the sea-air interface:

\[
FCO_2 = K_{oa} \Delta pCO_2 \quad (22)
\]
\[
FO_2 = K_o [O_2(sat) - O_2] \quad (23)
\]
\[
\alpha = \exp[-60.2409 + \frac{9345.17}{T} + 23.3585 \log \left( \frac{T}{100} \right) + S(0.023517 - 0.023656T + 0.0047036T^2)] \quad (24)
\]

where, $k$ is the gas exchange coefficient (piston velocity, in m/d) which is a function of water temperature and wind speed (Wanninkhof, 1992; Liss and Merlivat, 1986), $\alpha$ is the $CO_2$ solubility in seawater (in mmol m$^{-3}$ μatm$^{-1}$) which is a function of temperature and salinity (Weiss, 1974), $\Delta pCO_2$ (in μatm) is the difference between air and sea $pCO_2$, and $O_2(sat)$ is the oxygen saturation concentration (in mmol m$^{-3}$) in seawater which is a function of temperature and atmospheric pressure (Weiss, 1970).

The eolian iron flux, $FFe$, is given by:

\[
FFe = \frac{C_{dust} S_{Fe} Pr C_{Fe} S_{Fe}}{55.84} \quad (25)
\]

where, $C_{dust}$ is the seasonal atmospheric dust concentration in ng/(kg of air) from Tegen and Fung [1994], $S_{Fe}=1000$ is the scavenging ratio (Duce, 1995), $Pr$ is the daily National Centers for Environmental Prediction (NCEP) precipitation in kg/m$^2$/d, $C_{Fe}=0.035$ is the iron mass fraction in the dust, and $S_{Fe}=0.1$ is the soluble iron fraction. The numerical factors are used to convert dust concentration to an iron flux ($FFe$) in pmol/m$^2$/d. The seasonal variability of precipitation and the iron flux for the period of 1970-1980 is shown in Figure 5.
Table 1. Summary of model variables and input parameter definitions and values. Initial surface and bottom concentrations are provided when appropriate

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Value</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>P</td>
<td>0.2</td>
<td>Initial phytoplankton concentration (mmol N/m³)</td>
</tr>
<tr>
<td>Z</td>
<td>0.1</td>
<td>Initial zooplankton concentration (mmol N/m³)</td>
</tr>
<tr>
<td>NH₄</td>
<td>0.1</td>
<td>Initial ammonium concentration (mmol N/m³)</td>
</tr>
<tr>
<td>NO₃</td>
<td>Climatology</td>
<td>Initial nitrate concentration (mmol N/m³)</td>
</tr>
<tr>
<td>Fe</td>
<td>50/400</td>
<td>Initial iron concentration (pM)</td>
</tr>
<tr>
<td>DOC</td>
<td>10/0</td>
<td>Initial dissolved organic carbon (mmol C/m³)</td>
</tr>
<tr>
<td>TCO₂</td>
<td>2050/2100</td>
<td>Initial total CO₂ Concentration (mmol CO₂/m³)</td>
</tr>
<tr>
<td>O₂</td>
<td>320/100</td>
<td>Initial oxygen concentration (mmol O₂/m³)</td>
</tr>
<tr>
<td>π₁</td>
<td></td>
<td>Regenerated production fraction</td>
</tr>
<tr>
<td>π₂</td>
<td></td>
<td>New production fraction</td>
</tr>
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<td>KNO₃</td>
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<td>Half saturation for NO₃ uptake (mmol N/m³)</td>
</tr>
<tr>
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<td>Half saturation for NH₄ uptake (mmol N/m³)</td>
</tr>
<tr>
<td>KFe</td>
<td>35</td>
<td>Half saturation for Fe uptake (pM)</td>
</tr>
<tr>
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<td>1</td>
<td>Maximum zooplankton grazing rate (d⁻¹)</td>
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<tr>
<td>Nₚ</td>
<td></td>
<td>Net community production (mmol C/m³/d)</td>
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<td>Phytoplankton death rate (d⁻¹)</td>
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<td>Phytoplankton growth rate at 0 °C (d⁻¹)</td>
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<td>0.0633</td>
<td>Temperature sensitivity of algal growth (°C⁻¹)</td>
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<td>Respiration coefficient</td>
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<td>Temperature sensitivity of algal resp. (°C⁻¹)</td>
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<td>Maximum photoacclimation param. (µEin/m²/s)</td>
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<tr>
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<td>250 (&gt;60m)</td>
<td>Maximum photoacclimation param. (µEin/m²/s)</td>
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<td>Ammonium inhibition of NO₃ uptake</td>
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<td>Maximum phytoplankton sinking Rate (m/d)</td>
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<td>Chlorophyll to nitrogen ratio</td>
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<td>g</td>
<td>0</td>
<td>Zooplankton death rate (d⁻¹)</td>
</tr>
<tr>
<td>h</td>
<td>0.35</td>
<td>Quadratic coefficient of zooplankton mortality (mmol⁻¹ m³ d⁻¹)</td>
</tr>
<tr>
<td>Rₘₐₓ</td>
<td>4</td>
<td>Maximum zooplankton grazing rate (d⁻¹)</td>
</tr>
<tr>
<td>A</td>
<td>0.8</td>
<td>Ivlev constant (m²/mmol N)</td>
</tr>
<tr>
<td>TH</td>
<td>5</td>
<td>Maximum C threshold for Z grazing (mg C/m³)</td>
</tr>
<tr>
<td>γ</td>
<td>0.3</td>
<td>Unassimilated zooplankton ingestion Ratio</td>
</tr>
<tr>
<td>rₜₒ</td>
<td>0.019</td>
<td>Respiration rate for zooplankton at 0 °C (d⁻¹)</td>
</tr>
<tr>
<td>kₙᵣ</td>
<td>0.15</td>
<td>Temperature sensitivity of Z respiration (d⁻¹)</td>
</tr>
<tr>
<td>aₚ</td>
<td>0.2</td>
<td>Fraction of dead P converted to NH₄</td>
</tr>
<tr>
<td>aₜ</td>
<td>0.2</td>
<td>Fraction of dead Z converted to NH₄</td>
</tr>
<tr>
<td>aₚ'</td>
<td>0.1</td>
<td>Fraction of dead P converted to DOC</td>
</tr>
<tr>
<td>aₜ'</td>
<td>0.1</td>
<td>Fraction of dead Z converted to DOC</td>
</tr>
<tr>
<td>rₑc</td>
<td>0.01</td>
<td>Respiration rate of DOC into CO₂ (d⁻¹)</td>
</tr>
<tr>
<td>Aₙₘₐₓ</td>
<td>2.0</td>
<td>Maximum rate of nitrification (mmol/d)</td>
</tr>
<tr>
<td>Dₘₐₙ</td>
<td>0.0095</td>
<td>Minimum inhibition dosage for nitrification (W/m²)</td>
</tr>
<tr>
<td>Kₐₜ</td>
<td>0.036</td>
<td>Half saturation dosage for nitrification photoinhibition (W/m²/nm)</td>
</tr>
<tr>
<td>cₚₑl</td>
<td>0.8</td>
<td>Fecal pellet remineralization fraction</td>
</tr>
<tr>
<td>Kₑₘₜ</td>
<td>17.3</td>
<td>Minimum bottom eddy diffusion (m³/d)</td>
</tr>
</tbody>
</table>
Figure 5. Time series of precipitation rate and eolian iron flux for 1970-1980.

