Use of Guided Acoustic Waves to Assess the Effects of Thermal-Mechanical Cycling on Composite Stiffness

Michael D. Seale and Eric I. Madaras
Langley Research Center, Hampton, Virginia

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Acknowledgments

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Abstract

The introduction of new, advanced composite materials into aviation systems requires a thorough understanding of the long-term effects of combined thermal and mechanical loading. As part of a study to evaluate the effects of thermal-mechanical cycling, a guided acoustic (Lamb) wave measurement system was used to measure the bending and out-of-plane stiffness coefficients of composite laminates undergoing thermal-mechanical loading. The system uses a pulse/receive technique that excites an antisymmetric Lamb mode and measures the time-of-flight over a wide frequency range. Given the material density and plate thickness, the bending and out-of-plane shear stiffnesses are calculated from a reconstruction of the velocity dispersion curve. A series of 16 and 32-ply composite laminates were subjected to a thermal-mechanical loading profile in load frames equipped with special environmental chambers. The composite systems studied were a graphite fiber reinforced amorphous thermoplastic polyimide and a graphite fiber reinforced bismaleimide thermoset. The samples were exposed to both high and low temperature extremes as well as high and low strain profiles. The bending and out-of-plane stiffnesses for composite samples that have undergone over 6,000 cycles of thermal-mechanical loading are reported. The Lamb wave generated elastic stiffness results have shown decreases of up to 20% at 4,936 loading cycles for the graphite/thermoplastic samples and up to 64% at 4,706 loading cycles for the graphite/thermoset samples.

Introduction

Advanced composite materials, which are gaining wide use in a variety of structural applications, are required to operate under severe environmental conditions for thousands of hours. In such environments, deterioration with age can cause a significant decrease in the load-carrying capability of these materials, which could compromise safety. Therefore, techniques are required to nondestructively evaluate the integrity of composites which will be subjected to these hostile operating conditions.

Among the various techniques available, guided acoustic waves (Lamb waves) offer a convenient method of evaluating these composite materials. As shown by Karim, et al. and Mal, et al., inversion techniques can be used to ascertain the material parameters of composites from experimental Lamb wave data.

Studies have been conducted which show a reduction in Lamb wave velocity due to a loss of stiffness caused by matrix cracking. Seale, et al. showed a correlation between Lamb wave velocity and stiffness measured with strain gages as well as a correlation between Lamb wave velocity and crack density for mechanically fatigued composite samples. Dayal and Kinra showed that for Lamb wave propagation in the plane of the plate, both wavespeed and attenuation were sensitive to cracking. Tang and Henneke noted that Lamb waves provide information about the in-plane elastic properties of a plate. This type of measurement is more useful due to the fact that composites are commonly designed to carry in-plane loads. Similarly, Dayal, et al. noted that the Lamb wave interaction with cracks is much stronger in the plane of the plate and, thus, provides an effective method to detect damage due to transverse matrix cracking. Recently, Shih, et al. used measurements of the extensional Lamb mode velocity to calculate laminate stiffness constants in mechanically fatigued composites.

Under general thermal-mechanical loading, thermal degradation as well as mechanical fatigue damage may occur. The above studies illustrate the use of Lamb waves to examine mechanical fatigue damage. However, in only a few cases have ultrasonic non-destructive evaluation techniques been used for assessing either thermal degradation or thermal-mechanical cycling in polymer matrix composites. Ultrasonic Lamb waves have been shown by Seale, et al. and Bar-Cohen, et al. to be an effective method for characterizing thermal damage in composites.
In this study, a scanning system was used to measure the Lamb wave velocity over a wide frequency range for composites which were subjected to thermal-mechanical cycling. From the Lamb wave velocity data, the bending and out-of-plane stiffness values were determined for each of the specimens. The following section will describe the composites studied as well as the loading profile to which these samples were subjected. This will be followed by a brief summary of laminated plate theory and the process of reconstructing the velocity dispersion curve to obtain material stiffness values. A description of the Lamb wave scanning system and an evaluation of the accuracy of the measurement technique is then presented. The ensuing section describes the stiffness measurements on the composite samples. Finally, the results for samples which have been undergone up to 6,000 loading cycles are presented and the effectiveness of the Lamb wave technique in measuring thermal-mechanical damage in composites is discussed.

Composite Materials and Thermal-Mechanical Loading Profile

The composite materials studied were a graphite fiber reinforced amorphous thermoplastic polyimide, IM7/K3B, and a graphite fiber reinforced bismaleimide thermoset, IM7/5260. The samples were manufactured with 16 and 32 plies and had stacking sequences of [45/0/-45/90]_{2s} and [45/0/-45/90]_{4s}, respectively. The size of all of the samples was 122-cm by 30.5-cm. The IM7/K3B samples were all constructed with 16 plies and had a nominal thickness of 0.223 cm. The IM7/5260 specimens consisted of both 16 and 32-ply architectures and had nominal thicknesses of 0.248 cm and 0.483 cm, respectively.

