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Abstract

In many advanced low NOx gas turbine combustion techniques, such as rich-burn/quick-mix/lean-burn (RQL), jet mixing in a reacting, hot, fuel-rich crossflow plays an important role in minimizing all pollutant emissions and maximizing combustion efficiency. Assessing the degree of mixing and predicting jet penetration is critical to the optimization of the jet injection design strategy. Different passive scalar quantities, including carbon, oxygen, and helium are compared to quantify mixing in an atmospheric RQL combustion rig under reacting conditions. The results show that the O2-based jet mixture fraction underpredicts the C-based mixture fraction due to jet dilution and combustion, whereas the He tracer overpredicts it possibly due to differences in density and diffusivity. The He-method also exhibits significant scatter in the mixture fraction data that can most likely be attributed to differences in gas density and turbulent diffusivity. The jet mixture fraction data were used to evaluate planar spatial unmixedness, which showed good agreement for all three scalars. This investigation suggests that, with further technique refinement, O2 or a He tracer could be used instead of C to determine the extent of reaction and mixing in an RQL combustor.

Nomenclature

\( d \) orifice axial length

\( f \) jet mixture fraction

\( f_{yi} \) jet mixture fraction based on mass fraction of species \( i \)

\( f_{xi} \) jet mixture fraction based on molar fraction (or concentration) of species \( i \)

\( f_{var} \) variance of all point \( f \) values in a plane w.r.t. \( f_{avg} \)

\( f_{avg} \) area-weighted average jet mixture fraction specific to each plane

\( J \) jet to crossflow momentum-flux ratio

\( M_{i} \) molar mass of species \( i \)

\( \phi \) equivalence ratio = \( \frac{(\text{fuel/air})_{local}}{(\text{fuel/air})_{stoichiometric}} \)

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Introduction

Many advanced low NOx combustion techniques, such as lean premixed prevaporized injection, lean direct injection, and rich-burn/quick-mix/lean-burn (RQL) rely on the rapid and thorough mixing of air and fuel in order to minimize all pollutant emissions and maximize combustion efficiency. Various studies have found that fuel-air ratio non-uniformities significantly affect NOx emissions [1,2,3].

In gas turbine combustion, jet mixing in a reacting, hot, fuel-rich crossflow plays an important role due to air jet injection in the primary, secondary, and dilution zones of the combustor. Assessing the degree of mixing and predicting jet penetration is especially critical in the RQL combustion concept. One of the advantages of RQL over other combustion techniques is quick and complete mixing between the rich and lean zones of the combustor in order to eliminate hot, near-stoichiometric reactant pockets that may lead to NOx formation. In addition to combustion, the assessment of jet mixing into a crossflow can be applied to a wide range of fields such as gas turbine cooling and staging, fuel-air premixing, vertical short takeoff and landing aircraft, and pollutant discharge from stacks or pipes.

This study compares the use of different scalar quantities, including carbon, oxygen, and an inert tracer gas to quantify mixing in an atmospheric RQL combustion rig under reacting conditions.

Background

Most experimental jet-in-crossflow studies have focused on non-reacting systems, with only a limited number of tests having been reported under reacting conditions. Although isothermal testing is useful and convenient, actual combustor mixing and performance needs to be measured in a combusting flow. An extensive listing of these isothermal and reacting studies can be found in [4,5,6,7].

The diagnostic technique chosen to determine mixing in reacting systems is important to the outcome of this study. Qualitative characterization of the mixing process can be inferred through the measurement of temperature profiles and species concentrations. However, to determine the true extent of mixing in a reactant flow field, one needs to measure, experimentally, the jet mixture fraction \( f \).

Two techniques, used in numerous studies and summarized by Jones et al. [8], can be used to measure or deduce \( f \) in a transverse flow. The first method is to use non-intrusive optical diagnostics, such as laser-induced fluorescence (LIF), Rayleigh scattering [9,10], or Raman scattering, to quantify spatial and temporal unmixedness. Planar imaging eliminates the need for extractively measuring multiple species and for sampling at multiple points in the flame.
However, optical methods are limited by the availability of costly laser and detector systems, the practicality of optical access into the flow, the need to seed or modify the fuel to obtain the desired optical signal, as well as in-flame interferences such as molecular quenching.

The second approach, which is the focus of this study, is based on the measurement of a conserved scalar (i.e., unaffected by the chemical reaction), such as carbon, oxygen, nitrogen, or hydrogen mass fraction, equivalence ratio, or an inert gas. This treatment assumes that the slowest chemical kinetic reaction rate is much faster than the turbulent mixing time scales [11]. Under this assumption, local instantaneous composition measurements correspond to chemical equilibrium and can be related to a strictly conserved scalar variable. Furthermore, this technique assumes a well-mixed recirculation zone in which mixing times are much less than residence times [11].

Previous studies [8,12,13] have used carbon mass fraction and equivalence ratio to calculate $f$. Aspirated emissions samples were analyzed for CO, CO$_2$, O$_2$, total hydrocarbons (THCs), and, in the case of Jones et al. [8], H$_2$. These analyses directly capture all carbon-carrying species needed to determine a C-based $f$. However, in the case of a jet in a rich crossflow, other quantities, such as the oxygen atom (O), the oxygen molecule (O$_2$), or an inert tracer gas such as helium (He) or neon (Ne), can be used to simplify the calculation of $f$. With respect to O$_2$, because it is a key participant in the combustion reactions, it cannot truly be considered a conserved scalar. However, since it is only present in the jet flow and since there is considerable excess air present in the downstream flow, its concentration profile can not only be used to indicate jet presence and dispersion, as was shown in [12,13], but potentially mixture fraction as well.