The 30-year $pCO_2$ atmospheric time series used to force the model is based on a least-squares fit to the 15 years (1978-1993) of $pCO_2$ observations in Cold Bay, Alaska, the closest long-term monitoring site at roughly the same latitude of OWS E. The $pCO_2$ time series is given by:

$$pCO_2(air) = A_0 + A_1 t + A_2 \sin\left(\frac{2\pi t}{12} + A_3\right) + A_4 \sin\left(\frac{2\pi t}{6} + A_5\right) + A_6 \sin\left(\frac{2\pi t}{4} + A_7\right)$$

(26)

where $t$ is the time in months, $A_0 = 280.8 \mu$atm is the intercept, $A_1 = 0.134 \mu$atm mo$^{-1}$ is the slope, the amplitudes ($A_2, A_4, A_6$) are 6.61, 3.01, and 0.87 $\mu$atm, respectively. The phases ($A_3, A_5, A_7$) are 0.77, -15.2, and 0.15 radians, respectively. Figure 6 shows the time series of atmospheric $pCO_2$ at Cold Bay, at Mauna Loa, and the synthesized signal (dashed line) using the analytical formula (26). Note that the long-term trend at Cold Bay and Mauna Loa are essentially identical, while there is a significant difference in the seasonal amplitudes. The fact that the trends are similar and the amplitudes are different can be attributed to atmospheric mixing processes. Specifically, the atmospheric seasonal mixing is imparted preferentially along latitude lines by virtue of stronger zonal flows in the atmosphere, allowing meridional gradients of $pCO_2$ to be much stronger than the zonal gradients. Conversely, the long-term trend in $pCO_2$ distribution is latitudinally more uniform because the meridional mixing time scale is short when compared to the $pCO_2$ trend due to anthropogenic sources.

Sensitivity tests were conducted off-line using the air-sea flux formulation implemented in the model. Four formulations were tested; Liss and Merlivat [1986], Tans et al. [1990], Wanninkhof [1992], and McGillis and Wanninkhof [1999]. Monthly averaged (1973-1978) winds, SST, salinity, and $\Delta pCO_2$ from Wong and Chan [1991] were used in these calculations. The Liss and Merlivat [1986] method provides the smallest sea-air flux (-2.19 mmol $CO_2$ m$^{-2}$ d$^{-1}$), whereas the methods of Tans et al. [1990] and Wanninkhof [1992] provide very similar results (Figure 7). The largest sea-air flux (-31.8 mmol $CO_2$ m$^{-2}$ d$^{-1}$) was provided by the McGillis and Wanninkof [1999] method since it is a cubic function of the wind speed ($W$).
Figure 6. Time series of Mauna Loa and Cold Bay atmospheric $pCO_2$. The dashed line represents the time series of $pCO_2$ used to force the model.

Figure 7. Comparison between sea-air $CO_2$ flux calculations using four different parameterizations for the gas exchange coefficient.
\[ K_o = [1.09W - 0.333W^2 + 0.078W^3] \left( \frac{Sc}{660} \right)^{-1/2} \]  

(27)

where \( Sc \) is the Schmidt number given as a function of temperature \( T \) as:

\[ Sc = 2073.1 - 125.62T + 3.627T^2 - 0.043219T^3 \]  

(28)

Equation (27) is used for the stand-alone flux calculations using climatological winds and various formulations for \( K \). For the actual model simulations we use the formula suggested by Wanninkhof and McGillis [1999] for short-term (< 1 day) winds given by:

\[ K_o = 0.0283W^3 \left( \frac{Sc}{660} \right)^{-1/2} \]  

(29)

We adopted the McGillis and Wanninkhof, [1999] method for this study. We conducted several sensitivity runs using different methods to derive the gas exchange coefficient. Figure 8 shows the \( \Delta pCO_2 \) and air-sea flux seasonal plots simulated by the model for three different gas exchange coefficient methods. The surface \( CO_2 \) fluxes obtained with the Liss and Merlivat [1986], Wanninkhof [1992], and Wanninkhof and McGillis [1999] are -6.8, -8.8, and -10.5 mmol/m²/d, respectively. The negative sign indicates that the flux is from the atmosphere to the ocean in all three cases. We discuss more details of these results in section 4.

Figure 8. Seasonal variability of sea-air \( \Delta pCO_2 \) and surface flux predicted by the model using three different gas exchange formulations.
3.0 OCEANIC \( pCO_2 \) FORMULATION

To calculate the \( pCO_2 \) concentration in seawater we must first understand the thermodynamics of the \( CO_2 \) system. The total \( CO_2 \) concentration in seawater, \( TCO_2 \), can be written as:

\[
TCO_2 = \left[ CO_2 \right] + \left[ HCO_3^- \right] + \left[ CO_3^{2-} \right]
\]  

(30)

where all quantities in square brackets are stoichiometric concentrations; \([CO_2]\) is the dissolved carbon dioxide, \([HCO_3^-]\) is the bicarbonate ion, and \([CO_3^{2-}]\) is the carbonate ion. Another quantity that influences the calculation of \( pCO_2 \) is the total alkalinity, \( TA \), which can be written as the sum of its major terms:

\[
TA = CA + \left[ B(OH)_4^- \right] + \left[ OH^- \right] - \left[ H^+ \right]
\]

