A Comparison of Techniques for Scheduling Fleets of Earth-Observing Satellites

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Abstract
Earth observing satellite (EOS) scheduling is a complex real-world domain representative of a broad class of oversubscription scheduling problems. Oversubscription problems are those where requests for a facility exceed its capacity. These problems arise in a wide variety of NASA and terrestrial domains and are an important class of scheduling problems because such facilities often represent large capital investments. We have run experiments comparing multiple variants of the genetic algorithm, hill climbing, simulated annealing, squeaky wheel optimization and iterated sampling on two variants of a realistically-sized model of the EOS scheduling problem. These are implemented as permutation-based methods; methods that search in the space of priority orderings of observation requests and evaluate each permutation by using it to drive a greedy scheduler. Simulated annealing performs best and random mutation operators outperform our squeaky (more intelligent) operator. Furthermore, taking smaller steps towards the end of the search improves performance.

Introduction
A growing fleet of scientific, military, and commercial Earth observing satellites (EOS) circles the globe. Although there are approximately 60 EOS satellites in orbit today, image collection is nearly always scheduled separately for each satellite with manual coordination, if any. Some studies (Globus et al. 2002) (Rao, Soma, & Padmashree 1998) have suggested that automatic coordination of multiple satellites can be beneficial, but the best scheduling technique to use is not clear. The problem is complicated by the fact that EOS scheduling is subject to multiple complex constraints, including power, thermal, data capacity, and the limited time each satellite spends over each target. Furthermore, when we consider the total number of observations that can be performed by a satellite constellation (thousands) and the number of options (time windows) there are for each observation, we find that the search space for EOS scheduling problems is quite large.

More importantly from a research point of view, EOS scheduling is one instance of a larger class of oversubscription scheduling problems. These problems are characterized by more requests for a resource than can be satisfied, insuring that some requests remain unfulfilled. In addition to EOS, such problems include scheduling planetary probes, telescopes, the deep space network, supercomputers, wind tunnels and other test facilities. In general, oversubscription problems arise when requests for a facility need to be scheduled so as to optimize productivity subject to a complex set of operational constraints, but the requests interact with each other weakly (e.g., through shared resources) and do not generate additional requests. It is these properties that distinguish oversubscription scheduling problems from the more general, and more difficult, class of oversubscription planning problems (Smith 2004).

Our work focuses on permutation-based (Syswerda & Palmucci 1991) approaches to scheduling problems. The key insight underlying such approaches is that if we could greedily schedule the EOS observation requests in an optimal order then we would produce an optimal schedule.1 Thus, a greedy scheduler allows us to search the space of priority vectors (a.k.a. permutations) rather than the space of schedules. This change of representation has two key advantages: First, and most importantly, the greedy scheduler can take any permutation and produce a feasible (though generally sub-optimal) schedule. This means that we can make local moves, including genetic crossover operations, without straying into infeasible space (in contrast to methods that search in the space of schedules which must work hard to maintain feasibility, or find ways to evaluate the goodness of infeasible schedules). Second, if there are many possible times at which observations can be scheduled it is often the case that the space of possible permutations is significantly smaller than the space of possible schedules.

Computational scheduling techniques have been applied to the EOS scheduling problem by several authors, including:

1. Sherwood (Sherwood et al. 1998) used ASPEN, a general purpose scheduling system, to automate

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1 We should note that proving optimality for a permutation-based method in a domain requires a detailed analysis of the constraints and optimization criteria of the domain as well as the details of the greedy scheduler.
scheduling of NASA's EO-1 satellite.

2. Potter and Gasch (Potter & Gasch 1998) described a clever algorithm for scheduling NASA's Landsat 7 satellite featuring greedy search forward in time with fix-up to free resources for high priority observation.

3. Lamaitre's group has examined EOS scheduling issues including comparison of multiple techniques. See, for example, (Lamaitre, Verfaillie, & Bataille 1998), (Bensana, Lamaitre, & Verfaillie 1999) and (Lamaitre et al. 2000).

4. Wolfe and Sorensen (Wolfe & Sorensen 2000) compared three algorithms on the window-constrained packing problem, which is related to EOS scheduling. They found that the genetic algorithm produced the best schedules, albeit at a significant CPU cost.

Our study compares thirteen EOS scheduling algorithms on two variants of a realistically-sized model problem. In particular, we compare simulated annealing, hill climbing, the genetic algorithm, squeaky wheel optimization, and iterated sampling (ISAMP). In the next section we describe the scheduling problem and our model. A description of the scheduling techniques follows. The nature and results of our computational experiments are then presented along with analysis.

