Nonlinear Flutter Aspects of the Flexible HSCT Semispan Model

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The nonlinear aspects that lead to the flutter of an HSCT Flexible Semispan Model are analyzed. A hierarchy of spectral moments was used to determine the characteristics of the aerodynamic loading and structural strains and motions. The results show that the frequency of the bending motion of the wing varied significantly as the Mach number was increased between 0.90 and 0.97. Examination of the pressure coefficients in terms of mean value and fluctuations showed that the flow characteristics over the wing changed significantly around a Mach number of 0.97. A strong shock was identified near the trailing edge. Nonlinear analysis of the pressure fluctuations, under these conditions, showed nonlinear coupling involving low-frequency components at pressure locations where the mean value was at a local minimum. This shows that the aerodynamic forces acting on the model had nonlinearly coupled frequency components. The results presented here show how nonlinear analysis tools can be used to identify nonlinear aspects of the flutter phenomenon which are needed in the validation of nonlinear computational methodologies.

Keywords: Nonlinear aeroelasticity, Flutter, Bispectrum.

Introduction

Flutter instabilities encountered in flight into or through the transonic regime can cause significant motions, damage or loss of the aircraft. Because of the complexities involved in the aerodynamic and structural aspects of the flutter phenomenon, the prediction of its boundaries is extremely difficult. Predictions based on linear models do not take into consideration complex aspects such as flow separation, shock formation, large structural deformations, or nonlinear coupling between the fluid flow and the structural motions. On the other hand, any methodology proposed for modeling nonlinear aerodynamic and structural aspects of flutter phenomena need to be validated. Considering the current limitations of computing power and technologies, one has to assess the viability of using inviscid or viscous codes with different turbulence models, the number of degrees of freedom and the forms of the structural operators.

The issues, presented above, point to the need for identification of nonlinear aspects of flutter. Such identification can be used as a benchmark for validation of nonlinear computational codes and methodologies against experimental data. Additionally, it would allow for determination of optimal measurements for prediction of onset of aeroelastic instabilities, would assist in the development of reduced-order models and would provide effective means for obtaining improved performance with reduced uncertainties through operation beyond boundaries based on linear analysis.

The goal of this effort is to identify nonlinear aspects that lead to the flutter of an HSCT (High Speed Civil Transport) Flexible Semispan Model (FSM) in experiments conducted at the NASA Langley Research Center (LaRC). The high amplitude responses observed in these experiments in different regions and with different characteristics present a unique opportunity for determining nonlinear aspects of the flutter mechanism of this configuration. Of particular interest for this work is a high dynamic response region which occurred over a large range of dynamic pressures around a Mach number of 0.98. At the top of this region is a "hard" flutter point that resulted in the loss of the model. The characteristics of the aerodynamic loading
and structural strains and motions, as the "hard" flutter is encountered, are determined through analysis of pressure, strain and acceleration data. The nonlinear aspects are identified by using higher-order spectral moments. The use of these moments to investigate limit cycle responses observed on fighter aircraft has been also proposed by Stearman et al.\(^1\)

**Experimental Setup**

The FSM experiments were conducted in the Langley Transonic Dynamics Tunnel (TDT) at the NASA LaRC. The TDT is a closed-circuit, continuous-flow, variable-pressure, wind tunnel with a 16-foot square test section with cropped corners. The tunnel uses either air or a heavy gas as the test medium, can operate at stagnation pressures from near vacuum to atmospheric, and has a Mach number range from near zero to 1.2 and is capable of maximum Reynolds numbers of about 3 million per foot in air and 10 million per foot in heavy gas. The tests, analyzed here, were conducted in the spring of 1996 with dichlorodifluoromethane, R-12, as the test medium. Since 1998, 1,1,1,2 tetrafluoroethane, R-134a, has been used as the test medium instead of R-12. The TDT is specially configured for flutter testing, with excellent model visibility from the control room and a rapid tunnel shutdown capability for model safety (bypass valves).