(31)

where \( CA = [HCO_3^-] + 2[CO_3^{2-}] \) is the carbonate alkalinity, \([B(OH)_4^-]\) is the borate ion concentration, and \([OH^-]\) and \([H^+]\) are the products of \( H_2O \) dissociation. The partial pressure of dissolved \( CO_2 \) is defined by the relationship:

\[
pCO_2 = \frac{[CO_2]}{\alpha}
\]

(32)

where \([CO_2]\) represents the carbon dioxide in solution and \( \alpha \) (mmol m\(^{-3}\) μatm\(^{-1}\)) is the solubility of carbon dioxide in seawater (Weiss, 1974). We can calculate \([CO_2]\) from \( TCO_2 \) and \( TA \) (the values for the hydrogen ion activity, \( H^+ \), and the carbonate alkalinity, \( CA \), are also computed). We follow the recursive formulation of Antoine and Morel [1995] to estimate the dissolved \([CO_2]\) concentration

\[
[CO_2] = TCO_2 \cdot A + \left[ \frac{AK_r \cdot TCO_2 \cdot K_r - 4A + Z}{2(K_r - 4)} \right]
\]

(33)

where \( A \) takes the value of \( TA \) initially. \( K_r \) is equal to \( K_1/K_2 \), where \( K_1 \) and \( K_2 \) (mmol m\(^{-3}\)) are the dissociation constants of carbonic acid, which are a function of temperature and salinity (Goyet and Poisson, 1989). The other quantities required to calculate \([CO_2]\) are

\[
Z = \sqrt{(TCO_2 K_r)^2 + AK_r(2TCO_2 - A)(4 - K_r)}
\]

(34)

\[
H^+ = \frac{(\left[ CO_2 \right] K_1)}{2A} + \sqrt{\frac{(\left[ CO_2 \right] K_1)^2 + 8A[CO_2]K_1K_2}{2A}}
\]

(35)

\[
CA = TA - BR \frac{K_B}{K_B + H^+} \cdot \frac{K_w}{H^+} + H^+
\]

(36)

\[
K_1 = 10^{-pK_1}, K_2 = 10^{-pK_2}
\]

(37)

\[
pK_1 = \frac{812.27}{T} + 3.356 - 0.00171 S \log(T) + 0.000091 S^2
\]

(38)

\[
pK_2 = \frac{1450.87}{T} + 4.604 - 0.00385 S \log(T) + 0.000182 S^2
\]

(39)
\[ K_w = 10^{-pK_w} \]
\[ pK_w = \frac{3441}{T} + 2.241 - 0.09415 S^{0.5} \]
\[ \ln(K_B) = \frac{-8966.9 - 2890.53S^{0.5} - 77.9425S^{1.5} - 0.09963S^2}{T} + 148.0248 + 137.1942S^{0.5} + 1.62142S + (-24.4344 - 25.085S^{0.5} - 0.2474S) \log(T) + 0.053105TS^{0.5} \]

where \( BR = 0.00042S/35.0 \text{ mmol m}^{-3} \) is the borate concentration (Whitfield and Turner, 1981), and \( K_B \) and \( K_w \) are the dissociation constants for boric acid and sea water, respectively (Weiss, 1974).

The above equations are repeated, with the variable \( A \) taking the value of \( CA \) at the previous iteration, until \(| CA - A | < 10^{-8} \). The value of \( pCO_2 \) is then estimated according to:

\[ pCO_2 = \frac{TCO_2}{a\left(1 + \frac{K_1}{H^+} + \frac{K_1K_2}{H^{+2}} \right)} \]

Table 2 shows a comparison between \( pCO_2 \) values measured at OWS P (Wong and Chan, 1991) and those calculated using equations (33) through (44). The data were acquired during the winter of 1975 (17 January and 9 February). A very close agreement (less than 1%) is achieved between the observed and calculated \( pCO_2 \) values.

Table 2. Oceanic properties of surface sea water from OWS P in early 1975 (Wong and Chan, 1991). The measured (a) \( pCO2 \) values are compared with those calculated (b) using equations (30) through (43). The difference between measured and calculated values (ε) is 2.1 \( \mu \text{atm} \)

<table>
<thead>
<tr>
<th>Date</th>
<th>SST</th>
<th>SSS</th>
<th>TA</th>
<th>TCO2</th>
<th>pCO2,a</th>
<th>pCO2,b</th>
<th>ε</th>
</tr>
</thead>
<tbody>
<tr>
<td>17 Jan</td>
<td>5.8</td>
<td>32.656</td>
<td>2216</td>
<td>2039</td>
<td>312.6</td>
<td>310.5</td>
<td>-2.1</td>
</tr>
<tr>
<td>9 Feb</td>
<td>5.8</td>
<td>32.678</td>
<td>2203</td>
<td>2030</td>
<td>317.4</td>
<td>315.3</td>
<td>-2.1</td>
</tr>
</tbody>
</table>

Data collected during 1973-1978 (Wong and Chan, 1991) were used to validate and formulate model parameters. The salinity data is much sparser so that an analytical formulation must be obtained to provide an uninterrupted sequence of values to force the model. A regression of salinity versus temperature yields the linear relationship \( S = 32.8124 - 0.01719T \). The total alkalinity can be expressed as a linear function of salinity. For example, the linear formulation for \( TA \) of Clayton et al. [1995], with an intercept adapted to reproduce the mean \( TA \) values at OWS P, can be used to produce an hourly time series of \( TA \) values to force the model (\( TA = 117.8 + 64.232S \)). However, since the salinity at OWS P does not change significantly (32.59 to 32.72 psu), the model results are not significantly different than assuming a constant value for \( TA \). Also, there is little information available on the seasonal variability of \( TA \) at OWS P for model verification. Therefore, we used a constant value of 2215 \( \mu \text{eq/kg} \), which is also the value used by Antoine and Morel [1995b], and calculated at OWS P in January 1975 by Wong and Chan [1991]. Table 3 summarizes the parameters used in the geochemical portions of the model (iron flux and carbonate chemistry).
Table 3. Summary of parameters used in the iron flux formulation and carbonate chemistry