**EOS Scheduling Problem**

We first describe the real EOS scheduling problem. Then we describe the model problems used in this experiment.

EOS scheduling attempts to take as many high-priority observations as possible within a fixed period of time with a fixed set of satellite-born sensors. For example, the Landsat 7 satellite scheduler is considered to have done a good job if 250 observations are made each day. EOS scheduling is complicated by a number of important constraints. Potin (Potin 1998) lists some of these constraints as:

1. Revisit limitations. A target must be within sight of the satellite. EOS satellites travel in fixed orbits, usually about 800 km up and 100 minutes per orbit. These orbits pass over any particular place on Earth at limited times so there are only a few observation windows (and sometimes none) for a given target.

2. Time required to take each image. Most Earth observing satellites take a one-dimensional image and use the spacecraft's orbital motion to sweep out the area to be imaged. For example, a Landsat image requires 24 seconds of orbital motion.

3. Limited on-board data storage. Images are typically stored on a solid state recorder (SSR) until they can be sent to the ground.

4. Ground station availability. The data in the SSR is sent to the ground (SSR dumps) when the satellite passes over a ground station. Ground station windows are limited as with any other target.

5. Transition time between look angles (slewing). Some instruments are mounted on motors that can point side-to-side (cross-track).

6. Power and thermal control availability.

7. Coordination of multiple satellites.

8. Cloud cover. Some sensors cannot see through clouds.

9. Stereo pair acquisition or multiple observations of the same target by different sensors or the same sensor at different times.

Both variants of our model problem exhibit all these constraints except the last two. The problems consist of three satellites in Sun-synchronous orbits (orbits in which the equator is crossed at the same local time each orbit) for one week. The satellites are spaced ten minutes apart. Each satellite carries one sensor mounted on a cross-track slewable motor that can point up to 24 degrees to either side of nadir (nadir is straight down) and turns one degree in two seconds. In Problem 1, each satellite has an SSR capable of storing 50 arbitrary units. In Problem 2, the SSR stores 75 units.

We model power and thermal constraints using so-called duty cycle constraints, the approach taken by Landsat 7. A duty cycle constraint requires that the sensor not be turned on for longer that a maximum time within any interval of a certain length. Our model problem uses the Landsat 7 duty cycles. Specifically, a sensor may not be used for more than:

1. 34 minutes in any 100 minute period.
2. 52 minutes in any 200 minute period, or
3. 131 minutes in any 600 minute period.

There is one ground station in Alaska. Whenever a satellite comes within sight of the ground station it is assumed to completely empty its SSR, which is then available for additional observation storage. There are approximately 75 SSR dumps per spacecraft during the week. Since some orbits are over oceans and all targets are on land, some SSR dump opportunities are wasted on an empty SSR.

6300 observation targets were randomly generated on land. Of these, 6114 are observable by at least one satellite during the one week scheduling period. The targets are assumed to be at the center of a rectangle that requires 24 seconds of satellite motion to image. Each observation requires one, three, or five arbitrary storage units (evenly distributed) on the SSR. Each observation was assigned a priority from one to six evenly spaced in 0.1 increments. Each observation has 2-24 windows, times when a satellite is within view of the observation's target. Orbits and windows were determined by the free version of the Analytical Graphics Inc.'s Satellite Tool Kit, also known as the STK (see www.stk.com).

The fitness (quality) of each schedule is determined by a weighted sum (smaller values indicate better fitness):
where \( F \) is the fitness, \( O_u \) is the set of unscheduled observation, \( P_o \) is an observation's priority, \( S \) is the total time spent slewing, \( A \) is the sum of the off-nadir pointing angle for all scheduled observations, \( w \) stands for weight, \( w_p = 1 \), \( w_s = 0.01 \), and \( w_a = 0.00137 \) for Problem 1 and \( w_p = 0.02 \) for Problem 2. Note that the weights favor the priority of unscheduled observations over pointing and slewing time objectives, and that the off-nadir pointing objective has very little influence on Problem 1. \( w_a \) is set so that scheduling another observation always increases fitness, but just barely for a \( P_o = 1 \) observation. \( w_a \) in Problem 2 is set similarly.

There are only two differences between the model problem variants: Problem 2 has more SSR space and the off-nadir pointing objective is much more important. Additional SSR space implies that the duty cycle constraint will be more important.

### Scheduling Algorithms

This study compares thirteen search algorithms applied to the EOS scheduling problem. The simplest techniques were hill climbing, simulated annealing, two variants of the genetic algorithm, and ISAMP (essentially random search). By using a more intelligent mutation operator, these algorithms (except ISAMP) become variants of squeaky wheel optimization (Joslin & Clements 1999).

