Nonlinear Oscillations and Flow of Gas Within Closed and Open Conical Resonators

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ABSTRACT

A dissonant acoustic resonator with a conical shaped cavity was tested in four configurations: (A) baseline resonator with closed ends and no blockage, (B) closed resonator with internal blockage, (C) ventilated resonator with no blockage, and (D) ventilated resonator with an applied pressure differential. These tests were conducted to investigate the effects of blockage and ventilation holes on dynamic pressurization. Additionally, the investigation was to determine the ability of acoustic pressurization to impede flow through the resonator. In each of the configurations studied, the entire resonator was oscillated at the gas resonant frequency while dynamic pressure, static pressure, and temperature of the fluid were measured. In the final configuration, flow through the resonator was recorded for three oscillation conditions. Ambient condition air was used as the working fluid. The baseline results showed a marked reduction in the amplitude of the dynamic pressure waveforms over previously published studies due to the use of air instead of refrigerant as the working fluid. A change in the resonant frequency was recorded when blockages of differing geometries were used in the closed resonator, while acoustic pressure amplitudes were reduced from baseline measurements. A sharp reduction in the amplitude of the acoustic pressure waves was expected and recorded when ventilation ports were added. With elevated pressure applied to one end of the resonator, flow was reduced by oscillating the cavity at the fluid fundamental resonant frequency compared to cases without oscillation and oscillation off-resonance.

INTRODUCTION

The ability to generate high-amplitude pressure waveforms within acoustic resonators has been shown to be highly dependent upon the shape of the cavity. Researchers have investigated closed resonators of cylindrical, conical, horn-cone, and bulb shape with the interest of their application to refrigeration systems. Their research focused on using R-134a refrigerant as the working fluid and has shown generated pressures exceeding four times that of the ambient fluid at rest. They have shown that high-amplitude pressure generation can be applied to acoustic pumps, compressors, and thermal management of electronics. The purpose of this work is to determine whether acoustic pressurization can be used to control or even restrict flow. If possible, this would be the first step toward developing acoustic-based seals.

The study presented herein seeks to evaluate the effects of seal-like features such as central blockages (e.g. shafts), end cap openings (e.g. seal clearances), and pressure differentials on acoustic pressurization. Additional features were added to the baseline resonator investigated to determine the effects of the modifications. In one configuration, a centrally located cylindrical blockage was added to the interior of the resonator for added structural support. Another resonator configuration tested was a modification of the closed resonator to an open resonator with the addition of orifices to each of the two flat ends of the resonator. The final configuration aims to show that the flow of gas through the resonator can be reduced under certain conditions. The objective of this study was to investigate the effects of blockage and ventilation holes on the dynamic pressurization and to investigate the ability of acoustic pressurization to impede flow through a resonator at fluid resonance condition.

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EXPERIMENTAL APPARATUS

A. Resonator Test Section
The resonating cavity used in this study had a conical shape, having shape characteristics shown in Figure 1, and was fabricated from aluminum alloy 7075-T6 with a 0.36 cm (0.14 inch) side wall thickness. End caps were machined from the same material and had minimum thickness of 0.25 cm (0.098 inch). A composite illustration of the resonator supporting the four configurations tested is shown in Figure 2.

1. Baseline Configuration
The baseline experimental configuration (referred to as configuration A) consisted of a sealed conical resonator cavity, free from internal obstructions. The total mass of the test section was 4.08 lbm (1850.7 g).

2. Conical Resonator With Internal Blockage
This test section configuration was identical to the baseline configuration except for the addition of a centrally located cylindrical blockage internal to the resonating cavity, referred to as configuration B in Figure 2. Four different diameter cylinders were individually tested. Each cylinder was manufactured from aluminum alloy 7075-T651 to diameters of 0.403, 0.423, 0.433, and 0.443 inch (1.02, 1.07, 1.10, and 1.13 cm) and had masses between 0.0843 lbm (38.3 g) and 0.101 lbm (45.8 g). The cylinders were mounted inside the resonators with the use of a clearance pilots in the two end caps. The cylinders were manufactured to a length equal to the resonator plus 0.016 inch (0.406 mm) to prevent axial movement within the resonator during testing.

3. Conical Resonator With Ventilation Orifices
For this configuration, referred to as configuration C in Figure 2, holes were made in the resonator end caps for ventilation of the otherwise sealed conical resonator. One orifice, 0.102 inch (0.259 cm) in diameter, was made in the end cap covering the wide end of the resonator. Eight holes of 0.025 inch (0.635 mm) diameter were drilled on a 0.418 inch (1.06 cm) diameter bore circle on the narrow end cap. Therefore, the total cross-sectional area of the holes at the wide end of the resonator was 2.0 times the area of the holes at the narrow end of the resonator. The holes in the end caps of the resonator served to ventilate the resonator to the ambient laboratory air. The resonator test section was otherwise free from obstruction.