Thermal-mechanical cycling of the samples was performed in either 98-kN (22-kip) or 222-kN (50-kip) capacity load frames equipped with environmental chambers which had a usable temperature range of -54 °C to +344 °C. The chamber dimensions were 40-cm wide by 67-cm tall by 40-cm deep. Thus, the upper and lower portions of the samples remained outside of the chambers and only the middle 67-cm section along the length of each of the samples was subjected to thermal extremes. A photo of an environmental chamber is shown in Fig. 1 and an image of a composite sample is shown in Fig. 2.
For all of the samples, the load was applied in the 0° direction (along the length of the specimens). Both high and low strain profiles as well as high and low temperature profiles were used. The low-strain profiles had strain levels which ranged from 0 to 2,000 microstrain with a sustained strain at or above 1,040 microstrain for 180 minutes. The high-strain profiles had strain levels which ranged from 0 to 3,000 microstrain with a sustained strain at or above 1,560 microstrain for 180 minutes. The temperature extremes for the high-temperature cycling were chosen to be -18 °C and +177 °C with a sustained temperature of +177 °C for 180 minutes. The temperature extremes for the low-temperature cycling were chosen to be -18 °C and +135 °C with a sustained temperature of +135 °C for 180 minutes. Each loading cycle lasted for a total of 255 minutes.

The thermal-mechanical loading profile used for this study is shown in Fig. 3. In the figure, the temperature and strain axes have been normalized to the values of temperature and strain which were maintained for a duration of 180 minutes for each cycle. The IM7/K3B samples were subjected to high temperature profiles and both high and low strain profiles. The 16-ply IM7/5260 samples were subjected to low strain levels and high and low temperature profiles. The 32-ply IM7/5260 samples were exposed to low temperature and high strain profiles only. The various profiles for the samples are summarized in Table I.

Table I. Test Matrix for Composite Samples.

<table>
<thead>
<tr>
<th>Loading Profile</th>
<th>IM7/K3B</th>
<th>IM7/5260</th>
</tr>
</thead>
<tbody>
<tr>
<td>Low Strain/Low Temp.</td>
<td>16 Ply</td>
<td>16 Ply</td>
</tr>
<tr>
<td>Low Strain/High Temp.</td>
<td></td>
<td>32 Ply</td>
</tr>
<tr>
<td>High Strain/High Temp.</td>
<td></td>
<td>16 Ply</td>
</tr>
</tbody>
</table>

Laminated Plate Theory

Consider a composite lamina with the 1-axis defined as along the fiber direction, the 2-axis transverse to the fibers, and the 3-axis being out of the plane of the plate. For a lamina assumed to be under plane stress, the stress-strain relationship is given by

\[
\begin{bmatrix}
\sigma_{11} & \sigma_{12} & 0 \\
\sigma_{12} & \sigma_{22} & 0 \\
0 & 0 & 0
\end{bmatrix}
\begin{bmatrix}
\varepsilon_1 \\
\varepsilon_2 \\
\gamma_{23}
\end{bmatrix}
\begin{bmatrix}
Q_{11} & Q_{12} & 0 & 0 & 0 \\
Q_{12} & Q_{22} & 0 & 0 & 0 \\
0 & 0 & Q_{44} & 0 & 0 \\
0 & 0 & 0 & Q_{55} & 0 \\
0 & 0 & 0 & 0 & Q_{66}
\end{bmatrix}
\begin{bmatrix}
\varepsilon_1 \\
\varepsilon_2 \\
\gamma_{23}
\end{bmatrix}
\]

(1)

where \(\sigma\) and \(\tau\) represent the stresses and \(\varepsilon\) and \(\gamma\) represent the strains. The \(Q_{ij}\) are the plane-stress stiffness components for \(i, j = 1, 2, 6\) and the shear stiffness components for \(i, j = 4, 5\).

Composite laminates often consist of individual lamina with the fibers oriented at various angles with respect to the structural axes (see Fig. 4). The angle \(\theta\) is defined as positive for a counterclockwise rotation from the laminate (x-y) axes to the individual lamina (1-2) axes. The bending stiffnesses, \(D_{ij}\), and the out-of-plane stiffnesses, \(A_{ij}\), for the entire laminate are obtained by integrating the \(Q_{ij}\) through the thickness of the plate. These stiffness values are defined as

\[
D_{ij} = \int_{-h/2}^{h/2} (Q_{ij'})z^2 dz \\
A_{ij} = \int_{-h/2}^{h/2} (Q_{ij'})dz 
\]

(2)
Figure 4. Rotation of coordinate system from the lamina (1-2) axes to the laminate (x-y) axes.

and

\[ A_{jj} = \frac{h}{2} \int \left( Q_{jj}' \right)_k dz \quad j = 4, 5 \]

where \( h \) is the total thickness of the plate, the subscript \( k \) represents each layer in the laminate, and \( k_j \) is a shear correction factor. The \( Q_{ij}' \) represent the transformed stiffness coefficients rotated according to the orientation of each ply with respect to the structural axes.

**Lamb Waves and Plate Theory Approximations**

Lamb waves arise from a coupling between the shear-vertical (SV) and compressional (P) waves reflected at the stress-free boundaries at the top and bottom of a thin plate. The Lamb mode solutions are grouped into two classes which are defined in terms of the symmetry of the displacements of the plate with respect to the mid-plane. The modes are labeled as symmetric, \( S_n \), and antisymmetric, \( A_n \). For reference, the Lamb wave dispersion curves for the first three symmetric and antisymmetric modes in the composite samples used in this study are shown in Fig. 5. The dispersion curves shown in the figure were generated using a through-the-thickness finite element model, detailed in Dong and Huang\(^{11}\) and Datta, et al.\(^{12}\) As can be seen from the figure, higher order symmetric and antisymmetric modes begin to propagate as the frequency increases. However, at frequencies below 500 kHz, only the lowest order symmetric mode, \( S_0 \), and lowest order antisymmetric mode, \( A_0 \), propagate.