Helium has served as an inert tracer in various studies to determine a wide range of parameters, such as groundwater transport [14], fluid flow in a porous rock [15], residence time in a spray-drying tower [16], automobile exhaust flow rate [17], impervious wall effectiveness of film-cooling slots [18], scalar flow field in a combustor rig under isothermal (non-reacting) conditions [11,19,20], and mass transport rates in a non-reacting jet-in-crossflow [21,22]. Helium is an inexpensive, readily available gas that is detectable using gas chromatography, mass spectrometry, or a catharometer (thermal conductivity detector).

The purpose of this study is to use alternative passive scalars, namely O, O$_2$, and He to generate jet mixture fractions at specific planes in an RQL combustion rig. The mixture fraction data are then used to determine the degree of spatial mixing of chemical species at each of the measurement planes in the combustor. The results are compared to carbon-based $f$ results to demonstrate the viability of a simpler method that requires the analysis of only a single compound to quantify air-fuel mixing, and to determine suitability of this diagnostic in this experiment and for future reacting applications.

This study expands upon two previous studies by Leong et al. [12,13]. In ref. 12 the setup for reacting tests in an RQL crossflow configuration was described and characterized, and in ref. 13 the optimal number of jet injection orifices was determined to obtain rapid mixing of air jets in a rich crossflow and a uniformly lean, low temperature mixture at the exit plane of the combustor. Most of the species concentrations required for the carbon and oxygen-based mass mixture fractions calculations were collected during the second study [13]. In the work reported herein, a protocol for the sampling and analysis of the helium tracer gas is established. Tracer gas concentrations are then measured under reacting conditions for a series of RQL modules with a different number of jet orifices. Data are collected at specified planes and spatial coordinates to allow direct comparison with results obtained in ref. 13.
Experiment

This section describes the experimental setup, the data measurement protocol, and the procedure for calculating carbon-based and tracer gas-based mixture fractions.

Reacting Test Facility

The reacting jet-in-crossflow experimental set-up, shown in figure 1, has been described in detail in previous papers [12,13]. The upward-fired atmospheric test facility supplies a uniform, fuel-rich composition of gases to the quick-mix section. The quick-mix section utilizes interchangeable quartz tubes containing different jet orifice configurations.

A schematic of the quartz module, shown with the location of the planes of interest, is depicted in figure 2. The inner and outer diameters of the tube are, respectively, 80 mm by 85 mm, and its length is 280 mm. Four different modules were tested, with each one containing a different number of circular orifices (10, 12, 14, or 18) arranged equidistantly around the circumference of the tube. (Note that measurement results for an 8 hole module were reported in ref. 13, but are not included here because He data were not collected for this module). The orifice centerlines are located 115 mm from the entrance of the module. The four measurement planes are displaced from the orifice leading edge as follows: one duct radial length upstream ($x/R = -1$), one orifice diameter downstream ($x/R = d/R$), and one-half and one duct radial lengths downstream ($x/R = 0.5, 1$). This particular region was chosen because, based on data presented by Leong et al. [13], this is where the greatest changes in spatial unmixedness occurred. For each module tested, point samples were taken from a two-orifice sector at 16 radially equidistant locations (see figure 2).

Emissions data, required for calculation of carbon and oxygen-based mixture fractions, were previously presented in ref. 13 for planes $x/R = -1, d/R, and 1$. Additional emissions samples, using the same setup and procedure as outlined in refs. 12 and 13, were collected at $x/R = 0.5$ because intense mixing activity occurs at this plane according to tracer gas data. Emissions were analyzed using the following techniques: CO and CO$_2$ by non-dispersive infrared absorption, O$_2$ by paramagnetism, and THCs by flame ionization.

The experiment utilizes gaseous propane as the combustion fuel. Propane is first mixed with air to yield a fuel-air equivalence ratio $\phi$ of 1.67 in the rich combustion section. The rich product generation is described in more detail in ref.12. The rich-burning mixture, with average temperatures at the $x/R = -1$ plane of 1500 K, enters the quartz mixing section and undergoes additional reaction with jets of air to result in an overall $\phi$ of 0.45. The jet air is fed by a plenum that surrounds the rich combusion chamber and the quartz tube. Heat transferred from the combustor to the plenum air heats the jets of air to 480 K before they enter the jet-mixing section.