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Value</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>C_{a0}</td>
<td>Climatological</td>
<td>Atmospheric dust concentration (µg/kg of air)</td>
</tr>
<tr>
<td>S_{Fe}</td>
<td>1000</td>
<td>Iron scavenging ratio</td>
</tr>
<tr>
<td>C_{Fe}</td>
<td>0.035</td>
<td>Iron mass fraction</td>
</tr>
<tr>
<td>S_{Fe}</td>
<td>0.1</td>
<td>Soluble iron fraction</td>
</tr>
<tr>
<td>K_o</td>
<td>Eqs. 27, 29</td>
<td>Gas exchange coefficient</td>
</tr>
<tr>
<td>Sc</td>
<td>Eq. 28</td>
<td>Schmidt number</td>
</tr>
<tr>
<td>TA</td>
<td>2215</td>
<td>Total Alkalinity (µeq/kg)</td>
</tr>
<tr>
<td>[CO_2]</td>
<td>Eq. 33</td>
<td>Carbon dioxide in solution (mmol/kg)</td>
</tr>
<tr>
<td>pCO_2</td>
<td>Eqs. 32, 43</td>
<td>Partial pressure of CO_2 in sea water (µatm)</td>
</tr>
<tr>
<td>α</td>
<td>Eq. 24</td>
<td>CO_2 solubility in sea water (mmol/m^3/µatm)</td>
</tr>
<tr>
<td>CA</td>
<td>Eq. 36</td>
<td>Carbonate alkalinity (µeq/kg)</td>
</tr>
<tr>
<td>K_1, K_2</td>
<td>Eq. 37</td>
<td>Dissociation constants for carbonic acid</td>
</tr>
<tr>
<td>K_p, K_w</td>
<td>Eqs. 40, 42</td>
<td>Dissociation constants for borate and water</td>
</tr>
<tr>
<td>BR</td>
<td>0.00042S/35</td>
<td>Borate concentration (mmol/m^3)</td>
</tr>
<tr>
<td>H^+</td>
<td>Eq. 35</td>
<td>Hydrogen ion concentration</td>
</tr>
</tbody>
</table>

4.0 MODEL SKILL ASSESSMENT

4.1 Model Sensitivity to Forcing and Parameterization

Table 4 shows a summary of the model response to different forcing and parameterization. We provide a comparison between the model results and available data sets from OWS P in the next subsection. An additional parameter test was performed to evaluate the sensitivity of the carbon dioxide variables to changes in salinity. One of the objectives of this test is to evaluate the required sensitivity and accuracy of salinity remote sensors so that measurements can be useful in the determination of the surface carbon flux in the ocean.

Table 4. Summary of model sensitivity to different parameterizations. The criteria for improvements include agreement with data such as phytoplankton (P) concentration, primary productivity (PP), and pCO_2

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Range</th>
<th>Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>R_{w}</td>
<td>3.0-5.0</td>
<td>4.0 for best P, PP</td>
</tr>
<tr>
<td>g</td>
<td>Linear to quadratic</td>
<td>g=0.35Z^2 for best P, PP</td>
</tr>
<tr>
<td>Fe, DOC</td>
<td>Added components</td>
<td>Improved PP seasonality</td>
</tr>
<tr>
<td>a_{w}(λ) and a*(λ)</td>
<td>For OWS P and Warm Pool</td>
<td>Values for OWS P were used</td>
</tr>
<tr>
<td>E_{w}(λ)</td>
<td>Up to 14% adjustment</td>
<td>Improvement in SST</td>
</tr>
<tr>
<td>Gas exchange K_{w}(W^2)</td>
<td>1, 2, and 4xWanninkhof</td>
<td>4x best pCO_2 variability</td>
</tr>
<tr>
<td>K_{w}(w^3)</td>
<td>K_{w}=(0.0283W^3)/(Sc/660)^0.5</td>
<td>Best agreement with observed pCO_2</td>
</tr>
<tr>
<td>pCO_2 calculation from SST, S, TA and TCO_2</td>
<td>Antoine and Morel (1995), P.Murphy (personal communication), DOE</td>
<td>All within less than 5%</td>
</tr>
<tr>
<td>TCO_2 (350m)</td>
<td>Constant to seasonal</td>
<td>TCO_2=2100 best profile</td>
</tr>
<tr>
<td>CO_2 flux (FCO_2) forcing</td>
<td>Top layer, distributed within mixed layer (ML)</td>
<td>ML approach required for stability (large K_w only)</td>
</tr>
<tr>
<td>Iron flux (FFE) forcing</td>
<td>S_{w}=0.05.01.0.2.0.3</td>
<td>Best P, PP with S_{w}=0.05</td>
</tr>
<tr>
<td>Carbon Production</td>
<td>Cloern et al. (1995), Redfield Ratio</td>
<td>Redfield Ratio more internally consistent</td>
</tr>
</tbody>
</table>
We use the relationship of Millero et al. [1998], which depends on temperature ($T$) and salinity ($S$), to calculate the total alkalinity ($TA$) at each model time step

$$NTA = 2300-7.00(T-20)-0.158(T-20)^2$$

(44)

$$TA=NTA \frac{S}{35}$$

(45)

where $NTA$ is the salinity normalized alkalinity. The salinity is calculated from the regression on temperature based on the salinity and temperature data from OWS P

$$S=32.8124-0.01719T$$

(46)

We conducted two runs, one using the salinity derived from equation (46), and another using the salinity in equation (46) with a positive bias of 0.5 psu. We adopted the gas exchange coefficient of Wanninkhof and McGillis [1999] in both runs. The results are summarized in Table 5. The parameters that are most sensitive to the salinity variability are the $\Delta pCO_2$, and, consequently, the air-sea $CO_2$ flux. These are also the two variables with standard deviations larger than the mean. The dissolved $CO_2$ does not change much (< 1%). The 24.3% increase in $CO_2$ uptake from the atmosphere, due to the 0.5 psu increase in salinity, is compensated by an approximately equivalent decrease in the $CO_2$ supply via the bottom flux.