The same conical resonator hardware with ventilation orifices was used to determine if flow through the cavity could be reduced. The only modification to the previous setup was metered, pressurized air was applied to the plenum attached to the narrow end of the conical resonator, (referred to as configuration D in Figure 2). The plenum cavity was cylindrical in shape, (1.25 inch (3.18 cm) diameter, 2.49 inch length (6.32 cm)). In this configuration, no blockages were internal to the resonator.

B. Shaker Table
An electrodynamic shaker system was used to oscillate the acoustic resonators at the frequencies of interest. The resonators were mounted to the shaker table in order to excite the gas contained in the cavity. A PC-based data acquisition and control system supplied a 0 to 5 Volt sinusoidal voltage to the shaker system’s amplifier. The amplifier output signal excited the electrodynamic shaker table to produce a near sinusoidal acceleration of 0 to 100 times that of gravity.

C. Data Acquisition and Control System
Both the control of the shaker table oscillation and acquisition of data were completed using a single PC-based program. The oscillation of the shaker table was controlled within 0.001 Hz. The control system was capable of operating in two modes. In the first mode, the frequency of oscillation was swept between a minimum and maximum frequency with discrete frequency steps (generally 1 Hz or less). The second mode of operation was used to lock on a phase difference between the acceleration and narrow end dynamic pressure signals. This second mode was useful when loitering on the resonant frequency, since the temperature of the gas changed and caused the resonant frequency to shift upward with the speed of sound.

The PC-based system also collected all the temperature, acceleration, static and dynamic pressure measurements. The data was sampled at a rate of 1.25 million samples per second in 12-bit operation. The system was capable of collecting data either on command (when loitering on the resonant frequency) or automatically (when control was in frequency sweep mode).

D. Instrumentation
Piezoelectric accelerometers were mounted on the test section and used quartz crystal sensing elements to measure the instantaneous acceleration of the resonator body. The acceleration amplitudes noted in the results section are one half the peak-to-peak measurements of this sensor. Since the acceleration amplitude was controlled manually using the shaker table amplifier, these measurements were accurate to approximately 5% over the course of a test case.
The dynamic pressure magnitudes of the acoustic waveforms were recorded using acceleration compensated piezoelectric pressure sensors. The sensors were mounted so as not to protrude into the resonator cavity and disrupt the generated planar waves.

Mounted through the side wall at both the narrow and wide ends, each resonator was instrumented with K-type thermocouples and orifices for static pressure measurements. Care was taken in sizing the length and diameter of the pressure tube between the resonator and the static pressure transducer; the tubes were sized small enough to acoustically filter out the AC-component of the pressure wave, but large enough to capture the rapid changes in the DC-component of static pressure. The orifices diameters were 0.004 inch (0.102 mm) on the wide end and 0.030 inch (0.762 mm) on the narrow end of the resonator.

For the last resonator configuration investigated, conical resonator with \( \Delta p \) applied, a 200 SLPM capacity flow meter was attached to the air line supplying the plenum and measured the rate of air flowing through the test section. The error of the measurements for this instrument was calibrated to be less than 1% of full scale in the range of interest.

RESULTS

To facilitate comparisons between resonators and between experimental data sets, all of the results are presented in dimensionless form. Since the processes presented by the authors are sensitive to slight variations in fluid static pressure and temperature, the subtle variation in the results would be masked without non-dimensional transformation. The graph axes are

\[
\frac{p}{p_0}, \tau, \frac{p_{\text{MAX}}}{p_0}, \Omega,
\]

where \( p \) is the total (static plus dynamic) pressure in absolute terms, \( p_{\text{MAX}} \) is the maximum total pressure recorded during a cycle, \( p_0 \) is the average absolute static pressure of the gas in the non-oscillating resonator before and after the sample was taken. \( \Omega \) and \( \tau \) are dimensionless frequency and time respectively. The dimensionless variables are defined by

\[
\Omega = \frac{2 \cdot f \cdot l}{8314 \cdot \gamma \cdot T_K \cdot MW}
\]

and

\[
\tau = \frac{f \cdot t}{2\pi}
\]

where \( f \) is the frequency of oscillation, \( l \) is the length of the resonator, \( \gamma \) is the specific heat ratio of the gas (1.4 for air), \( T_K \) is the absolute temperature, \( MW \) is the average gas molecular weight (28.964 kg/kmol for air), and \( t \) is the time.