The rich equivalence ratio is obtained by setting the mass flow rates of propane and crossflow air at 2.96 g/sec and 27.5 g/sec, respectively. The lean equivalence ratio downstream of the jets requires a total jet mass flow rate of 75.2 g/sec. The reference velocity of the total flow is 18 m/sec. Based on the temperatures measured in the reacting system, the jet-to-crossflow density ratio is 3.3, and the jet-to-crossflow momentum-flux ratio $J$ is 57. This set of conditions is the same as utilized in previous experiments [12,13], and was selected to fall within the range of gas turbine combustor operating conditions [4,5,6,23]. $J$ is kept constant by keeping the total effective orifice area (903 mm$^2$) constant for each of the modules tested. This results in different orifice diameters for each orifice number configuration, namely 12.5, 11.5, 10.6, and 9.4 mm respectively for the 10, 12, 14, and 18 round hole modules.
The Mixture Fraction Determination

The experiment consists of jet air streams injected into a cylindrically-confined crossflow of a fuel-rich mixture of partially-reacted propane and air. Based on the method by Jones et al. [8], the mixture fraction in terms of the jet fluid is defined as

$$f_i = \frac{Y^\text{crossflow}_i - Y^\text{sample}_i}{Y^\text{crossflow}_i - Y^\text{jet}_i}$$  \hspace{1cm} (1)$$

where the jet mixture fraction $f$ is related in terms of the mass fractions $Y_i$ of a conserved scalar $i$ in the crossflow, jets, and extracted gas sample. The jet mixture fraction tracks the amount of the jet fluid relative to the total mixture at a specific location in the combustor. A gas sample composed entirely of crossflow fluid yields a value of $f = 0$, while a sample comprised wholly of jet fluid produces a value of $f = 1$.

As shown in Table 1, four different formulations for mass-based jet mixture fraction were examined. In each case, the table lists the measured quantities, the minimum number of unknown variables needed to calculate $f$, and the assumptions and equations required to solve for these unknowns. The mass-fraction based calculations using C, O, O2, and He as the conserved scalars follow the procedure outlined in [8]. Key assumptions in this method are:

1. The combustion gas mixture is composed of major species only (i.e., CO, CO2, O2, H2O, N2, H2, and THCs) and the respective molar fractions sum to unity.
2. The O2/N2 and thus O/N ratios are the same in the sample stream as in the combustion air.
3. The sampled C/H molar ratio is the same as in the fuel stream.
4. To ensure a unique solution to the system of linear equations (i.e., equal number of equations and unknowns), two hydrocarbons are included: C3H8 as well as C2H4, which is a byproduct from the pyrolysis of C3H8.
5. In the absence of a direct measurement for hydrogen, the H2 molar fraction is assumed to be proportional to the CO molar fraction [24,25].

Assumptions 2 and 3 also imply that all major species have equal diffusivities, a reasonable assumption in turbulent flows according to [11]. Assumption 3 is used to infer a molar fraction $X$ for H2O and thus convert the measured dry basis emissions $X_{i,\text{dry}}$ to a wet basis $X_{i,wet}$ to represent the gases as found in the actual combustion reaction. To perform this basis conversion, Jones et al. [8] uses a matrix formulation of the form

$$AX_{\text{wet}} = X_{\text{dry}}$$  \hspace{1cm} (2)$$

with a solution given by

$$X_{\text{wet}} = A^{-1}X_{\text{dry}}$$  \hspace{1cm} (3)$$

where $A$ is an invertible, square matrix, representing the coefficient matrix in the linear system of equations setup using the assumptions listed in Table 1.

The C- and O-based mixture fractions are considered to give the most comprehensive $f$ values, since the calculations use all available data and only the five assumptions just listed. In fact, the values for $f_{YC}$ and $f_{YO}$ will be almost equal given that both fractions are calculated using the same linear equations set under the same assumptions. Thus, all $f_{YC}$ results in this study can be considered interchangeable with $f_{YO}$. It should be noted that oxygen atom-based $f$ calculations
may be subject to higher percentage uncertainties under certain assumptions due to the subtraction of two nearly equal numbers (i.e., in the numerator of the mixture fraction formula) [26].

Using $O_2$ and He as passive scalars can simplify the determination of $f$ since only data from a single species is needed for the calculation if molar fractions are used. In the case of $O_2$, under equilibrated lean combustion conditions, the concentration will vary as a direct function of equivalence ratio and, by definition of $f$, of mixture fraction as well. Any $O_2$ present in rich regions can be considered as a diluent, which also allows it to serve as quasi-conserved scalar for determining mixture fraction. As shown in table 1, the ratio of measured to maximum (20.9%) $O_2$ concentrations can be used to represent $f_{XO_2}$.

In the tracer gas case, the helium was injected into the crossflow air rather than into the jets to maintain a fair comparison between the mixing fields obtained by the previous carbon atom tracking and the inert tracer method. (In the carbon-based method, the only source of carbon is from the crossflow, not the air jets). Seeding the jet flow, which is 2.5 times the mass flow of the crossflow, would have required helium flow rates that would have quickly depleted available helium supplies during the course of a test. In addition, seeding the crossflow allows for the assessment of its uniformity.

Initially, neon and argon were considered as tracers, since their molecular weights and thus densities and diffusivities more closely match those of propane and air as shown in table 2. Argon, however has a very high background concentration (9340 ppm) compared to helium (5 ppm) and neon (18 ppm) [27] and thus was not pursued. Preliminary studies were conducted on the RQL module using the procedure in order to compare helium and neon as inert tracers. Concentration measurements for both gases injected into the crossflow yielded similar results, suggesting that either could be used as a tracer. Helium has an extensive history as an inert tracer and is much cheaper and more readily available than neon. These practical considerations lead to the choice of helium for use in this experiment.