In this region, the \( S_0 \), or extensional plate mode, is almost nondispersive and the \( A_0 \), or flexural plate mode, is highly dispersive. Since this study uses velocity measurements for the flexural mode, only those solutions will be treated here.

![Dispersion curves](image)

**Flexural mode equations**

For a symmetric quasi-isotropic plate, the dispersion relation for the flexural plate mode propagating in the 0° direction (along the structural x-axis) is given by\(^{10}\)

\[
\begin{align*}
((D_{11}k^2 + A_{55} - I\omega^2)(D_{66}k^2 + A_{44} - I\omega^2)) \\
(A_{55}k^2 - \rho^*\omega^2) - (D_{16}k^2)(A_{55}k^2 - \rho^*\omega^2) \\
- (A_{55}k^2)(D_{66}k^2 + A_{44} - I\omega^2) = 0
\end{align*}
\]

(4)

For waves propagating in the 90° direction of a symmetric quasi-isotropic plate, the relation is\(^{10}\)

\[
\begin{align*}
((D_{22}k^2 + A_{44} - I\omega^2)(D_{66}k^2 + A_{55} - I\omega^2)) \\
(A_{44}k^2 - \rho^*\omega^2) - (D_{16}k^2)(A_{44}k^2 - \rho^*\omega^2) \\
- (A_{44}k^2)(D_{66}k^2 + A_{55} - I\omega^2) = 0
\end{align*}
\]

(5)

In the equations, \( \omega \) is the angular frequency and \( k \) is the wavenumber. \( I \) and \( \rho^* \) are defined as\(^{13}\)
\[ I = \int_0^h \rho dz \] (6)

and

\[ \rho^* = \int_0^h \rho z^2 dz \] (7)

where \( \rho \) is the density and \( h \) is the plate thickness. Multiple roots exist for the dispersion relations given by Eqs. (4) and (5). However, as evidenced by Fig. 5, only those which satisfy the condition that the velocity approaches zero as the frequency approaches zero are the ones corresponding to the \( A_0 \) mode. If the density, thickness, and stiffnesses are known, the dispersion curve can be obtained by selecting wavenumbers, \( k \), and solving Eqs. (4) and (5) for the corresponding angular frequencies, \( \omega \). Once \( \omega \) and \( k \) are known, the phase velocity, \( v \), is given by

\[ v = \frac{\omega}{k} \] (8)

and the frequency, \( f \), is obtained from the angular frequency by using the relation

\[ f = \frac{\omega}{2\pi}. \] (9)

The dispersion curve is then generated by plotting the velocity as a function of frequency. For a further description of plate theory and how the laminate stiffnesses relate to the flexural wave velocity, the reader is referred to Tang, et al.\textsuperscript{10}

Effects of Stiffness on Velocity

For propagation in the 0° direction, the effects of altering \( A_{55} \) and \( D_{11} \) on the flexural dispersion relation given by Eq. (4) are shown in Fig. 6. Decreasing the values of \( D_{16}, D_{66} \), and \( A_{44} \) by 25% did not significantly alter the dispersion curve for Lamb wave propagation in the 0° direction and were omitted from the figure for clarity. The effects of altering these three parameters are shown in Fig. 7. In Fig. 6, it can be seen that decreasing \( A_{55} \) by 25% alters the curve by a significant amount while a smaller shift in the curve is seen when \( D_{11} \) is reduced by 25%.

![Figure 6. Flexural dispersion curves using full values of \( D_{11}, D_{16}, D_{66}, A_{44}, \) and \( A_{55} \), with \( D_{11} \) reduced by 25%, and with \( A_{55} \) reduced by 25%. The curves with reduced values of \( D_{16}, D_{66}, \) and \( A_{44} \) are not discernible from the curve constructed using the full stiffness values.](image)

Shown in Fig. 7 is a plot of the percent change in velocity as a function of frequency for 25% reductions in each stiffness value. The figure clearly shows that the only constants which change the velocity by more than 0.5% are \( D_{11} \) and \( A_{55} \). Also, changing \( D_{11} \) has a greater effect on the velocity at lower frequencies while changes in \( A_{55} \) alter the dispersion curve at higher frequencies. The dispersion curve for propagation in the 90° direction (along the structural y-axis) given by Eq. (5) has the same trends as seen in Fig. 6, except the constants controlling the behavior are \( D_{22} \) and \( A_{44} \). The values of \( D_{16}, D_{66}, \) and \( A_{55} \) do not significantly affect the dispersion curve for Lamb waves propagating in the 90° direction. As with propagation in the 0° direction, these values will be held constant and the values of \( D_{22} \) and \( A_{44} \) will be used to fit the experimental data.

**Lamb Wave Scanning System**

The system used in this study, Lamb Wave Imager\textsuperscript{TM} (LWI), is a commercial ultrasonic scanner developed by Digital Wave Corporation (DWC) in...
Figure 7. Plot of the percent reduction in velocity as a function of frequency for a 25% decrease in each stiffness constant.

Englewood, Colorado. It is capable of measuring the elastic properties for isotropic as well as anisotropic materials. The system consists of a scanner, scanner control unit, a pair of transducers, and a computer. The scanning control and data analysis is performed by a commercial software package developed by DWC. A schematic of the system is shown in Fig. 8.

