DOPPLER AND REFLECTIVITY MEASUREMENTS AT TWO CLOSELY-SPACED FREQUENCIES

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1. INTRODUCTION

Spaceborne and airborne radars are limited with respect to the mass and size of the instrument and the power available to operate it. As a consequence, dual-wavelength radars that require separate antennas and power amplifiers are expensive and often impractical. However, if the frequency difference can be reduced so that a single antenna and the same radio-frequency subsystem can be used for both frequencies, dual-wavelength Doppler measurements can be made with a radar of about the same size and mass as its single-frequency counterpart.

In the first part of the paper we present calculations of the reflectivity factor differences as functions of the center frequency from 10 to 35 GHz and for frequency differences between -10% and 10% of the center frequency. The results indicate that differential-frequency operation at Ka-band frequencies (26.5 - 40 GHz) provides relatively strong differential signals if the frequencies can be separated by at least 5%. Unlike lower frequency operation, the differential signals at Ka-band (both reflectivity and Doppler) are directly related to the median mass diameter. An important feature of the differential mean Doppler is that it depends only on the drop-size dependent part of the radial velocity. In principle, the mean and mean differential Doppler data from a nadir-looking platform can be used to infer vertical air motion and characteristics of the particle size distribution (Meneghini et al., 2001).

To test the instrument concept, the ER-2 Doppler radar (Heymsfield et al., 1996) was modified for differential frequency operation. Measurements by the modified radar, operating at frequencies of 9.1 GHz and 10 GHz, were made using an 8° zenith-pointing offset parabolic antenna. Simultaneous data were taken with an optical rain gauge and an impact disdrometer. Measured and DSD-estimated values of the differential dBZ mean Doppler are presented in section 3.

2. DIFFERENTIAL FREQUENCY CALCULATIONS

For the results shown here, the hydrometeors are taken to be spherical and the scattering cross sections are calculated from Mie theory. We define the equivalent reflectivity factor difference, \( \delta Z_e(f, \delta f) \), or more simply, the differential reflectivity, by

\[
\delta Z_e(f, \delta f) = \text{sgn}(\delta f) \left[ dBZ_e(f) - dBZ_e(f+\delta f) \right] \tag{1}
\]

where \( \text{sgn}(x) = 1 \) for \( x > 0 \) and \( -1 \) for \( x < 0 \) so that \( \delta Z_e \) is always taken as the difference between \( dBZ_e \) at the lower frequency to that at the higher frequency. The equivalent reflectivity factor at frequency \( f \) is given by

\[
Z_e(f) = 10 \log_{10} Z(f) \tag{2}
\]

where \( Z_e(f) = \frac{7.4}{\lambda^2} \left( \frac{\pi \sigma_{bl}(\lambda, D)}{K_w} \right) N(D) \right \ dD \)

and where \( N(D) \) is the drop size distribution (mm\(^{-1}\) m\(^3\)). For the calculations presented, \( N(D) \) is assumed to be an exponential. Because \( \delta Z_e \) is proportional to the log of a ratio of \( Z_e \) measurements, it is independent of number concentration but dependent on the median mass diameter, \( D_0 \). The differential mean Doppler, \( \delta v(f, \delta f) \), can be defined in a similar way:

\[
\delta v(f, \delta f) = \text{sgn}(\delta f) \left[ <v(f)> - <v(f+\delta f)> \right] \tag{3}
\]

where \( <v(f)> \) is the mean Doppler velocity at the radar frequency \( f \). Shown in Fig. 1 are contour plots of \( \delta Z_e \).

Fig. 1: Contour plots of \( \delta Z_e \) in the \( f-\delta f \) space for rain with \( D_0=2 \) mm (top) and snow with \( D_0=4.31 \) mm (bottom).

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Fig. 3 Maximum singular value plot for open and nominal closed loop system.

Fig. 5 Maximum singular value plot for closed-loop system under different actuator failures

Fig. 4 Variation of $H_{\infty}$ norm with 5% errors in natural frequency, 500 cases

Fig. 6 Time response of pointing under disturbance for four conditions: Operational, Act-1 Failure, Act-2 Failure, and Act-3 Failure
note that there are 3 mechanisms at work. In rain, at X-band frequencies, $\delta Z_e$ is negative, i.e., $\text{dB}Z_e$ increases locally with $f$. Generally speaking, larger $D_0$ values are associated with larger values of $|\delta Z_e|$ although it must be noted that $|\delta Z_e|$ attains a maximum at $D_0=1.8$ mm and begins to decrease thereafter. As the signals propagate into the rain $\delta Z_e$ becomes progressively less negative because the attenuation at the higher frequency is larger than that at the lower. Because $\delta Z_e$ is positive in dry snow, a change in the sign of $\delta Z_e$ occurs as the signals transit the melting layer.