The injection of the helium tracer into the crossflow, the assumption that the jet air stream contains negligible levels of helium, and the approximation that the helium concentration at the crossflow injection plane is relatively uniform lead to the helium-based jet mixture fraction relationship $f_{XHe}$ shown in table 1. (Variation across the plane was found to be less than 3%.) The value $f_{XHe}$ gives the relative change in helium concentration with respect to the maximum concentration in the plane $x/R = –1$. Helium gas of ultra-pure carrier grade (99.999% purity) is supplied at a flow rate of 4.5 l/min and injected into the propane stream. This is the minimum flow rate tested under the current operating conditions that produces a distinct signal, which corresponds to a maximum volume concentration of 0.3% of the rich crossflow mixture. The propane-helium mixture is injected into the crossflow air, and flows through a 4.3-m mixing length filled with baffles to prepare the gas mixture for combustion. The resulting mass fractions of helium, fuel, and air upstream and downstream of the jet mixing section are noted in table 3.

First, the mass-fraction-based $f_{YO_2}$ and $f_{YHe}$ were determined in order to provide a point of reference to compare to $f_{YC}$ and $f_{YO}$. Then, the molar fraction (or concentration)-based $f_{XO_2}$ and $f_{XHe}$ were calculated. The accuracy of using molar fraction instead of mass fraction relies on the fact that most of the sample mass and volume at the measurement planes within the jet injection section are composed of jet air. As a result, one can make the following approximations:

1. The total mass of the sample is constant (it actually varies by $\pm$4% across the sampling planes)
2. $X_{dry}$ is linearly proportional to $X_{wet}$ (the average difference between $X_{dry}$ and $X_{wet}$ is approximately 6% for $O_2$ and He).
3. Because of approximations 1 and 2 and given the linear relationship between \( Y_i \) and \( X_i \) (i.e., \( Y_i = \frac{M_i}{M_{\text{sample}}} X_i \), where \( M_i \) is the molar mass of species \( i \) and \( M_{\text{sample}} \) is the molecular weight of the sample), \( f_{Y_{\text{wet}}} \approx f_{X_{\text{dry}}} \). The maximum deviation of \( f_x \) with respect to \( f_y \) was calculated to be \( \pm 0.08 \) for \( f_{X_C} \), \( \pm 0.03 \) for \( f_{X_O_2} \), and \( \pm 0.05 \) for \( f_{X_{He}} \).

The procedure for collecting the CO, CO\(_2\), O\(_2\), and THC emissions used to determine \( f_{Y_C} \), \( f_{Y_O} \), \( f_{Y_O_2} \), and \( f_{X_O_2} \) was outlined in refs. 12 and 13. The experimental component in this paper involves the measurement of the helium tracer gas used for calculating \( f_{X_{He}} \) and \( f_{Y_{He}} \).

**Inert Gas Tracer Sampling Protocol**

The injection and sampling train of the helium tracer system is shown in figure 3. Gas samples are extracted from the flow field and drawn through a water-cooled probe with a pump. After condensing water from the sample through an impinger submersed in an ice bath, the gas is sent to a gas chromatograph (HP 5890 Series II) to measure the helium concentration. When a sample analysis is initiated, the volume of gas contained in the 250-\( \mu l \) sample loop of the gas chromatograph is injected into the column, while the balance of the extracted gas is diverted through a flow bypass.

The gas chromatograph setup is optimized to obtain the fastest elution time of the helium tracer gas with acceptable chromatographic separation. In order to separate the helium atoms from the heavier molecules of fuel, air, and combustion products, the sample flows through two columns, connected in series. Both columns, manufactured by J&W Scientific, Inc., are megabore, capillary, gas solid (GS) columns, with an inner diameter of 0.54 mm, and a length of 30 m. Ultra-pure grade hydrogen (99.999% H\(_2\) concentration) is used as the carrier gas in order to minimize the sample elution time, as well as prevent chromatographic interference from H\(_2\) generated from the combustion of fuel-rich mixtures.

Chromatographic separation takes place in two stages. The gas sample is injected into the GS-Q column before flowing through the GS-MolSieve column. The GS-Q column separates hydrocarbon molecules such as methane, ethane, and propane, while the GS-MolSieve column separates compounds of low molecular weight, including helium, neon, oxygen, nitrogen, and carbon monoxide. The effects of the hydrocarbon molecules on the sensitivity of the MolSieve column necessitated the use of timed valve switching. The valve controlling the flow circuitry is switched 30 sec after the helium enters the GS-MolSieve column and interrupts the flow between the GS-Q and GS-MolSieve columns. The carrier gas flow through the GS-Q column is reversed (backflushed) to flush the sample containing the hydrocarbon molecules out of the system, while the helium continues to separate from the remainder of the sample in the GS-MolSieve column as it moves toward the detector.

To detect helium, the gas chromatograph uses a thermal conductivity detector (TCD). The TCD detects the difference in the thermal conductivities of the eluted sample and the carrier gas, generating a differential voltage signal. The output from the TCD is connected to an integrator (Spectra Physics DataJet), which in turn is connected to a computer. The WINner on Windows software package by Thermo Separation Products was used to integrate the resulting chromatograms. From helium calibration runs performed before and after each test, a constant of proportionality is obtained to quantify the integrated areas under the peaks in terms of volumetric concentration.