The scanner control unit incorporates a receiver, a high-voltage amplifier, and a motor controller. The receiver has an amplification range from 0 to 66 dB. The high-voltage amplifier is used to amplify the pulse used to drive the sending transducer. It has a bandwidth of 12 kHz to 1 MHz and a maximum output of 350 volts peak-to-peak. The motor controller is capable of independently controlling the motion of each of the scanner motors. The computer contains a function generator card that produces a sinusoidal pulse and an 8-bit A/D board that digitizes the received signals.

The scanner consists of a scan frame, a scan bridge, and a scan head. An image of the scanner is shown in Fig. 9. The scan frame dimensions are 50.8-cm wide by 61.0-cm long by 10.2-cm tall. These dimensions were chosen to enable the scanner to fit inside the environmental chambers where durability testing was being performed. The scan frame incorporates guide rods, a motor, and drive screw to control the motion along the y-axis. The scan bridge uses guides, a motor, and drive screw to govern the motion along the x-axis. The scan head is comprised of the ultrasonic transducers as well as a z-axis motor and a delta-x motor. The z-axis motor is used to raise and lower the transducers. Coupling between the article under test and the transducers is achieved through a thin rubber face plate which is attached to the bottom of the transducers. Bicycle tire patch material proved to be a convenient source for the rubber face plate and provided a good coupling between the test specimen and the transducers. The delta-x motor regulates the spacing between the stationary sending transducer and the movable receiving transducer.

For a scan, the two transducers are used in a pulse/receive arrangement to determine the velocity of the flexural plate mode over a wide frequency range. The
receiving sensor is moved in small increments by the delta-x motor in order to assure that the same peak in the waveform is followed over the total separation distance. A schematic of the measurement locations is displayed in Fig. 10. Fig. 11 shows sample signals corresponding to the different receiving transducer positions for a 100 kHz, 4-cycle Gaussian-enveloped sine wave input signal. The signal was received at five different locations separated by 0.5-cm increments. The dashed line on the signals indicates the peak which is followed for the time-of-flight measurements.

Once the time of arrival from each peak is measured, the velocity at each frequency is calculated from the known transducer separation and the measured time-of-flight. After the velocity as a function of frequency is measured, the bending and out-of-plane shear stiffnesses are obtained from a reconstruction of the flexural mode dispersion curve. The velocity measurements have been shown by Huang, et al.\textsuperscript{14} to be accurate and repeatable to within 1% resulting in reconstructed stiffness values repeatable to within 4%.

The x and y-axis motors are used to move the scan head over the surface to map the time-of-flight, velocity, and stiffness of the entire specimen. Access to only one side of the material is required and no couplants are required because the sensors are dry coupled to the surface of the plate.

**Scanner Accuracy Evaluation**

To evaluate the accuracy of the stiffness measurements obtained from Lamb wave velocity measurements, the elastic stiffness was measured in 25 different regions on a large rolled aluminum plate. The plate had dimensions of 50.8 cm by 38.1 cm and a thickness of 0.32 cm. The scan area was 12.0 cm by 12.0 cm with a step size of 3.0 cm and the starting point was 15.0 cm away from the two closest edges of the plate. For the velocity measurement at each location, the sensor separation was varied from 2.75 cm to 4.75 cm in increments of 0.5 cm. An 8-cycle Gaussian-enveloped sine wave was used to generate the signal and the sampling rate was chosen to be 25 MHz. The frequency was swept from 30 to 150 kHz in 10-kHz steps and the velocity at each frequency was measured. Since the material is isotropic, only two independent elastic constants exist. From the data, the dispersion curve was reconstructed and values for the longitudinal and shear modulus which best fit the experimental data were obtained.

For the case of a single isotropic lamina, the stiffness values in Eqs. (4) and (5) take the form\textsuperscript{15}

\[
A_{44} = A_{55} = 2Gh \\
D_{11} = D_{22} = \frac{G^2h^3}{3(4G - E)} \\
D_{16} = 0 \\
D_{66} = \frac{Gh^3}{6}
\] (10)

where $G$ is the shear modulus, $E$ is the longitudinal modulus, and $h$ is the thickness. Longitudinal and shear modulus values of 67.7 GPa and 25.0 GPa,\textsuperscript{16} respectively, were used in the plate theory model to predict a dispersion curve for comparison to the experimental data and the reconstructed dispersion curve.
Shown in Fig. 12 is a plot of the average experimental velocity at each frequency, the reconstructed dispersion curve, and the dispersion curve predicted by the plate theory model. As can be seen from the figure, the agreement between the predicted dispersion curve and the reconstructed dispersion curve is excellent. The standard deviations in the velocity at each frequency for the 25 measurement locations were all within 1% of the average with most values being within 0.5% from the average. This small deviation produces error bars on the order of the size of the symbols in the figure. The average reconstructed stiffnesses and the standard deviations for the 25 measurement locations were 66.4 ± 2.0 GPa for the longitudinal modulus and 23.3 ± 1.3 GPa for the shear modulus.

**Stiffness Measurements in Composites**

The Lamb Wave Imager™ was used to measure the stiffness of thermal-mechanically loaded composites at various cycling levels. An 8-cycle Gaussian-enveloped sine wave was used to generate the signal and the received signal was sampled at 25 MHz. The receiving sensor was moved in increments of 0.4 cm for a total distance of 2.0 cm. The frequency was swept in 10-kHz steps from 30 kHz to 200 kHz and the velocity at each frequency was obtained. Due to the large size and the irregular shape of the samples, the density was estimated from common values for polymer matrix composites and taken to be a constant value of 1560 kg/m³.