Note that the climatological $\Delta pCO_2$ mean is reduced with the increased salinity, but the surface air-sea flux into the ocean actually increases despite the very small change in the gas exchange coefficient. This result seems counter-intuitive at first glance but becomes clear after inspection of the seasonal variations of $\Delta pCO_2$ and $K$. Figure 9 shows the seasonal variability of the surface $CO_2$ flux, $\Delta pCO_2$ and $K$. The solid and dashed lines represent results from runs 1 and 2, respectively. The $K$ values for the two runs are virtually identical. Figure 9 clearly shows that the $\Delta pCO_2$ is largely positive from May through September and negative during the rest of the year. However, $K$ is largest during the winter, spring and fall vigorous wind forcing, but significantly reduced during May through August when the wind speeds subside at OWS P. This phase opposition of $\Delta pCO_2$ and $K$ explains why the surface flux increases despite a climatological decrease in the $\Delta pCO_2$ mean value. Note also that the $\Delta pCO_2$ from Run 2 is more negative during winter, spring and fall than the $\Delta pCO_2$ from Run 1.

### Table 5. Summary of sensitivity run based on a 0.5 psu salinity increase from Run 1 to Run 2.

The averages are based on years 1960-1980

<table>
<thead>
<tr>
<th></th>
<th>Run 1</th>
<th>Run 2</th>
<th>Difference</th>
<th>Percent</th>
</tr>
</thead>
<tbody>
<tr>
<td>$S$(psu)</td>
<td>32.67</td>
<td>33.17</td>
<td>0.5</td>
<td>1.5</td>
</tr>
<tr>
<td>$TCO_2$(µmol/kg)</td>
<td>2007.1 ± 22.7</td>
<td>2033.1 ± 22.6</td>
<td>26.0</td>
<td>1.3</td>
</tr>
<tr>
<td>$pCO_2$(µatm)</td>
<td>315.6 ± 23.5</td>
<td>314.2 ± 24.4</td>
<td>-1.4</td>
<td>0.5</td>
</tr>
<tr>
<td>$FCO_2$(gC/m²/yr)</td>
<td>-42.4 ± 47.9</td>
<td>-52.7 ± 55.6</td>
<td>-10.3</td>
<td>24.3</td>
</tr>
<tr>
<td>Bottom $CO_2$ Flux (gC/m²/yr)</td>
<td>-25.1 ± 8.2</td>
<td>-15.8 ± 5.5</td>
<td>9.31</td>
<td>37.0</td>
</tr>
<tr>
<td>$TA$(µeq/kg)</td>
<td>2201.2 ± 11.4</td>
<td>2234.9 ± 11.5</td>
<td>33.69</td>
<td>1.5</td>
</tr>
<tr>
<td>$CO_2$(µmol/kg)</td>
<td>14.8 ± 0.9</td>
<td>14.7 ± 0.9</td>
<td>-0.11</td>
<td>0.7</td>
</tr>
<tr>
<td>$G$(µmol/kg/µatm)</td>
<td>47.13 ± 3.98</td>
<td>47.0 ± 4.00</td>
<td>-0.13</td>
<td>0.3</td>
</tr>
<tr>
<td>$\Delta pCO_2$(µatm)</td>
<td>3.58 ± 26.77</td>
<td>2.15 ± 27.75</td>
<td>-1.43</td>
<td>39.9</td>
</tr>
<tr>
<td>$K$(mmol/m²/d/µatm)</td>
<td>1.376 ± 2.752</td>
<td>1.372 ± 2.744</td>
<td>-0.004</td>
<td>0.3</td>
</tr>
</tbody>
</table>
Figure 9. Seasonal variability surface flux, sea-air $\Delta pCO_2$, and gas exchange coefficient predicted by the model for two runs with a salinity difference of 0.5 psu.
4.2 Model-Data Comparison

Table 6 provides a comparison between model and observed (Wong and Chan, 1991) biogeochemical parameters. Both model and observed values are averaged over years 1973-1978. Primary production, chlorophyll and nitrate are depth-averaged (0-80 m). This particular model run uses the gas exchange coefficient ($K$) from Wanninkhof [1992]. The model primary production is within 20% of the observed value. Chlorophyll, nitrate, and SST are all within less than 5% of the observed values. The salinity is obtained via a regression with SST; thus it is not independent of the observations and should not be evaluated as a model parameter. A comparison between model (solid line) and observed (dotted line) seasonal temperature profiles, averaged over the overlapping model-data years (1958-1966), is shown in Figure 10. The agreement is quite good. The model profiles represent the seasonal variability of the temperature stratification and SST at OWS P reasonably well. A very small warming trend (0.001 °C/month not shown here) was identified below 175 meters (below the euphotic zone). We removed the trend after the fact for display purposes only. These small discrepancies do not significantly affect the model results.

![Figure 10. Comparison between model and observed seasonal temperature profiles averaged over the period of 1958-1966.](image-url)
The model $T\text{CO}_2$ is about 2% lower on average than the observed $T\text{CO}_2$. The mean atmospheric $p\text{CO}_2$ is within 3% of the measured mean. The largest uncertainty lies in the calculation of the air-sea $CO_2$ flux ($FCO_2$). The surface flux is the most elusive quantity in the oceanic $CO_2$ measurements and modeling. It depends on accurate measurements of $\Delta pCO_2$ and a robust formulation for the gas exchange coefficient ($K_o$), since direct measurements of the air-sea flux are not yet available. As we have shown in section 2, there are multiple gas exchange coefficient formulations in the literature which yield a wide range of values for a given wind speed. For example, as shown in Table 7, $FCO_2$ can change significantly depending on which formulation for $K_o$ is used. The value calculated from the observed $\Delta pCO_2$ and $K_o$ from Liss and Merlivat [1986] is -8.3 gC/m²/yr; if $K_o$ from Wanninkhof [1992] is used the flux increases to -19.1 gC/m²/yr. Alternatively, the flux calculated by the model using $K_o$ from Wanninkhof and McGillis [1999] is -38.1 gC/m²/yr. In view of this wide range of calculated values, we decided to conduct a series of sensitivity runs with the model to assess the effects of different formulations for $K_o$.

We conducted 7 sensitivity runs:

(1) baseline run with the best parameter set for the biology components (shown in Table 4) and $K_o$ from Wanninkhof [1992];

(2) same run as in (1) except for using $K_o$ from Liss and Merlivat [1986];

(3) same run as in (1) except for doubling $K_o$;

(4) same run as in (1) except for quadrupling $K_o$;

(5) same run as in (4) except for no iron;

(6) same run as in (4) except for removal of biological drawdown of $CO_2$ (abiotic); and,

(7) same run as in (1) except for $K_o$ from Wanninkhof and McGillis [1999].