Completion of the analysis requires approximately 1.5 min, followed by 30 sec to flush out the columns to prepare them for the next sample. The gases elute in the following order: helium at 0.59 min, air at 0.66 min, and CO at 0.74 min.
Results and Discussion

Mixture Fraction

The simplified molar mixture fraction formulations proposed in this paper, namely $f_{\text{XO}_2}$ and $f_{\text{XHe}}$, are plotted in figure 4 and 5 versus $f_{\text{YC}}$ and equivalence ratio $\phi$. Figure 4 also graphs $f_{\text{XC}}$ versus $f_{\text{YC}}$, showing that the molar fraction-based mixture fraction slightly overpredicts $f_{\text{YC}}$ by approximately 5%. The equivalence ratio was calculated from $f_{\text{YC}}$ according to Jones et al. [11] using the following formula:

$$\phi = \frac{\xi}{1-\xi} \left(1 + \frac{Y_{N_2}}{Y_{O_2}}\right) \frac{5M_{O_2}}{M_{C,H_8}}$$  \hspace{1cm} (4)

where

$$\xi = \frac{Y_{\text{sample}}}{Y_{\text{fuel}}}(1-f) \frac{M_{C,H_8}}{M_{\text{crossflow}}}$$  \hspace{1cm} (5)

Figures 4 and 5 include data collected at all the measurement planes for the four test modules. The data are grouped in terms of sampling radius to better explain certain results. Grouping by module type or sampling plane did not yield any identifiable trends. Figures 4 and 5 show that $f_{\text{XO}_2}$ and $f_{\text{XHe}}$ correlate positively with $f_{\text{YC}}$, but they exhibit significant deviations from the carbon-based mixture fraction. Experimental uncertainties for $f_{\text{XHe}}, f_{\text{XO}_2}$, and $f_{\text{YC}}$ are, respectively, ±0.08, ±0.01, and ±0.02. The apparent gap in data points in the region of $0.2 < f < 0.4$, which corresponds to near-stoichiometric combustion, illustrates the staging in RQL combustion that causes the reaction to shift from $\phi = 1.67$ to $\phi = 0.45$ by quick mixing to avoid hot stoichiometric pockets.

In the case of $f_{\text{XO}_2}$, the values underpredict $f_{\text{YC}}$. Two trends are evident in figure 4, one corresponding to combustion equilibrium (predicted by the NASA Equilibrium Code) and the other to jet dilution and quenching of the reaction. The dilution effect is linear in both the slightly rich and slightly lean regimes. Extra scatter in the data around the knee at near-stoichiometric conditions (i.e., for $0.3 < f < 0.5$) indicates non-equilibrium conditions, resulting in higher than equilibrium O2 and CO values. Figure 4 suggests that the deviation occurs away from the walls (i.e., $r = R/3, 2R/3$), from which one can surmise that the non-equilibrium conditions are probably due to the intense, turbulent, quick mix transition from rich to lean conditions following jet injection. Near the edges of the combustor (i.e., $r = R$), where jet interaction is less, equilibrium conditions prevail. Thus, in addition to the usefulness of O2 concentration profiles to track jet trajectories and determine the general zones where reacting and mixing processes are occurring (as shown in ref. 12), one can use O2 to distinguish between the two processes.

As seen in figure 5, the $f_{\text{XHe}}$ data overpredict and show considerable scatter with respect to $f_{\text{YC}}$. The overprediction may be attributed to (a) the higher molecular and turbulent diffusivity of He with respect to the other major products of combustion, and (b) the use of molar fraction rather than mass fraction which can introduce a positive bias of up to 0.05 for high mixture fraction values. The data collected at $r = R$, where, as previously noted, equilibrium conditions hold, appear to correlate well with $f_{\text{YC}}$. However, once the jet interaction is thrust into the picture, the tracer may be unable to follow the high momentum jet trajectories. In ref. 12, it was shown that overpenetrating jets displace the rich reacting fluid towards the walls, while the jet mass migrates.
and accumulates in the central core of the combustor. This is corroborated by the fact that the
flows at $r = 2R/3$ and $R/3$ seem to either completely trap ($f = 0$) or totally exclude ($f = 1$) the He
tracer molecules.

The scatter, on the other hand, may be attributed to a variety of factors, in addition to
experimental uncertainty. The high turbulence at the jet-crossflow interface due to reacting and
mixing processes can cause large spatial-temporal fluctuations and asymmetries in the mixture
fraction. Density differences between He and the other major combustion products can result in
large differences in momentum flows and kinematic eddy viscosities (turbulent momentum
diffusivities), which in turn affects the He transport in the turbulent eddies in the mixing regions.
Previous isothermal experiments used He concentrations of at least 1%, while, in this study, the
concentrations were less than 0.3%. Although these values were chosen to minimize a potential
diluent effect, perhaps, in hindsight, the concentration levels were too low for use in reacting
conditions. Finally, there is the possibility of small offsets in the relative position of the sampling
probe between runs. As a result of the extreme scattering in the He data, this technique would
need further refinement before it would be seen as amenable for reliably determining mixture
fraction.