The elastic bending stiffness and out-of-plane shear stiffness of the material were computed from a reconstruction of the flexural plate mode dispersion curve. Since the only constants significantly affecting the curve are \( D_{11} \) and \( A_{55} \) (see Fig. 7), the curve fitting to the experimental data will only use these two parameters. The values of \( D_{16}, D_{66}, \) and \( A_{44} \) will be set at values obtained from Eqs. (2) and (3). For propagation in the 0° direction, the \( D_{11} \) and \( A_{55} \) stiffnesses in Eq. (4) were estimated by varying their values to produce the best fit to the experimentally obtained values of \( \omega \) and \( k \). The stiffnesses \( D_{22} \) and \( A_{44} \) in Eq. (5) were estimated in a similar manner from data obtained from velocity measurements in the 90° direction.

**Sample Reconstruction**

Shown in Fig. 13 is the average of ten experimental velocity measurements in the 0° direction for a baseline IM7/5260 sample and one with 2,353 loading cycles at low strain levels and high temperature extremes. Also shown are the reconstructed dispersion curves. The velocity error bars are on the order of the size of the symbols and, therefore, have been omitted from the figure. In the figure, the dispersion curve for the cycled sample is clearly shifted from that of the baseline sample. For the curves shown, the estimated value of \( A_{55} \) decreased by 34% and the estimated value of \( D_{11} \) increased by 2% for the cycled sample as compared to the baseline sample.

**Stiffness Mapping**

Stiffness mappings for samples with a variety of loading profiles and times were made in the environmental chambers as well as with the specimens removed from the chambers. With the samples out of the chambers, the entire specimen could be accessed and a stiffness mapping of 75 different regions could be obtained. However, due to the constraints of the chambers, only 20 stiffness measurements in the middle of the specimens could be made for the in situ measurements. Measurements were made both along the length of the samples as well as across the width of the samples to acquire a mapping of \( A_{55} \) and \( D_{11} \) as well as \( A_{44} \) and \( D_{22} \), respectively.
Results

Mapping Results

Sample results of stiffness mappings of $A_{55}$ are shown for the IM7/K3B and the IM7/5260 composites in Fig. 14 and Fig. 15, respectively. In these figures, the stiffnesses have been normalized to the average stiffness measured for the baseline sample in each set. The higher stiffness values in the regions at the bottom of the cycled specimens were due to that portion of the sample being out of the environmental chambers and, therefore, not subjected to the same thermal extremes as the rest of the sample. The average normalized stiffness, $A_{55}$, and standard deviation for all of the samples measured are compiled in Tables II-V. Also shown in the tables are the normalized values of $D_{11}$ measured for each sample.

Table II. Normalized 0° stiffness measurement results for the IM7/K3B low-strain/high-temperature profile samples.

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Normalized $D_{11}$</th>
<th>Normalized $A_{55}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00 ± 0.11</td>
<td>1.00 ± 0.02</td>
</tr>
<tr>
<td>1,092</td>
<td>1.01 ± 0.22</td>
<td>0.91 ± 0.06</td>
</tr>
<tr>
<td>2,339</td>
<td>0.97 ± 0.06</td>
<td>0.90 ± 0.02</td>
</tr>
<tr>
<td>2,353</td>
<td>0.90 ± 0.08</td>
<td>0.92 ± 0.02</td>
</tr>
<tr>
<td>4,420</td>
<td>0.98 ± 0.11</td>
<td>0.88 ± 0.03</td>
</tr>
</tbody>
</table>

Table III. Normalized 0° stiffness measurement results for the IM7/K3B high-strain/high-temperature profile samples.

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Normalized $D_{11}$</th>
<th>Normalized $A_{55}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00 ± 0.11</td>
<td>1.00 ± 0.02</td>
</tr>
<tr>
<td>1,086</td>
<td>0.96 ± 0.12</td>
<td>0.91 ± 0.04</td>
</tr>
<tr>
<td>1,143</td>
<td>0.98 ± 0.09</td>
<td>0.90 ± 0.04</td>
</tr>
<tr>
<td>2,353</td>
<td>1.00 ± 0.15</td>
<td>0.91 ± 0.02</td>
</tr>
<tr>
<td>4,936</td>
<td>0.93 ± 0.16</td>
<td>0.80 ± 0.05</td>
</tr>
<tr>
<td>4,993</td>
<td>0.88 ± 0.08</td>
<td>0.83 ± 0.05</td>
</tr>
</tbody>
</table>

Figure 13. Experimental dispersion curves for a baseline IM7/5260 sample and one with 2,353 loading cycles at a low strain/high temperature profile. Also shown are the reconstructed dispersion curves for the baseline (solid line) and cycled (dashed line) samples.

Figure 14. Stiffness mappings of $A_{55}$ for cycled IM7/K3B samples.

Figure 15. Stiffness mappings of $A_{55}$ for cycled IM7/5260 samples.
Table IV. Normalized 0° stiffness measurement results for the IM7/5260 low-strain/high-temperature profile samples.

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Normalized D_{11}</th>
<th>Normalized A_{55}</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00 ± 0.09</td>
<td>1.00 ± 0.01</td>
</tr>
<tr>
<td>2,353</td>
<td>1.01 ± 0.14</td>
<td>0.67 ± 0.04</td>
</tr>
<tr>
<td>4,706</td>
<td>0.90 ± 0.28</td>
<td>0.36 ± 0.03</td>
</tr>
</tbody>
</table>

Table V. Normalized 0° stiffness measurement results for the IM7/5260 low-strain/low-temperature profile samples.