The results are summarized in Table 7. A comparison between the sensitivity runs for $K$ (runs 1, 2, 3, 4, and 7) reveals that, as $K$ increases, $\Delta pCO_2$ decreases accordingly but $FCO_2$ increases much more slowly. For example, the mean values for $K$, $\Delta pCO_2$, and $FCO_2$ from run 1 are 0.34, -20.4, and -38.1. Conversely, the mean values for $K$, $\Delta pCO_2$, and $FCO_2$ from run 7 are 1.287, -2.3, and -45.6, respectively. Thus, for run 7, $K$ is about 4 times larger, $\Delta pCO_2$ is 9 times smaller, but $FCO_2$ is only 20% larger. This means that there is a dynamic negative feedback in the model that prevents the surface flux from assuming unrealistically large values no matter how large the value of $K$ is. Table 4 also shows that the iron and the biological uptake affect the surface flux significantly. The run without iron limitation (run 5) provides a surface flux 30% larger, whereas the abiotic run (run 6) reverses the flux direction to +15.8 gC/m²/yr. The question that still remains is what formulation for $K$ provides the most realistic $pCO_2$ variability. The relative influence of light and nutrient limitation on the phytoplankton growth simulated by the model is shown in the climatological vertical profiles of light limitation ($L_{lim}$), nitrate and ammonium limitation ($N_{lim}$), and iron limitation ($Fe_{lim}$) of Figure 11. Within the top 50 meters iron is the limiting factor, while below 50 meters, and within the euphotic zone, light is the limiting factor.

Figure 12 shows the seasonal variations of SST, SSS, nitrate, chlorophyll, total carbon dioxide, in situ $pCO_2$, and $pCO_2$ normalized to 10 °C obtained from the model simulation (solid lines) and from observations (black circles and triangles). The chlorophyll data consist of two sources. The Wong and Chan [1991] data for the period of 1973-1978 (triangles), and the National Oceanic Data Center (NOAA/NODC) data set for the period of 1959-1980 (circles). All parameters simulated by the model are in good agreement with observations, except for the $pCO_2$. 

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Table 6. Comparison between model and observed parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Model</th>
<th>Data</th>
</tr>
</thead>
<tbody>
<tr>
<td>PP (gC/m²/yr)</td>
<td>168</td>
<td>140</td>
</tr>
<tr>
<td>Chlorophyll (mg/m³)</td>
<td>0.33</td>
<td>0.41¹</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.32²</td>
</tr>
<tr>
<td>Nitrate (μM)</td>
<td>10.8</td>
<td>10.6</td>
</tr>
<tr>
<td>SST (°C)</td>
<td>7.8</td>
<td>8.2</td>
</tr>
<tr>
<td>SSS (psu)</td>
<td>32.68</td>
<td>32.67</td>
</tr>
<tr>
<td>TCO₂ (mmol/m³)</td>
<td>2016.1</td>
<td>2059.7</td>
</tr>
<tr>
<td>Air pCO₂ (μatm)</td>
<td>320.9</td>
<td>329.8</td>
</tr>
<tr>
<td>Ocean pCO₂ (μatm)</td>
<td>300.5</td>
<td>317.0</td>
</tr>
<tr>
<td>ΔpCO₂ (μatm)</td>
<td>-20.4</td>
<td>-12.8</td>
</tr>
<tr>
<td>K (mmol/m²/μatm/d)</td>
<td>0.340</td>
<td>0.137Ⅲ</td>
</tr>
<tr>
<td>FCO₂ (gC/m²/yr)</td>
<td>-38.1</td>
<td>-8.3Ⅲ</td>
</tr>
<tr>
<td></td>
<td></td>
<td>-19.1</td>
</tr>
</tbody>
</table>

I. From Wong and Chan [1991]
II. From McClain et al. [1996]
III. Calculated quantities based on wind speed, CO₂ solubility, and ΔpCO₂.

Values using K from Liss & Merlivat and Wanninkhof, respectively.

Figure 11. Climatological profiles of light and nutrient limitation predicted by the model.
Table 7. Comparison between 7 different model runs. All values were obtained by averaging the model-data overlapping years (1973-1978), except for the last run (K from Wanninkhof and McGillis, 1999) where 21 years (1960-1980) were used for the averages. The first 2 spin-up years (1958-1959) were eliminated from the averages.

<table>
<thead>
<tr>
<th>Run Type</th>
<th>PP (gC/m²/yr)</th>
<th>Chl-a (mg/m³)</th>
<th>NO₃ (µM)</th>
<th>Ocean pCO₂ (µatm)</th>
<th>TCO₂ (mmol/m²)</th>
<th>ΔpCO₂ (µatm)</th>
<th>K=K_oα (mmol/m² /µatm/d)</th>
<th>FCO₂ (gC/m²/yr)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline1</td>
<td>168</td>
<td>0.33</td>
<td>10.8</td>
<td>300.5</td>
<td>2016.1</td>
<td>-20.4</td>
<td>0.340</td>
<td>-38.1</td>
</tr>
<tr>
<td>Baseline2</td>
<td>168</td>
<td>0.33</td>
<td>10.8</td>
<td>282.3</td>
<td>2005.4</td>
<td>-38.6</td>
<td>0.156</td>
<td>-29.6</td>
</tr>
<tr>
<td>2xK_o</td>
<td>168</td>
<td>0.33</td>
<td>10.8</td>
<td>311.4</td>
<td>2022.5</td>
<td>-9.5</td>
<td>0.679</td>
<td>-42.7</td>
</tr>
<tr>
<td>4xK_o</td>
<td>168</td>
<td>0.33</td>
<td>10.8</td>
<td>317.0</td>
<td>2025.0</td>
<td>-3.9</td>
<td>1.358</td>
<td>-44.4</td>
</tr>
<tr>
<td>No iron</td>
<td>198</td>
<td>0.35</td>
<td>4.6</td>
<td>314.6</td>
<td>2023.8</td>
<td>-6.3</td>
<td>1.358</td>
<td>-57.3</td>
</tr>
<tr>
<td>Abiotic</td>
<td>0</td>
<td>0</td>
<td>38.8</td>
<td>329.7</td>
<td>2028.3</td>
<td>7.7</td>
<td>1.385</td>
<td>15.8</td>
</tr>
<tr>
<td>K_o(W³)</td>
<td>174</td>
<td>0.33</td>
<td>10.8</td>
<td>318.6</td>
<td>2023.1</td>
<td>-2.3</td>
<td>1.287</td>
<td>-45.6</td>
</tr>
</tbody>
</table>
Figure 12. Model (solid line) versus observed (black circles and triangles) seasonal variability of sea surface temperature and salinity, nitrate and chlorophyll averaged over the upper 80 meters, surface total carbon dioxide, $pCO_2$ at in situ temperature, and $pCO_2$ normalized to 10 °C. The gas exchange coefficient of Wanninkhof [1992] was used in this simulation.
The model $pCO_2$ is up to 40 μatm lower in the winter-spring months and about 20 μatm higher in
the summer. A significant improvement is achieved when the McGillis and Wanninkhof [1999] formu-
lation for $K$ is used. Figure 13 shows the improved results. Note that the $pCO_2$ seasonal variability is
now much closer to the observed data. Figure 14 compares the model and observed $pCO_2$ interannual
variability for the period of 1973-1974. Predictions from run 1 (dotted line) and run 7 (solid line) are
shown together with the observed values (solid black circles). It is quite evident that more realistic
amplitude and phase of the seasonal cycle are achieved when the McGillis and Wanninkhof [1999]
formulation for $K$ is used. Therefore we adopted this $K$ formulation for our interannual run. The results
of the interannual run are discussed in the following sections.