Between the EDOP data and DSD-derived estimates of $\delta Z_e$ are noisy, the correlation is relatively good. This is encouraging in the sense that the (9.1 GHz, 10 GHz) combination is far from optimum, suggesting that sets of frequencies at Ka-band, separated by 5% to 10%, should yield stable estimates of $\delta Z_e$ and $\delta v$.

4. SUMMARY

Computations of the differential-frequency radar reflectivity factor and mean Doppler suggest that useful information on the drop size distribution and vertical air motion are feasible at Ka-band frequencies where the signal levels are relatively strong and directly related to the median drop diameter. As such, the measurement concept has applications to airborne and spaceborne sensing of rain and cloud. Experimental tests of the concept were conducted using the X-band EDOP radar where it was shown that measurements of $\delta Z_e$ correlate fairly well with estimates derived from measured drop size distributions.

5. REFERENCES


for rain (top) and snow (bottom) cases. For example, the values of \( \delta Z_e \) for the frequency pair (25 GHz, 26.25 GHz) can be found at the (x, y) coordinates (25 GHz, +5%) yielding \( \delta Z_e = 0.45 \) dB in the case of rain and \( \delta Z_e = 0.6 \) dB for snow. For a fixed center frequency we can examine the behavior of \( \delta Z_e \) in the \( \delta f - D_0 \) space by contour plots of the type shown in Fig. 2. Comparisons of the 14 and 35 GHz results reveal two advantages of operating at the higher frequency: larger signal strength and a 1-to-1 relationship between \( \delta Z_e \) and \( D_0 \). At 14 GHz, in contrast, more than one value of \( D_0 \) is consistent with the \( \delta Z_e \) measurement over certain ranges. Contours of \( n \), the number of independent samples required for the mean differential signal level to be greater than the standard deviation of the measurement, are also shown on the figures.

3. EDOP DIFFERENTIAL MEASUREMENTS

Differential frequency measurements were made using the ER-2 Doppler radar (EDOP) in a ground-based, zenith-looking configuration. To modify the EDOP for differential measurements, the local oscillator (LO) at 9.6 GHz was disconnected and replaced with two synthesized HP-83640 sweep generators. These oscillators were used both to generate the transmit pulse and to mix the received signals down to the intermediate frequency (IF). The LO frequencies were chosen to produce transmit frequencies of 9.1 and 10 GHz, a separation that was found to be the practical limit based on the performance characteristics of the EDOP traveling wave tube amplifier (TWTA). It should be noted that the generation, transmission, and reception of the two frequencies were done simultaneously (Bidwell et al., 2000).

On March 27, 2000, an impact disdrometer and optical rain gauge were placed next to the zenith-directed antenna. Approximately 3 hours of data were collected. Because the modified radar was uncalibrated, the radar return powers were converted into radar reflectivities, by an additive constant, using the drop size distribution data near the beginning of the measurement period. Height versus time plots of \( dBZ_e(9.1 \text{ GHz}) \) and \( \delta Z_e(f=9.1 \text{ GHz}, \delta f=0.9 \text{ GHz}) \) are shown in the top and center panels of Fig. 3. Displayed in the bottom panel are selected vertical profiles of \( \delta Z_e \). Corresponding plots of \( \langle v(9.1 \text{ GHz}) \rangle \) and \( \delta v(9.1, 0.9) \) are shown in Fig. 4. The data show that the rain was primarily stratiform with a well-defined bright-band at a height of approximately 2.2 km. To understand the \( \delta Z_e \),

![Fig. 2: Contour plots of \( \delta Z_e \) in \( \delta f - D_0 \) space for fixed center frequencies of 14 GHz (top) and 35 GHz (bottom).](image)

![Fig. 3: Height-time plots of \( dBZ_e(9.1 \text{ GHz}) \) (top), \( \delta Z_e(9.1 \text{ GHz}, 0.9 \text{ GHz}) \) (center) and height-profiles of \( \delta Z_e \) (bottom).](image)