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Normalized D_{11}</th>
<th>Normalized A_{55}</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00 ± 0.09</td>
<td>1.00 ± 0.01</td>
</tr>
<tr>
<td>1,809</td>
<td>0.92 ± 0.17</td>
<td>0.97 ± 0.09</td>
</tr>
<tr>
<td>2,353</td>
<td>0.85 ± 0.11</td>
<td>0.99 ± 0.04</td>
</tr>
<tr>
<td>5,637</td>
<td>0.93 ± 0.18</td>
<td>0.96 ± 0.08</td>
</tr>
</tbody>
</table>

Table VI. Normalized 0° stiffness measurement results for the IM7/5260 high-strain/low-temperature profile samples.

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Normalized D_{11}</th>
<th>Normalized A_{55}</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00 ± 0.08</td>
<td>1.00 ± 0.01</td>
</tr>
<tr>
<td>1,759</td>
<td>1.01 ± 0.10</td>
<td>1.01 ± 0.03</td>
</tr>
<tr>
<td>2,353</td>
<td>0.96 ± 0.23</td>
<td>0.99 ± 0.07</td>
</tr>
<tr>
<td>6,001</td>
<td>1.03 ± 0.24</td>
<td>0.94 ± 0.08</td>
</tr>
</tbody>
</table>

Stiffness results were also obtained for values of $A_{44}$ from measurements in the 90° direction. Sample results of the $A_{44}$ scans for the same samples shown in Figs. 14 and 15 are shown in Figs. 16 and 17, respectively. As with the $A_{55}$ measurements, the stiffnesses have been normalized to the average stiffness obtained for the baseline specimen in each sample set. The average normalized stiffnesses $A_{44}$ and $D_{22}$ as well as standard deviations for the samples are shown in Tables VII-XI.

Table VII. Normalized 90° stiffness measurement results for the IM7/K3B low-strain/high-temperature profile samples.

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Normalized D_{22}</th>
<th>Normalized A_{44}</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00 ± 0.10</td>
<td>1.00 ± 0.02</td>
</tr>
<tr>
<td>1,086</td>
<td>0.81 ± 0.06</td>
<td>0.87 ± 0.04</td>
</tr>
<tr>
<td>1,143</td>
<td>0.92 ± 0.15</td>
<td>0.88 ± 0.05</td>
</tr>
<tr>
<td>2,353</td>
<td>0.94 ± 0.11</td>
<td>0.92 ± 0.02</td>
</tr>
<tr>
<td>4,936</td>
<td>0.81 ± 0.06</td>
<td>0.85 ± 0.03</td>
</tr>
<tr>
<td>4,993</td>
<td>0.91 ± 0.11</td>
<td>0.87 ± 0.06</td>
</tr>
</tbody>
</table>

Figure 16. Stiffness mappings of $A_{44}$ for cycled IM7/K3B samples.

Figure 17. Stiffness mappings of $A_{44}$ for cycled IM7/5260 samples.

Table VIII. Normalized 90° stiffness measurement results for the IM7/K3B high-strain/high-temperature profile samples.

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Normalized D_{22}</th>
<th>Normalized A_{44}</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00 ± 0.10</td>
<td>1.00 ± 0.02</td>
</tr>
<tr>
<td>1,086</td>
<td>0.81 ± 0.06</td>
<td>0.87 ± 0.04</td>
</tr>
<tr>
<td>1,143</td>
<td>0.92 ± 0.15</td>
<td>0.88 ± 0.05</td>
</tr>
<tr>
<td>2,353</td>
<td>0.94 ± 0.11</td>
<td>0.92 ± 0.02</td>
</tr>
<tr>
<td>4,936</td>
<td>0.81 ± 0.06</td>
<td>0.85 ± 0.03</td>
</tr>
<tr>
<td>4,993</td>
<td>0.91 ± 0.11</td>
<td>0.87 ± 0.06</td>
</tr>
</tbody>
</table>
Table IX. Normalized 90° stiffness measurement results for the IM7/5260 low-strain/high-temperature profile samples.

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Normalized $D_{22}$</th>
<th>Normalized $A_{44}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00 ± 0.06</td>
<td>1.00 ± 0.02</td>
</tr>
<tr>
<td>2,353</td>
<td>0.86 ± 0.09</td>
<td>0.73 ± 0.05</td>
</tr>
<tr>
<td>4,706</td>
<td>0.77 ± 0.16</td>
<td>0.43 ± 0.03</td>
</tr>
</tbody>
</table>

Table X. Normalized 90° stiffness measurement results for the IM7/5260 low-strain/low-temperature profile samples.

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Normalized $D_{22}$</th>
<th>Normalized $A_{44}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00 ± 0.06</td>
<td>1.00 ± 0.02</td>
</tr>
<tr>
<td>1,809</td>
<td>0.98 ± 0.22</td>
<td>1.01 ± 0.10</td>
</tr>
<tr>
<td>2,353</td>
<td>1.01 ± 0.21</td>
<td>0.99 ± 0.06</td>
</tr>
<tr>
<td>5,637</td>
<td>0.83 ± 0.15</td>
<td>0.96 ± 0.08</td>
</tr>
</tbody>
</table>

Table XI. Normalized 90° stiffness measurement results for the IM7/5260 high-strain/low-temperature profile samples.