We represent a schedule as a permutation or arbitrary, non-temporal ordering of the observations. The observations are scheduled one at a time in the order indicated by the permutation. In pseudo-code:

1. \( \text{int[i] permutation} = \text{permutation of the integers 1-numberOfObservations} \)
2. \( \text{for(int i = 1; i != numberOfObservations; i++)} \)
   
   (a) \( \text{schedule observation permutation[i] if it does not violate any of the current constraints} \)

This allows us to search in permutation-space as opposed to schedule-space. A simple, greedy, deterministic, one-observation scheduler assigns resources to observations in the order indicated by the permutation. This produces a set of timelines with all of the scheduled observations, the time they were taken, and the resources (SSR, sensor, pointing angle) used. The one-observation scheduler assigns times and resources to observations using earliest-first scheduling heuristics while maintaining consistency with all constraints. If an observation cannot be scheduled without violating the current constraints (those created by scheduling observations from earlier in the permutation), the observation is left unscheduled.

Earliest-first scheduling starting at \( time = 0 \) had problems. We discovered that the one-observation scheduler works better if, for each observation, 'earliest-first' starts at some initial time rather than \( time = 0 \). The initial time, set randomly at first, is generally different for each observation. The one-observation scheduler starts at the initial time and looks forward for a constraint-free window. If none is found before the end of time, the scheduler wraps around to \( time = 0 \).

The time each observation is scheduled (or, if unscheduled, what time 'earliest-first' search started) is stored and preserved by mutation and crossover. The extra scheduling flexibility may explain why this approach works better than earliest-first starting at \( time = 0 \).

Constraints are enforced by representing sensors, slew-motors and SSRs as timelines. Scheduling an observation causes timelines to take on appropriate values (i.e., in use for a sensor, slew motor setting, amount of SSR memory available) at appropriate times. These timelines are checked for constraint violations as the one-observation scheduler attempts to schedule additional observations.

The simplest search technique tested was ISAMP, which is essentially a random search. With ISAMP, each schedule is generated from a random permutation with random start times for the one-observation scheduler. The rest of the search techniques start with random permutations and generate new permutations with mutation and/or crossover. The techniques tested were:

1. Hill climbing (Hc), which starts with a single randomly generated permutation. This permutation (the parent) is mutated to produce one new permutation (a child) which, if the child represents a more fit schedule than the parent, replaces the parent.
2. Simulated annealing (Sa), which is similar to hill climbing except that less fit children can replace the parent with a probability that depends on an artificial temperature. The temperature starts at 100 (arbitrary units) and is multiplied by 0.92 every 1000 children (100,000 children are generated per job).
3. A steady-state tournament selection genetic algorithm (Gs) with population size 100. The individual to replace is chosen by a tournament from the whole population where the least fit is replaced. Tournament size is always two.
4. A generational elitist genetic algorithm (Gg) with population size 110 where the 10 best individuals are copied into the next generation. Parents are chosen by tournament (size = 2).

Each search technique was tested with three mutation operators:

1. Random swap (Rs). Two permutation locations are chosen at random and the observations are swapped, with 1-15 swaps (chosen at random) per mutation. Earlier experiments (Globus et al. 2003) determined that allowing more than one swap improved scheduling (see Table 3).
2. Temperature-dependent swap (Td). Here the number of swaps (1-15) is still chosen at random but with a bias. Early in evolution a larger number of swaps
tend to be used, and later in evolution fewer swaps are performed. This is analogous to the 'temperature' dependent behavior of simulated annealing. The choice of the number of swaps is determined by a weighted roulette wheel where the weights vary linearly as evolution proceeds starting at \( n \) and ending at \( 16 - n \) where \( n \) is the number of swaps. Earlier experiments tried fewer swaps early in evolution and more swaps later. This didn't work as well.

3. Squeaky shift (Ss). This implements squeaky wheel optimization. The mutator shifts 1-15 (chosen randomly) 'deserving' observations earlier in the permutation. Early in the permutation an observation is more likely to be scheduled since fewer other observations will have been scheduled to create additional constraints. Each observation to shift forward is chosen by a tournament of size 50, 100, 200, or 300 (chosen at random each time). The observation is always chosen from the last half of the permutation. The position-to-shift-in-front-of is chosen by a tournament of the same size (each time) and is guaranteed to be at a location at least half way towards the front of the permutation (starting at the 'deserving' observation). The observation most deserving to move earlier in the permutation is determined by the following characteristics (in order):

(a) unscheduled rather than scheduled
(b) higher priority
(c) later in the permutation

The position-to-shift-in-front-of tournament looks for the opposite characteristics.