The model planform\(^2\) was a 1/12th scale configuration based on an early design known as the Reference H configuration. In order to accommodate pressure instrumentation at the wing tip of the model, the original Reference H airfoil thickness was increased to a constant four-percent thickness over the entire wing span. Figure 1 shows the planform layout and main components of the model. The leading and trailing edges were removable in order to access pressure instrumentation in those regions. A removable tip cap allowed access to pressure instrumentation at the wing tip. It should be noted that the FSM was not intended to be a flutter clearance model but, rather, a model that would exhibit an HSCT-like flutter mechanism within the range of operation of the TDT. As such, and in order to induce flutter at around 200 psf, a 2.2 lb. mass was added to the aft tip section. This mass was fabricated out of tungsten and bonded into the outboard removable trailing-edge section of the FSM (see Figure 1). Additional reinforcements and local strengthening of the attachment surface between the main wing box and the outboard removable trailing-edge section was performed in order to handle the added stress of the additional mass.

The instrumentation layout consisted of 131 in situ unsteady pressure transducers located at the 10, 30, 60, and 95% span stations (Figure 1). Six additional unsteady pressure transducers were installed at the 20% chord station for the 20, 45, and 75% span stations for both upper and lower surfaces. Channels were carved into the foam core to accommodate the wiring for the instrumentation. Specially designed pressure transducer holders were used to eliminate any leakage around the transducer and to provide easy access to the transducers. Instrumentation also included 14 accelerometers installed throughout the wing (Figure 1). The FSM was instrumented with three bending strain gages and one torsion strain gage. All gages were located at mid-span, a region of high stress concentrations. One bending strain gage was placed near the leading edge and will be referred to as the forward strain gage or FWD. Another was placed near the trailing edge and will be referred to as the aft strain gage or AFT. The third was placed at mid-chord and will be referred to as the middle strain gage or MID. The torsion strain gage was placed at mid-chord.

**Data Analysis**

The aerodynamic and structural aspects of the flutter phenomenon are determined via a frequency domain analysis that is based on a hierarchy of spectral moments. The power spectrum is used to determine the distribution of power among the frequency components in the pressure, strain and acceleration data. The cross-power spectrum, its normalized value, the linear coherence, and the phase relation of the same frequency components between different signals are used to characterize the bending and torsion characteristics of the model. The nonlinear aspects of the aerodynamic loading are determined from estimates of higher-order spectral moments, namely, the auto- and cross-bispectrum. For a discrete, stationary, real-valued, zero-mean process, the auto-bispectrum is estimated as\(^3\)

$$
\hat{B}_{xx}[l_1,l_2] = \frac{1}{M} \sum_{k=1}^{M} \left| X_T^{(k)}[l_1 + l_2] X_T^{(k)}[l_1] X_T^{(k)}[l_2] \right|^2
$$

(1)
where \( X_T^{(k)}[l] \) is the Discrete Fourier Transform of the \( k^{th} \) ensemble of the time series \( x(t) \) taken over a time \( T \) and \( M \) is the number of these ensembles. The auto-bispectrum of a signal is a two-dimensional function of frequency and is generally complex-valued. In averaging over many ensembles, the magnitude of the auto-bispectrum will be determined by the presence of a phase relationship among sets of the frequency components at \( l_1, l_2 \), and \( l_1 + l_2 \). If there is a random phase relationship among these three components, the auto-bispectrum will average to a very small value. Should there be any phase relationship among these frequency components, the corresponding auto-bispectrum will average to a very small value. Should there be any phase relationship among the different frequency components in two signals because of its phase-preserving effect.