To better quantify linear correlations between the mixture fraction data, two parameters
were selected: (1) standard errors ($\sigma$), which give the magnitude of typical deviation from the
estimated linear regression line, and (2) coefficients of determination ($R^2$), which represent the
proportion of a data set that can be explained by the linear regression model. These values are
presented in table 4. Thus, $\sigma$ and $R^2$ quantify the data scatter, while the regression curve fit
would quantify the actual agreement between the various mixture fraction formulations. The
statistical analysis confirms the better fit for the $O_2$ data, whose $\sigma$ is on the order of half of that of
the He data. The analysis also shows the He data to be consistently overpredicting $f_{YC}$ by ~10%
and $O_2$ underpredicting $f_{YC}$ also by ~10%.

To better visualize and compare the various scalars, stacked sector plots, presented in figure 6
to 8, were generated to show the evolution of the scalar flow field through the modules in terms
of $f_{YC}$ (reproduced from ref.13), $f_{XO2}$, and $f_{XHe}$. Note that the flow is upward such that the farthest
upstream plane is at the bottom, and the farthest downstream plane is at the top. The $f_{XO2}$ and $f_{XHe}$
results suggest a qualitative match with the $f_{YC}$ data. All plots show uniformity at $x/R = -1$ and
similar trends in jet penetration at $x/R = d/R$.

The ideal, fully-mixed case occurs when the jets mix uniformly with the crossflow. One can
calculate the ideal jet mixture fraction by substituting the jet and crossflow mass fractions, based
on input mass flow rates, into eq. (1) to yield an $f$ of 0.714. The $f_{YC}$ stack plots in figure 6 indicate
that such a region occurs at the plane $x/R = 1$. The $f_{XHe}$ data shown in figure 8 indicate poorer
mixing with most of the downstream flow composed of jet fluid. The $f_{XO2}$ data plotted in figure 7,
on the other hand, suggest only a narrow band of good mixing, but with crossflow fluid still
present in the central and outer rings of the combustor. Both helium and oxygen-based $f$ data
show steeper gradients than their equivalent carbon-based values.

### Spatial Unmixedness

To determine the effectiveness of the tracer gas method in assessing overall mixing, one can
calculate spatial unmixedness $U_S$ based on $f$. $U_S$ is the normalized variance quantifying planar
mixing and is defined by as:

$$U_S = \frac{f_{var}}{f_{avg}} \frac{1}{1 - f_{avg}}$$

(6)
where $f_{var}$ refers to the variance of all $f$'s in a plane that deviate from $f_{avg}$, the area-weighted average jet mixture fraction specific to each plane [28]. $U_S$ values lie between 0 (perfect fuel-air mixing) and 1 (totally unmixed system). Figure 9 reveals that $U_{S,XYC}$ and $U_{S,XHe}$ correlate reasonably well with each other and with $U_{S,YC}$. The same data are plotted versus axial distance $x/R$ in figure 10. At the orifice trailing edge (i.e., where $x/R = d/R$) where all the jet mass is injected, $U_S$ reaches a peak and then decreases downstream as the jets mix with the crossflow. It appears that the procedure of calculating a planar variance and then normalizing the result eliminates some of the scatter and discrepancies seen in the point measurement mixture fraction data (see table 4 for the corresponding $\sigma$ and $R^2$ regression values).

**Comparison of Conserved Scalar Measurement Methodologies**

The quantitative results discussed above warrant a brief discussion of the relative advantages and disadvantages of each technique. The carbon-based method requires several emissions analyzers for simultaneous species measurement, but also permits localized characterization of pollutant emissions, which can then be evaluated with respect to local mixing efficiency. This method is also the most comprehensive technique since all major species are included in the mixture fraction calculation.

The oxygen-based method only uses a single ($O_2$) analyzer, but would require a back calculation to correct for dilution or lean combustion in order to extract the actual local mixture fraction. However, this method appears to be the simplest technique for the rapid characterization of local jet mixture fraction and spatial unmixedness, despite the fact that the effective use of $O_2$ as a passive scalar is predicated on the assumption that $O_2$ is present in only one of the two flows. Both the C-based and $O_2$-based methods allow one to assess the degree of reaction versus mixing occurring between the two streams.

The helium-based method, on the other hand, only provides mixing information and requires the added complication of metering and injecting a tracer gas. However, He-based measurements could serve as simpler diagnostic substitute to quantify mixing in the absence of a full emissions measurement console. Furthermore, this method could be used to independently verify the carbon-based mixture fraction calculations. The gas chromatographic analysis used for He detection could also be configured to measure emissions and helium simultaneously. Hence, using a single sampling system, one could then apply any of the above methods to characterize the mixing field.

If helium or other inert tracer gases are to be used in future experiments to determine mixture fractions, the effect of tracer gas density and diffusivity on its dispersion in the mixing field need to be investigated. It would be useful to determine the linearity of the tracer injection method, since a normalized response curve should be independent of quantity of tracer injected [16]. In addition, the sensitivity and repeatability of the tracer gas analysis system should be improved, for example, by ensuring a constant pressure sample injection and using multipoint calibration for the gas chromatographic analysis. Use of a commercial helium detector, instead of gas chromatography, would also help to overcome sensitivity issues, as well as speeding up the gas analysis.