5.0 SEASONAL VARIABILITY

Figures 15, 16, and 17 show the seasonal variability (from 1960-1980 monthly averages) of the
physical and biogeochemical model parameters. These are the vertical velocity, vertical eddy diffusivity,
temperature, photosynthetically available radiation (PAR), nitrate, ammonium, zooplankton, phytoplank-
ton, total carbon dioxide, oxygen, and iron. The vertical velocity is very weak in general (maximum of
3 cm/d) with upwelling peaks in the spring and fall when the wind curl is largest. Maximum downwelling
occurs in December. The vertical advection effects are minimal when compared to vertical diffusion
($K_v$). Maximum surface $K_v$ values ranging from 900 to 1000 m$^2$/d occur in late fall and winter. The
depth penetration of large $K_v$ values follows the seasonal changes of the mixed layer depth; largest in
winter (120 m) and smallest in summer (20-40 m). Downwelling light intensity and penetration are
larger during April-August, peaking in May-June. The warmer temperatures are confined to the top 50
meters and the time period of May-October, with a peak in August-September. The seasonal variability
of phytoplankton, nitrate and iron are strongly correlated with top 50-meter peaks extending from May
through October. This is consistent with photosynthetic consumption of nutrients during the high growth
season. Total carbon dioxide and oxygen are strongly correlated with temperature due to the strong
dependence of solubility on temperature.

Oxygen anomalies relative to the temperature-determined saturation value (Figure 18) show that
there is a seasonal cycle of air-sea flux, with ingassing in winter and outgassing in summer. The oxygen
anomaly in the abiotic case is consistently less than in the full coupled model, suggesting that net
community production ($N_p$) is positive at all times of the year. The biologically generated anomalies
contribute very little to the air-sea flux of oxygen. The difference between the biotic and abiotic cases
is greatest in summer, with a maximum of 3.3 μM in July, reflecting the seasonal cycle of $N_p$. This
summer maximum in the NetCP was hypothesized by Wong and Chan [1991] to explain the absence of
a strong seasonal supersaturation of $pCO_2$. The oxygen supersaturation in the summer months is 1.9-
2.8 times the value expected from thermal forcing alone. This is consistent with the oxygen supersat-
urations determined by Emerson et al. [1993], which range from 1.4-2.6 times the values for argon (an
inert tracer of abiotic effects on oxygen), so rates of biological new production in the model are reason-
able and even on the high side.
Figure 13. As in Figure 12, except that the gas exchange coefficient of Wanninkhof and McGillis [1999] was used in this simulation.
Figure 14. Comparison between model and observed $pCO_2$ (in situ and normalized to 10 ºC) for the period of 1973-1978. Results from two model runs are shown: (1) the dotted line shows the model results using the gas exchange formulation of Wanninkhof [1992]; (2) the solid line shows the model results using the gas exchange formulation of Wanninkhof and McGillis [1999]. The solid black circles are the monthly averaged observed values.
Figure 15. Seasonal variability of vertical velocity, vertical eddy diffusivity, temperature, and downwelling irradiance simulated by the model.
Figure 16. Seasonal variability of nitrate, ammonium, zooplankton, and phytoplankton concentrations simulated by the model.
Figure 17. Seasonal variability of temperature, total carbon dioxide, oxygen, and iron concentrations simulated by the model.
6.0 INTERANNUAL VARIABILITY

The interannual variability of the major parameters simulated by the model is illustrated in the profile time series shown in Figures 19 and 20, and in the surface time series shown in Figure 21. The temperature profile shows distinct warm and cold periods. Two warm periods occur on the series, one during 1960-1965 and another during 1976-1980. The period during 1966-1975 exhibits colder (~1 °C) temperatures in the top 150 meters. The oxygen profile series shows higher (~20 mmol/kg) concentrations during the cold period due to increased solubility. The phytoplankton concentration in the upper 20 meters was higher (~0.1 mg/m³) during the warmest temperature events (1961, 1963, and 1979).

![O₂ Anomaly (O₂ - O₂ sat)](image)

**Figure 18. Seasonal variability of surface oxygen anomaly predicted by the model.**
Results from two runs are presented, an abiotic run (dotted line) and a biotic run (solid line).