Similarly to defining the auto-bicoherence, one can define a normalized cross-bispectrum to quantify the level of quadratic coupling in two signals. This normalized value is called the cross-bicoherence and is defined as

\[
b_{yxx}^2[l_1, l_2] = \frac{1}{\sqrt{M}} \sum_{k=1}^{M} \left| y^{(k)}[l_1 + l_2] X_T^{(k)}[l_1] X_T^{(k)}[l_2] \right|^2 \frac{1}{\sqrt{M}} \sum_{k=1}^{M} X_T^{(k)}[l_1 + l_2]^2
\]

(2)

By Schwarz inequality, the value of \( b_{yxx}^2[l_1, l_2] \) varies between zero and one. If there is no phase relationship among the frequency components at \( l_1, l_2 \), and \( l_1 + l_2 \), the value of the auto-bicoherence will be near zero. If there is a phase relationship among the frequency components at \( l_1, l_2 \), and \( l_1 + l_2 \), then the value of the auto-bicoherence will be near unity. Values of the auto-bicoherence between zero and one indicate partial quadratic coupling.

For systems where multiple signals are considered, detection of nonlinearities can be achieved by using the cross-spectral moments. For two signals \( x(t) \) and \( y(t) \), their cross-bispectral density function is estimated as

\[
B_{yxx}[l_1, l_2] = \frac{1}{M} \sum_{k=1}^{M} \left| Y_T^{(k)}[l_1 + l_2] X_T^{(k)}[l_1] X_T^{(k)}[l_2] \right|^2
\]

(3)

where \( X_T^{(k)}[l] \) and \( Y_T^{(k)}[l] \) are the Discrete Fourier Transforms of the \( k^{th} \) ensemble of the time series \( x(t) \) and \( y(t) \), respectively and that are taken over a time \( T \). The cross-bispectrum, as defined in equation (3), provides a measure of the nonlinear relation among frequency components at \( l_1 \) and \( l_2 \) in \( x(t) \) and their sum frequency component \( l_1 + l_2 \) in \( y(t) \). Similar to the auto-bispectrum, the cross-bispectrum of signals \( x(t) \) and \( y(t) \) is a two-dimensional function in frequency and is generally complex-valued. In averaging over many ensembles, the magnitude of the cross-bispectrum will also be determined by the presence of a phase relationship among sets of the frequency components at \( l_1, l_2 \), and \( l_1 + l_2 \). If there is a random phase relationship among the three components, the cross-bispectrum will average to a very small value. Should there be any phase relationship among these frequency components, the corresponding cross-bispectral value will have a large magnitude. The cross-bispectrum is then able to detect nonlinear phase coupling among different frequency components in two signals because of its phase-preserving effect.
Table 1 Run Numbers and Test Conditions.

<table>
<thead>
<tr>
<th>Run#</th>
<th>Mach Number</th>
<th>Dynamic Pressure (psf)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1062</td>
<td>0.922</td>
<td>226.58</td>
</tr>
<tr>
<td>1063</td>
<td>0.933</td>
<td>230.23</td>
</tr>
<tr>
<td>1064</td>
<td>0.940</td>
<td>232.83</td>
</tr>
<tr>
<td>1065</td>
<td>0.950</td>
<td>236.00</td>
</tr>
<tr>
<td>1066</td>
<td>0.962</td>
<td>240.11</td>
</tr>
<tr>
<td>1067</td>
<td>0.967</td>
<td>245.80</td>
</tr>
<tr>
<td>model lost</td>
<td>0.979</td>
<td>249.60</td>
</tr>
</tbody>
</table>

![Graph showing Mach Number vs. Dynamic Pressure](image)

Fig. 2 Summary of the flutter and high dynamic response regions for the FSM wind-tunnel model.

The forward gage is at 14.6 Hz with significant peaks at 12.7 and 5.4 Hz. On the other hand, the highest peak in middle and aft gages is at 12.2 Hz with significant peaks at 5.4 Hz and 12.7 Hz. As flutter is approached, in Run 1067, the spectra of the forward gage has one significant peak near 14.2 Hz with a relatively smaller one at 12.7 Hz. The peak in the spectra of the middle and aft gages is at 12.7 Hz. Additionally, one difference must be stressed. The spectra in Run 1067 shows significantly higher levels at the lowest measured frequency, 0.5 Hz.