**Conclusions**

This study investigated the use of passive scalars, namely the carbon atom, the oxygen molecule, and helium (as an inert tracer gas) to quantify jet mixing in a reacting crossflow. The results show that mole fraction $O_2$ and He-based jet mixture fractions correlate positively
but exhibit significant deviations from the mass fraction C-based localized jet mixture fraction. In general, the O$_2$-based mixture fraction underpredicts the C-based mixture fraction due to jet dilution and combustion, with additional discrepancies near $\phi = 1$ due to non-equilibrium conditions in the RQL quick mixing zone. The He tracer, on the other hand, overpredicts the C-based mixture fraction, possibly due to differences in density and diffusivity, and exhibits significant scatter most likely attributable to differences in gas density and turbulent diffusivity. However, the data show a much better quantitative agreement between the O$_2$, He, and C-based methods when assessing planar mixing fields in terms of spatial unmixedness. Although the combustor rig was designed to test RQL combustion, the results of this experiment can potentially be applied more generally as a diagnostic to assess air-fuel mixing in other types of reacting systems.

References

<table>
<thead>
<tr>
<th>Conserve Scalar</th>
<th>Jet mixture fraction ((f)) formula</th>
<th>Known quantities</th>
<th>Unknown quantities</th>
<th>Equations and assumptions</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Y_C), (Y_O)</td>
<td>(f_{Y_C} = 1 - \frac{Y_{\text{sample}}}{Y_{\text{crossflow}}}) (X_{\text{CO},\text{dry}}, X_{\text{CO}<em>2,\text{dry}}, X</em>{\text{O}<em>2,\text{dry}}, X</em>{\text{THC, dry}})</td>
<td>(X_{\text{CO},\text{dry}}, X_{\text{CO}<em>2,\text{dry}}, X</em>{\text{O}<em>2,\text{dry}}, X</em>{\text{THC, dry}})</td>
<td>(X_{\text{CO},\text{wet}}, X_{\text{CO}<em>2,\text{wet}}, X</em>{\text{O}<em>2,\text{wet}}, X</em>{\text{THC, wet}})</td>
<td>1-4) (X_{i,\text{dry}} = \frac{X_{i,\text{wet}}}{1 - X_{i,\text{H}_2,O}}), (i = \text{CO, CO}_2, \text{O}_2, \text{THC})</td>
</tr>
<tr>
<td>(Y_O)</td>
<td>(f_{Y_O} = \frac{Y_{\text{crossflow}} - Y_{\text{sample}}}{Y_{\text{crossflow}} - Y_{\text{jet}}})</td>
<td>(X_{\text{CO},\text{dry}}, X_{\text{CO}<em>2,\text{dry}}, X</em>{\text{O}<em>2,\text{dry}}, X</em>{\text{THC, dry}})</td>
<td>(X_{\text{CO},\text{wet}}, X_{\text{CO}<em>2,\text{wet}}, X</em>{\text{O}<em>2,\text{wet}}, X</em>{\text{THC, wet}})</td>
<td>5) C:H = 3:8</td>
</tr>
<tr>
<td>(Y_{He})</td>
<td>(f_{Y_{He}} = 1 - \frac{Y_{\text{sample}}}{Y_{\text{He}}})</td>
<td>(X_{\text{CO},\text{dry}}, X_{\text{CO}<em>2,\text{dry}}, X</em>{\text{O}<em>2,\text{dry}}, X</em>{\text{THC, dry}})</td>
<td>(X_{\text{CO},\text{wet}}, X_{\text{CO}<em>2,\text{wet}}, X</em>{\text{O}<em>2,\text{wet}}, X</em>{\text{THC, wet}})</td>
<td>6) O:N = 0.209/0.791</td>
</tr>
<tr>
<td>(X_{O_2})</td>
<td>(f_{X_{O_2}} = \frac{X_{\text{sample}}}{X_{\text{O_2}}} = \frac{[O_2]_{\text{sample}}}{20.9%})</td>
<td>(X_{\text{O}_2,\text{dry}})</td>
<td>None</td>
<td>7) (X_{\text{H}<em>2} = 0.65X</em>{\text{CO}})</td>
</tr>
<tr>
<td>(X_{He})</td>
<td>(f_{X_{He}} = 1 - \frac{X_{\text{crossflow}}}{X_{\text{He}}})</td>
<td>(X_{\text{He, dry}})</td>
<td>None</td>
<td>8) (\sum_i X_{i,\text{wet}} = 1)</td>
</tr>
</tbody>
</table>

(1-9) same as above
(10) \(X_{O_2,\text{dry}} = 0\); \(X_{O_2,\text{wet}} = 20.9\%\)
TABLE 2.—KEY PROPERTIES OF SPECIES USED IN THE DETERMINATION OF JET MIXTURE FRACTION