The secular $pCO₂$ upward trend shown in the top tier of Figure 21 is manifested in the profile series of total carbon dioxide concentration in Figure 19. The carbon dioxide increase of about 20 mmol/m³ in 20 years, caused by the increased surface flux, is noticeable at depths of up to 250 meters. The highest drawdown in the iron, nitrate, and carbon dioxide concentrations occurred during 1961-1963, a period of warmest euphotic zone temperatures during which solubility was lowest and phytoplankton growth was highest. Figure 22 shows the yearly and depth averaged (0-100 m) temperature and $TCO₂$ variability, and the surface $CO₂$ flux and oceanic $pCO₂$ variability for the period of 1960-1980. The interannual changes and trends are highlighted in this figure. Note the cooling trend in the temperature during the 1960s, followed by a warming trend during the mid to late 1970s. The air-sea $CO₂$ flux is always negative, indicating that OWS P is a sink of atmospheric $CO₂$. The $pCO₂$ trends upward almost monotonically showing an increase of about 30 μatm in 20 years. The $TCO₂$ follows the $pCO₂$ trend, showing that the atmosphere and ocean are tightly coupled at OWS P.
Figure 19. Interannual variability of temperature, vertical eddy diffusivity, total carbon dioxide, and oxygen simulated by the model.
Figure 20. Interannual variability of phytoplankton, iron, nitrate, and ammonium simulated by the model.
Figure 21. Time series of simulated atmospheric $pCO_2$, ocean $pCO_2$, SST, mixed layer depth, total carbon dioxide, oxygen, iron, nitrate, and ammonium.
7.0 CARBON FLUX BUDGET

Figure 23 represents the climatological (1960-1980) ecosystem carbon flux balance. The main compartments in this flow chart are the phytoplankton, zooplankton, respired DOC, and total $CO_2$ carbon stocks. The numbers indicate the carbon flux between ecosystem components in gC/m²/yr. The ammonium and nitrate boxes were replaced by the net community production (76 gC/m²/yr), which represents all sources and sinks of macronutrients combined (equation 14). Note that the air-sea (44 gC/m²/yr) and bottom (23 gC/m²/yr) carbon fluxes are balanced by the POC+DOC export (60 gC/m²/yr) and fecal pellet loss (7 gC/m²/yr) through the bottom. The total gross production (uptake) is 174 gC/m²/yr. Therefore, the total carbon required for photosynthesis is partitioned among the following sources: 44% (76 gC/m²/yr) originates from the $TCO_2$ pool - of these 44%, 5% comes from DOC respiration, 13% comes from the bottom flux, and 25% from the atmosphere (air-sea flux). The other 56% (98 gC/m²/yr) of the required equivalent carbon comes from the recycling of zooplankton and phytoplankton losses (death, respiration, and fecal pellet production).

8.0 SUMMARY AND CONCLUSIONS

A coupled ecosystem/carbon flux model was developed, validated, and used to simulate biogeochemical parameters at OWS P. A series of sensitivity runs revealed that the most significant improvement in the simulation of the surface $pCO_2$ is obtained by the use of a recently developed cubic formulation for the gas exchange coefficient (Wanninkhof and McGillis, 1999). This result shows that the ocean and atmosphere are much more closely coupled at high (> 10 m/s) wind speeds than indicated by the previous wind-dependent formulations (Liss and Merlivat, 1986; Tans et al., 1990; Wanninkhof, 1992).

All biogeochemical parameters, when averaged over the period of available concurrent observations (1973-1978), are within less than 5% of the observed values. The only exception is the sea-air $CO_2$ flux which departs more significantly from previously reported values. We attribute this difference to the elusive nature of sea-air $CO_2$ estimates in the ocean and the variety of formulations used in the literature to derive the gas exchange coefficient. For example, our lowest $CO_2$ flux estimate is -29.6 gC/m²/yr when we use the Liss and Merlivat [1986] gas exchange formulation. Wong and Chan [1991], also using the Liss and Merlivat [1986] gas exchange formulation, report a value of -8.4 g C/m²/yr. Our $CO_2$ flux value is even higher (-45.6 gC/m²/yr) when we use the Wanninkhof and McGillis [1999] gas exchange formulation. However, the model estimates for the surface flux and those derived from $\Delta pCO_2$ measurements are not entirely equivalent because the model provides a dynamically coupled flux estimate, whereas the air-sea flux estimates from observed $\Delta pCO_2$ are obtained from a relatively small number of discrete data points. Therefore, global estimates of air-sea $CO_2$ flux derived using air-sea flux models to extrapolate from observed $pCO_2$ may not be realistic. In the short term, fully prognostic models may give the best estimates provided that they achieve sufficient agreement with other observable quantities such as temperature, chlorophyll, and $TCO_2$.  

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Figure 22. Yearly averaged time series of ocean temperature (0-100 m mean), air-sea carbon dioxide flux, surface carbon dioxide partial pressure, and total carbon dioxide concentration temperature (0-100 m mean) simulated by the model for the period of 1960-1980.
Figure 23. Flow chart of simulated climatological carbon flux balance showing the principal carbon exchange compartments in the coupled ecosystem/carbon-flux model.
REFERENCES


Oudot, C., and C. Andrié, Short-term changes in the partial pressure of CO₂ in eastern tropical Atlantic surface seawater and in atmospheric CO₂ mole fraction, *Tellus 41 B*, 537-553, 1989.


**Title:** One-Dimensional Coupled Ecosystem-Carbon Flux Model for the Simulation of Biogeochemical Parameters at Ocean Weather Station P

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**ABSTRACT:**
In this Technical Publication, we describe the model functionality and analyze its application to the seasonal and interannual variations of phytoplankton, nutrients, \( pCO_2 \) and \( CO_2 \) concentrations in the eastern subarctic Pacific at Ocean Weather Station P (OWSP, 50°N 145°W). We use a verified one-dimensional ecosystem model (McClain et al., 1996), coupled with newly incorporated carbon flux and carbon chemistry components, to simulate 22 years (1958-1980) of \( pCO_2 \) and \( CO_2 \) variability at Ocean Weather Station P (OWS P). This relatively long period of simulation verifies and extends the findings of previous studies (Wong and Chan, 1991; Archer et al., 1993; Antoine and Morel, 1995a; Antoine and Morel, 1995b) using an explicit approach for the biological component and realistic coupling with the carbon flux dynamics. The slow currents and the horizontally homogeneous ocean in the subarctic Pacific make OWS P one of the best available candidates for modeling the chemistry of the upper ocean in one dimension. The chlorophyll and ocean currents composite for 1998 shown in Figure 1 illustrates this premise. The chlorophyll concentration map was derived from SeaWiFS data and the currents are from an OGCM simulation (from R. Murtugudde).

**Subject Terms:** ecosystem dynamics, biogeochemistry, carbon flux

**Distribution/Availability Statement:**
Unclassified–Unlimited
Subject Category: 42
Report available from the NASA Center for AeroSpace Information, 7121 Standard Drive, Hanover, MD 21076-1320. (301) 621-0390.