In the case of the genetic algorithms, half of all children are created by mutation and the other half by crossover. The crossover operator is position-based crossover (Syswerda & Palmucci 1991). Roughly half of the permutation positions are chosen at random (50% probability per position). The observations in these positions are copied from the father to the same permutation location in the child. The remaining observations fill in the child's other permutation positions in the order they appear in the mother.

We tested a number of other mutation operators. The ones examined in this experiment performed the best. See (Globus et al. 2003) and Table 3 for some of these data. There was not time to implement and test 'max-flexibility' (Kramer & Smith 2003). We did test heuristic-biased stochastic sampling (HBSS) (Bresina 1996) with contention heuristics (Frank et al. 2002), a technique proposed for the EOS scheduling problem that searches schedule-space rather than permutation-space. HBSS was hundreds of times slower than the permutation-based techniques, required far more memory, and produced very poor schedules. There are many techniques that search schedule-space and these results are not sufficient to draw conclusions comparing permutation-space and schedule-space search.

**Experiment**

To find the best algorithm for the model problems we compared a total of thirteen techniques. These were ISAMP and every combination of four search techniques - hill climbing, simulated annealing, steady state GA, and generational GA - crossed with three mutation operators - 1-15 random swaps, 1-15 temperature dependent swaps, and 1-15 squeaky shifts. Thirty-two jobs with identical parameters (except the random number seed) were run for each algorithm. Each job generated approximately 100,000 schedules (the GA jobs generated slightly more).

Table 1 compares the algorithms for Problem 1 and Table 2 for Problem 2. In Table 1 and the figures, the techniques are ordered by the mean fitness in Problem 1. Table 2 is ordered by the mean fitness in Problem 2. Most, although not all, of the differences were statistically significant by both t-test and ks-test, with confidence levels usually far above 99%. For the most part, the ordering is similar for all fitness objectives (priority, slewing time, or off-nadir pointing), although there are some exceptions. Table 3 shows similar results with slightly different techniques on a smaller but related problem. We have had similar results on other problems as well.

Simulated annealing is the clear winner for all problems. For Problem 1, hill climbing with temperature dependent swaps equals simulated annealing with random swaps, but on Problem 2 simulated annealing always wins. Even hill climbing outperforms both forms of the genetic algorithm and this is true regardless of mutation operator. ISAMP, as one might expect for random search, performed the worst.

For simulated annealing and hill climbing, temperature dependent swaps outperform all other mutation operators, although for the genetic algorithms random swaps outperform temperature dependent swaps. Both random swaps and temperature dependent swaps clearly outperform squeaky shifts for all search techniques.

The small standard deviations for all algorithms suggest that all jobs for a given algorithm get about the same fitness. Thus, even if the fitness landscape is multi-modal, most of the minima must be about the same. Figures 1 and 2, which show the breadth of each fitness distribution over 32 jobs, confirms this view. For this reason, we suspect that this problem requires mostly exploitation, rather than exploration, which also explains the poor GA results. Evolutionary change is spread out over the GA populations rather than concentrated on a single individual as in simulated annealing and hill climbing.

The squeaky shift mutator's performance relative to random swaps suggests that it is smart in the wrong way. In preliminary experiments we also tried swapping, rather than shifting, observations (see Table 3). The shift operator performed the best, but still not as well as the random swap mutator (data not published). If random outperforms intelligent, then clearly intel-
ligence is being applied in the wrong way. We do not understand the dynamics of permutation-space scheduling in any fundamental way, and we don't even know if the dynamics are similar for different problems. Until a better understanding is reached, the random swap operators - with a decrease in the number of swaps as evolution proceeds - appear best.

Figures 3 and 4 show one effect of changing $w_a$ from 0.00137 in Problem 1 to 0.2 in Problem 2. In Problem 2, the absolute value of the off-nadir pointing is reduced and the range of values is greatly reduced, suggesting that the pointing objective is important enough to affect the search.

Summary

We compared thirteen different permutation-space search techniques for scheduling EOS fleets on realistically-sized model problems. Simulated annealing outperformed hill climbing which, in turn, outperformed the genetic algorithm. Simple random swap mutation outperformed the more 'intelligent' squeaky mutation. Reducing the number of random swaps as evolution proceeds further improved performance. Although we examined only two closely related problems here, we have seen essentially the same results on other EOS scheduling problems.