<table>
<thead>
<tr>
<th>Compound</th>
<th>Molar mass, (g/mol)</th>
<th>Maximum concentration, (% dry)</th>
<th>Maximum density, a (g/m³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Air</td>
<td>28.8</td>
<td>100.0</td>
<td>931.7</td>
</tr>
<tr>
<td>CO</td>
<td>12.0</td>
<td>10.0</td>
<td>151.2</td>
</tr>
<tr>
<td>CO₂</td>
<td>44.0</td>
<td>13.2</td>
<td>180.0</td>
</tr>
<tr>
<td>O₂</td>
<td>32.0</td>
<td>20.9</td>
<td>273.5</td>
</tr>
<tr>
<td>C₃H₈</td>
<td>44.1</td>
<td>2.2 b</td>
<td>38.8</td>
</tr>
<tr>
<td>H₂O</td>
<td>34.0</td>
<td>14.8</td>
<td>205.2</td>
</tr>
<tr>
<td>He</td>
<td>4.0</td>
<td>0.3</td>
<td>0.5</td>
</tr>
<tr>
<td>Ne</td>
<td>20.2</td>
<td>0.2</td>
<td>1.9</td>
</tr>
<tr>
<td>Ar</td>
<td>39.9</td>
<td>---</td>
<td>---</td>
</tr>
</tbody>
</table>

aDensity (ρ) is given by $\rho = 100 \cdot \frac{PM}{RT} \cdot C$, where P = 1 atm, T = 298 K, M = molar mass, R = 8.314 J/molK, and C = concentration in %.

bMeasured as total unburned hydrocarbons corrected to propane.
TABLE 3.—OVERALL CONSTITUENT MASS FRACTIONS IN ZONES UPSTREAM AND DOWNSTREAM OF JET MIXING SECTION, BASED ON FLOW RATES OF FUEL, AIR, AND TRACER GAS

<table>
<thead>
<tr>
<th>Zone</th>
<th>Helium</th>
<th>Propane</th>
<th>Air</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Y_{\text{rich}})</td>
<td>(4.4 \times 10^{-4})</td>
<td>0.097</td>
<td>0.90</td>
</tr>
<tr>
<td>(Y_{\text{lean}})</td>
<td>(1.3 \times 10^{-4})</td>
<td>0.028</td>
<td>0.97</td>
</tr>
</tbody>
</table>

\(a_{\text{rich}} = \text{helium} + \text{propane} + \text{air}

\(b_{\text{lean}} = \text{rich} + \text{air jets}\)

TABLE 4.—STANDARD ERROR (\(\sigma\)) AND COEFFICIENTS OF DETERMINATION (\(R^2\)) FOR O2 AND He-BASED MIXTURE FRACTIONS (\(f_X\)) AND SPATIAL UNMIXEDNESS (\(U_S\)) WITH RESPECT TO \(f_{YC}\) AND \(U_{S,YC}\)

<table>
<thead>
<tr>
<th>Parameter</th>
<th>(f_{XO2})</th>
<th>(f_{XHe})</th>
<th>(U_{S,O2})</th>
<th>(U_{S,He})</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\sigma)</td>
<td>0.09</td>
<td>0.12</td>
<td>0.06</td>
<td>0.08</td>
</tr>
<tr>
<td>(R^2)</td>
<td>0.94</td>
<td>0.90</td>
<td>0.96</td>
<td>0.93</td>
</tr>
</tbody>
</table>

\(a_{\text{The \(\sigma\) and \(R^2\) values for jet mixture fraction \(f\) were calculated using all the data obtained for each module, except for points at the upstream plane } x/R = -1 \text{ where } f \text{ is uniform and approximately zero.}\)
Figure 1.—RQL combustor setup.

Figure 2.—Location of planes and sampling points in RQL combustor module.
Figure 3.—Setup of helium injection system, sampling train, and analysis system.

Figure 4.—Comparison between carbon mass fraction-based \( f_{YC} \) and oxygen concentration-based \( f_{XO2} \) jet mixture fractions.
Figure 5.—Comparison between carbon mass fraction-based ($f_{YC}$) and helium concentration-based ($f_{XHe}$) jet mixture fractions.

Figure 6.—Carbon mass fraction-based ($f_{YC}$) mixture fraction fields.
Figure 7.—Oxygen concentration-based \( f_{\text{O}_2} \) mixture fraction fields.

Figure 8.—Helium concentration-based \( f_{\text{He}} \) mixture fraction fields.
Figure 9.—Comparison between carbon mass fraction-based ($U_{S,YC}$), oxygen concentration-based ($U_{S,XO2}$), and helium-concentration based ($U_{S,X,He}$) spatial unmixedness for all modules.

Figure 10.—Spatial unmixedness ($U_S$) values at each measurement plane.
Assessing Jet-Induced Spatial Mixing in a Rich, Reacting Crossflow

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In many advanced low NOx gas turbine combustion techniques, such as rich-burn/quick-mix/lean-burn (RQL), jet mixing in a reacting, hot, fuel-rich crossflow plays an important role in minimizing all pollutant emissions and maximizing combustion efficiency. Assessing the degree of mixing and predicting jet penetration is critical to the optimization of the jet injection design strategy. Different passive scalar quantities, including carbon, oxygen, and helium are compared to quantify mixing in an atmospheric RQL combustion rig under reacting conditions. The results show that the O2-based jet mixture fraction underpredicts the C-based mixture fraction due to jet dilution and combustion, whereas the He tracer overpredicts it possibly due to differences in density and diffusivity. The He-method also exhibits significant scatter in the mixture fraction data that can most likely be attributed to differences in gas density and turbulent diffusivity. The jet mixture fraction data were used to evaluate planar spatial unmixedness, which showed good agreement for all three scalars. This investigation suggests that, with further technique refinement, O2 or a He tracer could be used instead of C to determine the extent of reaction and mixing in an RQL combustor.