In summary, the analysis of the response of the strain gages shows a frequency around 12.7 Hz which is associated with a torsion mode. The bending frequency decreased as the Mach number was increased between 0.9 and 0.96. Around a Mach number of 0.97, however, this frequency increased. As will be discussed below, this variation in the frequency is mostly due to changing flow characteristics.

To aid in the analysis of the results obtained with the power spectrum, cross-power spectra between the three gages were obtained. The level of coherence along with the phase difference between peak frequency components are shown in Table 2. The results clearly show that the low-frequency peaks are highly coherent in all runs with near zero phase difference. This indicates that these peaks represent a bending motion. As for the 12.7 Hz, which is present in all spectra, the results show improved level of coherence as flutter is approached. Additionally, the results show a phase difference between the three gages which agrees with the argument that the 12.7 Hz represents a torsional motion which becomes highly coherent as flutter is approached. As for the 14.2 Hz peak that appears in the forward strain gage in Run 1067, the results show high level of coherence with the other gages with...
Table 2  Phase Difference and Coherence between SG peaks.

<table>
<thead>
<tr>
<th>Run</th>
<th>Peaks (Hz)</th>
<th>Phase Difference (rad)</th>
<th>Coherence</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>FWD-MID</td>
<td>MID-AFT</td>
</tr>
<tr>
<td>1062</td>
<td>12.7</td>
<td>2.00</td>
<td>0.34</td>
</tr>
<tr>
<td></td>
<td>15.0</td>
<td>0.13</td>
<td>0.49</td>
</tr>
<tr>
<td></td>
<td>17.5</td>
<td>-0.15</td>
<td>-0.12</td>
</tr>
<tr>
<td>1063</td>
<td>7.8</td>
<td>-0.03</td>
<td>0.03</td>
</tr>
<tr>
<td></td>
<td>10.2</td>
<td>0.02</td>
<td>0.12</td>
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<tr>
<td></td>
<td>12.7</td>
<td>1.28</td>
<td>0.64</td>
</tr>
<tr>
<td>1064</td>
<td>7.8</td>
<td>-0.003</td>
<td>0.06</td>
</tr>
<tr>
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<td>12.7</td>
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<td>2.77</td>
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<tr>
<td></td>
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</tr>
<tr>
<td></td>
<td>12.7</td>
<td>1.38</td>
<td>2.34</td>
</tr>
<tr>
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<td>0.07</td>
<td>0.16</td>
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<tr>
<td></td>
<td>12.7</td>
<td>1.67</td>
<td>2.16</td>
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<tr>
<td></td>
<td>14.6</td>
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<td>2.37</td>
</tr>
<tr>
<td>1067</td>
<td>12.7</td>
<td>2.26</td>
<td>2.60</td>
</tr>
<tr>
<td></td>
<td>14.2</td>
<td>0.67</td>
<td>2.92</td>
</tr>
</tbody>
</table>

Fig. 4  Power spectra of the forward, middle and aft bending strain gages.

Fig. 5  Power spectra of the leading edge, middle and trailing edge accelerometers.

a phase difference. Examining the mode shapes of the wing shows that this mode is close to one of the wind-off modes of the FSM.

Motion Characterization with Accelerometers

Spectra of the accelerations of the wing tip are shown in Figure 5. The results show that the wing tip accelerations in the middle and near the leading and trailing edges have a peak of about 12.7 Hz. Moreover, there is no indication of the decrease in the frequency of the wing bending observed in the spectra of the strain gages. It should also be noted that the spectra of the accelerations do not show distinctive effects that identify any variations as the flutter boundary is crossed.

Surface Loads and Aerodynamic Characterization with Pressure Transducers

Mean values of the pressure coefficients, $C_p$, at the 95% and 60% span stations along the chord on both upper and lower surfaces of the wing are shown in Figure 6. The results show a small decrease in the pressure coefficient at different chord locations as the Mach number is increased. This is especially true on the upper surface. Moreover, at specific locations, such as $x/c = 30\%$ and 80% along the 95% span and $x/c = 55\%$ and 85% along the 60% span, there is a local increase, in absolute sense, in the pressure coefficient along the chord. This increase could result from different flow effects; one of which is the formation of shocks on the surface of the wing. In particular, we note the large increase in mean pressure around the 80% chord.
location on both surfaces in Run 1067. This large increase in pressure is most likely due to the formation of a strong shock near the trailing edge.