An important follow-up to our work would be an equally thorough study of non-permutation methods; those that search in the space of all possible schedules. We examined one candidate, HBSS with contention heuristics, which performed very poorly. We conjecture that the simplicity of local search in permutation-space (particularly the fact that we do not need to search in infeasible space) will lead permutation-based methods to dominate on many oversubscription problems. However, this conjecture can only be evaluated by a head-to-head comparison of the best permutation-based and schedule-based search algorithms.

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References


Table 1: Scheduling algorithms tested ordered by mean fitness for 32 jobs on Problem 1. All values are means except column 3. Smaller values are best. Column heading labels refer to Equation 1. Sa stands for simulated annealing, Hc for hill climbing, Gs for steady-state GA, Gg for generational GA, Rs for random swaps, Td for temperature dependent swaps, and Ss for squeaky shifts.

| algorithm | F (fitness) | F StdDev | \( \sum_{O_o} P_o \) (priority) | \( S/O_u \) (slewing) | \( A/O_u \) (pointing) | \( |O_u| \) (unscheduled) |
|-----------|-------------|----------|----------------------------------|-----------------|-----------------|-----------------|
| SaTd      | 9205        | 20       | 8571                             | 17              | 10.1            | 2211            |
| HcTd      | 9310        | 21       | 8659                             | 18              | 10.3            | 2289            |
| SaSr      | 9311        | 19       | 8662                             | 18              | 10.2            | 2250            |
| HcSr      | 9368        | 25       | 8716                             | 18              | 10.3            | 2313            |
| SaGs      | 9489        | 19       | 8872                             | 19              | 10.4            | 2553            |
| HcGs      | 9507        | 24       | 8865                             | 19              | 10.4            | 2512            |
| GgSr      | 9700        | 38       | 9017                             | 20              | 10.3            | 2430            |
| GsSr      | 9700        | 25       | 9019                             | 20              | 10.4            | 2430            |
| GgTd      | 9741        | 31       | 9049                             | 20              | 10.5            | 2428            |
| GgGg      | 9834        | 24       | 9130                             | 20              | 10.5            | 2458            |
| GgGs      | 9964        | 53       | 9081                             | 21              | 10.5            | 2652            |
| GsSs      | 10010       | 46       | 9330                             | 21              | 10.4            | 2673            |
| ISAMP     | 10463       | 11       | 9727                             | 23              | 10.7            | 2723            |

Table 2: Same as Table 1 except data (and ordering) from Problem 2.

| algorithm | F (fitness) | F StdDev | \( \sum_{O_o} P_o \) (priority) | \( S/O_u \) (slewing) | \( A/O_u \) (pointing) | \( |O_u| \) (unscheduled) |
|-----------|-------------|----------|----------------------------------|-----------------|-----------------|-----------------|
| SaTd      | 5571        | 23       | 3954                             | 16              | 9.5             | 1118            |
| SaSr      | 5648        | 22       | 4009                             | 17              | 9.6             | 1125            |
| SaGs      | 5786        | 29       | 4163                             | 18              | 9.9             | 1332            |
| HcTd      | 5870        | 28       | 4237                             | 18              | 9.7             | 1246            |
| HcSr      | 5913        | 36       | 4273                             | 18              | 9.6             | 1258            |
| HcGs      | 6032        | 38       | 4419                             | 18              | 9.8             | 1421            |
| GgSr      | 6306        | 45       | 4640                             | 19              | 10.0            | 1371            |
| GgGs      | 6317        | 44       | 4646                             | 19              | 10.0            | 1375            |
| GgTg      | 6340        | 35       | 4642                             | 19              | 10.1            | 1351            |
| GgTd      | 6489        | 39       | 4782                             | 20              | 10.2            | 1399            |
| GgTs      | 6735        | 66       | 5088                             | 21              | 10.2            | 1615            |
| GsSs      | 6839        | 78       | 5185                             | 21              | 10.3            | 1638            |
| ISAMP     | 7797        | 12       | 6124                             | 23              | 10.6            | 1774            |

Table 3: Results from a somewhat different problem with a different, but related, set of search techniques. Note that the overall results are similar. Here the problem has two satellites and 4000+ observations with SSR size, slewing rate and times, and other aspects different from the model that generated Tables 1 and 2. Details can be found in (Globus et al. 2003).
Figure 1: Comparison fitness (vertical axis) for 32 jobs in Problem 1. The boxes indicate the second and third quartiles. The line inside the box is the median and the whiskers are the extent of the data. Outliers are represented by small circles.

Figure 2: Same as Figure 1 with data from Problem 2.
Figure 3: Mean off-nadir pointing angle needed for each scheduled observation (mean of $A/|O_u|$ from Equation 1).

Figure 4: Same as Figure 3 with data from Problem 2.