<table>
<thead>
<tr>
<th>Cycles</th>
<th>Normalized $D_{22}$</th>
<th>Normalized $A_{44}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00 ± 0.06</td>
<td>1.00 ± 0.01</td>
</tr>
<tr>
<td>1,759</td>
<td>1.03 ± 0.32</td>
<td>1.01 ± 0.12</td>
</tr>
<tr>
<td>2,353</td>
<td>1.04 ± 0.29</td>
<td>1.00 ± 0.08</td>
</tr>
<tr>
<td>6,001</td>
<td>0.90 ± 0.18</td>
<td>0.90 ± 0.08</td>
</tr>
</tbody>
</table>

**IM7/K3B Samples**

Shown in Fig. 18 are the normalized values of $A_{55}$ as a function of loading cycles for the IM7/K3B samples which were loaded at high temperatures for both low and high strain levels. The results of $A_{44}$ for the same specimens showed a similar trend. A significant decrease was observed in the out-of-plane stiffness with extended cycling. Additionally, it was observed that the stiffness for the high-strain profile showed a greater decrease than the stiffness for the low-strain profile at levels approaching 5,000 cycles. At this level, the stiffness for the high-strain samples decreased by 20% and the stiffness for the low-strain samples decreased by over 10%.

Plotted in Fig. 19 as a function of loading cycles are the normalized stiffnesses $A_{44}$ and $A_{55}$ for the IM7/K3B specimens loaded at high temperatures and low strain levels. The stiffnesses for the high-strain profiles showed a similar trend. In the figure, the values of $A_{55}$ showed a greater decrease than the values of $A_{44}$.

**IM7/5260 Samples**

As the tabulated results indicate, there was only about a 5% decrease in the average out-of-plane stiffnesses, $A_{44}$ and $A_{55}$, for the IM7/5260 samples cycled at low temperature levels. In contrast to the IM7/K3B samples, no discernible difference between high and low strain levels was observed in the out-of-plane stiffness values. Also, there were no appreciable differences between the values of $A_{44}$ and $A_{55}$. One thing of interest to note, however, are the much larger standard deviations in the cycled samples as compared to the baseline samples.
For two IM7/5260 samples, a temperature in excess of the recommended maximum operating temperature (135 °C) was used to accelerate the thermal-mechanical cycling process. The results for the normalized values of $A_{55}$ for specimens loaded at low strain levels for high and low temperature profiles are shown in Fig. 20. The results of the stiffness $A_{44}$ were similar. In Fig. 20, linear fits to the respective data were made in order to display the difference in trends between the samples. The difference in stiffness loss for the samples loaded at high temperatures as compared to the ones loaded at low temperatures was dramatic. Thus, the IM7/5260 specimens did not perform well when subjected to excessive temperatures.

**Comparison of IM7/K3B and IM7/5250 Samples**

A final comparison is made between IM7/5260 and IM7/K3B specimens loaded at identical strain and temperature profiles. Shown in Fig. 21 are the normalized values of $A_{55}$ for samples loaded at low strain levels and a high temperature profile. The results for $A_{44}$ were similar. As can be seen from the figure, the IM7/K3B samples performed much better under higher temperature conditions than the IM7/5260 samples. This is consistent with the fact that the maximum recommended operating temperature of IM7/K3B (177 °C) is greater than the maximum recommended operating temperature of IM7/5260 (135 °C).

**Discussion**

In general, the out-of-plane shear carrying capabilities of the composite are matrix dominated, which can be seen from the definition of $A_{44}$ and $A_{55}$ in Eq. (3). It is expected, and previous measurements show, that matrix cracking due to mechanical fatigue damage in composites leads to a decrease in elastic moduli. Shown in Fig. 22 is a photomicrograph of the free edge of an IM7/5260 sample which was subjected to high mechanical strains and low temperature levels. The figure clearly shows extensive matrix cracking occurring in the +45 and 90 degree plies. Photomicrographs taken of the thermal-mechanically loaded IM7/K3B samples also exhibited matrix cracks.

**IM7/K3B Samples**

Due to matrix cracking, the decrease in the out-of-plane stiffness for the IM7/K3B materials demonstrated in Figs. 14, 16, 18, and 19 was as expected. In addition, if the amount of matrix cracking is related to the strain levels, lower values of $A_{44}$ and $A_{55}$ should be observed in the low-strain samples when compared to the high-strain samples. This was the approximate relationship seen in Fig. 18. Ultrasonic attenuation measurements in these samples have produced similar results suggesting matrix cracking was more prevalent in the high-strain versus low-strain samples.
For the IM7/K3B results shown in Fig. 19, the values of $A_{44}$ did not show as large of a decrease in stiffness with loading cycles as the values of $A_{55}$. Loading in the $0^\circ$ direction would tend to produce matrix cracks in the $90^\circ$ plies as well as the $\pm 45^\circ$ plies, but not in the $0^\circ$ plies. Considering that the Lamb wave interaction with cracking is stronger for propagation perpendicular to the crack direction, it is expected that $A_{55}$ will be sensitive to matrix cracking in the $90^\circ$ and $\pm 45^\circ$ plies and that $A_{44}$ will be sensitive to cracks in the $0^\circ$ and $\pm 45^\circ$ plies. Since $0^\circ$ ply cracks are not expected to an extensive degree in this loading configuration, only the $\pm 45^\circ$ ply cracks would adversely affect the value of $A_{44}$. Therefore, this should lead to a less significant decrease in stiffness for $A_{44}$ than $A_{55}$, which is consistent with observation in the IM7/K3B samples.