Figures 7 and 8 show the power spectra at specific chord locations along the 60% span. These locations were chosen because they either have a low mean pressure coefficient or they are near the trailing edge in the region after the shock. Of interest in both figures is the fact that, except in Run 1067, the peaks in the spectra at all locations are at frequencies that correspond to the bending oscillations of the model. As for Run 1067, the largest peak is a band of low frequencies. This clearly indicates a change in the flow character in Run 1067 when compared to the other runs. This change is most likely due to the formation of the shock as could be deduced from Figure 6. Spectra at similar locations along the 95% span are shown in Figures 9 and 10. As in the spectra along the 60% span, the results show high energy in the low frequency components in Run 1067 which is not observed in the other runs.

Further insight into the origin and role of the low frequency components observed in the pressure spectra of Run 1067 can be obtained from the auto-bispectra of the pressure fluctuations on the upper surface at $x/c=0.55$ at the 60% span and at $x/c=0.80$ at the 95% span which are shown in Figure 11. At $x/c=0.80$, the results show a high level of nonlinear coupling between the 0.5 Hz and the region between 3.0 and 11.0 Hz. This nonlinear coupling has its origin in the flow field and implies that flow structures with these frequencies are coupled. On the other hand, there is no notion of coupling between the 0.5 Hz component and the frequency components observed in the strain gage measurements, namely 12.7 and 14.2 Hz. This indicates that the detected nonlinear effects in the pressure data at these locations are aerodynamic in nature. The

auto-bispectrum at $x/c=0.55$ at the 60% span station shows self coupling at the 0.5 Hz. Estimates of the auto-bispectrum at other pressure taps did not show nonlinear coupling at the same levels observed in these taps. Yet, it is important to note that these taps are at locations where the pressure coefficients are relatively large, in absolute sense.

The extent of nonlinear coupling between frequency components at both pressure taps are determined with the cross-bicoherence which is shown in Figure 12. The results show that the 0.5 Hz component at $x/c=0.55$ at the 60% span station is coupled with several components at $x/c=0.80$ at the 95% span station. This shows that pressure forces acting at these
Fig. 9 Power spectra of the pressure fluctuations along 95% span at specified chord locations on the upper surface

Fig. 10 Power spectra of the pressure fluctuations along 95% span at specified chord locations on the lower surface

locations contain nonlinearly coupled frequency components. The importance of these results lies in the fact that this nonlinearity, involving the low frequency components, was only observed in Run 1067, as the flutter point is approached, and is associated with the formation of the shock. Moreover, this gives insight into the origin of the low-frequency component observed in the strain gages in Run 1067, see Figure 4.

Conclusions

In this work, flutter aspects that lead to the structural failure of an HSCT Flexible Semispan Model were analyzed. Spectral analysis was used to determine the characteristics of the aerodynamic loading and structural strains and motions. In particular, higher-order spectral moments, namely the auto- and cross-bispectrum, were used to identify nonlinear aspects of this flutter phenomenon. The results show important and new insights. The frequency of the bending motion of the wing decreased continuously as the Mach number was increased between 0.90 and 0.96. Around a Mach number of 0.97, this frequency increased. Examination of the pressure coefficients in terms of mean value and fluctuations showed that the flow characteristics over the wing changed significantly around a Mach number of 0.97. A strong shock was identified near the trailing edge. Nonlinear analysis of the pressure fluctuations, under these conditions, showed nonlinear coupling involving low-frequency components at pressure taps where the mean value was at a local minimum. This indicates that the aerodynamic forces acting on the model had
nonlinearly coupled frequency components. These results show how nonlinear analysis tools can be used to provide insights into nonlinear flutter which is needed in the validation of nonlinear computational methodologies.

Acknowledgments

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References