A. Baseline Configuration

The baseline resonator was assembled as shown in Figure 2 (configuration A) with the narrow end mounted towards the shaker table. In this configuration, higher acceleration amplitudes were achieved by taking advantage of the compliance of the shaker table mounting hardware. The test section was oscillated at acceleration amplitudes of 20, 40, 60, and 80 times that of gravity, as measured by the narrow end accelerometer. For each of the acceleration amplitudes, measurements were taken while sweeping oscillation frequencies from below to above fluid resonance in 0.5 Hz increments. At the highest acceleration amplitude, additional data was collected while decreasing oscillation frequency from above to below resonance.

At frequency increments of 0.5 Hz, the maximum dimensionless pressures recorded at the narrow end of the resonator are plotted in Figure 3. The sweep of frequencies were taken quickly enough as to minimize the amount of heat added to the fluid and therefore minimize the sound speed change, but slowly enough to minimize the effects of transients. The most notable transient was the amount of time required to take static pressure measurement through the acoustic filter orifice. For each of the acceleration amplitudes tested, the maximum pressure rises as the resonant frequency of the fluid is approached. The nonlinear behavior is evident as the resonant frequency shifts upward with increasing acceleration amplitude. At the highest acceleration amplitude, hysteresis is apparent as the resonant frequency is different between incrementally increasing and decreasing.

Figure 4 shows the pressure waveforms at the narrow and wide ends of the resonator. Additionally, the static pressure at the narrow end of the resonator is shown in comparison to the static pressure without oscillation \( (p/p_0 = 1.0) \). The peak-to-peak pressure is larger at the narrow end of the cone resonator than at the wide end. The narrow end pressure waveform is smooth and shows no signs of microshocks. The presence of microshocks would indicate that energy is being dissipated.
From an original gas temperature of 27.5 °C, a rise in the mean temperature of ~2.9 °C was recorded between before and after the 80 g sweep of frequencies plotted in Figure 3. Additionally, differences between air temperatures at each end of the cone resonator were also observed. At the same time the data plotted in Figure 4 was recorded, the gas temperatures at the narrow and wide ends of the conical resonator were 31.0 °C and 29.2 °C, respectively.

When resonator oscillation frequency approached the fluid resonance, the phase angle between the acceleration and narrow end pressure signals changed rapidly. Figure 5 shows the variation in phase angle during a sweep of frequency at 60 g acceleration amplitude. The phase angle at peak pressure was 95.3 degrees, but was rapidly dropping before and after the resonant frequency was approached. The data acquisition and control system was capable of holding this phase angle and would therefore maintain the resonant frequency as the input energy would raise the gas temperature thereby increasing the value of resonant frequency.

Upon comparison to the previously published results of Lawrenson et al., several differences were observed. Lawrenson reported that minimal working fluid heating occurred, so that resonant frequency changes were kept below 0.1%. Our results indicated that fluid heating was significant and such heating would increase the speed of sound 1% during a typical test cycle. This change in the speed of sound would produce a 13 Hz increase in the resonant frequency, necessitating the non-dimensionalization of the results for comparison.

The hysteresis observed in both the Lawrenson results and the results presented here was approximately the same. The multi-valued frequency response overlaps 4.5 Hz in Figure 3, whereas Lawrenson’s results present an approximate 4.6 Hz overlap.

Originally the resonator was equipped with a 0.004 inch (0.102 mm) orifice connecting the working fluid to the static pressure transducer at both ends of the resonator. Since rapid changes in static pressure were recorded at the narrow end of the cone resonator, and these rapid changes required significant amount of time to allow the static pressure transients to reach steady state, the orifice was enlarged to 0.030 inch (0.76 mm). This allowed for the incremental changes in frequency to occur more rapidly, minimizing the heat addition to the working gas.

**B. Conical Resonator With Internal Blockage**

The oscillated test section, shown in Figure 2 (configuration B), was identical to the baseline configuration except for the addition of an internal blockage. The blockage was cylindrical in cross-section with constant diameter at all axial locations. It was fixed within the resonator cavity and could not vibrate undesirably. Four blockages were evaluated having diameters of 0.403, 0.423, 0.433, and 0.443 inch (1.02, 1.07, 1.10, and 1.13 cm).

For each of the configurations, the oscillation frequency was increased incrementally in 0.5Hz steps until the resonant gas frequency was bounded. Figure 6 shows the frequency response of the gas pressure in the narrow end of the conical resonator. Each of the curves is similar in characteristics. The pressure is single valued at all frequencies indicating no hysteresis was present, though the curves leaned towards higher frequencies demonstrating mild hardening.