The tabulated values for the IM7/K3B samples indicate an increase in standard deviation for $A_{44}$ and $A_{55}$ in the cycled samples as compared to the baseline samples. The larger standard deviation in the cycled samples was most likely due to localized damaged regions in the specimens due to the loading process. Reports on ultrasonic attenuation measurements in these samples indicated that initially, the damage was localized and, as the number of loading cycles increased, the damage became more homogeneous throughout the sample.\textsuperscript{19}

**IM7/5260 Samples**

As was seen in Tables IV-VI as well as Tables IX-XI, the standard deviations of the measurements increased substantially during the early stages of cycling for the IM7/5260 samples. The measured values of $A_{55}$ and $A_{44}$ were higher at some locations and lower at others. The higher stiffness values observed might be attributable to additional curing that could occur during the thermal cycling.\textsuperscript{20} Additional curing would tend to increase the stiffness of the matrix and thus, increase the out-of-plane stiffness. Countering this effect would be the development of matrix cracks which would tend to lower the stiffness. The juxtaposition of the two processes would lead to little loss in the mean out-of-plane stiffness values at the earlier numbers of cycles, yet would lead to an increase in the variability of the values. Once the curing has reached its maximum possible state and the matrix crack density increases, the matrix damage would dominate and the IM7/5260 specimens should show a general loss in out-of-plane stiffness.

**Bending Stiffness**

In the tables, the values of $D_{11}$ and $D_{22}$ for both the IM7/K3B and the IM7/5260 samples were reported. Physically, the bending stiffness is controlled by the fibers if the plate bending occurs in the fiber direction and by the matrix if the bending direction of the plate is perpendicular to the fibers. Due to the fact that a quasi-isotropic architecture was used for these samples, the bending stiffness will be affected by both the fiber and the matrix. Since fiber damage was probably not occurring in these samples, the values of $D_{11}$ and $D_{22}$ would predominately reflect the intact fiber load carrying capability and would only be influenced by matrix cracking to a minor degree. Therefore, in general, a very small decrease in the bending stiffness values due to the matrix cracking might be expected.

What is most notable in the tabulated values of $D_{11}$ and $D_{22}$ are that the standard deviations in the bending stiffnesses were 2 to 9 times greater than the standard deviations in the out-of-plane shear stiffnesses. The large standard deviations in the measure-
ments represent the insensitivity of the dispersion curve to changes in bending stiffness over the measurement frequency range (30 kHz to 200 kHz). In this region, the parameter dominating the behavior of the curve will be the out-of-plane stiffness (see Fig. 7). Only a few data points exist at the very low frequencies (below 50 kHz) where the bending stiffness controls the behavior of the curve. Due to this lack of data, the constants $D_{11}$ and $D_{22}$ will not be as accurate as the constants $A_{55}$ and $A_{44}$. Although the tables show a small increase in some of the values of $D_{11}$ and $D_{22}$ instead of the expected small decrease, the large standard deviations associated with the measurement cover up any true significance.

Conclusions

Lamb wave imaging is a method for nondestructively measuring the elastic properties of a material. The scanner requires access to only one side of a specimen with no immersion or couplants. It has been shown by this study to be an effective method in providing a quantitative measure of stiffness changes due to thermal-mechanical loading in composite materials. The IM7/K3B samples which were loaded at high temperatures and high strain levels showed a 20% decrease in stiffness after 4,936 cycles. The IM7/5260 samples loaded at low temperatures for both high and low strain levels showed less than a 10% decrease in stiffness after 6,001 cycles. However, the IM7/5260 samples which were subjected to excessively high temperatures and low strain levels showed a decrease in stiffness of over 60% after 4,706 cycles. The bending stiffnesses showed few effects of thermal-mechanical loading due to their insensitivity to matrix cracking as well as the large standard deviations arising from the frequency range used for the measurements. All of the samples showed an increase in stiffness variation for the thermal-mechanically cycled specimens.

References


18. Private communication, Karen Whitley of NASA Langley Research Center and Steven Grossen Lockheed Martin.


The introduction of new, advanced composite materials into aviation systems requires a thorough understanding of the long-term effects of combined thermal and mechanical loading. As part of a study to evaluate the effects of thermal-mechanical cycling, a guided acoustic (Lamb) wave measurement system was used to measure the bending and out-of-plane stiffness coefficients of composite laminates undergoing thermal-mechanical loading. The system uses a pulse/receive technique that excites an antisymmetric Lamb mode and measures the time-of-flight over a wide frequency range. Given the material density and plate thickness, the bending and out-of-plane shear stiffnesses are calculated from a reconstruction of the velocity dispersion curve. A series of 16 and 32-ply composite laminates were subjected to a thermal-mechanical loading profile in load frames equipped with special environmental chambers. The composite systems studied were a graphite fiber reinforced amorphous thermoplastic polyimide and a graphite fiber reinforced bismaleimide thermoset. The samples were exposed to both high and low temperature extremes as well as high and low strain profiles. The bending and out-of-plane stiffnesses for composite samples that have undergone over 6,000 cycles of thermal-mechanical loading are reported. The Lamb wave generated elastic stiffness results have shown decreases of up to 20% at 4,936 loading cycles for the graphite/thermoplastic samples and up to 64% at 4,706 loading cycles for the graphite/thermoset samples.