The resonant frequency tended to increase with increased blockage diameter. Increased blockage diameter also reduced the maximum pressure obtained from 1.20 to 1.17 by increasing the blockage diameter from 0.403 to 0.443 inch (1.02 to 1.13 cm) respectively. The reduction in the maximum pressure can be theoretically linked to the increased thermal and viscous losses caused by the increased surface area of the larger diameter blockages. However, the addition of the larger diameter blockages is more likely further away from the optimum resonator shape in the design space and is being studied further.

**C. Conical resonator with ventilation orifices**

The otherwise closed resonator was opened with the addition of orifices in the resonator end caps, (Figure 2, configuration C). This modification, though minor, had a strong impact on the ability to generate high-amplitude standing waves. The frequency response curve in these conditions is shown in Figure 7 along with the results from the closed resonator experiments. The resonant frequency is similar to that of the closed resonator without internal blockages, but the maximum amplitude of the pressure waves is reduced 75%. The acoustics are considered non-linear even at this reduced pressure amplitudes as the pressures exceeded 10% overpressure.

**D. Conical Resonator With Ap Applied**

In the final configuration, tests were performed to determine whether the acoustic pressurization could reduce flow through the resonator. As shown in Figure 2 (configuration D), metered pressurized air was supplied to the plenum chamber while the pressure drop between the plenum and ambient pressure was measured. To determine a baseline condition, the flow rates were measured at different values of plenum pressurization without oscillating the test section.
A plot of the pressure differential ($\Delta p$) between the plenum and the ambient conditions against the flow rate of air though the resonator is shown in Figure 8 as the baseline measurements.

In addition to the baseline measurements taken without resonator oscillations, the test section was oscillated at two frequencies. One frequency corresponded to the fundamental resonant frequency of the gas contained within the resonator. The second frequency was approximately 50 Hz (or 4%) lower than the resonant frequency. The flow rate data from each of these conditions is also plotted in Figure 8.

Oscillation of the resonator test section at the resonant frequency reduced the amount of air flowing through the resonator by 5 to 58% over the differential pressure range investigated, whereas non-resonant oscillations failed to impede the air flow. To confirm this result was a real effect, the apparatus was disassembled and reassembled and the flow resisting behavior was repeated. Note from Figure 8, that when test off-resonance, the flow behavior was identical to the no oscillation case. This is the first known application of non-linear acoustic excitation to restrict flow between high and low pressure cavities. This finding sets the stage for future development of an acoustic-based seal.

**CONCLUSIONS**

The use of air as the working fluid reduced the magnitude of the pressure waveforms from those reported by other researchers. The addition of axisymmetric cylindrical blockage to the resonating cavity increased the gas resonant frequency while significantly reducing the acoustic pressures generated. An additional reduction in the generated pressure range was observed when the resonator configuration was modified from closed to ventilated. However, when applying a pressure differential across the resonator, the flow of gas was restricted when the cavity oscillation was at the fundamental acoustic resonance frequency as compared to the off-resonance condition. This finding indicated that it is indeed possible to restrict flow using acoustic pressurization and demonstrates initial feasibility for the development of an acoustic-based seal.

**REFERENCES**


For $0 \leq z \leq 0.17$ [m],
\[
r(z) = 0.0056 + 0.268 \cdot z \text{ [m]}
\]

Figure 1. Contour of the conical resonator.

Figure 2. Schematic of the acoustic resonator test section in configurations A (closed resonator without blockage), B (closed resonator with blockage), C (open resonator without blockage), and D (open resonator without blockage with pressurized plenum).
Figure 3. Graph showing the changes in maximum pressure amplitude with varying frequency for a closed conical resonator filled with ambient pressure air at maximum accelerations of 20, 40, 60, and 80 times that of gravity.

Figure 4. Graph showing the pressure waveforms at the wide and narrow ends of a closed conical resonator filled with ambient pressure air at maximum acceleration of 80 times that of gravity.
Figure 5. Variation of phase angle (between narrow end acceleration and pressure signals) with frequency and measured narrow end pressure in a closed resonator oscillated at 60 g acceleration amplitude.

Figure 6. Graph showing the changes in maximum pressure amplitude with frequency for a closed conical resonator with various diameter cylindrical blockages ($\phi$0.403 inch (1.02 cm), $\phi$0.423 inch (1.07 cm), $\phi$0.433 inch (1.10 cm), and $\phi$0.443 inch (1.13 cm)) filled with ambient pressure air at maximum acceleration 80 times that of gravity.
Figure 7. Comparison of the maximum pressure amplitudes between a closed conical resonator with and without cylindrical blockage filled with ambient pressure air at maximum acceleration 80 times that of gravity.

Figure 8. Flow rate through an open conical resonator and the effect of no oscillation, off-resonance oscillation, and on-resonance oscillation of the cavity.
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